

Which of the following are (recursive) definitions of the set of integers  $\mathbb{Z}$ ? (Select True/False for each one.)

1.

Basis Step:  $5 \in \mathbb{Z}$

Recursive Step: If  $x \in \mathbb{Z}$ , then  $x + 1 \in \mathbb{Z}$  and  $x - 1 \in \mathbb{Z}$

2.

Basis Step:  $0 \in \mathbb{Z}$

Recursive Step: If  $x \in \mathbb{Z}$ , then  $x + 1 \in \mathbb{Z}$  and  $x - 1 \in \mathbb{Z}$  and  $x + 2 \in \mathbb{Z}$  and  $x - 2 \in \mathbb{Z}$

3.

Basis Step:  $0 \in \mathbb{Z}$

Recursive Step: If  $x \in \mathbb{Z}$ , then  $x + 2 \in \mathbb{Z}$  and  $x - 1 \in \mathbb{Z}$

4.

Basis Step:  $0 \in \mathbb{Z}$

Recursive Step: If  $x \in \mathbb{Z}$ , then  $x + 1 \in \mathbb{Z}$  and  $x + 2 \in \mathbb{Z}$