

## Mixture and Alligation

Q. What ratio water mixed to milk to gain 20%?

→ To gain 20% we sold to 120 ₹ in which milk is of 100 ₹  
∴ In 100 litre milk we add 20 litre water.

$$\therefore \text{Ratio } 20/100$$

Q. Tea worth ₹125, ₹145 and third variety mixed in 1:1:2  
Sold at CP of 160 ₹ per kg price of third variety is?

→

$$125\left(\frac{1}{4}\right) + 145\left(\frac{1}{4}\right) + \left(\frac{x \times 2}{4}\right) = 160$$

$$x = 185 \text{ ₹}$$

Q. Selling 1000 kg sugar, Part sold at 10% profit, rest at 30% profit he have 15% profit overall find quantity sold at 30%?

→ here we have to find in what ratio if two quantities added then they give 15 ₹/kg if they give 10 ₹, 30 ₹ per kg. then we will use that ratio to find two parts of 1000 kg.

$$\therefore \begin{array}{ccc} 10 & & 30 \\ & \searrow & \swarrow \\ & 15 & \\ & \swarrow & \searrow \\ 15 & & 5 \end{array} \quad \text{hence ratio is } \frac{3}{1}$$

to find quantities we will use ratio

$$\text{as } \left[ \frac{1}{4} \times 1000 = 250 \text{ kg} \right] \text{ \& } \left[ \frac{3}{4} \times 1000 = 750 \text{ kg} \right]$$

Q. 50% alcohol mix. replaced some amount with another 20% alcohol mix. to get 25% alcohol, The replaced quantity is?

→ Let alcohol replaced with price.

$$\begin{array}{ccc} 50\% & & 20\% \\ & \searrow & \swarrow \\ & 25\% & \\ & \swarrow & \searrow \\ 5 & & 5 \end{array}$$

Ratio of final mix is  $\frac{1}{5}$

that means first type (50%) is  $\frac{1}{6}$   
and second type (20%) is  $\frac{5}{6}$

Hence second type is replaced amount.

$$\therefore \text{Quantity Replaced is } \frac{5}{6}$$

Q. Container have 30 lit milk; 5 lit taken replaced with water. It is repeated twice. What is amount of milk now?

→ Process done 3 times total.

$$\text{milk remained} = A \left[1 - \frac{B}{A}\right]^n$$

$$= 30 \left[1 - \frac{5}{30}\right]^3$$

$$\approx 17$$

Q. Two alloys Cu & Al, one have copper half as much as Al. Another have copper thrice of Al. How many times second alloy must be added to get Cu twice of Al?

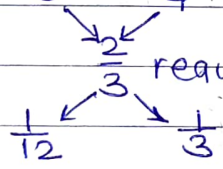
→ To find how much time we need to add second alloy first we find ratio of first: second alloys and part the second have is his frequency of addition.

∴ Take Copper as our property like price/kg, then

first alloy Copper is  $\frac{1}{3}$  and Aluminium is  $\frac{2}{3}$

second alloy Copper is  $\frac{3}{4}$  and Aluminium is  $\frac{1}{4}$

①  $\frac{1}{3}$       ②  $\frac{3}{4}$



required proportion of mix,

Ratio of first to second is

$$\text{Ratio} = \frac{1/12}{1/3} = \frac{1}{4}$$

Here  $\frac{1}{12}$  is first alloy  $\frac{1}{3}$  is second alloy hence second alloy added 4 times.

Q. vessel is filled with 3 parts water, 5 part Syrup. How much mixture must be drawn off and replaced with water so that half water half syrup?

→ if x lit. is removed and x water added.

$$\text{water is} = 3 - \frac{3x}{8} + x$$

$$\text{Syrup is} = 5 - \frac{5x}{8}$$

$$\therefore 3 - \frac{3x}{8} + x = 5 - \frac{5x}{8}$$

$$\therefore \boxed{x = \frac{8}{5}}$$



Imp

Part of mixture replaced is  $\left(\frac{8 \times 1}{5 \times 8}\right) = \frac{1}{5}$

Q. can contain mixture of two liquids A & B in ratio 7:5 when 9 litre mixture drawn off and the can filled with B ratio A and B becomes 7:9  
 How many litres of liquid A was contained initially

$\rightarrow A \Rightarrow \left(\frac{7x - 7 \times 9}{12} \times 9\right) \Rightarrow \left(\frac{28x - 21}{4}\right)$

$B \Rightarrow \left(\frac{5x - 5 \times 9}{12} \times 9\right) + 9 \Rightarrow \left(\frac{20x - 15}{4} + 9\right) \Rightarrow (20x + 21)$

$\therefore \frac{28x - 21}{20x + 21} = \frac{7}{9}$

$\therefore x = 3$

$\therefore A \Rightarrow (7 \times 3) = 21$

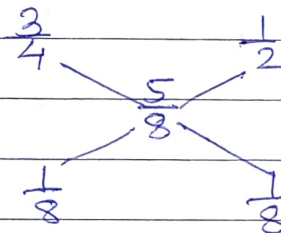
Q. 2 cans of milk in first 25% water second have 50% in how much quantity they should mix to get 12 litres of milk in 3:5?

$\rightarrow$  Let Prices according to mixture quality be

①  $\Rightarrow \frac{3}{4}$

then

②  $\Rightarrow \frac{1}{2}$

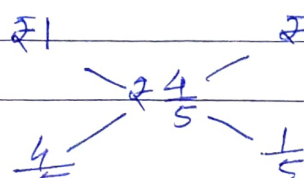


Ratio of water to milk in 12 litre from two cans  
 1:1

**6 litre 6 litre should mix**

Q. Dishonest milkman sells milk at CP but make 25% profit what is amount of water?

$\rightarrow$  let he sells 125 litre milk then to make 25% CP should be 100 hence milk is  $\frac{4}{5}$



Ratio = 4:1  
 milk = 80 litre  
 water = 20 litre.

Q. Jar of whiskey with 40% alcohol, part replaced by alcohol and now percentage of alcohol found to be 26%. quantity of replaced whisky.

→

①	②	Ratio = 1:2 for 1:2 ratio quantity replaced is $\frac{2}{3}$ .
40%	19%	
26%		
7	14	

Q. The cost of rice type ① 15 ₹/kg & ② 20 ₹/kg if the mixed in 2:3

→

15	20	$\frac{20-x}{x-15} = \frac{15}{20} = \frac{3}{4}$ $x = 18$
x		
20-x	x-15	

Q. 8 litre drawn from wine then filled with water, This operation is performed three more times. The ratio of quantity of wine now left in cask to that water ~~is~~ 16:65, How much wine did cask held?

→

$$\frac{x \left[1 - \frac{8}{x}\right]^4}{x} = \frac{16}{85}$$

$$\left(1 - \frac{8}{x}\right)^4 = \left(\frac{2}{3}\right)^4$$

$$x = 24$$

Q. merchant has 1000 kg of sugar, Part of which he sells at 8% profit rest 18% he gains 14% of whole quantity sold at 18% is?

→

①	②	Quantity of 18% = $\frac{2}{2+3} \times 1000$ = 600 kg
8	18	
14		
4	6	
2	3	