



Today's agenda

↳ Recursion

↳ How to write Recursive code.

Why recursion →

↳ Tree

↳ Backtracking

Google ← ↳ DP → Amazon

↳ Graph



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Recursion:

↳ function calling itself.

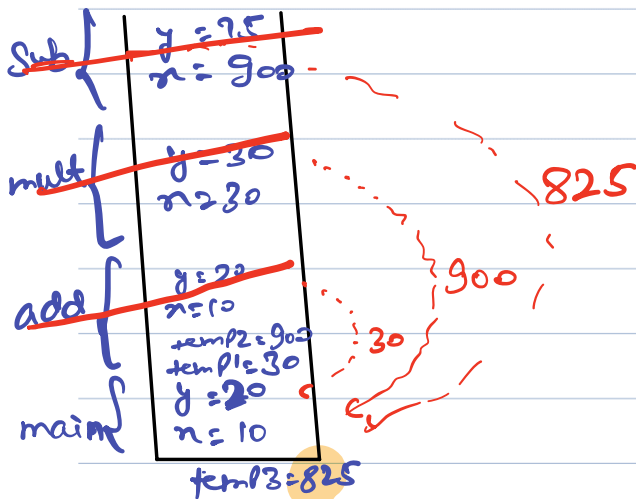
* function call

```
main ( ) {  
    int x = 10;  
    int y = 20;  
    int temp1 = add(x, y);  
    int temp2 = mult(temp1, 30);  
    int temp3 = sub(temp2, 75);  
    s.o.p(temp3);  
}
```

```
int add(int x, int y){  
    return x + y;  
}
```

```
int mult(int x, int y){  
    return x * y;  
}
```

```
int sub(int x, int y){  
    return x - y;  
}
```





// Thought Process

$$n=5$$

$$\text{Sum}(n) = 1 + 2 + 3 + \dots + n-1 + n$$

$$\text{Sum}(5) = \text{Sum}(4) + 5$$

$$\text{Sum}(4) = \text{Sum}(3) + 4$$

$$\text{Sum}(3) = \text{Sum}(2) + 3$$

$$\text{Sum}(2) = \text{Sum}(1) + 2$$

$$\text{Sum}(1) = \text{Sum}(0) + 1$$



Q) Given N , find sum of no.s from $1 \dots N$, using recursion.

Three magical steps of recursion.

Faith: define what your function should do and have faith that it works.

Main logic: Solve your Problem with SubProblem

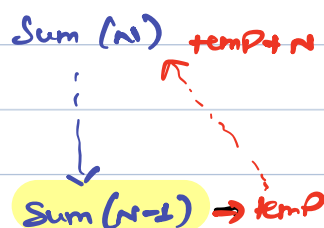
↳ smaller instance of same Problem.

Base case: Solution to Smallest SubProblem.

```
int Sum (int N) {  
    if (N == 1) { return 1; }  
  
    int temp = Sum (N-1);  
  
    return temp + N;  
}
```

Faith: Given N , Calculate & return sum of first N natural no.s.

Main logic:



↳ overall T.C: $O(1) * N = O(N)$

↳ overall S.C: $O(1) * N = O(N)$

base case: $N == 1 \rightarrow 1$



Q) find factorial of N .

Ex: $N=3 \rightarrow 3 \times 2 \times 1 = 6$

$N=4 \rightarrow 4 \times 3 \times 2 \times 1 = 24$

```
int fact(int n) {  
    if (n == 0) return 1;  
}
```

Goal: Given N , calculate & return factorial of N .

```
    int temp = fact(n-1);  
    return temp * n;  
}
```

main logic:

$fact(n) \rightarrow temp * n$
 \downarrow
 $fact(n-1) \rightarrow temp$

overall T.C: $O(1) * N = O(N)$

overall S.C: $O(1) * N = O(N)$

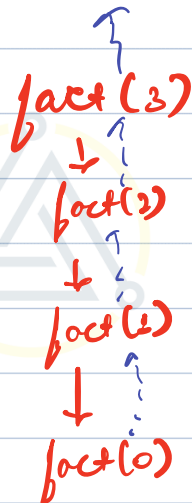
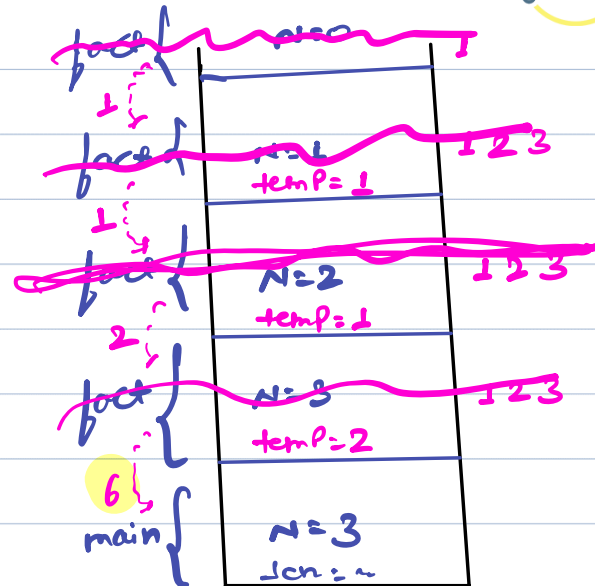
base case:

$fact(0) = 1$

dry run



```
int fact(int n) {  
  1 if (n == 0) { return 1; }  
  
  2 int temp = fact(n-1);  
  
  3 return temp * n;  
}
```



Break till 9:40 PM



Q) Print N^{th} fibonacci number, with recursion.

Ex:

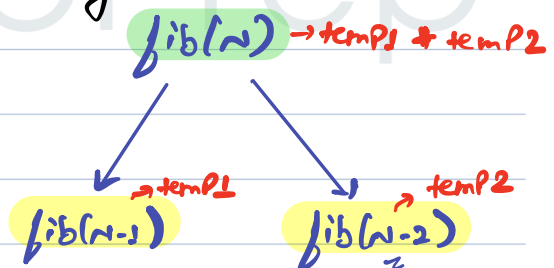
	0	1	2	3	4	5	6	7	8	9	10
Fib:	0	1	1	2	3	5	8	13	21	34	55

$$\text{fib}(n) = \text{fib}(n-1) + \text{fib}(n-2).$$

```
int fib(int n) {  
    if (n == 0) { return 0; }  
    if (n == 1) { return 1; }  
    int temp1 = fib(n-1);  
    int temp2 = fib(n-2);  
    return temp1 + temp2;  
}
```

Faith: Given n , calculate & return nth fibonacci number.

Main logic:



T.C of 1 function: $O(1)$
No. of functions: 2^n

Base Case:

$\hookrightarrow \text{fib}(0) = 0$
 $\text{fib}(1) = 1$

overall sc: $O(1) * N$
 $= O(N)$

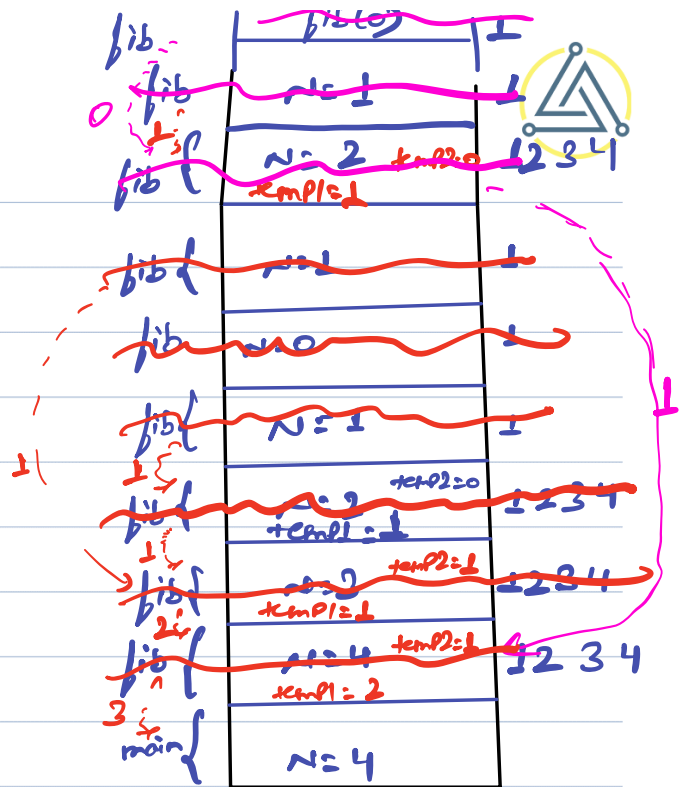

```

int fib(int n) {
1  if (n == 0) { return 0; }
   if (n == 1) { return 1; }

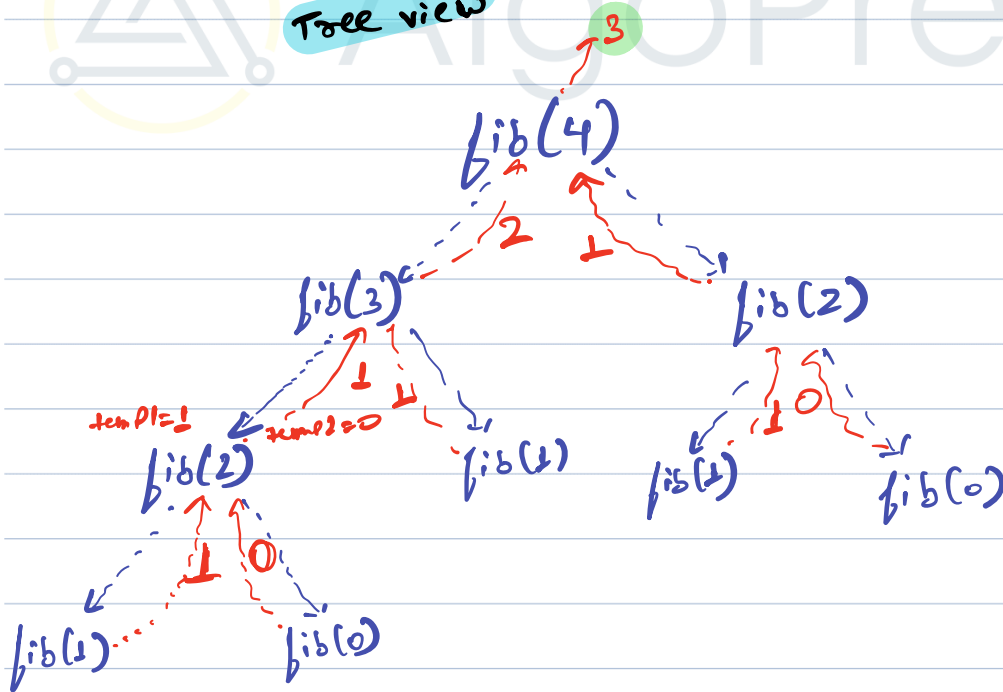
2  int temp1 = fib(n-1);
3  int temp2 = fib(n-2);

4  return temp1 + temp2;
}

```



Tree view





Q) Print increasing

↳ Given N , Print all the numbers from $1 \rightarrow N$, using recursion.

```
void Printincreasing (int N) {  
    if (N == 1) { s.o.p(1);  
        return; }  
}
```

Faith: Given N , Print nos from 1 to N .

Main logic:

```
Printincreasing (N-1);  
s.o.p (N);  
return;
```

{ 1 2 3 ... N-1 } N

Base Case:

```
if (N == 1) { s.o.p(1);  
    return; }
```

}

Tracing



```
void Printincreasing (int n) {
```

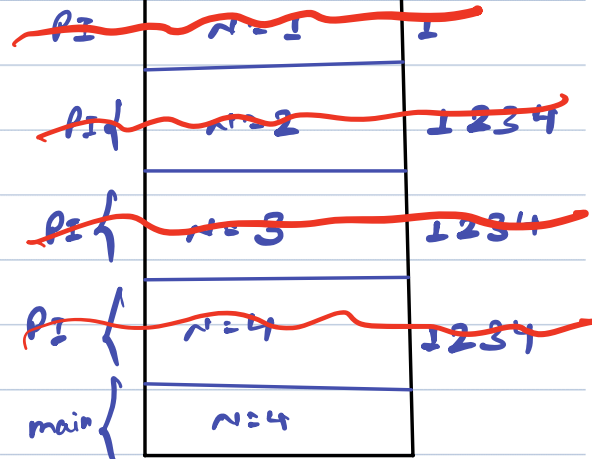
```
1 if (n == 1) { s.o.p(1);  
   return; }
```

```
2 Printincreasing (n-1);
```

```
3 s.o.p(n);
```

```
4 return;
```

```
}
```



- 1
- 2
- 3
- 4

PI(4) 4 ✓

↓

PI(3) 3 ✓

↓

PI(2) 2 ✓

↓

PI(1) ✓

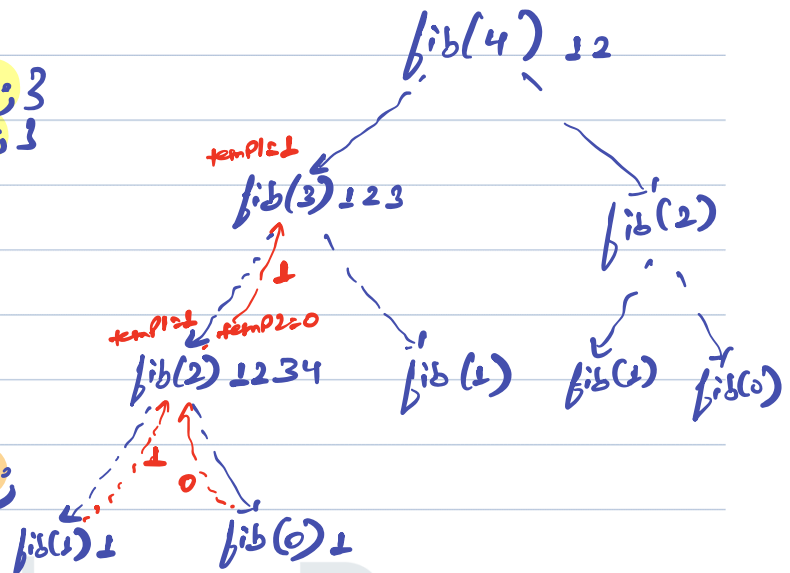


```
int fib(int n) {  
1 if (n == 0) { return 0; }  
2 if (n == 1) { return 1; }  
3
```

```
4 int temp1 = fib(n-1);
```

```
5 int temp2 = fib(n-2);
```

```
6 return temp1 + temp2;  
7 }
```



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