### Technology B Relaxation

July 24, 2021

#### 1 RRAM Relaxation Data Notebook

This notebook contains the analysis on empirical RRAM relaxation data across three technologies (A, B, C). It loads and processes the measurements taken for each technology.

```
[1]: # Imports
   import json
   import matplotlib.pyplot as plt
   import numpy as np
   import pandas as pd
   import scipy.signal
   import scipy.stats
   # from matplotlib.offsetbox import AnchoredText

%config InlineBackend.figure_format = 'svg'
```

#### 1.1 Load the technology and its settings

Below, choose which technology to load data and settings for:

```
[2]: # Choose technology here
TECH = 'B'

# Load settings for technology
with open(f"data/tech{TECH}/settings.json") as sfile:
    settings = json.load(sfile)
```

#### 1.2 Time series analysis

In this section, we will look at example time series data on a log scale and also examine the power spectral density (PSD). First, let us load the time series data:

```
[]: # Load data for technology
data = np.loadtxt(f"data/tech{TECH}/tsdata.min.tsv.gz", delimiter='\t',

→usecols=range(settings["ts_npts"]))
```

#### 1.2.1 Example Time Series Data

Below, we can look at the time series data for the ranges chosen above:

```
[]: # Plot example time series data
    fig = plt.figure(figsize=(4,2.7))
     ax = fig.add_subplot(111)
     ax.set_title(f"Conductance Time Series Examples\n(Tech {TECH}, Room Temp)")
     for i, r in enumerate([0, 8, 16, 31]):
         # Select data
         d = data[i,2:]
         # Plot time series data
         plt.plot(np.arange(0, len(d)/settings["fs"], 1/settings["fs"]), d*1e6, __
     →label=r, linewidth=0.8)
     # Format and display
     ax.legend(title="Range #", ncol=4, loc=9)
     ax.set_ylim(*settings["ts_ylim"])
     ax.set_xlabel("Time (s)")
     ax.set ylabel("Meas. Conductance (µS)")
     ax.set xscale("log")
     plt.savefig(f"figs/tech{TECH}/time-series.pdf", bbox_inches="tight")
    plt.show()
```

#### 1.2.2 Power Spectral Density (PSD)

In this section, we will look at the PSDs to understand the relaxation behavior better:

```
[]: # Plot power spectral density (PSD)
     fig = plt.figure(figsize=(4,4))
     ax = fig.add_subplot(111)
     ax.set_title(f"Conductance Power Spectral Density\n(Tech {TECH}, Room Temp)")
     slopes = []
     for i, r in enumerate([0, 8, 16, 31]):
         # Select data
         d = data[i,2:]
         # # Lomb-Scargle PSD
         \# f = np.logspace(np.log10(1/600), np.log10(2), 500)
         # f = np.logspace(np.log10(2), np.log10(400/2), 1000)
         \# p = scipy.signal.lombscargle(d["time"], d["g"], f)
         # Welch PSD
         f, p = scipy.signal.welch(d, fs=settings["fs"],__
     →nperseg=settings["psd_nperseg"])
         plt.plot(f, p, label=r, linewidth=0.8)
         # # Power law fit
         # a, b = np.polyfit(np.log(f[[30,-30]]), np.log(p[[30,-30]]), 1)
         # print(f"Range {r} slope: {a}")
```

```
# slopes.append(a)
    # plt.plot(f[1:], np.exp(a*np.log(f[1:]) + b), 'k--', zorder=10, ___
 \rightarrow linewidth=2)
    # # 1/f fit
    # fitfn = lambda logf, A: A - logf
    # params, _ = scipy.optimize.curve_fit(fitfn, np.log(f), np.log(p))
    \# A = params[0]
    # print(A)
    # plt.plot(f, np.exp(fitfn(np.loq(f), A)), 'k--', zorder=10, linewidth=2)
# Format and display
# ax.add artist(AnchoredText("Slopes: [%.2f, %.2f]" % (max(slopes), u
→min(slopes)), loc=1, frameon=False))
plt.plot(*settings["psd_fpts"], 'k--', zorder=10, linewidth=4)
if "psd_f2pts" in settings:
    plt.plot(*settings["psd_f2pts"], 'k--', zorder=10, linewidth=4)
ax.legend(title="Range #", ncol=2, loc=3)
ax.set_xlabel("Frequency (Hz)")
ax.set_ylabel("Power Spectral Density (S$^2$/Hz)")
ax.set_xscale("log")
ax.set_xlim(*settings["psd_xlim"])
ax.set_ylim(*settings["psd_ylim"])
ax.set_yscale("log")
plt.text(*settings["psd_ftextloc"], "1/f behavior")
if "psd_f2textloc" in settings:
    plt.text(*settings["psd f2textloc"], "1/f$^2$")
plt.savefig(f"figs/tech{TECH}/psd.pdf", bbox_inches="tight")
plt.show()
```

#### 1.3 Relaxation data analysis

Here, we will be analyzing the large dataset relaxation behavior. We will examine: (1) examples of conductance distribution broadening behavior over time, (2) scatterplot of conductance deviation vs. conductance, (3) standard deviation vs. time for different starting conductance values. First let us load the data:

```
[3]: # Load data for technology

colnames = ["addr", "time", "r", "g", "gi", "range", "timept"]

data = pd.read_csv(f"data/tech{TECH}/relaxdata.min.tsv.gz", names=colnames,

→sep='\t')

data.head()
```

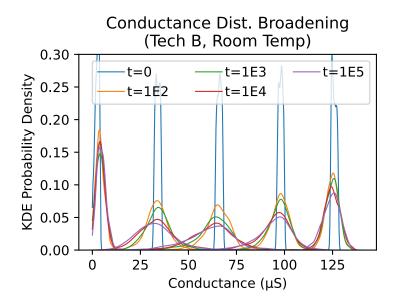
```
[3]:
       addr time
                                                  gi range timept
              0.0 416797.383397 0.000002 0.000002
    0
          0
                                                          0
                                                                  0
    1
          2
              0.0
                    94570.348039 0.000011 0.000011
                                                          2
                                                                  0
              0.0
    2
                    64998.894320 0.000015 0.000015
                                                          3
                                                                  0
```

```
3 6 0.0 62715.065513 0.000016 0.000016 3 0
4 8 0.0 82504.325744 0.000012 0.000012 3
```

#### 1.3.1 Conductance distribution broadening behavior

Below are examples of conductance broadening behavior over time:

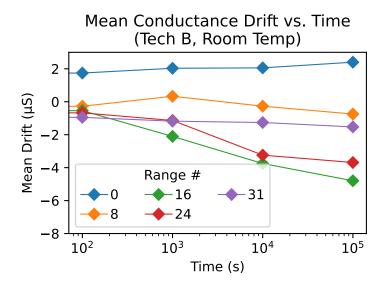
```
[4]: # Select ranges to study
     ranges = [0, 8, 16, 24, 31]
     # Conductance broadening behavior
     fig = plt.figure(figsize=(4, 2.7))
     ax = fig.add_subplot(111)
     ax.set_title(f"Conductance Dist. Broadening\n(Tech {TECH}, Room Temp)")
     colors = plt.rcParams["axes.prop_cycle"].by_key()["color"]
     for time, color in zip(settings["times"], colors):
         for r in ranges:
             gx = np.linspace(0, settings["gmax"]*1.1e6, 500)
             gvals = data[(data["range"] == r) & (data["timept"] == time)]["g"]
             pdf = scipy.stats.gaussian_kde(gvals*1e6).pdf(gx)
             label = (f''t=\{time\}'') if time < 100 else f''t=1E\{int(np.log10(time))\}''\}_{ij}
      \rightarrowif r == 0 else None
             plt.plot(gx, pdf, color=color, label=label, linewidth=0.8)
     ax.legend(ncol=3, handletextpad=0.2)
     ax.set_ylim(*settings["gbroad_ylim"])
     ax.set_xlabel("Conductance (µS)")
     ax.set_ylabel("KDE Probability Density")
     plt.savefig(f"figs/tech{TECH}/broadening-time.pdf", bbox_inches="tight")
     plt.show()
```



#### 1.3.2 Mean Drift and Variance Growth (Time Dependence)

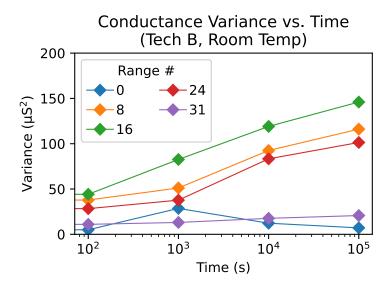
Here, we examine the drift of the distribution mean and variance growth as a function of time.

```
[5]: # Mean drift behavior (time dependence)
     fig = plt.figure(figsize=(4, 2.5))
     ax = fig.add_subplot(111)
     ax.set_title(f"Mean Conductance Drift vs. Time\n(Tech {TECH}, Room Temp)")
     colors = plt.rcParams["axes.prop_cycle"].by_key()["color"]
     for r, color in zip(ranges, colors):
         d = data[(data["range"] == r) & (data["gi"] <= settings["gmax"])]</pre>
         gi = d.groupby("timept").mean()["gi"]*1e6
         gf = d.groupby("timept").mean()["g"]*1e6
         deltag = gf - gi
         plt.plot(deltag.index, deltag, '-D', color=color, label=r, linewidth=0.8)
     ax.legend(title="Range #", ncol=2 if TECH == 'C' else 3, handletextpad=0.2)
     if "gmeandrift_t_ylim" in settings:
         ax.set_ylim(*settings["gmeandrift_t_ylim"])
     ax.set_xscale("log")
     ax.set_xlabel("Time (s)")
     ax.set_ylabel("Mean Drift (µS)")
     plt.savefig(f"figs/tech{TECH}/mean-drift-vs-time.pdf", bbox_inches="tight")
     plt.show()
```



```
[6]: # Variance behavior (time dependence)
fig = plt.figure(figsize=(4, 2.5))
ax = fig.add_subplot(111)
```

```
ax.set_title(f"Conductance Variance vs. Time\n(Tech {TECH}, Room Temp)")
colors = plt.rcParams["axes.prop_cycle"].by_key()["color"]
for r, color in zip(ranges, colors):
    d = data[(data["range"] == r) & (data["gi"] <= settings["gmax"])]
    gi = d.groupby("timept").mean()["gi"]*1e6
    gfvar = d.groupby("timept").var()["g"]*(1e6**2)
    plt.plot(gfvar.index, gfvar, '-D', color=color, label=r, linewidth=0.8)
ax.legend(title="Range #", ncol=3 if TECH == 'A' else 2, handletextpad=0.2)
if "gvar_t_ylim" in settings:
    ax.set_ylim(*settings["gvar_t_ylim"])
ax.set_xscale("log")
ax.set_xscale("log")
ax.set_xlabel("Time (s)")
ax.set_ylabel("Variance (µS$^2$)")
plt.savefig(f"figs/tech{TECH}/var-vs-time.pdf", bbox_inches="tight")
plt.show()</pre>
```



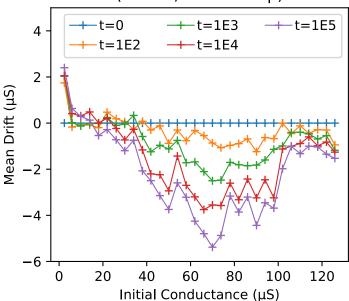
#### 1.3.3 Mean Drift and Variance Growth (Conductance Dependence)

Here, we examine the drift of the distribution mean and variance growth as a function of conductance.

```
[7]: # Mean drift behavior (conductance dependence)
fig = plt.figure(figsize=(4, 3.5))
ax = fig.add_subplot(111)
ax.set_title(f"Mean Drift vs. Init. Conductance\n(Tech {TECH}, Room Temp)")
colors = plt.rcParams["axes.prop_cycle"].by_key()["color"]
for time, color in zip(settings["times"], colors):
    d = data[(data["timept"] == time) & (data["gi"] <= settings["gmax"])]
    gi = d.groupby("range").mean()["gi"]*1e6</pre>
```

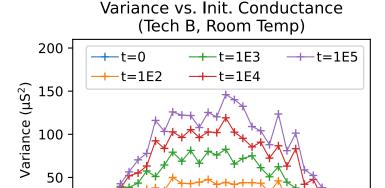
```
gf = d.groupby("range").mean()["g"]*1e6
  deltag = gf - gi
  label = (f"t={time}" if time < 100 else f"t=1E{int(np.log10(time))}")
  plt.plot(gi, deltag, '-+', color=color, label=label, linewidth=0.8)
ax.legend(ncol=3, handletextpad=0.2)
ax.set_ylim(*settings["gmeandrift_gi_ylim"])
ax.set_ylim(*settings["gmeandrift_gi_ylim"])
ax.set_ylabel("Initial Conductance (µS)")
ax.set_ylabel("Mean Drift (µS)")
plt.savefig(f"figs/tech{TECH}/mean-drift-vs-g.pdf", bbox_inches="tight")
plt.show()</pre>
```

## Mean Drift vs. Init. Conductance (Tech B, Room Temp)



```
[8]: # Variance behavior (conductance dependence)
fig = plt.figure(figsize=(4, 2.5))
ax = fig.add_subplot(111)
ax.set_title(f"Variance vs. Init. Conductance\n(Tech {TECH}, Room Temp)")
colors = plt.rcParams["axes.prop_cycle"].by_key()["color"]
for time, color in zip(settings["times"], colors):
    d = data[(data["timept"] == time) & (data["gi"] <= settings["gmax"])]
    gi = d.groupby("range").mean()["gi"]*1e6
    gfvar = (d.groupby("range")).var()["g"]*(1e6**2)
    label = (f"t={time}" if time < 100 else f"t=1E{int(np.log10(time))}")
    plt.plot(gi, gfvar, '-+', color=color, label=label, linewidth=0.8)
ax.legend(ncol=3, handletextpad=0.2)
ax.set_ylim(*settings["gvar_gi_ylim"])</pre>
```

```
ax.set_xlabel("Initial Conductance (µS)")
ax.set_ylabel("Variance (µS$^2$)")
plt.savefig(f"figs/tech{TECH}/var-vs-g.pdf", bbox_inches="tight")
plt.show()
```



#### 1.4 Temperature dependence analysis via 1hr bake

0

20

40

60

Initial Conductance (µS)

80

100

120

Here, we analyze the effect of baking on the distribution broadening. In particular, we will examine examples of the conductance distributions broadening for different temperatures and then analyze the temperature-dependent mean drift and variance. We can first load the data and preprocess it a little bit:

```
[9]: # Load data for technology
    colnames = ["addr", "time", "r", "g", "temp"]
    data = pd.read_csv(f"data/tech{TECH}/bake.tsv.gz", names=colnames, sep='\t')

# Get conductance range
    data["gi"] = data.groupby("addr")["g"].transform("first")
    data["range"] = np.int32(data["gi"] / settings["gmax"] * 32)

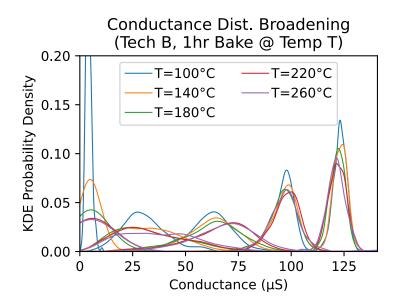
# Show data
    data.head()
```

```
[9]:
         addr
               time
                                                temp
                                                                 range
        32768
                0.0
                     302397.414786
                                     0.000003
                                                 100
                                                      0.000003
        32770
                0.0
                     221077.221379
                                     0.000005
                                                 100
                                                      0.000005
     1
                                                                     1
     2
        32772
                0.0 145631.108730
                                     0.000007
                                                      0.000007
                                                 100
                                                                     1
     3
        32774
                0.0
                       54867.601004
                                     0.000018
                                                 100
                                                      0.000018
                                                                     4
       32776
                0.0
                       88193.354991
                                     0.000011
                                                 100
                                                      0.000011
                                                                     2
```

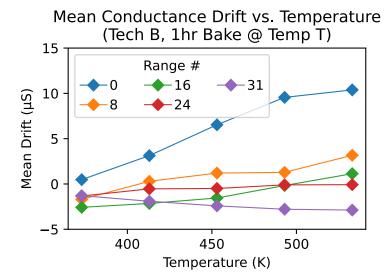
#### 1.4.1 Conductance distribution broadening behavior

Below are examples of conductance broadening behavior at different temperatures:

```
[10]: # Select ranges to study
     ranges = [0, 8, 16, 24, 31]
      # Conductance broadening behavior
     fig = plt.figure(figsize=(4, 2.7))
     ax = fig.add_subplot(111)
     ax.set_title(f"Conductance Dist. Broadening\n(Tech {TECH}, 1hr Bake @ Temp T)")
     colors = plt.rcParams["axes.prop_cycle"].by_key()["color"]
     for temp, color in zip(settings["temps"], colors):
         for r in ranges:
             gx = np.linspace(0, settings["gmax"]*1.1e6, 500)
             gvals = data[(data["range"] == r) & (data["temp"] == temp) &__
       pdf = scipy.stats.gaussian_kde(gvals*1e6).pdf(gx)
             plt.plot(gx, pdf, color=color, label=f"T={temp}°C" if r==0 else None,
       \rightarrowlinewidth=0.8)
     ax.legend(ncol=2, handletextpad=0.2)
     ax.set_xlim(0,settings["gmax"]*1.1e6)
     ax.set_ylim(*settings["gbroad_temp_ylim"])
     ax.set xlabel("Conductance (µS)")
     ax.set_ylabel("KDE Probability Density")
     plt.savefig(f"figs/tech{TECH}/broadening-temp.pdf", bbox_inches="tight")
     plt.show()
```



```
[11]: # Mean drift behavior (temperature dependence)
      fig = plt.figure(figsize=(4, 2.5))
      ax = fig.add_subplot(111)
      ax.set_title(f"Mean Conductance Drift vs. Temperature\n(Tech {TECH}, 1hr Bake @_
      →Temp T)")
      colors = plt.rcParams["axes.prop_cycle"].by_key()["color"]
      for r, color in zip(ranges, colors):
          d = data[(data["range"] == r) & (data["gi"] <= settings["gmax"])]</pre>
          gi = d.groupby("temp").mean()["gi"]*1e6
          gf = d.groupby("temp").mean()["g"]*1e6
          deltag = gf - gi
          plt.plot(deltag.index + 273, deltag, '-D', color=color, label=r, __
       →linewidth=0.8)
      ax.legend(title="Range #", ncol=2 if TECH == 'C' else 3, handletextpad=0.2)
      if "gmeandrift temp ylim" in settings:
          ax.set_ylim(*settings["gmeandrift_temp_ylim"])
      ax.set_xlabel("Temperature (K)")
      ax.set_ylabel("Mean Drift (μS)")
      plt.savefig(f"figs/tech{TECH}/mean-drift-vs-temp.pdf", bbox_inches="tight")
      plt.show()
```



# Conductance Variance vs. Temperature (Tech B, 1hr Bake @ Temp T)

