



# Vidyavardhini's College of Engineering and Technology

## Department of Artificial Intelligence & Data Science

### Experiment 8

**Aim:** Implementation of unification algorithm in Prolog.

**Objective:** To study about how to use AI Programming language (Prolog) for developing interfacing engine using Unification process and knowledge declared in Prolog.

**Requirement:** Turbo Prolog 2.0 or above / Windows Prolog.

#### Theory:

Unification is a process of making two different logical atomic expressions identical by finding a substitution. .... It takes two literals as input and makes them identical using substitution. Let  $\Psi_1$  and  $\Psi_2$  be two atomic sentences and be a unifier such that,  $\Psi_1 = \Psi_2$ , then it can be expressed as UNIFY( $\Psi_1, \Psi_2$ ).

**For example,** if one term is  $f(X, Y)$  and the second is  $f(g(Y, a), h(a))$  (where upper case names are variables and lower case are constants) then the two terms can be unified by identifying  $X$  with  $g(h(a), a)$  and  $Y$  with  $h(a)$  making both terms look like  $f(g(h(a), a), h(a))$ . The unification can be represented by a pair of substitutions  $\{X \mapsto g(h(a), a)\}$  and  $\{Y \mapsto h(a)\}$ .  $\square$

#### Unification Algorithm:

```
FUNCTION unify( t1, t2 ) RETURNS (unifiable : BOOLEAN, sigma :SUBSTITUTION) BEGIN
IF t1 OR t2 is a variable THEN BEGIN
  let x be the variable and let t be the other term IF x == t THEN (unifiable, sigma) := (TRUE,
  NULL_SUBSTITUTION); ELSE IF x occurs in t THEN
  unifiable == FALSE;
  ELSE (unifiable, sigma) := (TRUE,
  {x <- t}); ENDELSE
BEGIN
  assume t1 == f(x1,....., xn) and t2 == g(y1,
  ... ym) IF f != g OR m != n THEN
  unifiable = FALSE; ELSE BEGIN
  N k
  := 0;
  unifiable := TRUE;
  sigma := NULL_SUBSTITUTION;
  WHILE k < m AND
  unifiable DO BEGIN
  k := k + 1;
  (unifiable, tau) := unify( sigma( xk ), sigma( yk ) ); IF unifiable THEN sigma := compose(tau, sigma );
  END
  END
  END
  RETURN (unifiable,sigma); END
```

#### Implementation Notes

1. To extract the name of a functor and its arguments, you may use the special built-in rules **functor/3**, **arg/3**, and **"=.."**. (Prolog allows overloading of rule names; the notation `foo/2` denotes the `foo` rule that takes two arguments.) They are used as follows:

1. `functor(f(x,y),F,N) ==> F=f and N=2` 2. `arg(1,f(x,y),A) ==> A=x` 3. `f(x,y)=.. L ==> L`



$= [f, x, y]$

Incidentally, an atom is treated as a 0-argument functor.

- As an option, you may encode functors to be unified as lists in prefix notation. Foreexample,  $f(x)$  would be encoded as  $[f, x]$ . For a more complicated example, the following function:  $f(3, g(x))$  would be encoded as:

$[f, 3, [g, x]]$

This notation doesn't look as nice, but it might make the implementation simpler.

- You must choose how to distinguish variables from atoms in the expressions you are matching. For example, if **a** and **b** are constants, then unification of **a** and **b** should fail. However, if **A** and **B** are both variables, then unification should succeed, with the single substitution **A**  $\rightarrow$  **B**. A reasonable choice is that t, u, v, w, x, y, and z are variables, while all other letters are constants. In any case, please document your choice.

### Testing Your Unifier

Here are some tests you should try before stopping work on your unifier. Harder tests are towards the bottom.

- Two atoms should unify iff both atoms are the same. Two different atoms should fail to unify.
- A variable should unify with anything that does not contain that variable. Foreexample, x should unify with  $f(g(y), 3, (h(a, z)))$ , but not with  $f(x)$ .
- A variable should unify with itself. For example, x should unify with x.
- Your algorithm should handle cases where a variable appears in multiple locations  
For example, all of the following should unify:
  - $f(x, x) = f(a, a)$ 
    - $f(x, g(x)) = f(a, g(x))$
  - $f(x, y) = f(y, x)$
 And the following should NOT unify
  - $f(x, x) = f(a, b)$ 
    - $f(x, g(x)) = g(a, g(b))$
- When unifying functors, all arguments should unify. For example,  $g(h(1, 2, 3, 4), 5)$  does not unify with  $g(h(1, 8, 3, 4), 5)$ .
- There are plenty of other things to try. These are just some examples to start.

### Unification in Prolog:

The way in which Prolog matches two terms is called unification. The idea is similar to that of unification in logic: we have two terms and we want to see if they can be made to represent the same structure. For example, we might have in our database the single Prolog clause:

`parent(alan, clive).` and give the query:

`?- parent(X, Y).`

We would expect X to be instantiated to alan and Y to be instantiated to clive when the query succeeds. We would say that the term `parent(X, Y)` unifies with the term `parent(alan, clive)` with X bound to alan and Y bound to clive. The unification algorithm in Prolog is roughly this:

**df:un** Given two terms and which are to be unified:

If **a** and **b** are constants (i.e. atoms or numbers) then if they are the same succeed. Otherwise fail.



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If  $t_1$  is a variable then instantiate to  $t_2$ . Otherwise, If  $t_1$  is a variable then instantiate to  $t_2$ .

Otherwise, if  $t_1$  and  $t_2$  are complex terms with the same arity (number of arguments), find the principal functor of  $t_1$  and principal functor of  $t_2$ . If these are the same, then take the ordered set of arguments of  $t_1$  and the ordered set of arguments of  $t_2$ . For each pair of arguments  $a_i$  and  $b_i$  from the same position in the term, must unify  $a_i$  with  $b_i$ . Otherwise fail.

**For example:** applying this procedure to unify  $\text{foo}(a, X)$  with  $\text{foo}(Y, b)$  we get:  $\text{foo}(a, X)$  and  $\text{foo}(Y, b)$  are complex terms with the same

arity (2). The principal functor of both terms is  $\text{foo}$ .

The arguments (in order) of  $\text{foo}(a, X)$  are  $a$  and  $X$ . The arguments (in order) of  $\text{foo}(Y, b)$  are  $Y$  and  $b$ . So  $a$  and  $Y$  must unify, and  $X$  and  $b$  must unify.  $Y$  is a variable so we instantiate  $Y$  to  $a$ .

$X$  is a variable so we instantiate  $X$  to  $b$ .

The resulting term, after unification is  $\text{foo}(a, b)$ .

The built in Prolog operator '=' can be used to unify two terms. Below are some examples of its use. Annotations are between \*\* symbols.

| ?-  $a = a$ .      \*\* Two identical atoms unify \*\* yes

| ?-  $a = b$ .      \*\* Atoms don't unify if they aren't identical \*\* no

| ?-  $X = a$ .      \*\* Unification instantiates a variable to an atom \*\*  $X = a$

yes

| ?-  $X = Y$ . \*\* Unification binds two differently named variables \*\*  $X = \_125451$       \*\* to a single, unique variable name \*\*

$Y = \_125451$

yes

| ?-  $\text{foo}(a, b) = \text{foo}(a, b)$ . \*\* Two identical complex terms unify \*\* yes

| ?-  $\text{foo}(a, b) = \text{foo}(X, Y)$ . \*\* Two complex terms unify if they are \*\*  $X = a$       \*\* of the same arity, have the same principal \*\*

$Y = b$       \*\* functor and their arguments unify \*\* yes

| ?-  $\text{foo}(a, Y) = \text{foo}(X, b)$ . \*\* Instantiation of variables may occur \*\*  $Y = b$       \*\* in either of the terms to be unified \*\*  $X =$



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a yes

| ?- foo(a,b) = foo(X,X). \*\* In this case there is no unification \*\* no \*\* because foo(X,X) must have the same

\*\*

\*\* 1st and 2nd arguments \*\*

| ?- 2\*3+4 = X+Y. \*\* The term 2\*3+4 has principal functor + \*\* X=2\*3 \*\* and

therefore unifies with X+Y with X instantiated \*\* Y=4 \*\* to 2\*3 and Y

instantiated to 4 \*\*yes

| ?- [a,b,c] = [X,Y,Z]. \*\* Lists unify just like other terms \*\* X=a

Y=

b Z=

cyes

| ?- [a,b,c] = [X|Y]. \*\* Unification using the '|' symbol can be used \*\* X=a \*\* to find the head element,

X, and tail list, Y, \*\* Y=[b,c] \*\* of a list \*\*

yes

| ?- [a,b,c] = [X,Y|Z]. \*\* Unification on lists doesn't have to be \*\* X=a \*\* restricted to finding the first head element \*\*

Y=b \*\* In this case we find the 1st and 2nd elements \*\* Z=[c] \*\* (X and Y) and then the tail

list (Z) \*\*

yes

| ?- [a,b,c] = [X,Y,Z|T]. \*\* This is a similar example but there \*\* X=a \*\* the first 3 elements are unified with

\*\*



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Y=b                      \*\* variables X, Y and Z, leaving the \*\*Z=c                      \*\* tail, T, as an empty list

[] \*\* T=[]

Yes

| ?- [a,b,c] = [a|[b|[c|[]]]]. \*\* Prolog is quite happy to unify these \*\* yes\*\* because they are just notational

\*\*

\*\* variants of the same Prolog term \*\*

### Code:

#### Code 1:

```
is_changed = True
```

```
# Add more initial facts
```

```
facts = [["vertebrate", "duck"], ["flying", "duck"], ["mammal", "cat"], ["insect", "bee"], ["vertebrate", "dog"]]
```

```
def assert_fact(fact):
```

```
    global facts
```

```
    global is_changed
```

```
    if fact not in facts:
```

```
        facts += [fact]
```

```
        is_changed = True
```

```
while is_changed:
```

```
    is_changed = False
```

```
for A1 in facts:
```

```
    if A1[0] == "mammal":
```

```
        assert_fact(["vertebrate", A1[1]])
```

```
    if A1[0] == "vertebrate":
```

```
        assert_fact(["animal", A1[1]])
```

```
    if A1[0] == "vertebrate" and ["flying", A1[1]] in facts:
```

```
        assert_fact(["bird", A1[1]])
```

```
print(facts)
```

### Output:

```
[['vertebrate', 'duck'], ['flying', 'duck'], ['mammal', 'cat'], ['insect', 'bee'], ['vertebrate', 'dog'], ['animal', 'duck'], ['animal', 'cat'], ['animal', 'dog'], ['vertebrate', 'cat'], ['bird', 'duck']]
```



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### Code 2:

```
is_changed = True
facts = [["can_fly", "sparrow"], ["has_feathers", "sparrow"], ["animal", "sparrow"]]
def assert_fact(fact):
    global facts
    global is_changed
    if fact not in facts:
        facts.append(fact)
        is_changed = True
while is_changed:
    is_changed = False
    for A1 in facts:
        if A1[0] == "animal":
            assert_fact(["living_organism", A1[1]])
            if A1[0] == "living_organism" and ["can_fly", A1[1]] in facts:
                assert_fact(["bird", A1[1]])
print(facts)
```

```
is_changed = True
facts = [["mammal", "lion"], ["has_fur", "lion"], ["animal", "lion"]]
def assert_fact(fact):
    global facts
    global is_changed
    if fact not in facts:
        facts.append(fact)
        is_changed = True
while is_changed:
    is_changed = False
    for A1 in facts:
        if A1[0] == "animal":
            assert_fact(["living_organism", A1[1]])
            if A1[0] == "living_organism" and ["mammal", A1[1]] in facts:
                assert_fact(["warm_blooded", A1[1]])
print(facts)
```

### Output:

```
['can_fly', 'sparrow'], ['has_feathers', 'sparrow'], ['animal', 'sparrow'], ['living_organism', 'sparrow'], ['bird', 'sparrow']]
['mammal', 'lion'], ['has_fur', 'lion'], ['animal', 'lion'], ['living_organism', 'lion'], ['warm_blooded', 'lion']]
```

### Conclusion:

Thus, we have studied about how to use AI Programming language (Prolog) for developing Interfacing engine using Unification process and knowledge declared in Prolog.