Poisson:
$$p(x) = \lambda^x e^{-\lambda}$$

$$P(y|\theta) = \prod_{i=1}^{n} P(y_i|\theta)$$

$$= \prod_{i=1}^{n} P(y_i | \Theta) P(y_2 | \Theta) \dots P(y_n | \Theta)$$

$$P(y|\theta) = \frac{10}{11} \quad y'' = \frac{10}{2!} \quad (2!)^{4} \quad (6!)^{2} \quad (1!)^{2} \quad (6!)^{2} \quad (1!)^{2} \quad (1!$$

(p)
$$b(x) = K$$

$$\frac{p(x) = k}{\infty} \frac{p(x) dx}{= \infty} = \frac{k(x)^{\infty}}{\infty}$$

not a proper prior.

c) Using prior p(x) = K p(0/y) & p(y10) · p(0) i.e. p(x/y) & P(y/x).P(x) $\frac{10}{\sqrt{11}} \frac{\sqrt{9}}{\sqrt{9}} e^{-\frac{1}{2}\sqrt{11}}$ $\frac{1}{21} \frac{\sqrt{9}}{\sqrt{9}} e^{-\frac{1}{2}\sqrt{11}}$ $\frac{1}{21} \frac{\sqrt{9}}{\sqrt{9}} e^{-\frac{1}{2}\sqrt{11}}$ X 72,91 6-2010) 19 y; ! b(x/y) a x = 10x Ti y:1 = (a))) ∞ × -1 = 5 y; (i) B = 0.1 (ii) $\chi = \frac{1}{2}y_1 + 1 = 22 + 1 = 23$ (b)= (iv) V(x) = Gamma (= y: +1) (V) Of the form Gamma (Ey; +1,0.1

(C) Ganna (23,0.1) Heore Parion; $p(\lambda) = Gamma(\alpha, \beta) = \frac{1}{(\alpha)\beta^{\alpha}} \lambda^{\alpha-1} e^{-\lambda/\beta}$ p(0/y) & p(y/0).p(0) ie. p(xly) & p(ylx).p(x) $X = \frac{1}{2} =$ α $(\lambda^{2}y^{2})$ $e^{-10\lambda}$ $(\Gamma(\alpha)^{2})$ $(\Gamma(\alpha)^{2})$ $P(x|y) \propto \chi^{\frac{10}{2}y;+\alpha-1} e^{-10\chi-\chi/B}$ $(Y(\alpha)\beta^{\alpha})(f_{1}^{\alpha}y_{1}^{\alpha})$ $= \frac{2}{3} + \frac{1}{3} + \frac{1}{3} = \frac{$

For the above Equation Gamma Functions

$$\alpha = 1 = 20$$

$$\alpha = 1 = 41$$

$$\alpha = 42$$

$$\alpha = 1 = 20$$

$$\beta = 1 = 0.05$$

$$20$$

$$P(N|\Theta y) \propto Gamma(42, 1/20)$$

$$Patien P(N) = Gamma(20, 0.1) = 3$$

$$Posterion g(1) : 2 Gamma(20, 0.1)$$

$$From (1) : C) = Non-informative paien a = (2 y; +1) = 1$$

Forom (1) e) with informative paid.

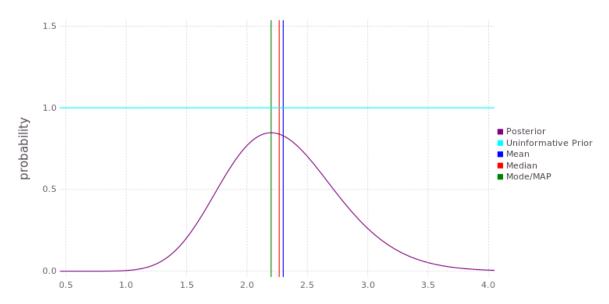
When we observe the value $x \otimes B$ provided in (1).e as the posterior of opinion-informative parish, it can be said that for x = 20, Total number of orims which were counted x = 20, x = 20,

and for $\beta = 0.1$, total no. of samples considered for the data were n = 1 = 10

Thus, the informative prior incorporates the data about previous information while evaluating the parameter for posterior.

1.d

```
In [17]:
         x = collect(0:0.001:10);
         prior = ones(length(x));
         median val = Base.median(d);
         mean val = Base.mean(d);
         mode val = Distributions.modes(d);
         posterior1 = pdf.(d,x);
         myplot = Gadfly.plot(
         layer(x=x,y=posterior1,Geom.line,Theme(default color=colorant"purple")),
         layer(x=x,y=prior,Geom.line,Theme(default_color=colorant"cyan")),
         layer(xintercept=[mean_val],Geom.vline(color=colorant"blue")),
         layer(xintercept=[median val],Geom.vline(color=colorant"red")),
         layer(xintercept=[mode_val[1]],Geom.vline(color=colorant"green")),
         Coord.Cartesian(xmin=0.5, xmax=4,ymax=1.5), Guide.ylabel("probability"),
         Guide.xlabel(""),
         Guide.manual color key("", ["Posterior", "Uninformative Prior",
         "Mean", "Median", "Mode/MAP"], ["purple", "cyan", "blue", "red", "green"]));
         draw(PNG(8inch, 4inch), myplot)
```



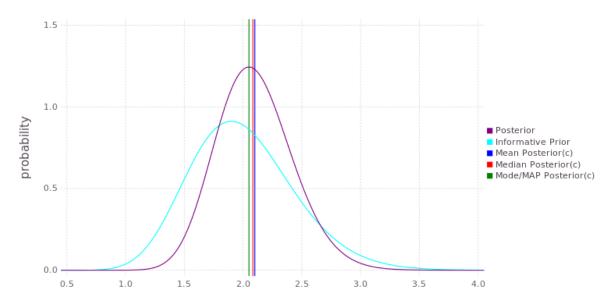
Out[17]: false

WARNING: both Gadfly and Base export "cross"; uses of it in module Main must be qualified

1.f

```
In [19]: posterior_2nd = Gamma(42,0.05)
posterior2 = pdf.(posterior_2nd,x);
prior_2nd = Gamma(20,0.1)
prior2 = pdf.(prior_2nd,x);
```

```
In [20]:
         x = collect(0:0.001:10);
         median val = Base.median(posterior 2nd);
         mean val = Base.mean(posterior 2nd);
         mode val = Distributions.modes(posterior 2nd);
         myplot 2 = Gadfly.plot(
         layer(x=x,y=posterior2,Geom.line,Theme(default color=colorant"purple")),
         layer(x=x,y=prior2,Geom.line,Theme(default color=colorant"cyan")),
         layer(xintercept=[mean val],Geom.vline(color=colorant"blue")),
         layer(xintercept=[median val],Geom.vline(color=colorant"red")),
         layer(xintercept=[mode_val[1]],Geom.vline(color=colorant"green")),
         Coord.Cartesian(xmin=0.5, xmax=4,ymax=1.5), Guide.ylabel("probability"),
         Guide.xlabel(""),
         Guide.manual_color_key("", ["Posterior", "Informative Prior",
         "Mean Posterior(c)", "Median Posterior(c)", "Mode/MAP Posterior(c)"], ["purpl
         e","cyan","blue","red","green"]));
         draw(PNG(8inch, 4inch), myplot_2)
```



Out[20]: false

The informative prior tells us that 19 crimes were previously observed over 10 days. The new posterior with informative prior is plotted above and shows that 21 crimes are observed with higher probability as compared to posterior with non informative prior.

```
In [23]: prob_6_crimes = 1 - cdf(crime,6)
Out[23]: 0.005165998190080345
```

The Probability of 6 or more crimes today is 0.0051

In []:			
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