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Statistics For Data Science

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1 Basic Terminologies

1.1 Population

An entire set of items you want to study

1.2 Sample

A subset of population used to estimate statistical behavior of the whole population

1.3 Histogram

A histogram is a graphical representation of numerical data that groups the data into bins and displays the frequency of data points within each bin as bars

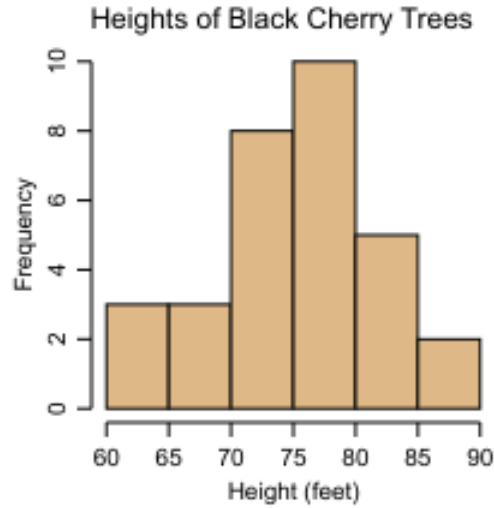


Figure 1: Example of a Histogram

2 Law of large numbers

As the number of trials (or samples) increases, the sample average (or empirical mean) will converge to the expected value (or population mean).

2.0.1 Weak Law of large numbers

The weak law states that the sample average of a sequence of independent identically distributed (i.i.d.) random variables converges in probability to the expected value as the number of samples goes to infinity

$$\bar{X}_n = \frac{1}{n} \sum_{i=1}^n X_i \xrightarrow{p} \mu \quad \text{as } n \rightarrow \infty$$

which means,

$$\forall \varepsilon > 0, \lim_{n \rightarrow \infty} \mathbf{P}(|\bar{X}_n - \mu| > \varepsilon) = 0$$

2.0.2 Strong Law of large numbers

The strong law states that the sample average of a sequence of i.i.d. random variables converges almost surely to the expected value as the number of samples goes to infinity

$$\bar{X}_n = \frac{1}{n} \sum_{i=1}^n X_i \xrightarrow{a.s.} \mu \quad \text{as } n \rightarrow \infty$$

Which means,

$$P(\lim_{n \rightarrow \infty} \bar{X}_n = \mu) = 1$$

3 Central-Limit Theorem

4 Measure of Central Tendency

4.1 Mean/Expected Value

Average of all data points, sensitive to outliers since a single large outlier could easily skew mean

$$\mu = \frac{\sum x_i}{n}$$

4.2 Median

The middle data point when data are sorted, robust to outliers

4.3 Mode

The most frequent data point of the dataset

5 Measure of Spread

Range: Difference between minimum value and maximum value

$$Range = x_{max} - x_{min}$$

5.1 Variance

Average squared deviation, Variance represents Expected variance between mean and data points, It's basically MSE of a model that just predicts mean, that kinda gives an intuitive understanding of how it measures spread

$$\begin{aligned}
\sigma^2 &= E[(X - \mu)^2] \\
\sigma^2 &= E[(X - E[X])^2] \\
\sigma^2 &= E[X^2] - (E[X])^2 \\
\sigma^2 &= \frac{\sum (x_i - \mu)^2}{n} (Population) \\
s^2 &= \frac{\sum (\bar{x}_i - \mu)^2}{n - 1} (Sample)
\end{aligned}$$

5.2 Standard Deviation

Root of Variance, RMSE of a model that just predicts mean, standard deviation gives in interpretable terms like RMSE

$$\sigma = \sqrt{\sigma^2}$$

5.3 Inter Quartile Range(IQR)

Difference between 75th Percentile/3rd Quartile and 25th Percentile/1st Quartile, it is used for outlier detection

$$IQR = Q_3 - Q_1$$

We calculate lower bounds and upper bounds to detect the outliers

$$\text{lower bound} = Q_1 - 1.5 \times IQR$$

$$\text{upper bound} = Q_3 + 1.5 \times IQR$$

the data points which values outside of the bounds is considered to be outliers, for more extreme detection $3 \times IQR$ is also used

6 Probability Distributions

6.1 Discrete Distributions

A discrete probability distribution describes the probability of occurrence of each value of a discrete random variable

- Discrete random variable: Countable values like 1,2,3
- Each individual value has an associated probability
- The sum of probabilities for all possible values is 1

$$\sum_i P(X = x_i) = 1$$

6.2 Continuous Distributions

7 Discrete Probability Distributions

7.1 Benoulli Distribution

The benouli distribution is a discrete probability distribution for a random variable which takes only two possibilities, Sucess or a failure

7.1.1 Probability Mass Function(PMF)

$$P(X = x) = \begin{cases} p & \text{if } x=1 \\ 1 - p & \text{if } x=0 \\ 0 & \text{Otherwise} \end{cases}$$

Also written as

$$P(X = x) = p^x(1 - p)^{1-x}, \quad \text{for } x \in \{0, 1\}$$

7.1.2 Statistical Parameters

Mean

Mean is the expected value over many repetitions of the same single-trial experiment, thus it would be p since, p is probability of 1 appearing and (1-p) is probability of 0 appearing

$$\mu = 1 \times (p) + 0 \times (1 - p)$$

$$\mu = p$$

Variance

Variance can be defined as $\sigma^2 = E(X^2) - (E(x))^2$, Refer Variance chapter. For Bernoulli distribution, $E(X^2) = p$, $E(X) = p$, substituting we get

$$\sigma^2 = p - p^2$$

$$\sigma^2 = p(1 - p)$$

Mode

Mode for Bernoulli would what ever the outcome which is more favored, which can be defined as

$$Mode = \begin{cases} 1 & \text{If } p > 0.5 \\ 0 & \text{If } p < 0.5 \end{cases}$$

7.1.3 Examples

- Will it rain tomorrow?
- Will this patient recover?
- Will this product be defective?

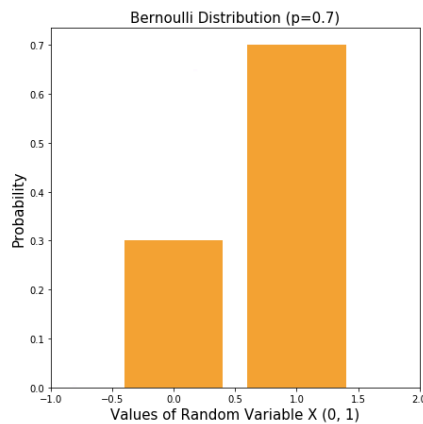


Figure 2: Example of a Bernoulli Distribution

7.2 Binomial

Binomial Distribution is a discrete probability distribution that models the probability of obtaining a specific number of successes in a fixed number of independent trials(n), these independent trials are just Bernoulli trials, you could see the similarity between them in statistical parameters

7.2.1 Probability Mass Function(PMF)

$$P(X = x) = nCx \times p^x \times (1 - p)^{(n-x)}$$

where,

n - no of trials,

p - probability of success

x - number of success

7.2.2 Statistical Parameters

Mean

Mean represents Average number of success from your trails which would be number of trials (n) times probability of success (p)

$$\mu = n \times p$$

Variance

Variance represents Expected variance between mean and data points,

$$\sigma^2 = n \times p \times (1 - p)$$

Mode

$$Mode = \begin{cases} \text{floor}((n+1)p) & \text{if } (n+1)p \text{ is not an Integer} \\ \text{floor}((n+1)p), \text{floor}((n+1)(1-p)) & \text{if } (n+1)p \text{ is an Integer} \end{cases}$$

$$\text{Mode(if } p = 0.5) = \begin{cases} \frac{n}{2} & \text{if } (n+1)p \text{ is not an Integer} \\ \frac{(n-1)}{2}, \frac{(n+1)}{2} & \text{if } (n+1)p \text{ is an Integer} \end{cases}$$

7.2.3 Examples

- How many patients will recover out of 50?
- How many rainy days this month?
- How many defective products in a batch of 1000?

7.3 Negative-Binomial

7.4 Multinomial

7.5 Geometric

7.6 Hypergeometric

7.7 Poisson

7.8 Discrete Uniform

7.9 Normal Distribution

7.9.1 Use cases

- When there is only one trial
- When the outcome is binary True/False Yes/No

8 Shape of the Distributions

8.1 Skewness

Measure of Asymmetry

8.1.1 Right-skewed

tail on the right ($mean > median$)

8.1.2 Left-skewed

tail on the left ($mean < median$)

9 Hypothesis Testing

9.1 Null Hypothesis(H_0)

Null Hypothesis is the default claim basically means no effect/ no difference

9.2 Alternate Hypothesis(H_a)

Alternate Hypothesis is the hypothesis that u want to prove

9.3 One sided Test

When you have to test if the parameter is greater than or less than the hypothesised value, but not both

Null: $H_0 : \mu = \mu_0$

Alternate: $H_a : \mu > \mu_0$ or $\mu < \mu_0$

9.4 Two sided Test

When you have to test if the parameter is different from the hypothesised value in either direction Null: $H_0 : \mu = \mu_0$

Alternate: $H_a : \mu \neq \mu_0$

9.5 Test Statistic

A test statistic is a function of the sample data that is used to decide whether to accept/reject the null hypothesis

$$\text{Test Statistic} = \frac{\text{How surprised we are}}{\text{How surprised we can be}}$$

$$\text{Test Statistic} = \frac{\text{Observed Value} - \text{Expected value under } H_0}{\text{Standard Error of observed value}}$$

9.6 Sampling distribution under H_0

If null hypothesis is true, what would the distribution of my test statistic look like across repeated samples. the sample mean/ test statistic follows normal distribution thanks to CLT (central limit theorem), we use that to calculate p-value.

1. Calculate sample statistic(\bar{x}, s^2)
2. Compute test statistic(t-test,z-test...)
3. Compare the computed test statistic to the corresponding distribution to get the p-value

9.7 p-value

The p-value is the probability of observing your data assuming the null hypothesis is true

if p is small($p < \alpha$), we reject null's hypothesis if p is high($p > \alpha$), we reject alternate hypothesis

10 Machine Learning

Machine learning(ML) is a way of teaching computers to learn patterns from data and make prediction.

10.1 Type of Machine learning

- Supervised Learning
- Unsupervised Learning
- Reinforcement Learning
- Semi-Supervised Learning

11 Types of Data

11.1 Qualitative Data

Describes Qualities, Characteristics , or categories

11.1.1 Nominal

Pure categories without order, Example: blood type(A,B,AB,O), brand names

11.1.2 Ordinal

Categories with meaningful order, Examples: Rank, Survey rating

11.2 Quantitative Data

Measureable quantities, Numbers have meaningful terms in terms of magnitude

11.2.1 Discrete

Countable values, no in-betweens. Examples: number of cars

11.2.2 Continuous

Continuous measurements; can take any value within a range, Examples: Height, weight, temperature

12 Data Cleaning

12.1 Define the target variable

Analyse over all data and pinpoint what you want to predict in the dataset,
if your data is discrete like class - classification,
if you have a continuous variable - Regression

12.2 Policy Document

Policy document is a meta data document that defines each column, A policy document could define type of the data, nullable, pattern of the data, Range, units, Logical constraints, description... etc Example:

Column	Type	Null	Pattern/Range	Constraint	Notes
user_id	string	No	regex [A-Z0-9]8	unique	id
age_years	int	No	[0,120]	–	cap outliers
gender	cat	Yes	{M,F,O}	–	harmonize
signup_date	date	No	YYYY-MM-DD	churn_date	UTC
churn	binary	No	{0,1}	target	def: 30d leave
income_inr	float	Yes	[0,1e8] INR	winsorize top 1%	currency check
email	string	Yes	regex email	–	PII → hash

12.3 Outlier Detection

12.3.1 Inter Quartile Range(IQR)

Difference between 75th Percentile/3rd Quartile and 25th Percentile/1st Quartile, it is used for outlier detection

$$IQR = Q_3 - Q_1$$

We calculate lower bounds and upper bounds to detect the outliers

$$\text{lower bound} = Q_1 - 1.5 \times IQR$$

$$\text{upper bound} = Q_3 + 1.5 \times IQR$$

the data points which values outside of the bounds is considered to be outliers, for more extreme detection $3 \times IQR$ is also used

12.3.2 Z-score

How far your point is away from the mean in terms of standard deviation

$$z_i = \frac{x_i - \mu}{\sigma}$$

if $z_i > 3$, the point is very unusual and a potential outlier considers all data above 3 SD as outliers and eliminates it

12.4 Percentile/Quantile Trimming

Trim of top and bottom 1-5 percentage of data, commonly used in competitions to make sure there are no outliers

12.5 Domain Rules

Domain rules like ages should range between 0 - 120, or temperatures should range between -50 to 60 degrees

12.6 Impute missing values

You can either delete the row entirely or chose to impute the missing values

12.6.1 Numerical data

- small missing values - mean
- skewed - median
- important values - regression imputation
- many missing - add a missign flag (0) or remove the column entirely
- if you are not sure you can test all the methods with cross validation and chose a impuation method (recomended for large datasets)

12.6.2 Categorical

- Low cardinatlity(few categories) - Mode impuation
- High cardinatlity - Add a new "missing" category

12.6.3 Time series

- Short gaps - forward/backward fill
- Long gaps - Interpolation
- seasonal data - seasonal average + Iterpolation(optional)

12.6.4 Images

take mean or median of the neighbours to fill in the missing pixels, or drop the image from the dataset

12.6.5 Text

Drop the entire row or add [missing] token

12.7 Data transformation

12.7.1 Standarization

$$x_i = \frac{x_i - \mu}{\sigma}$$

- used in linear regression, SVM, PCA, K-means
- makes mean 0, and std 1
- used to standarize all the numerical featuers so that they don't dominate over one another

12.7.2 Min-Max scaling

$$x_i = \frac{x_i - \min(x)}{\max(x) - \min(x)}$$

- Used in: neural networks, gradient based models, image pixel scaling
- Fits everything in [0,1]
- Helps model converge faster

12.7.3 Robust scaling

$$x_i = \frac{x - \text{x-median}}{\text{IQR}}$$

- Used in Models sensitive to outliers: regression, SVM, KNN
- Ignores extreme values, centers around median
- Robust to outliers

12.8 Log transformation

$$x_i = \log(x + c)$$

- used in skewed data(income , population, counts)
- used in exponentialisue data to make it more linear
- Compresses large numbers, spreads out small ones to make distribution closer to normal

12.9 Text processing

lemmatizaiton and so on

12.9.1 Lowercasing

Converts all the letters into lowercase

12.9.2 Noise Removal

Remove punctuation, numbers, symbols,stopwords(if not useful)

12.9.3 Tokenization

- Convert sentence into smaller units token
- example: I like data science = [I,like, data, science]
- Tokens are mostly words but not always

12.9.4 Stemming

- chops suffixes from the words
- example: "playing" → "play", "studies" → "studi"

12.9.5 Lemmatization

- Advanced form of stemming
- reduces to dictionary base form
- example: "playing" → "play", "studies" → "study"
- requires POS(part of speech) tagging, slower but better

12.10 Handling spelling and special entities

- Spelling correction
- Handle emojis, mention, hashtags (social media)

12.11 Name Entity Recognition

- NER can be used for censoring sensity information
- for extracting NER and use it as features for the algorithms

12.12 Encoding

12.12.1 Bag of Words(BOW)

- Bag of words is one-hot encoding for words
- Dictionary based bag of words is often used for larger datasets
- It represent frequency of words in a vector format

12.12.2 Term frequency-Inverse document frequency (TF-IDF)

- Mesure How important a word is to a document relative to the whole corpus
- common words, less importance
- Rare document specific word, higher importance

- Vectorize a word BOW style and find TF-IDF for each words to form a vector which can be used alongside with cosine similarity to find similar documents
- Drawbacks - doesn't consider order of the words

$$TFIDF(t, d) = TF(t, d) \times IDF(t)$$

Term Frequency is defined as number of times term t appears in document d by total number terms in the document

$$TF(t, d) = \frac{f_{t,d}}{\sum_{t' \in d} f_{t',d}}$$

Inverse Document Frequency is a penalty for words that appear in many documents

$$IDF(t) = \log \left(\frac{N}{DF(t)} \right)$$

12.12.3 Embedding

- Word2vec, embedding models
- converts words/sentences to vectors
- the embedding encodes the meaning of the sentence / word
- Words similar to each other are near to each other

12.13 Image processing

13 Feature engineering and selection

14 Supervised Learning

15 Unsupervised Learning

16 Evaluation Metrics for Regression

16.1 Mean Absolute Error

$$MAE = \frac{1}{n} \sum |y_i - \hat{y}_i|$$

- Robust to outliers, treats all errors equally doesn't square the errors like RMSE, MSE..etc
- It's used when your model can tolerate moderate outliers
- Interpretability - Has same unit as the thing you are predicting/easy to understand
- Gives out constant gradient (bad for gradient based loss function)

16.1.1 Gradient of MAE

$$\frac{d}{d\hat{y}}|y - \hat{y}| = \begin{cases} +1 & \text{if } \hat{y} < y \\ -1 & \text{if } \hat{y} > y \\ \text{undefined} & \text{if } \hat{y} = y \end{cases}$$

As you can see no matter how far the error is from true value it always gives a constant gradient as it treats every error as same stics

16.2 Mean Squared Error

$$MSE = \frac{1}{n} \sum (y_i - \hat{y}_i)^2$$

- Penalizes large errors/outliers
- Gives out strong gradient signals

16.2.1 Gradient of MSE

$$\frac{dMSE}{d\hat{y}} = -\frac{2}{n}(y - \hat{y})$$

It points in the direction of the error, and it grows linearly with size of the error. Larger the gradient, when prediction are more wrong \rightarrow model adjusts faster

16.3 Root Mean Squared Error(RMSE)

$$RMSE = \sqrt{MSE}$$

- It combines interpretability of MAE and sensitive to errors of MSE
- It has smooth gradient curves just like MSE, and it's preferred for gradient descent

16.3.1 Gradient of RMSE

$$\frac{dRMSE}{d\hat{y}_i} = \frac{1}{n \times RMSE}(\hat{y}_i - y_i)$$

1. The gradient strength changes with RMSE, if your RMSE is very large the gradient becomes small, and if your RMSE is very small the gradient becomes large.
2. It makes RMSE a Non-constantly scaled loss
3. MSE is preferred over RMSE in training, but RMSE is preferred while reporting for interpretability

16.4 R-Square(R^2)

R^2 is the coefficient of determination. it tells how well your regression model explains the variation in the dependent variable(Y) using independent variables(X)

$$R^2 = 1 - \frac{SS_{res}}{SS_{tot}}$$

where,

- $SS_{res} = \sum (y_i - \hat{y}_i)^2 \rightarrow$ Residual sum of squares(error)/MSE

- $SS_{tot} = \sum (y_i - \bar{y}_i)^2 \rightarrow$ Total sum of squares (total variability)

$$R^2 = 1 - \frac{\sum (y_i - \hat{y}_i)^2}{\sum (y_i - \bar{y}_i)^2}$$

Or, it can also be written more intuitively as

$$R^2 = 1 - \frac{MSE}{\sigma^2}$$

- Let us understand the formula (1-) operator just switches from maximizing to minimizing so you can ignore that.
- $\frac{MSE}{\sigma^2}$ Explains how well our model performs to a model that just predicts mean everytime, so if the ratio is 1, then our model is same as the dumb model, we have to reduce the ratio but the world likes "more the better" approach add (1-) operator we have to maximize the error and it's called as R^2
- R^2 ranges from $(-\infty, 1]$

16.5 Adjusted R^2

$$R_{adj}^2 = 1 - \left(\frac{(1 - R^2)(n - 1)}{n - k - 1} \right)$$

The above mentioned is textbook formula but we use our simplified representation for R^2

$$R^2 = 1 - \frac{MSE}{\sigma^2}$$

so, R_{adj}^2 would be

$$R_{adj}^2 = 1 - \frac{MSE_{adj}}{\sigma_{adj}^2}$$

MSE adjusted accounts for the number of freedoms used up to predict the data, which is K, represents number of parameters like number of predictors, number of bias

$$MSE_{adj} = \frac{\sum (y_i - \hat{y}_i)^2}{n - k}$$

Variance adjusted for number of freedoms used up which is 1 (mean), thus it'd be n-1 insted of n

$$\sigma_{adj}^2 = \frac{\sum (y_i - \mu)^2}{n - 1}$$

Substituting we get,

$$R_{adj}^2 = 1 - \left(\frac{MSE}{\sigma^2} \times \frac{n - 1}{n - k} \right)$$

where

- n - number of samples/ training samples
- k - number of parameters

16.6 Mean Absolute Percentage Error(MAPE)

MAPE is a metric used to measure accuracy of a predictive model. It expresses the prediction error as the percentage of actual values

$$MAPE = \frac{1}{n} \sum_{i=1}^n \left| \frac{y_i - \hat{y}_i}{y_i} \right| \times 100$$

MAPE is just like MAE but it gives out the error in percentage thus it's easier to intrepret

16.7 Huber Loss

Huber loss is a robust loss function/evaluation metric that has both strengths of MAE and MSE

$$L_{\delta} = \begin{cases} \frac{1}{2}(y - \hat{y})^2 & \text{for } |y - \hat{y}| \leq \delta \\ \delta \cdot (|y - \hat{y}| - 1/2\delta) & \text{otherwise} \end{cases}$$

where,

- δ is a hyperparameter that controls the behavior between MSE and MAE behavior

16.7.1 Gradient of Huberloss

$$\frac{\partial L}{\partial \hat{y}} = \begin{cases} -(y - \hat{y}) & \text{if } |y - \hat{y}| \leq \delta \\ -\delta \cdot \text{sign}(y - \hat{y}) & \text{otherwise} \end{cases}$$

example graph goes here

17 Evaluation Metrics for Classification

17.1 Basic Terminologies

17.1.1 True Positive

Correctly predicted positive class

17.1.2 False Positive

Falsely Predicted Positive class, actually negative

17.1.3 True Negative

Correctly predicted negative class

17.1.4 False Negative

Falsely predicted negative class, actually positive

17.2 Accuracy

Out of all predictions how many are correct, ratio between correct predictions and total predictions is accuracy

$$Accuracy = \frac{\text{Correct predictions}}{\text{Total predictions}}$$

can also be written as,

$$Accuracy = \frac{TP + TN}{TP + TN + FP + FN}$$

17.3 Precision

Out of all my positive class prediction how much did I get correctly, ratio between correct positive class prediction and total positive class predicted

$$\text{Precision} = \frac{\text{No of correct positive class predicted}}{\text{No of positive class predicted}}$$

can also be written as,

$$\text{Precision} = \frac{TP}{TP + FP}$$

Use when FP is costly, when you want every positive prediction to be trust worthy, measures reliability

17.4 Negative Predicted Value (NPV)

Out of all my negative predictions how much did I get correctly, ratio between

$$\text{NPV} = \frac{\text{No of correct negative class predicted}}{\text{No of negative class predicted}}$$

can also be written as,

$$\text{NPV} = \frac{TN}{TN + FN}$$

Use when FN is costly, when you want every negative class to be trust worthy

17.5 Recall(TPR)

Out of all positive cases how many did I predict correctly, also known as True Positive Rate(TPR) ratio of correctly predicted positive class and total positive cases

$$\text{Recall} = \frac{\text{No of correctly predicted positive class}}{\text{No of actual positive class}}$$

$$\text{Recall} = \frac{TP}{TP + FN}$$

Use when FN is costly/ wrongly classifying , did it recall everything, predict all positive cases

17.6 Specificity

Out of all negative cases how many did I predict correctly, Basically Recall for negative class

$$\text{Specificity} = \frac{\text{No of correctly predicted negative class}}{\text{No of actual negative class}}$$

$$\text{Specificity} = \frac{TN}{TN + FP}$$

Use when FP is costly, when predicting negative class is important

17.7 False Positive Rate(FPR)

Out of all negative cases how many did I fail to predict,

$$\text{FPR} = \frac{\text{No of wrongly predicted negative class}}{\text{No of actual Negative class}}$$

$$\text{FPR} = \frac{FP}{TN + FP}$$

$$\text{FPR} = 1 - \text{specificity}$$

17.8 F-score

It's a harmonic mean between precision and recall

$$F_{\beta} = \frac{(1 + \beta^2) \cdot \text{Precision} \cdot \text{Recall}}{(\beta^2 \cdot \text{Precision}) + \text{Recall}}$$

17.8.1 Derivation

$$\frac{1}{F_{\beta}} = \frac{w_p}{\text{Precision}} + \frac{w_r}{\text{Recall}}$$

We want harmonic ratio of precision and recall,

$$\frac{w_r}{w_p} = \beta^2$$

We want the weights to add up to one

$$w_r + w_p = 1$$

By solving we get

$$w_r = \frac{\beta^2}{1 + \beta^2}$$
$$w_p = \frac{1}{1 + \beta^2}$$

18 AUC-ROC curve

18.1 Receiver Operating Characteristic (ROC)

The ROC curve plots the True Positive Rate(TPR) vs False Positive Rate(FPR) at various threshold settings, it let's you decide which one is best for you based on your requirement

18.2 Area Under the Curve (AUC)

The AUC tells how much of the curve is under the line, usually compared with other models

Higher AUC = Better model performance

Auc Score	Intrepretation
0.5	Random guessing
0.7 - 0.8	Acceptable
0.8 - 0.9	Excellent
>0.9	Outstanding

19 Regularization

Regularization adds a penalty for complexity to prevent overfitting, make model simpler

$$\text{Regularized Loss} = \text{Loss} + \text{Regularization parameter}$$

19.1 L1

L1 adds the sum of absolute value of coefficients to the loss function, it is used for feature selection since it encourages the optimizer to shrink unwanted features to zero

$$L1 = \lambda \sum |w_i|$$

19.2 L2

L2 adds the sum of coefficient squares to the loss function this makes the gradient strength smooth, thus it won't reduce everything to zero, but towards zero, use it when you think all features contribute to ur model

$$L2 = \lambda \sum w_i^2$$

19.3 Elastic net

It's a combination of L1 and L2 where you want to have both sparsity(l2) and stability(l1)

$$\text{Elastic Net} = \alpha L1 + (1 - \alpha)L2$$

20 Time Series

21 TODOO

1. pca
2. complete the Distributions, some intro to probability
3. Time series, ML, other stuff