Assessment: Jacobians and Hessians

LATEST SUBMISSION GRADE

100%

1. In this assessment, you will be tested on all of the different topics you have in covered this module. Good luck!

Calculate the Jacobian of the function $f(x,y,z)=x^2cos(y)+e^zsin(y)$ and evaluate at the point $(x, y, z) = (\pi, \pi, 1).$

- (a) $J(x, y, z) = (-2\pi, -e, 0)$
- $\int J(x,y,z) = (-2\pi,e,0)$
- $\int J(x,y,z) = (-2\pi,e,1)$
- $\int J(x,y,z) = (-2\pi, -e, 1)$

✓ Correct

Well done!

2. Calculate the Jacobian of the vector valued functions:

 $u(x,y)=x^2y-cos(x)sin(y)$ and $v(x,y)=e^{x+y}$ and evaluate at the point $(0,\pi)$.

- $\bigcirc \begin{bmatrix} e^\pi & 1 \\ 0 & e^\pi \end{bmatrix}$
- $egin{pmatrix} e^{\pi} & 1 \ e^{\pi} & 0 \end{bmatrix}$
- $igcirc \left[egin{matrix} 0 & e^\pi \ 1 & e^\pi \end{matrix}
 ight]$
- $egin{array}{ccc} egin{pmatrix} 0 & 1 \ e^\pi & e^\pi \end{bmatrix}$.
 - ✓ Correct

Well done!

3. Calculate the Hessian for the function $f(x,y)=x^3cos(y)-xsin(y)$.

$$O_H = \begin{bmatrix} 6\cos(x) & -3x^2\sin(y) - \cos(y) \\ -3x^2\sin(y) - \cos(y) & x\sin(y) - y^3\cos(x) \end{bmatrix}$$

$$\bigcirc H = egin{bmatrix} 6cos(y) & -3x^2sin(y)-cos(y^2) \ -3x^2sin(y)-cos(y) & x^2sin(y)-x^3cos(y) \end{bmatrix}$$

$$O H = \begin{bmatrix} 6x^2cos(y) & -3x^2sin(y) - cos(x) \\ -3x^2sin(y) - cos(y) & xsin(y) - xcos(y) \end{bmatrix}$$

✓ Correct

Well done!

Calculate the Hessian for the function $f(x, y, z) = xy + sin(y)sin(z) + z^3e^x$.

$$H = \begin{bmatrix} e^x z^3 & 1 & 3e^x z^2 \\ 1 & -\sin(y)\sin(z) & \cos(y)\cos(z) \\ 3e^x z^2 & \cos(y)\cos(z) & 6e^x z - \sin(y)\sin(z) \end{bmatrix}$$

$$H = \begin{bmatrix} 3e^{x}z^{2} & -1 & 3e^{x}z \\ 1 & -\sin(x^{2})\sin(z) & \cos(y)\cos(z) \\ 3e^{x}z & \cos(y)\cos(z) & 6e^{y}z^{2} - \sin(y)\sin(z) \end{bmatrix}$$

$$H = \begin{bmatrix} 2e^{x}z^{3} & 1 & e^{x}z^{2} \\ 0 & -\sin(x)\sin(z) & \cos(y)\cos(z) \\ 3e^{x}z^{2} & \cos(y)\cos(z) & 6e^{2x} - \sin(y)\sin(x) \end{bmatrix}$$

$$H = egin{bmatrix} 2e^xz^3 & 1 & e^xz^2 \ 0 & -sin(x)sin(z) & cos(y)cos(z) \ 3e^xz^2 & cos(y)cos(z) & 6e^{2x} - sin(y)sin(x) \end{bmatrix}$$

$$H = \begin{bmatrix} -e^x z^3 & 0 & 3e^y z^2 \\ 1 & \sin(y)\sin(z) & \cos(y)\cos(z) \\ 3e^x z & \cos(y)\cos(z) & 6e^{-xz} - \sin(y)\sin(z) \end{bmatrix}$$

Correct

Well done!

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5. Calculate the Hessian for the function $f(x,y,z)=xycos(z)-sin(x)e^yz^3$ and evaluate at the point (x,y,z)=(0,0,0)

$$H = \begin{bmatrix} 0 & 1 & 0 \\ 1 & 0 & 0 \\ 0 & 0 & 0 \end{bmatrix}$$

$$\begin{array}{c}
O \\
H = \begin{bmatrix}
0 & 1 & 0 \\
0 & 0 & 0 \\
0 & 1 & 0
\end{bmatrix}$$

$$\begin{array}{c}
 H = \begin{bmatrix}
 0 & 0 & 0 \\
 1 & 0 & 0 \\
 0 & 1 & 0
\end{bmatrix}$$

$$\begin{array}{c}
O \\
H = \begin{bmatrix}
0 & 0 & 0 \\
1 & 0 & 1 \\
0 & 0 & 0
\end{bmatrix}$$

Well done!