

IF STATE SPACE OF X IS DISCRETE, THEN X IS A DISCRETE RANDOM VARIABLE.

$$p_X(x) = \mathbb{P}(X=x) \quad \text{PROBABILITY MASS FUNCTION}$$

MOMENTS OF X

$$E[X^n] = \sum_{i \in S} i^n p_X(i)$$

↑
SAMPLE SPACE

ZEROth MOMENT

$$E[X^0] = \sum p_X(i) = 1$$

FIRST MOMENT

$$E[X] = \sum i p_X(i)$$

MEAN

μ_X

SECOND MOMENT

$$E[X^2] = \sum i^2 p_X(i)$$

$$E[(X - \mu_X)^2] = \text{VARIANCE}$$

σ_X^2

$$\sqrt{E[(X - \mu_X)^2]} = \text{STANDARD DEVIATION}$$

↑
 σ_X

FAMOUS DISCRETE RANDOM VARIABLES

• BERNOLLI

$$X=0 \quad \mathbb{P}(X=0) = 1-p$$

$$X=1 \quad \mathbb{P}(X=1) = p$$

$$E[X] = p$$

$$0 \leq p \leq 1$$

A STOCHASTIC PROCESS OF INDEPENDENT, IDENTICAL
BERNOULLI VARIABLES

$$X_t = [00011011001 \dots]$$

↑
FIRST HIT

n - HOW MANY HITS?

• GEOMETRIC Z

$$P_Z(k) = (1-p)^{k-1} \cdot p \quad k = 0, 1, 2, \dots$$

OF LOSSES BEFORE FIRST HIT IN X_t

$$E[Z] = \frac{1}{p}$$

• BINOMIAL Y

$$P_Y(k) = \binom{n}{k} \cdot p^k (1-p)^{n-k}$$

$$\binom{n}{k} = \frac{n!}{k! (n-k)!}$$

OF HITS IN n BERNOLLI TRIALS