

# ECE 598NSG/498NSU

## Deep Learning in Hardware

### Fall 2020

#### Low-complexity DNNs

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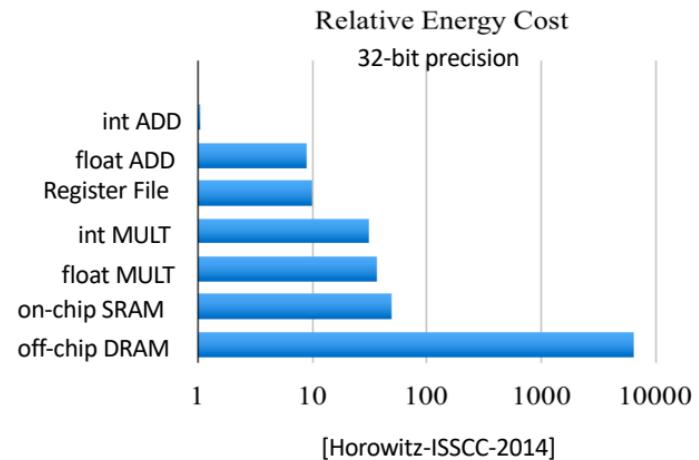
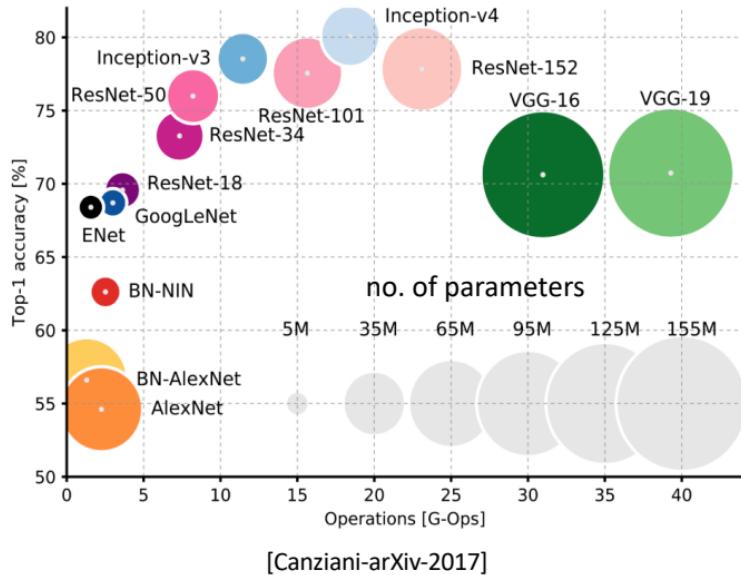
# Today

- Motivation
- Low-complexity network - MobileNet
- Low-complexity network – SqueezeNet
- Low-complexity network – ShuffleNet

# Motivation

- faster training
- easier '*over the air*' updates to Edge devices
- fewer off-chip accesses during inference – lower latency and energy costs of inference
  - e.g., FPGA on-chip memory < 10 MB

# Memory Access Energy in DNNs



- Require large no. of parameters → don't fit within on-chip SRAM
- off-chip DRAM accesses are 100x more energy expensive

# Low-Complexity DNNs

- Two approaches
- 1: design a low-complexity network from scratch
  - based on design intuitions (MobileNet, SqueezeNet)
- 2: reduce the complexity of a large network
  - model compression
  - factorization
  - distillation
  - binarization/ternarization
- need to address complexity vs. accuracy trade-off

# Three Low-Complexity Networks

- MobileNet
- SqueezeNet
- ShuffleNet

# MobileNet

## MobileNets: Efficient Convolutional Neural Networks for Mobile Vision Applications

Andrew G. Howard  
Weijun Wang

Menglong Zhu  
Tobias Weyand

Bo Chen  
Marco Andreetto

Dmitry Kalenichenko  
Hartwig Adam

Google Inc.

intrinsically a low-complexity network → embedded vision apps.



	# of Layers	# of parameters CONV	# of parameters FC	# of MACs CONV	# of MACs FC	Top-1 error %	Top-5 error %
AlexNet	5C – 3F	3.7M	58.6M	1,077M	58.6M	42.9	15.3
VGGNet	13/ <b>16</b> /19C – 3F	14.7M	123.6M	15,360M	123.6M	28.07	9.33
ResNet	18/ <b>34</b> /50/101/152C – 1F	21M	512K	3,643M	512K	21.53	5.6
DenseNet	120/ <b>160</b> /168/200C – 1F	~ 52M	1.152M	> 7B	1.152M	20.85	5.3
MobileNet	27C – 1F	3.1M	1M	532M	1M	29.4	11.022

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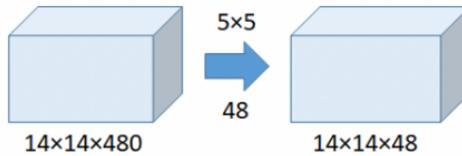
- Objective: to design small, low-latency models for embedded platforms
- 5X smaller model complexity than ResNet but higher error rates

- optimizes size and latency
- parametrized network -> can design many versions
- two parameters: width and resolution multipliers
- built from

depth-wise separable convolutions →

standard convolution = depth-wise separable x point-wise convolutions

- depth-wise separable convolutions – first proposed in (Sifre, Ph.D. thesis, 2014) – use pointwise convolutions to reduce input dimension of larger filters
- Used by Inception modules in GoogleNet

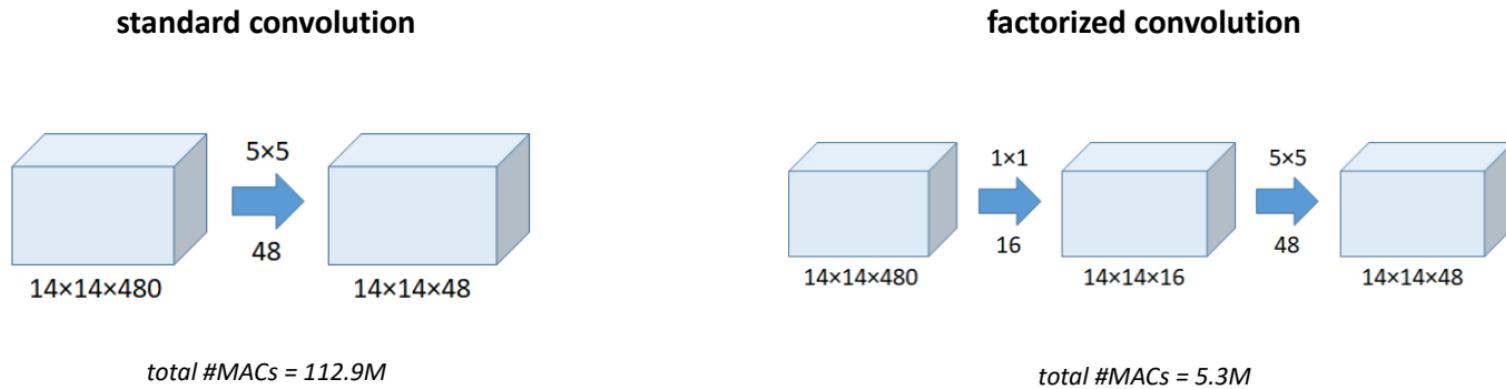


*total #MACs = 112.9M*



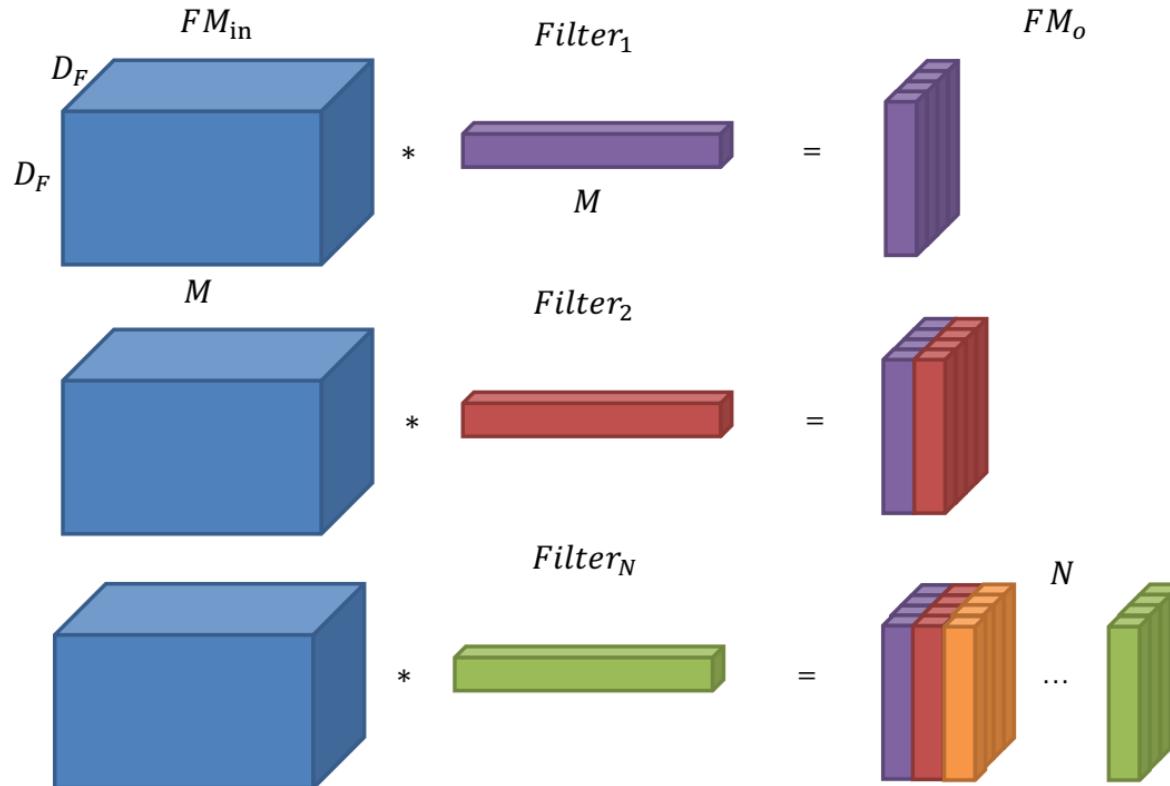
*total #MACs = 5.3M*

- depth-wise separable convolutions – first proposed in (Sifre, Ph.D. thesis, 2014) → factorize convolutions to save complexity
- better than reducing size of filters for accuracy
- Used by Inception modules in GoogleNet

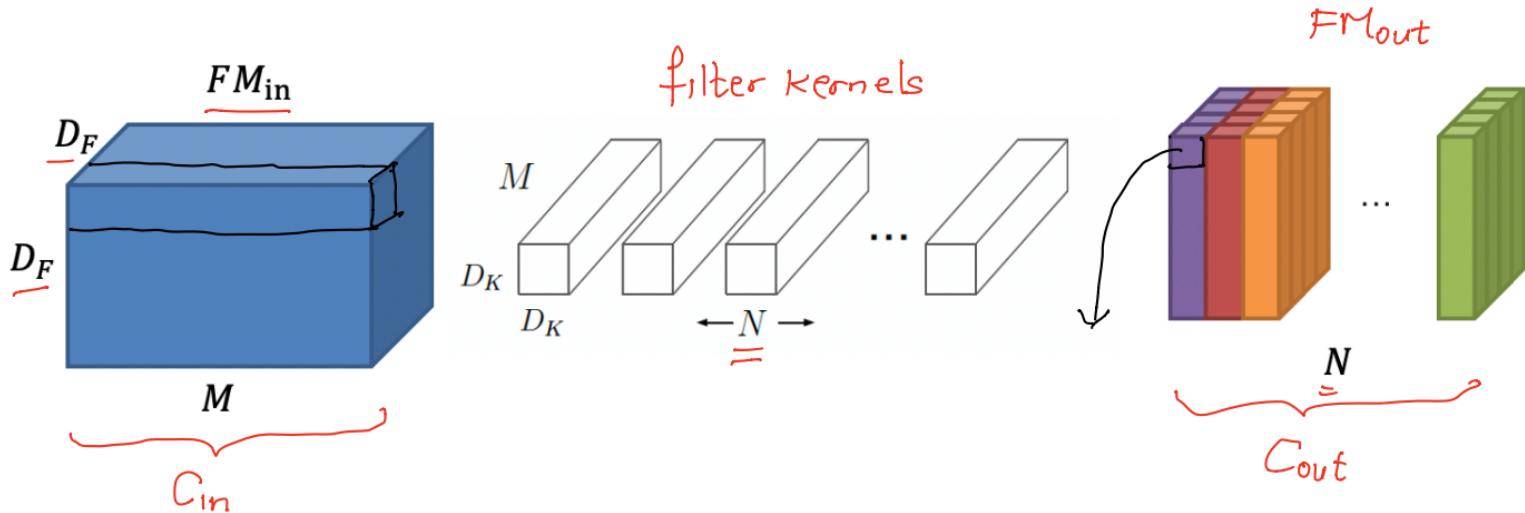


input and output FM sizes in both are the same → reduces impact on accuracy

# Standard Convolution



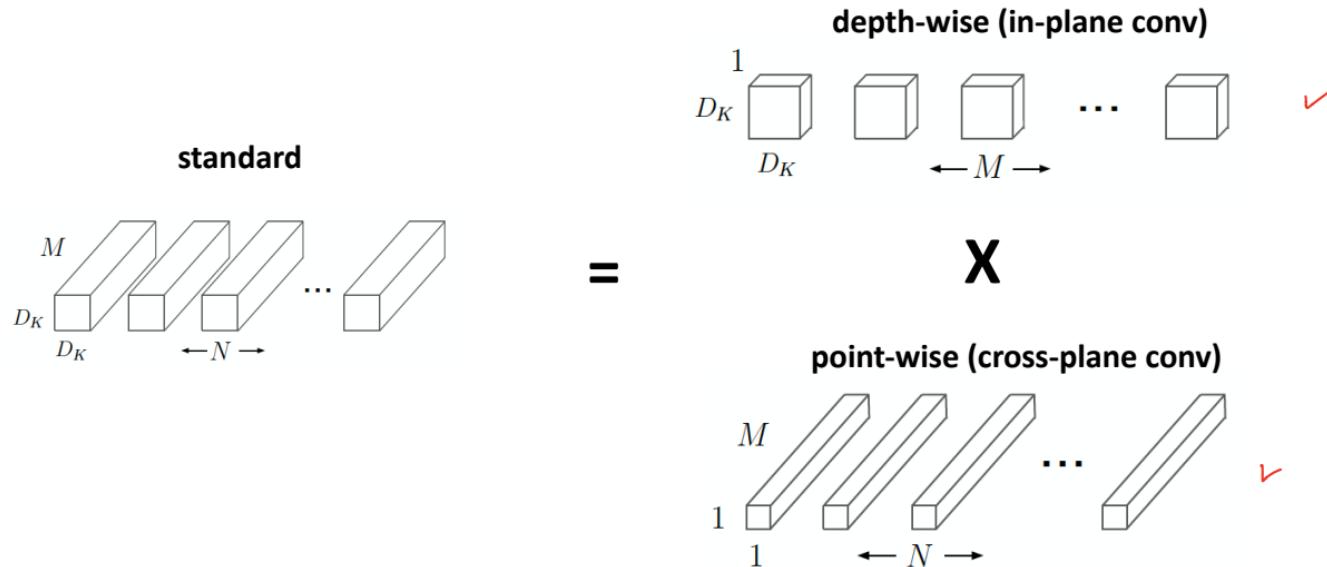
# Standard Convolution Filters

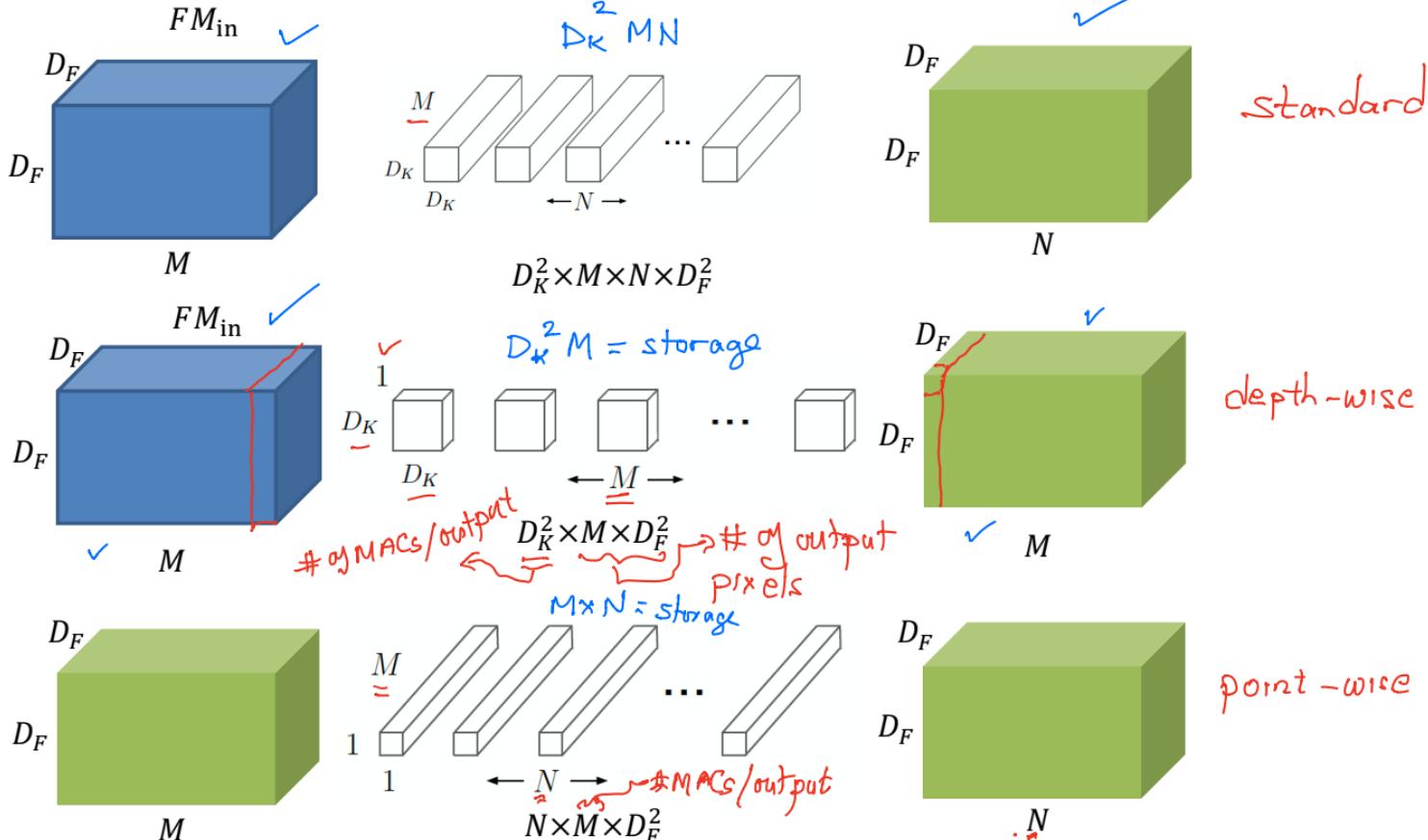


- Kernel size:  $D_K^2 \times M \times N$
- Computational cost:  $D_K^2 \times M \times N \times D_F^2$

# Depth-wise Separable Convolutions

- breaks the relationship between  $N$  and kernel size
- depth-wise separable convolution = depth-wise convolution  $\times$  point-wise convolution





# Computational Cost

- Standard:  $D_K^2 \times M \times N \times D_F^2$

$\cdot DW$                    $\cdot PW$

- Depth-wise separable:  $D_K^2 \times M \times D_F^2 + N \times M \times D_F^2$

- second term usually dominates  $\leftarrow N > M$

- Savings:

$$\begin{aligned} &\rightarrow \frac{D_K^2 \times M \times D_F^2 + N \times M \times D_F^2}{D_K^2 \times M \times N \times D_F^2} = \underbrace{\frac{1}{N} + \frac{1}{D_K^2}}_{\approx \frac{1}{D_K^2}} \approx \frac{1}{D_K^2} \\ &\rightarrow \end{aligned}$$

- MobileNet:  $D_K = 3 \rightarrow 8\times\text{-}9\times$  savings in computational & storage

$\frac{1+M}{N}$  (A)  
↑  
Storage Cost ( $w$ )

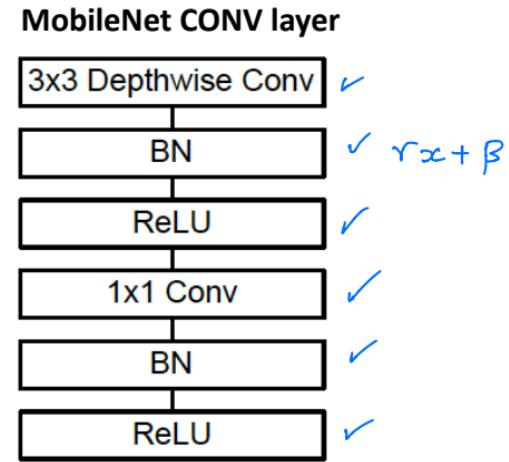
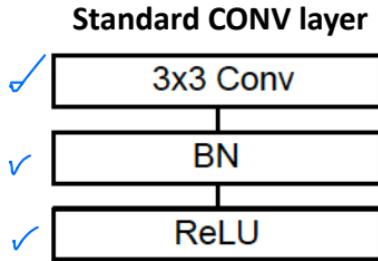
Std:  $D_K^2 MN$

DWS:  $D_K^2 M + MN$

ratio =  $\frac{D_K^2 M + MN}{D_K^2 MN}$

$= \frac{1}{N} + \frac{1}{D_K^2} \approx \frac{1}{D_K^2}$

# Network Architecture



- MobileNet Layer 1 is standard CONV → true for most lightweight networks.

# MobileNet Architecture – 28 Layers

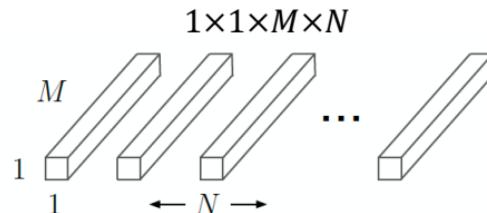
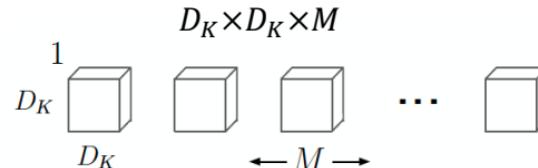
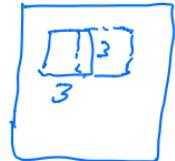
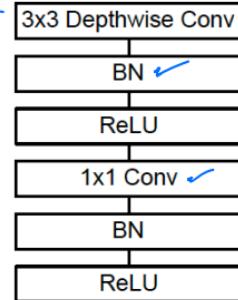
Table 1. MobileNet Body Architecture

Type / Stride	Filter Shape	Input Size
Conv / s2✓	$3 \times 3 \times 3 \times 32$	$224 \times 224 \times 3$
Conv dw / s1	$3 \times 3 \times 32$ dw	$112 \times 112 \times 32$
Conv / s1	$1 \times 1 \times 32 \times 64$	$112 \times 112 \times 32$
Conv dw / s2	$3 \times 3 \times 64$ dw	$112 \times 112 \times 64$
Conv / s1	$1 \times 1 \times 64 \times 128$	$56 \times 56 \times 64$
Conv dw / s1	$3 \times 3 \times 128$ dw	$56 \times 56 \times 128$
Conv / s1	$1 \times 1 \times 128 \times 128$	$56 \times 56 \times 128$
Conv dw / s2	$3 \times 3 \times 128$ dw	$56 \times 56 \times 128$
Conv / s1	$1 \times 1 \times 128 \times 256$	$28 \times 28 \times 128$
Conv dw / s1	$3 \times 3 \times 256$ dw	$28 \times 28 \times 256$
Conv / s1	$1 \times 1 \times 256 \times 256$	$28 \times 28 \times 256$
Conv dw / s2	$3 \times 3 \times 256$ dw	$28 \times 28 \times 256$
Conv / s1	$1 \times 1 \times 256 \times 512$	$14 \times 14 \times 256$
5× Conv dw / s1	$3 \times 3 \times 512$ dw	$14 \times 14 \times 512$
Conv / s1	$1 \times 1 \times 512 \times 512$	$14 \times 14 \times 512$
Conv dw / s2	$3 \times 3 \times 512$ dw	$14 \times 14 \times 512$
Conv / s1	$1 \times 1 \times 512 \times 1024$	$7 \times 7 \times 512$
Conv dw / s2	$3 \times 3 \times 1024$ dw	$7 \times 7 \times 1024$
Conv / s1	$1 \times 1 \times 1024 \times 1024$	$7 \times 7 \times 1024$
Avg Pool / s1	Pool $7 \times 7$	$7 \times 7 \times 1024$
FC / s1	$1024 \times 1000$	$1 \times 1 \times 1024$
Softmax / s1	Classifier	$1 \times 1 \times 1000$

remove for shallow network

standard

DWS layer =



# Computational Costs by Layer Type

Table 2. Resource Per Layer Type

Type	Mult-Adds	Parameters
Conv $1 \times 1$	94.86%	74.59%
Conv DW $3 \times 3$	3.06%	1.06%
Conv $3 \times 3$	1.19%	0.02%
Fully Connected	0.18%	24.33%

dominates ←

- most of the cost in point-wise convolutions → 95% computation and 75% of storage
- point-wise convolutions = dot-products

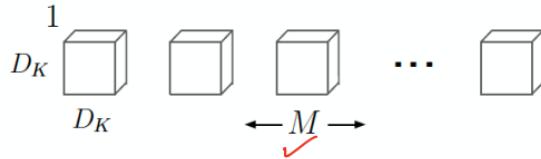
# Parameterizing MobileNet

- how to generate MobileNets with different size, accuracy, latency trade-offs?
- parameterize the network with:
  - width multiplier – scales the number of channels  $(\alpha)$
  - resolution multiplier – scales the 2D size of the FMs  $(\rho)$

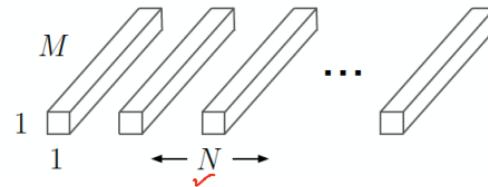
# Width Multiplier

- width multiplier ( $\alpha \in (0,1]$ ):  $\underline{N} \rightarrow \underline{\underline{\alpha N}}$ ;  $\underline{M} \rightarrow \underline{\underline{\alpha M}}$  ( $\underline{\alpha = 1}$ : baseline)

depth-wise



point-wise

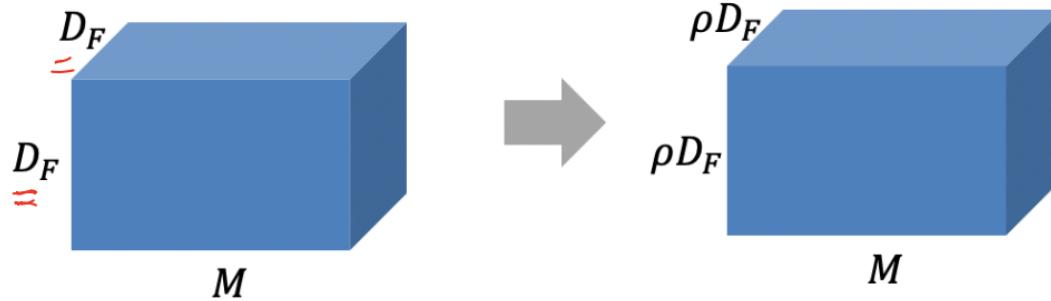


- computational cost reduced roughly by  $\underline{\underline{\alpha^2}}$ ; storage cost also reduced by  $\underline{\underline{\alpha^2}}$

$$D_K^2 \times M \times D_F^2 + N \times M \times D_F^2 \rightarrow D_K^2 \times \underline{\underline{\alpha M}} \times D_F^2 + \underline{\underline{\alpha N}} \times \underline{\underline{\alpha M}} \times D_F^2 \\ (\underline{\underline{\alpha^2}})$$

# Resolution Multiplier

- resolution multiplier ( $\rho \in (0,1]$ ):  $D_F \rightarrow \rho D_F$ ; ( $\rho = 1$ : baseline) – implicitly set via assigning input resolution



- computational cost: reduced roughly by  $\underline{\rho^2}$ ; storage cost is intact.

$$D_K^2 \times M \times D_F^2 + N \times M \times D_F^2 \rightarrow D_K^2 \times M \times \underline{\rho^2} D_F^2 + N \times M \times \underline{\rho^2} D_F^2$$

# Total Cost with Both Multipliers

Table 3. Resource usage for modifications to standard convolution.

Note that each row is a cumulative effect adding on top of the previous row. This example is for an internal MobileNet layer with  $D_K = 3, M = 512, N = 512, D_F = 14$ .

Layer/Modification	Million	Million	Parameters
	Mult-Adds		
Convolution	462	2.36	2.36
Depthwise Separable Conv	52.3	0.27	0.27
width $M \leftarrow \sqrt{\alpha} = 0.75$	$x (0.75)^2$	0.15	0.15
res: $M \cdot \rho = 0.714$	$x (0.714)^2$	0.15	0.15

← Mobile net using standard conv.

- Baseline:  $D_K^2 \times M \times D_F^2 + N \times M \times D_F^2$
- Reduced:  $D_K^2 \times \alpha M \times \rho^2 D_F^2 + \alpha N \times \alpha M \times \rho^2 D_F^2$
- overall: computational cost reduced by  $(\alpha\rho)^2$ ; storage cost by  $(\alpha)^2$

# Accuracy vs. Size

Table 4. Depthwise Separable vs Full Convolution MobileNet

Model	ImageNet Accuracy	Million Mult-Adds	Million Parameters
✓ Conv MobileNet	✓ 71.7%	↙ 4866	↙ 29.3
✓ MobileNet	✓ 70.6%	↙ 569	↙ 4.2

⇒ Table 5. Narrow vs Shallow MobileNet

Model	ImageNet Accuracy	Million Mult-Adds	Million Parameters
✓ = 0.75 MobileNet	68.4%	325 ✓	2.6 ✓
Shallow MobileNet	65.3%	307 ✓	2.9 ✓

- Shallow MobileNet – remove 5 layers with 14×14×512 FMs
- narrow network preserves depth → good for accuracy

# Accuracy vs. Size

Table 6. MobileNet Width Multiplier

<u>Width Multiplier</u>	ImageNet Accuracy	Million Mult-Adds	Million Parameters
1.0 MobileNet-224	70.6%	569	4.2
✓ 0.75 MobileNet-224	68.4%	325	2.6
✓ 0.5 MobileNet-224	63.7%	149	1.3
✓ 0.25 MobileNet-224	50.6%	41	0.5

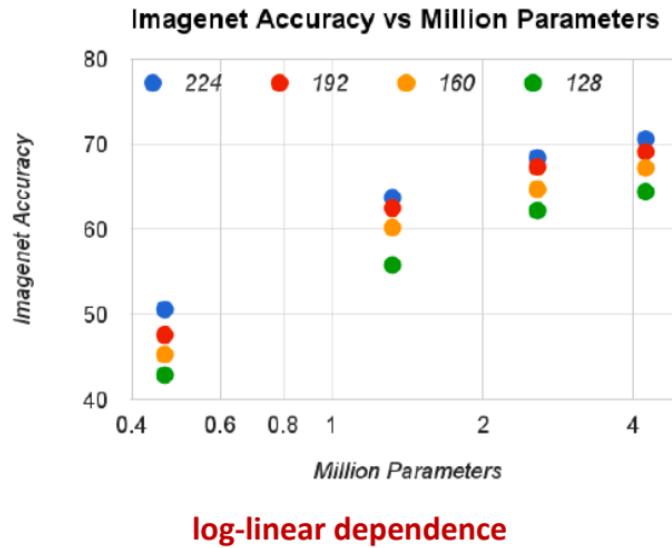
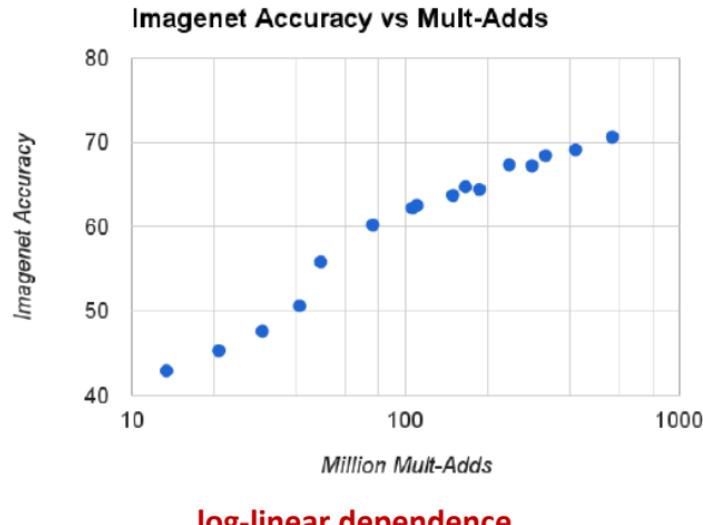
sharp drop

Table 7. MobileNet Resolution

<u>Resolution</u>	ImageNet Accuracy	Million Mult-Adds	Million Parameters
1.0 MobileNet-224	70.6%	569	4.2
1.0 MobileNet-192	69.1%	418	4.2
1.0 MobileNet-160	67.2%	290	4.2
1.0 MobileNet-128	64.4%	186	4.2

smooth roll-off

# Accuracy vs. Storage/Complexity Trade-off



- Networks generated as a cross-product:

$$\alpha \in \{1, 0.75, 0.5, 0.25\} \times \rho \in \{224, 192, 160, 128\}$$

# SqueezeNet

SQUEEZENET: ALEXNET-LEVEL ACCURACY WITH  
50X FEWER PARAMETERS AND <0.5MB MODEL SIZE

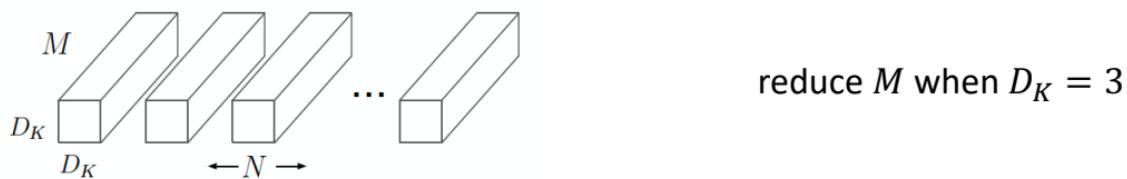
**Forrest N. Iandola<sup>1</sup>, Song Han<sup>2</sup>, Matthew W. Moskewicz<sup>1</sup>, Khalid Ashraf<sup>1</sup>,  
William J. Dally<sup>2</sup>, Kurt Keutzer<sup>1</sup>**

<sup>1</sup>DeepScale\* & UC Berkeley    <sup>2</sup>Stanford University

- another low-complexity network
- based on a set of design intuitions to reduce network size

# Design Strategies

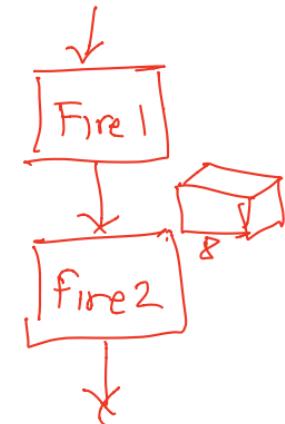
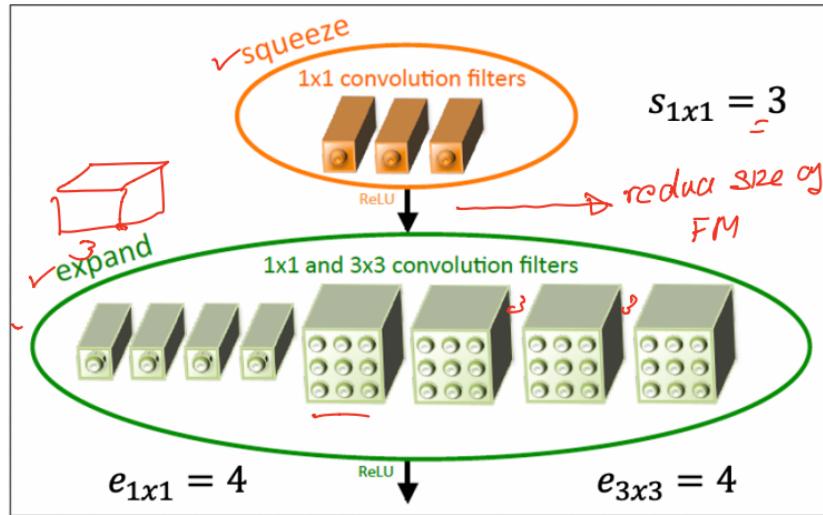
- **S1:** replace  $3 \times 3$  filters with  $1 \times 1$  filters  $\rightarrow 9 \times$  fewer parameters
- **S2:** decrease the number of input channels to  $3 \times 3$  filters  $\rightarrow$  reduces the number of parameters (width multiplier)



reduce  $M$  when  $D_K = 3$

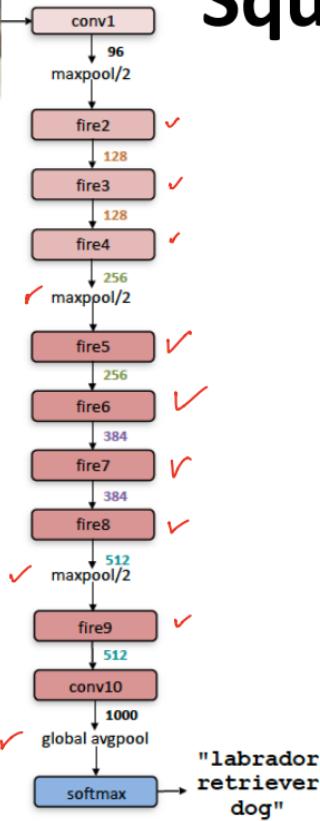
- **S3:** downsample late in network  $\rightarrow$  conv layers have large activation maps  $\rightarrow$  better accuracy

# Fire Module



# of kernels in  
squeeze

- concatenation of squeeze (**S1**) and expand layers
- parameterized by 3 variables:  $s_{1 \times 1}, e_{1 \times 1}, e_{3 \times 3}$
- Set:  $s_{1 \times 1} < e_{1 \times 1} + e_{3 \times 3}$  per **S2** → # kernels in expand layer



# SqueezeNet Architecture

- Conv1: standard; no FC layer
- 8 Fire modules (fire2-9)
- max pooling after conv1, fire4, fire8, conv10 (per **S3**)

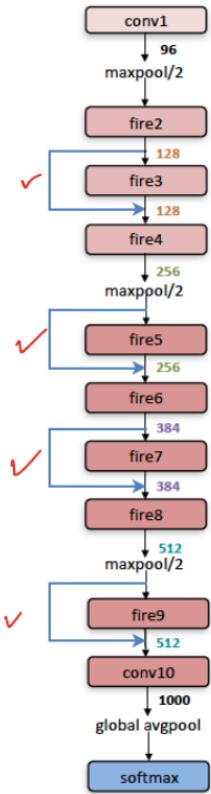
Table 1: SqueezeNet architectural dimensions. (The formatting of this table was inspired by the Inception2 paper (Ioffe & Szegedy, 2015).)

layer name/type	output size	filter size / stride (if not a fire layer)	depth	$s_{1x1}$ (#1x1 squeeze)	$e_{1x1}$ (#1x1 expand)	$e_{3x3}$ (#3x3 expand)	$s_{1x1}$ sparsity	$e_{1x1}$ sparsity	$e_{3x3}$ sparsity	# bits	#parameter before pruning	#parameter after pruning	
input image	224x224x3										-	-	
conv1	111x111x96	7x7/2 (x96)	1							6bit	14,208	14,208	
maxpool1	55x55x96	3x3/2	0										
fire2	55x55x128		2	16	64	64	100%	100%	33%	6bit	11,920	5,746	
fire3	55x55x128		2	16	64	64	100%	100%	33%	6bit	12,432	6,258	
fire4	55x55x256		2	32	128	128	100%	100%	33%	6bit	45,344	20,646	
maxpool4	27x27x256	3x3/2	0										
fire5	27x27x256		2	32	128	128	100%	100%	33%	6bit	49,440	24,742	
fire6	27x27x384		2	48	192	192	100%	50%	33%	6bit	104,880	44,700	
fire7	27x27x384		2	48	192	192	50%	100%	33%	6bit	111,024	46,236	
fire8	27x27x512		2	64	256	256	100%	50%	33%	6bit	188,992	77,581	
maxpool8	13x13x512	3x3/2	0										
fire9	13x13x512		2	64	256	256	50%	100%	30%	6bit	197,184	77,581	
conv10	13x13x1000	1x1/1 (x1000)	1							6bit	513,000	103,400	
avgpool10	1x1x1000	13x13/1	0										
				activations				parameters				compression info	
												1,248,424 (total)	421,098 (total)

# Design Intuitions

- add 1 pixel zero-padding to input of  $3 \times 3$  expand filters  $\rightarrow 3 \times 3$  and  $1 \times 1$  filters  
output activations have identical dimensions
- ✓ • ReLU is applied to activations from squeeze and expand layers (Nair & Hinton, 2010)
- dropout (Srivastava et. al., 2014) with ratio 50% after fire9
- no FC layer (inspired by NiN Lin et al., 2013)
- linearly decrease learning rate from 0.04 down (Mishkin et al., 2016)
- expand layer implemented in Caffe as concatenation of  $1 \times 1$  filters and  $3 \times 3$  filters

with simple bypass



- similar to ResNet
- simple bypass applies to fire modules with same # of input and output dimensions
- complex bypass applied to fire modules with differing input/output dimensions (adds extra parameters)
- Squeeze layers limit information; bypass layers compensate for it

with complex bypass

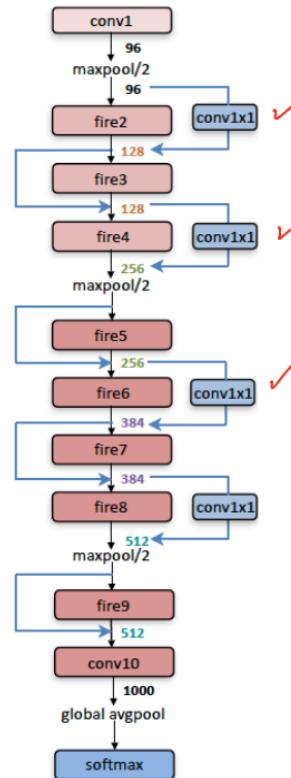


Table 3: SqueezeNet accuracy and model size using different macroarchitecture configurations

	Architecture	Top-1 Accuracy	Top-5 Accuracy	Model Size
✓	Vanilla SqueezeNet	57.5%	80.3%	4.8MB ✓
✓	SqueezeNet + Simple Bypass	<b>60.4%</b> ✓	<b>82.5%</b>	4.8MB ✓
✓	SqueezeNet + Complex Bypass	58.8% ✓	82.0%	7.7MB

- also applied model compression -> low-complexity model is further compressible

# ShuffleNet

## ShuffleNet: An Extremely Efficient Convolutional Neural Network for Mobile Devices

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Xinyu Zhou\*

Mengxiao Lin

Jian Sun

Megvii Inc (Face++)

{zhangxiangyu, zxy, linmengxiao, sunjian}@megvii.com

- Another low complexity network for mobile devices
- Channel shuffle and ShuffleNet Unit

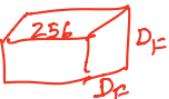
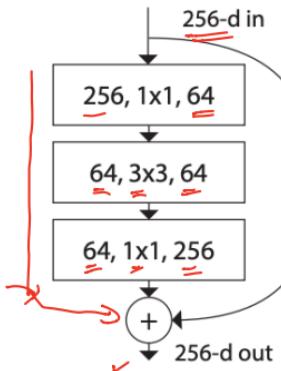
# Design Strategy

- Repurpose two principles:
  - Use of repeated blocks of same shape (VGG and ResNet)
  - Use of split-transform-merge strategy (Inception models – GoogleLeNet, DWS)  
SqueezeNet)
- Channel Shuffle: related input and output channels by cross talking
- Replace standard convolution with 1x1 Point-wise Group convolution and 3x3 Depth-wise Separable convolution

# Group Convolution

Xie et al., '17, ResNext

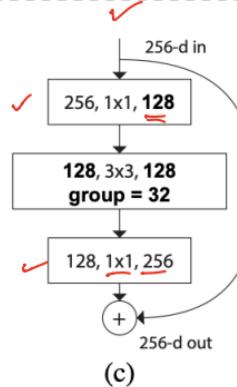
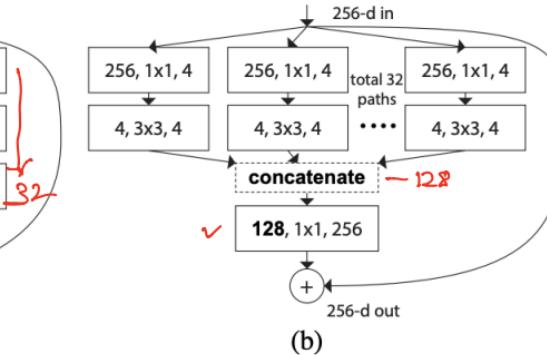
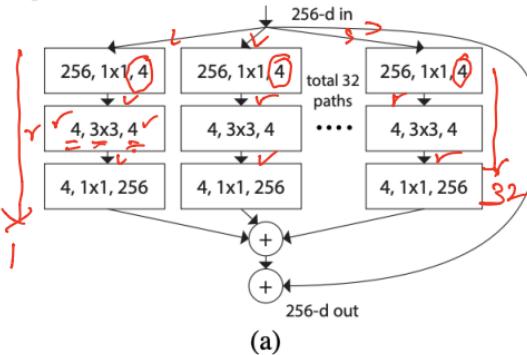
## Standard ResNet block



- used by AlexNet to distribute computations across GPUs; used by ResNext to enhance accuracy without increasing computational cost (use of cardinality)
- GC: split input FM into  $C$  (cardinality) groups; each group responsible for certain depth; concatenate (sum) each group at the end

## ResNext block with $C = 32$

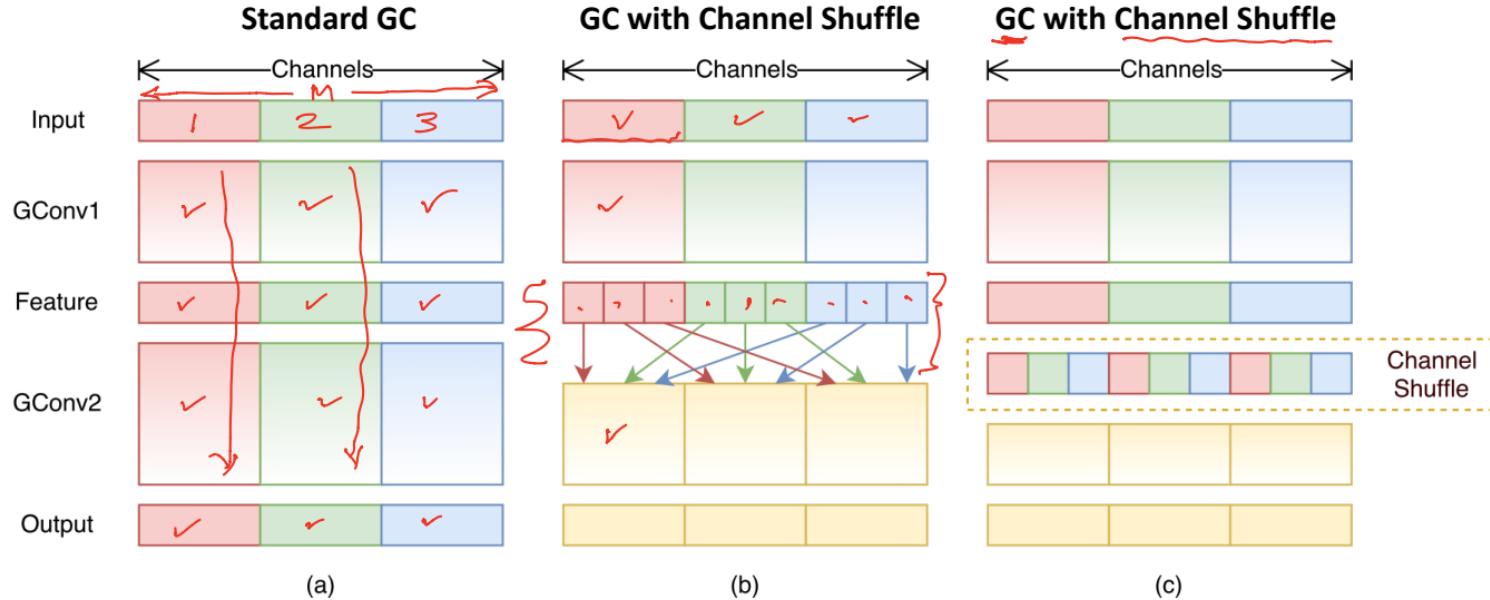
*equivalent*



*block equivalent*

GC

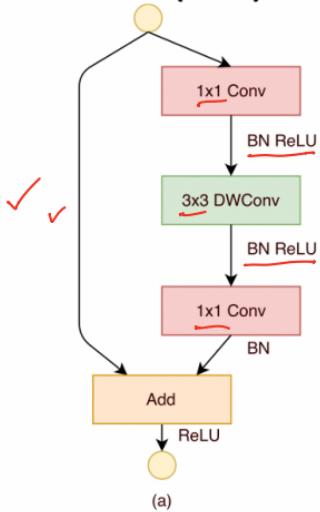
# Channel Shuffle



- allow information flow between channel groups and strengthen representation
- differentiable operation, meaning end-to-end training is available

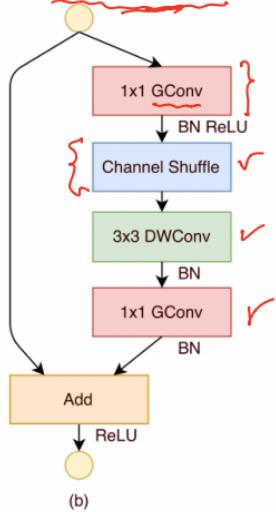
# ShuffleNet Units

bottleneck (DWS) unit



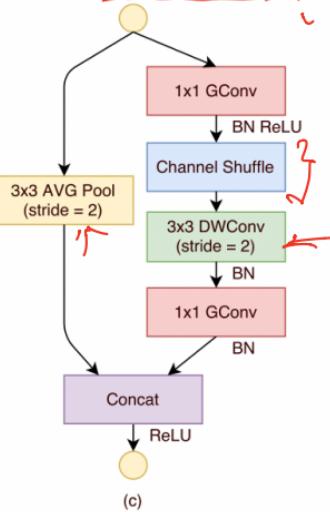
(a)

DWS GC unit



(b)

DWS GC unit (stride=2)



(c)

- Consist of 1x1 group convolution followed by channel shuffle, 3x3 depthwise separable Convolution, and 1x1 group convolution
- Batch Normalization and ReLU after each convolution except the last 1x1 GConv
- Element-wise addition or concatenation to inputs at the final step

# ShuffleNet Architecture

Layer	Output size	KSize	Stride	Repeat	Output channels ( $g$ groups)				
					$g = 1$	$g = 2$	$g = 3$	$g = 4$	$g = 8$
Image	$224 \times 224$				3	3	3	3	3
✓ Conv1	$112 \times 112$	$3 \times 3$	2	1	24	24	24	24	24
✓ MaxPool	$56 \times 56$	$3 \times 3$	2						
✓ Stage2	$28 \times 28$		2 ✓	1	144	200	240	272	384
	$28 \times 28$		1 ✓	3	144	200	240	272	384
✓ Stage3	$14 \times 14$		2 ✓	1	288	400	480	544	768
	$14 \times 14$		1 ✓	7	288	400	480	544	768
✓ Stage4	$7 \times 7$		2 ✓	1	576	800	960	1088	1536
	$7 \times 7$		1 ✓	3	576	800	960	1088	1536
GlobalPool	$1 \times 1$	$7 \times 7$							
✓ FC					1000	1000	1000	1000	1000
Complexity					143M	140M	137M	133M	137M

- Conv1: standard
- 3 stages of ShuffleNet unit groups
  - Each contains ShuffleNet units with stride = 1 and stride = 2
  - The number of units in each stage is specified by the number of repeats

# Accuracy vs. Use of Channel Shuffle

Model	Cls err. (%), no shuffle	Cls err. (%), shuffle	Δ err. (%)
ShuffleNet 1x ( $g = 3$ )	34.5	<b>32.6</b>	1.9
ShuffleNet 1x ( $g = 8$ )	37.6	<b>32.4</b>	5.2
ShuffleNet 0.5x ( $g = 3$ )	45.7	<b>43.2</b>	2.5
ShuffleNet 0.5x ( $g = 8$ )	48.1	<b>42.3</b>	5.8
ShuffleNet 0.25x ( $g = 3$ )	56.3	<b>55.0</b>	1.3
ShuffleNet 0.25x ( $g = 8$ )	56.5	<b>52.7</b>	3.8

- Small number represents better accuracy
- Channel Shuffle provide 6% decrease in classification error

# Accuracy vs. Architecture

Complexity (MFLOPs)	VGG-like	ResNet	Xception-like	ResNeXt	ShuffleNet (ours)
140	50.7	37.3	33.6	33.3	<b>32.4</b> ( $1\times, g = 8$ )
38	-	48.8	45.1	46.0	<b>41.6</b> ( $0.5\times, g = 4$ )
13	-	63.7	57.1	65.2	<b>52.7</b> ( $0.25\times, g = 8$ )

Model	Complexity (MFLOPs)	Cls err. (%)	$\Delta$ err. (%)
1.0 MobileNet-224	569	29.4	-
ShuffleNet $2\times$ ( $g = 3$ )	524 ✓	<b>26.3</b> ✓	3.1
ShuffleNet $2\times$ (with SE[13], $g = 3$ )	527 ✓	<b>24.7</b> ✓	4.7
✓ 0.75 MobileNet-224	325 ✓	31.6 ✓	-
ShuffleNet $1.5\times$ ( $g = 3$ ) ✓	292 ✓	<b>28.5</b> ✓	3.1
0.5 MobileNet-224	149	36.3	-
ShuffleNet $1\times$ ( $g = 8$ )	140	<b>32.4</b>	3.9
0.25 MobileNet-224	41	49.4	-
ShuffleNet $0.5\times$ ( $g = 4$ )	38	<b>41.6</b>	7.8
ShuffleNet $0.5\times$ (shallow, $g = 3$ )	40	42.8	6.6

- achieves best performance across all network architectures

# Summary

- Trade-off between complexity and accuracy
- Based on design intuitions to preserve accuracy
- separable convolutions
- use of point-wise convolutions
- delaying max-pooling
- others

Lessons : accuracy vs. complexity

- ① DWs
- ② 1 layer - standard conv
- ③ push averaging (max pool/ar. pool) towards the output
- ④ preserve depth

↓  
regular / parameterized networks

## Course Web Page

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