

Assignment Code: DS-AG-005

Statistics Basics| Assignment

Question 1: What is the difference between descriptive statistics and inferential statistics? Explain with examples.

Answer: **Descriptive statistics**

Descriptive statistics are about **summarizing and describing the data you already have**. They don't try to go beyond the dataset or make predictions—they just tell you *what the data looks like*.

Common tools:

- Mean, median, mode
- Range, variance, standard deviation
- Tables, charts, graphs (bar charts, histograms, pie charts)

Example:

Suppose a teacher records the exam scores of **30 students in a class**.

- The **average score** is 72
- The **highest score** is 95 and the **lowest** is 40
- A bar chart shows how many students fall into each score range

All of this is **descriptive statistics** because it only summarizes the scores of those 30 students—nothing more.

Inferential statistics

Inferential statistics go a step further. They use **sample data to draw conclusions or make predictions about a larger population**.

Common tools:

- Hypothesis testing (t-test, chi-square test, ANOVA)
- Confidence intervals
- Regression analysis
- Correlation

Example:

Now imagine those same 30 students are a **sample** taken from a school with **1,000 students**.

- You use the sample's average score to **estimate the average score of all 1,000 students**
- You test whether **boys and girls differ significantly in their exam performance**
- You calculate a **95% confidence interval** for the true average score of the entire school

This is **inferential statistics** because you're using a sample to make conclusions about a **population**.

Question 2: What is sampling in statistics? Explain the differences between random and stratified sampling.

Answer: **Sampling in statistics**

Sampling is the process of selecting a **subset (sample)** from a **larger group (population)** in order to study it.

Because studying an entire population is often too costly, time-consuming, or impractical, statisticians use samples to make conclusions about the whole population.

Example:

Instead of surveying **all voters in a country**, a researcher surveys **2,000 voters** to predict election outcomes.

Random sampling

In **random sampling**, every individual in the population has an equal chance of being selected.

How it works:

- Names are chosen using a lottery method or random number generator
- Selection is completely unbiased

Example:

A school has 1,000 students. Each student is given a number, and **100 numbers are selected randomly** by a computer.

Those 100 students form the sample.

Key features:

- Simple and unbiased
 - Easy to understand
 - May accidentally over- or under-represent some groups
-

Stratified sampling

In **stratified sampling**, the population is first divided into **subgroups (strata)** based on a specific characteristic (such as age, gender, class, or income).

Then **random samples are taken from each subgroup**, usually in proportion to their size.

Example:

A school has:

- 60% female students
- 40% male students

If a sample of 100 students is needed:

- 60 females are randomly selected
- 40 males are randomly selected

This ensures both groups are properly represented.

Key features:

- Ensures representation of all important subgroups
- More accurate when the population is diverse
- Slightly more complex than random sampling

Question 3: Define mean, median, and mode. Explain why these measures of central tendency are important.

Answer: **Mean**

The **mean** is the **average** of a set of numbers.

It is found by adding all the values and dividing by the total number of values.

Formula:

$$\text{Mean} = (\text{Sum of all observations}) \div (\text{Number of observations})$$

Example:

For the data: 2, 4, 6, 8

$$\text{Mean} = (2 + 4 + 6 + 8) \div 4 = 5$$

Median

The **median** is the **middle value** of a dataset when the data are arranged in ascending or descending order.

- If the number of observations is **odd**, the median is the middle number.
- If the number of observations is **even**, the median is the average of the two middle numbers.

Example:

Data: 3, 5, 7, 9, 11

$$\text{Median} = 7$$

Mode

The **mode** is the value that **occurs most frequently** in a dataset.

A dataset may have:

- One mode (unimodal)
- More than one mode (bimodal or multimodal)
- No mode

Example:

Data: 2, 4, 4, 6, 8

Mode = 4

Importance of measures of central tendency

Measures of central tendency are important because they:

1. Summarize large data sets

They represent a large amount of data with a single value, making it easier to understand.

2. Describe the typical or central value

They show where most data values tend to cluster.

3. Help in comparison

Means, medians, or modes can be used to compare different datasets (e.g., average marks of two classes).

4. Support decision-making

They are used in fields like economics, education, business, and health to guide planning and policy decisions.

5. Handle different types of data

- Mean is useful for numerical data
- Median is best when there are extreme values
- Mode works well for categorical data

Question 4: Explain skewness and kurtosis. What does a positive skew imply about the

Data

Answer: **Kurtosis**

Kurtosis measures the **peakedness or flatness** of a distribution compared to a normal distribution.

It also indicates how **heavy or light the tails** of the distribution are.

Types of kurtosis

1. **Leptokurtic**

- Very sharp peak
- Heavy tails
- More extreme values (outliers)

2. **Mesokurtic**

- Moderate peak
- Similar to a normal distribution

3. **Platykurtic**

- Flat peak
 - Light tails
 - Fewer extreme values
-

What does a positive skew imply about the data?

A **positive skew** implies that:

- Most observations are **smaller values**
- A few **large values** stretch the distribution to the right
- The **mean is pulled upward** by extreme high values
- The data are **not symmetrically distributed**

Question 5: Implement a Python program to compute the mean, median, and mode of a given list of numbers

Answer:

```
from collections import Counter
```

```
def calculate_mean(numbers):
    return sum(numbers) / len(numbers)

def calculate_median(numbers):
    numbers.sort()
    n = len(numbers)
    mid = n // 2

    if n % 2 == 0:
        return (numbers[mid - 1] + numbers[mid]) / 2
    else:
        return numbers[mid]

def calculate_mode(numbers):
    freq = Counter(numbers)
    max_freq = max(freq.values())
    modes = [num for num, count in freq.items() if count == max_freq]

    if len(modes) == len(numbers):
        return None # No mode
    else:
        return modes[0]
```

```
return modes

# Example usage
data = [2, 4, 4, 6, 8, 10]

mean = calculate_mean(data)
median = calculate_median(data)
mode = calculate_mode(data)

print("Mean:", mean)
print("Median:", median)
print("Mode:", mode)
```

Question 6: Compute the covariance and correlation coefficient between the following two datasets provided as lists in Python:

```
list_x = [10, 20, 30, 40, 50]
list_y = [15, 25, 35, 45, 60]
```

Answer:import math

```
# Given lists
list_x = [10, 20, 30, 40, 50]
list_y = [15, 25, 35, 45, 60]

n = len(list_x)
```

```

# Mean of X and Y

mean_x = sum(list_x) / n

mean_y = sum(list_y) / n


# Covariance

covariance = sum((list_x[i] - mean_x) * (list_y[i] - mean_y) for i in range(n)) / n


# Standard deviations

std_x = math.sqrt(sum((x - mean_x) ** 2 for x in list_x) / n)

std_y = math.sqrt(sum((y - mean_y) ** 2 for y in list_y) / n)


# Correlation coefficient

correlation = covariance / (std_x * std_y)

print("Covariance:", covariance)
print("Correlation Coefficient:", correlation)

```

Question 7: Write a Python script to draw a boxplot for the following numeric list and identify its outliers. Explain the result:

```
data = [12, 14, 14, 15, 18, 19, 19, 21, 22, 22, 23, 23, 24, 26, 29, 35]
```

Answer: import matplotlib.pyplot as plt
import numpy as np

```
# Data

data = [12, 14, 14, 15, 18, 19, 19, 21, 22, 22, 23, 23, 24, 26, 29, 35]

# Convert to NumPy array

arr = np.array(data)

# Quartiles

Q1 = np.percentile(arr, 25)

Q3 = np.percentile(arr, 75)

IQR = Q3 - Q1

# Outlier limits

lower_bound = Q1 - 1.5 * IQR

upper_bound = Q3 + 1.5 * IQR

# Identify outliers

outliers = arr[(arr < lower_bound) | (arr > upper_bound)]

# Boxplot

plt.boxplot(arr)

plt.title("Boxplot of Data")

plt.ylabel("Values")

plt.show()
```

```
print("Q1:", Q1)
print("Q3:", Q3)
print("IQR:", IQR)
print("Outliers:", outliers)
```

Question 8: You are working as a data analyst in an e-commerce company. The marketing team wants to know if there is a relationship between advertising spend and daily sales.

- Explain how you would use covariance and correlation to explore this relationship.
- Write Python code to compute the correlation between the two lists:

```
advertising_spend = [200, 250, 300, 400, 500]
daily_sales = [2200, 2450, 2750, 3200, 4000]
```

Answer:import math

```
# Given data
advertising_spend = [200, 250, 300, 400, 500]
daily_sales = [2200, 2450, 2750, 3200, 4000]
```

```
n = len(advertising_spend)
```

```
# Means
mean_x = sum(advertising_spend) / n
mean_y = sum(daily_sales) / n
```

```
# Covariance

covariance = sum(
    (advertising_spend[i] - mean_x) * (daily_sales[i] - mean_y)
    for i in range(n)
) / n

# Standard deviations

std_x = math.sqrt(sum((x - mean_x) ** 2 for x in advertising_spend) / n)
std_y = math.sqrt(sum((y - mean_y) ** 2 for y in daily_sales) / n)

# Correlation coefficient

correlation = covariance / (std_x * std_y)

print("Covariance:", covariance)
print("Correlation Coefficient:", correlation)
```