

# IC3 Proposal

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## 1 Implementing IC3 Model Checking

### 1.1 Our understanding of the algorithm

- We need to maintain a sequence of frames  $R_i$ .
- Each frame is a CNF formula representing the set of states.
- We query to check  $(R_n \wedge \neg P)$  is sat.
- If  $(R_n \wedge \neg P)$  is unsat
  - We create a new empty frame  $R_{(n+1)}$ .
  - We try to push clauses from previous frames to this.
  - A clause  $c$  can be pushed if  $R_j \wedge T \wedge \neg c'$  is unsat. (this is the propagation phase)
- If  $(R_n \wedge \neg P)$  is sat
  - We can find a cube  $s$  such that  $s$  is subset of  $R_n$  and doesn't satisfy the property.
  - We need to block such  $s$  in  $R_n$ .
  - To block this in  $R_n$ , we query  $(R_{(n-1)} \wedge T \wedge s')$ .
  - If unsat, then  $s$  is blocked in  $R_n$ . We need to add  $\neg s$  to  $R_n$ .
  - If sat, We get a new cube which needs to be blocked in  $R_{(n-1)}$ .
  - At this point, we proceed as we did previously.
  - If the model doesn't satisfy the property, we'll get a cube which needs to be blocked, but it intersects with the initial state (and can't be blocked)

Each time IC3 blocks Bad for one additional level, it enters the propagation phase.

## 1.2 Pseudo code for the blocking phase.

- Q is the queue maintaining the proof obligations
- A proof obligation is a tuple  $\langle s, f \rangle$  where f is a frame, and s is the cube we want to block in frame f.

```
While !Empty(Q) do
   $\langle s, f \rangle \leftarrow \text{pop}(Q)$ 
  assert  $\sim s$  is (f - 1) invariant

  if f = 0 then
    return Error "Counter Example Found"

  if SAT( $\sim s \wedge R_{(f-1)} \wedge T \wedge s'$ )           -- Optimization 2 in the paper

    t  $\leftarrow$  get predecessors of (s)
    Add (Q,  $\langle t, f-1 \rangle$ )
    Add (Q,  $\langle s, f \rangle$ )
  else
    ?? (generalizaiton part)                       -- Optimization 1 in the paper
```