

CA and MCA of NYCABS dataset

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Load Required Packages: to be increased over the course

```
rm(list=ls())
requiredPackages <- c("effects", "FactoMineR", "car", "factoextra", "RColorBrewer", "ggplot2", "missMDA", "mvn")
missingPackages <- requiredPackages[!(requiredPackages %in% installed.packages()[, "Package"])] 

if(length(missingPackages)) install.packages(missingPackages)
lapply(requiredPackages, require, character.only = TRUE)

## [[1]]
## [1] TRUE
##
## [[2]]
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## [1] TRUE
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## [[11]]
## [1] TRUE
##
## [[12]]
## [1] TRUE
##
## [[13]]
```

```

## [1] TRUE
# Useful function and Data
load("Taxi5000_raw_DataCleanv3.RData")
calcQ <- function(x) {
  s.x <- summary(x)
  iqr<-s.x[5]-s.x[2]
  list(souti=s.x[2]-3*iqr, mouti=s.x[2]-1.5*iqr, min=s.x[1], q1=s.x[2], q2=s.x[3], q3=s.x[5], ma

```

CA: f.cost (discretization of Total_amount) vs f.hour and f.tt and period ...

```

par(mfrow=c(1,1))
llvout<-which(df$mvout==TRUE);length(llvout)

## [1] 0
#llout<-unique(c(llout,llvout))
tt<-table(df[,c("f.total","pick_up_period")])
tt

##          pick_up_period
## f.total      night morning valley afternoon
##   (-1,7.8]    203     275    363     412
##   (7.8,11]    177     218    331     461
##   (11,16.6]   185     204    340     475
##   (16.6,46]   222     280    333     387

prop.table(tt,1)

##          pick_up_period
## f.total      night   morning   valley afternoon
##   (-1,7.8]  0.1620112 0.2194733 0.2897047 0.3288109
##   (7.8,11]  0.1491154 0.1836563 0.2788543 0.3883741
##   (11,16.6] 0.1536545 0.1694352 0.2823920 0.3945183
##   (16.6,46] 0.1816694 0.2291326 0.2725041 0.3166939

prop.table(table(df$pick_up_period))

## 
##      night   morning   valley afternoon
## 0.1617345 0.2007809 0.2809289 0.3565557

prop.table(tt,2)

##          pick_up_period
## f.total      night   morning   valley afternoon
##   (-1,7.8]  0.2579416 0.2814739 0.2655450 0.2374640
##   (7.8,11]  0.2249047 0.2231320 0.2421361 0.2657061
##   (11,16.6] 0.2350699 0.2088025 0.2487198 0.2737752
##   (16.6,46] 0.2820839 0.2865916 0.2435991 0.2230548

prop.table(table(df$f.total))

## 
##  (-1,7.8]  (7.8,11]  (11,16.6]  (16.6,46]

```

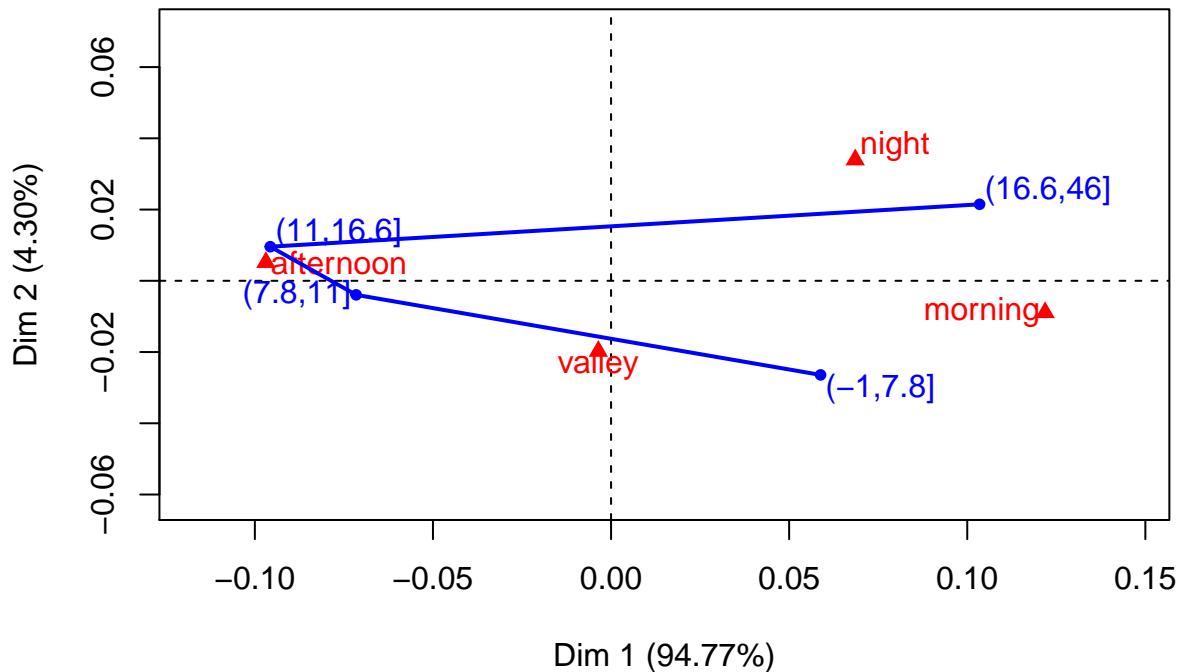
```

## 0.2575010 0.2439375 0.2474312 0.2511303
# From the chi-square test we see that the p.value is less than 0.05 which meand that we can reject the
chisq.test(tt)

##
## Pearson's Chi-squared test
##
## data: tt
## X-squared = 36.424, df = 9, p-value = 3.334e-05
res.ca<-CA(tt)
lines(res.ca$row$coord[,1],res.ca$row$coord[,2],lwd=2,col="blue")

```

CA factor map



```

names(res.ca)

## [1] "eig"   "call"  "row"   "col"   "svd"
res.ca$row$contrib[,1:2]

##           Dim 1      Dim 2
## (-1,7.8] 12.55998 55.799559
## (7.8,11] 17.61430  1.177242
## (11,16.6] 31.92607  7.050975
## (16.6,46] 37.89965 35.972224

res.ca$row$coord[,1:2]

##           Dim 1      Dim 2
## (-1,7.8]  0.05882227 -0.026415570

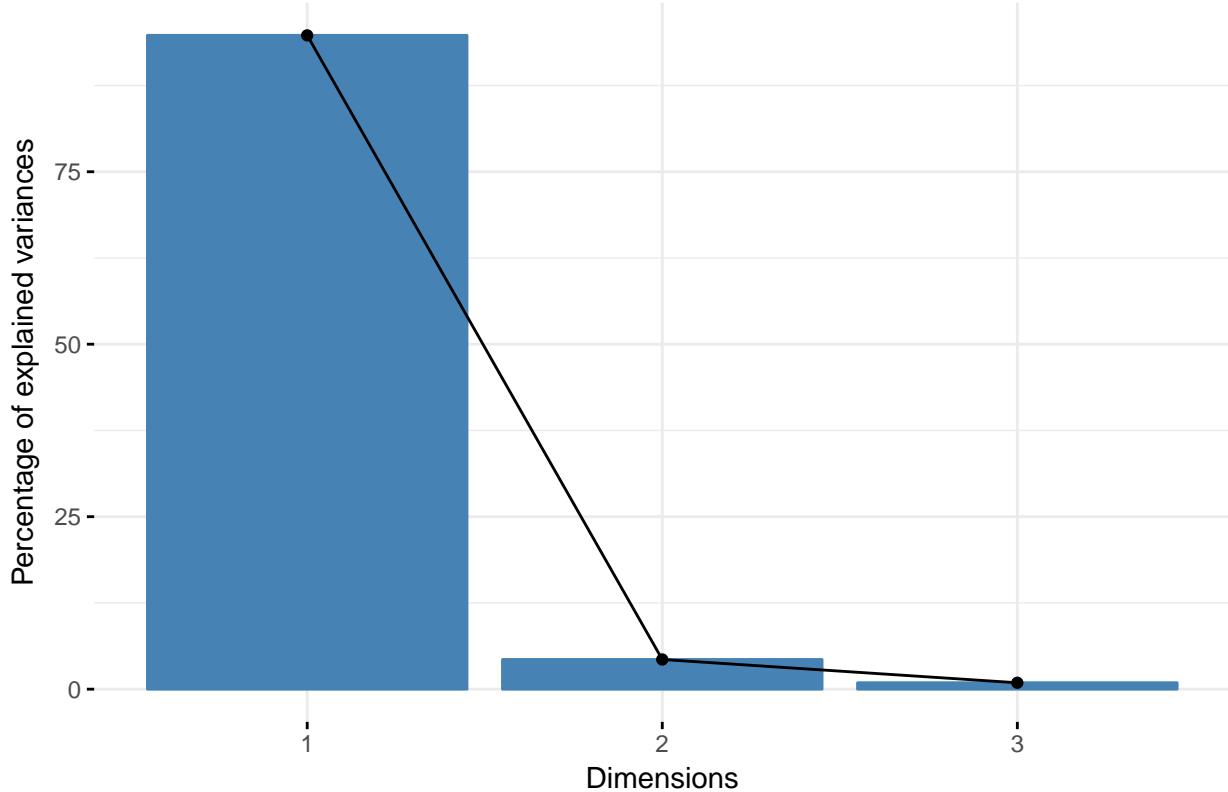
```

```

## [1] -0.07156986 -0.003942100
## [2] -0.09567143  0.009579249
## [3]  0.10346770  0.021476731
fviz_eig(res.ca)

```

Scree plot



#From the variance and the eigenvalues we conclude that the first Dim explains a huge part of the data .
summary(res.ca,dig=2)

```

##
## Call:
## CA(X = tt)
##
## The chi square of independence between the two variables is equal to 36.42355 (p-value = 3.333947e-0
##
## Eigenvalues
##                               Dim.1   Dim.2   Dim.3
## Variance                  0.007   0.000   0.000
## % of var.                94.768   4.302   0.930
## Cumulative % of var.    94.768  99.070 100.000
##
## Rows
##           Iner*1000   Dim.1     ctr   cos2   Dim.2     ctr   cos2
## (-1,7.8] |      1.075 | 0.059 12.560  0.829 | -0.026 55.800  0.167 |
## (7.8,11] |      1.293 | -0.072 17.614  0.966 | -0.004  1.177  0.003 |
## (11,16.6] |      2.313 | -0.096 31.926  0.979 |  0.010  7.051  0.010 |
## (16.6,46] |      2.805 |  0.103 37.900  0.958 |  0.021 35.972  0.041 |

```

```

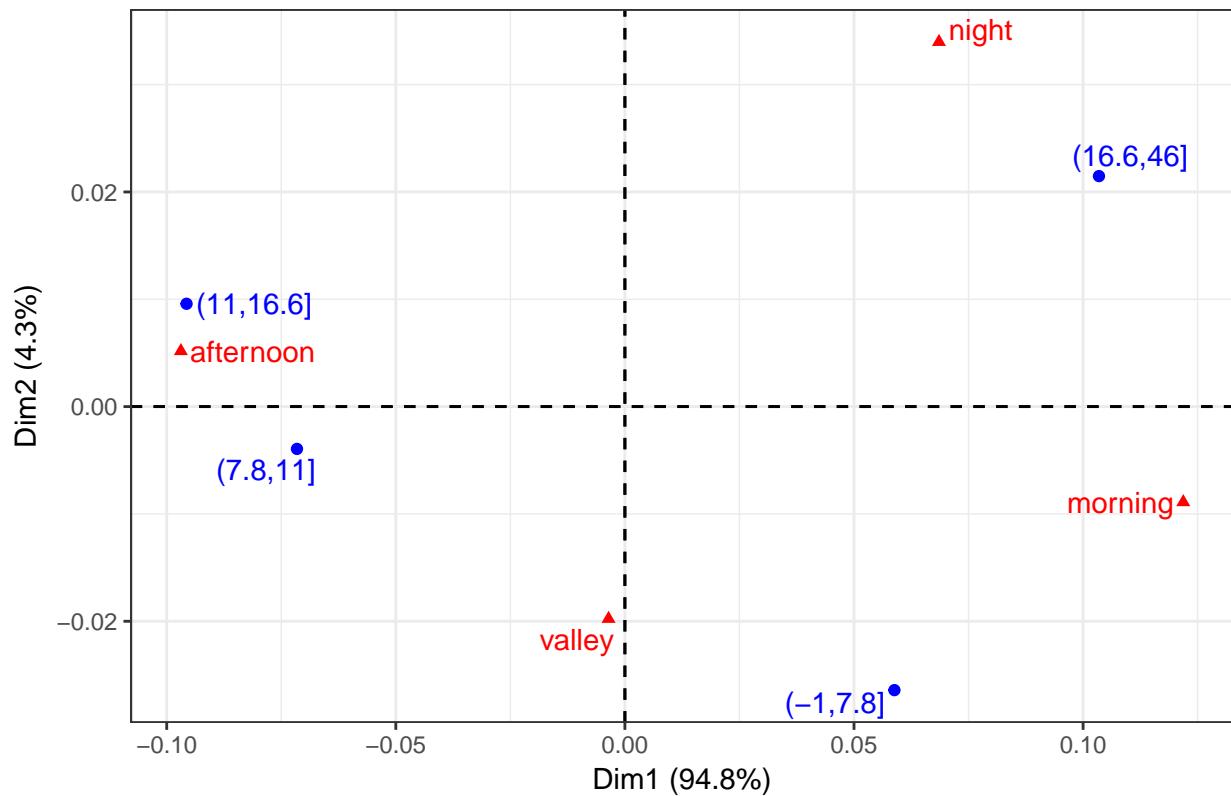
##           Dim.3   ctr   cos2
## (-1,7.8]  0.004  5.890  0.004 |
## (7.8,11] -0.013 56.815  0.031 |
## (11,16.6]  0.010 36.280  0.011 |
## (16.6,46] -0.002  1.015  0.000 |
##
## Columns
##           Iner*1000   Dim.1   ctr   cos2   Dim.2   ctr   cos2
## night      | 0.957 | 0.069 10.713  0.794 | 0.034 57.995  0.195 |
## morning    | 3.021 | 0.122 42.034  0.987 | -0.009 4.937  0.005 |
## valley     | 0.140 | -0.004 0.050  0.026 | -0.020 34.103  0.786 |
## afternoon  | 3.368 | -0.097 47.202  0.994 | 0.005 2.965  0.003 |
##
##           Dim.3   ctr   cos2
## night      0.008 15.119  0.011 |
## morning    -0.011 32.950  0.008 |
## valley     0.010 37.754  0.188 |
## afternoon -0.005 14.177  0.003 |

```

We see that the column points and the row points are far away from each other and thus not similar

```
fviz_ca_biplot(res.ca,repel=TRUE)+theme_bw()
```

CA – Biplot



```

tt<-table(df[,c("f.total","f.ttime")])
tt

##           f.ttime
## f.total      (-1,6] (6,9.78] (9.78,15.7] (15.7,215]
## (-1,7.8]    1011     234       5        3

```

```

##   (7.8,11]    206     741     232      8
##   (11,16.6]     2     224     751     227
##   (16.6,46]     4     10     232     976
prop.table(tt,1)

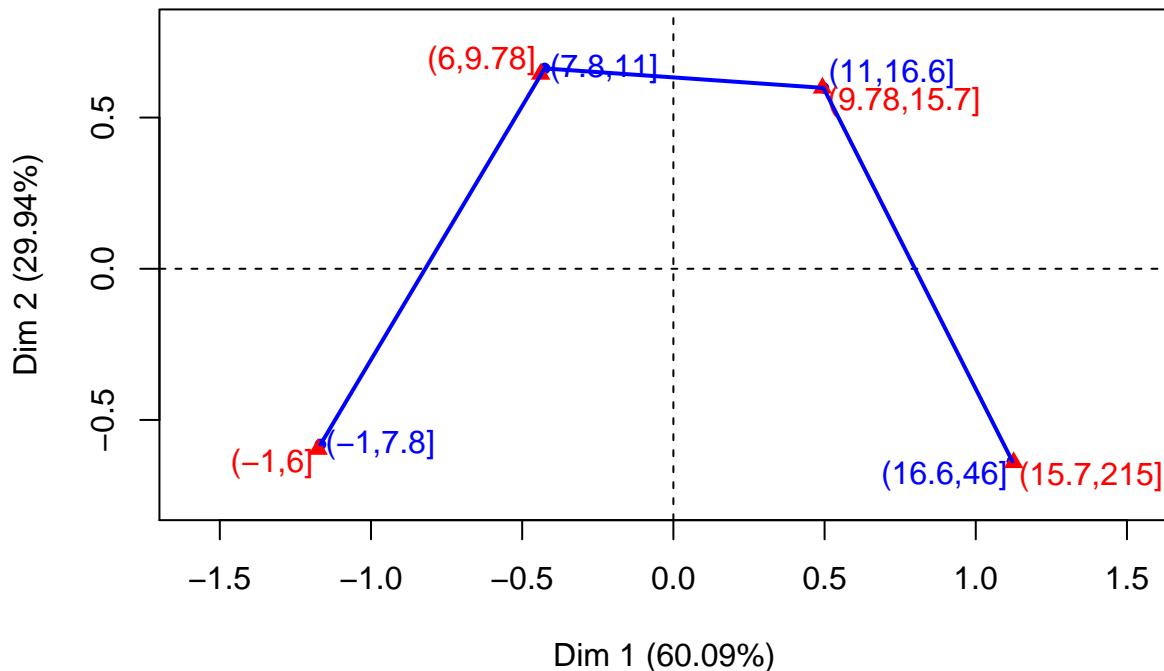
##          f.ttime
## f.total      (-1,6]   (6,9.78] (9.78,15.7] (15.7,215]
##   (-1,7.8]  0.806863528 0.186751796 0.003990423 0.002394254
##   (7.8,11]  0.173546757 0.624262848 0.195450716 0.006739680
##   (11,16.6] 0.001661130 0.186046512 0.623754153 0.188538206
##   (16.6,46] 0.003273322 0.008183306 0.189852700 0.798690671
prop.table(table(df$f.ttime))

##
##   (-1,6]   (6,9.78] (9.78,15.7] (15.7,215]
##   0.2513358 0.2484587 0.2507193 0.2494862
#Same as the Ca before this 2 facotrs are dependent because of the really small p.value and the big X-s
chisq.test(tt)

## Pearson's Chi-squared test
##
## data: tt
## X-squared = 6249, df = 9, p-value < 2.2e-16
#From the plot we see that the longer the trips is the more it costs which was also expected.
res.ca<-CA(tt)
lines(res.ca$row$coord[,1],res.ca$row$coord[,2],lwd=2,col="blue")

```

CA factor map



```
#We need to consider the first 2 dimentions which together explain 90% of the data.
summary(res.ca)
```

```
##
## Call:
## CA(X = tt)
##
## The chi square of independence between the two variables is equal to 6248.958 (p-value = 0).
##
## Eigenvalues
##                               Dim.1   Dim.2   Dim.3
## Variance                  0.772   0.384   0.128
## % of var.                60.089  29.938   9.973
## Cumulative % of var.    60.089  90.027 100.000
##
## Rows
##          Iner*1000      Dim.1     ctr   cos2   Dim.2     ctr
## (-1,7.8] | 445.665 | -1.167  45.457  0.787 | -0.581 22.627
## (7.8,11] | 205.119 | -0.426  5.730  0.216 |  0.663 27.852
## (11,16.6] | 206.262 |  0.496  7.900  0.296 |  0.598 23.024
## (16.6,46] | 427.162 |  1.121 40.913  0.739 | -0.637 26.497
##          cos2   Dim.3     ctr   cos2
## (-1,7.8] 0.195 | -0.175  6.166  0.018 |
## (7.8,11] 0.522 |  0.470 42.025  0.262 |
## (11,16.6] 0.429 | -0.479 44.333  0.275 |
## (16.6,46] 0.238 |  0.195  7.477  0.022 |
```

```

## 
## Columns
##          Iner*1000      Dim.1      ctr      cos2      Dim.2      ctr
## (-1,6] | 444.908 | -1.175  44.958  0.780 | -0.597 23.277
## (6,9.78] | 204.837 | -0.439   6.204  0.234 |  0.644 26.778
## (9.78,15.7] | 206.535 |  0.493   7.895  0.295 |  0.598 23.307
## (15.7,215] | 427.928 |  1.125  40.943  0.738 | -0.641 26.639
##          cos2      Dim.3      ctr      cos2
## (-1,6] | 0.201 | -0.184  6.632  0.019 |
## (6,9.78] | 0.503 |  0.466 42.173  0.264 |
## (9.78,15.7] | 0.434 | -0.473 43.726  0.271 |
## (15.7,215] | 0.239 |  0.196  7.469  0.022 |

res.ca$row$contrib[,1:2]

##           Dim 1      Dim 2
## (-1,7.8] 45.456861 22.62710
## (7.8,11]  5.729620 27.85203
## (11,16.6] 7.900036 23.02413
## (16.6,46] 40.913483 26.49674

res.ca$row$coord[,1:2]

##           Dim 1      Dim 2
## (-1,7.8] -1.1671449 -0.5812360
## (7.8,11] -0.4257338  0.6625470
## (11,16.6] 0.4963658  0.5981251
## (16.6,46] 1.1212390 -0.6369044

res.ca$row$cos2[,1:2]

##           Dim 1      Dim 2
## (-1,7.8] 0.7870818 0.1951980
## (7.8,11] 0.2155503 0.5220423
## (11,16.6] 0.2955551 0.4291594
## (16.6,46] 0.7391000 0.2384818

#The 2st two eigenectors give us 90% of the variance so they are sufficient.
res.ca$eig

##      eigenvalue percentage of variance cumulative percentage of variance
## dim 1  0.7716655             60.088810                  60.08881
## dim 2  0.3844636             29.937788                  90.02660
## dim 3  0.1280793              9.973402                 100.00000

sum(res.ca$eig[1:2,1])/sum(res.ca$eig[1:3,1])

## [1] 0.900266

sum(res.ca$eig[1:3,1])

## [1] 1.284208

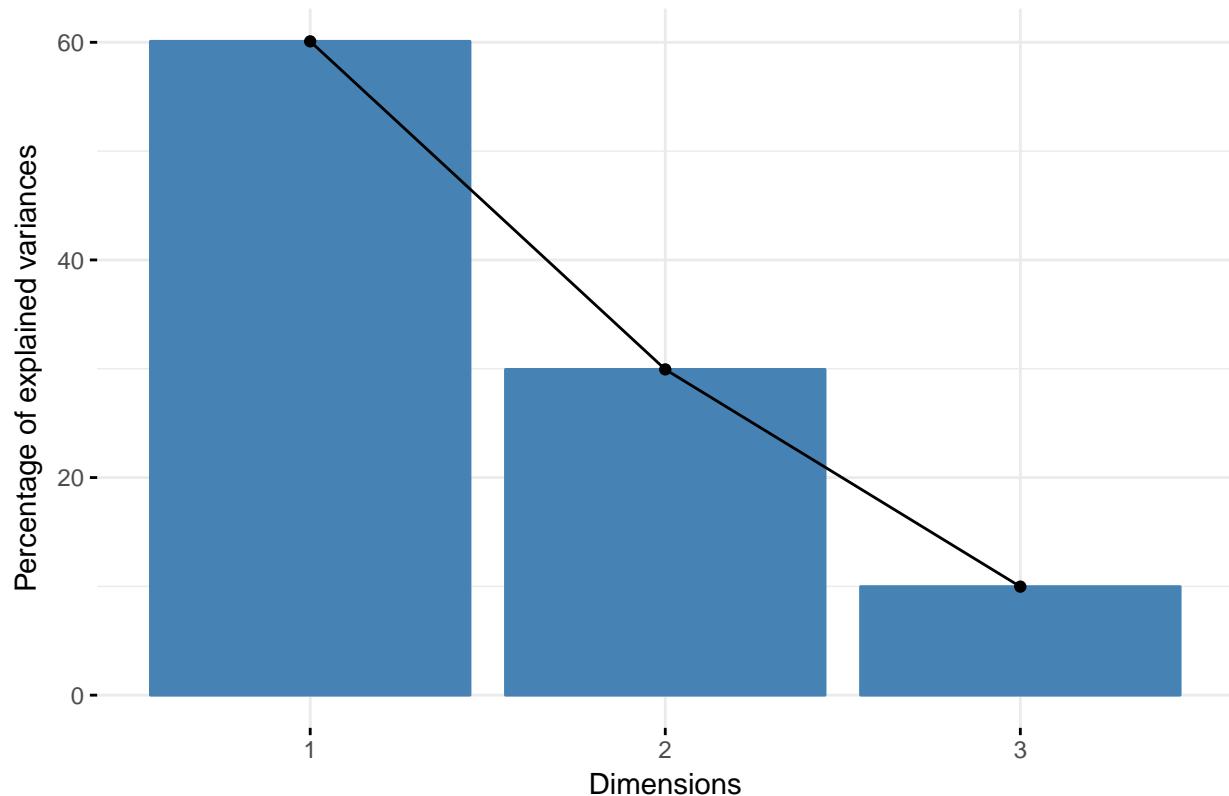
res.ca$call$marge.col

##      (-1,6]    (6,9.78] (9.78,15.7] (15.7,215]
## 0.2513358  0.2484587  0.2507193  0.2494862

fviz_eig(res.ca)

```

Scree plot



```
summary(res.ca,dig=2)
```

```
##
## Call:
## CA(X = tt)
##
## The chi square of independence between the two variables is equal to 6248.958 (p-value = 0).
##
## Eigenvalues
##                               Dim.1   Dim.2   Dim.3
## Variance                 0.772   0.384   0.128
## % of var.                60.089  29.938  9.973
## Cumulative % of var.    60.089  90.027 100.000
##
## Rows
##           Iner*1000   Dim.1     ctr   cos2   Dim.2     ctr
## (-1,7.8] | 445.665 | -1.167  45.457  0.787 | -0.581 22.627
## (7.8,11] | 205.119 | -0.426   5.730  0.216 |  0.663 27.852
## (11,16.6] | 206.262 |  0.496   7.900  0.296 |  0.598 23.024
## (16.6,46] | 427.162 |  1.121  40.913  0.739 | -0.637 26.497
##           cos2   Dim.3     ctr   cos2
## (-1,7.8] | 0.195 | -0.175  6.166  0.018 |
## (7.8,11] | 0.522 |  0.470  42.025  0.262 |
## (11,16.6] | 0.429 | -0.479  44.333  0.275 |
## (16.6,46] | 0.238 |  0.195  7.477  0.022 |
##
```

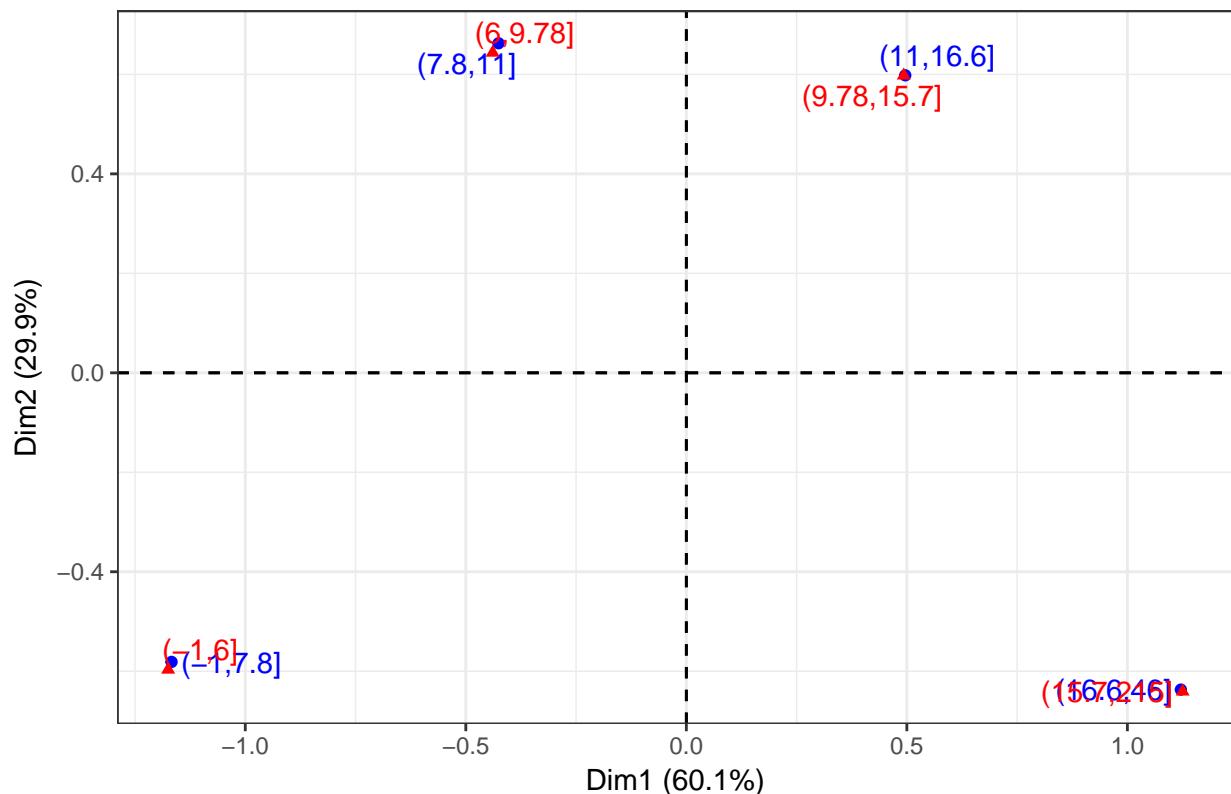
```

## Columns
##          Iner*1000    Dim.1     ctr   cos2    Dim.2     ctr
## (-1,6] | 444.908 | -1.175  44.958  0.780 | -0.597 23.277
## (6,9.78] | 204.837 | -0.439   6.204  0.234 |  0.644 26.778
## (9.78,15.7] | 206.535 |  0.493   7.895  0.295 |  0.598 23.307
## (15.7,215] | 427.928 |  1.125  40.943  0.738 | -0.641 26.639
##          cos2    Dim.3     ctr   cos2
## (-1,6] | 0.201 | -0.184  6.632  0.019 |
## (6,9.78] | 0.503 |  0.466 42.173  0.264 |
## (9.78,15.7] | 0.434 | -0.473 43.726  0.271 |
## (15.7,215] | 0.239 |  0.196  7.469  0.022 |

fviz_ca_biplot(res.ca,repel=TRUE)+theme_bw()

```

CA – Biplot



```

#tt<-table(df[,c("AnyTip","f.ttime")]) # No tinc sentit fer-ho
#tt
#res.ca<-CA(tt)
#fviz_ca_biplot(res.ca,repel=TRUE)+theme_bw()

```

MCA using multivariant

```

par(mfrow=c(1,1))
names(df)

## [1] "VendorID"                      "lpep_pickup_datetime"

```

```

## [3] "Lpep_dropoff_datetime"      "Store_and_fwd_flag"
## [5] "RateCodeID"                "Pickup_longitude"
## [7] "Pickup_latitude"           "Dropoff_longitude"
## [9] "Dropoff_latitude"          "Passenger_count"
## [11] "Trip_distance"             "Fare_amount"
## [13] "Extra"                     "MTA_tax"
## [15] "Tip_amount"                "Tolls_amount"
## [17] "improvement_surcharge"     "Total_amount"
## [19] "Payment_type"              "Trip_type"
## [21] "mis_ind"                  "AnyTip"
## [23] "trip_length"               "trip_distance_km"
## [25] "travel_time"                "pick_up_hour"
## [27] "pick_up_period"            "espeed"
## [29] "f.passenger"               "f.distance"
## [31] "f.pickup_longitude"         "f.pickup_latitude"
## [33] "f.dropoff_longitude"        "f.dropoff_latitude"
## [35] "f.fare_amount"              "f.extra"
## [37] "f.MTA_tax"                 "f.Improvement_surcharge"
## [39] "f.tip_amount"               "f.toll"
## [41] "f.total"                   "f.ttime"

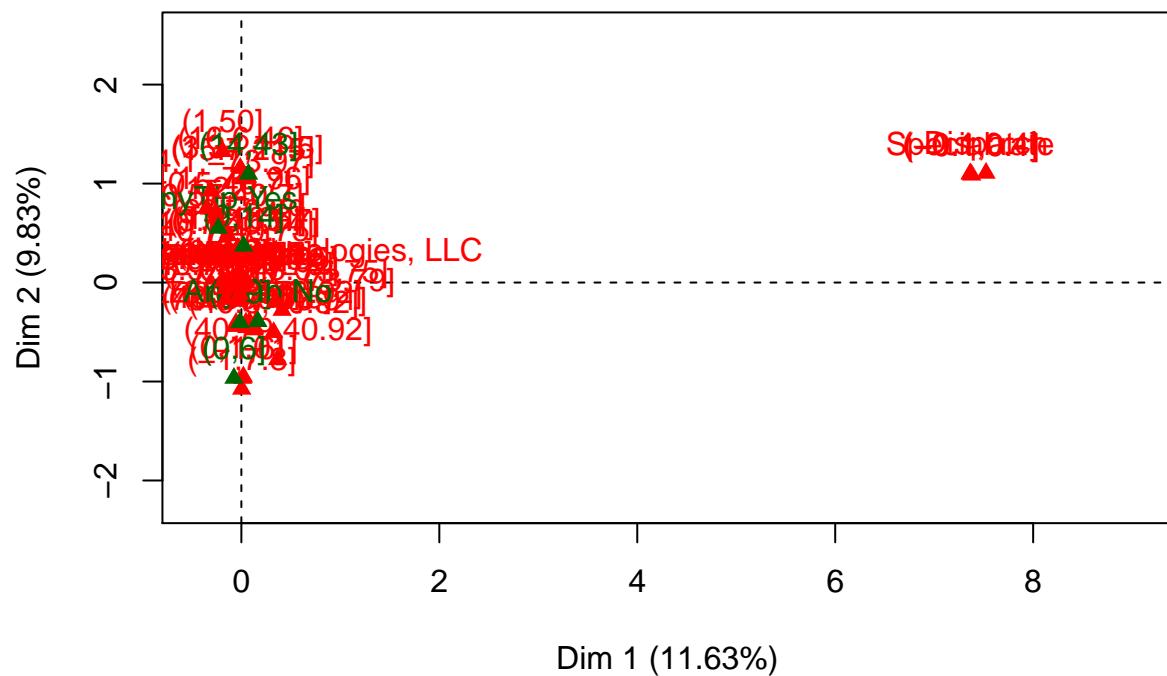
#explain we don't use this variable cause it is too bad balanced
summary(df$Store_and_fwd_flag)

##      Store_and_fwd Not_Store_and_fwd
##      4848                      18

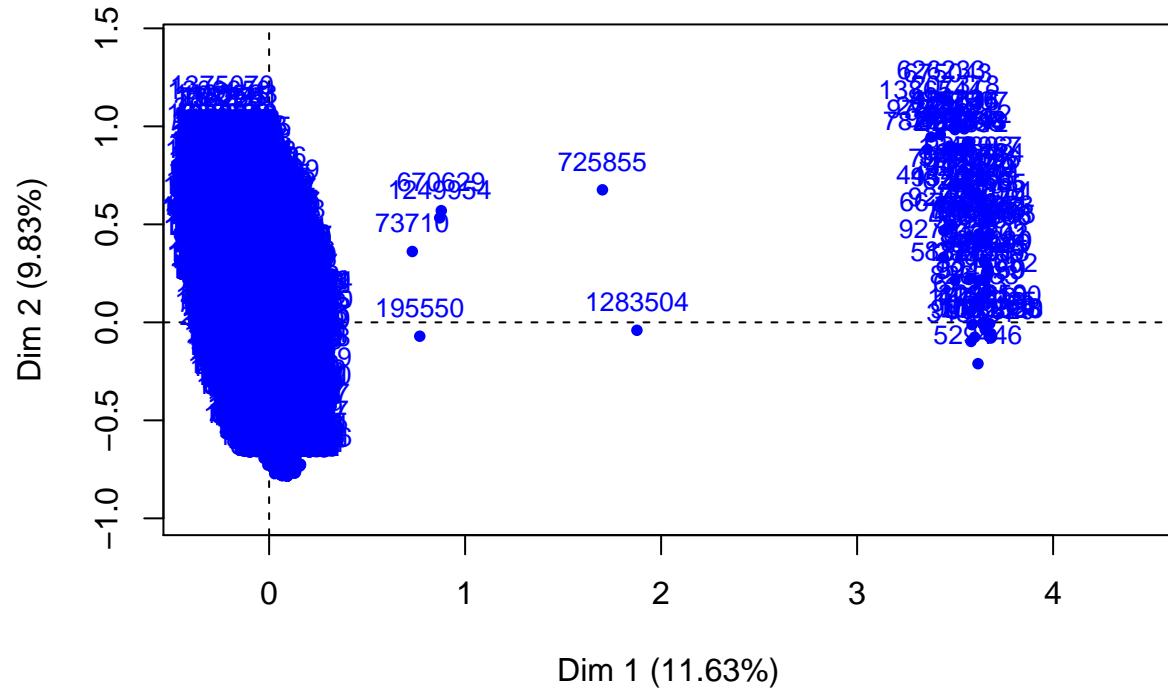
#add espeed factor as active (we need to generate it)
vars_dis <- names(df)[c(1,19,20,22,29:40,42)]
vars_cat<-names(df)[c(1, 5,19:20,22,27, 29:42)]#10, 21 not working
#add f.totalamount as quali.sup
res.mca<-MCA(df[,c(vars_cat,"Total_amount")],quali.sup=c(5,13),quanti.sup=21)

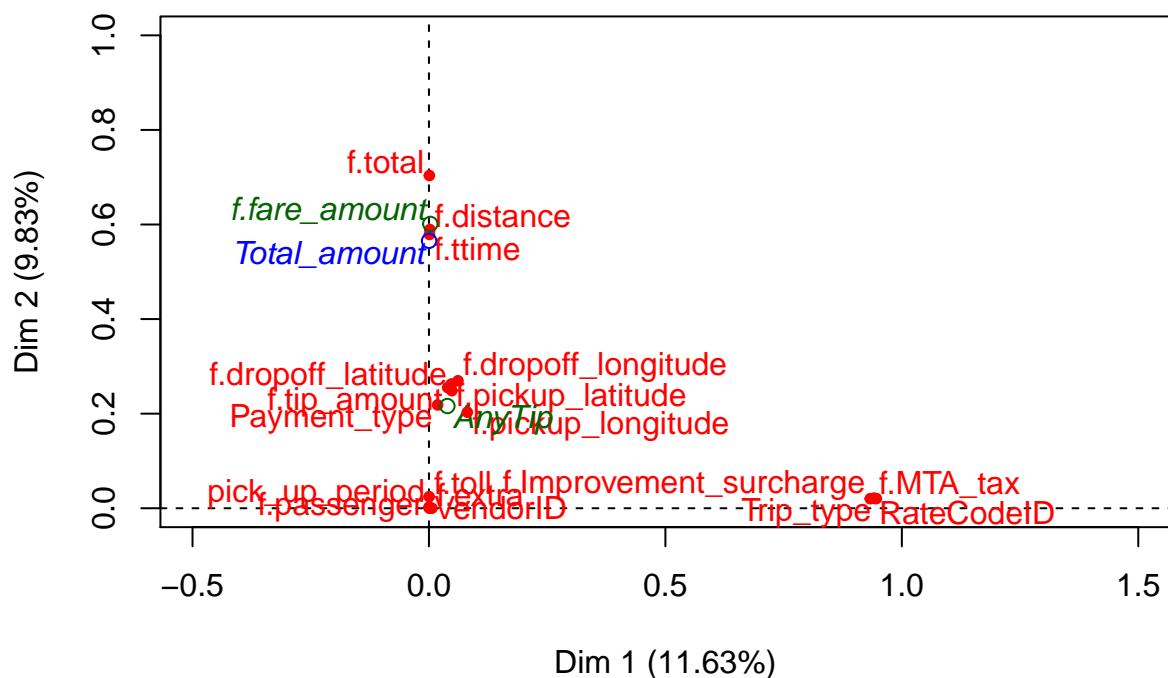
```

MCA factor map

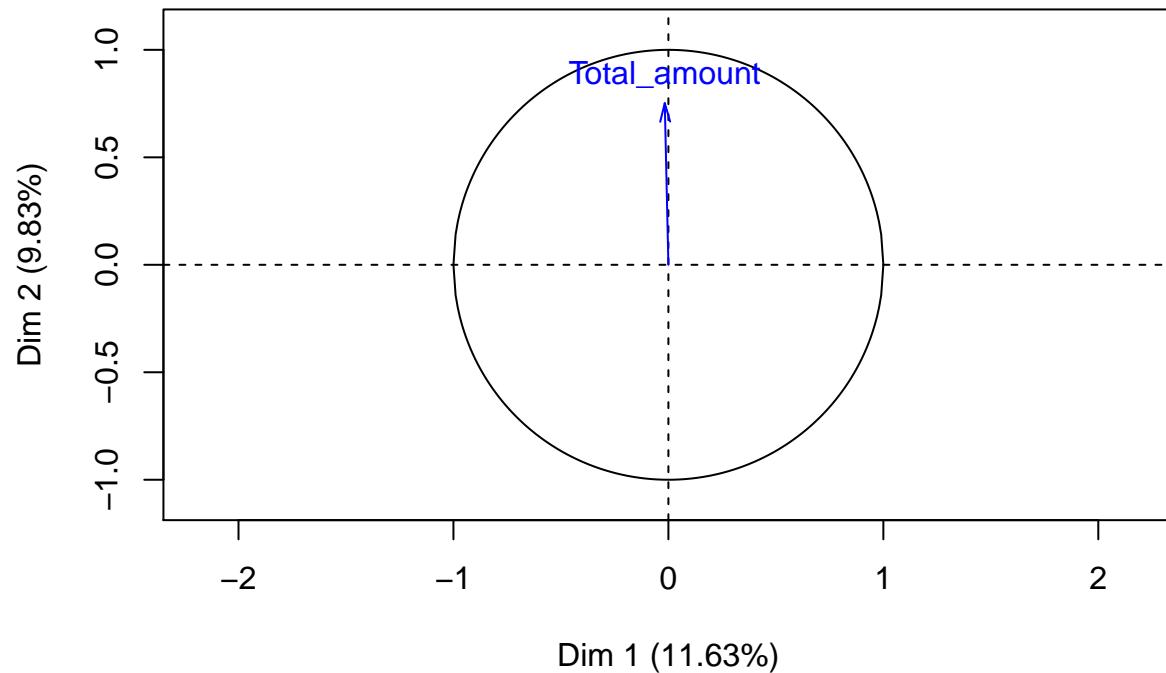


MCA factor map

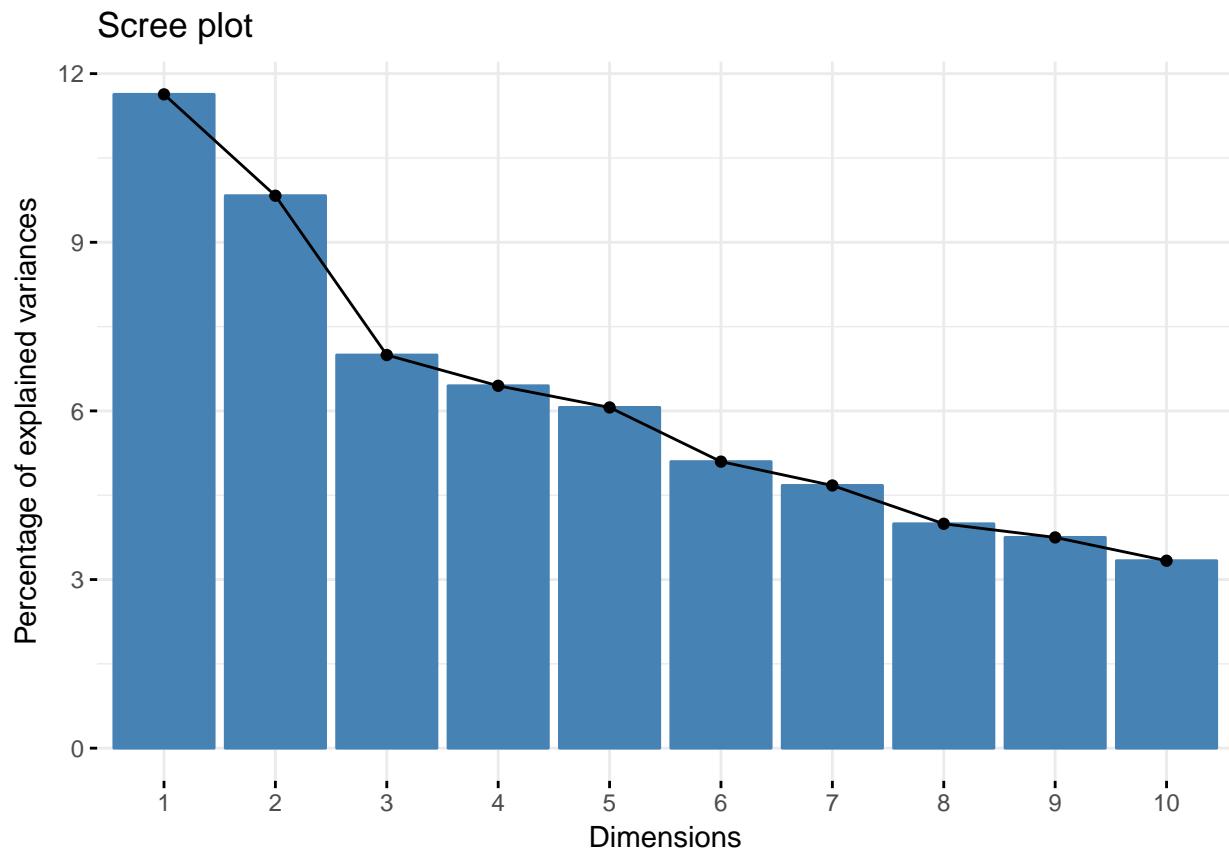




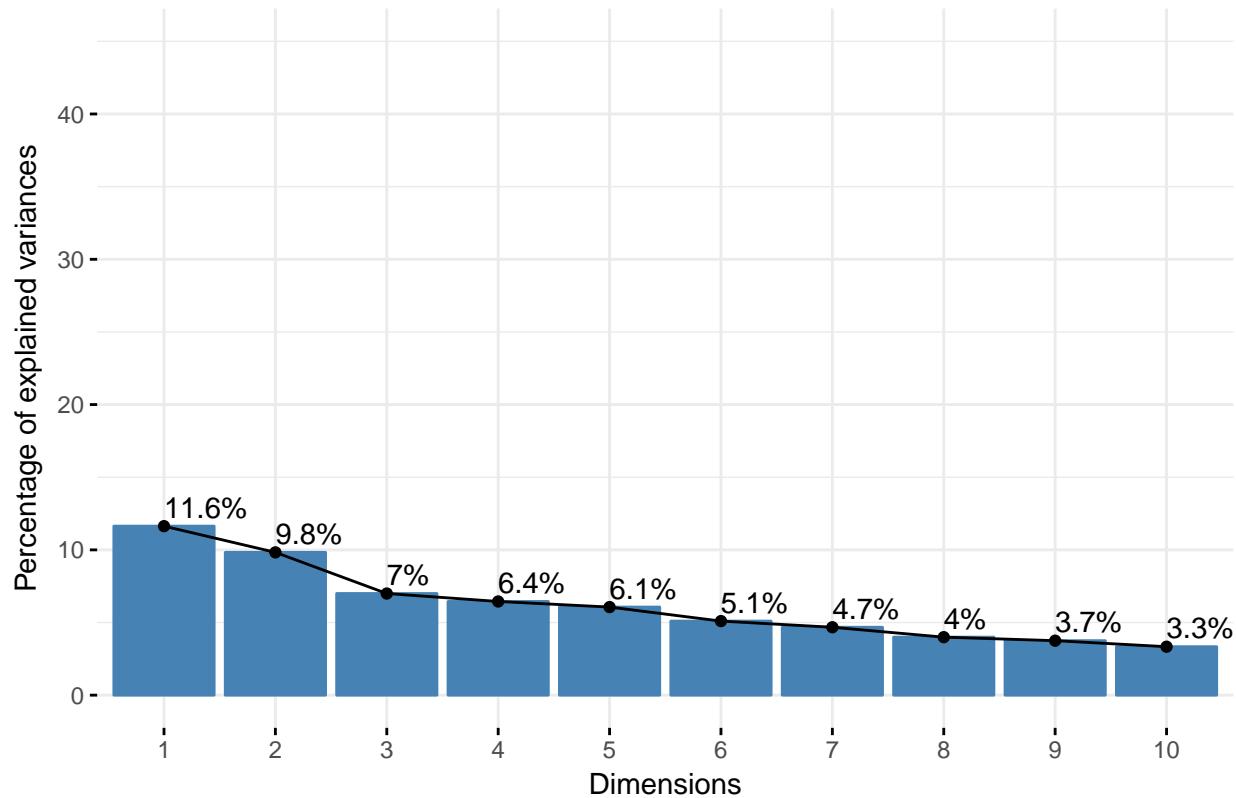
Supplementary variables on the MCA factor map



```
# We see that all of the eigenvectors are really small, so we will use a similiar rule like in the PCA
fviz_eig(res.mca)
```



Scree plot



```
get_eigenvalue(res.mca)
```

```
##          eigenvalue variance.percent cumulative.variance.percent
## Dim.1    0.2261765402      11.6319364                  11.63194
## Dim.2    0.1911102515      9.8285272                  21.46046
## Dim.3    0.1359984308      6.9942050                  28.45467
## Dim.4    0.1253575716      6.4469608                  34.90163
## Dim.5    0.1178666778      6.0617149                  40.96334
## Dim.6    0.0991214132      5.0976727                  46.06102
## Dim.7    0.0908755725      4.6736009                  50.73462
## Dim.8    0.0776108087      3.9914130                  54.72603
## Dim.9    0.0729017237      3.7492315                  58.47526
## Dim.10   0.0648386658      3.3345600                  61.80982
## Dim.11   0.0619088374      3.1838831                  64.99371
## Dim.12   0.0576966185      2.9672547                  67.96096
## Dim.13   0.0552112413      2.8394353                  70.80040
## Dim.14   0.0540182528      2.7780816                  73.57848
## Dim.15   0.0525391877      2.7020154                  76.28049
## Dim.16   0.0491398601      2.5271928                  78.80769
## Dim.17   0.0460239064      2.3669438                  81.17463
## Dim.18   0.0457852141      2.3546682                  83.52930
## Dim.19   0.0405587859      2.0858804                  85.61518
## Dim.20   0.0392198668      2.0170217                  87.63220
## Dim.21   0.0370060530      1.9031684                  89.53537
## Dim.22   0.0339188719      1.7443991                  91.27977
## Dim.23   0.0313546178      1.6125232                  92.89229
```

```

## Dim.24 0.0278196973      1.4307273      94.32302
## Dim.25 0.0250900563      1.2903458      95.61336
## Dim.26 0.0194981903      1.0027641      96.61613
## Dim.27 0.0172792123      0.8886452      97.50477
## Dim.28 0.0141305567      0.7267143      98.23149
## Dim.29 0.0114623094      0.5894902      98.82098
## Dim.30 0.0082052451      0.4219840      99.24296
## Dim.31 0.0071780552      0.3691571      99.61212
## Dim.32 0.0041939532      0.2156890      99.82781
## Dim.33 0.0021405803      0.1100870      99.93789
## Dim.34 0.0006779947      0.0348683      99.97276
## Dim.35 0.0005296239      0.0272378      100.00000

names(res.mca)

## [1] "eig"         "call"        "ind"         "var"         "svd"
## [6] "quali.sup"   "quanti.sup"
summary(res.mca,nbelements=50)

##
## Call:
## MCA(X = df[, c(vars_cat, "Total_amount")], quanti.sup = 21, quali.sup = c(5,
##       13))
##
##
## Eigenvalues
##                               Dim.1   Dim.2   Dim.3   Dim.4   Dim.5   Dim.6
## Variance                  0.226   0.191   0.136   0.125   0.118   0.099
## % of var.                11.632   9.829   6.994   6.447   6.062   5.098
## Cumulative % of var.    11.632  21.460  28.455  34.902  40.963  46.061
##                               Dim.7   Dim.8   Dim.9   Dim.10  Dim.11  Dim.12
## Variance                  0.091   0.078   0.073   0.065   0.062   0.058
## % of var.                4.674   3.991   3.749   3.335   3.184   2.967
## Cumulative % of var.   50.735  54.726  58.475  61.810  64.994  67.961
##                               Dim.13  Dim.14  Dim.15  Dim.16  Dim.17  Dim.18
## Variance                  0.055   0.054   0.053   0.049   0.046   0.046
## % of var.                2.839   2.778   2.702   2.527   2.367   2.355
## Cumulative % of var. 70.800  73.578  76.280  78.808  81.175  83.529
##                               Dim.19  Dim.20  Dim.21  Dim.22  Dim.23  Dim.24
## Variance                  0.041   0.039   0.037   0.034   0.031   0.028
## % of var.                2.086   2.017   1.903   1.744   1.613   1.431
## Cumulative % of var. 85.615  87.632  89.535  91.280  92.892  94.323
##                               Dim.25  Dim.26  Dim.27  Dim.28  Dim.29  Dim.30
## Variance                  0.025   0.019   0.017   0.014   0.011   0.008
## % of var.                1.290   1.003   0.889   0.727   0.589   0.422
## Cumulative % of var. 95.613  96.616  97.505  98.231  98.821  99.243
##                               Dim.31  Dim.32  Dim.33  Dim.34  Dim.35
## Variance                  0.007   0.004   0.002   0.001   0.001
## % of var.                0.369   0.216   0.110   0.035   0.027
## Cumulative % of var. 99.612  99.828  99.938  99.973 100.000
##
## Individuals (the 50 first)
##                               Dim.1     ctr     cos2     Dim.2     ctr
## 285 | -0.017  0.000  0.000 |  0.280  0.008

```

## 307	0.029 0.000 0.001 0.074 0.001
## 401	-0.036 0.000 0.001 0.099 0.001
## 593	0.080 0.001 0.003 -0.617 0.041
## 636	-0.207 0.004 0.026 0.636 0.043
## 886	-0.228 0.005 0.031 0.276 0.008
## 904	-0.016 0.000 0.000 -0.118 0.002
## 978	-0.030 0.000 0.000 0.266 0.008
## 1135	-0.093 0.001 0.006 -0.362 0.014
## 1282	-0.055 0.000 0.002 -0.348 0.013
## 1409	0.056 0.000 0.002 -0.449 0.022
## 1475	-0.103 0.001 0.006 0.216 0.005
## 1495	-0.203 0.004 0.026 0.783 0.066
## 1905	0.091 0.001 0.005 -0.131 0.002
## 2126	0.064 0.000 0.002 -0.063 0.000
## 2151	0.084 0.001 0.004 -0.555 0.033
## 2201	-0.185 0.003 0.021 0.738 0.059
## 2271	-0.009 0.000 0.000 -0.162 0.003
## 2747	0.074 0.000 0.003 -0.569 0.035
## 3065	-0.181 0.003 0.020 0.774 0.064
## 3089	-0.085 0.001 0.005 0.470 0.024
## 3130	0.045 0.000 0.001 -0.649 0.045
## 3221	0.056 0.000 0.002 -0.512 0.028
## 3420	0.035 0.000 0.001 -0.693 0.052
## 3679	-0.031 0.000 0.001 0.073 0.001
## 4310	-0.020 0.000 0.000 0.030 0.000
## 4754	-0.063 0.000 0.002 -0.253 0.007
## 5241	-0.219 0.004 0.027 0.604 0.039
## 5277	-0.011 0.000 0.000 -0.431 0.020
## 5649	-0.195 0.003 0.018 0.322 0.011
## 6353	0.045 0.000 0.001 -0.207 0.005
## 6364	-0.163 0.002 0.013 -0.040 0.000
## 6755	-0.082 0.001 0.004 -0.244 0.006
## 6869	-0.016 0.000 0.000 -0.330 0.012
## 7079	0.059 0.000 0.002 -0.455 0.022
## 7211	0.038 0.000 0.001 -0.360 0.014
## 7342	-0.128 0.001 0.010 -0.178 0.003
## 7802	-0.143 0.002 0.013 -0.129 0.002
## 8138	-0.125 0.001 0.009 0.258 0.007
## 8443	-0.084 0.001 0.005 0.271 0.008
## 8619	0.017 0.000 0.000 0.106 0.001
## 8891	0.038 0.000 0.001 -0.192 0.004
## 8960	-0.096 0.001 0.006 -0.266 0.008
## 9207	0.038 0.000 0.001 0.152 0.002
## 9503	0.048 0.000 0.001 0.147 0.002
## 9747	0.000 0.000 0.000 0.281 0.009
## 9765	3.643 1.206 0.911 0.575 0.036
## 9984	-0.215 0.004 0.024 0.617 0.041
## 10034	-0.137 0.002 0.011 0.679 0.050
## 10199	0.066 0.000 0.003 -0.499 0.027
##	cos2 Dim.3 ctr cos2
## 285	0.050 -0.112 0.002 0.008
## 307	0.003 -0.612 0.057 0.240
## 401	0.006 -0.302 0.014 0.057
## 593	0.202 -0.469 0.033 0.116

```

## 636          0.243 |  0.266  0.011  0.043 |
## 886          0.046 |  0.606  0.055  0.221 |
## 904          0.009 | -0.516  0.040  0.164 |
## 978          0.037 | -0.482  0.035  0.120 |
## 1135         0.085 |  0.198  0.006  0.026 |
## 1282         0.074 | -0.117  0.002  0.008 |
## 1409         0.128 | -0.149  0.003  0.014 |
## 1475         0.028 |  0.265  0.011  0.042 |
## 1495         0.382 |  0.248  0.009  0.038 |
## 1905         0.011 | -0.453  0.031  0.130 |
## 2126         0.002 | -0.677  0.069  0.247 |
## 2151         0.193 |  0.047  0.000  0.001 |
## 2201         0.341 |  0.023  0.000  0.000 |
## 2271         0.016 | -0.556  0.047  0.185 |
## 2747         0.204 | -0.495  0.037  0.154 |
## 3065         0.362 | -0.081  0.001  0.004 |
## 3089         0.138 | -0.348  0.018  0.075 |
## 3130         0.266 | -0.292  0.013  0.054 |
## 3221         0.162 |  0.077  0.001  0.004 |
## 3420         0.305 |  0.294  0.013  0.055 |
## 3679         0.003 | -0.364  0.020  0.068 |
## 4310         0.001 |  0.042  0.000  0.001 |
## 4754         0.039 |  0.414  0.026  0.104 |
## 5241         0.203 |  0.404  0.025  0.091 |
## 5277         0.106 |  0.313  0.015  0.056 |
## 5649         0.049 |  0.048  0.000  0.001 |
## 6353         0.021 | -0.018  0.000  0.000 |
## 6364         0.001 |  0.617  0.057  0.184 |
## 6755         0.038 | -0.083  0.001  0.004 |
## 6869         0.065 |  0.189  0.005  0.021 |
## 7079         0.134 | -0.516  0.040  0.172 |
## 7211         0.082 | -0.446  0.030  0.126 |
## 7342         0.020 |  0.439  0.029  0.121 |
## 7802         0.011 |  0.530  0.042  0.182 |
## 8138         0.040 | -0.174  0.005  0.018 |
## 8443         0.047 |  0.172  0.004  0.019 |
## 8619         0.007 | -0.545  0.045  0.195 |
## 8891         0.024 | -0.479  0.035  0.148 |
## 8960         0.045 | -0.021  0.000  0.000 |
## 9207         0.014 | -0.437  0.029  0.119 |
## 9503         0.014 | -0.735  0.082  0.339 |
## 9747         0.014 | -0.778  0.091  0.109 |
## 9765         0.023 |  0.139  0.003  0.001 |
## 9984         0.200 |  0.348  0.018  0.064 |
## 10034        0.279 | -0.326  0.016  0.064 |
## 10199        0.156 | -0.556  0.047  0.194 |

##
## Categories (the 50 first)
##                               Dim.1      ctr     cos2 v.test
## Creative Mobile Technologies, LLC | -0.048  0.012  0.001 -1.755 |
## VeriFone Inc.                   |  0.013  0.003  0.001  1.755 |
## Standard rate                  | -0.128  0.394  0.941 -67.668 |
## Special rate                   |  7.365 22.724  0.941  67.668 |
## Credit card                     | -0.138  0.228  0.018 -9.414 |

```

	Dim.2	ctr	cos2	v.test
## Cash	0.134	0.223	0.018	9.435
## Other	-0.024	0.000	0.000	-0.139
## Street-hail	-0.126	0.382	0.946	-67.847
## Dispatch	7.524	22.859	0.946	67.847
## night	0.046	0.009	0.000	1.421
## morning	0.045	0.010	0.001	1.587
## valley	0.014	0.001	0.000	0.622
## afternoon	-0.058	0.029	0.002	-3.003
## (0,1]	0.004	0.000	0.000	0.649
## (1,6]	-0.022	0.002	0.000	-0.649
## (0,1.01]	0.021	0.003	0.000	0.848
## (1.01,1.8]	-0.057	0.020	0.001	-2.305
## (1.8,3.31]	-0.024	0.004	0.000	-0.975
## (3.31,11.5]	0.060	0.022	0.001	2.431
## (-74.1,-73.96]	-0.350	0.755	0.041	-14.127
## (-73.96,-73.95]	-0.158	0.145	0.008	-6.135
## (-73.95,-73.92]	0.082	0.043	0.002	3.389
## (-73.92,-73.79]	0.411	1.050	0.057	16.683
## (40.5,40.7]	-0.259	0.412	0.022	-10.442
## (40.7,40.74]	-0.125	0.090	0.005	-4.820
## (40.74,40.8]	0.054	0.020	0.001	2.322
## (40.8,40.92]	0.326	0.636	0.034	12.901
## (-74.1,-73.97]	-0.309	0.538	0.028	-11.755
## (-73.97,-73.94]	-0.155	0.168	0.010	-6.807
## (-73.94,-73.91]	0.130	0.103	0.006	5.209
## (-73.91,-73.75]	0.345	0.699	0.037	13.495
## (40.57,40.7]	-0.234	0.354	0.020	-9.753
## (40.7,40.75]	-0.081	0.044	0.002	-3.473
## (40.75,40.79]	-0.018	0.002	0.000	-0.665
## (40.79,40.92]	0.366	0.789	0.042	14.336
## (-0.1,0.5]	0.034	0.024	0.006	5.485
## (0.5,2]	-0.183	0.128	0.006	-5.485
## (-0.1,0.4]	7.364	22.723	0.941	67.666
## (0.4,0.5]	-0.128	0.394	0.941	-67.666
## (-0.1,0.1]	7.379	22.536	0.933	67.380
## (0.1,0.8]	-0.126	0.386	0.933	-67.380
## (-0.1,1]	0.154	0.365	0.040	13.893
## (1,22]	-0.258	0.610	0.040	-13.893
## (-1,1]	0.003	0.000	0.001	1.567
## (1,50]	-0.190	0.012	0.001	-1.567
## (-1,7.8]	0.003	0.000	0.000	0.127
## (7.8,11]	0.046	0.013	0.001	1.837
## (11,16.6]	-0.038	0.009	0.000	-1.508
## (16.6,46]	-0.011	0.001	0.000	-0.446
## (-1,6]	0.013	0.001	0.000	0.538
## Creative Mobile Technologies, LLC	0.023	0.003	0.000	0.826
## VeriFone Inc.	-0.006	0.001	0.000	-0.826
## Standard rate	-0.019	0.010	0.021	-10.099
## Special rate	1.099	0.599	0.021	10.099
## Credit card	0.476	3.232	0.218	32.563
## Cash	-0.461	3.112	0.215	-32.374
## Other	-0.188	0.007	0.000	-1.098
## Street-hail	-0.018	0.010	0.020	-9.972

## Dispatch	1.106	0.584	0.020	9.972	
## night	0.025	0.003	0.000	0.754	
## morning	0.000	0.000	0.000	0.004	
## valley	-0.043	0.015	0.001	-1.882	
## afternoon	0.023	0.005	0.000	1.183	
## (0,1]	-0.021	0.011	0.002	-3.412	
## (1,6]	0.115	0.059	0.002	3.412	
## (0,1.01]	-0.952	6.628	0.305	-38.491	
## (1.01,1.8]	-0.442	1.429	0.066	-17.869	
## (1.8,3.31]	0.340	0.834	0.038	13.620	
## (3.31,11.5]	1.065	8.242	0.378	42.883	
## (-74.1,-73.96]	0.750	4.105	0.189	30.287	
## (-73.96,-73.95]	-0.060	0.024	0.001	-2.317	
## (-73.95,-73.92]	-0.399	1.200	0.056	-16.466	
## (-73.92,-73.79]	-0.280	0.575	0.026	-11.349	
## (40.5,40.7]	0.705	3.627	0.167	28.462	
## (40.7,40.74]	0.295	0.591	0.027	11.365	
## (40.74,40.8]	-0.454	1.631	0.077	-19.362	
## (40.8,40.92]	-0.503	1.790	0.081	-19.897	
## (-74.1,-73.97]	0.925	5.705	0.255	35.201	
## (-73.97,-73.94]	-0.169	0.236	0.011	-7.420	
## (-73.94,-73.91]	-0.476	1.638	0.075	-19.096	
## (-73.91,-73.75]	-0.192	0.258	0.012	-7.529	
## (40.57,40.7]	0.576	2.535	0.118	23.988	
## (40.7,40.75]	0.223	0.398	0.019	9.582	
## (40.75,40.79]	-0.119	0.092	0.004	-4.440	
## (40.79,40.92]	-0.777	4.205	0.190	-30.421	
## (-0.1,0.5]	-0.002	0.000	0.000	-0.390	
## (0.5,2]	0.013	0.001	0.000	0.390	
## (-0.1,0.4]	1.098	0.598	0.021	10.090	
## (0.4,0.5]	-0.019	0.010	0.021	-10.090	
## (-0.1,0.1]	1.087	0.579	0.020	9.926	
## (0.1,0.8]	-0.019	0.010	0.020	-9.926	
## (-0.1,1]	-0.390	2.774	0.255	-35.231	
## (1,22]	0.653	4.643	0.255	35.231	
## (-1,1]	-0.018	0.010	0.024	-10.916	
## (1,50]	1.325	0.702	0.024	10.916	
## (-1,7.8]	-1.076	8.667	0.402	-44.200	
## (7.8,11]	-0.407	1.173	0.053	-16.117	
## (11,16.6]	0.349	0.875	0.040	13.949	
## (16.6,46]	1.155	9.737	0.447	46.647	
## (-1,6]	-0.966	6.819	0.313	-39.043	
##	Dim.3	ctr	cos2	v.test	
## Creative Mobile Technologies, LLC	0.174	0.265	0.008	6.346	
## VeriFone Inc.	-0.048	0.073	0.008	-6.346	
## Standard rate	-0.015	0.009	0.013	-7.980	
## Special rate	0.869	0.526	0.013	7.980	
## Credit card	0.101	0.206	0.010	6.935	
## Cash	-0.105	0.225	0.011	-7.344	
## Other	0.420	0.050	0.001	2.460	
## Street-hail	-0.015	0.009	0.014	-8.232	
## Dispatch	0.913	0.560	0.014	8.232	
## night	-0.340	0.765	0.022	-10.428	
## morning	-0.019	0.003	0.000	-0.674	

```

## valley          0.071  0.058  0.002  3.091 |
## afternoon      0.109  0.174  0.007  5.680 |
## (0,1]          0.023  0.018  0.003  3.719 |
## (1,6]          -0.125 0.098  0.003 -3.719 |
## (0,1.01]       0.485  2.416  0.079  19.604 |
## (1.01,1.8]     0.160  0.263  0.009  6.464 |
## (1.8,3.31]     -0.069 0.048  0.002 -2.752 |
## (3.31,11.5]    -0.581 3.441  0.112 -23.372 |
## (-74.1,-73.96] 0.955  9.347  0.306  38.554 |
## (-73.96,-73.95] 0.159  0.243  0.008  6.159 |
## (-73.95,-73.92] -0.037 0.014  0.000 -1.516 |
## (-73.92,-73.79] -1.060 11.592 0.380 -42.976 |
## (40.5,40.7]     1.053  11.360 0.371  42.493 |
## (40.7,40.74]    -0.381 1.386  0.044 -14.683 |
## (40.74,40.8]    -0.846 7.953  0.267 -36.067 |
## (40.8,40.92]    0.227  0.512  0.017  8.972 |
## (-74.1,-73.97] 0.541  2.745  0.087  20.599 |
## (-73.97,-73.94] 0.437  2.203  0.075  19.124 |
## (-73.94,-73.91] 0.064  0.042  0.001  2.566 |
## (-73.91,-73.75] -1.101 11.853 0.381 -43.081 |
## (40.57,40.7]    0.961  9.903  0.329  39.994 |
## (40.7,40.75]    -0.530 3.151  0.106 -22.749 |
## (40.75,40.79]   -0.793 5.727  0.180 -29.627 |
## (40.79,40.92]   0.292  0.837  0.027  11.449 |
## (-0.1,0.5]      -0.010 0.003  0.000 -1.546 |
## (0.5,2]          0.051  0.017  0.000  1.546 |
## (-0.1,0.4]       0.886  0.547  0.014  8.144 |
## (0.4,0.5]        -0.015 0.010  0.014 -8.144 |
## (-0.1,0.1]       0.920  0.582  0.014  8.397 |
## (0.1,0.8]        -0.016 0.010  0.014 -8.397 |
## (-0.1,1]          -0.051 0.066  0.004 -4.568 |
## (1,22]            0.085  0.110  0.004  4.568 |
## (-1,1]             0.020  0.016  0.029  11.784 |
## (1,50]            -1.430 1.150  0.029 -11.784 |
## (-1,7.8]          0.444  2.072  0.068  18.230 |
## (7.8,11]           0.101  0.102  0.003  4.013 |
## (11,16.6]         -0.036 0.013  0.000 -1.453 |
## (16.6,46]         -0.518 2.749  0.090 -20.910 |
## (-1,6]             0.479  2.359  0.077  19.370 |

## Categorical variables (eta2)
##                               Dim.1 Dim.2 Dim.3
## VendorID                  | 0.001 0.000 0.008 |
## RateCodeID                 | 0.941 0.021 0.013 |
## Payment_type                | 0.018 0.218 0.012 |
## Trip_type                  | 0.946 0.020 0.014 |
## pick_up_period              | 0.002 0.001 0.024 |
## f.passenger                 | 0.000 0.002 0.003 |
## f.distance                   | 0.002 0.589 0.151 |
## f.pickup_longitude           | 0.081 0.203 0.519 |
## f.pickup_latitude             | 0.047 0.263 0.519 |
## f.dropoff_longitude           | 0.061 0.270 0.412 |
## f.dropoff_latitude             | 0.048 0.249 0.480 |
## f.extra                      | 0.006 0.000 0.000 |

```

```

## f.MTA_tax | 0.941 0.021 0.014 |
## f.Improvement_surcharge | 0.933 0.020 0.014 |
## f.tip_amount | 0.040 0.255 0.004 |
## f.toll | 0.001 0.024 0.029 |
## f.total | 0.001 0.704 0.121 |
## f.ttime | 0.001 0.579 0.110 |

##
## Supplementary categories
## Dim.1   cos2   v.test   Dim.2
## AnyTip No | 0.167  0.039  13.772 | -0.393
## AnyTip Yes | -0.234  0.039 -13.772 |  0.550
## (0,6] | -0.075  0.002 -3.086 | -0.966
## (6,9] | -0.013  0.000 -0.542 | -0.403
## (9,14] |  0.022  0.000  0.892 |  0.369
## (14,43] |  0.072  0.002  2.821 |  1.096
##          cos2   v.test   Dim.3   cos2
## AnyTip No | 0.216 -32.428 | -0.074  0.008
## AnyTip Yes | 0.216  32.428 |  0.104  0.008
## (0,6] | 0.323 -39.632 |  0.459  0.073
## (6,9] | 0.056 -16.554 |  0.157  0.009
## (9,14] | 0.045  14.758 | -0.107  0.004
## (14,43] | 0.375  42.725 | -0.554  0.096
##          v.test
## AnyTip No | -6.121 |
## AnyTip Yes |  6.121 |
## (0,6] | 18.825 |
## (6,9] |  6.433 |
## (9,14] | -4.282 |
## (14,43] | -21.589 |

##
## Supplementary categorical variables (eta2)
## Dim.1 Dim.2 Dim.3
## AnyTip | 0.039 0.216 0.008 |
## f.fare_amount | 0.003 0.601 0.136 |

##
## Supplementary continuous variable
## Dim.1   Dim.2   Dim.3
## Total_amount | -0.017 |  0.752 | -0.324 |

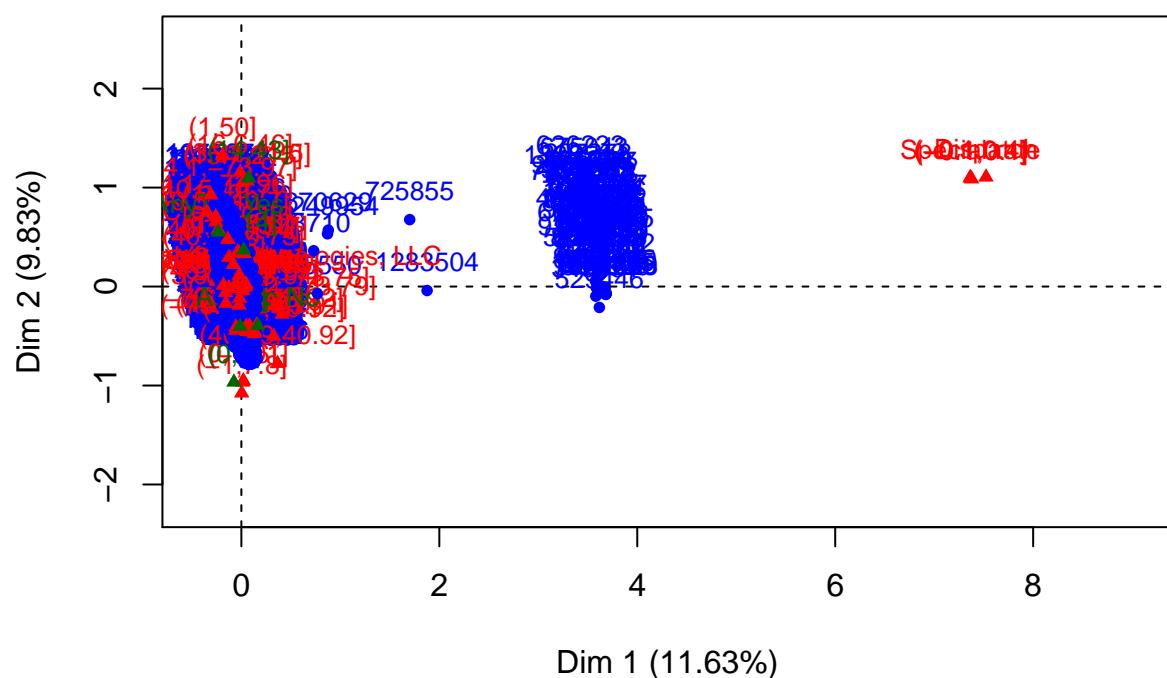
mean(res.mca$eig)

## [1] 26.04711

# Individual Representation
plot.MCA(res.mca, choix=c("ind"), cex=0.8)

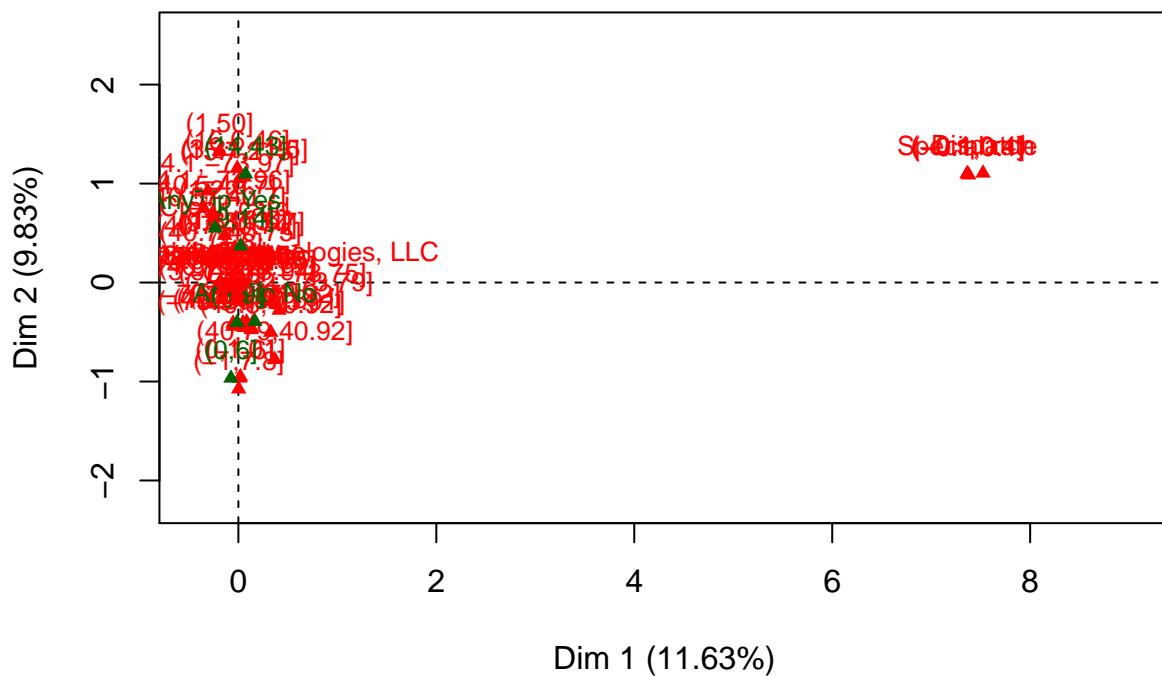
```

MCA factor map



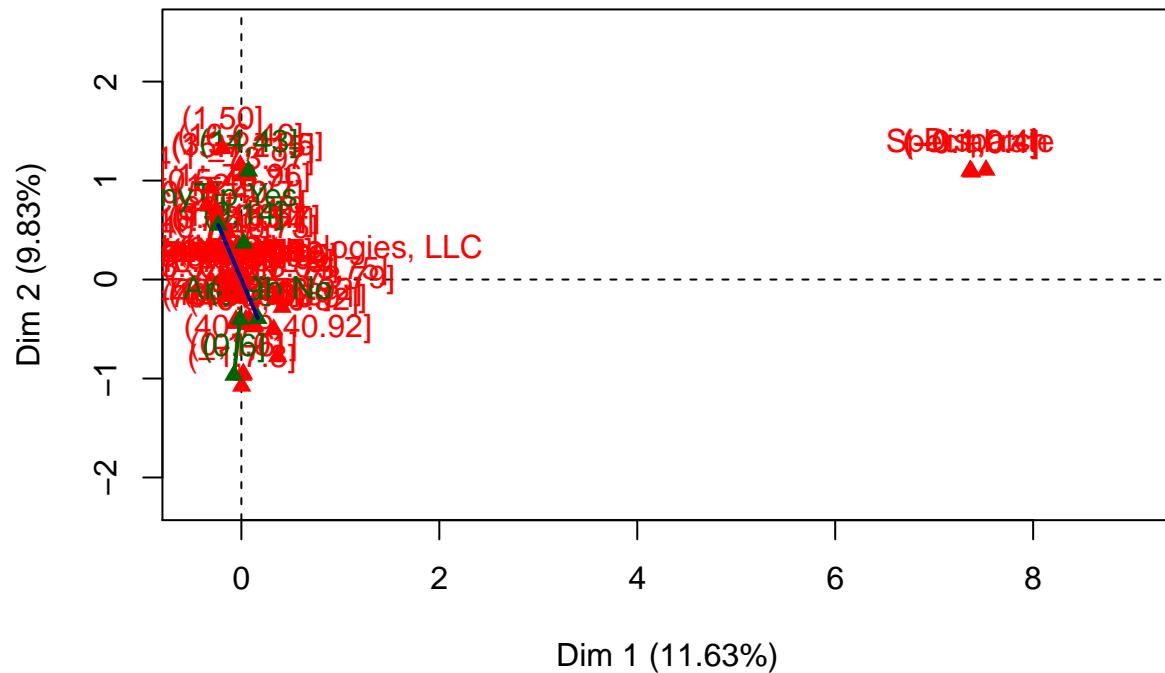
```
plot.MCA(res.mca, choix=c("ind"), invisible=c("ind"), cex=0.8)
```

MCA factor map



```
# Representation of categories
plot.MCA(res.mca, choix=c("ind"), invisible=c("ind"), axes=c(1,2))
lines(res.mca$quali.sup$coord[3:4, 1], res.mca$quali.sup$coord[3:4,2], lwd=2, col="darkgreen") # Trencada
lines(res.mca$quali.sup$coord[1:2,1], res.mca$quali.sup$coord[1:2,2], lwd=2, col="darkblue") # Trencada An
```

MCA factor map

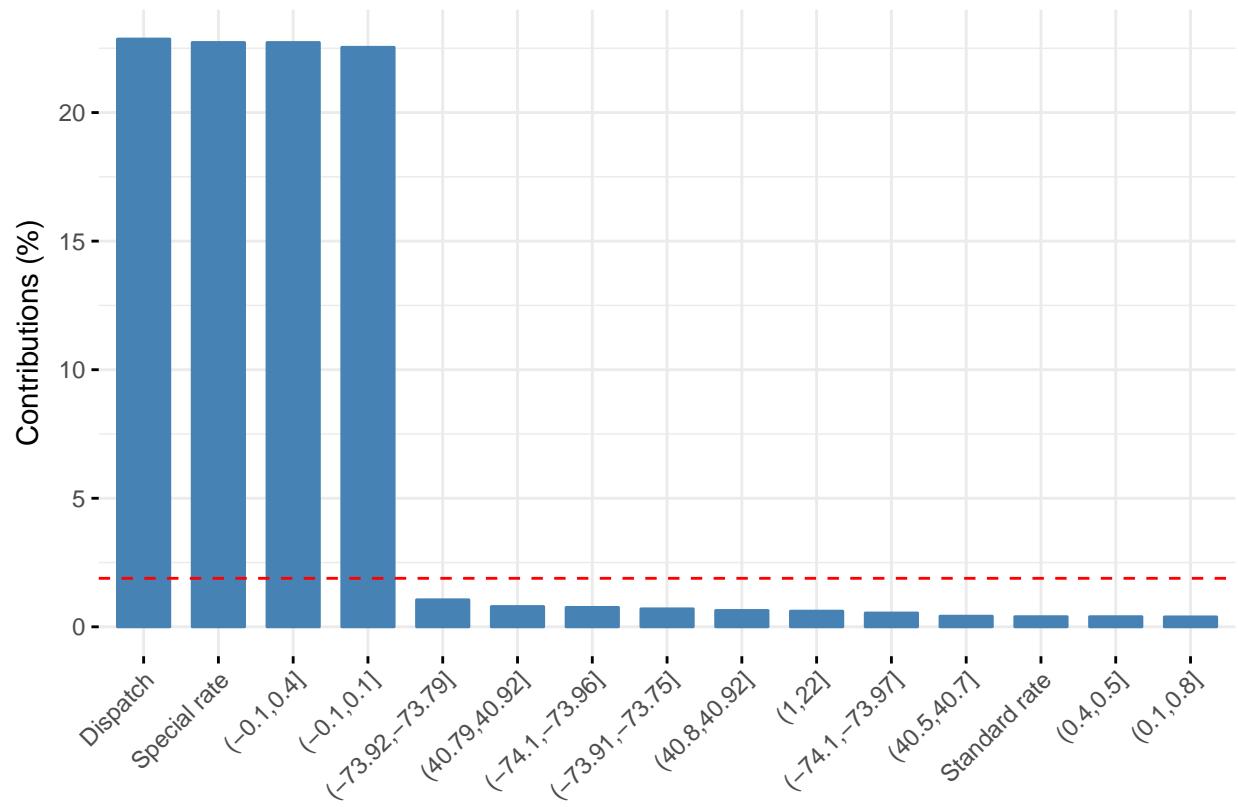


```

names(res.mca)
## [1] "eig"         "call"        "ind"         "var"         "svd"
## [6] "quali.sup"   "quanti.sup"
# Contributions of rows to dimension 1
fviz_contrib(res.mca, choice = "var", axes = 1, top = 15)

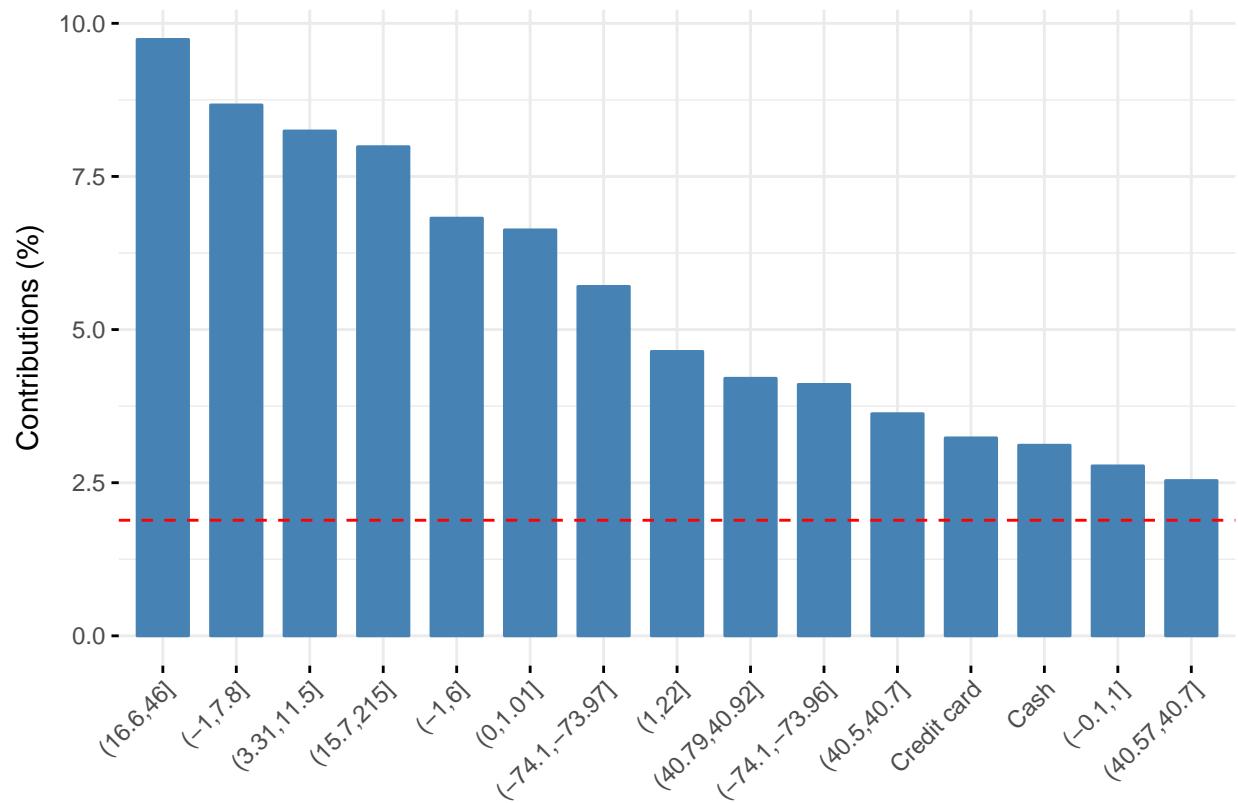
```

Contribution of variables to Dim-1



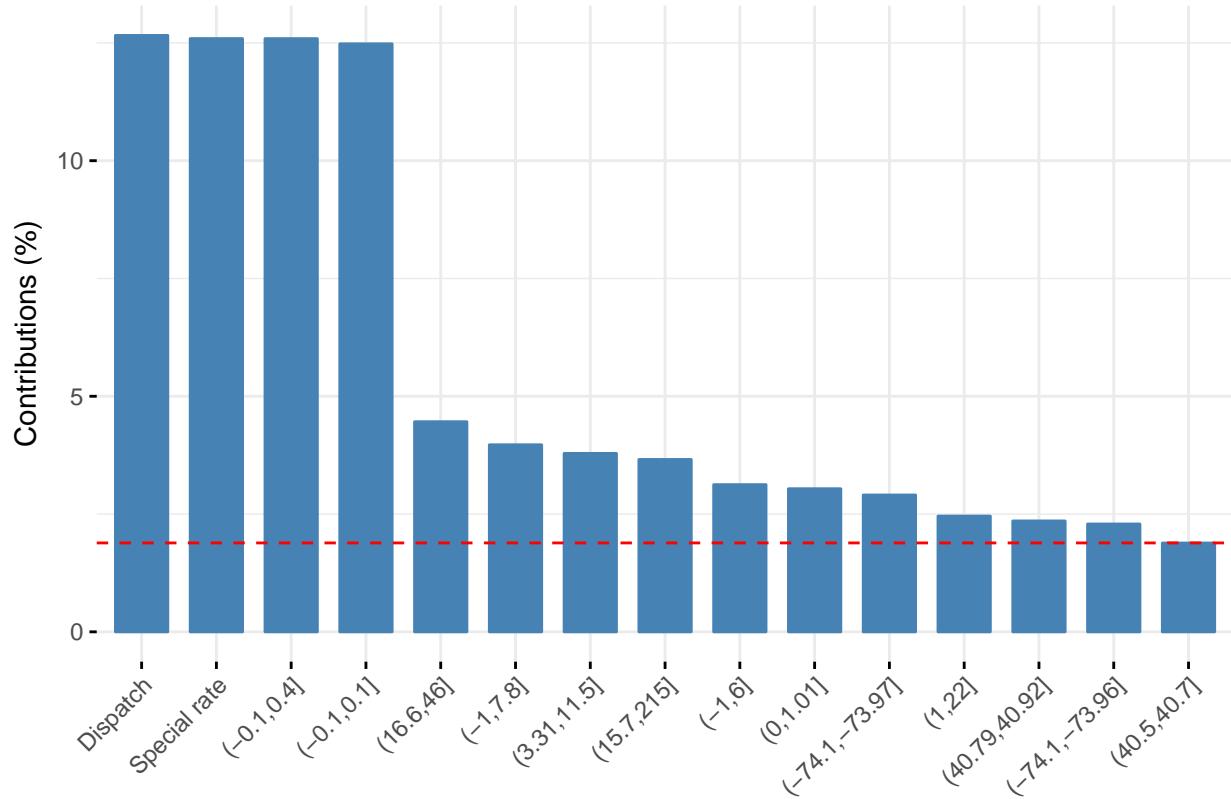
```
# Contributions of rows to dimension 2  
fviz_contrib(res.mca, choice = "var", axes = 2, top = 15)
```

Contribution of variables to Dim–2



```
# Total contribution to dimension 1 and 2  
fviz_contrib(res.mca, choice = "var", axes = 1:2, top = 15)
```

Contribution of variables to Dim-1–2

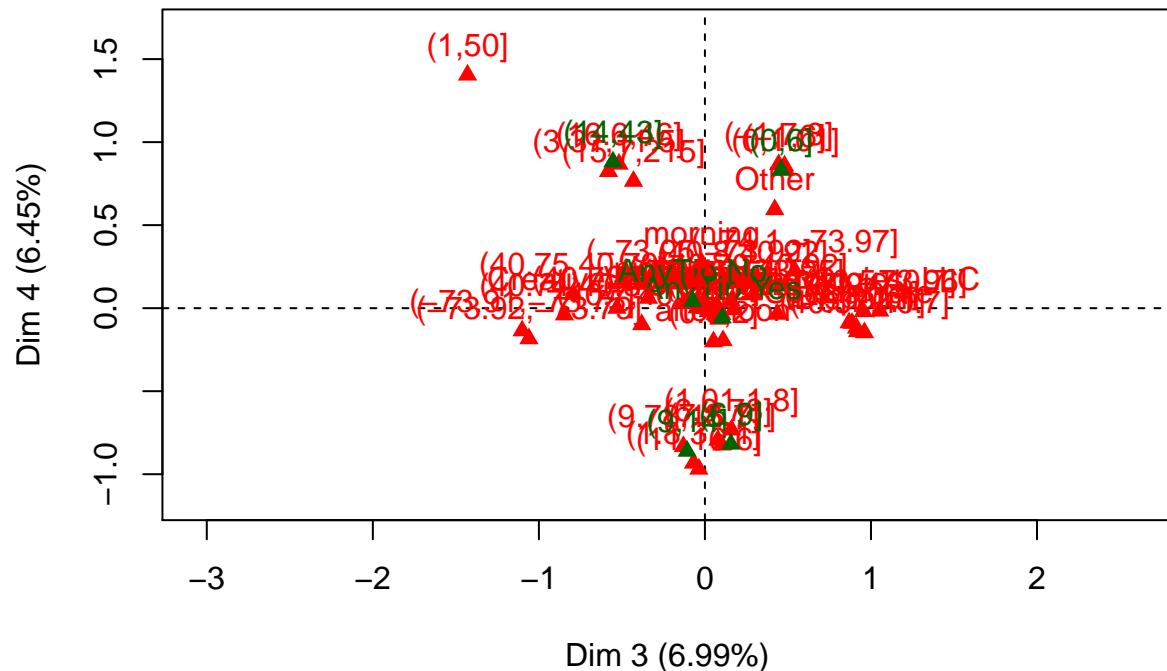


#we see that the provider of the record, categories of the rate code are most contributive and the t
head(round(res.mca\$var\$contrib,2), 10)

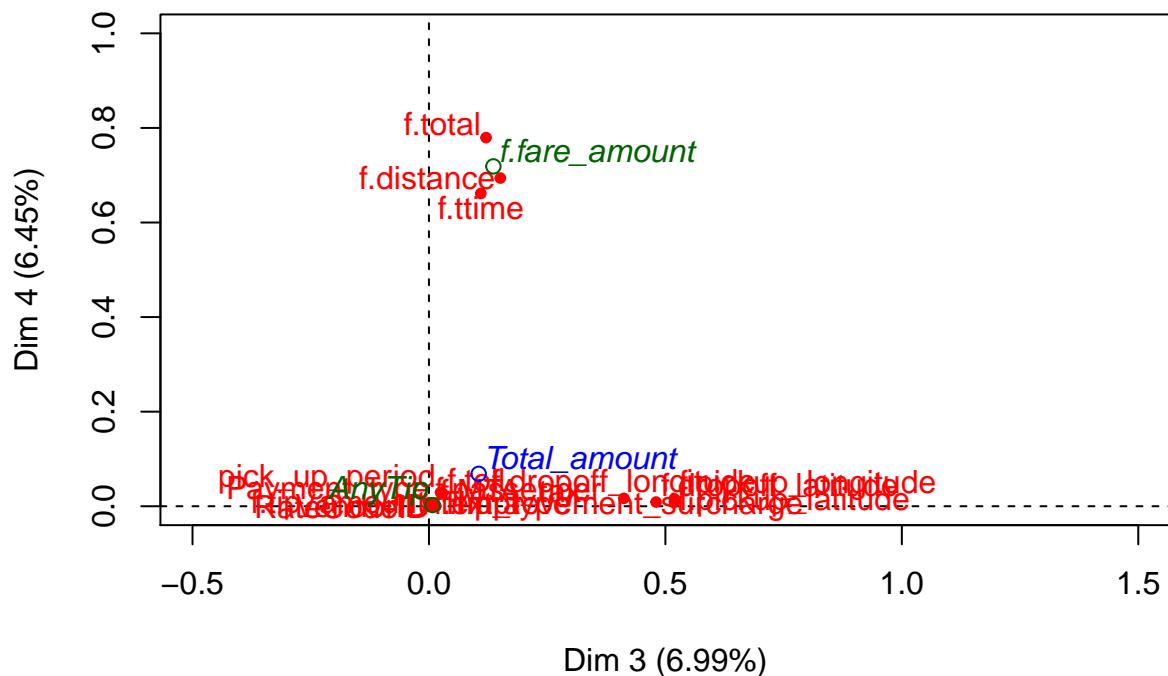
```
##                                     Dim 1 Dim 2 Dim 3 Dim 4 Dim 5
## Creative Mobile Technologies, LLC 0.01  0.00  0.27  0.00  0.00
## VeriFone Inc.                      0.00  0.00  0.07  0.00  0.00
## Standard rate                      0.39  0.01  0.01  0.00  0.00
## Special rate                        22.72  0.60  0.53  0.01  0.07
## Credit card                         0.23  3.23  0.21  0.03  1.65
## Cash                                0.22  3.11  0.23  0.02  1.71
## Other                               0.00  0.01  0.05  0.11  0.13
## Street-hail                          0.38  0.01  0.01  0.00  0.00
## Dispatch                            22.86  0.58  0.56  0.01  0.07
## night                               0.01  0.00  0.77  0.03  0.64
```

```
plot.MCA(res.mca, choix=c("ind"), invisible=c("ind"), axes=c(3,4))
```

MCA factor map



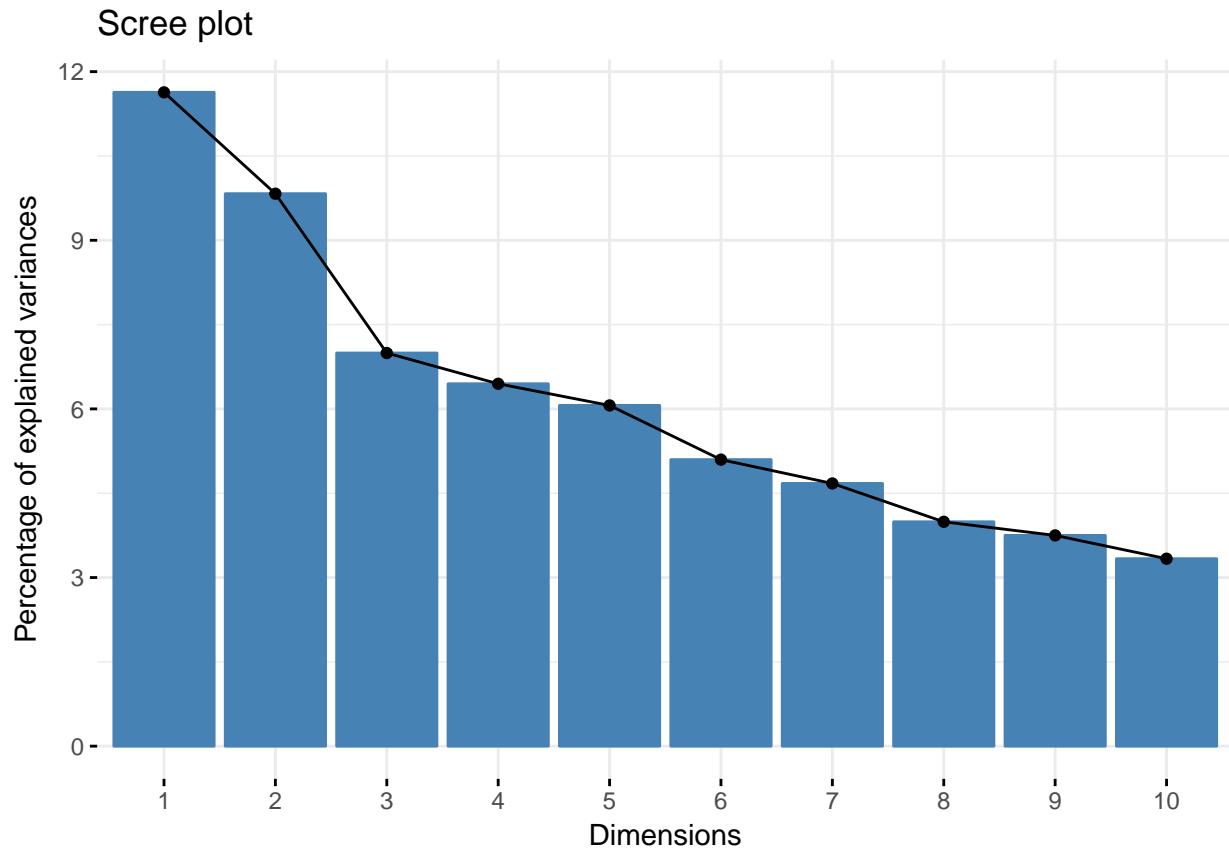
```
plot.MCA(res.mca, choix=c("var"), axes=c(3,4))
```

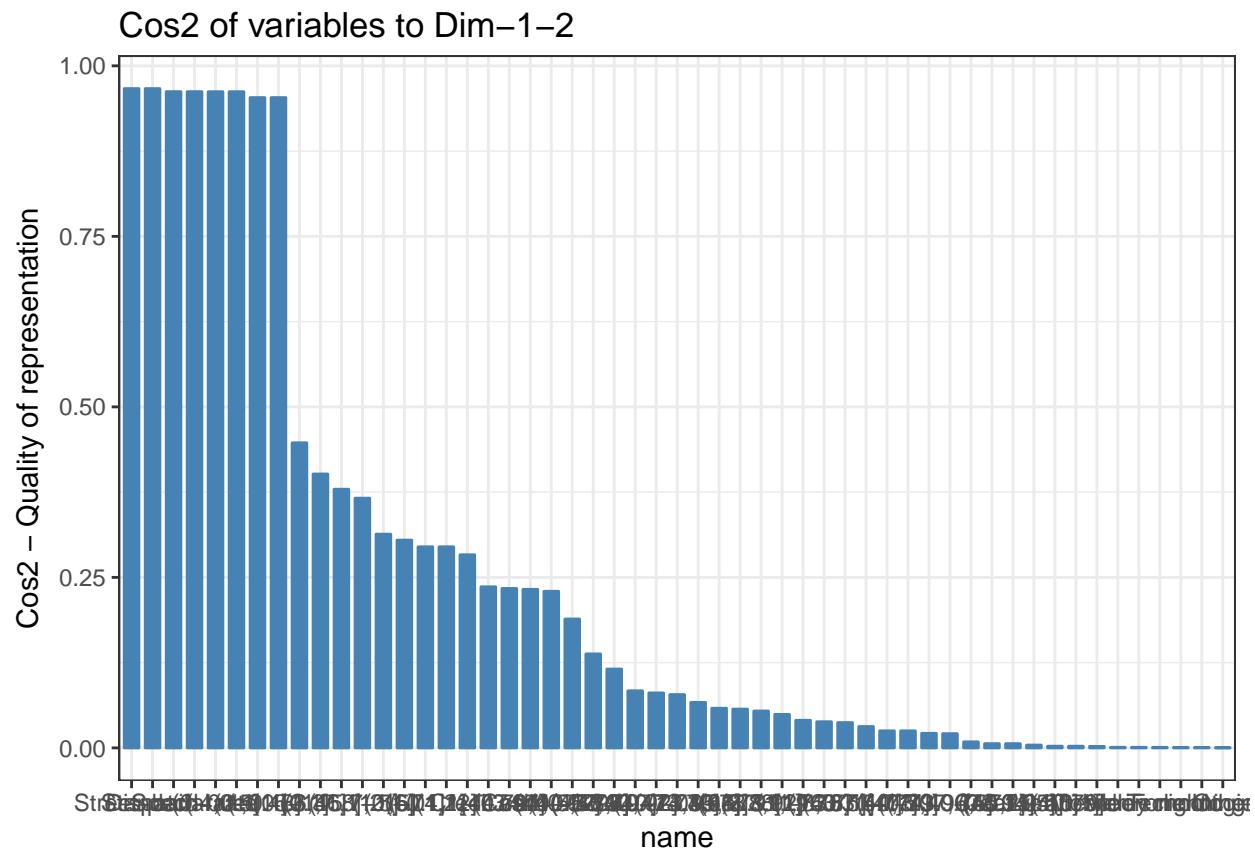


```
# Use modern ggplot facilities
names(res.mca)

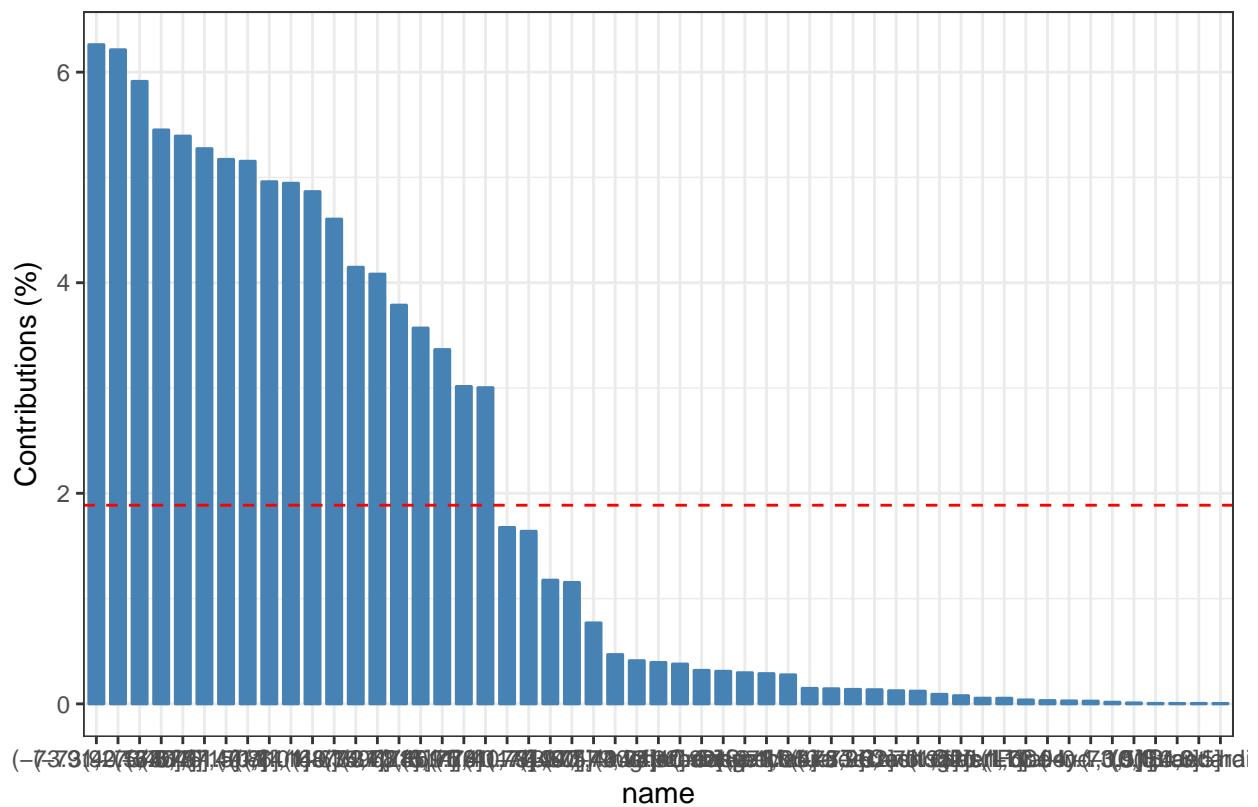
## [1] "eig"      "call"     "ind"      "var"      "svd"
## [6] "quali.sup" "quanti.sup"

fviz_eig(res.mca)
```



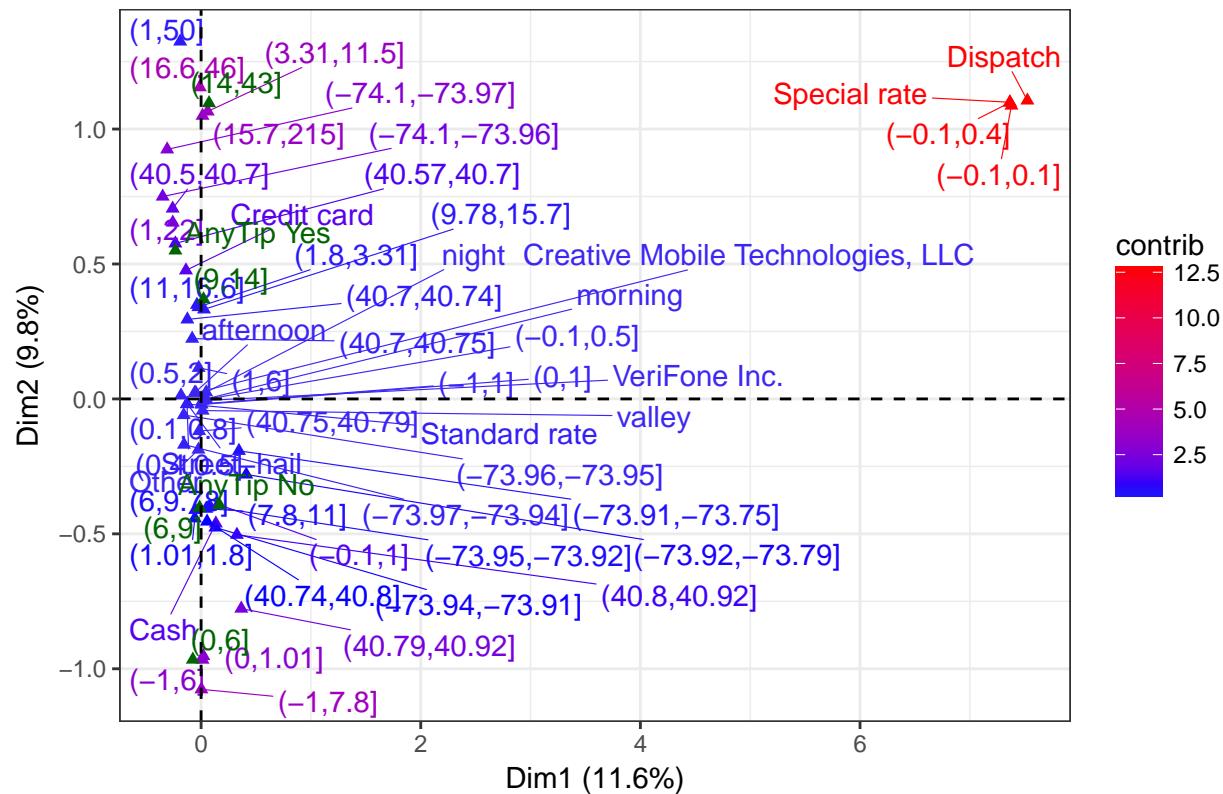


Contribution of variables to Dim–3–4



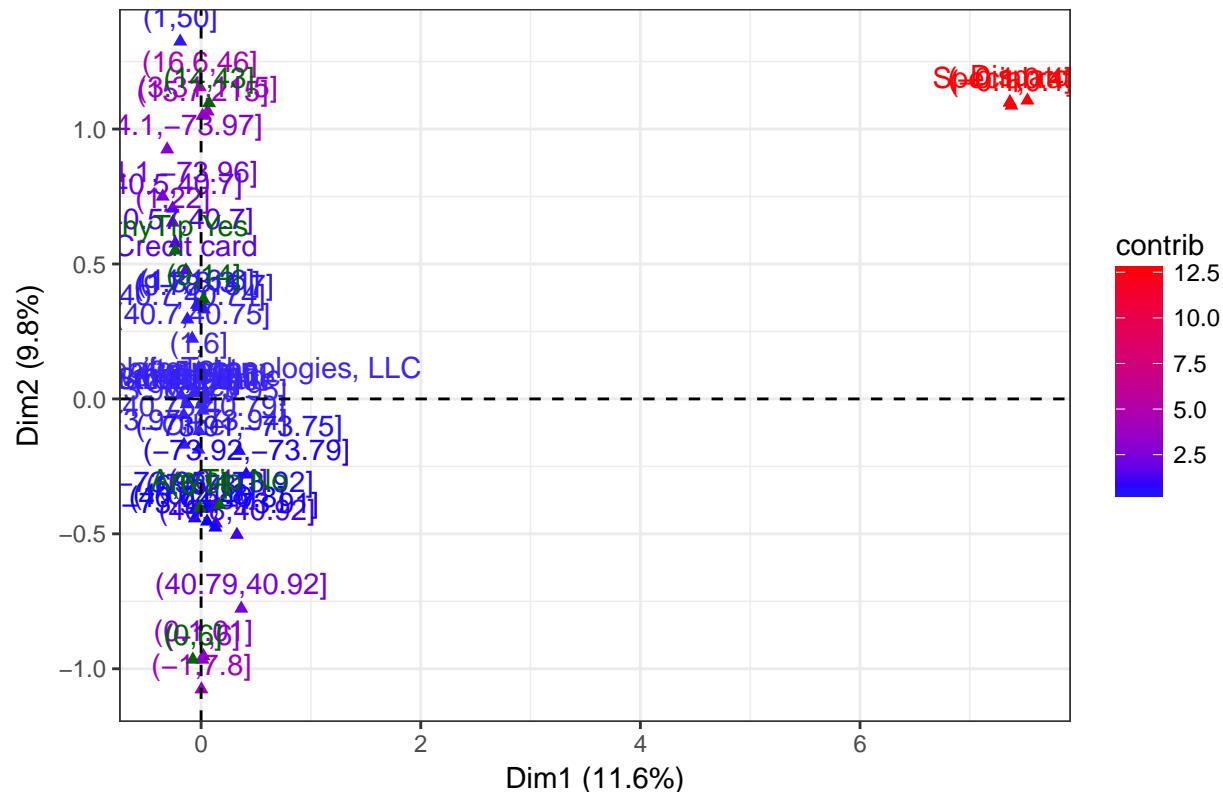
```
fviz_mca_var(res.mca, col.var="contrib", repel=TRUE)+  
  scale_color_gradient2(low="green", mid="blue",  
  high="red", midpoint=0.75)+theme_bw()
```

Variable categories – MCA

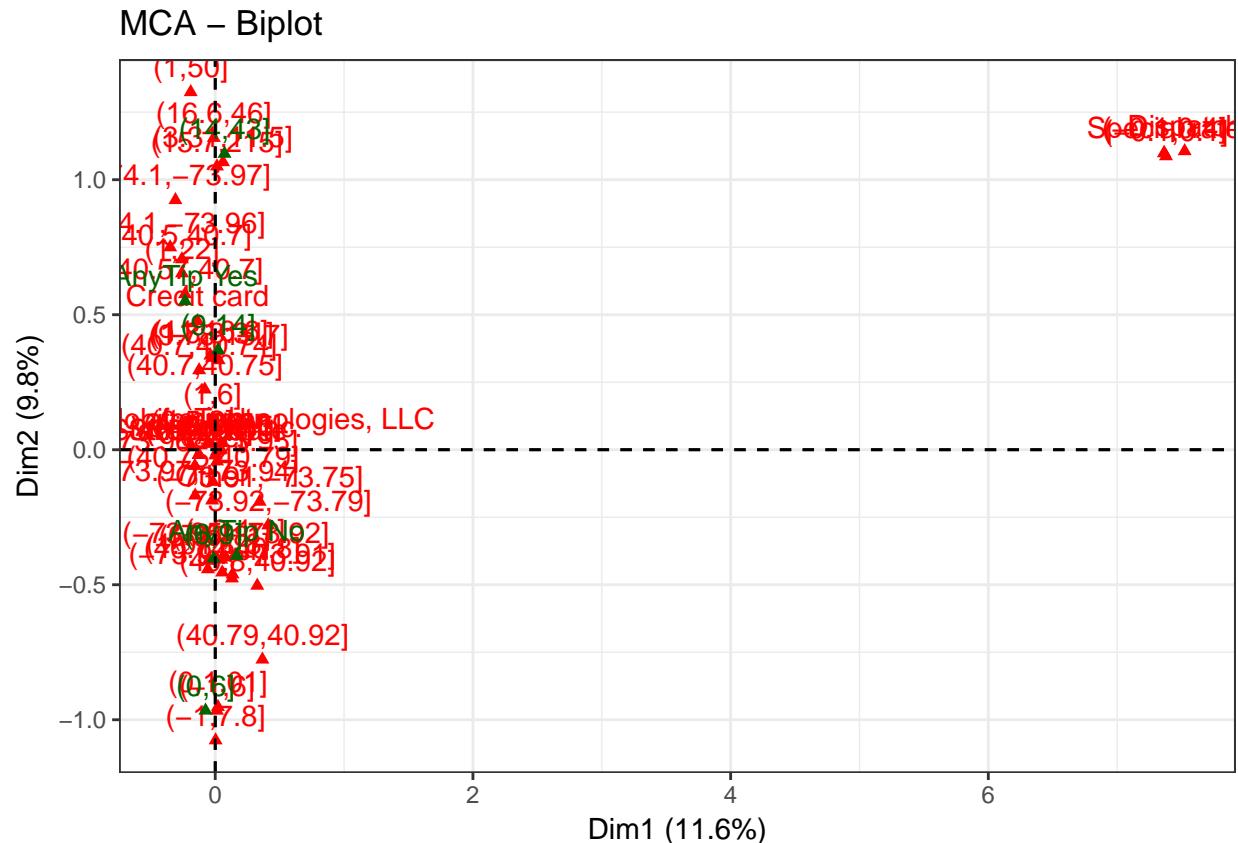


```
fviz_mca_var(res.mca, col.var="contrib", repel=F)+  
  scale_color_gradient2(low="green", mid="blue",  
  high="red", midpoint=0.75)+theme_bw()
```

Variable categories – MCA



```
fviz_mca_biplot(res.mca, invisible="ind", axes=1:2, repel=FALSE)+theme_bw()
```

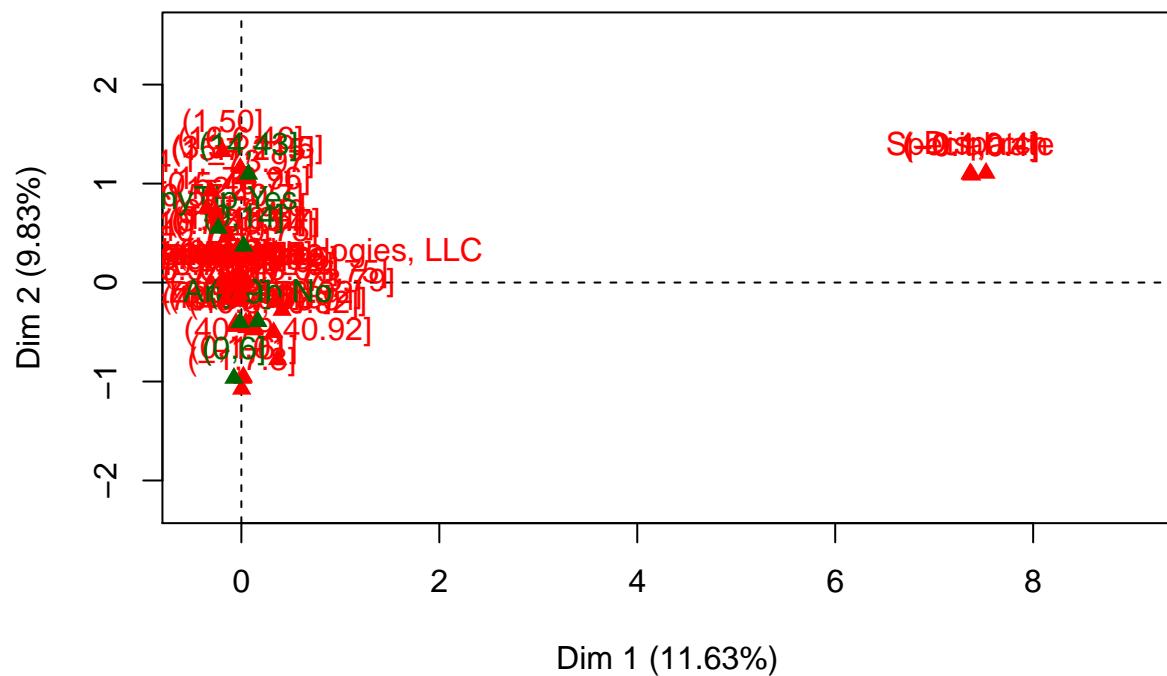


```
#fviz_mca_biplot(res.mca, axes=1:2, repel=TRUE, arrows=c(TRUE, FALSE)) + theme_bw()
```

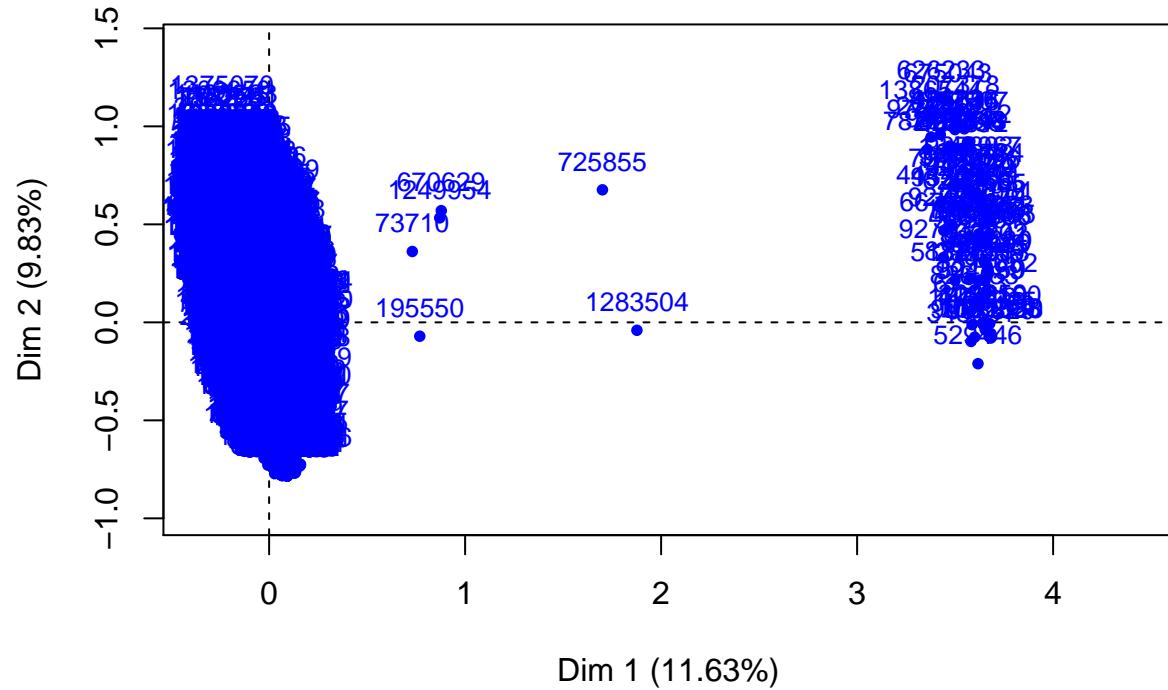
Synthesis through HCPC: Hierarchical Clustering

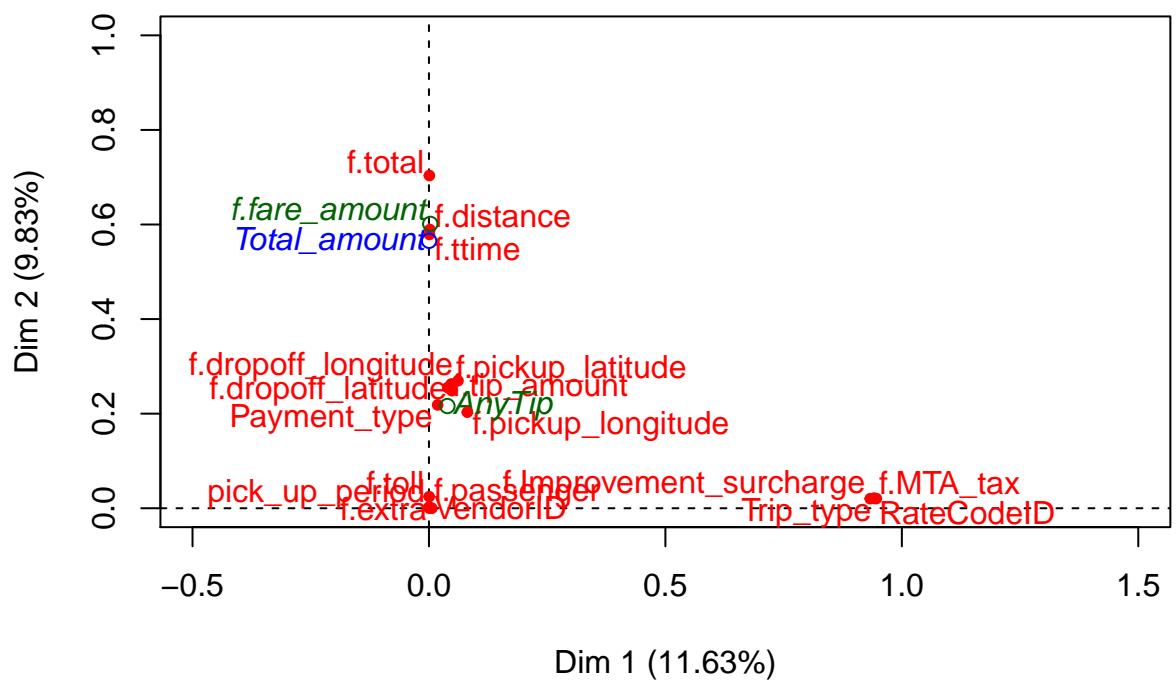
```
###  
### Clustering the individuals  
### Before, you have to perform a MCA with the number of axes  
### that you have decided to take into account (indicated through ncp=)  
?HCPC  
res.mca<-MCA(df[,c(vars_cat,"Total_amount")],quali.sup=c(5,13),quanti.sup=21,ncp=26)
```

MCA factor map

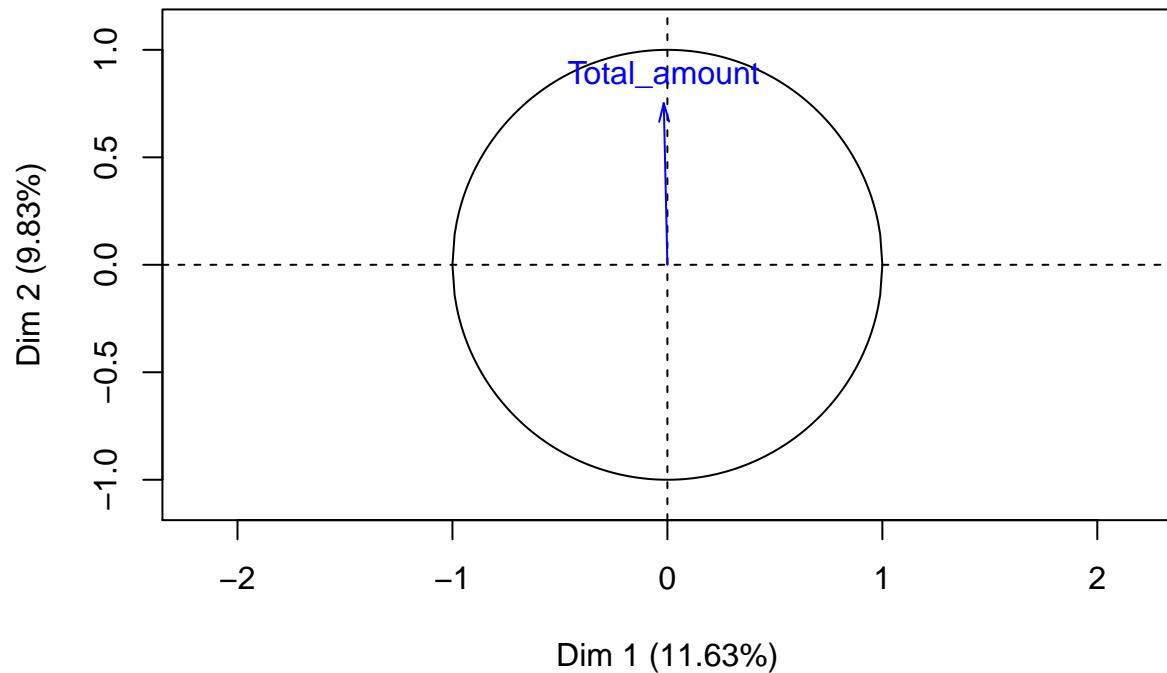


MCA factor map



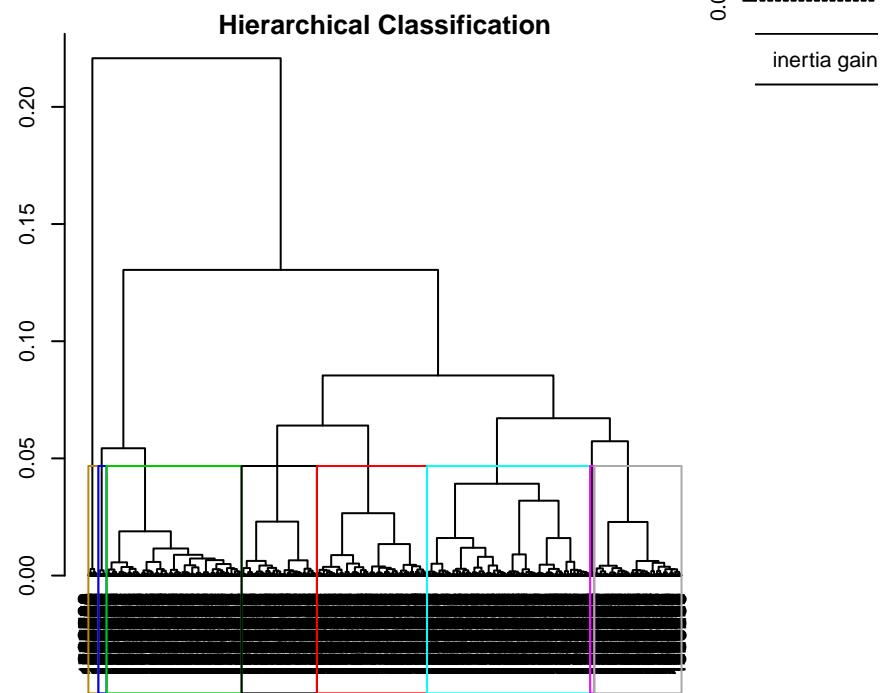


Supplementary variables on the MCA factor map

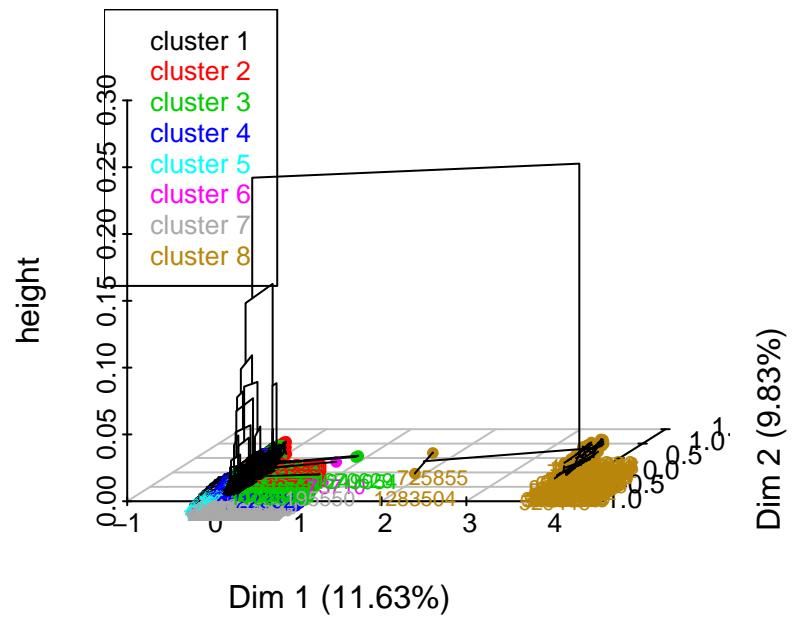


```
res.hcpc<-HCPC(res.mca,nb.clust=8,order=TRUE)
```

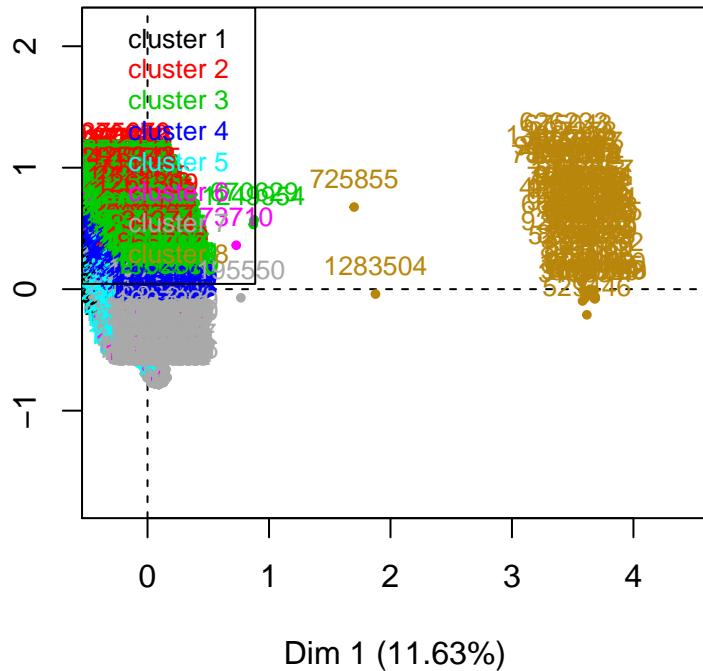
Hierarchical Clustering



Hierarchical clustering on the factor map

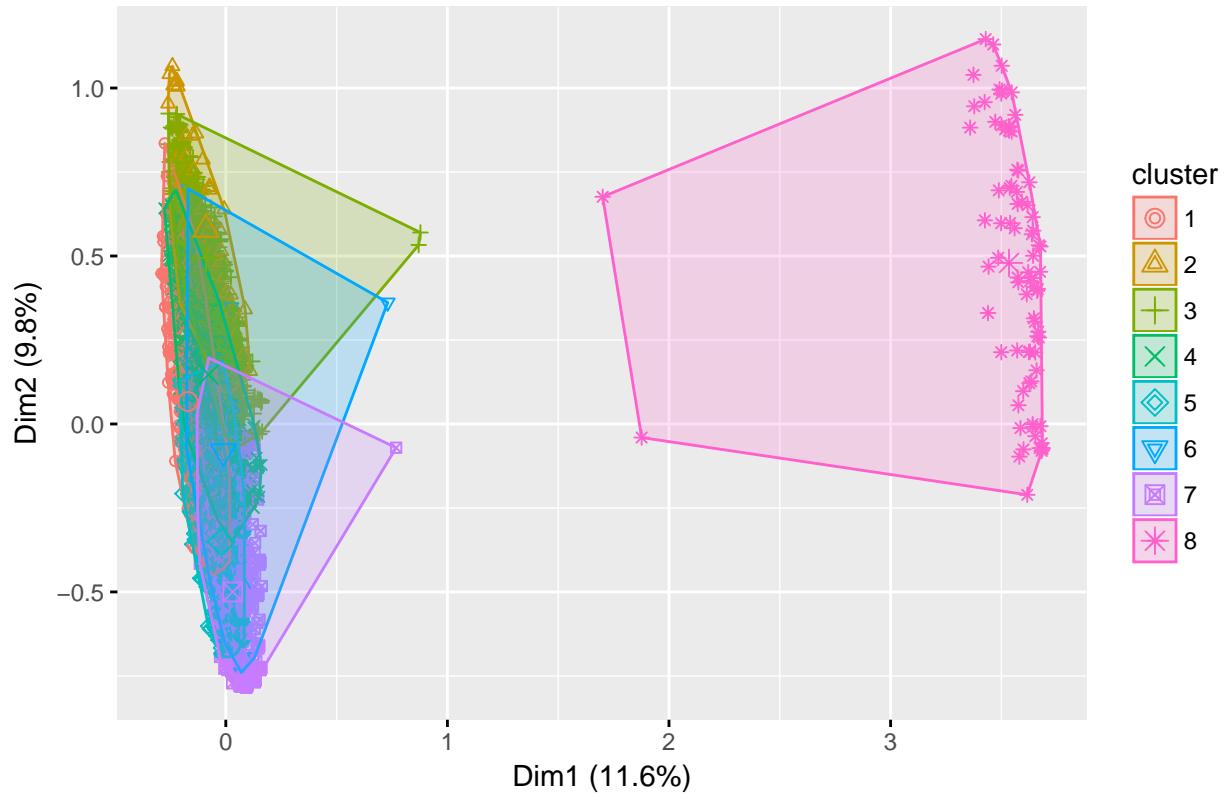


Factor map



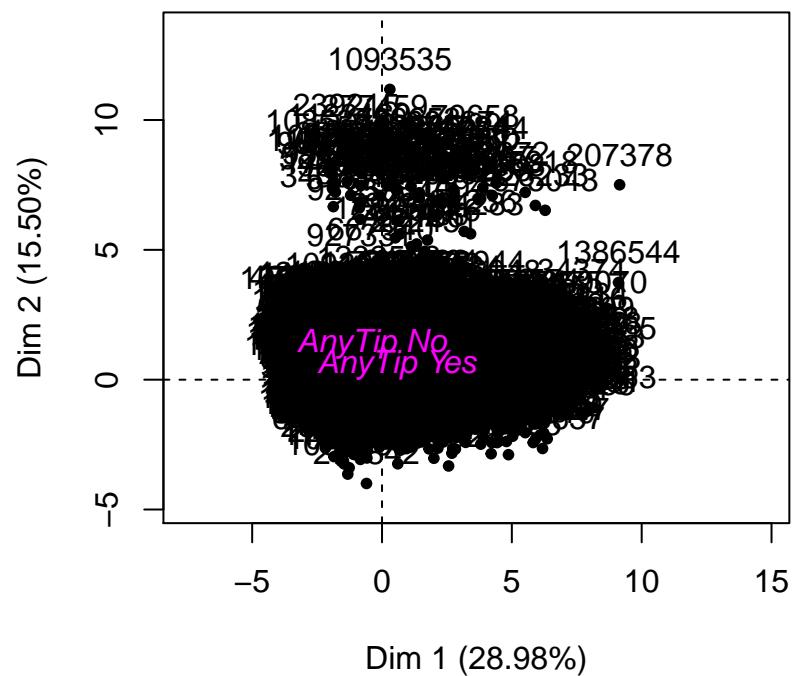
```
names(res.hcpc)  
## [1] "data.clust" "desc.var"    "desc.axes"   "call"        "desc.ind"  
fviz_cluster(res.hcpc, geom = "point", main = "Factor map")
```

Factor map

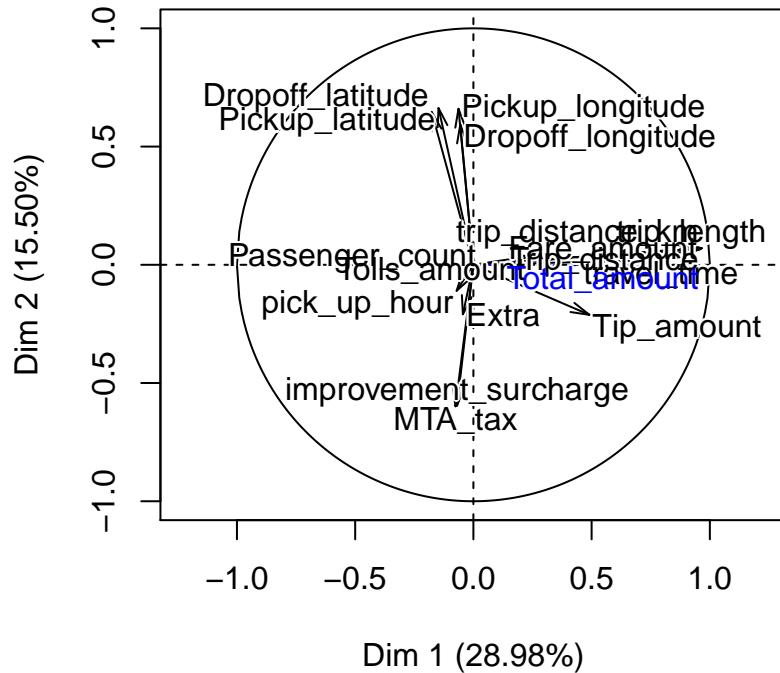


```
#Anytip
vars_con_pca<-c(6,7,8,9,10,11,12,13,14,15,16,17,18,22,23,24,25,26)
res.pca<-PCA(df[,vars_con_pca], quanti.sup = 13, quali.sup = 14, ncp = 6 ) # TotalAmount and AnyTip
```

Individuals factor map (PCA)

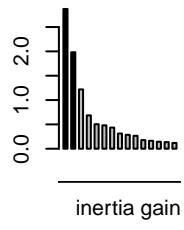
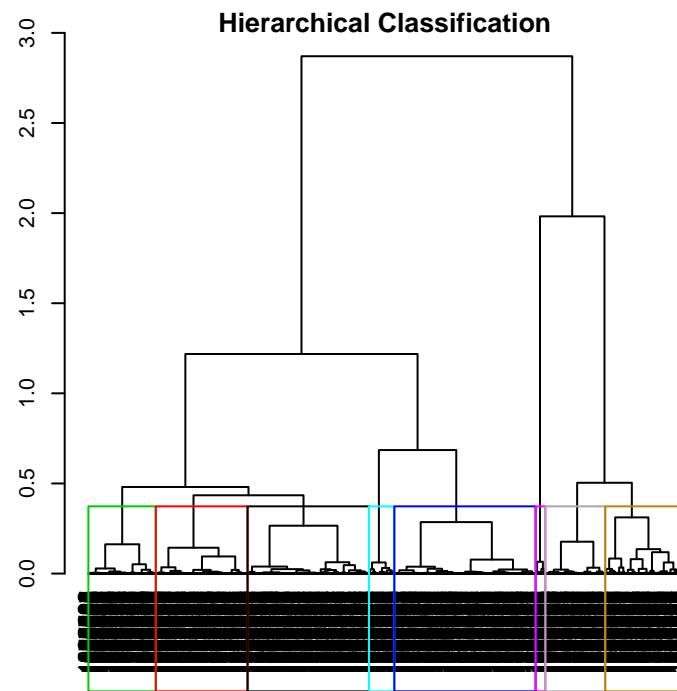


Variables factor map (PCA)

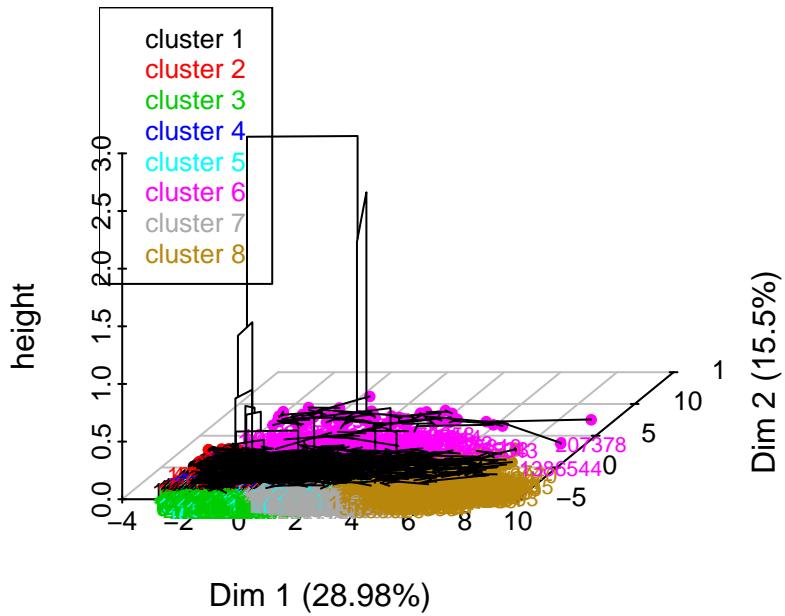


```
res.hcpcPCA <- HCPC(res.pca, nb.clust = 8, order=TRUE)
```

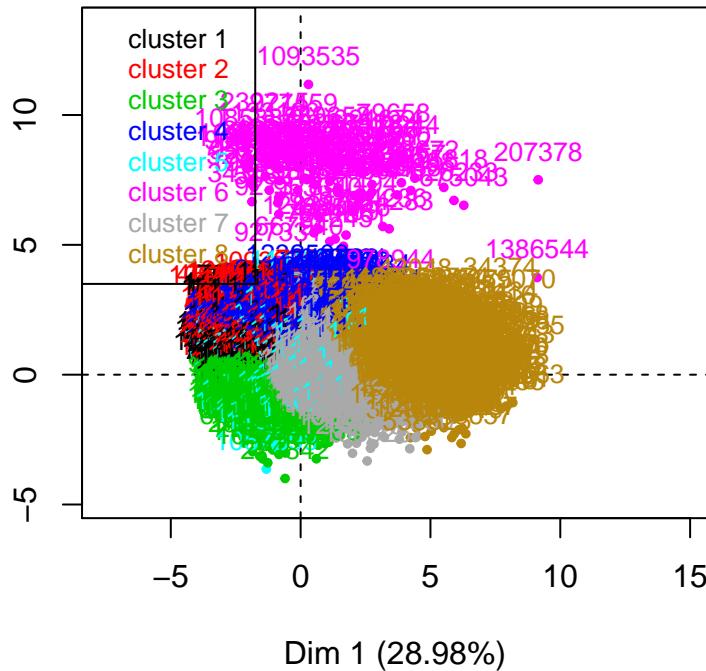
Hierarchical Clustering



Hierarchical clustering on the factor map



Factor map



```
table (res.hcpc$data.clust$clust, res.hcpcPCA$data.clust$clust)
```

```
##  
##      1   2   3   4   5   6   7   8  
##  1   0   1 608   7  27   0  19   0  
##  2   1   2   0   0   3   0  14  47  
##  3  14  21   8  93  36   0 546 369  
##  4 167 174 277 183  56   0 141   0  
##  5 184 230 253 356  84   0   0   1  
##  6   5  11   6   0   0   0   9   3  
##  7 264 523   0   3  32   0   3   3  
##  8   0   0   0   0   0  81   1   0
```

```
claHPPCA<-factor(res.hcpcPCA$data.clust$clust,labels=paste("kHP-",1:8))
```

```
claHP<-factor(res.hcpc$data.clust$clust,levels=c(5,7,1,4,2,8,3,6),labels=c("kKM-5","kKM-7","kKM-1","kKM-2","kKM-3","kKM-4","kKM-5","kKM-6"))
```

```
tt
```

```
##      claHP  
## claHPPCA kKM-5 kKM-7 kKM-1 kKM-4 kKM-2 kKM-8 kKM-3 kKM-6  
##  kHP- 1    184    264     0    167     1     0    14     5  
##  kHP- 2    230    523     1    174     2     0    21    11  
##  kHP- 3    253     0    608    277     0     0     8     6  
##  kHP- 4    356     3     7    183     0     0    93     0  
##  kHP- 5     84    32    27    56     3     0    36     0  
##  kHP- 6     0     0     0     0     0    81     0     0  
##  kHP- 7     0     3    19   141    14     1    546     9
```

```

##    kHP- 8      1      3      0      0     47      0     369      3
sum(diag(tt))/sum(tt))

## [1] 0.4379367
#F.total
vars_con_pca<-c(6,7,8,9,10,11,12,13,14,15,16,17,18,23,24,25,26,41)
names(df[,vars_con_pca])

## [1] "Pickup_longitude"      "Pickup_latitude"
## [3] "Dropoff_longitude"     "Dropoff_latitude"
## [5] "Passenger_count"       "Trip_distance"
## [7] "Fare_amount"           "Extra"
## [9] "MTA_tax"                "Tip_amount"
## [11] "Tolls_amount"          "improvement_surcharge"
## [13] "Total_amount"          "trip_length"
## [15] "trip_distance_km"      "travel_time"
## [17] "pick_up_hour"          "f.total"

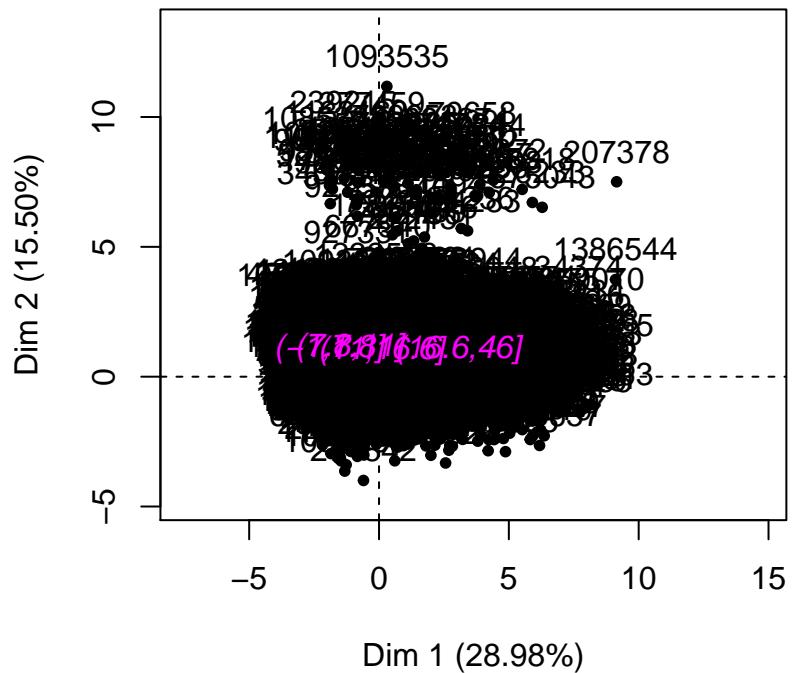
names(df)

## [1] "VendorID"                  "lpep_pickup_datetime"
## [3] "Lpep_dropoff_datetime"     "Store_and_fwd_flag"
## [5] "RateCodeID"                "Pickup_longitude"
## [7] "Pickup_latitude"           "Dropoff_longitude"
## [9] "Dropoff_latitude"          "Passenger_count"
## [11] "Trip_distance"             "Fare_amount"
## [13] "Extra"                     "MTA_tax"
## [15] "Tip_amount"                "Tolls_amount"
## [17] "improvement_surcharge"    "Total_amount"
## [19] "Payment_type"              "Trip_type"
## [21] "mis_ind"                  "AnyTip"
## [23] "trip_length"               "trip_distance_km"
## [25] "travel_time"                "pick_up_hour"
## [27] "pick_up_period"            "espeed"
## [29] "f.passenger"                "f.distance"
## [31] "f.pickup_longitude"        "f.pickup_latitude"
## [33] "f.dropoff_longitude"       "f.dropoff_latitude"
## [35] "f.fare_amount"              "f.extra"
## [37] "f.MTA_tax"                  "f.Improvement_surcharge"
## [39] "f.tip_amount"                "f.toll"
## [41] "f.total"                   "f.ttime"

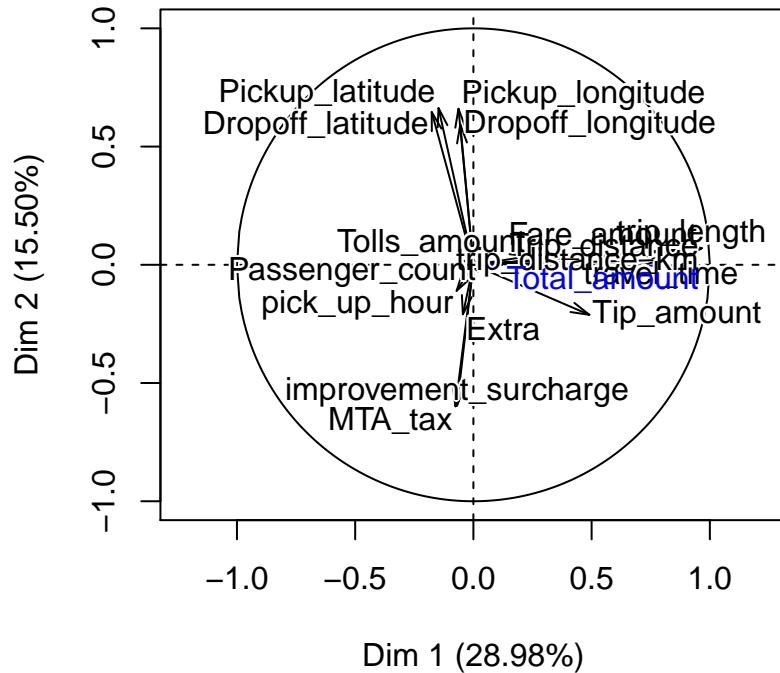
res.pca<-PCA(df[,vars_con_pca], quanti.sup = 13, quali.sup = 18, ncp = 6 ) # TotalAmount and f.total

```

Individuals factor map (PCA)

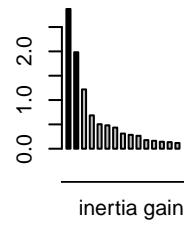
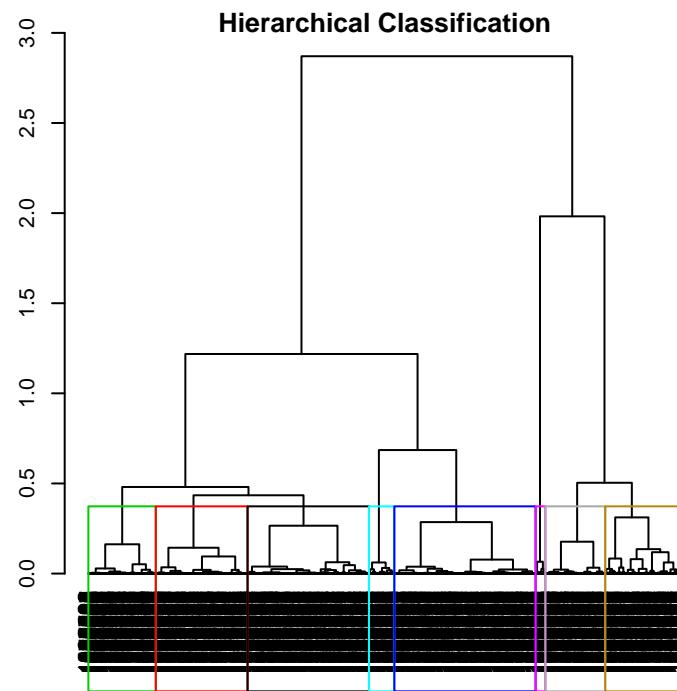


Variables factor map (PCA)

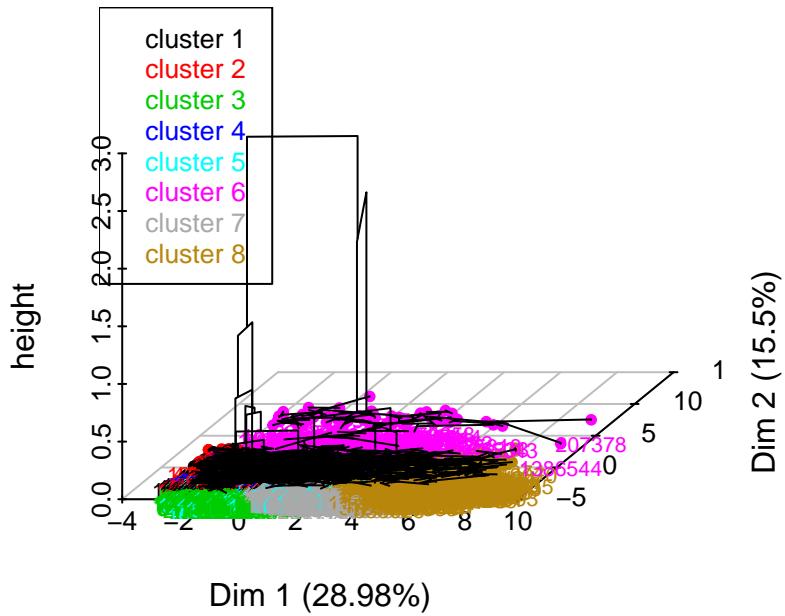


```
res.hcpcPCA <- HCPC(res.pca, nb.clust = 8, order=TRUE)
```

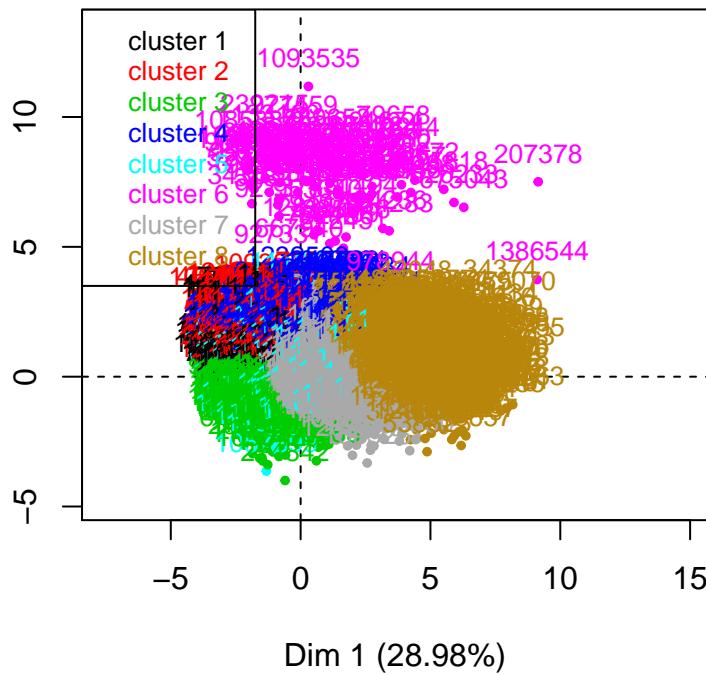
Hierarchical Clustering



Hierarchical clustering on the factor map



Factor map



```

claHPPCA<-factor(res.hcpcPCA$data.clust$clust,labels=paste("kHP-",1:8))
claHP<-factor(res.hcpc$data.clust$clust,levels=c(4,7,1,5,2,8,3,6),labels=c("kKM-5","kKM-7","kKM-1","kKM-2","kKM-3","kKM-4","kKM-5","kKM-6"))
tt<-table(claHPPCA,claHP)
tt

##          claHP
##  claHPPCA kKM-5 kKM-7 kKM-1 kKM-4 kKM-2 kKM-8 kKM-3 kKM-6
##    kHP- 1    167    264     0    184     1     0    14     5
##    kHP- 2    174    523     1    230     2     0    21    11
##    kHP- 3    277     0    608    253     0     0     8     6
##    kHP- 4    183     3     7    356     0     0    93     0
##    kHP- 5     56    32    27    84     3     0    36     0
##    kHP- 6     0     0     0     0     0    81     0     0
##    kHP- 7   141     3    19     0    14     1   546     9
##    kHP- 8     0     3     0     1    47     0   369     3

sum(diag(tt))/sum(tt))

## [1] 0.4699959

```