

VARIABLES	<i>msgs</i> , <i>nodeTS</i> , <i>nodeState</i> , <i>nodeLastWriter</i> , <i>issuedWriteTS</i> , <i>aliveNodes</i> , <i>receivedAcks</i>
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The consistent invariant: all alive nodes in valid state should have the same value / TS

$$HConsistent \triangleq \forall k, s \in aliveNodes : \begin{array}{l} \vee nodeState[k] \neq \text{"valid"} \\ \vee nodeState[s] \neq \text{"valid"} \\ \vee nodeTS[k] = nodeTS[s] \end{array}$$
$$\begin{aligned}
HMessage &\triangleq \\
&[type : \{ "INV", "ACK" \}, sender : NODES, \\
&\quad version : 0 .. MAX_VERSION, \\
&\quad tieBreaker : NODES] \\
&\cup \\
&[type : \{ "VAL" \}, \\
&\quad version : 0 .. MAX_VERSION, \\
&\quad tieBreaker : NODES]
\end{aligned}$$
$$\begin{array}{ll}
HTypeOK \triangleq & \text{The type correctness invariant} \\
\wedge \quad msgs & \subseteq HMessage \\
\wedge \quad aliveNodes & \subseteq NODES \\
\wedge \forall n \in NODES : receivedAcks[n] & \subseteq (NODES \setminus \{n\}) \\
\wedge \quad nodeLastWriter \in [NODES \rightarrow NODES] & \\
\wedge \quad issuedWriteTS \in [NODES \rightarrow [version : 0 .. MAX_VERSION, & \\
& tieBreaker : NODES]] \\
\wedge \quad nodeTS \in [NODES \rightarrow [version : 0 .. MAX_VERSION, & \\
& tieBreaker : NODES]] \\
\wedge \quad nodeState \in [NODES \rightarrow \{\text{"valid"}, \text{"invalid"}, \text{"invalid_write"}, & \\
& \text{"write"}, \text{"replay"}\}]
\end{array}$$
$$\begin{array}{ll}
HInit & \triangleq \text{The initial predicate} \\
\wedge \text{ msgs} & = \{\} \\
\wedge \text{ aliveNodes} & = NODES \\
\wedge \text{ receivedAcks} & = [n \in NODES \mapsto \{\}] \\
\wedge \text{ nodeState} & = [n \in NODES \mapsto \text{"valid"}] \\
\wedge \text{ nodeLastWriter} & = [n \in NODES \mapsto \text{CHOOSE } k \in NODES : \\
& \quad \forall m \in NODES : k \leq m]
\end{array}$$

$$\begin{array}{l}
\wedge \text{ nodeTS} \quad = [n \in \text{NODES} \mapsto [\text{version} \mapsto 0, \\
\quad \quad \quad \text{tieBreaker} \mapsto \\
\quad \quad \quad \text{CHOOSE } k \in \text{NODES} : \\
\quad \quad \quad \forall m \in \text{NODES} : k \leq m]] \\
\wedge \text{ issuedWriteTS} \quad = [n \in \text{NODES} \mapsto [\text{version} \mapsto 0, \\
\quad \quad \quad \text{tieBreaker} \mapsto \\
\quad \quad \quad \text{CHOOSE } k \in \text{NODES} : \\
\quad \quad \quad \forall m \in \text{NODES} : k \leq m]] \\
\hline
\text{send}(m) \triangleq \text{msgs}' = \text{msgs} \cup \{m\} \\
\text{receivedAllAcks}(n) \triangleq \text{receivedAcks}[n] = \text{NODES} \setminus \{n\} \\
\text{equalTS}(v1, tb1, v2, tb2) \triangleq \\
\quad \wedge \quad v1 = v2 \\
\quad \wedge \quad tb1 = tb2 \\
\text{greaterTS}(v1, tb1, v2, tb2) \triangleq \\
\quad \vee v1 > v2 \\
\quad \vee \wedge \quad v1 = v2 \\
\quad \quad \wedge \quad tb1 > tb2 \\
\text{isAlive}(n) \triangleq n \in \text{aliveNodes} \\
\text{nodeFailure} \triangleq \\
\quad \wedge \text{aliveNodes}' = \text{aliveNodes} \setminus \{\text{CHOOSE } k \in \text{aliveNodes} : \forall m \in \text{aliveNodes} : k \leq m\} \\
\quad \wedge \text{UNCHANGED } \langle \text{msgs}, \text{nodeState}, \text{nodeTS}, \text{nodeLastWriter}, \text{issuedWriteTS}, \text{receivedAcks} \rangle \\
\hline
\text{HRead}(n) \triangleq \\
\quad \wedge \text{nodeState}[n] = \text{"valid"} \\
\quad \wedge \text{UNCHANGED } \langle \text{msgs}, \text{nodeTS}, \text{nodeState}, \text{nodeLastWriter}, \\
\quad \quad \quad \text{aliveNodes}, \text{issuedWriteTS}, \text{receivedAcks} \rangle \\
\text{HWrite}(n) \triangleq \\
\quad \wedge \text{nodeState}[n] \in \{\text{"valid"}\} \\
\quad \wedge \text{nodeTS}[n].\text{version} < \text{MAX_VERSION} \\
\quad \wedge \text{receivedAcks}' = [\text{receivedAcks} \text{ EXCEPT } ![n] = \{\}] \\
\quad \wedge \text{nodeLastWriter}' = [\text{nodeLastWriter} \text{ EXCEPT } ![n] = n] \\
\quad \wedge \text{nodeState}' = [\text{nodeState} \text{ EXCEPT } ![n] = \text{"write"}] \\
\quad \wedge \text{nodeTS}' = [\text{nodeTS} \text{ EXCEPT } ![n].\text{version} = \\
\quad \quad \quad \text{nodeTS}[n].\text{version} + 1, \\
\quad \quad \quad ![n].\text{tieBreaker} = n] \\
\quad \wedge \text{issuedWriteTS}' = [\text{issuedWriteTS} \text{ EXCEPT } ![n].\text{version} = \\
\quad \quad \quad \text{nodeTS}[n].\text{version} + 1, \\
\quad \quad \quad ![n].\text{tieBreaker} = n] \\
\quad \wedge \text{send}([type \mapsto \text{"INV"}, \\
\quad \quad \quad sender \mapsto n,
\end{array}$$

$$\begin{aligned}
& \text{version} \mapsto \text{nodeTS}[n].\text{version} + 1, \\
& \text{tieBreaker} \mapsto n]) \\
& \wedge \text{UNCHANGED } \langle \text{aliveNodes} \rangle
\end{aligned}$$

$$\begin{aligned}
H\text{ReplayWrite}(n) & \triangleq \\
& \wedge \text{nodeState}[n] = \text{"invalid"} \\
& \wedge \neg \text{isAlive}(\text{nodeLastWriter}[n]) \\
& \wedge \text{nodeLastWriter}' = [\text{nodeLastWriter} \text{ EXCEPT } ![n] = n] \\
& \wedge \text{nodeState}' = [\text{nodeState} \text{ EXCEPT } ![n] = \text{"replay"}] \\
& \wedge \text{receivedAcks}' = [\text{receivedAcks} \text{ EXCEPT } ![n] = \{\}] \\
& \wedge \text{issuedWriteTS}' = [\text{issuedWriteTS} \text{ EXCEPT } ![n] = \text{nodeTS}[n]] \\
& \wedge \text{send}([type \mapsto \text{"INV"}, \\
& \quad \text{sender} \mapsto n, \\
& \quad \text{version} \mapsto \text{nodeTS}[n].\text{version}, \\
& \quad \text{tieBreaker} \mapsto \text{nodeTS}[n].\text{tieBreaker}]) \\
& \wedge \text{UNCHANGED } \langle \text{nodeTS}, \text{aliveNodes} \rangle
\end{aligned}$$

$$\begin{aligned}
H\text{RcvAck}(n) & \triangleq \\
& \exists m \in \text{msgs} : \\
& \wedge m.\text{type} = \text{"ACK"} \\
& \wedge m.\text{sender} \neq n \\
& \wedge m.\text{sender} \notin \text{receivedAcks}[n] \\
& \wedge \text{equalTS}(m.\text{version}, \\
& \quad m.\text{tieBreaker}, \\
& \quad \text{issuedWriteTS}[n].\text{version}, \\
& \quad \text{issuedWriteTS}[n].\text{tieBreaker}) \\
& \wedge \text{nodeState}[n] \in \{\text{"write"}, \text{"invalid_write"}, \text{"replay"}\} \\
& \wedge \text{receivedAcks}' = [\text{receivedAcks} \text{ EXCEPT } ![n] = \\
& \quad \text{receivedAcks}[n] \cup \{m.\text{sender}\}] \\
& \wedge \text{UNCHANGED } \langle \text{msgs}, \text{nodeLastWriter}, \text{issuedWriteTS}, \\
& \quad \text{aliveNodes}, \text{nodeTS}, \text{nodeState} \rangle
\end{aligned}$$

$$\begin{aligned}
H\text{SendVals}(n) & \triangleq \\
& \wedge \text{nodeState}[n] \in \{\text{"write"}, \text{"replay"}\} \\
& \wedge \text{receivedAllAcks}(n) \\
& \wedge \text{nodeState}' = [\text{nodeState} \text{ EXCEPT } ![n] = \text{"valid"}] \\
& \wedge \text{send}([type \mapsto \text{"VAL"}, \\
& \quad \text{version} \mapsto \text{nodeTS}[n].\text{version}, \\
& \quad \text{tieBreaker} \mapsto \text{nodeTS}[n].\text{tieBreaker}]) \\
& \wedge \text{UNCHANGED } \langle \text{nodeTS}, \text{nodeLastWriter}, \text{issuedWriteTS}, \\
& \quad \text{aliveNodes}, \text{receivedAcks} \rangle
\end{aligned}$$

$$\begin{aligned}
H\text{CoordinatorActions}(n) & \triangleq \\
& \vee H\text{Read}(n) \\
& \vee H\text{ReplayWrite}(n) \text{ this is for failures} \\
& \vee H\text{Write}(n)
\end{aligned}$$

$\vee HRcvAck(n)$
 $\vee HSendVals(n)$

$HRcvInv(n) \triangleq$
 $\exists m \in msgs :$
 $\wedge m.type = \text{"INV"}$
 $\wedge m.sender \neq n$
 $\wedge send([type \mapsto \text{"ACK"},$
 $\quad sender \mapsto n,$
 $\quad version \mapsto m.version,$
 $\quad tieBreaker \mapsto m.tieBreaker])$
 $\wedge \vee \wedge greaterTS(m.version,$
 $\quad m.tieBreaker,$
 $\quad nodeTS[n].version,$
 $\quad nodeTS[n].tieBreaker)$
 $\wedge nodeLastWriter' = [nodeLastWriter \text{ EXCEPT } ![n] = m.sender]$
 $\wedge nodeTS' = [nodeTS \text{ EXCEPT } ![n].version = m.version,$
 $\quad ![n].tieBreaker = m.tieBreaker]$
 $\wedge \vee \wedge nodeState[n] \in \{\text{"valid"}, \text{"invalid"}, \text{"replay"}\}$
 $\wedge nodeState' = [nodeState \text{ EXCEPT } ![n] = \text{"invalid"}]$
 $\vee \wedge nodeState[n] \in \{\text{"write"}, \text{"invalid_write"}\}$
 $\wedge nodeState' = [nodeState \text{ EXCEPT } ![n] = \text{"invalid_write"}]$
 $\vee \wedge \neg greaterTS(m.version,$
 $\quad m.tieBreaker,$
 $\quad nodeTS[n].version,$
 $\quad nodeTS[n].tieBreaker)$
 $\wedge \text{UNCHANGED } \langle nodeState, nodeTS, nodeLastWriter \rangle$
 $\wedge \text{UNCHANGED } \langle issuedWriteTS, aliveNodes, receivedAcks \rangle$

$HRcvVal(n) \triangleq$
 $\exists m \in msgs :$
 $\wedge nodeState[n] \neq \text{"valid"}$
 $\wedge m.type = \text{"VAL"}$
 $\wedge equalTS(m.version,$
 $\quad m.tieBreaker,$
 $\quad nodeTS[n].version,$
 $\quad nodeTS[n].tieBreaker)$
 $\wedge nodeState' = [nodeState \text{ EXCEPT } ![n] = \text{"valid"}]$
 $\wedge \text{UNCHANGED } \langle msgs, nodeTS, nodeLastWriter, issuedWriteTS,$
 $\quad aliveNodes, receivedAcks \rangle$

$HFollowerActions(n) \triangleq$
 $\vee HRcvInv(n)$
 $\vee HRcvVal(n)$

$$HNext \triangleq$$

$$\begin{aligned} &\vee \exists n \in NODES : \\ &\quad \vee HFollowerActions(n) \\ &\quad \vee HCoordinatorActions(n) \\ &\quad \vee nodeFailure \text{ this is for failures} \end{aligned}$$

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