Assignment 1: Extracting Parallelism

Due Sep 8, before the class

The purpose of this assignment is for you

- to develop insight about how to extract parallelism from simple codes.
- to recognize cases where some form of parallelism may not be correct
- to acknowledge that sometimes adding work is necessary

Note: Often when talking about algorithms, the weights of tasks are denoted with their complexity. Note: 1 and 2 are exercise/warm up. 3, 4 and 5 are harder. All problems are independent.

1 Transform

Consider the transform function:

```
void transform (int* a, int* b, int n) {
  for (int i=0; i<n; ++i)
    b[i] = f(a[i]);
}</pre>
```

Question: Extract the dependencies. Assume the call to f cost O(1).

Question: What is the width? the critical path? the work?

Question: How does a schedule look like on P processors.

2 Reduce

Consider the reduce function:

```
template < typename T, typename op>
T reduce (T* array, size_t n) {
  T result = array[0];
  for (int i=1; i < n; ++i)
    result = op (result, array[i]);
  return result;
}</pre>
```

So if you define T as int and op as sum, it boils down to computing the sum of the array. You could use op as max and compute the maximum value of the array.

2.1 int, sum

Consider first the int, sum case which computes the sum of an array of integers.

Question: Extract the dependencies of this problem. What is the width? the critical path? the work? Question: Noticing that the different loop iterations could execute in any order. Introduce a mutual exclusion clause on the dependency graph. Does that help?

Question: Assuming you have P processors, rewrite the code to introduce one local variable per processor to store partial computation. Extract the dependencies now. What is the width, critical path and work? **Question:** What does a schedule look like on P processors?

2.2 Variants

Question: Would these two parallel versions (with mutual exclusion and with local variable) be correct for int, max? Why?

Question: Would these two parallel versions (with mutual exclusion and with local variable) be correct for string, concat? Why?

Question: Would these two parallel versions (with mutual exclusion and with local variable) be correct for float, sum? Why?

Question: Would these two parallel versions (with mutual exclusion and with local variable) be correct for float, max? Why?

3 Find first

3.1 in an array

Question: Write a sequential algorithm that search a value val in an array arr of size n and return the position pos of the first location where arr[pos] == val. (and returns n otherwise.)

Question: What is the complexity of this algorithm? (as a function of pos and n).

Question: Can you make a parallel algorithm with $\theta(n)$ work? What is its critical path and width? **Question:** Can you make a parallel algorithm with $\theta(pos)$ work? What is its critical path and width?

3.2 in a linked list

Question: What do you think about doing the same thing with a linked list?

4 Prefix sum

Prefixsum is the algorithm that computes $pr[i] = \sum_{j \leq i} arr[i]$ and often written sequentially:

```
void prefixsum (int* arr, int n, int* pr) {
  pr[0] = arr[0];
  for (int i=1; i<n; ++i)
    pr[i] = pr[i-1] + arr[i];
}</pre>
```

Question: What is the structure of the dependency of prefixsum?

Question: How can you make it parallel? (Hint: you have to add work, a single pass on the array is not enough)

5 Merge Sort

Question: Recall the merge sort algorithm.

Question: Extract dependency on the merge sort algorithm. What is the critical path, work, and width? (Hint: instead of using loop iterations as a task, you can use function calls and function return as tasks. Think that merge sort is recursive.)

Question: How does the schedule of such an algorithm look like when P=4?

Question: Can you extract more parallelism? (Hint: increase the amount of work slightly)