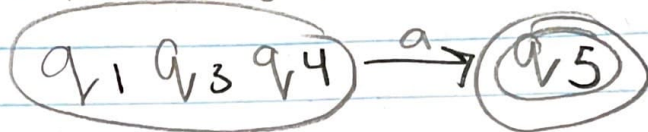


## HW # 3 Akash

- 1) Remove inaccessible states  $q_2$  &  $q_6$ . Next, partition into equivalence class.

$q_1, q_3, q_4$        $q_5$   
 non final state      Final state

No further partitioning possible since  $q_1, q_3, q_4$  are indistinguishable.



2) a)  $(a+b+c)^* \cup b$

b)  $a$

c)  $a$

d)  $(\lambda)^*$

e)  $(\lambda)^* + (ab)^*$

3) a)  $(0+10)^* (11) (0+01)^* + (0+10)^* (0+01)^*$

On the left side, we have all strings that include the substring "11" since they can have a  $\infty$  amount of 0 or 10's preceding the "11" &

$\infty$  amount of 0 or 01's following the "11".

This makes sure the "11" substring is always padded by a 0 on either end, and allows for any amount of solo 1's. The right side is any string without "11" as substring, collection of 0's with a stray 1 sometimes.

$$3) b) 1^*(0^*11^*)^*0^*1^*$$

Prevent string "010" with parentheses portion since it allows 0 to only be followed by a "11" or, on the outside, by another 0. The left most 1 serves all strings that start with 1's & right most 1 serves all strings that end with 1's.

$$4) a) S \rightarrow aA \mid a \mid B \\ A \rightarrow aB \mid \lambda \\ B \rightarrow Aa$$

$$b) S \rightarrow aA \mid a \mid B \\ A \rightarrow aB \\ B \rightarrow Aa \mid a$$

$$c) S \rightarrow aA \mid a \mid Aa \\ A \rightarrow aB \\ B \rightarrow Aa \mid a$$

$$5) S \rightarrow AB \mid BA \\ A \rightarrow aA \mid a \\ B \rightarrow bB \mid b$$

$$L = (0^n 1^n \mid n \geq 0)$$

initial state S

FA : two final states

Transition:

S to A	0	S to B	1
A to A	0	A to B	1
B to A	0	B to B	1