

Characteristics of Matched Filter Receiver

The impulse response of the matched filter resembles the mirror image of the received waveform. The impulse response of a matched filter is the inverse Fourier transform of the frequency response function. It is given by,

$$h(t) = \int_{-\infty}^{\infty} H(f) \exp(j2\pi ft) df \quad \dots (1)$$

It is also defined as the output of the filter as a function of time, when the input is an impulse i.e.,

$$h(t) = G_a \int_{-\infty}^{\infty} S^*(f) \exp(-j2\pi f(t_1 - t)) df \quad \dots (2)$$

Where,

$S^*(f)$ – Complex conjugate of $S(f)$

t_1 – Fixed value of time at which a signal is observed to be maximum

G_a – A constant, equal to maximum filter gain.

But,

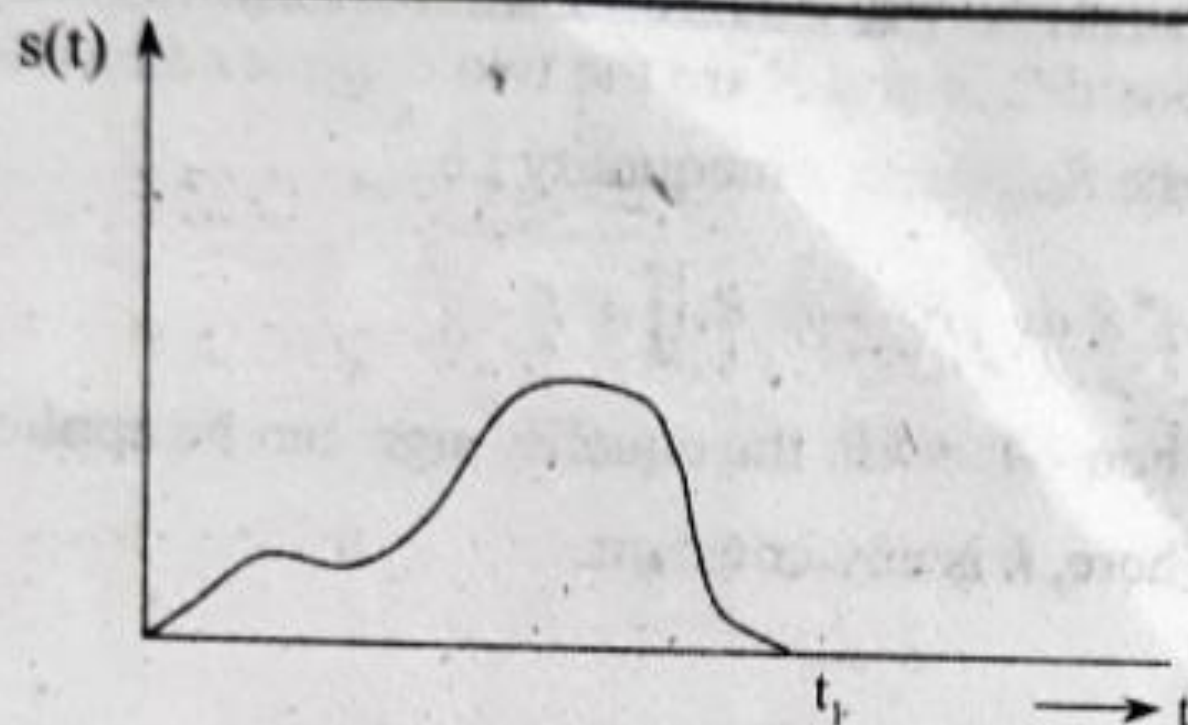
$$S^*(f) = S(-f)$$

So, equation (2) can be written as,

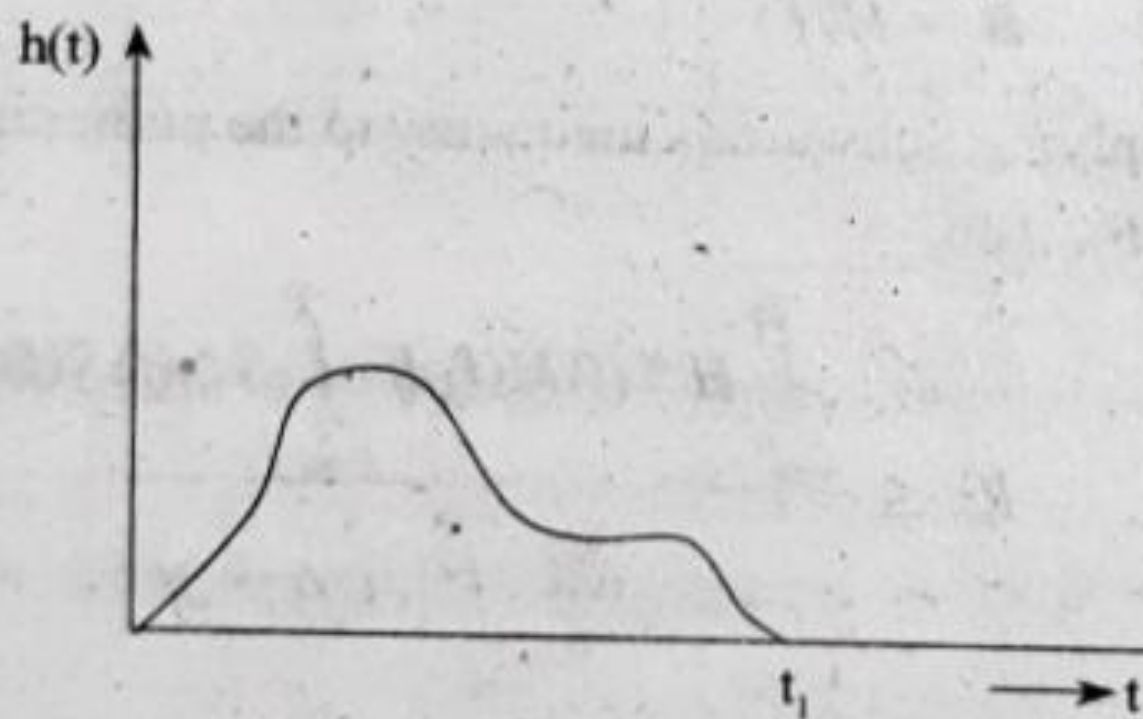
$$h(t) = G_a \int_{-\infty}^{\infty} S(f) \exp [j2\pi f(t_1 - t)] df$$

$$h(t) = G_a s(t_1 - t)$$

The impulse response of a matched filter is not defined for $t < 0$. Figure below illustrates the impulse response for a signal $s(t)$.



(a) Received Waveform $s(t)$



(b) Impulse Response $h(t)$

Figure

Expression for the F