

Practical No.1

Basics of R software

- 1) R is a software for data analysis and statistical computing.
- 2) This software is used for effective data handling ad output storage is possible
- 3) It is capable of graphical display
- 4) It is a free software

Q1 $2^2 + \sqrt{25} + 35$

> $(2^{*}2) + \text{sqrt}(25) + 35$

[1] 44

Q2 $2 \times 5 \times 3 + 62 \div 5 + \sqrt{49}$

> $2 * 5 * 3 + (62 / 5) + \text{sqrt}(49)$

= 49.4

Q3 $\sqrt{76 + 4 \times 2 + 9 \div 5}$

> $\text{sqrt}(76 + (4 * 2) + (9 / 5)) = 9.262829$

Q4 $42 + |-10| + 7^2 + 3 \times 9$

> $42 + \text{abs}(-10) + (7^{**2}) + 3 \times 9$

= 128

$$Q2) x = 20$$

$$y = 80$$

find $x+y$; x^2+y^2 , $\sqrt{y^2-x^2}$, $|x-y|$

$$x+y$$

50

$$x^2+y^2$$

1300

$$\sqrt{y^2-x^2}$$

137.8405

$$|x-y|$$

10

$$Q2 \quad C(2,3,4,5)^2$$

4 9 16 25

$$C(4,5,6,8)^3$$

12 15 18 24

$$C(2,3,5,7) * C(-2,-3,-5,-4)$$

-4 -9 -25 -28

$$C(2,3,5,7) * C(8,9)$$

16 27 40 63

$c(1, 2, 3, 4, 5) \wedge c(2, 3, 7)$

Error

$c(1, 2, 3, 4, 5, 6) \wedge c(2, 3)$

1	8	9	64	25	216
1^2	2^3	3^2	4^3	5^2	6^3

Q4 find the sum, product, maximum, minimum of the values
 $5, 8, 6, 7, 9, 10, 15, 5$

> $x = c(5, 8, 6, 7, 9, 10, 15, 5)$

> length(x)

8

> sum(x)

65

> prod(x)

11346000

> max(x)

15

> min(x)

5

> $x \leftarrow \text{matrix}(\text{rows}=4, \text{ncol}=2, \text{data} = c(1, 2, 3, 4, 5, 6, 7, 8))$

> $x[, 1] [, 2]$

[1,]	1	5
[2,]	2	6
[3,]	3	7
[4,]	4	8

$$86 \quad x = \begin{bmatrix} 1 & 4 & 7 \\ 2 & 5 & 8 \\ 3 & 6 & 9 \end{bmatrix}$$

$$y = \begin{bmatrix} 2 & 4 & 10 \\ -2 & 8 & -11 \\ 10 & 6 & 12 \end{bmatrix}$$

> x<-matrix (nrow=3, ncol=3, data = c(1,2,3,4,5,6,8,9))

> y<-matrix (nrow=3, ncol=3, data = c(2,-2,10,4,6,16,10,

> x+y

$$\begin{bmatrix} [1] & [2] & [3] \\ [1] & 3 & 8 & 17 \\ [2] & 0 & 13 & -3 \\ [3] & 13 & 12 & 21 \end{bmatrix}$$

> x*y

$$\begin{bmatrix} [1] & [2] & [3] \\ [1] & 2 & 16 & 70 \\ [2] & -4 & 40 & -88 \\ [3] & 150 & 36 & 108 \end{bmatrix}$$

> x*2 + y*3

$$\begin{bmatrix} [1] & [2] & [3] \\ [1] & 8 & 20 & 44 \\ [2] & -2 & 34 & -17 \\ [3] & 36 & 30 & 54 \end{bmatrix}$$

> $x \leftarrow c(2, 4, 6, 1, 3, 5, 7, 18, 16, 14, 17, 19, 3, 3, 2, 5, 0, 15, 9, 14, 18, 10, 12)$

> length(x)

[1] 23

> a = table(x)

> a

x

0	1	2	3	4	5	6	7	8	10	12	14	15	16	17	18	19
1	1	2	3	1	2	1	1	1	1	1	2	1	1	1	2	1

> transform

[1] x	freq
0	1
1	1
2	2
3	3
4	1
5	1
6	2
7	1
9	1
10	1
12	1
14	2
15	1
16	1
17	1
18	2
19	1

Practical No. 2

P.d.f and c.d.f.

Can the following be p.d.f?

$$\text{i) } f(x) = \begin{cases} 2-x & ; 1 \leq x \leq 2 \\ 0 & \text{o.w} \end{cases}$$

$$\Rightarrow \int_1^2 (2-x) dx$$

$$\Rightarrow \int_1^2 2dx - \int_1^2 x dx$$

$$= 2x \Big|_1^2 - \frac{x^2}{2} \Big|_1^2$$

$$= (4-2) - (2-0.5)$$

$$\neq 1$$

Not a p.d.f

$$\text{ii) } f(x) = \begin{cases} 3x^2 & , 0 < x < 1 \\ 0 & \text{o.w} \end{cases}$$

$$\int \frac{\partial x^3}{\partial}$$

$$= x^3 \Big|_0^1$$

58.

$$= 1$$

It is a p.d.f.

$$\text{(ii)} \quad f(x) = \begin{cases} \frac{3x}{2} (1 - \frac{x}{2}) & ; 0 \leq x \leq 2 \\ 0 & \text{otherwise} \end{cases}$$

[1]

$$\int_0^3 \left(\frac{3x}{2} - \frac{3x^2}{4} \right) dx$$

$$= \frac{3}{2} \int_0^2 x dx - \frac{3}{4} \int_0^2 x^2 dx$$

$$= \frac{3}{2} \left[\frac{x^2}{2} \right]_0^2 - \frac{1}{4} \left[x^3 \right]_0^2$$

$$= \frac{3}{4} [x^2]_0^2 - \frac{1}{4} [x^3]_0^2$$

$$= \frac{3}{4} [4] - \frac{1}{4} [8]$$

$$= 1$$

It is a p.d.f.

Q2 Can the following be pmf?

(i)	x	1	2	3	4	5
	$p(x)$	0.2	0.3	-0.1	0.5	0.1

Since one probability is negative it is not pmf.

(ii)	x	0	1	2	3	4	5
	$p(x)$	0.1	0.3	0.2	0.2	0.1	0.1

Since $p(x) > 0 \ \forall x$
 $\sum p(x) = 1$

It is a pmf.

(iii)	x	10	20	30	40	50
	$p(x)$	0.2	0.3	0.3	0.2	0.2

Since $p(x) \rightarrow 0 \ \forall x$

$\sum p(x) \neq 1$

\therefore It is not a pmf.

Find $P(x \leq 2)$, $P(2 \leq x < 4)$, $P(\text{at least } 4)$, $P(3 \leq x \leq 6)$

x	0	1	2	3	4	5	6
	0.1	0.1	0.2	0.2	0.1	0.2	0.1

$$\rightarrow P(x < 2)$$

$$P(0) + P(1) + P(2)$$

$$0.1 + 0.1 + 0.2$$

$$0.4$$

$$P(2 \leq x \leq 4)$$

$$P(2) + P(3)$$

$$0.2 + 0.2$$

$$0.4$$

$$P(\text{at least } 4)$$

$$P(4) + P(5) + P(6)$$

$$= 0.1 + 0.2 + 0.1$$

$$= 0.4$$

$$P(3 < x < 6)$$

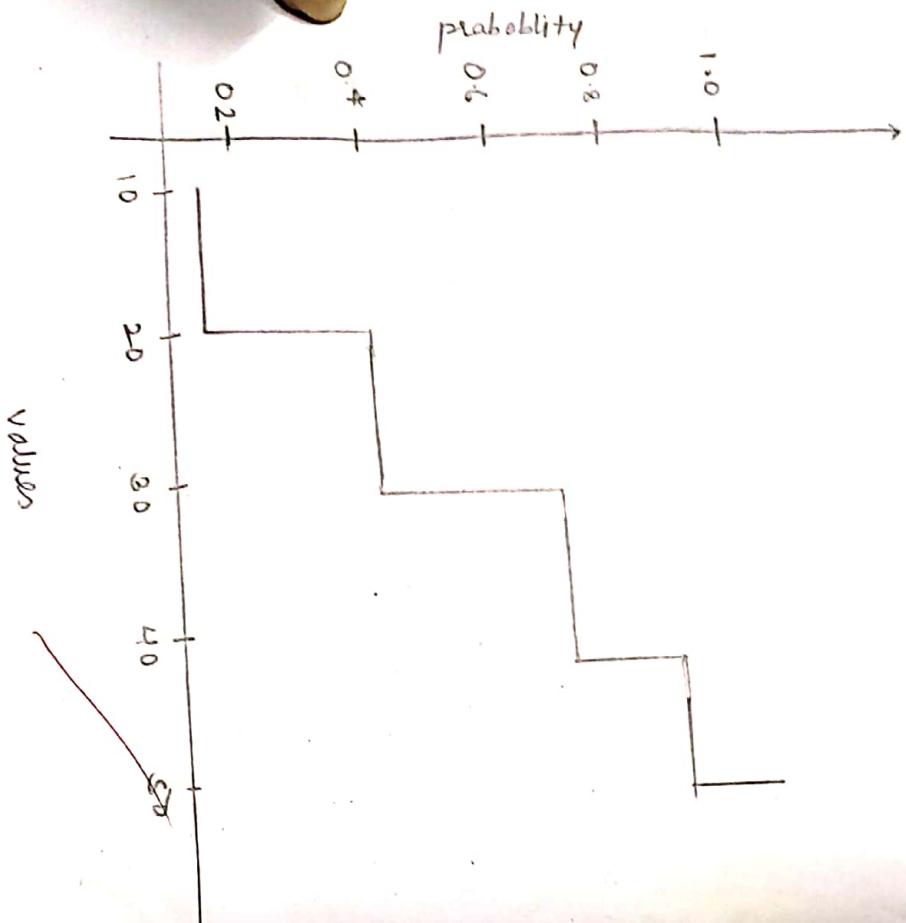
$$P(4) + P(5)$$

$$= 0.1 + 0.2$$

$$= 0.3$$

Practical 3 Probability Distribution

Graph of cdf



find c.d.f of the following p.m.b draw the graph

$$\begin{array}{ll}
 x: & 10 \quad 20 \quad 30 \quad 40 \quad 50 \\
 p(x) & 0.25 \quad 0.25 \quad 0.3 \quad 0.2 \quad 0.1
 \end{array}$$

$$\begin{aligned}
 b(x) = & 0 & x < 10 \\
 & 0.15 & 10 \leq x < 20 \\
 & 0.40 & 20 \leq x < 30 \\
 & 0.70 & 30 \leq x < 40 \\
 & 0.90 & 40 \leq x < 50 \\
 & 1.0 & x \geq 50
 \end{aligned}$$

$> x = c(10, 20, 30, 40, 50)$

$> prob = c(0.15, 0.25, 0.3, 0.2, 0.1)$

$> cumsum(prob)$

$[1] 0.15 \quad 0.40 \quad 0.70 \quad 0.90 \quad 1.00$

$> plot(x, cumsum(prob), xlab = "values", ylab = "probability",$

$\text{main} = "graph of cdf", "s")$

Binomial Distribution

- Q2 Suppose there are 12 mcq in a test each question has 5 option & only one of them is correct. Find the probability of having
(1) 5 correct answer (2) Atmost 4 correct

Given that

$$n=12, p=1/5, q=4/5$$

x = Total no. of correct answer

$$x \sim B(n, p)$$

$$n=12, p=1/5, q=4/5, x=15+2 \leq n$$

$$> n=12; p=1/5; q=4/5; x=5$$

$$> \text{sum}(n, p, q, x)$$

[1] 18

$$> \text{dbinom}(5, 12, 1/5)$$

[1] 0.65315022

$$> \text{pbinom}(14, 12, 1/5)$$

[1] 0.9274445

Q3

There are 10 members in committee, the probability of any member attending a meeting is 0.9. find the probability

- 1) 7 members attended
- 2) At least 5 members attended
- 3) At most 6 members attended.

→ Given that

$$n = 10, p = 0.9, q = 0.1$$

x = Total no. of members attended

$$x \sim B(n, p)$$

$$n = 10, p = 0.9, q = 0.1$$

$$n = 10; p = 0.9, q = 0.1$$

dbinom(7, 10, 0.9)

[1] 60573953

$$1 - \text{pbinom}(4, 10, 0.9)$$

[1] ~~0.998865~~ 999853

$$> \text{pbinom}(6, 10, 0.9)$$

[1] 0.0127952

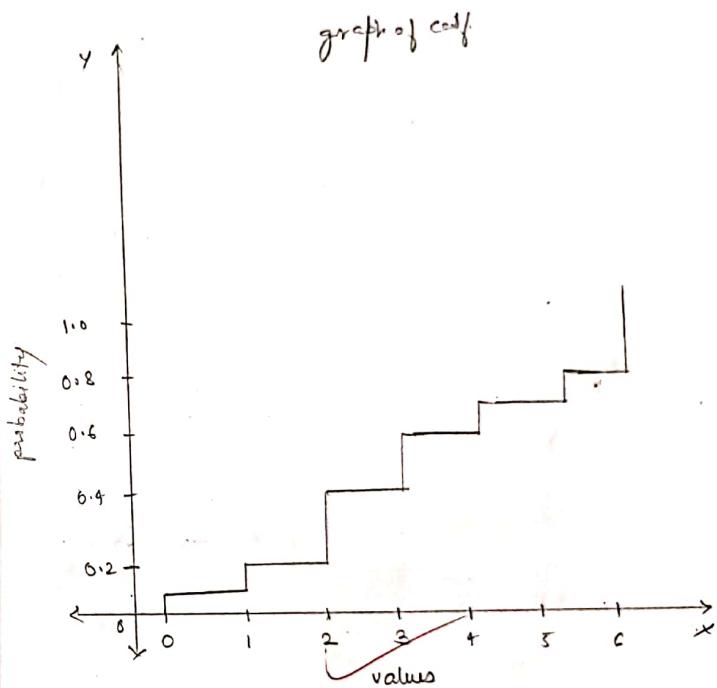
Find the cdf & draw the graph

x	0	1	2	3	4	5	6
$p(x)$	0.1	0.1	0.2	0.2	0.1	0.2	0.1

```

> x=c(0,1,2,3,4,5,6)
> prob=c(0.1,0.2,0.1,0.2,0.1,0.2,0.2)
> cumsum(prob)
> [1] 0.1 0.2 0.4 0.6 0.7 0.8 1.0
> plot(x,cumsum(prob),xlab="values", ylab="probability",
main="graph of cdf", "s")

```



AM
1/12/09

Practical 4

Binomial Distribution

45.

1. Find the complete binomial distribution where $n=5$ & $p=0.1$
2. Find the probability of exactly 10 success in 100 trials where $p=0.1$
3. X follows binomial distribution with $n=12$, $p=0.25$
(i) $P(X=5)$
(ii) $P(X \leq 5)$
(iii) $P(X > 7)$
(iv) $P(8 < X < 7)$
- 4) The probability of a salesman makes a sale to a customer is 0.15. Find the probability
(i) No Sale for 10 customer
(ii) More than 3 sale to 20 customer
- 5) A student writes 5 mcq's. Each question has 4 options out of which one is correct. Calculate the probability of atleast 3 correct answer.
- 6) X follows binomial distribution with $n=10$, $p=0.4$.
Plot the graph of pmf & cd.f.

* Note:

$$P(x=x) = \text{dbinom}(x, n, p)$$

$$P(x \leq x) = \text{pbinom}(x, n, p)$$

$$P(x > x) = 1 - \text{pbinom}(x, n, p)$$

To find the value of x for which the probability is given as p , command is qbinom
 $\Rightarrow \text{qbinom}(p, n, p)$

Answer:

1) $n=5, p=0.1$

$$\text{dbinom}(0:5, 5, 0.1)$$

[1] 0.59049 0.32805 0.7290 0.00810 0.00045 0.00001

2) $x=10, n=100, p=0.1$

$$\text{dbinom}(10, 100, 0.1)$$

[1] 0.1318653

3) (1) $n=12, p=0.25$

$$P(X=5) = \text{dbinom}(5, 12, 0.25)$$

$$> \text{dbinom}(5, 12, 0.25)$$

[1] 0.1082414

i) $P(X \leq 5) = \text{pbinom}(x, n, p)$
 $> \text{pbinom}(5, 12, 0.25)$
[1] 0.9455978

ii) $P(5 < X < 7) = \text{dbinom}(x, n, p)$
 $> \text{dbinom}(6, 12, 0.25)$
[1] 0.04014945

iii) $P(X > 7)$
 $= 1 - P(X \leq 7)$
 $> 1 - \text{pbinom}(7, 12, 0.25)$
[1] 0.0278157

iv) $p = 0.15$
(i) $n = 10, p = 0.15, x = 6$
 $> \text{dbinom}(0, 10, 0.15)$
[1] 0.1968794

v) $p = 0.15, n = 20$
 $P(X > 3) = 1 - P(X \leq 3)$
 $> 1 - \text{pbinom}(3, 20, 0.15)$
[1] 0.3522748

5) $n = 5, p = 1/4$

$$P(X \geq 3)$$

$$1 - P(X \leq 2)$$

$$> 1 - pbinom(3, 5, 1/4)$$

$$[1] 0.15625$$

c) $n = 10, p = 0.4$

$$x = 0:n$$

$$\text{prob} = \text{dbinom}(x, n, p)$$

$$\text{cumprob} = \text{pbinom}(x, n, p)$$

`d = data.frame ("xvalues" = x, "probability" = prob)`

`print(d)`

`> prob = dbinom(0:10, 10, 0.4)`

`> prob`

`> cumprob = pbinom(0:10, 10, 0.4)`

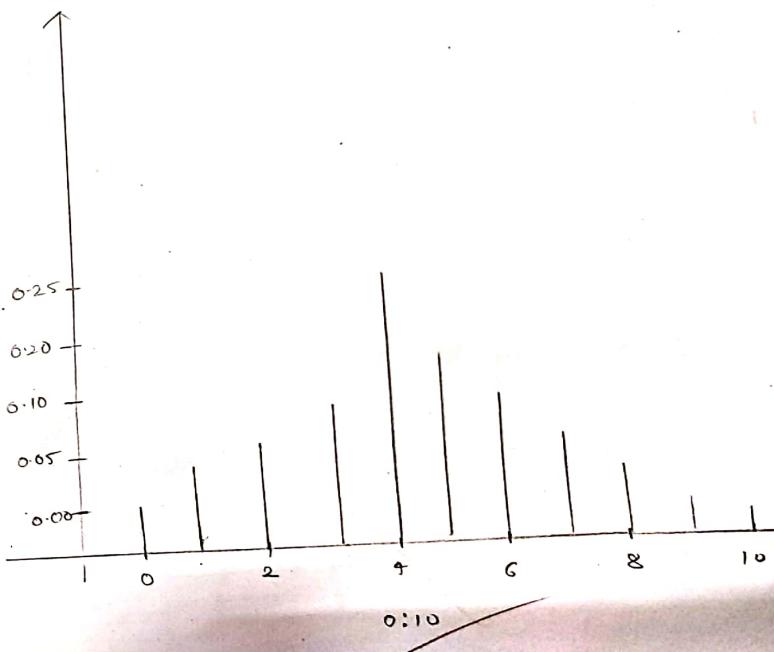
`> cumprob`

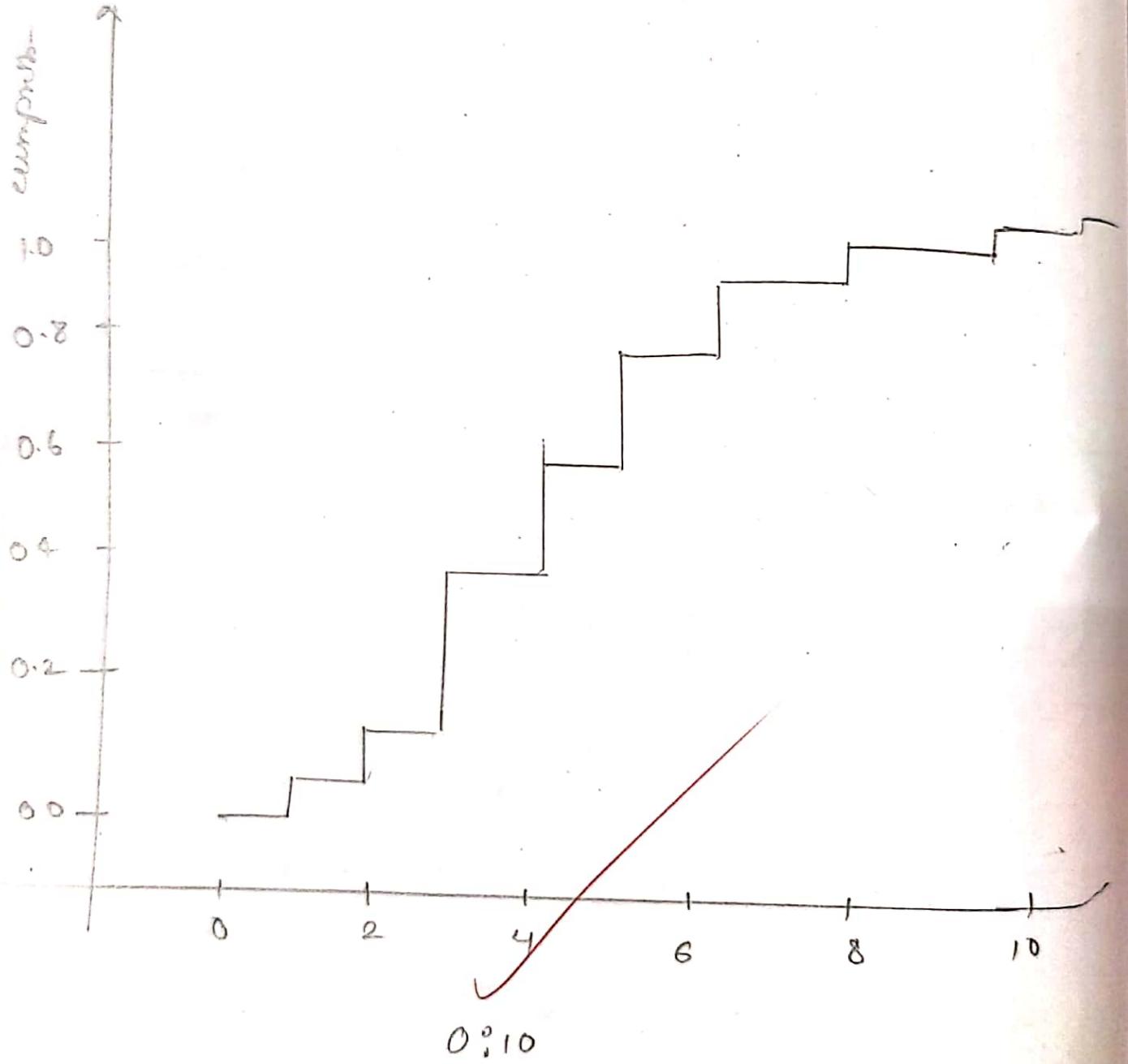
`> d = data.frame ("xvalues" = 0:10, "probability" = b)`

`> print(d)`

`> plot(0:10, prob, "h")`

`> plot(0:10, cumprob, "b")`





0.10
18.2.9

Practical No. 5

Normal Distribution

* NOTE

$$P(x - \bar{x}) = \text{denom} (\bar{x}, \mu, \sigma)$$

$$P(x \leq \bar{x}) = \text{pnorm} (\bar{x}, \mu, \sigma)$$

$$P(x > \bar{x}) = 1 - \text{pnorm} (\bar{x}, \mu, \sigma)$$

$$P(x_1 < x < x_2) = \text{pnorm} (x_2, \mu, \sigma) - \text{pnorm} (x_1, \mu, \sigma)$$

To find the values of k so that

$$P(X \leq k) = P ; \text{ qnorm}(p, \mu, \sigma)$$

To generate n random no of the command is $rnorm(n, \mu, \sigma)$

1] $X \sim N(\mu = 50, \sigma^2 = 100)$

Find (i) $P(X \leq 40)$

(ii) $P(X > 55)$

(iii) $P(42 \leq X \leq 60)$

(iv) $P(X \leq k) = 0.7, k = ?$

2] $X \sim N(\mu = 100, \sigma^2 = 36)$

(i) $P(X \leq 116)$

(ii) $P(X \leq 95)$

(iii) $P(X > 115)$

(iv) $P(95 \leq X \leq 105)$

v) $P(X \leq k) = 0.7 \Rightarrow k = ?$

3) Generate 10 random no from a normal distribution with mean ($\mu = 60$) & S.D ($\sigma = 5$)

Also calculate the sample median, mean, variance & standard deviation.

4) Draw the graph of standard normal distribution.

Answers:

$$[1] (i) >a = \text{pnorm}(40, 50, 10)$$

cat ("P(X ≤ 40) is ", a)

$$[1] 0.1586583$$

$$(ii) >b = 1 - \text{pnorm}(55, 50, 10)$$

cat ("P(X > 55) is ", b)

$$[1] 0.3085375$$

$$(iii) >c = \text{pnorm}(60, 50, 10) - \text{pnorm}(42, 50, 10)$$

$$[1] 0.6294893$$

$$(iv) >d = \text{qnorm}(0.7, 50, 10)$$

cat ("P(X ≤ d) = 0.7, k is ", d)

$$[1]$$

$$2) >a = \text{pnorm}(110, 100, 6)$$

$$[1] 0.9522096$$

$$(ii) >b = \text{pnorm}(95, 100, 6)$$

$$[1] 0.2028284$$

$$(iii) >c = 1 - \text{pnorm}(115, 100, 6)$$

$$[1] 0.00620965$$

18:

iv) $d = \text{pnorm}(105, 100, 6) - \text{pnorm}(95, 100, 6)$
[1] 0.5953432

v) $e = \text{qnorm}(0.1, 100, 6)$
[1] 98.47992

[3] $n=10, \mu=60, \sigma=5$
 $x = \text{rnorm}(10, 60, 5)$

[1] 64.36801 56.28557 51.12444 62.66236 57.07212 52.90557
63.04319 59.3558 59.98091 57.45464

> am = mean(x)

> am

[1] 58.30124

> me = median(x)

> me

[1] 58.22385

> n = 10

> Variance = (n-1) * var(x)/n

> variance

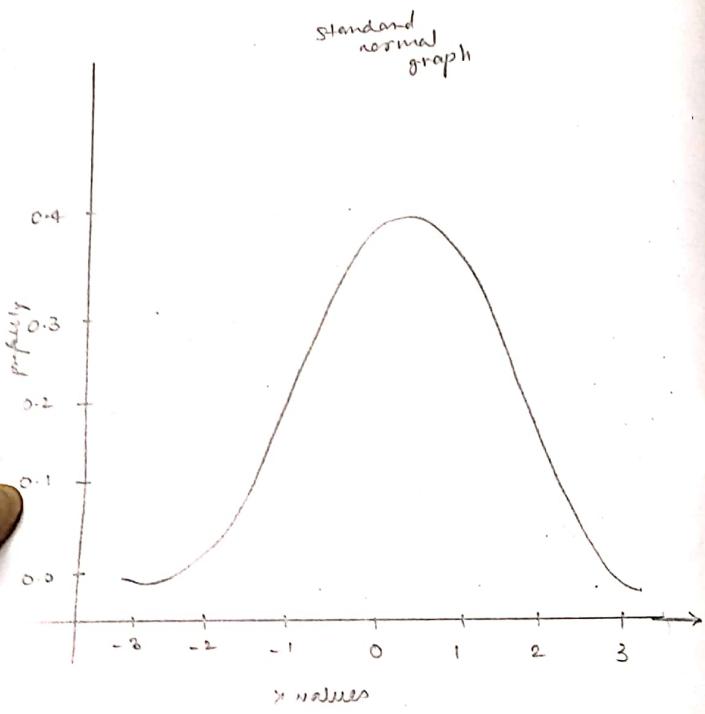
[1] 17.05339

> sd = sqrt(variance)

> sd

[1] 4.129575

25



53

```
>x = seq(-3,3,by=0.1)
```

```
>y = dnorm(x)
```

```
>y
```

```
>plot(x,y,xlab="xvalues",ylab="probability",main="standard normal graph")
```

~~PM
2-1.70~~

X Distribution

- 1) Test the hypothesis (H_0) $H_0: \mu = 10$ against $H_1: \mu \neq 10$. A sample of size 400 is selected which gives the mean 10.2 & standard deviation 2.25. Test the hypothesis at 5% level of significance.

> $m_0 = 10$, $m_x = 10.2$

> $m_0 = 10$; $m_x = 10.2$; $sd = 2.25$; $n = 400$

> $z_{\text{cal}} = (m_x - m_0) / (sd / \sqrt{n})$

[1] 1.7778

> cat("zcal is", " $=$ ", zcal)

[1] zcal is = 1.7778

> pvalue = 2 * (1 - pnorm(abs(zcal)))

> pvalue

[1] 0.07549036

\therefore The answer is more than 0.05, the value of the ~~H_0~~ is accepted

- 2) Test the hypothesis: $H_0: \mu = 75$ against $H_1: \mu \neq 75$. A sample of size 100 is selected and sample mean is 80 with standard deviation of 3. Test the hypothesis at 8% level of significance.

> $m_0 = 75$, $m_x = 80$, $sd = 3$, $n = 100$

> $z_{\text{cal}} = (m_x - m_0) / (sd / \sqrt{n})$

> zcal

[1] 16.6667

> cat ("zcal is = ", zcal)

zcal is = 16.667

> pvalue = 2 * (1 - pnorm (abs (zcal)))

> pvalue

[1]

since, the value is less than 0.05, the value of H_0 is rejected.

3) Test the hypothesis $H_0: \mu = 25$ $H_1: \mu < 25$ at 5% level of

significance. Following sample of 30 is selected

20, 24, 27, 35, 30, 46, 26, 27, 10, 20, 30, 37, 35, 21, 22, 23

24, 25, 26, 27, 28, 29, 30, 39, 27, 15, 19, 22, 20, 18.

> x = c(20, 24, 27, 35, 30, 46, 26, 27, 10, 20, 30, 37, 35, 21, 22, 23, 24, 25,

26, 27, 28, 29, 30, 39, 27, 15, 19, 22, 20, 18)

> x

> mx = mean(x)

> mx

[1] 26.0667

> n = length(x)

> n

[1] 30

> variance = (n-1) * var(x) / n

> variance

[1] 52.91556

> sd = sqrt(variance)

> sd

[1] 7.279805

88

```
> mo=25; mx=26.07; sd=7.28; n=50  
> zcal = (mx-mo) / (sd / (sqrt(n)))  
> zcal  
[1] 0.8050318  
> cat("zcal is ", " ", zcal)  
[1] zcal is 0.8050318  
> pvalue = 2 * (1 - pnorm (abs(zcal)))  
> pvalue  
[1] 0.4208013
```

\therefore The value is more than 0.05, the value of H_0 is accepted.

3) Experience has shown that 20% students of our college smoke. A sample of 400 students reveal that out of 400 only 50 smoke. Test hypothesis that the experience gives the correct proportion.

```
> P=0.2  
> Q=1-P  
> P=50/400  
> n=400  
> zcal = (P - p) / sqrt (P * Q / n)  
> zcal  
[1] -3.75  
> pvalue = 2 * (1 - pnorm (abs(zcal)))  
> pvalue  
[1] 0.001768376
```

Value of α is less than 0.5, therefore H_0 is rejected

s) Test the hypothesis $H_0: p=0.5$ against $H_1: p \neq 0.5$. Sample of 200 is selected & the proportion is calculated 0.58. Test the hypothesis at 1% level of significance.

> $p = 0.5$

> $p = 0.5$

> $q = 1 - p$

> $n = 200$

> $z_{\text{cal}} = (p - P) / \sqrt{P * q / n}$

> z_{cal}

[1] 1.697056

> $p\text{value} = 2 * (1 - \text{pnorm}(\text{abs}(z_{\text{cal}})))$

> $p\text{value}$

[1] 0.08968602

Value of α is more than ≈ 0.1 , therefore H_0 is accepted

AM
22-01-20

Large Sample Tests

A study of noise level in 2 hospital is calculated below to test the hypothesis that the noise level into hospital are same or not.

	Hos A	Hos B
No. of sample	84	34
mean	61	59
S.D	7	8

H_0 : The noise levels are same

$$n_1 = 84$$

$$n_2 = 34$$

$$m_x = 61$$

$$m_y = 59$$

$$s_{dx} = 7$$

$$s_{dy} = 8$$

$$> z = (m_x - m_y) / \sqrt{(s_{dx}^2/n_1) + (s_{dy}^2/n_2)}$$

> z

$$[1] 1.229059$$

> cat ("z calculated is = ", z)

z calculated is - 1.229059 > pvalue = 2 * (1 - pnorm (abs(z)))

> pvalue

$$[1] 0.04550026$$

∴ since pvalue is 0.0455, we reject H_0 at 5% level of significance.

2) 2 random sample of size 1000 & 2000 are drawn from 2 population with a mean 67.5 & 68 respectively & with the same sd of 2.5. Test the hypothesis that the mean of 2 population are equal.

$$H_0: \text{2 populations are equal}$$

$$n_1 = 1000$$

$$n_2 = 2000$$

$$\bar{x}_1 = 67.5$$

$$\bar{x}_2 = 68$$

$$s_{\bar{x}_1} = 2.5$$

$$s_{\bar{x}_2} = 2.5$$

$$> z = (\bar{x}_2 - \bar{x}_1) / \sqrt{(s_{\bar{x}_1}^2 / n_1) + (s_{\bar{x}_2}^2 / n_2)}$$

> z

$$[1] -5.163978$$

> cat("z calculated is = ", z)

$$z \text{ calculated is } = -5.163978$$

> pvalue = 2 * (1 - pnorm (abs(z)))

> pvalue

$$[1] 2.417564e-07$$

since pvalue is $2.417564e-07$, we reject H_0 at 5% level of significance.

Q3

- 3) In a first year class (F4BSC), 20% of a random sample of 400 students had defective eye sight. In a class, 15.5% of 500 sample had the same defect. Is the difference of proportion is same.

$$n_1 = 400$$

$$n_2 = 500$$

$$p_1 = 0.2$$

$$p_2 = 0.155$$

$$p = (n_1 * p_1 + n_2 * p_2) / (n_1 + n_2)$$

$$> p$$

$$[1] 0.175$$

$$> q = 1 - p$$

$$> q$$

$$0.825$$

$$> z = (p_1 - p_2) / \sqrt{p * q * (1/n_1 + 1/n_2)}$$

$$> z$$

$$[1] 1.76547$$

$$> cat ("z calculated is = ", z)$$

$$[1] z calculated is 1.76547$$

$$> pvalue = 2 * (1 - pnorm (abs(z)))$$

$$> pvalue$$

$$[1] 0.07748487$$

Since pvalue is 0.077, we ~~reject~~ at 5% level of significance.

4) From each of the box of apples, a sample size of 200 is collected. It is found that there are 44 bad apples in 1st sample & 30 bad apples in 2nd sample. Test the hypothesis that 2 boxes are equivalent in term of no. of bad apples.

H_0 = The proportion of boxes is same.

$$n_1 = 200$$

$$n_2 = 200$$

$$p_1 = 44/200$$

$$p_2 = 30/200$$

$$\geq p = (n_1 * p_1 + n_2 * p_2) / (n_1 + n_2)$$

$$\geq p$$

$$[1] 0.185$$

$$\geq q = 1 - p$$

$$\geq q$$

$$[1] 0.815$$

$$\geq z = (p_1 - p_2) / \sqrt{p_1 * q_1 * (1/n_1 + 1/n_2)}$$

$$\geq z$$

$$[1] 1.8027$$

$\geq \text{cat} ("z \text{ calculated is } = ", z)$

calculated is 1.8027

$$\geq \text{pvalue.} = 2 * (1 - \text{pnorm}(\text{abs}(z)))$$

$$\geq \text{pvalue}$$

$$[1] 0.0714$$

Since pvalue is 0.0714, we ~~reject~~^{accept} at 5% level of significance.

Q. In a MA class, out of sample of 60, mean height is 63.5 inch with a SD 2.5. In a Mcom class, out of 50 student mean height 69.5 inch with SD of 2.5. Test the hypothesis, that the mean of MA & Mcom are same.

for the mean height of MA & Mcom student are equal.

$$n_1 = 60$$

$$n_2 = 50$$

$$m_x = 63.5$$

$$m_y = 69.5$$

$$sdx = 2.5$$

$$sdy = 2.5$$

$$> z = (m_x - m_y) / \sqrt{((sdx^2/n_1) + (sdy^2/n_2))}$$

> z

$$(1) = 12.53359$$

> cat(*z (calculated is 1, 2))

z calculated is ~ -12.53359

> pvalue = 2 * (1 - pnorm (abs (2)))

> pvalue

$$(1) 0.04550026$$

since pvalue is 0.04550026 is, we reject H₀ at 5% of level of significance.

An
5.2.20

Small Sample Test-

Q1) Two tons are selected & height are found to be 63, 68, 69, 71, 72 cms. Test hypothesis that mean height are 66 cm or not at 1%

$$\text{no. of mean} = 66 \text{ cm.}$$

$$\Rightarrow \text{mean} = 66$$

$$\Rightarrow x = c(63, 63, 68, 69, 71, 71, 72)$$

$$\Rightarrow t\text{-test}(x)$$

one Sample t-test

data : x

$$t = 47.94, df = 6, pvalue = 5.22 - 0.9$$

alternative hypothesis: true mean is not equal to 69.95 percent confidence interval.

$$64.66479 \quad 71.62092$$

Sample estimates

mean estimate of x

$$68.14286$$

\therefore pvalue < 0.01 is rejected on the 1% level of significance

2) Two random sample was drawn from two different population

$$\text{Sample 1} = 8, 10, 12, 11, 16, 15, 18, 7$$

$$\text{Sample 2} = 20, 15, 18, 9, 8, 10, 11, 12$$

Test the hypothesis that there is no difference between the population mean at 5% los.

$\therefore H_0$ There is no difference in the population mean.

Q3.

```
> x = c(8, 10, 12, 11, 16, 15, 18, 7)
> y = c(20, 15, 18, 9, 8, 10, 11, 12)
> t.test(x, y)
```

welch two sample t-test

data : x & y
 $t = -0.36247$, $df = 18.837$, $p\text{-value} = 0.7228$

alternative hypothesis: true difference in mean is not equal to 0

Sample estimates

mean of x mean of y
 12.125 12.875

$p\text{-value} < 0.01$ is accepted in the t-test on 1% level of significance

Q3 following or the weights of 10 people.

Before: (100, 125, 95, 96, 98, 102, 115, 109, 109, 110)

After: (95, 180, 95, 98, 90, 100, 110, 85, 100, 101)

H0: The Dist. program is not effective

```
> x = c(100, 125, 95, 96, 98, 102, 115, 109, 109, 110)
> y = c(95, 180, 95, 98, 90, 100, 110, 85, 100, 101)
> t.test(x, y, paired = T, alternative = "less")
```

Paired t-test

data : x & y

$t = -2.3215$, $df = 9$, $p\text{-value} = 0.9773$

alternative hypothesis: true difference in means is less than 0
 95 percent confidence interval
 -1.96 17.89635

Sample estimates:
 mean of the differences
 10

64

(a) Marks before & after a training program is given below

before: (20, 25, 32, 28, 27, 26, 35, 25)
 after: (30, 25, 32, 37, 37, 40, 40, 23)

Test the hypothesis that training program is effective or not

H0: The training program is not effective

```
> x = c()
> y = c()
> t.test(x, y, paired = T, alternative = "greater")
```

Paired t-test

data : x & y

$t = 3.3859$, $df = 7$, $p\text{-value} = 0.9942$

95 percent confidence interval
 -8.967899 14.6

Sample estimates:
 mean of the difference
 -5.75

(b) Two random samples were

Q5 Two random sample were drawn from two normal population
so the values are

A =

B =

Test whether the population have same variance at 5% level

of

H_0 : variance of the population are equal

$\rightarrow x = c(66, 67, 75, 76, 82, 84, 88, 90, 92)$

$\rightarrow y = c(64, 66, 74, 78, 82, 85, 87, 92, 93, 95, 97)$

$\rightarrow \text{var.test}(x | y)$

F-test to compare two variances

data: x ~ y

F = 0.70686, num df = 8, denom df = 10, p-value = 0.6359
alternative hypothesis: true ratio of variances is not equal
to 1 95 percent confidence interval:

0.1833662 8.036093

sample estimates:

ratio of variance

0.7068867

Q6) The AP of sample 100 observation is 52 if S.D is 7 test the hypothesis that the population mean is 55 or not at 5% level of significance.

H₀: population mean = 55

> n = 100

> m_x = 52

> m_o = 55

> gd = 7

? zcal = (m_x - m_o) / gd / sqrt(n)

> pvalue = 2 * (1 - pnorm(abs(zcal)))

> pvalue

[1] 1.82153e-05

Practical 9

67

chi square & ANOVA

use the following data to test whether the condition of the name depends upon the child condition or not.

		cond of home	
		clean	dirty
cond clean	fairly	70	80
	dirty	80	20

Dirty	35	45
-------	----	----

→ Ho condition of the name & child are independent

> $x = c(70, 80, 35, 80, 20, 45)$

> $m = 3$

> $n = 2$

> $y = \text{matrix}(x, \text{ncol} = m, \text{ncol} = n)$

	[1,1]	[1,2]
[1,]	70	50
[2,]	80	20
[3,]	35	45

> $pvalue = \text{chisq.test}(y)$

> $pvalue$

58

Pearson chi squared test

data: y
 χ^2 = squared = 25.646, df = 2, pvalue = 2.698e-06

pvalue is less than 0.05 we reject H_0 at 5%. L.O.S.

2. Table below show the relation between the performance of mathematics & computers of CS students

		maths				
		H9	M9	L9		
Comp	H9	56	71	12		
	M9	47	163	38		
L9	14	42	35			

H_0 : performance between maths & computer are independent

$$x = c(56, 47, 14, 71, 163, 42, 12, 38, 85)$$

$$m = 3$$

$$n = 3$$

y = matrix(x, nrow = m, ncol = n)

	[1,]	[2,]	[3,]
[1,]	56	71	12
[2,]	47	163	38
[3,]	14	42	85

Pearson's chi-square test

i) use the following data to
pvalue = chisq.test(y)

pvalue

data y

$$\chi^2 = 195.78, \text{ df} = 4, \text{ pvalue} < 2.2 \times 10^{-16}$$

ii) varieties desperation

A 50, 52

B 53, 55, 53

C 60, 58, 57, 56

D 52, 54, 59, 55

mean A, B, C, D

> x1 = c(50, 52)

> x2 = c(53, 55, 53)

> x3 = c(60, 58, 57, 56)

> x4 = c(52, 54, 59, 55)

> d = stack(list(b1 = x1, b2 = x2, b3 = x3, b4 = x4))

> oneway.list(values ~ ind, data = d, var.equal = T)

anova = anova(values ~ ind, data = d)

$F = 11.735$, num df = 3, denom df = 9, pvalue = 0.0183
 summary(anova).

	Df	sumsq	mean sq	F value	Pr (> F)
ind	3	71.06	23.688	11.73	0.00183
Residuals	9	18.17	2.019		

∴ Pvalue is less than 0.05 we reject H₀ at 5% LOS.

Q3.

Pearson's anova on the following table.

Types	Observation
A	6, 7, 8
B	4, 6, 5
C	8, 6, 10
D	6, 9, 9

a = c(6, 7, 8)

b = c(4, 6, 8)

c = c(8, 6, 10)

d = c(6, 9, 9)

d = stack

One way test (values mind, data = d, var.equal = T)

One way analysis of means

data = values n ind

F = 2.6607

, num df = 3, denom df = 8, pvalue = 0.1

* anova = aov (value ~ ind, data = d)

> anova

Call

aov (formula = values ~ ind, data = d)

Terms

ind

Residuals

sum of
square18
318
8

Residual standard error: 1.5

Estimated effects may be unbalanced

> summary (anova)

Df	sumsq	mean sq	Fvalue	pr(>F)
ind	18	6.00	2.667	0.119
residuals	8	1.8	2.25	

Since the p-value is greater than 0.05 we accept the hypothesis at 87.90%

15.

Practical - 10

Non parametric test

Following are the amounts of sulphur oxide
a factor

17, 15, 20, 29, 19, 18, 22, 25, 27, 9, 24, 20, 17, 6, 24, 14, 15, 23, 24,
26 apply sign test the hypothesis that the population
medium is 21.5 against the alternative is less than 21.5

H_0 : population median = 21.5

H_1 : It is less than 21.5

$$> x = c(17, 15, 20, 29, 19, 18, 22, 25, 27, 9, 24, 20, 17, 6, 24, 14, \\ 15, 23, 24, 26)$$

γx

[1] 17 15 20 29 19 18 22 25 27 9 24 20 17 6 24 14
15 23 24 26.

$$m = 21.5$$

$$sp = \text{length} [x > m]$$

$$sp = \text{length} (x < m)$$

$$\gamma n = sp + sn$$

[1] 20

$$> pv = \text{pbinom}(sp, n, 0.5)$$

$$[1] 0.4119015$$

If the alternative is greater than medium.

$$pv = \text{pbinom}(sn, n, 0.5)$$

- 2: For the observation $12, 19, 31, 28, 43, 40, 55, 49, 70, 63$, apply sign test to test population median is 25 against the alternative it is more than 25.

$\gt x = c(12, 19, 31, 28, 43, 40, 55, 49, 70, 63)$

$\gt m = 25$

$\gt sp = \text{length}(x[x > m])$

$\gt sn = \text{length}(x[x < m])$

$\gt n = sp + sn$

$\gt pv = \text{pbinom}(sn, n, 0.5)$

$\gt pv$

[1] 0.0596875

- 3: For the following

$60, 65, 63, 89, 61, 71, 58, 51, 48, 66$. Test the hypothesis using wilcoxon sign test. for tested the hypothesis that median is 60 against the alternative it is greater than 60.

H_0 : Median is 60.

H_1 : It is greater than 60.

$\gt x = c(60, 65, 63, 89, 61, 71, 58, 51, 48, 66)$

$\gt m = 60$

$\gt sp = \text{length}(x[x > m])$

$\gt sn = \text{length}(x[x < m])$

$\gt n = sp + sn$

$\gt pv = \text{pbisom}(sn, n, 0.5)$

[1] 0.2539063

45

$v = 29$, pvalue = 0.2886

Note: If the alternative is less, wilcox.test(x, alter= "greater", mu = 60)

If the alternative is not equal to wilcox.test(x, alter= "2 sided", mu = 60)

4. Use wilcoxon sign test the hypothesis where median is 12 against the alternative is less than 12

12, 13, 10, 20, 15, 5, 1, 7, 6, 11, 9, 20

$x = c(12, 13, 10, 20, 15, 5, 1, 7, 6, 11, 9, 20)$

$> m = 12$

$> Sp = \text{length}(x[x > m])$

$> Sn = \text{length}(x[x < m])$

$> n = Sp + Sn$

$> Pv = \text{pbinom}(Sn, n, 0.5)$

[1] data x

$v = 25$, pvalue = 0.2521

Acc/Rej

A.U. 3.30
11.