

Activity Selection Problem

Ac-1

There are n different activity are given with their starting and ending time. Select maximum number of activity to solve by a single person.

1- Sort the activity with their ending time.

2- Find compatible activity and add to list.

$$\begin{array}{l} \downarrow \quad \downarrow \\ n + n \log n \\ O(n \log n) \end{array}$$

Algorithm

Greedy - activity (s, f)

1- $n \leftarrow \text{length}(s)$

2- $A \leftarrow \{1\}$

3- $J \leftarrow 1$

4- for $i \leftarrow 2$ to n

5- do if $s_i \geq f_J$

6- then $A \leftarrow A \cup \{i\}$

7- $J \leftarrow i$

8- Return A

Question-1 Activity Selection Problem Example Ac-2

Start Time (s)	Finish Time (F)	Activity Name
5	9	A ₁
1	2	A ₂
3	4	A ₃
0	6	A ₄
5	7	A ₅
8	8	A ₆

Solution:

Step-1: Sort the given activities in ascending order according to their finishing time:

The table after we have sorted it:

Start Time (s)	Finish Time (F)	Activity Name
1	2	A ₂
3	4	A ₃
0	6	A ₄
5	7	A ₅
5	9	A ₁
8	9	A ₆

Step 2: Select the First activity from Sorted Array ^{Ac-3}
 $act[]$ and add it to the $sol[]$ array,
thus $sol = \{A_2\}$

Step 3: Repeat step 4 and 5 for the remaining activities in $act[]$

Step 4: If the ~~Next~~ start time of the currently selected activity is greater than or equal to the finish time of the previously selected activity, then add it to $sol[]$

Step 5: Select the next activity in $act[]$

For the data given in the above Table,

[A] Select activity A_3 . Since the start time of A_3 is greater than the finish time of A_2 i.e. $[S(A_3) > F(A_2)]$

We add A_3 to the Solution set.

Thus $sol = \{A_2, A_3\}$

[B] Select A_4 . Since $[S(A_4) < F(A_3)]$, it is not added to the Solution set.

[C] Select A_5 . Since $[S(A_5) > F(A_3)]$, A_5 gets added to the Solution set.

Thus $sol = \{A_2, A_3, A_5\}$

AC-4
[D] Select A1, Since $S(A1) < F(A5)$, A1 is not added to the solution set

[E] Select A6, A6 is added to the solution set since $S(A6) > F(A5)$.

Thus Sol = { A2, A3, A5, A6 }

Step 6: At last, print the array sol[]

Hence, the ~~max~~ execution schedule of maximum number of non-conflicting activities will be:

(1, 2) (3, 4) (5, 7) (8, 9)

