## Defining sets

To define sets:

To define a set using **roster method**, explicitly list its elements. That is, start with { then list elements of the set separated by commas and close with }.

To define a set using **set builder definition**, either form "The set of all x from the universe U such that x is ..." by writing

$$\{x \in U \mid ...x...\}$$

or form "the collection of all outputs of some operation when the input ranges over the universe U" by writing

$$\{...x... \mid x \in U\}$$

We use the symbol  $\in$  as "is an element of" to indicate membership in a set.

**Example sets**: For each of the following, identify whether it's defined using the roster method or set builder notation and give an example element.

{AUG, UAG, UGA, UAA}

## Rna motivation

RNA is made up of strands of four different bases that encode genomic information in specific ways. The bases are elements of the set  $B = \{A, C, U, G\}$ .

Formally, to define the set of all RNA strands, we need more than roster method or set builder descriptions.

## Set recursive definition

New! Recursive Definitions of Sets: The set S (pick a name) is defined by:

Basis Step: Specify finitely many elements of S

Recursive Step: Give rule(s) for creating a new element of S from known values existing in S,

and potentially other values.

The set S then consists of all and only elements that are put in S by finitely many (a nonnegative integer number) of applications of the recursive step after the basis step.

## Set recursive examples

<b>Definition</b> The set of nonnegative integers $\mathbb{N}$ is defined (recursively) by:	
Basis Step: Recursive Ste	ep:
Examples:	
<b>Definition</b> The set of all integers $\mathbb{Z}$ is defined (recursively) by:	
Basis Step: Recursive Step:	
Examples:	
<b>Definition</b> The set of RNA strands $S$ is defined (recursively) by:	
Basis Step: Recursive Step:	$\mathbf{A} \in S, \mathbf{C} \in S, \mathbf{U} \in S, \mathbf{G} \in S$ If $s \in S$ and $b \in B$ , then $sb \in S$
where $sb$ is string concatenation.	
Examples:	
<b>Definition</b> The set of bitstrings (strings of 0s and 1s) is defined (recursively) by:	
Basis Step: Recursive Step:	
<i>Notation:</i> We call the set of bitstrings $\{0,1\}^*$ .	
Examples:	