Defining sets

To define sets:

To define a set using **roster method**, explicitly list its elements. That is, start with { then list elements of the set separated by commas and close with }.

To define a set using **set builder definition**, either form "The set of all x from the universe U such that x is ..." by writing

$$\{x \in U \mid ...x...\}$$

or form "the collection of all outputs of some operation when the input ranges over the universe U" by writing

$$\{...x... \mid x \in U\}$$

We use the symbol \in as "is an element of" to indicate membership in a set.

Example sets: For each of the following, identify whether it's defined using the roster method or set builder notation and give an example element.

Rna motivation

RNA is made up of strands of four different bases that encode genomic information in specific ways. The bases are elements of the set $B = \{A, C, U, G\}$.

Formally, to define the set of all RNA strands, we need more than roster method or set builder descriptions.

Set recursive definition

New! Recursive Definitions of Sets: The set S (pick a name) is defined by:

Basis Step: Specify finitely many elements of S

Recursive Step: Give rule(s) for creating a new element of S from known values existing in S,

and potentially other values.

The set S then consists of all and only elements that are put in S by finitely many (a nonnegative integer number) of applications of the recursive step after the basis step.

Set recursive examples

Definition The set of nonnegative integers \mathbb{N} is defined (recursively) by:
Basis Step: Recursive Step:
Examples:
Definition The set of all integers \mathbb{Z} is defined (recursively) by:
Basis Step: Recursive Step:
Examples:
Definition The set of RNA strands S is defined (recursively) by:
Basis Step: $A \in S, C \in S, U \in S, G \in S$ Recursive Step: If $s \in S$ and $b \in B$, then $sb \in S$
where sb is string concatenation.
Examples:
Definition The set of bitstrings (strings of 0s and 1s) is defined (recursively) by:
Basis Step: Recursive Step:
<i>Notation:</i> We call the set of bitstrings $\{0,1\}^*$.
Examples: