Technology A Relaxation Current

August 17, 2021

1 RRAM Relaxation Data Notebook

This notebook contains the analysis on empirical RRAM relaxation data across three technologies (A, B, C). It loads and processes the measurements taken for each technology.

```
[1]: # Imports
  import gzip
  import json
  import matplotlib.pyplot as plt
  import numpy as np
  import pandas as pd
  import scipy.signal
  import scipy.stats
  # from matplotlib.offsetbox import AnchoredText

%config InlineBackend.figure_format = 'svg'
```

1.1 Load the technology and its settings

Below, choose which technology to load data and settings for:

```
[2]: # Choose technology here
TECH = 'A'

# Load settings for technology
with open(f"data/tech{TECH}/settings.json") as sfile:
    settings = json.load(sfile)
```

1.2 Time series analysis

In this section, we will look at example time series data on a log scale and also examine the power spectral density (PSD). First, let us load the time series data:

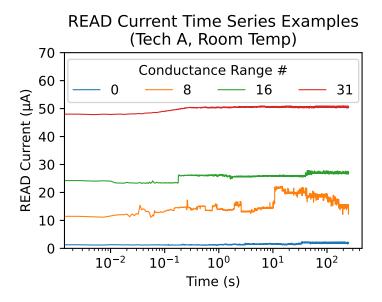
1.2.1 Example Time Series Data

Below, we can look at the time series data for the ranges chosen above:

```
[3]: # Load data for technology with gzip.open(f"data/tech{TECH}/tsdata.min.tsv.gz", "rt") as datafile:
```

```
# Plot example time series data
    fig = plt.figure(figsize=(4,2.7))
    ax = fig.add_subplot(111)
    ax.set_title(f"READ Current Time Series Examples\n(Tech {TECH}, Room Temp)")
    for r in settings["ts_ranges"]:
         # Select data
        d = datafile.readline()
        print(r, "step 1")
        d = np.fromstring(d, dtype=float, sep='\t')[2:]
        print(r, "step 2")
         # Plot time series data
        plt.plot(np.arange(len(d))/settings["fs"], d*1e6*0.2, label=r,__
 \rightarrowlinewidth=0.8)
    # Format and display
    ax.legend(title="Conductance Range #", ncol=4, loc=9)
    ax.set_ylim(*[v*0.2 for v in settings["ts_ylim"]])
    ax.set_xlabel("Time (s)")
    ax.set_ylabel("READ Current (μA)")
    ax.set xscale("log")
    plt.savefig(f"figs/tech{TECH}/time-series-i.png", dpi=300,
 ⇔bbox_inches="tight")
    plt.show()
0 step 1
0 step 2
```

```
0 step 1
0 step 2
8 step 1
8 step 2
16 step 1
16 step 2
31 step 1
31 step 2
```

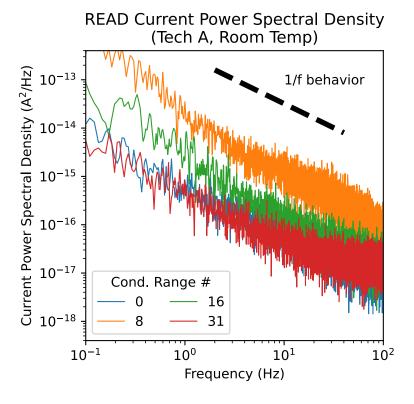


1.2.2 Power Spectral Density (PSD)

In this section, we will look at the PSDs to understand the relaxation behavior better:

```
[4]: # Load data for technology
    with gzip.open(f"data/tech{TECH}/tsdata.min.tsv.gz", "rt") as datafile:
        # Plot power spectral density (PSD)
        fig = plt.figure(figsize=(4,4))
        ax = fig.add_subplot(111)
        ax.set_title(f"READ Current Power Spectral Density\n(Tech {TECH}, Room_
     →Temp)")
        slopes = []
        for i, r in enumerate(settings["ts_ranges"]):
            # Select data
            d = datafile.readline()
            print(r, "step 1")
            d = np.fromstring(d, dtype=float, sep='\t')[2:]
            print(r, "step 2")
            # # Lomb-Scargle PSD
            \# f = np.logspace(np.log10(1/600), np.log10(2), 500)
            # f = np.logspace(np.log10(2), np.log10(400/2), 1000)
            \# p = scipy.signal.lombscargle(d["time"], d["g"], f)
            # Welch PSD
            f, p = scipy.signal.welch(d*0.2, fs=settings["fs"],__
      plt.plot(f, p, label=r, linewidth=0.8)
```

```
# # Power law fit
         # a, b = np.polyfit(np.log(f[[30,-30]]), np.log(p[[30,-30]]), 1)
         # print(f"Range {r} slope: {a}")
         # slopes.append(a)
         # plt.plot(f[1:], np.exp(a*np.log(f[1:]) + b), 'k--', zorder=10, ___
 \rightarrow linewidth=2)
         # # 1/f fit
         # fitfn = lambda logf, A: A - logf
         \# params, \_ = scipy.optimize.curve\_fit(fitfn, np.log(f), np.log(p))
         \# A = params[0]
         # print(A)
         # plt.plot(f, np.exp(fitfn(np.log(f), A)), 'k--', zorder=10, 
 \rightarrow linewidth=2)
    # Format and display
    # ax.add_artist(AnchoredText("Slopes: [%.2f, %.2f]" % (max(slopes), ____
 \rightarrow min(slopes)), loc=1, frameon=False))
    plt.plot(settings["psd_fpts"][0], np.array(settings["psd_fpts"][1])*0.2**2,__
 if "psd f2pts" in settings:
        plt.plot(settings["psd_f2pts"][0], np.array(settings["psd_f2pts"][1])*0.
 \rightarrow2**2, 'k--', zorder=10, linewidth=4)
    ax.legend(title="Cond. Range #", ncol=2, loc=3)
    ax.set xlabel("Frequency (Hz)")
    ax.set_ylabel("Current Power Spectral Density (A$^2$/Hz)")
    ax.set xscale("log")
    ax.set xlim(*settings["psd xlim"])
    ax.set_ylim(*[v*0.2**2 for v in settings["psd_ylim"]])
    ax.set yscale("log")
    plt.text(settings["psd_ftextloc"][0], settings["psd_ftextloc"][1]*0.2**2,
 →"1/f behavior")
    if "psd_f2textloc" in settings:
        plt.text(settings["psd_f2textloc"][0], settings["psd_f2textloc"][1]*0.
 \rightarrow 2**2, "1/f$^2$")
    plt.savefig(f"figs/tech{TECH}/psd-i.png", dpi=300, bbox_inches="tight")
    plt.show()
0 step 1
0 step 2
8 step 1
8 step 2
16 step 1
16 step 2
31 step 1
31 step 2
```



1.3 Relaxation data analysis

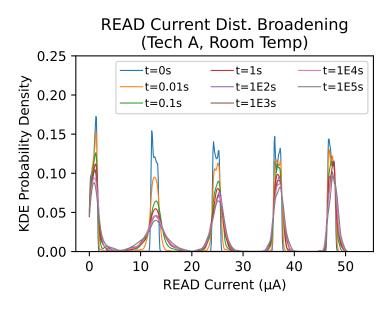
Here, we will be analyzing the large dataset relaxation behavior. We will examine: (1) examples of conductance distribution broadening behavior over time, (2) scatterplot of conductance deviation vs. conductance, (3) standard deviation vs. time for different starting conductance values. First let us load the data:

```
[5]:
         addr
                                                                     timept
                time
                                                         gi
                                                             range
        80000
                       337532.079408
                                       0.000003
                                                  0.000003
                 0.0
                                                                  0
                                                                        0.0
     0
        80001
     1
                 0.0
                        76320.104403
                                       0.000013
                                                  0.000013
                                                                  1
                                                                        0.0
     2
        80002
                                                                  2
                                                                        0.0
                 0.0
                        48034.594014
                                       0.000021
                                                  0.000021
     3
        80003
                        21027.150891
                                       0.000048
                                                  0.000048
                                                                  6
                                                                        0.0
                 0.0
        80004
                 0.0
                        33193.229603
                                       0.000030
                                                  0.000030
                                                                  4
                                                                        0.0
```

1.3.1 Conductance distribution broadening behavior

Below are examples of conductance broadening behavior over time:

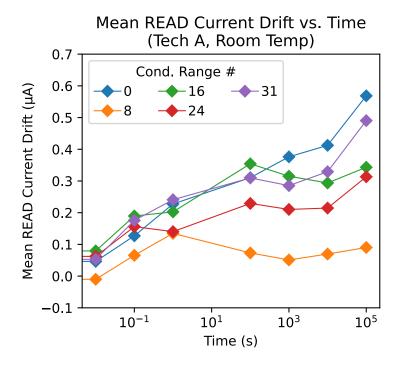
```
[6]: # Select ranges to study
     ranges = [0, 8, 16, 24, 31]
     # Conductance broadening behavior
     fig = plt.figure(figsize=(4, 2.7))
     ax = fig.add_subplot(111)
     ax.set_title(f"READ Current Dist. Broadening\n(Tech {TECH}, Room Temp)")
     colors = plt.rcParams["axes.prop_cycle"].by_key()["color"]
     for time, color in zip(settings["times"], colors):
         for r in ranges:
             gx = np.linspace(0, settings["gmax"]*1.1e6, 500)
             gvals = data[(data["range"] == r) & (data["timept"] == time)]["g"]
             pdf = scipy.stats.gaussian_kde(gvals*1e6).pdf(gx)
             label = (f"t=\{time\}s" if time < 100 else <math>f"t=1E\{int(np.log10(time))\}s"\}_{\sqcup}
      \rightarrowif r == 0 else None
             plt.plot(gx*0.2, pdf, color=color, label=label, linewidth=0.8)
     ax.legend(ncol=3, handletextpad=0.2, fontsize="small")
     ax.set_ylim(*settings["gbroad_ylim"])
     ax.set_xlabel("READ Current (µA)")
     ax.set_ylabel("KDE Probability Density")
     plt.savefig(f"figs/tech{TECH}/broadening-time-i.pdf", bbox_inches="tight")
     plt.show()
```



1.3.2 Mean Drift and Variance Growth (Time Dependence)

Here, we examine the drift of the distribution mean and variance growth as a function of time.

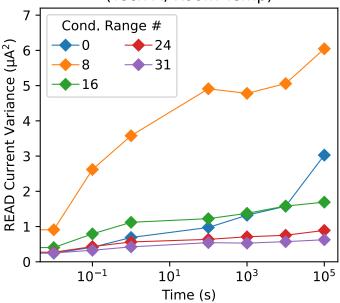
```
[7]: # Mean drift behavior (time dependence)
     fig = plt.figure(figsize=(4, 3.5))
     ax = fig.add_subplot(111)
     ax.set_title(f"Mean READ Current Drift vs. Time\n(Tech {TECH}, Room Temp)")
     colors = plt.rcParams["axes.prop_cycle"].by_key()["color"]
     for r, color in zip(ranges, colors):
         d = data[(data["range"] == r) & (data["gi"] <= settings["gmax"])]</pre>
         gi = d.groupby("timept").mean()["gi"]*1e6
         gf = d.groupby("timept").mean()["g"]*1e6
         deltag = gf - gi
         plt.plot(deltag.index, deltag * 0.2, '-D', color=color, label=r,__
      →linewidth=0.8)
     ax.legend(title="Cond. Range #", ncol=2 if TECH == 'C' else 3, handletextpad=0.
     →2)
     if "gmeandrift_t_ylim" in settings:
         ax.set_ylim(*[v*0.2 for v in settings["gmeandrift_t_ylim"]])
     ax.set_xscale("log")
     ax.set_xlabel("Time (s)")
     ax.set_ylabel("Mean READ Current Drift (μA)")
     plt.savefig(f"figs/tech{TECH}/mean-drift-vs-time-i.pdf", bbox_inches="tight")
     plt.show()
```



```
[8]: # Variance behavior (time dependence)
fig = plt.figure(figsize=(4, 3.5))
```

```
ax = fig.add_subplot(111)
ax.set_title(f"READ Current Variance vs. Time\n(Tech {TECH}, Room Temp)")
colors = plt.rcParams["axes.prop_cycle"].by_key()["color"]
for r, color in zip(ranges, colors):
    d = data[(data["range"] == r) & (data["gi"] <= settings["gmax"])]
    gfvar = d.groupby("timept").var()["g"]*(0.2e6**2)
    plt.plot(gfvar.index, gfvar, '-D', color=color, label=r, linewidth=0.8)
ax.legend(title="Cond. Range #", ncol=2, handletextpad=0.2)
if "gvar_t_ylim" in settings:
    ax.set_ylim(*[v*0.2**2 for v in settings["gvar_t_ylim"]])
ax.set_xscale("log")
ax.set_xscale("log")
ax.set_ylabel("Time (s)")
ax.set_ylabel("READ Current Variance (µA$^2$)")
plt.savefig(f"figs/tech{TECH}/var-vs-time-i.pdf", bbox_inches="tight")
plt.show()</pre>
```

READ Current Variance vs. Time (Tech A, Room Temp)



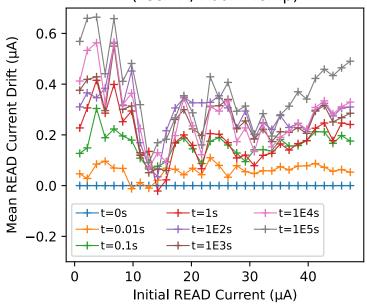
1.3.3 Mean Drift and Variance Growth (Conductance Dependence)

Here, we examine the drift of the distribution mean and variance growth as a function of conductance.

```
[9]: # Mean drift behavior (conductance dependence)
fig = plt.figure(figsize=(4, 3.5))
ax = fig.add_subplot(111)
ax.set_title(f"Mean Drift vs. Init. READ Current\n(Tech {TECH}, Room Temp)")
```

```
colors = plt.rcParams["axes.prop_cycle"].by_key()["color"]
for time, color in zip(settings["times"], colors):
    d = data[(data["timept"] == time) & (data["gi"] <= settings["gmax"])]
    gi = d.groupby("range").mean()["gi"]*1e6
    gf = d.groupby("range").mean()["g"]*1e6
    deltag = gf - gi
    label = (f"t={time}s" if time < 100 else f"t=1E{int(np.log10(time))}s")
    plt.plot(gi*0.2, deltag*0.2, '-+', color=color, label=label, linewidth=0.8)
ax.legend(ncol=3, handletextpad=0.2, fontsize="small")
ax.set_ylim(*[v*0.2 for v in settings["gmeandrift_gi_ylim"]])
ax.set_xlabel("Initial READ Current (µA)")
ax.set_ylabel("Mean READ Current Drift (µA)")
plt.savefig(f"figs/tech{TECH}/mean-drift-vs-g-i.pdf", bbox_inches="tight")
plt.show()</pre>
```

Mean Drift vs. Init. READ Current (Tech A, Room Temp)

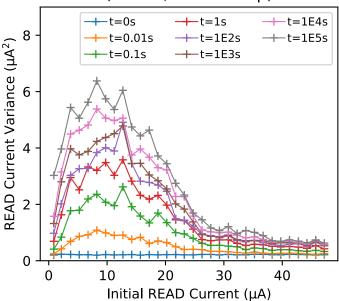


```
[10]: # Variance behavior (conductance dependence)
fig = plt.figure(figsize=(4, 3.5))
ax = fig.add_subplot(111)
ax.set_title(f"Variance vs. Init. READ Current\n(Tech {TECH}, Room Temp)")
colors = plt.rcParams["axes.prop_cycle"].by_key()["color"]
for time, color in zip(settings["times"], colors):
    d = data[(data["timept"] == time) & (data["gi"] <= settings["gmax"])]
    gi = d.groupby("range").mean()["gi"]*1e6
    gfvar = (d.groupby("range")).var()["g"]*(1e6**2)</pre>
```

```
label = (f"t={time}s" if time < 100 else f"t=1E{int(np.log10(time))}s")
plt.plot(gi*0.2, gfvar*0.2**2, '-+', color=color, label=label, linewidth=0.

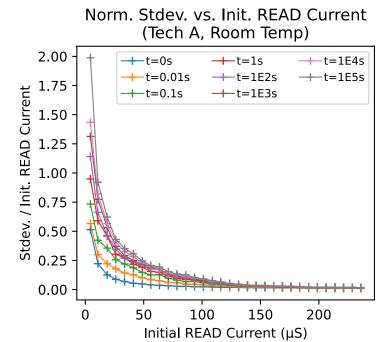
38)
ax.legend(ncol=3, handletextpad=0.2, fontsize="small")
ax.set_ylim(*[v*0.2**2 for v in settings["gvar_gi_ylim"]])
ax.set_xlabel("Initial READ Current (µA)")
ax.set_ylabel("READ Current Variance (µA$^2$)")
plt.savefig(f"figs/tech{TECH}/var-vs-g-i.pdf", bbox_inches="tight")
plt.show()
```

Variance vs. Init. READ Current (Tech A, Room Temp)



```
[11]: # Norm. stdev. behavior (conductance dependence)
fig = plt.figure(figsize=(4, 3.5))
ax = fig.add_subplot(111)
ax.set_title(f"Norm. Stdev. vs. Init. READ Current\n(Tech {TECH}, Room Temp)")
colors = plt.rcParams["axes.prop_cycle"].by_key()["color"]
for time, color in zip(settings["times"], colors):
    d = data[(data["timept"] == time) & (data["gi"] <= settings["gmax"])]
    gi = d.groupby("range").mean()["gi"]*1e6
    gfnormdev = d.groupby("range").std()["g"] / d.groupby("range").mean()["gi"]
    label = (f"t={time}s" if time < 100 else f"t=1E{int(np.log10(time))}s")
    plt.plot(gi, gfnormdev, '-+', color=color, label=label, linewidth=0.8)
ax.legend(ncol=3, handletextpad=0.2, fontsize="small")
ax.set_xlabel("Initial READ Current (µS)")
ax.set_ylabel("Stdev. / Init. READ Current")</pre>
```

```
plt.savefig(f"figs/tech{TECH}/norm-stdev-vs-g-i.pdf", bbox_inches="tight")
plt.show()
```



1.4 Temperature dependence analysis via 1hr bake

Here, we analyze the effect of baking on the distribution broadening. In particular, we will examine examples of the conductance distributions broadening for different temperatures and then analyze the temperature-dependent mean drift and variance. We can first load the data and preprocess it a little bit:

```
[12]: # Load data for technology
    colnames = ["addr", "time", "r", "g", "temp"]
    data = pd.read_csv(f"data/tech{TECH}/bake.tsv.gz", names=colnames, sep='\t')

# Get conductance range
    data["gi"] = data.groupby(["addr", "temp"])["g"].transform("first")
    data["range"] = np.int32(data["gi"] / settings["gmax"] * 32)

# Filter out the rest of the data
    data = data[data["time"] > 100].groupby(["addr", "temp"]).first().reset_index()

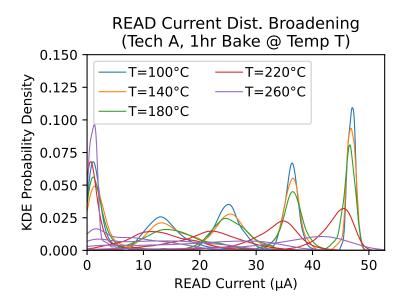
# Show data
    data.head()
```

```
addr temp
[12]:
                                                            gi range
                          time
                                          r
     0 80000
                                 6317.765383 0.000158 0.000112
               100 7164.671020
                                                                   14
     1 80000
               140 4493.587238
                                 7598.918623 0.000132 0.000068
                                                                    9
     2 80000
               180 5263.012372 16033.495632 0.000062 0.000015
                                                                    1
     3 80000
               220 4566.413692 43554.782008 0.000023 0.000006
                                                                    0
     4 80000
               260 5199.774635 82084.987230 0.000012 0.000016
                                                                    2
```

1.4.1 Conductance distribution broadening behavior

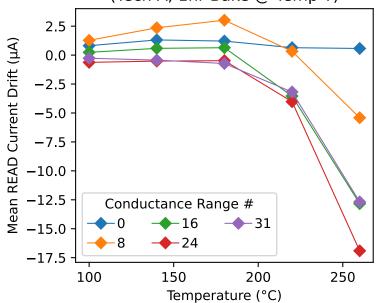
Below are examples of conductance broadening behavior at different temperatures:

```
[13]: # Select ranges to study
      ranges = [0, 8, 16, 24, 31]
      # Conductance broadening behavior
      fig = plt.figure(figsize=(4, 2.7))
      ax = fig.add_subplot(111)
      ax.set title(f"READ Current Dist. Broadening\n(Tech {TECH}, 1hr Bake @ Temp T)")
      colors = plt.rcParams["axes.prop_cycle"].by_key()["color"]
      for temp, color in zip(settings["temps"], colors):
          for r in ranges:
              gx = np.linspace(0, settings["gmax"]*1.1e6, 500)
              gvals = data[(data["range"] == r) & (data["temp"] == temp)]["g"]
              pdf = scipy.stats.gaussian_kde(gvals*1e6).pdf(gx)
              plt.plot(gx*0.2, pdf, color=color, label=f"T={temp}°C" if r==0 else_
       →None, linewidth=0.8)
      ax.legend(ncol=2, handletextpad=0.2)
      ax.set_xlim(0, settings["gmax"]*1.1e6*0.2)
      ax.set_ylim(*settings["gbroad_temp_ylim"])
      ax.set_xlabel("READ Current (µA)")
      ax.set ylabel("KDE Probability Density")
      plt.savefig(f"figs/tech{TECH}/broadening-temp-i.pdf", bbox_inches="tight")
      plt.show()
```



```
[14]: # Mean drift behavior (temperature dependence)
      fig = plt.figure(figsize=(4, 3.5))
      ax = fig.add_subplot(111)
      ax.set_title(f"Mean READ Current Drift vs. Temperature\n(Tech {TECH}, 1hr Bake_
      →@ Temp T)")
      colors = plt.rcParams["axes.prop_cycle"].by_key()["color"]
      for r, color in zip(ranges, colors):
          d = data[data["range"] == r]
          gi = d.groupby("temp").mean()["gi"]*1e6
          gf = d.groupby("temp").mean()["g"]*1e6
          deltag = gf - gi
          plt.plot(deltag.index, deltag * 0.2, '-D', color=color, label=r,__
       \rightarrowlinewidth=0.8)
      ax.legend(title="Conductance Range #", ncol=2 if TECH == 'C' else 3,
       →handletextpad=0.2)
      if "gmeandrift_temp_ylim" in settings:
          ax.set_ylim(*[v*0.2 for v in settings["gmeandrift_temp_ylim"]])
      ax.set_xlabel("Temperature (°C)")
      ax.set_ylabel("Mean READ Current Drift (µA)")
      plt.savefig(f"figs/tech{TECH}/mean-drift-vs-temp-i.pdf", bbox_inches="tight")
      plt.show()
```

Mean READ Current Drift vs. Temperature (Tech A, 1hr Bake @ Temp T)



```
[15]: # Variance behavior (temperature dependence)
      fig = plt.figure(figsize=(4, 3.5))
      ax = fig.add_subplot(111)
      ax.set_title(f"READ Current Variance vs. Temperature\n(Tech {TECH}, 1hr Bake @_
      →Temp T)")
      colors = plt.rcParams["axes.prop_cycle"].by_key()["color"]
      for r, color in zip(ranges, colors):
          d = data[data["range"] == r]
          gfvar = d.groupby("temp").var()["g"]*(1e6**2)
          plt.plot(gfvar.index, gfvar*0.2**2, '-D', color=color, label=r, linewidth=0.
      ⇔8)
      ax.legend(title="Cond. Range #", ncol=1, handletextpad=0.2)
      if "gvar_temp_ylim" in settings:
          ax.set_ylim(*[v*0.2**2 for v in settings["gvar_temp_ylim"]])
      ax.set xlabel("Temperature (°C)")
      ax.set_ylabel("READ Current Variance (µA$^2$)")
      plt.savefig(f"figs/tech{TECH}/var-vs-temp-i.pdf", bbox inches="tight")
      plt.show()
```

READ Current Variance vs. Temperature (Tech A, 1hr Bake @ Temp T) 140 -Cond. Range # 120 **→**0 READ Current Variance (μA^2) |8 100 **◆**−16 -24 80 60 40 20 0 150 200 100 250 Temperature (°C)