1. Physical Inspiration: Turbulent Flow and Reynolds Decomposition

From turbulence theory:

$$u(x,t) = u_bar(x) + u_prime(x,t)$$

We analogously define for temperature:

$$T(t) = T_bar(t) + T_prime(t)$$

Where:

- T_bar(t): Stable rolling mean over time window -- base state.
- T_prime(t): Fluctuating component -- anomalies, faults, or sensor issues.

2. Feature Definitions

Rolling Mean (T_bar): Mean temperature in a 1-hour window.

Delta Upper/Lower (DeltaUpper, DeltaLower): Spread from mean -> measures turbulence.

1st Derivative (DeltaT): Rate of temperature change.

2nd Derivative (Delta2T): Acceleration -- flags sudden spikes.

3. System State Mapping

A. Window Classification:

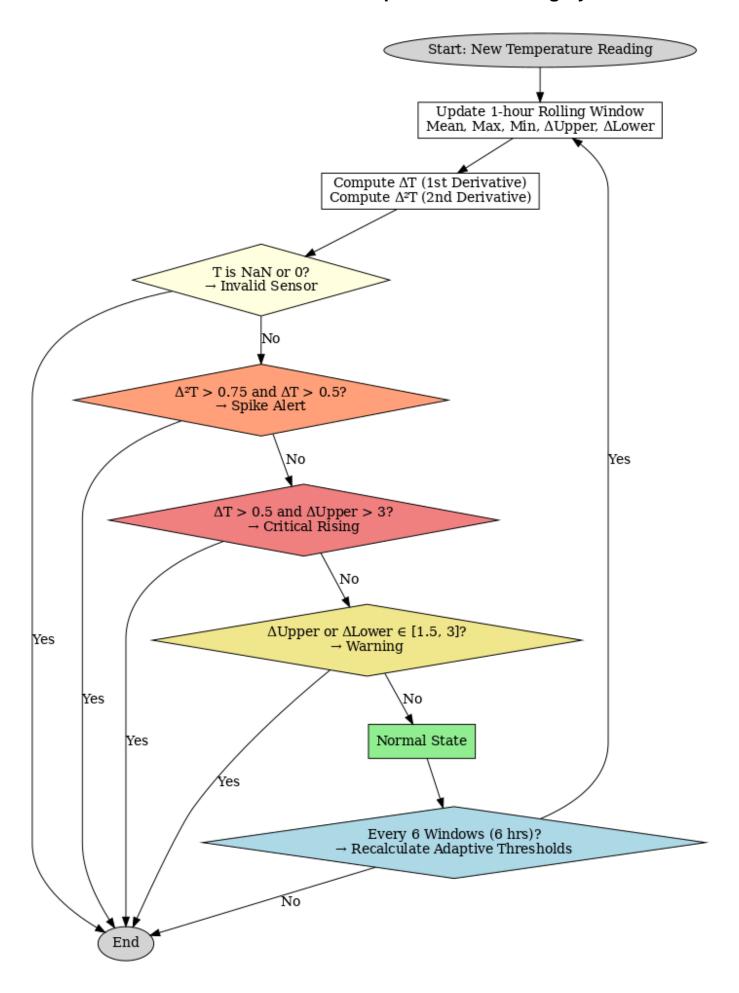
- Delta < 1.5C -> Normal
- Delta in [1.5, 3.0] -> Warning
- Delta > 3.0 -> Critical
- B. Derivative Thresholds:
- |DeltaT| > 0.5 -> Temperature drift
- |Delta2T| > 0.75 -> Spikes or quick shifts

4. Decision Tree Logic

- 1. Update 1-hour rolling window: Mean, Max, Min, DeltaUpper, DeltaLower
- 2. Compute DeltaT, Delta2T
- 3. If T is NaN or 0 -> Invalid
- 4. If Delta2T > 0.75 and DeltaT > 0.5 -> Spike Alert
- 5. If DeltaT > 0.5 and DeltaUpper > 3 -> Critical
- 6. If DeltaUpper or DeltaLower in [1.5, 3] -> Warning

- 7. Else -> Normal
- 8. Every 6 hrs: Adapt thresholds

5. Algorithm Flowchart



Plot: Temperature vs Rolling Stats

Plot: Temperature Gradient (1st Derivative)

Plot: Rate of Rate of Change (2nd Derivative)

Plot: Deviation from Rolling Mean

Plot: System Health Timeline