

EXTENDS *ZeusOwnership*

$sharing\_ok \triangleq \forall nn \in APP\_LIVE\_NODES : \vee \neg has\_data(nn)$   
 $\vee tState[nn] = \text{"valid"}$

$arb\_replay(n) \triangleq$   
 $\wedge upd\_rEID(n)$   
 $\wedge upd\_o\_meta\_driver(n, oTS[n].ver, oTS[n].tb)$   
 $\wedge o\_send\_inv(n, n, oTS[n], oVector[n], rTS[n], rID[n], rType[n])$

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Requester replays msg after a failure

$OFRequester \triangleq$   
 $\exists n \in APP\_LIVE\_NODES :$   
 $\wedge oState[n] = \text{"request"}$   
 $\wedge rEID[n] < mEID$   
 $\wedge upd\_rEID(n)$   
 $\wedge o\_send\_req(rTS[n], rID[n], rType[n])$   
 $\wedge unchanged\_mtco$

$OFDriverRequester \triangleq$  waits for sharing-ok + computes next *oVec* transitions to *valid* +  
send vals with the proper changes in the *oVec*  
 $\exists n \in LB\_LIVE\_NODES :$   
 $\wedge oState[n] = \text{"drive"}$   
 $\wedge has\_rcvd\_all\_ACKs(n)$   
 $\wedge \neg requester\_is\_alive(n)$   
 $\wedge o\_send\_val(oTS[n])$   
 $\wedge upd\_o\_meta(n, oTS[n].ver, oTS[n].tb, \text{"valid"}, 0, post\_oVec(n, 0, oVector[n]), \{\})$   
 $\wedge unchanged\_mtrc$

$OFArbReplay \triangleq$  drivers resets acks and replays msg on arbiter failures  
if the failed arbiter was an owner we need to wait for sharing-ok  
for convinience arb-replays happen on any failure (e.g., requester)

$\exists n \in mAliveNodes :$   
 $\wedge (oState[n] = \text{"drive"} \vee oState[n] = \text{"invalid"})$   
 $\wedge (n \in LB\_LIVE\_NODES \vee oVector[n].owner = n)$   
 $\wedge rEID[n] < mEID$   
 $\wedge \vee oVector[n].owner \in mAliveNodes$   
 $\vee sharing\_ok$   
 $\wedge arb\_replay(n)$   
 $\wedge unchanged\_mtc$

$OLBArbiterACK \triangleq$  ACK an INV message which has the same as local *s\_ts* but wasn't applied  
 $\exists n \in LB\_LIVE\_NODES : \exists m \in oMmsgs :$

$\wedge \neg inv\_to\_be\_applied(n, m)$   
 $\wedge o\_rcv\_inv\_equal\_ts(m, n)$   
 $\wedge o\_send\_ack(n, m.oTS, 0)$   
 $\wedge unchanged\_mtrco$

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$INV$  response to an owner who did an arb-replay due to a lost val  
 $OFMOArbiterLostVALOldReplay \triangleq$   
 $\exists l \in LB\_LIVE\_NODES : \exists a \in APP\_LIVE\_NODES :$   
 $\wedge oState[a] = \text{"drive"}$   
 $\wedge oVector[a].owner = a$   
 $\wedge is\_greaterTS(oTS[l], oTS[a])$   
 $\wedge o\_send\_inv(l, l, oTS[l], oVector[l], rTS[l], rID[l], rType[l])$   
 $\wedge unchanged\_mtrco$

message failures  
 $OFMOArbiterINVLostVAL \triangleq$  An  $INV$  is received (w/ higher ts) to a non-valid owner  
 who lost a  $VAL$  for the message that demoted him  
 $\exists n \in APP\_LIVE\_NODES : \exists m \in oMsgs :$   
 $\wedge oVector[n].owner = n$   
 $\wedge o\_rcv\_inv\_greater\_ts(m, n)$   
 $\wedge m.oVector.owner \neq n$   
 $\wedge upd\_o\_meta\_apply\_val\_n\_reset\_o\_state(n)$   
 $\wedge o\_send\_ack(n, m.oTS, tVersion[n])$   
 $\wedge unchanged\_mtrc$

$OFMRequesterVALReplay \triangleq$  Requester receives a  $RESP$  (already applied)  
 and re-sends a  $VAL$  to arbiters  
 $\exists n \in APP\_LIVE\_NODES : \exists m \in oMsgs :$   
 $\wedge o\_rcv\_resp(m, n)$   
 $\wedge m.rTS.tb = n$   
 $\wedge m.oTS = oTS[n]$   
 $\wedge o\_send\_val(m.oTS)$   
 $\wedge unchanged\_mtrco$

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$block\_owner\_failures\_if\_not\_in\_tx\_valid\_state(n) \triangleq$   
 $\vee has\_valid\_data(n)$   
 $\vee \neg is\_valid\_owner(n)$

Emulate a node failure if there more than 2 alive nodes in  $LIVE\_NODE\_SET$   
 $nodeFailure(n, LIVE\_NODE\_SET) \triangleq$   
 $\wedge n \in LIVE\_NODE\_SET$   
 $\wedge block\_owner\_failures\_if\_not\_in\_valid\_state(n)$   
 $\wedge Cardinality(LIVE\_NODE\_SET) > 2$   
 Update Membership and epoch  $id$

$$\begin{aligned}
& \wedge mEID' = mEID + 1 \\
& \wedge mAliveNodes' = mAliveNodes \setminus \{n\} \\
& \text{Remove failed node from } oVectors \\
& \wedge oVector' = [l \in O\_NODES \mapsto [readers \mapsto oVector[l].readers \setminus \{n\}, \\
& \quad \quad \quad owner \mapsto \text{IF } oVector[l].owner = n \\
& \quad \quad \quad \quad \quad \text{THEN } 0 \\
& \quad \quad \quad \quad \quad \text{ELSE } oVector[l].owner \ ] ] \\
& \wedge unchanged\_Mtrc \\
& \wedge \text{UNCHANGED } \langle oState, oDriver, oRcvACKs, oTS \rangle
\end{aligned}$$


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$$\begin{aligned}
FNext & \triangleq \\
& \vee OFRequester \\
& \vee OFDriverRequester \\
& \vee OFArbReplay \\
& \vee OLBArbiterACK \\
& \vee OFMOArbiterINVLostVAL \\
& \vee OFMRequesterVALReplay \\
& \vee OFMOArbiterLostVALOldReplay \\
OFNext & \triangleq \\
& \vee ONext \\
& \vee FNext \\
& \vee \exists n \in mAliveNodes : \\
& \quad \vee nodeFailure(n, LB\_LIVE\_NODES) \quad \text{emulate } LB \text{ node failures} \\
& \quad \vee nodeFailure(n, APP\_LIVE\_NODES) \quad \text{emulate application node failures}
\end{aligned}$$

The complete definition of the algorithm

$$SFSpec \triangleq OInit \wedge \Box[OFNext]_{vars}$$

THEOREM  $SFSpec \Rightarrow Invariants$

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