

**MATH 3012-QHS: Applied Combinatorics**  
**Fall 2020**  
**Worksheet 2**

**Name:** \_\_\_\_\_

**Due Date: Every Tuesday 11.59 pm**

**Problem 1.** Let  $\mathbb{N}$  denote the set of positive integers. When  $f : \mathbb{N} \rightarrow \mathbb{N}$  is a function, let  $E(f)$  be the function defined by  $E(f)(n) = 2^{f(n)}$ . What is  $E^5(n^2)$ ?

**Problem 2.** If you have to put  $n + 1$  pigeons into  $n$  holes, you have to put two pigeons into the same hole. What happens if you have to put  $mn + 1$  pigeons into  $m$  holes.

**Problem 3.** Draw a graph with 6 vertices having degrees 5, 4, 4, 2, 1, and 1 or explain why such a graph does not exist.