

DISCRETE DISTRIBUTIONS

In [5]:

```
# for inline plots in jupyter
%matplotlib inline
# import matplotlib
import matplotlib.pyplot as plt
# for latex equations
from IPython.display import Math, Latex
# for displaying images
from IPython.core.display import Image
import numpy as np
```

In [6]:

```
# import seaborn
import seaborn as sns
# settings for seaborn plotting style
sns.set(color_codes=True)
# settings for seaborn plot sizes
sns.set(rc={'figure.figsize':(5,5)})
```

UNIFORM DISTRIBUTION

In [9]:

```
from scipy.stats import randint
import matplotlib.pyplot as plt
fig, ax = plt.subplots(1, 1)

# Calculate a few first moments:

low, high = 7, 31
mean, var, skew, kurt = randint.stats(low, high, moments='mvsk')

# Display the probability mass function (`pmf`):

x = np.arange(randint.ppf(0.01, low, high),
               randint.ppf(0.99, low, high))
ax.plot(x, randint.pmf(x, low, high), 'bo', ms=8, label='randint pmf')
ax.vlines(x, 0, randint.pmf(x, low, high), colors='b', lw=5, alpha=0.5)

# Alternatively, the distribution object can be called (as a function)
# to fix the shape and location. This returns a "frozen" RV object holding
# the given parameters fixed.

# Freeze the distribution and display the frozen `pmf`:

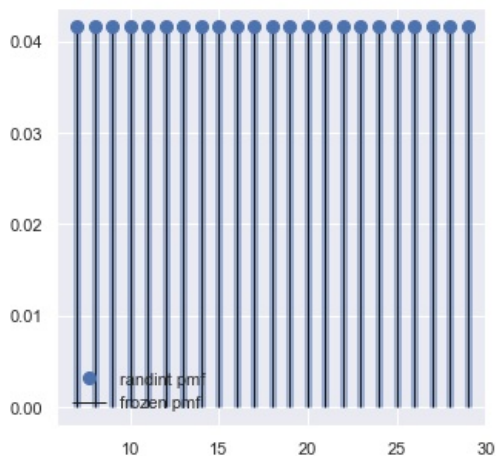
rv = randint(low, high)
ax.vlines(x, 0, rv.pmf(x), colors='k', linestyle='-', lw=1, label='frozen pmf')
ax.legend(loc='best', frameon=False)
plt.show()

# Check accuracy of `cdf` and `ppf`:

prob = randint.cdf(x, low, high)
np.allclose(x, randint.ppf(prob, low, high))
# True

# Generate random numbers:

r = randint.rvs(low, high, size=1000)
```



You can use Seaborn's `distplot` to plot the histogram of the distribution you just created. Seaborn's `distplot` takes in multiple arguments to customize the plot. You first create a plot object `ax`. Here, you can specify the number of bins in the histogram, specify the color of the histogram and specify density plot option with `kde` and linewidth option with `hist_kws`. You can also set labels for x and y axis using the `xlabel` and `ylabel` arguments.

Bernoulli Distribution

$$P(x) = \begin{cases} 1-p, & x = 0 \\ p, & x = 1 \end{cases}$$

In []:

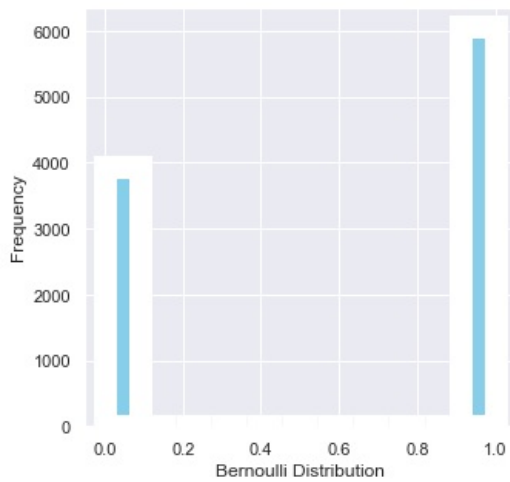
```
from scipy.stats import bernoulli
data_bern = bernoulli.rvs(size=10000, p=0.6)
```

In [17]:

```
ax= sns.distplot(data_bern,
                  kde=False,
                  color="skyblue",
                  hist_kws={"linewidth": 15,'alpha':1})
ax.set(xlabel='Bernoulli Distribution', ylabel='Frequency')
```

Out[17]:

```
[Text(0, 0.5, 'Frequency'), Text(0.5, 0, 'Bernoulli Distribution')]
```



BINOMINAL DISTRIBUTION

$$P(x) = \frac{n!}{(n-x)!x!} p^x q^{n-x}$$

In [14]:

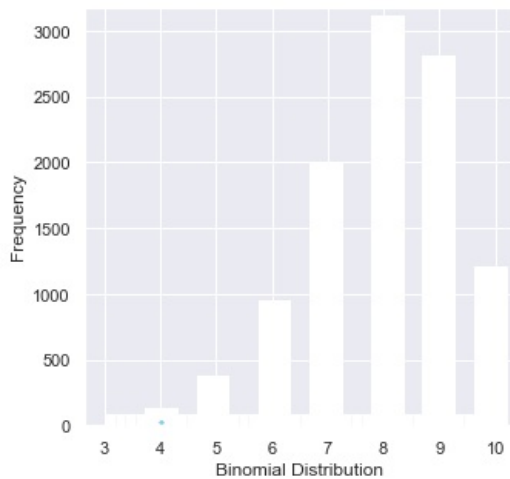
```
from scipy.stats import binom
data_binom = binom.rvs(n=10,p=0.8,size=10000)
```

In [15]:

```
ax = sns.distplot(data_binom,
                  kde=False,
                  color='skyblue',
                  hist_kws={"linewidth": 15,'alpha':1})
ax.set(xlabel='Binomial Distribution', ylabel='Frequency')
```

Out[15]:

```
[Text(0, 0.5, 'Frequency'), Text(0.5, 0, 'Binomial Distribution')]
```



Poisson Distribution

Poisson random variable is typically used to model the number of times an event happened in a time interval

$$P(X = x) = e^{-\mu} \frac{\mu^x}{x!} \quad \text{for } x = 0, 1, 2, \dots$$

In [12]:

```
from scipy.stats import poisson
data_poisson = poisson.rvs(mu=3, size=10000)
```

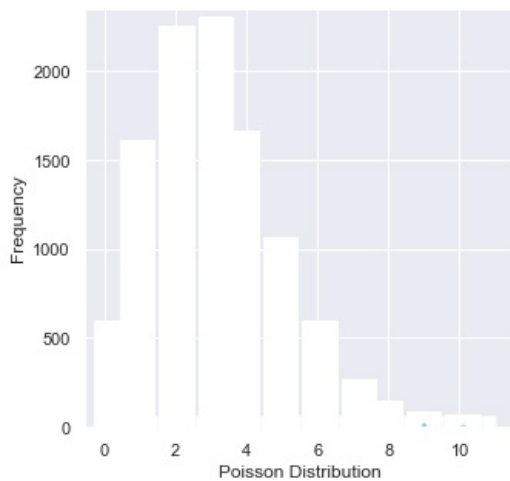
You can generate a poisson distributed discrete random variable using scipy.stats module's poisson.rvs() method which takes μ as a shape parameter and is nothing but the λ in the equation. To shift distribution use the loc parameter. size decides the number of random variates in the distribution. If you want to maintain reproducibility, include a random_state argument assigned to a number.

In [13]:

```
ax = sns.distplot(data_poisson,
                  bins=30,
                  kde=False,
                  color='skyblue',
                  hist_kws={"linewidth": 15, 'alpha':1})
ax.set(xlabel='Poisson Distribution', ylabel='Frequency')
```

Out[13]:

```
[Text(0, 0.5, 'Frequency'), Text(0.5, 0, 'Poisson Distribution')]
```



In []: