Lecture 8

May 24, 2023

1 Statistics

1.1 Importing necessary libraries

```
[1]: import numpy as np
import pandas as pd
import matplotlib.pyplot as plt
import seaborn as sns
```

1.2 Load dataset

```
[2]: data = sns.load_dataset('tips')
```

[3]: data.info()

<class 'pandas.core.frame.DataFrame'>
RangeIndex: 244 entries, 0 to 243
Data columns (total 7 columns):

#	Column	Non-	-Null Count	Dtype
0	total_bill	244	non-null	float64
1	tip	244	non-null	float64
2	sex	244	non-null	category
3	smoker	244	non-null	category
4	day	244	non-null	category
5	time	244	non-null	category
6	size	244	non-null	int64
dtype	es: category	(4),	float64(2),	int64(1)

memory usage: 7.4 KB

```
[4]: data.shape
```

[4]: (244, 7)

1.3 Measure of central tendency - Mean, Median and Mode

```
[5]: data.mean()
```

/var/folders/03/k1p5_v6d69bg7b999gdktlgw0000gn/T/ipykernel_5030/531903386.py:1: FutureWarning: The default value of numeric_only in DataFrame.mean is deprecated. In a future version, it will default to False. In addition, specifying 'numeric_only=None' is deprecated. Select only valid columns or specify the value of numeric_only to silence this warning.

data.mean()

[5]: total_bill 19.785943 tip 2.998279 size 2.569672

dtype: float64

[6]: data.median()

/var/folders/03/k1p5_v6d69bg7b999gdktlgw0000gn/T/ipykernel_5030/4184645713.py:1: FutureWarning: The default value of numeric_only in DataFrame.median is deprecated. In a future version, it will default to False. In addition, specifying 'numeric_only=None' is deprecated. Select only valid columns or specify the value of numeric_only to silence this warning.

data.median()

[6]: total_bill 17.795 tip 2.900 size 2.000

dtype: float64

[7]: data.mode()

[7]: total_bill tip sex smoker day time size
0 13.42 2.0 Male No Sat Dinner 2

1.4 Skewness

[8]: data.skew()

/var/folders/03/k1p5_v6d69bg7b999gdktlgw0000gn/T/ipykernel_5030/1188251951.py:1: FutureWarning: The default value of numeric_only in DataFrame.skew is deprecated. In a future version, it will default to False. In addition, specifying 'numeric_only=None' is deprecated. Select only valid columns or specify the value of numeric_only to silence this warning.

data.skew()

dtype: float64

1.5 Distribution plot

[9]: sns.distplot(data['tip'])

 $/var/folders/03/k1p5_v6d69bg7b999gdktlgw0000gn/T/ipykernel_5030/1692055996.py:1: UserWarning:$

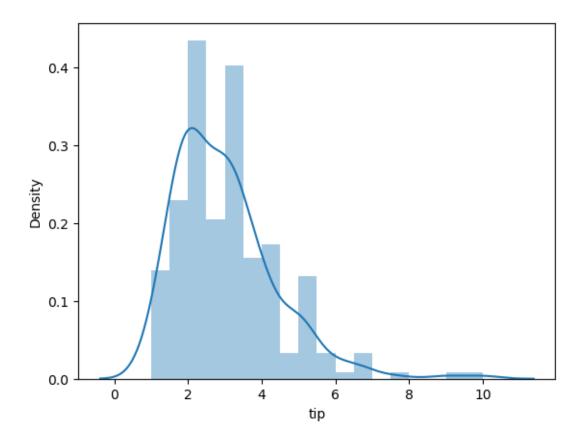
`distplot` is a deprecated function and will be removed in seaborn v0.14.0.

Please adapt your code to use either `displot` (a figure-level function with similar flexibility) or `histplot` (an axes-level function for histograms).

For a guide to updating your code to use the new functions, please see https://gist.github.com/mwaskom/de44147ed2974457ad6372750bbe5751

sns.distplot(data['tip'])

[9]: <Axes: xlabel='tip', ylabel='Density'>



/var/folders/03/k1p5_v6d69bg7b999gdktlgw0000gn/T/ipykernel_5030/3112811999.py:1:

UserWarning:

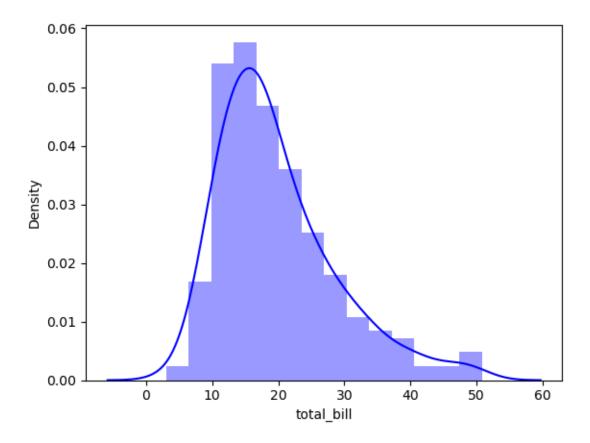
`distplot` is a deprecated function and will be removed in seaborn v0.14.0.

Please adapt your code to use either `displot` (a figure-level function with similar flexibility) or `histplot` (an axes-level function for histograms).

For a guide to updating your code to use the new functions, please see https://gist.github.com/mwaskom/de44147ed2974457ad6372750bbe5751

sns.distplot(data['total_bill'], color = 'b')

[10]: <Axes: xlabel='total_bill', ylabel='Density'>



1.6 Kurtosis

[11]: data.kurt()

/var/folders/03/k1p5_v6d69bg7b999gdktlgw0000gn/T/ipykernel_5030/2907027414.py:1: FutureWarning: The default value of numeric_only in DataFrame.kurt is deprecated. In a future version, it will default to False. In addition, specifying 'numeric_only=None' is deprecated. Select only valid columns or

specify the value of numeric_only to silence this warning.
 data.kurt()

dtype: float64

1.7 Range

[12]: data.max()

/var/folders/03/k1p5_v6d69bg7b999gdktlgw0000gn/T/ipykernel_5030/2904433368.py:1: FutureWarning: The default value of numeric_only in DataFrame.max is deprecated. In a future version, it will default to False. In addition, specifying 'numeric_only=None' is deprecated. Select only valid columns or specify the value of numeric_only to silence this warning.

data.max()

[12]: total_bill 50.81 tip 10.00 size 6.00

dtype: float64

[13]: data.min()

/var/folders/03/k1p5_v6d69bg7b999gdktlgw0000gn/T/ipykernel_5030/927168777.py:1: FutureWarning: The default value of numeric_only in DataFrame.min is deprecated. In a future version, it will default to False. In addition, specifying 'numeric_only=None' is deprecated. Select only valid columns or specify the value of numeric_only to silence this warning.

data.min()

[13]: total_bill

tip 1.00 size 1.00 dtype: float64

[14]: Range = data.max() - data.min()
print(Range)

3.07

total_bill 47.74 tip 9.00 size 5.00

dtype: float64

/var/folders/03/k1p5_v6d69bg7b999gdktlgw0000gn/T/ipykernel_5030/2656667832.py:1: FutureWarning: The default value of numeric_only in DataFrame.max is deprecated. In a future version, it will default to False. In addition, specifying 'numeric_only=None' is deprecated. Select only valid columns or specify the

value of numeric_only to silence this warning.

Range = data.max() - data.min()

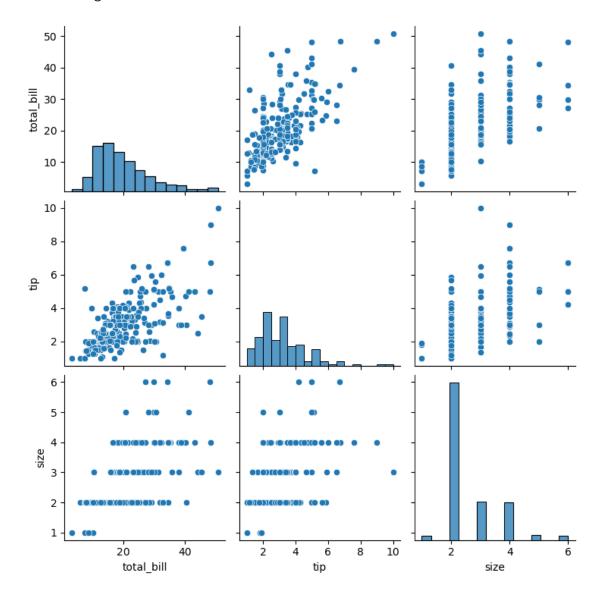
/var/folders/03/k1p5_v6d69bg7b999gdktlgw0000gn/T/ipykernel_5030/2656667832.py:1: FutureWarning: The default value of numeric_only in DataFrame.min is deprecated. In a future version, it will default to False. In addition, specifying 'numeric_only=None' is deprecated. Select only valid columns or specify the value of numeric_only to silence this warning.

Range = data.max() - data.min()

1.8 Pairplot

[15]: sns.pairplot(data)

[15]: <seaborn.axisgrid.PairGrid at 0x130d38250>



1.9 Interquartile range

```
[16]: quantiles = data.quantile(q=[0.75, 0.25])
      quantiles
     /var/folders/03/k1p5_v6d69bg7b999gdktlgw0000gn/T/ipykernel_5030/2995186764.py:1:
     FutureWarning: The default value of numeric_only in DataFrame.quantile is
     deprecated. In a future version, it will default to False. Select only valid
     columns or specify the value of numeric_only to silence this warning.
       quantiles = data.quantile(q=[0.75, 0.25])
                           tip size
[16]:
            total_bill
      0.75
               24.1275 3.5625
                                 3.0
      0.25
               13.3475 2.0000
                                 2.0
[17]: #Q3
      quantiles.iloc[0]
[17]: total_bill
                    24.1275
                     3.5625
      tip
                     3,0000
      size
      Name: 0.75, dtype: float64
[18]: #Q1
      quantiles.iloc[1]
[18]: total_bill
                    13.3475
      tip
                     2.0000
      size
                     2.0000
      Name: 0.25, dtype: float64
[19]: | IQR = quantiles.iloc[0]-quantiles.iloc[1]
      IQR
[19]: total_bill
                    10.7800
                     1.5625
      tip
                     1.0000
      size
      dtype: float64
     1.10 Upper extreme
     Q3 + 1.5*IQR
[20]: quantiles.iloc[0] + (1.5*IQR)
[20]: total_bill
                    40.29750
                     5.90625
      tip
```

size 4.50000

dtype: float64

1.11 Lower extreme

Q1 - 1.5*IQR

[21]: quantiles.iloc[1] - (1.5*IQR)

[21]: total_bill -2.82250 tip -0.34375

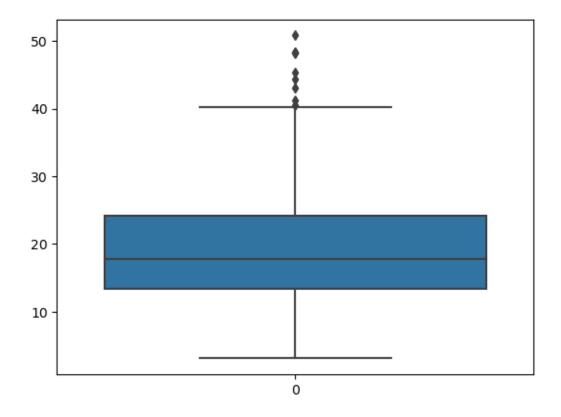
size 0.50000

dtype: float64

1.12 Boxplot

[22]: sns.boxplot(data['total_bill'])

[22]: <Axes: >



1.13 Standard deviation

[23]: data.std()

/var/folders/03/k1p5_v6d69bg7b999gdktlgw0000gn/T/ipykernel_5030/2723740006.py:1: FutureWarning: The default value of numeric_only in DataFrame.std is deprecated. In a future version, it will default to False. In addition, specifying 'numeric_only=None' is deprecated. Select only valid columns or specify the value of numeric_only to silence this warning.

data.std()

[23]: total_bill 8.902412 tip 1.383638 size 0.951100

dtype: float64

1.14 Variance

[24]: data.var()

/var/folders/03/k1p5_v6d69bg7b999gdktlgw0000gn/T/ipykernel_5030/445316826.py:1: FutureWarning: The default value of numeric_only in DataFrame.var is deprecated. In a future version, it will default to False. In addition, specifying 'numeric_only=None' is deprecated. Select only valid columns or specify the value of numeric_only to silence this warning.

data.var()

[24]: total_bill 79.252939 tip 1.914455 size 0.904591

dtype: float64

1.15 Scaling

```
[25]: from sklearn.preprocessing import StandardScaler scale = StandardScaler()
```

```
[26]: x = data[['tip', 'total_bill']]
```

[27]: x.head()

```
[28]: st_scale = scale.fit_transform(x)
      st_scale
[28]: array([[-1.43994695e+00, -3.14711305e-01],
             [-9.69205340e-01, -1.06323531e+00],
             [ 3.63355539e-01, 1.37779900e-01],
             [ 2.25754144e-01, 4.38315103e-01],
             [ 4.43019505e-01, 5.40744704e-01],
             [ 1.23965916e+00, 6.19536705e-01],
             [-7.22971264e-01, -1.23995452e+00],
             [ 8.81527488e-02, 7.98507107e-01],
             [-7.51939979e-01, -5.34203307e-01],
             [ 1.67816714e-01, -5.63468908e-01],
             [-9.32994446e-01, -1.07111451e+00],
             [ 1.44968234e+00, 1.74175992e+00],
             [-1.03438495e+00. -4.91430507e-01].
             [ 1.24660453e-03, -1.52624903e-01],
             [ 1.57309619e-02, -5.57840908e-01],
             [ 6.67527044e-01, 2.01939101e-01],
             [-9.61963161e-01, -1.06436091e+00],
             [ 5.15441291e-01, -3.93503306e-01],
             [ 3.63355539e-01, -3.16962505e-01],
             [2.54722859e-01, 9.72582994e-02],
             [ 7.83401903e-01, -2.10030504e-01],
             [-1.79807863e-01, 5.67366990e-02],
             [-5.56401155e-01, -4.52034507e-01],
             [ 3.31816444e+00, 2.21000952e+00],
             [ 1.31605821e-01, 3.83349840e-03],
             [-4.76737189e-01, -2.22412104e-01],
             [-7.22971264e-01, -7.22178510e-01],
             [-7.22971264e-01, -7.98719310e-01],
             [ 9.42729834e-01, 2.15446301e-01],
             [ 1.24660453e-03, -1.53017018e-02],
             [-1.12129109e+00, -1.15215771e+00],
             [-3.60862330e-01, -1.61629703e-01],
             [ 1.24660453e-03, -5.31952107e-01],
             [-3.97073223e-01, 1.01760699e-01],
             [ 1.96785429e-01, -2.25788904e-01],
             [ 4.35777326e-01, 4.81087904e-01],
             [-7.22971264e-01, -3.91252106e-01],
             [ 5.19418554e-02, -3.21464905e-01],
             [-4.98463725e-01, -1.23359303e-01],
             [ 1.44968234e+00, 1.29264551e+00],
             [-5.49158976e-01, -4.21643306e-01],
             [-3.31893615e-01, -2.61808105e-01],
             [ 4.46996767e-02, -6.58019309e-01],
             [-1.21543942e+00, -1.13752491e+00],
```

```
[ 1.88421306e+00, 1.19471831e+00],
[ 1.24660453e-03, -1.68383303e-01],
[ 1.44968234e+00, 2.75103101e-01],
[ 2.17390021e+00, 1.41983831e+00],
[-6.86760371e-01, 9.86482309e-01],
[ 1.24660453e-03, -1.96523304e-01],
[-3.60862330e-01, -8.15603311e-01],
[-2.88440543e-01, -1.06886331e+00],
[ 1.59452592e+00, 1.69110792e+00],
[-1.04162713e+00, -1.10825931e+00],
[ 9.71698549e-01, 6.49927905e-01],
[ 3.70597718e-01, -3.33113020e-02],
[ 1.24660453e-03, 2.05129992e+00],
[-1.08508020e+00, 7.45603907e-01],
[-8.96783553e-01, -9.61931312e-01],
[ 2.70257926e+00, 3.20616553e+00],
[ 1.53332357e-01, 5.67366990e-02],
[-7.22971264e-01, -6.72652109e-01],
[-7.37455622e-01, -9.86694512e-01],
[ 5.51652185e-01, -1.68383303e-01],
[-2.59471828e-01, -2.47175304e-01],
[ 1.09879285e-01, 3.30990987e-02],
[-3.82588866e-01, -3.75493706e-01],
[-1.44718913e+00, -1.88154652e+00],
[-7.15729086e-01, 4.99830989e-02],
[-6.57791656e-01, -5.37580108e-01].
[-7.44697800e-01, -8.74134511e-01],
[ 1.24660453e-03, -3.05706505e-01],
[ 1.02637106e-01, 7.96255907e-01],
[ 1.44968234e+00, 6.18411105e-01],
[-5.78127691e-01, -5.69096908e-01],
[-1.26613467e+00, -1.04410011e+00],
[ 5.91840340e-02, -2.10030504e-01],
[ 7.25464473e-01, 8.34526308e-01],
[ 1.24660453e-03, 3.34759902e-01],
[-2.08776577e-01, -2.80943305e-01],
[ 1.24660453e-03, -3.89393021e-02],
[ 2.90933752e-01, -3.51856105e-01],
[-8.46088302e-01, -1.09362651e+00],
[ 1.44968234e+00, 1.45135511e+00],
[-7.01244728e-01, -4.28396906e-01],
[ 1.57279938e+00, 1.69335912e+00],
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[ 1.24660453e-03, 1.03375751e+00],
```

```
[ 3.63355539e-01, 3.04368702e-01],
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[7.68917546e-01, 7.92486992e-02],
[ 9.35487655e-01, 6.10531905e-01],
[ 5.51652185e-01, -1.74011304e-01],
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[-3.24651436e-01, 4.68706304e-01],
[ 7.25464473e-01, 6.66811906e-01],
[ 3.63355539e-01, -2.78692105e-01],
[ 1.50037759e+00, 1.14181511e+00].
[-1.08508020e+00, -1.02834171e+00],
[-8.67814838e-01, -8.27984911e-01],
[-5.66908250e-02, 4.83339104e-01],
[-4.98463725e-01, -9.11279312e-01],
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[-5.92612048e-01, 3.41513502e-01],
[-1.08508020e+00, -7.94609025e-02],
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[-7.22971264e-01, -6.34381709e-01],
```

```
[-7.22971264e-01, -4.26145706e-01],
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[ 2.68085272e+00, 1.63370232e+00],
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[-5.05705904e-01, -3.77744906e-01],
[-1.08508020e+00, -1.28722972e+00],
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[-1.00541623e+00, -1.03509531e+00],
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[ 1.55831502e+00, -1.41104572e+00],
[ 1.31605821e-01, 1.35793031e+00],
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[ 3.99566432e-01, 1.67084712e+00],
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[ 1.92042396e+00, 3.98919103e-01],
[ 3.63355539e-01, 2.87749033e+00],
[ 2.53600915e+00, 3.80909503e-01],
[ 1.24660453e-03, 2.33720232e+00],
```

```
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[ 3.63355539e-01, -1.84141704e-01],
[ 7.25464473e-01, 3.73030302e-01],
[-1.08508020e+00, -4.61039307e-01],
[8.63065869e-01, 2.70789839e-03],
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[-7.08486907e-01, -4.84676907e-01],
[ 7.25464473e-01, -3.60860906e-01],
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[ 1.44968234e+00, 2.62535593e+00],
[-7.22971264e-01, -7.63825710e-01],
[-7.22971264e-01, -7.06420109e-01],
[ 7.25464473e-01, -1.21108103e-01],
[-7.15729086e-01, -7.93091310e-01],
[-7.22971264e-01, -7.63825710e-01],
[-3.60862330e-01, -3.81121706e-01],
[ 7.25464473e-01, 8.37510993e-02],
[ 1.67816714e-01, -3.73242506e-01],
[ 2.98175931e-01, 7.65864707e-01],
[ 1.24660453e-03, 2.13234312e+00],
[-7.01244728e-01, 5.04725504e-01],
[-5.56401155e-01, -7.90840110e-01],
[-7.22971264e-01. 1.15644791e+00].
[ 1.56555720e+00, 6.87072706e-01],
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```

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```

1.16 Normalization

```
[29]: from sklearn.preprocessing import MinMaxScaler
      minmaxscale = MinMaxScaler()
[30]: norm_scale = minmaxscale.fit_transform(x)
      norm_scale
[30]: array([[0.00111111, 0.29157939],
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```

1.17 Robust Scaler

```
[31]: from sklearn.preprocessing import RobustScaler robustscale = RobustScaler()

[32]: rob_scale = robustscale.fit_transform(x) rob_scale

[32]: array([[-1.20960000e+00, -7.46753247e-02], [-7.93600000e-01, -6.91558442e-01], [ 3.8400000e-01, 2.98237477e-01], [ 2.62400000e-01, 5.45918367e-01], [ 4.54400000e-01, 6.30333952e-01], [ 1.15840000e+00, 6.95269017e-01], [ -5.76000000e-01, -8.37198516e-01], [ 1.40800000e-01, 8.42764378e-01],
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[-4.22400000e-01, 2.75046382e-01],
[ 1.02400000e+00, 1.29081633e+00],
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[-5.76000000e-01, -6.64656772e-01],
[ 4.54400000e+00, 3.06261596e+00],
[ 1.66400000e-01, -1.84137291e-01],
[ 1.44000000e+00, -9.78200371e-01],
[ 1.79200000e-01, 1.30380334e+00],
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[ 1.34400000e-01, 1.40120594e+00],
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[-5.76000000e-01, -3.07513915e-01],
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[ 4.99200000e-01, 1.56354360e+00],
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[ 3.84000000e-01, 2.55612245e+00],
[ 2.30400000e+00, 4.98608534e-01],
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[-5.76000000e-01. 1.17486085e+00].
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[7.0400000e-01, -1.12708720e-01],
[-9.34400000e-01, -9.49443414e-01],
```

```
[-5.76000000e-01, -6.91558442e-01],
[ 1.34400000e+00, 2.34833024e+00],
[-5.76000000e-01, -4.44805195e-01],
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[7.04000000e-01, 8.48794063e-02],
[-5.69600000e-01, -4.68923933e-01],
[-5.76000000e-01, -4.44805195e-01],
[-2.56000000e-01, -1.29406308e-01],
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[ 2.11200000e-01, -1.22912801e-01],
[ 3.26400000e-01, 8.15862709e-01],
[ 6.4000000e-02, 1.94202226e+00],
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[-4.28800000e-01, -4.67068646e-01],
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[ 1.44640000e+00, 7.50927644e-01],
[ 3.90400000e+00, 2.83256030e+00],
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[ 2.30400000e+00, 9.62430427e-01],
[-1.15200000e+00, -4.54081633e-01],
[ 6.4000000e-02, 9.60575139e-01],
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[ 3.13600000e-01, -5.73747681e-01],
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[ 6.4000000e-02, -2.10111317e-01],
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[-1.21600000e+00, -4.81910946e-01],
[-1.10720000e+00, 1.39471243e+00],
[ 1.13280000e+00, 1.67300557e+00],
[ 1.93280000e+00, 1.04220779e+00],
[-5.76000000e-01, 8.70593692e-01],
[-5.76000000e-01, 4.52226345e-01],
[-7.36000000e-01, 2.31910946e-03],
```

```
[ 6.4000000e-02, 9.13729128e-02]])
```

1.18 Distribution

1.18.1 Uniform distribution

[33]: rand = np.random.rand(1000) sns.distplot(rand)

 $/var/folders/03/k1p5_v6d69bg7b999gdktlgw0000gn/T/ipykernel_5030/3868814289.py: 2: UserWarning:$

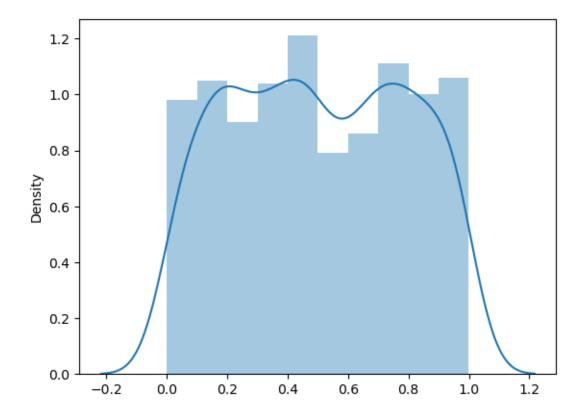
`distplot` is a deprecated function and will be removed in seaborn v0.14.0.

Please adapt your code to use either `displot` (a figure-level function with similar flexibility) or `histplot` (an axes-level function for histograms).

For a guide to updating your code to use the new functions, please see https://gist.github.com/mwaskom/de44147ed2974457ad6372750bbe5751

sns.distplot(rand)

[33]: <Axes: ylabel='Density'>



1.18.2 Exponential distribution

[34]: sns.distplot(np.log(rand))

 $/var/folders/03/k1p5_v6d69bg7b999gdktlgw0000gn/T/ipykernel_5030/1300547632.py:1: UserWarning:$

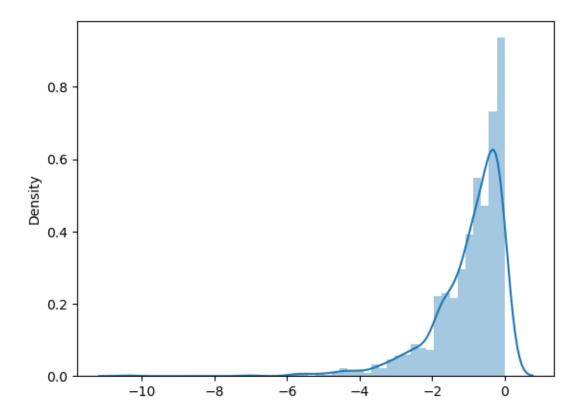
`distplot` is a deprecated function and will be removed in seaborn v0.14.0.

Please adapt your code to use either `displot` (a figure-level function with similar flexibility) or `histplot` (an axes-level function for histograms).

For a guide to updating your code to use the new functions, please see https://gist.github.com/mwaskom/de44147ed2974457ad6372750bbe5751

sns.distplot(np.log(rand))

[34]: <Axes: ylabel='Density'>



1.18.3 Normal distribution

[35]: sns.distplot(data.total_bill)

 $/var/folders/03/k1p5_v6d69bg7b999gdktlgw0000gn/T/ipykernel_5030/805800272.py:1: UserWarning:$

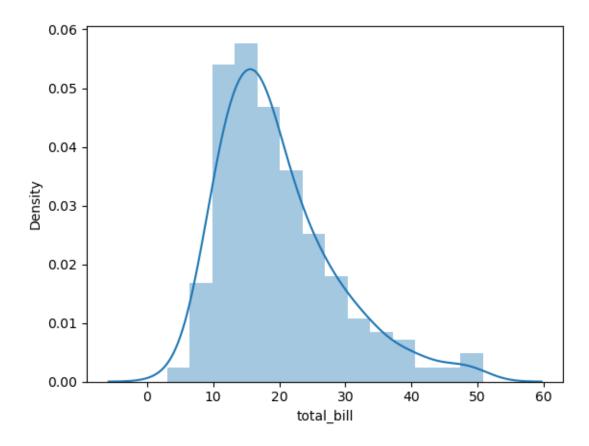
`distplot` is a deprecated function and will be removed in seaborn v0.14.0.

Please adapt your code to use either `displot` (a figure-level function with similar flexibility) or `histplot` (an axes-level function for histograms).

For a guide to updating your code to use the new functions, please see https://gist.github.com/mwaskom/de44147ed2974457ad6372750bbe5751

sns.distplot(data.total_bill)

[35]: <Axes: xlabel='total_bill', ylabel='Density'>



1.19 Central limit theorem

[38]: <Axes: ylabel='Density'>

The central limit theorem says that the sampling distribution of the mean will always be normally distributed, as long as the sample size is large enough.

