

Chapter : 16. COORDINATE GEOMETRY

Exercise : 16A

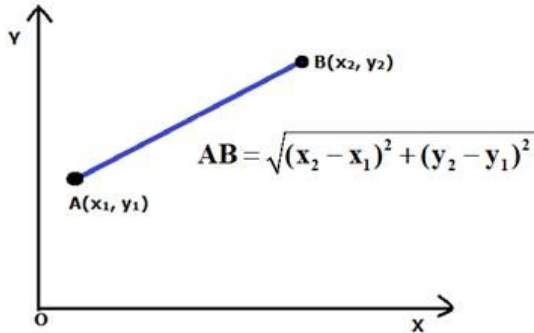
Question: 1 A

Find the distance

Solution:

In this question, we have to use the distance formula to find the distance between two points which is given by, say for points $P(x_1, y_1)$ and $Q(x_2, y_2)$ then

$$PQ = \sqrt{(x_2 - x_1)^2 + (y_2 - y_1)^2}$$



$$AB = \sqrt{\{(15 - 9)^2 + (11 - 3)^2\}}$$

$$= \sqrt{\{(6)^2 + (8)^2\}}$$

$$= \sqrt{\{36 + 64\}}$$

$$= \sqrt{100}$$

$$\therefore AB = 10 \text{ units.}$$

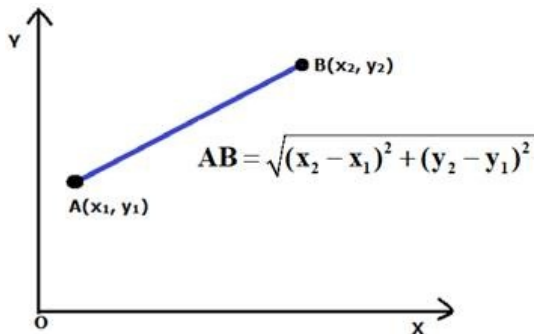
Question: 1 B

Find the distance

Solution:

In this question, we have to use the distance formula to find the distance between two points which is given by, say for points $P(x_1, y_1)$ and $Q(x_2, y_2)$ then

$$PQ = \sqrt{(x_2 - x_1)^2 + (y_2 - y_1)^2}$$



$$AB = \sqrt{\{(-5 - 7)^2 + (1 - (-4))^2\}}$$

$$= \sqrt{\{(-12)^2 + (5)^2\}}$$

$$= \sqrt{\{144 + 25\}}$$

$$= \sqrt{169}$$

$$\therefore AB = 13 \text{ units}$$

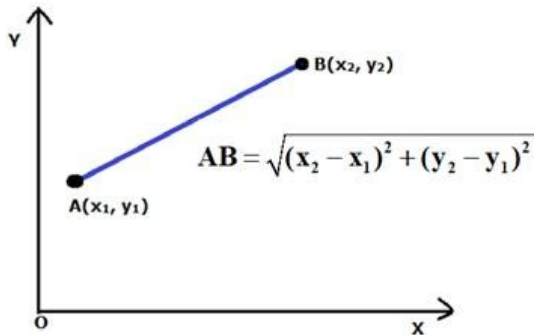
Question: 1 C

Find the distance

Solution:

In this question, we have to use the distance formula to find the distance between two points which is given by, say for points $P(x_1, y_1)$ and $Q(x_2, y_2)$ then

$$PQ = \sqrt{(x_2 - x_1)^2 + (y_2 - y_1)^2}$$



$$AB = \sqrt{\{9 - (-6)\}^2 + \{-12 - (-4)\}^2}$$

$$= \sqrt{\{(15)^2 + (-8)^2\}}$$

$$= \sqrt{\{225 + 64\}}$$

$$= \sqrt{289}$$

$$\therefore AB = 17 \text{ units}$$

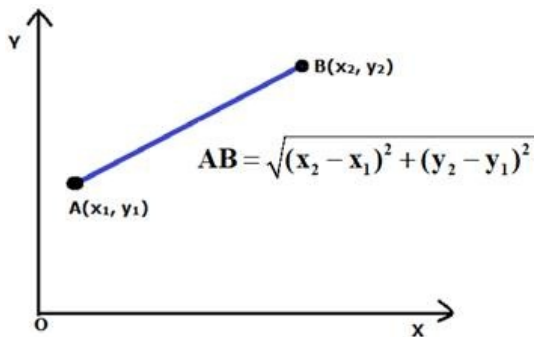
Question: 1 D

Find the distance

Solution:

In this question, we have to use the distance formula to find the distance between two points which is given by, say for points $P(x_1, y_1)$ and $Q(x_2, y_2)$ then

$$PQ = \sqrt{(x_2 - x_1)^2 + (y_2 - y_1)^2}$$



$$AB = \sqrt{\{4 - 1\}^2 + \{-6 - (-3)\}^2}$$

$$= \sqrt{\{(3)^2 + (-3)^2\}}$$

$$= \sqrt{\{9 + 9\}}$$

$$= \sqrt{18}$$

$$\therefore AB = 3\sqrt{2} \text{ units}$$

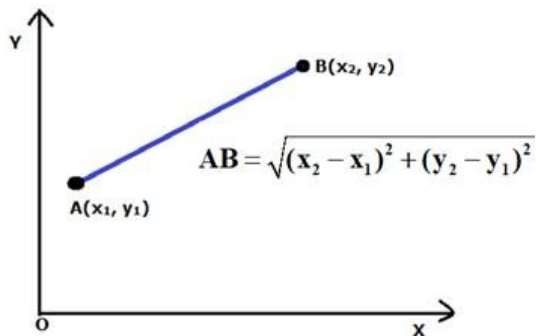
Question: 1 E

Find the distance

Solution:

In this question, we have to use the distance formula to find the distance between two points which is given by, say for points $P(x_1, y_1)$ and $Q(x_2, y_2)$ then

$$PQ = \sqrt{(x_2 - x_1)^2 + (y_2 - y_1)^2}$$



$$AB = \sqrt{\{((a - b) - (a + b))^2 + ((a + b) - (a - b))^2\}}$$

$$= \sqrt{\{(-2b)^2 + (2b)^2\}}$$

$$= \sqrt{\{4b^2 + 4b^2\}}$$

$$= \sqrt{8b^2}$$

$$\therefore AB = 2\sqrt{2}b \text{ units}$$

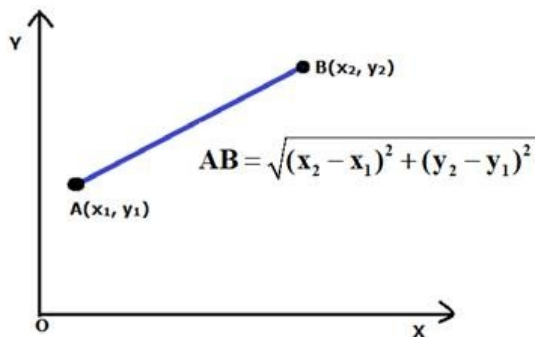
Question: 1 F

Find the distance

Solution:

In this question, we have to use the distance formula to find the distance between two points which is given by, say for points $P(x_1, y_1)$ and $Q(x_2, y_2)$ then

$$PQ = \sqrt{(x_2 - x_1)^2 + (y_2 - y_1)^2}$$



$$PQ = \sqrt{\{(a \cos a - a \sin a)^2 - (-a \sin a - a \cos a)^2\}}$$

$$= \sqrt{\{a^2 \cos^2 a + a^2 \sin^2 a - 2a^2 \sin a \cos a + a^2 \cos^2 a + a^2 \sin^2 a + 2a^2 \sin a \cos a\}}$$

$$= \sqrt{\{a^2 (\cos^2 a + \sin^2 a) + (a^2 (\cos^2 a + \sin^2 a))\}}$$

$$= \sqrt{a^2(1) + a^2(1)}$$

$$= \sqrt{a^2(1 + 1)}$$

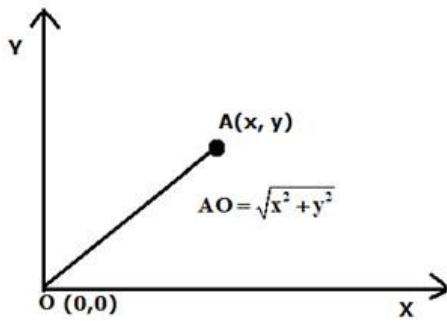
$$\therefore PQ = a\sqrt{2} \text{ units}$$

Question: 2 A

Find the distance

Solution:

Since it is given that the distance is to be found from origin so in this question we have to use the distance formula keeping one - point fix i.e. O (0,0), as shown below:



$$OA = \sqrt{\{(5 - 0)^2 + (-12 - 0)^2\}}$$

$$= \sqrt{\{(5)^2 + (-12)^2\}}$$

$$= \sqrt{\{25 + 144\}}$$

$$= \sqrt{169}$$

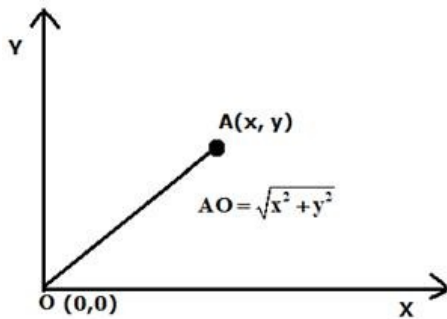
$$\therefore OA = 13 \text{ units}$$

Question: 2 B

Find the distance

Solution:

Since it is given that the distance is to be found from origin so in this question we have to use the distance formula keeping one - point fix i.e. O (0,0), as shown below:



$$OB = \sqrt{\{(-5 - 0)^2 + (5 - 0)^2\}}$$

$$= \sqrt{\{(-5)^2 + (5)^2\}}$$

$$= \sqrt{\{25 + 25\}}$$

$$= \sqrt{50}$$

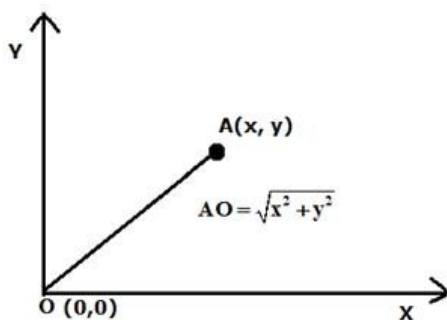
$$\therefore OB = 5\sqrt{2} \text{ units}$$

Question: 2 C

Find the distance

Solution:

Since it is given that the distance is to be found from origin so in this question we have to use the distance formula keeping one - point fix i.e. O (0,0), as shown below:



$$OC = \sqrt{(-4 - 0)^2 + (-6 - 0)^2}$$

$$= \sqrt{(-4)^2 + (-6)^2}$$

$$= \sqrt{16 + 36}$$

$$\therefore OC = \sqrt{52} \text{ units}$$

Question: 3

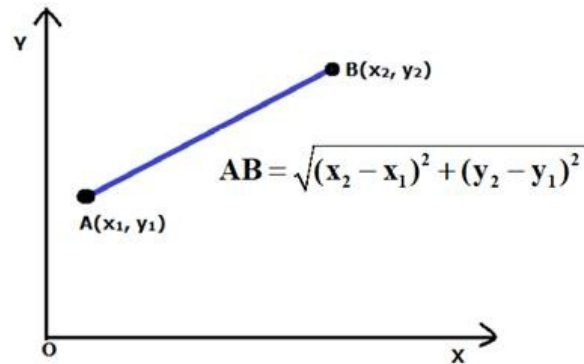
Find all possible

Solution:

Given:

Distance AB = 5 units

By distance formula, as shown below:



$$AB = \sqrt{(5 - x)^2 + (3 - (-1))^2}$$

$$5 = \sqrt{(5 - x)^2 + (4)^2}$$

$$5 = \sqrt{25 + x^2 - 10x + 16}$$

$$5 = \sqrt{41 + x^2 - 10x}$$

Squaring both sides we get

$$25 = 41 + x^2 - 10x$$

$$\Rightarrow 16 + x^2 - 10x = 0$$

$$\Rightarrow (x - 8)(x - 2) = 0$$

$$\Rightarrow x = 8 \text{ or } x = 2$$

\therefore The values of x can be 8 or 2

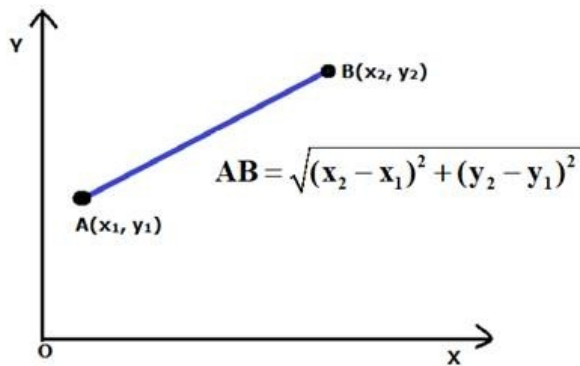
Question: 4

Find all possible

Solution:

Given, the distance AB = 10 units

By distance formula, as shown below:



$$AB = \sqrt{\{(10 - 2)^2 + (y - (-3))^2\}}$$

$$10 = \sqrt{\{(8)^2 + (y + 3)^2\}}$$

$$10 = \sqrt{\{64 + y^2 + 6y + 9\}}$$

$$10 = \sqrt{\{73 + y^2 + 6y\}}$$

Squaring both sides we get

$$100 = 73 + y^2 + 6y$$

On solving the equation, $100 = 73 + y^2 + 6y$

$$= 27 + y^2 + 6y = 0$$

$$= y^2 + 6y + 27 = 0$$

$$= (y - 3)(y + 9) = 0$$

$$= y = 3 \text{ or } y = -9$$

∴ The values of y can be 3 or -9

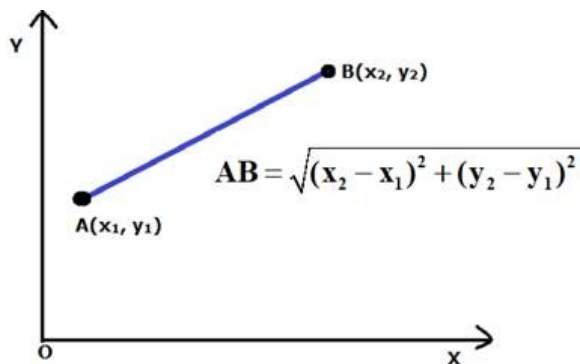
Question: 5

Find the values o

Solution:

Given the distance PQ = 10 units

By distance formula, as shown below:



$$PQ = \sqrt{\{(9 - x)^2 + (10 - 4)^2\}}$$

$$10 = \sqrt{\{(9 - x)^2 + (6)^2\}}$$

$$10 = \sqrt{\{81 + x^2 - 18x + 36\}}$$

$$10 = \sqrt{\{117 + x^2 - 18x\}}$$

Squaring both sides we get

$$= 100 = 117 + x^2 - 18x$$

$$= x^2 - 18x + 17x = 0$$

$$= (x - 1)(x - 17)$$

$$= x = 1 \text{ or } x = 17$$

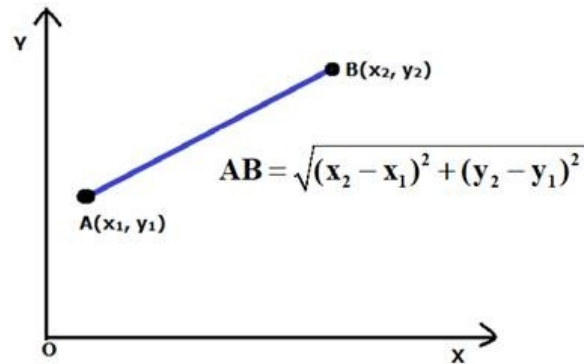
Question: 6

If the point A(x,

Solution:

Given that point A is equidistant from points B and C , so $AB = AC$

By distance formula, as shown below:



$$AB = \sqrt{(8 - x)^2 + (-2 - 2)^2}$$

$$= \sqrt{(8 - x)^2 + (-4)^2}$$

$$= \sqrt{64 + x^2 - 16x + 16}$$

$$= \sqrt{80 + x^2 - 16x}$$

$$AC = \sqrt{(2 - x)^2 + (-2 - 2)^2}$$

$$= \sqrt{(2 - x)^2 + (4)^2}$$

$$= \sqrt{4 + x^2 - 4x + 16}$$

$$= \sqrt{20 + x^2 - 4x}$$

$$\text{Now, } AB = AC$$

Squaring both sides, we get,

$$(80 + x^2 - 16x) = (20 + x^2 - 4x)$$

$$60 = 12x$$

$$x = 5$$

$$= AB = \sqrt{80 + x^2 - 16x}$$

$$= AB = \sqrt{80 + 5^2 - 16 \times 5}$$

$$= 5 \text{ units}$$

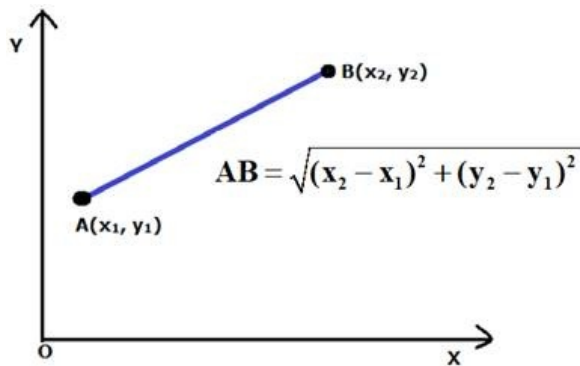
Question: 7

If the point A(0,

Solution:

Given that point A is equidistant from points B and C, so $AB = AC$

By distance formula, as shown below:



$$AB = \sqrt{\{(3 - 0)^2 + (p - 2)^2\}}$$

$$= \sqrt{\{(3)^2 + (p - 2)^2\}}$$

$$= \sqrt{\{9 + p^2 - 4p + 4\}}$$

$$= AB = \sqrt{\{13 + p^2 - 4p\}}$$

$$AC = \sqrt{\{(p - 0)^2 + (5 - 2)^2\}}$$

$$= \sqrt{\{(p)^2 + (3)^2\}}$$

$$= AB = \sqrt{\{9 + p^2\}}$$

$$\text{Now, } AB = AC$$

Squaring both sides, we get,

$$(13 + p^2 - 4p) = (9 + p^2)$$

$$= 4 = 4p$$

$$= p = 1$$

$$\text{Now, } AB = \sqrt{\{13 + p^2 - 4p\}}$$

$$= AB = \sqrt{(13 + 1 - 4)}$$

$$= \sqrt{10} \text{ units}$$

Therefore, the distance of AB = $\sqrt{10}$ units.

Question: 8

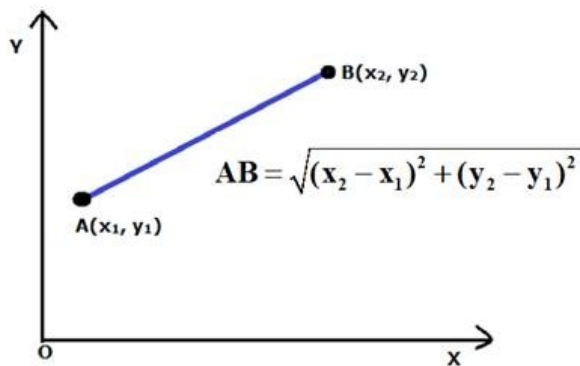
Find the point on

Solution:

Let the point be X(x,0) and the other two points are given as A(2, - 5) and B(- 2,9)

Given XA = XB

By distance formula, as shown below:



$$XA = \sqrt{\{(2 - x)^2 + (- 5 - 0)^2\}}$$

$$= \sqrt{\{(2 - x)^2 + (-5)^2\}}$$

$$= \sqrt{4 + x^2 - 4x + 25}$$

$$\Rightarrow XA = \sqrt{29 + x^2 - 4x}$$

$$XB = \sqrt{\{(-2 - x)^2 + (9 - 0)^2\}}$$

$$= \sqrt{\{(-2 - x)^2 + (9)^2\}}$$

$$= \sqrt{4 + x^2 + 4x + 81}$$

$$\Rightarrow XB = \sqrt{85 + x^2 + 4x}$$

Now since

$$XA = XB$$

Squaring both sides, we get,

$$(29 + x^2 - 4x) = (85 + x^2 + 4x)$$

$$56 = -8x$$

$$x = -7$$

The point on x axis is $(-7, 0)$

Question: 9

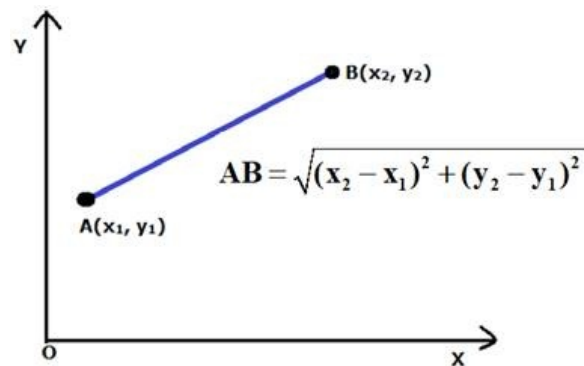
Find points on the

Solution:

Let the point be $X(x, 0)$

$$XA = 10$$

By distance formula, as shown below:



$$XA = \sqrt{\{(11 - x)^2 + (-8 - 0)^2\}}$$

$$10 = \sqrt{\{(11 - x)^2 + (-8)^2\}}$$

$$10 = \sqrt{121 + x^2 - 22x + 64}$$

$$10 = \sqrt{185 + x^2 - 22x}$$

Squaring both sides we get

$$100 = (185 + x^2 - 22x)$$

$$= 85 + x^2 - 22x = 0$$

$$= x^2 - 22x + 85 = 0$$

$$= (x - 5)(x - 17)$$

$$= x = 5 \text{ or } x = 17$$

The points are (5, 0) and (17, 0)

Question: 10

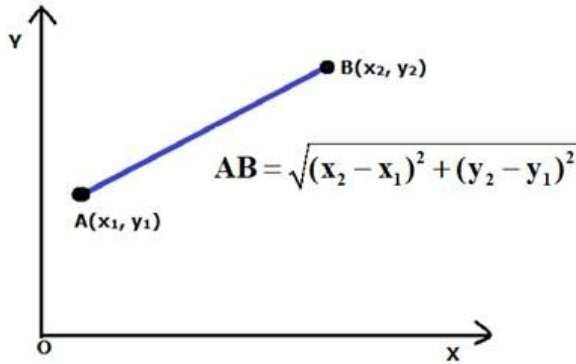
Find the point on

Solution:

Let the point be Y(0,y) and the other two points given as A(6,5) and B(- 4,3)

Given YA = YB

By distance formula, as shown below:



$$YA = \sqrt{\{(6 - 0)^2 + (5 - y)^2\}}$$

$$= \sqrt{\{(6)^2 + (5 - y)^2\}}$$

$$= \sqrt{\{36 + 25 + y^2 - 10y\}}$$

$$= YA = \sqrt{\{61 + y^2 - 10y\}}$$

$$YB = \sqrt{\{(- 4 - 0)^2 + (3 - y)^2\}}$$

$$= \sqrt{\{(- 4)^2 + (9 + y^2 - 6y)\}}$$

$$= \sqrt{\{16 + 9 + y^2 - 6y\}}$$

$$= YB = \sqrt{\{25 + y^2 - 6y\}}$$

Now, YA = YB

Squaring both sides, we get,

$$(61 + y^2 - 10y) = (25 + y^2 - 6y)$$

$$36 = 4y$$

$$= y = 9$$

The point is (0, 9)

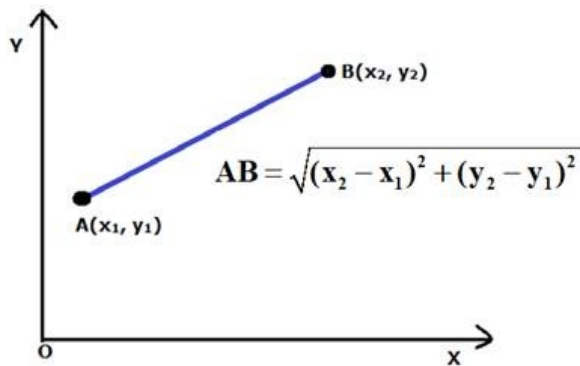
Question: 11

If the point P(x,

Solution:

The point P(x, y) is equidistant from the points A(5, 1) and B(- 1, 5), means PA = PB

By distance formula, as shown below:



$$PA = \sqrt{\{(5 - x)^2 + (1 - y)^2\}}$$

$$= \sqrt{\{(25 + x^2 - 10x) + (1 + y^2 - 2y)\}}$$

$$= PA = \sqrt{\{26 + x^2 - 10x + y^2 - 2y\}}$$

$$PB = \sqrt{\{(-1 - x)^2 + (5 - y)^2\}}$$

$$= \sqrt{\{(1 + x^2 + 2x + 25 + y^2 - 10y)\}}$$

$$= PB = \sqrt{\{(26 + x^2 + 2x + y^2 - 10y)\}}$$

Now, PA = PB

Squaring both sides, we get

$$26 + x^2 - 10x + y^2 - 2y = 26 + x^2 + 2x + y^2 - 10y$$

$$= 12x = 8y$$

$$= 3x = 2y$$

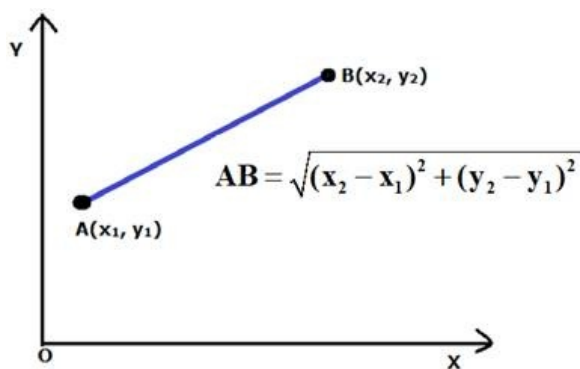
Hence proved.

Question: 12

If P(x, y) is a p

Solution:

By distance formula, as shown below:



$$PA = \sqrt{\{(6 - x)^2 + (-1 - y)^2\}}$$

$$= \sqrt{\{(36 + x^2 - 12x) + (1 + y^2 + 2y)\}}$$

$$= PA = \sqrt{\{37 + x^2 - 12x + y^2 + 2y\}}$$

$$PB = \sqrt{\{(2 - x)^2 + (3 - y)^2\}}$$

$$= \sqrt{\{(4 + x^2 - 4x + 9 + y^2 - 6y)\}}$$

$$= PB = \sqrt{\{(13 + x^2 - 4x + y^2 - 6y)\}}$$

Given: PA = PB

Squaring both sides, we get

$$(37 + x^2 - 12x + y^2 + 2y) = (13 + x^2 - 4x + y^2 - 6y)$$

$$24 = 8x - 8y$$

Dividing by 8

$$x - y = 3$$

Hence proved.

Question: 13

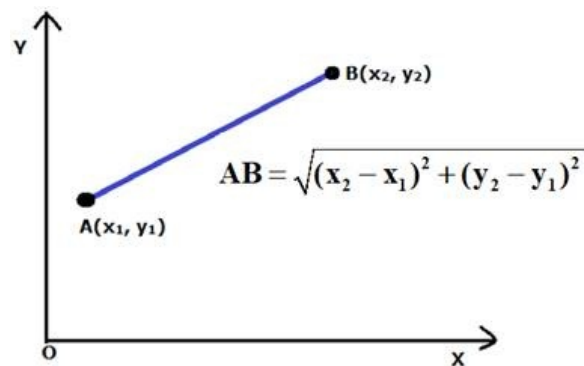
Find the coordina

Solution:

Let the point be $P(x, y)$, then since all three points are equidistant therefore

$$PA = PB = PC$$

By distance formula, as shown below:



$$\text{We have, } PA = \sqrt{\{(5 - x)^2 + (3 - y)^2\}}$$

$$= \sqrt{\{25 + x^2 - 10x + 9 + y^2 - 6y\}}$$

$$= PA = \sqrt{\{34 + x^2 - 10x + y^2 - 6y\}}$$

$$PB = \sqrt{\{(5 - x)^2 + (-5 - y)^2\}}$$

$$= \sqrt{\{25 + x^2 - 10x + 25 + y^2 + 10y\}}$$

$$= PB = \sqrt{\{50 + x^2 - 10x + y^2 + 10y\}}$$

$$PC = \sqrt{\{(1 - x)^2 + (-5 - y)^2\}}$$

$$= \sqrt{\{1 + x^2 - 2x + 25 + y^2 + 10y\}}$$

$$= PC = \sqrt{\{26 + x^2 - 2x + y^2 + 10y\}}$$

Squaring PA and PB we get

$$\{34 + x^2 - 10x + y^2 - 6y\} = \{50 + x^2 - 10x + y^2 + 10y\}$$

$$\Rightarrow -16 = 16y$$

$$\Rightarrow y = -1$$

Squaring PB and PC we get

$$\{50 + x^2 - 2x + y^2 + 10y\} = \{26 + x^2 - 10x + y^2 + 10y\}$$

$$24 = -8x$$

$$x = -3$$

$$P(-3, -1)$$

Question: 14

If the points A(4

Solution:

$$OA = \sqrt{\{(4 - 2)^2 + (3 - 3)^2\}}$$

$$= \sqrt{4}$$

$$= 2$$

$$OB = \sqrt{\{(x - 2)^2 + 4\}}$$

$$= \sqrt{\{x^2 + 4 - 4x + 4\}}$$

$$\sqrt{\{8 + x^2 - 4x\}}$$

$$OA^2 = OB^2$$

$$4 = 8 + x^2 - 4x$$

$$= x^2 - 4x + 4 = 0$$

$$= x^2 - 2x - 2x + 4 = 0$$

$$= x(x - 2) - 2(x - 2) = 0$$

$$= (x - 2)(x - 2) = 0$$

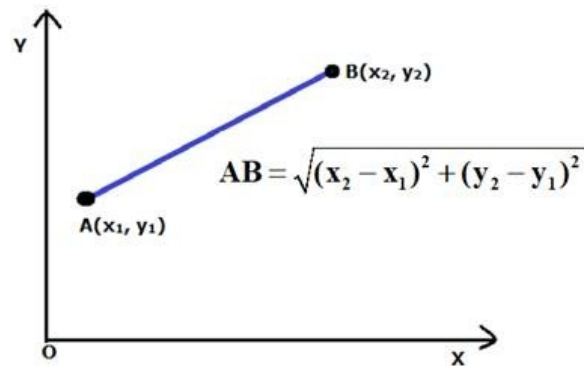
$$x = 2$$

Question: 15

If the point C(-

Solution:

By distance formula



$$AC = \sqrt{\{(3 - (-2))^2 + (-1 - 3)^2\}}$$

$$= \sqrt{\{(5)^2 + (-4)^2\}}$$

$$= \sqrt{\{25 + 16\}}$$

$$= \sqrt{\{41\}}$$

$$BC = \sqrt{\{(x - (-2))^2 + (8 - 3)^2\}}$$

$$= \sqrt{\{(x + 2)^2 + 5^2\}}$$

$$= \sqrt{\{x^2 + 4 + 2x + 25\}}$$

$$= \sqrt{\{x^2 + 2x + 29\}}$$

$$AB = BC$$

$$\sqrt{\{x^2 + 2x + 29\}} = \sqrt{\{41\}}$$

$$x = 2 \text{ or } x = -6$$

Since, $AB = BC$

$BC = \sqrt{41}$ units

Question: 16

If the point $P(2,$

Solution:

$AP = BP$

$$AP = \sqrt{\{(-2 - 2)^2 + (k - 2)^2\}}$$

$$= \sqrt{\{16 + k^2 - 4k + 4\}}$$

$$= \sqrt{(k^2 - 2k + 20)}$$

$$BP = \sqrt{\{(-2k - 2)^2 + (-3 - 2)^2\}}$$

$$= \sqrt{\{4k^2 + 8k + 4 + 25\}}$$

$$= \sqrt{(4k^2 + 8k + 29)}$$

Squaring AP and BP and equating them we get

$$k^2 - 4k + 20 = 4k^2 + 8k + 29$$

$$3k^2 + 12k + 9 = 0$$

$$(k + 3)(k + 1) = 0$$

$$\Rightarrow k = -3$$

$$\Rightarrow AP = \sqrt{41} \text{ units}$$

Or $k = -1$

$$\Rightarrow AP = 5 \text{ units}$$

Question: 17

If the point $(x,$

Solution:

Let point $P(x, y)$, $A(a + b, a - b)$, $B(a - b, a + b)$

Then $AP = BP$

$$AP = \sqrt{\{(a + b) - x\}^2 + \{(a - b) - y\}^2}$$

$$= \sqrt{\{(a + b)^2 + x^2 - 2(a + b)x + (a - b)^2 + y^2 - 2(a - b)y\}}$$

$$= \sqrt{a^2 + b^2 + 2ab + x^2 - 2(a + b)x + b^2 + a^2 - 2ab + y^2 - 2(a - b)y}$$

$$BP = \sqrt{\{(a - b) - x\}^2 + \{(a + b) - y\}^2}$$

$$= \sqrt{\{(a - b)^2 + x^2 - 2(a - b)x + (a + b)^2 + y^2 - 2(a + b)y\}}$$

$$= \sqrt{a^2 + b^2 - 2ab + x^2 - 2(a - b)x + b^2 + a^2 + 2ab + y^2 - 2(a + b)y}$$

Squaring and Equating both we get

$$a^2 + b^2 + 2ab + x^2 - 2(a + b)x + b^2 + a^2 - 2ab + y^2 - 2(a - b)y = a^2 + b^2 - 2ab + x^2 - 2(a - b)x + b^2 + a^2 + 2ab + y^2 - 2(a + b)y$$

$$-2(a + b)x - 2(a - b)y = -2(a - b)x - 2(a + b)y$$

$$ax + bx + ay - by = ax - bx + ay + by$$

Hence

$$bx = ay$$

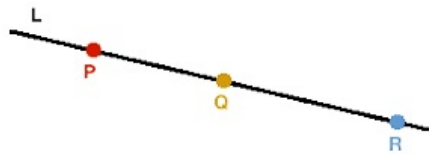
Question: 18

Using the distance

Solution:

Three or more points are collinear, if slope of any two pairs of points is same. With three points A, B and C if Slope of AB = slope of BC = slope of AC

then A, B and C are collinear points.



Collinear points P, Q, and R.

Slope of any two points is given by:

$$(y_2 - y_1)/(x_2 - x_1).$$

$$(i) \text{ Slope of AB} = (2 - (-1))/(5 - 1) = 3/4$$

$$\text{Slope of BC} = (5 - 2)/(9 - 5) = 3/4$$

$$\text{Slope of AB} = \text{slope of BC}$$

Hence collinear.

$$(ii) \text{ Slope of AB} = (1 - 9)/(0 - 6) = 8/6 = 4/3$$

$$\text{Slope of BC} = (-6 - 0)/(-7 - 1) = 6/6 = 1$$

$$\text{Slope of AC} = (-7 - 9)/(-6 - 6) = -16/-12 = 4/3$$

$$\text{Slope of AB} = \text{slope of AC}$$

Hence collinear.

$$(iii) \text{ Slope of AB} = ((3 - (-1)))/((2 - (-1)) = 4/3$$

$$\text{Slope of BC} = (11 - 2)/(8 - 3) = 9/5 = 1$$

$$\text{Slope of AC} = ((11 - (-1)))/((8 - (-1)) = 12/9 = 4/3$$

$$\text{Slope of AB} = \text{slope of AC}$$

Hence collinear.

$$(iv) \text{ Slope of AB} = (1 - 5)/((0 - (-2)) = -4/2 = -2$$

$$\text{Slope of BC} = (-3 - 1)/(2 - 0) = -4/2 = -2$$

$$\text{Slope of AB} = \text{slope of BC}$$

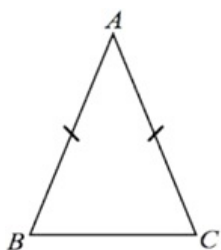
Hence collinear.

Question: 19

Show that the poi

Solution:

In an isosceles triangle any two sides are equal.



$$AB = \sqrt{\{(-2 - 7)^2 + (5 - 10)^2\}}$$

$$= \sqrt{\{(-9)^2 + (-5)^2\}}$$

$$= \sqrt{\{81 + 25\}}$$

$$= \sqrt{\{106\}}$$

$$BC = \sqrt{\{(-4 - 5)^2 + (3 - (-2))^2\}}$$

$$= \sqrt{\{(-9)^2 + (5)^2\}}$$

$$= \sqrt{\{81 + 25\}}$$

$$= \sqrt{\{106\}}$$

$$AB = BC$$

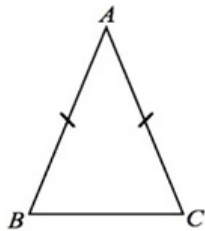
∴ It is an isosceles triangle.

Question: 20

Show that the poi

Solution:

In an isosceles triangle any two sides are equal.



$$AB = \sqrt{\{(6 - 3)^2 + (4 - 0)^2\}}$$

$$= \sqrt{\{(3)^2 + (4)^2\}}$$

$$= \sqrt{\{9 + 16\}}$$

$$= \sqrt{\{25\}} = 5 \text{ units}$$

$$BC = \sqrt{\{(-1 - 6)^2 + (3 - 4)^2\}}$$

$$= \sqrt{\{(-7)^2 + (-1)^2\}}$$

$$= \sqrt{\{49 + 1\}}$$

$$= \sqrt{\{50\}}$$

$$AC = \sqrt{\{(-1 - 3)^2 + (3 - 0)^2\}}$$

$$= \sqrt{\{(-4)^2 + (3)^2\}}$$

$$= \sqrt{\{16 + 9\}}$$

$$= \sqrt{\{25\}} = 5 \text{ units}$$

$$AB = AC$$

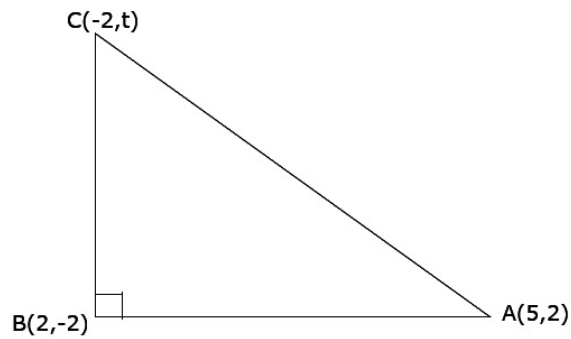
∴ It is an isosceles triangle.

Question: 21

If A(5, 2), B(2,

Solution:

Given: A(5, 2), B(2, -2) and C(-2, t) are the vertices of a right triangle with $\angle B = 90^\circ$ To



find: The value of t. **Solution:**

From the fig we

have $\angle B = 90^\circ$, so by Pythagoras theorem we have $AC^2 = AB^2 + BC^2$

$$AC^2 = (-2 - 5)^2 + (t - 2)^2$$

$$= (-7)^2 + t^2 + 4 - 2t = 49 + t^2 + 4 - 2t = 53 + t^2 - 2t$$

$$AB^2 = (2 - 5)^2 + (-2 - 2)^2 = (-3)^2 + (-4)^2$$

$$= 9 + 16$$

$$= 25$$

$$BC^2 = (-2 - 2)^2 + (t + 2)^2 = (-4)^2 + (t + 2)^2$$

$$= 16 + t^2 + 4 + 2t$$

$$= 20 + t^2 + 2t$$

$$AB^2 + BC^2 = 25 + 20 + t^2 + 2t = 45 + t^2 + 2t$$

$$AC^2 = 53 + t^2 - 2t$$

$$\Rightarrow 53 + t^2 - 2t = 45 + t^2 + 2t$$

$$\Rightarrow 53 - 45 = 4t$$

$$\Rightarrow 8 = 4t \Rightarrow t = 2$$

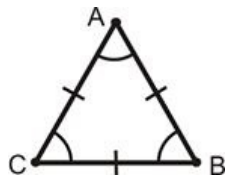
Question: 22

Prove that the po

Solution:

For an equilateral triangle

$$AB = BC = AC$$



$$AB = \sqrt{(6 - 4)^2 + (2 - 2)^2}$$

$$= \sqrt{(2)^2 + 0}$$

$$= \sqrt{4 + 0}$$

$$= \sqrt{4} = 2 \text{ units}$$

$$BC = \sqrt{(2 + \sqrt{3} - 2)^2 + (5 - 6)^2}$$

$$= \sqrt{3 + (-1)^2}$$

$$= \sqrt{4} = 2 \text{ units}$$

$$AC = \sqrt{(2 + \sqrt{3} - 2)^2 + (5 - 4)^2}$$

$$= \sqrt{\{3 + (-1)^2\}}$$

$$= \sqrt{\{4\}} = 2 \text{ units}$$

Hence , $AB = BC = AC$

\therefore ABC is an equilateral triangle.

Question: 23

Show that the poi

Solution:

Let the points be A (-3, -3), B (3, 3) and C (-3√3, 3√3)

$$\text{Then, } AB = \sqrt{(3 + 3)^2 + (-3 + 3)^2}$$

$$= \sqrt{(-6)^2 + (6)^2}$$

$$= \sqrt{36 + 36}$$

$$= \sqrt{72}$$

$$= 3\sqrt{8}$$

$$BC = \sqrt{(-3\sqrt{3} + 3)^2 + (3\sqrt{3} - 3)^2}$$

$$= \sqrt{(1 - \sqrt{3})^2 3^2 + (\sqrt{3} - 1)^2 3^2}$$

$$= 3\sqrt{[1 + 3 - 2\sqrt{3} + 3 + 1 + 2\sqrt{3}]}$$

$$= 3\sqrt{8}$$

$$CA = \sqrt{(-3\sqrt{3} - 3)^2 + (3\sqrt{3} - 3)^2}$$

$$= \sqrt{(-\sqrt{3} - 1)^2 3^2 + (\sqrt{3} - 1)^2 3^2}$$

$$= 3\sqrt{[3 + 1 + 2\sqrt{3} + 3 + 1 - 2\sqrt{3}]}$$

$$= 3\sqrt{8}$$

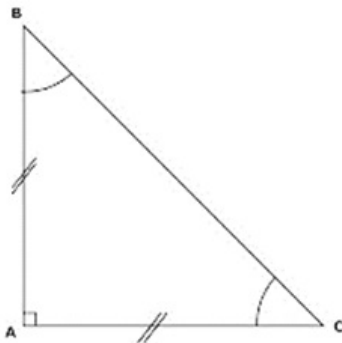
$$\therefore AB = BC = CA$$

\therefore A, B, C are the vertices of an equilateral triangle.

Question: 24

Show that the poi

Solution:



$$AB = \sqrt{\{(0 - 6)^2 + (3 - (-5))^2\}}$$

$$= \sqrt{\{(-6)^2 + (8)^2\}}$$

$$= \sqrt{\{36 + 64\}}$$

$$= \sqrt{\{100\}} = 10 \text{ units}$$

$$BC = \sqrt{\{(9 - 3)^2 + (8 - 0)^2\}}$$

$$= \sqrt{\{(6)^2 + (8)^2\}}$$

$$= \sqrt{\{36 + 64\}}$$

$$= \sqrt{\{100\}} = 10 \text{ units}$$

$$AC = \sqrt{\{(9 - (-5))^2 + (8 - 6)^2\}}$$

$$= \sqrt{\{(14)^2 + (2)^2\}}$$

$$= \sqrt{\{196 + 4\}}$$

$$= \sqrt{\{200\}}$$

For the right angled triangle

$$AC^2 = AB^2 + BC^2$$

$$AC^2 = 200$$

$$AB^2 + AC^2 = 100 + 100 = 200$$

Since $AB = BC$

\therefore ABC is an isosceles triangle.

$$\text{Area} = 1/2 (AB) (BC)$$

$$= 1/2 (10) (10)$$

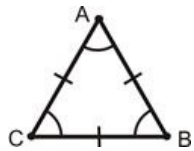
$$= 1/2 (100)$$

$$= 50 \text{ sq units}$$

Question: 25

Show that the poi

Solution:



$$OA = \sqrt{\{(\sqrt{3})^2 + (3 - 0)^2\}}$$

$$= \sqrt{\{(3) + (3)^2\}}$$

$$= \sqrt{\{3 + 9\}}$$

$$= \sqrt{\{12\}}$$

$$AB = \sqrt{\{(-\sqrt{3} - \sqrt{3})^2 + (3 - 3)^2\}}$$

$$= \sqrt{\{-2\sqrt{3}\}^2}$$

$$= \sqrt{\{12\}}$$

$$OB = \sqrt{\{(3 - 0)^2 + (-\sqrt{3} - 0)^2\}}$$

$$= \sqrt{\{9 + 3\}}$$

$$= \sqrt{\{12\}}$$

Since $OA = AB = OB$, \therefore equilateral triangle.

$$\text{Area} = 1/2 [x_1(y_2 - y_3) + x_2(y_3 - y_1) + x_3(y_1 - y_2)]$$

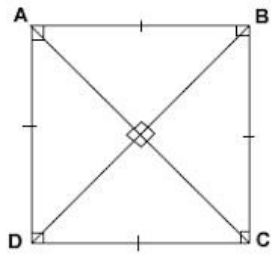
$$= 1/2[-3\sqrt{3} - 3\sqrt{3}]$$

$$= -3\sqrt{3} \text{ sq units}$$

Question: 26 A

Show that the fol

Solution:



$$AB = \sqrt{\{(0 - 3)^2 + (5 - 2)^2\}} = \sqrt{\{9 + 9\}} = \sqrt{18} \text{ units}$$

$$BC = \sqrt{\{(-3 - 0)^2 + (2 - 5)^2\}} = \sqrt{\{9 + 9\}} = \sqrt{18} \text{ units}$$

$$CD = \sqrt{\{(0 - (-3))^2 + (-1 - 2)^2\}} = \sqrt{\{9 + 9\}} = \sqrt{18} \text{ units}$$

$$DA = \sqrt{\{(0 - 3)^2 + (-1 - 2)^2\}} = \sqrt{\{9 + 9\}} = \sqrt{18} \text{ units}$$

$$AC = \sqrt{\{(-3 - 3)^2\}} = \sqrt{36} = 6 \text{ units}$$

$$BD = \sqrt{\{(-1 - 5)^2\}} = \sqrt{36} = 6 \text{ units}$$

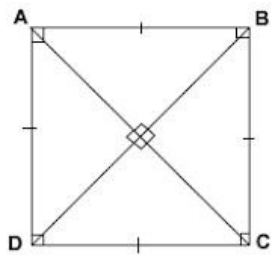
Since $AB = BC = CD = DA$ and $AC = BD$

\therefore ABCD is a square.

Question: 26 B

Show that the fol

Solution:



$$AB = \sqrt{\{(2 - 6)^2 + (1 - 2)^2\}} = \sqrt{\{16 + 1\}} = \sqrt{17} \text{ units}$$

$$BC = \sqrt{\{(1 - 2)^2 + (5 - 1)^2\}} = \sqrt{\{1 + 16\}} = \sqrt{17} \text{ units}$$

$$CD = \sqrt{\{(5 - 1)^2 + (6 - 5)^2\}} = \sqrt{\{16 + 1\}} = \sqrt{17} \text{ units}$$

$$DA = \sqrt{\{(5 - 6)^2 + (6 - 2)^2\}} = \sqrt{\{16 + 1\}} = \sqrt{17} \text{ units}$$

$$AC = \sqrt{\{(1 - 6)^2 + (5 - 2)^2\}} = \sqrt{\{25 + 9\}} = \sqrt{34} \text{ units}$$

$$BD = \sqrt{\{(5 - 2)^2 + (6 - 1)^2\}} = \sqrt{\{25 + 9\}} = \sqrt{34} \text{ units}$$

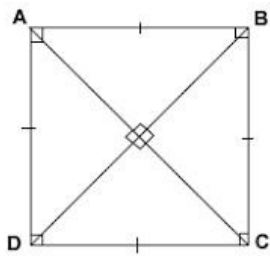
Since $AB = BC = CD = DA$ and $AC = BD$

\therefore ABCD is a square.

Question: 26 C

Show that the fol

Solution:



$$AB = \sqrt{\{(3 - 0)^2 + (1 - (-2))^2\}} = \sqrt{\{9 + 9\}} = \sqrt{18} \text{ units}$$

$$BC = \sqrt{\{(0 - 3)^2 + (4 - 1)^2\}} = \sqrt{\{9 + 9\}} = \sqrt{18} \text{ units}$$

$$CD = \sqrt{\{(-3 - 0)^2 + (1 - 4)^2\}} = \sqrt{\{9 + 9\}} = \sqrt{18} \text{ units}$$

$$DA = \sqrt{\{(-3 - 0)^2 + (1 - (-2))^2\}} = \sqrt{\{9 + 9\}} = \sqrt{18} \text{ units}$$

$$AC = \sqrt{\{(4 - (-2))^2\}} = \sqrt{\{36\}} = 6 \text{ units}$$

$$BD = \sqrt{\{(-3 - 3)^2 + (1 - 1)^2\}} = \sqrt{\{36\}} = 6 \text{ units}$$

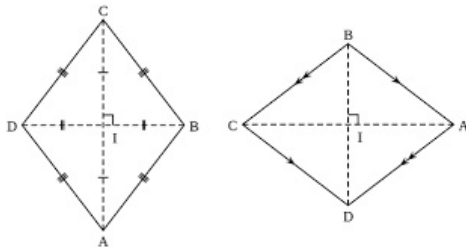
Since $AB = BC = CD = DA$ and $AC = BD$

\therefore ABCD is a square.

Question: 27

Show that the poi

Solution:



$$AC = \sqrt{\{(2 - (-3))^2 + (-32)^2\}} = \sqrt{\{25 + 25\}} = \sqrt{50} \text{ units}$$

$$BD = \sqrt{\{(4 - (-5))^2 + (4 - (-5))^2\}} = \sqrt{\{81 + 81\}} = \sqrt{162} \text{ units}$$

Area = $\frac{1}{2} \times$ (product of diagonals)

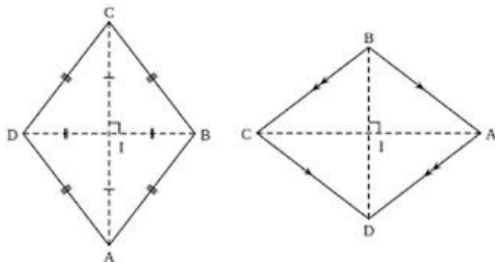
$$= \frac{1}{2} \times \sqrt{50} \times \sqrt{162}$$

$$= 45 \text{ sq units}$$

Question: 28

Show that the poi

Solution:



$$AB = \sqrt{\{(4 - 3)^2 + (5 - 0)^2\}} = \sqrt{\{1 + 25\}} = \sqrt{26} \text{ units}$$

$$BC = \sqrt{\{(-1 - 4)^2 + (4 - 5)^2\}} = \sqrt{\{25 + 1\}} = \sqrt{26} \text{ units}$$

$$CD = \sqrt{\{(-2 - (-1))^2 + (-1 - 4)^2\}} = \sqrt{\{1 + 25\}} = \sqrt{26} \text{ units}$$

$$DA = \sqrt{\{(-2 - 3)^2 + (0 - 1)^2\}} = \sqrt{\{25 + 1\}} = \sqrt{26} \text{ units}$$

$$AC = \sqrt{\{(-1 - 3)^2 + (4 - 0)^2\}} = \sqrt{\{32\}}$$

$$BD = \sqrt{\{(-2 - 4)^2 + (-1 - 5)^2\}} = \sqrt{\{36 + 36\}} = 6\sqrt{2} \text{ units}$$

Since $AB = BC = CD = DA$

Hence, ABCD is a rhombus

Area = $\frac{1}{2} \times (\text{product of diagonals})$

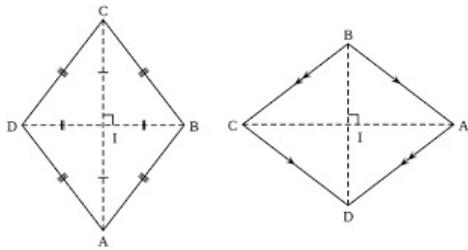
$$= \frac{1}{2} \times 4\sqrt{2} \times 6\sqrt{2}$$

$$= 24 \text{ sq units}$$

Question: 29

Show that the poi

Solution:



$$AB = \sqrt{\{(8 - 6)^2 + (2 - 1)^2\}} = \sqrt{\{4 + 1\}} = \sqrt{5} \text{ units}$$

$$BC = \sqrt{\{(9 - 8)^2 + (4 - 2)^2\}} = \sqrt{\{1 + 4\}} = \sqrt{5} \text{ units}$$

$$CD = \sqrt{\{(7 - 9)^2 + (3 - 4)^2\}} = \sqrt{\{4 + 1\}} = \sqrt{5} \text{ units}$$

$$DA = \sqrt{\{(7 - 6)^2 + (3 - 1)^2\}} = \sqrt{\{1 + 4\}} = \sqrt{5} \text{ units}$$

$$AC = \sqrt{\{(9 - 6)^2 + (4 - 1)^2\}} = \sqrt{\{9 + 9\}} = 3\sqrt{2} \text{ units}$$

$$BD = \sqrt{\{(7 - 8)^2 + (3 - 2)^2\}} = \sqrt{\{1 + 1\}} = \sqrt{2} \text{ units}$$

Since $AB = BC = CD = DA$

Hence, ABCD is a rhombus

Area = $\frac{1}{2} \times (\text{product of diagonals})$

$$= \frac{1}{2} \times 3\sqrt{2} \times \sqrt{2}$$

$$= 3 \text{ sq units}$$

Question: 30

Show that the poi

Solution:



$$AB = \sqrt{\{(5 - 2)^2 + (2 - 1)^2\}} = \sqrt{\{9 + 1\}} = \sqrt{10} \text{ units}$$

$$BC = \sqrt{\{(6 - 5)^2 + (4 - 2)^2\}} = \sqrt{\{1 + 4\}} = \sqrt{5} \text{ units}$$

$$CD = \sqrt{\{(3 - 6)^2 + (3 - 4)^2\}} = \sqrt{\{9 + 1\}} = \sqrt{10} \text{ units}$$

$$DA = \sqrt{\{(3 - 2)^2 + (3 - 1)^2\}} = \sqrt{\{1 + 4\}} = \sqrt{5} \text{ units}$$

Since $AB = CD$ and $BC = DA$

\therefore ABCD is Parallelogram

$$AC = \sqrt{\{(6 - 2)^2 + (4 - 1)^2\}} = \sqrt{\{16 + 9\}} = 5 \text{ units}$$

For a Rectangle

$$AC^2 = AB^2 + BC^2$$

$$\text{Here } AC^2 = 25$$

$$\text{But } AB^2 + BC^2 = 15$$

\therefore ABCD is not a rectangle

Question: 31

Show that A(1, 2)

Solution:



$$AB = \sqrt{\{(4 - 1)^2 + (3 - 2)^2\}} = \sqrt{\{9 + 1\}} = \sqrt{10} \text{ units}$$

$$BC = \sqrt{\{(6 - 4)^2 + (6 - 3)^2\}} = \sqrt{\{4 + 9\}} = \sqrt{13} \text{ units}$$

$$CD = \sqrt{\{(6 - 3)^2 + (5 - 6)^2\}} = \sqrt{\{9 + 1\}} = \sqrt{10} \text{ units}$$

$$DA = \sqrt{\{(3 - 1)^2 + (5 - 2)^2\}} = \sqrt{\{4 + 9\}} = \sqrt{13} \text{ units}$$

$$AB = CD \text{ and } BC = DA$$

\therefore ABCD is a parallelogram \therefore

$$AC = \sqrt{\{(6 - 1)^2 + (6 - 2)^2\}} = \sqrt{\{25 + 16\}} = \sqrt{41} \text{ units}$$

For a Rectangle

$$AC^2 = AB^2 + BC^2$$

$$\text{Here } AC^2 = 41$$

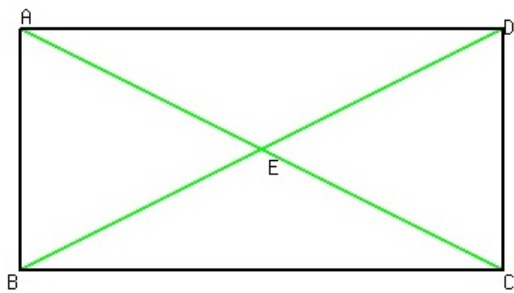
$$\text{But } AB^2 + BC^2 = 23$$

\therefore ABCD is not a rectangle

Question: 32 A

Show that the fol

Solution:



$$A(-4, -1), B(-2, -4), C(4, 0) \text{ and } D(2, 3)$$

$$AB = \sqrt{\{(-2 - (-4))^2 + (-4 - (-1))^2\}}$$

$$= \sqrt{\{4 + 9\}} = \sqrt{13} \text{ units}$$

$$BC = \sqrt{\{(4 - (-2))^2 + (0 - (-4))^2\}}$$

$$= \sqrt{\{36 + 16\}} = \sqrt{52}\text{units}$$

$$CD = \sqrt{\{(2 - 4)^2 + (3 - 0)^2\}}$$

$$= \sqrt{\{4 + 9\}} = \sqrt{13} \text{ units}$$

$$DA = \sqrt{\{(2 - (-4))^2 + (3 - (-1))^2\}}$$

$$= \sqrt{\{36 + 16\}} = \sqrt{52}\text{units}$$

$$AB = CD \text{ and } BC = DA$$

$$AC = \sqrt{\{(4 - (-4))^2 + (0 - (-1))^2\}}$$

$$= \sqrt{\{64 + 1\}} = \sqrt{65} \text{ units}$$

For a Rectangle

$$AC^2 = AB^2 + BC^2$$

$$\text{Here } AC^2 = 65$$

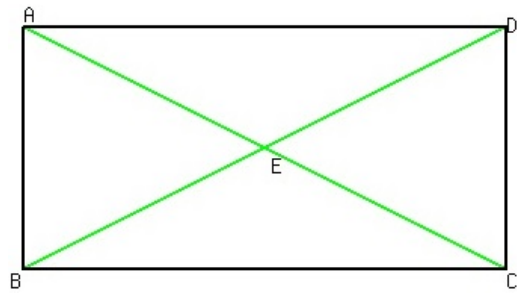
$$\text{But } AB^2 + BC^2 = 13 + 52 = 65$$

\therefore ABCD is a rectangle

Question: 32 B

Show that the fol

Solution:



$$AB = \sqrt{\{(14 - 2)^2 + (10 - (-2))^2\}}$$

$$= \sqrt{\{144 + 144\}} = \sqrt{288}$$

$$BC = \sqrt{\{(11 - 14)^2 + (10 - 13)^2\}}$$

$$= \sqrt{\{9 + 9\}} = \sqrt{18} \text{ units}$$

$$CD = \sqrt{\{(-1 - 11)^2 + (1 - 13)^2\}}$$

$$= \sqrt{\{144 + 144\}}$$

$$= \sqrt{288} \text{ units}$$

$$DA = \sqrt{\{(-1 - 2)^2 + (1 - (-2))^2\}}$$

$$= \sqrt{\{9 + 9\}} = \sqrt{18}\text{units}$$

$$AB = CD \text{ and } BC = DA$$

$$AC = \sqrt{\{(11 - 2)^2 + (13 - (-2))^2\}}$$

$$= \sqrt{\{81 + 225\}}$$

$$= \sqrt{306} \text{ units}$$

For a Rectangle

$$AC^2 = AB^2 + BC^2$$

$$\text{Here } AC^2 = 306$$

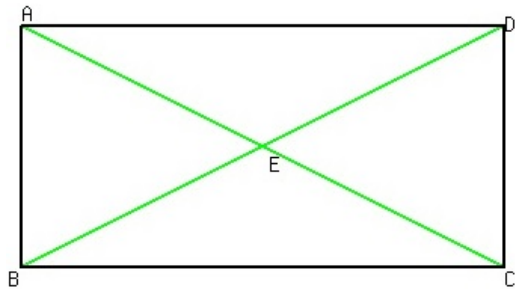
$$\text{But } AB^2 + BC^2 = 288 + 18 = 306$$

\therefore ABCD is a rectangle

Question: 32 C

Show that the fol

Solution:



$$AB = \sqrt{\{(6 - 0)^2 + (2 - (-4))^2\}}$$

$$= \sqrt{\{36 + 36\}}$$

$$= \sqrt{72} \text{units}$$

$$BC = \sqrt{\{(3 - 6)^2 + (5 - 2)^2\}}$$

$$= \sqrt{\{9 + 9\}}$$

$$= \sqrt{18} \text{units}$$

$$CD = \sqrt{\{(3 - (-3))^2 + (-1 - 5)^2\}}$$

$$= \sqrt{\{36 + 36\}}$$

$$= \sqrt{72} \text{ units}$$

$$DA = \sqrt{\{(-3 - 0)^2 + (-1 - (-4))^2\}}$$

$$= \sqrt{\{9 + 9\}}$$

$$= \sqrt{18} \text{units}$$

$$AB = CD \text{ and } BC = DA$$

$$AC = \sqrt{\{(3 - 0)^2 + (5 - (-4))^2\}}$$

$$= \sqrt{\{9 + 81\}}$$

$$= \sqrt{90} \text{ units}$$

For a Rectangle

$$AC^2 = AB^2 + BC^2$$

$$\text{Here } AC^2 = 90$$

$$\text{But } AB^2 + BC^2 = 72 + 18 = 90$$

\therefore ABCD is a rectangle

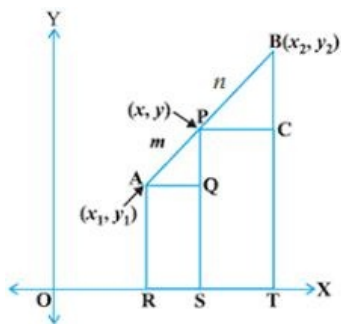
Exercise : 16B

Question: 1

Find the coordina

Solution:

Let the point P(x,y) divides AB



Then

$$X = (m_1x_2 + m_2x_1) / m_1 + m_2$$

$$= (2 \times 4 + 3 \times (-1)) / 2 + 3$$

$$= (8 - 3) / 5$$

$$= 5/5 = 1$$

$$Y = (m_1y_2 + m_2y_1) / m_1 + m_2$$

$$= (2 \times (-3) + 3 \times 7) / 5$$

$$= (-6 + 21) / 5$$

$$= 15 / 5 = 3$$

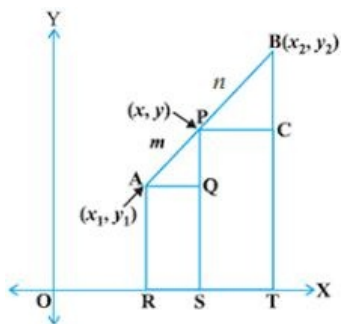
$$= (1, 3)$$

Question: 2

Find the coordina

Solution:

Let the point P(x,y) divides AB



Then

$$X = (m_1x_2 + m_2x_1) / m_1 + m_2$$

$$= (7 \times 4 + 2 \times (-5)) / 7 + 2$$

$$= (28 - 10) / 9$$

$$= 18/9 = 2$$

$$Y = (m_1y_2 + m_2y_1) / m_1 + m_2$$

$$= (7 \times (-7) + 2 \times 11) / 9$$

$$= (-49 + 22) / 9$$

$$= -27 / 9 = -3$$

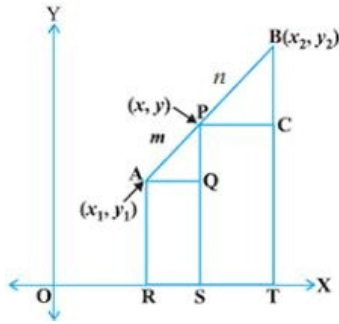
$$= (2, -3)$$

Question: 3

If the coordinate

Solution:

Let the point P(x,y) divides AB



Then

$$X = (m_1x_2 + m_2x_1) / m_1 + m_2$$

$$= (3 \times 2) + 4x(-2) / 3 + 4$$

$$= (6 - 8) / 7$$

$$= -2 / 7$$

$$Y = (m_1y_2 + m_2y_1) / m_1 + m_2$$

$$= (3 \times (-4) + 4 \times (-2)) / 7$$

$$= (-12 - 8) / 7$$

$$= -20 / 7$$

$$P\left(\frac{-2}{7}, \frac{-20}{7}\right)$$

Question: 4

Point A lies on t

Solution:

Let the point P(x,y) divides AB

Then

$$X = (m_1x_2 + m_2x_1) / m_1 + m_2$$

$$= (2 \times (-4) + 3 \times 6) / 2 + 3$$

$$= (-8 + 18) / 5$$

$$= 10 / 5 = 2$$

$$Y = (m_1y_2 + m_2y_1) / m_1 + m_2$$

$$= (2 \times (-1) + 3 \times (-6)) / 5$$

$$= (-2 - 18) / 5$$

$$= -20 / 5 = -4$$

If the point A also lies on the line $3x + k(y + 1) = 0$

Then

$$3 \times 2 + k(-4 + 1) = 0$$

$$6 - 3k = 0$$

$$6 = 3k$$

$$k = 2$$

Question: 5

Points P, Q, R an

Solution:

P divides the segment AB in ratio 1:4

Q divides the segment AB in ratio 2:3

R divides the segment AB in ratio 3:2

For coordinates of P

$$X = (m_1x_2 + m_2x_1) / m_1 + m_2$$

$$= (1 \times 6 + 4 \times 1) / 1 + 4$$

$$= (6 + 4) / 5$$

$$= 10 / 5 = 2$$

$$Y = (m_1y_2 + m_2y_1) / m_1 + m_2$$

$$= (1 \times 7 + 4 \times 2) / 5$$

$$= (7 + 8) / 5$$

$$= 15 / 5 = 3$$

$$= (2, 3)$$

For coordinates of Q

$$X = (m_1x_2 + m_2x_1) / m_1 + m_2$$

$$= (2 \times 6 + 3 \times 1) / 5$$

$$= (12 + 3) / 5$$

$$= 15 / 5 = 3$$

$$Y = (m_1y_2 + m_2y_1) / m_1 + m_2$$

$$= (2 \times 7 + 3 \times 2) / 5$$

$$= (14 + 6) / 5$$

$$= 20 / 5 = 4$$

$$= (3, 4)$$

For coordinates of R

$$X = (m_1x_2 + m_2x_1) / m_1 + m_2$$

$$= (3 \times 6 + 2 \times 1) / 5$$

$$= (18 + 2) / 5$$

$$= 20 / 5 = 4$$

$$Y = (m_1y_2 + m_2y_1) / m_1 + m_2$$

$$= (3 \times 7 + 2 \times 2) / 5$$

$$= (21 + 4) / 5$$

$$= 25 / 5 = 5$$

$$= (4, 5)$$

Hence

P(2, 3), Q(3, 4), R(4, 5)

Question: 6

Points P, Q and R

Solution:

P divides the segment AB in ratio 1:3

Q divides the segment AB in ratio 2:2

R divides the segment AB in ratio 3:1

For coordinates of P

$$X = (m_1x_2 + m_2x_1) / m_1 + m_2$$

$$= (1 \times 5 + 3 \times 1) / 1 + 3$$

$$= (5 + 3) / 4$$

$$= 8/4 = 2$$

$$Y = (m_1y_2 + m_2y_1) / m_1 + m_2$$

$$= (1 \times (-2) + 3 \times 6) / 4$$

$$= (-2 + 18) / 4$$

$$= 16 / 4 = 4$$

$$= (2, 4)$$

For coordinates of Q

$$X = (m_1x_2 + m_2x_1) / m_1 + m_2$$

$$= (2 \times 5 + 2 \times 1) / 4$$

$$= (10 + 2) / 4$$

$$= 12/4 = 3$$

$$Y = (m_1y_2 + m_2y_1) / m_1 + m_2$$

$$= (2 \times (-2) + 2 \times 6) / 4$$

$$= (-4 + 12) / 4$$

$$= 8 / 4 = 2$$

$$= (3, 2)$$

For coordinates of R

$$X = (m_1x_2 + m_2x_1) / m_1 + m_2$$

$$= (3 \times 5 + 1 \times 1) / 4$$

$$= (15 + 1) / 4$$

$$= 16/4 = 4$$

$$Y = (m_1y_2 + m_2y_1) / m_1 + m_2$$

$$= (3 \times (-2) + 1 \times 6) / 4$$

$$= (-6 + 6) / 4$$

$$= 0 / 4 = 0$$

$$= (4, 0)$$

\therefore the coordinates are P(2, 4), Q(3, 2), R(4, 0)

Question: 7

The line segment

Solution:

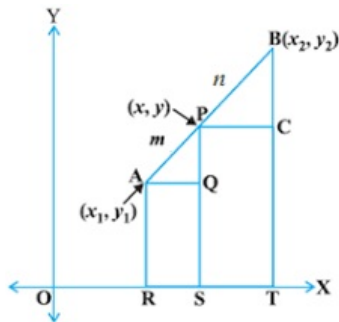
$$= 4 / 2 = 2$$

$$(-1, 2)$$

Question: 8 B

Find the coordina

Solution:



$$X = (m_1x_2 + m_2x_1) / m_1 + m_2$$

$$= (1 \times 8 + 1 \times (-11)) / 1 + 1$$

$$= (8 - 11) / 2$$

$$= -3/2$$

$$Y = (m_1y_2 + m_2y_1) / m_1 + m_2$$

$$= (1 \times (-2) + 1 \times (-8)) / 2$$

$$= (-2 - 8) / 2$$

$$= -10 / 2 = -5$$

$$\left(-\frac{3}{2}, -5 \right)$$

Question: 9

If (2, p) is the

Solution:

$$X = (m_1x_2 + m_2x_1) / m_1 + m_2$$

$$= (1 \times (-2) + 1 \times 6) / 1 + 1$$

$$= (-2 + 6) / 2$$

$$= 4/2 = 2$$

$$Y = (m_1y_2 + m_2y_1) / m_1 + m_2$$

$$= (1 \times 11 + 1 \times (-5)) / 2$$

$$= (11 - 5) / 2$$

$$= 6 / 2 = 3$$

$$p = 3$$

Question: 10

The midpoint of t

Solution:

$$X = (m_1x_2 + m_2x_1) / m_1 + m_2$$

$$= (1 \times (-2) + 1 \times 2a) / 1 + 1$$

$$= (-2 + 2a) / 2$$

$$(-2 + 2a) / 2 = 1$$

$$-2 + 2a = 2$$

$$2a = 4$$

$$a = 2$$

$$Y = (m_1 y_2 + m_2 y_1) / m_1 + m_2$$

$$= (1 \times 3b + 1 \times 4) / 2$$

$$= (3b + 4) / 2$$

$$(3b + 4) / 2 = 2a + 1$$

$$(3b + 4) / 2 = 5$$

$$(3b + 4) = 10$$

$$3b = 6$$

$$b = 2$$

$$a = 2, b = 2$$

Question: 11

The line segment

Solution:

$$X = (m_1 x_2 + m_2 x_1) / m_1 + m_2$$

$$= (1 \times 6 + 1 \times (-2)) / 1 + 1$$

$$= (6 - 2) / 2$$

$$= 4 / 2 = 2$$

$$Y = (m_1 y_2 + m_2 y_1) / m_1 + m_2$$

$$= (1 \times 3 + 1 \times 9) / 2$$

$$= (3 + 9) / 2$$

$$= 12 / 2 = 6$$

$$C(2, 6)$$

Question: 12

Find the coordinates

Solution:

Let the coordinates of A be x & y . So A(X, Y) and B(1, 4)

$$2 = (m_1 x_2 + m_2 x_1) / m_1 + m_2$$

$$2 = (1 \times 1 + 1 \times X) / 1 + 1$$

$$2 = (1 + X) / 2$$

$$1 + X = 4$$

$$x = 3$$

$$-3 = (m_1 y_2 + m_2 y_1) / m_1 + m_2$$

$$-3 = (1 \times 4 + 1 \times Y) / 2$$

$$-3 = (4 + Y) / 2$$

$$(4 + Y) = -6$$

$$Y = -10$$

$$A(3, -10)$$

Question: 13

In what ratio does

Solution:

$$2 = (m_1x_2 + m_2x_1) / m_1 + m_2$$

$$2 = (m_1 \times (-6) + m_2 \cdot 8) / m_1 + m_2$$

$$2 = (-6m_1 + 8m_2) / m_1 + m_2$$

$$-6m_1 + 8m_2 = 2(m_1 + m_2)$$

$$-8m_1 + 6m_2 = 0$$

$$5 = (m_1y_2 + m_2y_1) / m_1 + m_2$$

$$5 = (m_1 \times 9 + m_2 \cdot 2) / m_1 + m_2$$

$$5 = (9m_1 + 2m_2) / m_1 + m_2$$

$$9m_1 + 2m_2 = 5(m_1 + m_2)$$

$$4m_1 + 3m_2 = 0$$

Solving for m_1 and m_2 we get

$$m_1 = 3$$

$$m_2 = 4$$

$$3:4$$

Question: 14

Find the ratio in

Solution:

$$3/4 = (m_1x_2 + m_2x_1) / m_1 + m_2$$

$$3/4 = (m_1 \times 2 + m_2 (1/2)) / m_1 + m_2$$

$$3/4 = (2m_1 + m_2 / 2) / m_1 + m_2$$

$$6m_1 + 6m_2 = 16m_1 + 4m_2$$

$$6m_1 - 2m_2 = 0$$

$$5/12 = (m_1y_2 + m_2y_1) / m_1 + m_2$$

$$5/12 = (m_1 \times (-5) + m_2 (3/2)) / m_1 + m_2$$

$$5/12 = (-5m_1 + 3m_2 / 2) / m_1 + m_2$$

$$-120m_1 + 36m_2 = 10(m_1 + m_2)$$

$$130m_1 - 26m_2 = 0$$

Solving for m_1 and m_2 we get

$$m_1 = 1$$

$$m_2 = 5$$

$$1:5$$

Question: 15

Find the ratio in

Solution:

$$6 = (m_1y_2 + m_2y_1) / m_1 + m_2$$

$$6 = (m_1 \times 8 + m_2 \cdot 3) / m_1 + m_2$$

$$6 = (8m_1 + 3m_2) / m_1 + m_2$$

$$8m_1 + 8m_2 = 6(m_1 + m_2)$$

$$2m_1 - 3m_2 = 0$$

$$m_1:m_2 = 3:2$$

Now,

$$m = (m_1x_2 + m_2x_1) / m_1 + m_2$$

$$m = (m_1 \times 2 + m_2 (-4)) / m_1 + m_2$$

$$m = (2m_1 - 4m_2) / m_1 + m_2$$

$$2m_1 - 4m_2 = m(m_1 + m_2)$$

Putting the values of m_1 & m_2

$$m = -2/5$$

Hence, 3:2, $m = -2/5$

Question: 16

Find the ratio in

Solution:

$$-3 = (m_1x_2 + m_2x_1) / m_1 + m_2$$

$$-3 = (m_1 \times (-2) + m_2 (-5)) / m_1 + m_2$$

$$-3 = (-2m_1 - 5m_2) / m_1 + m_2$$

$$-2m_1 - 5m_2 = -3(m_1 + m_2)$$

$$2m_1 + 5m_2 = 3(m_1 + m_2)$$

$$m_1 - 2m_2 = 0$$

$$m_1:m_2 = 1:2$$

Now,

$$K = (m_1y_2 + m_2y_1) / m_1 + m_2$$

$$K = (m_1 \times 3 + m_2(-4)) / m_1 + m_2$$

$$K = (3m_1 - 4m_2) / m_1 + m_2$$

$$3m_1 - 4m_2 = k(m_1 + m_2)$$

Putting the values of m_1 & m_2

$$k = 2/3$$

Hence, 2:1, $k = 2/3$

Question: 17

In what ratio is

Solution:

The segment is divided by x - axis i.e the coordinates are (x,0)

$$x = (m_1x_2 + m_2x_1) / m_1 + m_2$$

$$x = (m_1 \times 5 + m_2 \cdot 2) / m_1 + m_2$$

$$x = (5m_1 + 2m_2) / m_1 + m_2$$

$$5m_1 + 2m_2 = x(m_1 + m_2)$$

$$(5 - x)m_1 + (2 - x)m_2 = 0$$

$$0 = (m_1y_2 + m_2y_1) / m_1 + m_2$$

$$0 = (m_1 \times 6 + m_2(-3)) / m_1 + m_2$$

$$0 = (6m_1 - 3m_2) / m_1 + m_2$$

$$6m_1 - 3m_2 = 0$$

Solving for m_1 and m_2 we get

$$m_1 = 1$$

$$m_2 = 2$$

$$(1 : 2),$$

Putting the values of m_1 and m_2

$$x = 3$$

Hence coordinates are (3,0)

Question: 18

In what ratio is

Solution:

The segment is divided by y - axis i.e the coordinates are (0,y)

$$0 = (m_1x_2 + m_2x_1) / m_1 + m_2$$

$$0 = (m_1 \times 3 + m_2(-2)) / m_1 + m_2$$

$$0 = (3m_1 - 2m_2) / m_1 + m_2$$

$$3m_1 - 2m_2 = 0$$

$$m_1 = 2$$

$$m_2 = 3$$

$$(2:3)$$

$$y = (m_1y_2 + m_2y_1) / m_1 + m_2$$

$$y = (m_1 \times 7 + m_2(-3)) / m_1 + m_2$$

$$y = (7m_1 - 3m_2) / m_1 + m_2$$

$$7m_1 - 3m_2 = y(m_1 + m_2)$$

Putting the values of m_1 and m_2

$$y = 1$$

Question: 19

In what ratio doe

Solution:

The line segment joining any two points (x_1, y_1) and (x_2, y_2) is given as:

$$(y - y_1) = \frac{(y_2 - y_1)}{(x_2 - x_1)}(x - x_1)$$

$$= y - (-1) = \left(\frac{9 - (-1)}{8 - 3}\right)(x - 3)$$

$$= y + 1 = 10/5 (x - 3)$$

$$= y + 1 = 2(x - 3)$$

$$= y + 1 = 2x - 6 \Rightarrow 2x - y = 7 \text{..eq(1) is the equation of line segment.}$$

Now, we have to find the point of intersection of eq (1) & the given line: $x - y - 2 = 0$

$$2x - y = 7$$

$$\& x - y - 2 = 0$$

$$2x - 7 = x - 2$$

$$\Rightarrow x = 7 - 2$$

$$\Rightarrow x = 5$$

$$\text{And, } y = 3$$

Let us say this point divides the line segment in the ratio of $k_1:k_2$

Then,

$$5 = \frac{(8k_1 + 3k_2)}{k_1 + k_2}$$

$$= 5k_1 + 5k_2 = 8k_1 + 3k_2$$

$$= 5k_1 - 8k_1 + 5k_2 - 3k_2 = 0$$

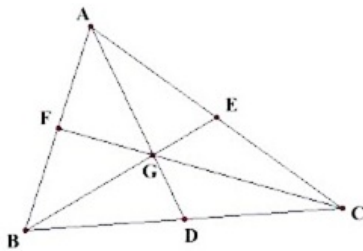
$$= -3k_1 + 2k_2 = 0$$

$$\Rightarrow \frac{k_1}{k_2} = \frac{2}{3}$$

Question: 20

Find the lengths

Solution:



For coordinates of median AD segment BC will be taken

$$X = (m_1x_2 + m_2x_1)/m_1 + m_2$$

$$= (1 \times 0 + 1 \times 2)/1 + 1$$

$$= (0 + 2)/2$$

$$= 2/2 = 1$$

$$Y = (m_1y_2 + m_2y_1)/m_1 + m_2$$

$$= (1 \times 3 + 1 \times 1)/2$$

$$= (3 + 1)/2$$

$$= 4 / 2 = 2$$

$$D(1,2)$$

By distance Formula

$$AD = \sqrt{(1 - 0)^2 + (2 + 1)^2}$$

$$= \sqrt{1 + 9}$$

$$= \sqrt{10}$$

For coordinates of BE, segment AC will be taken

$$X = (m_1x_2 + m_2x_1) / m_1 + m_2$$

$$= (1 \times 0 + 1 \times 0) / 1 + 1$$

$$= (0 + 0) / 2$$

$$= 0 / 2 = 0$$

$$Y = (m_1y_2 + m_2y_1) / m_1 + m_2$$

$$= (1 \times 3 + 1 \times (-1)) / 2$$

$$= (3 - 1) / 2$$

$$= 2 / 2 = 1$$

$$\therefore E(0,1)$$

By distance Formula

$$BE = \sqrt{(0 - 2)^2 + (1 - 1)^2}$$

$$= \sqrt{4 + 0}$$

$$= \sqrt{4} = 2$$

For coordinates of median CF segment AB will be taken

$$X = (m_1x_2 + m_2x_1) / m_1 + m_2$$

$$= (1 \times 2 + 1 \times 0) / 1 + 1$$

$$= (2 + 0) / 2$$

$$= 2 / 2 = 1$$

$$Y = (m_1y_2 + m_2y_1) / m_1 + m_2$$

$$= (1 \times (-1) + 1 \times 1) / 2$$

$$= (-1 + 1) / 2$$

$$= 0 / 2 = 0$$

$$F(1,0)$$

By distance Formula

$$CF = \sqrt{(1 - 0)^2 + (0 - 3)^2}$$

$$= \sqrt{1 + 9}$$

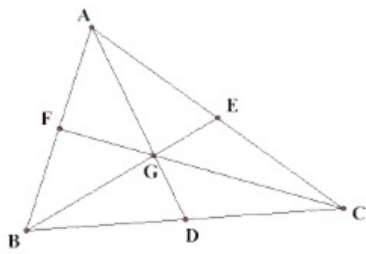
$$= \sqrt{10}$$

$$AD = \sqrt{10} \text{ units, } BE = 2 \text{ units, } CF = \sqrt{10} \text{ units}$$

Question: 21

Find the centroid

Solution:



First we need to calculate the coordinates of median

For coordinates of median AD segment BC will be taken

$$X = (m_1x_2 + m_2x_1) / m_1 + m_2$$

$$= (1 \times 8 + 1 \times 5) / 1 + 1$$

$$= (8 + 5) / 2$$

$$= 13/2$$

$$Y = (m_1y_2 + m_2y_1) / m_1 + m_2$$

$$= (1 \times 2 + 1 \times (-2)) / 2$$

$$= (0) / 2$$

$$= 0 / 2 = 0$$

$$D(13/2, 0)$$

The centroid of the triangle divides the median in the ratio 2:1

By section formula,

$$X = (m_1x_2 + m_2x_1) / m_1 + m_2$$

$$= (2 \times 13/2 + 1 \times (-1)) / 2 + 1$$

$$= (13 - 1) / 3$$

$$= 12/3 = 4$$

$$Y = (m_1y_2 + m_2y_1) / m_1 + m_2$$

$$= (2 \times 0 + 1 \times 0) / 2 + 1$$

$$= 0/3$$

$$= 0$$

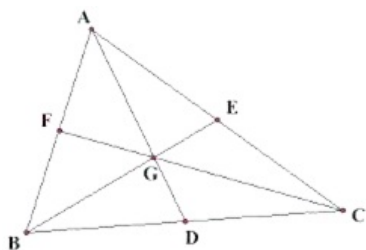
\therefore G coordinate is (4, 0)

Question: 22

If G(-2, 1) is t

Solution:

The figure is shown as:



$$-2 = (m_1x_2 + m_2x_1) / m_1 + m_2$$

$$-2 = (2 \times x + 1 \times 1) / 2 + 1$$

$$-2 = (2x + 1) / 3$$

$$-6 = 2x + 1$$

$$-7 = 2x$$

$$\Rightarrow x = -7/2$$

$$1 = (m_1 y_2 + m_2 y_1) / m_1 + m_2$$

$$1 = (2x y + 1x (-6)) / 3$$

$$1 = (2y - 6) / 2$$

$$2 = 2y - 6$$

$$8 = 2y$$

$$\Rightarrow y = 4$$

$$D(-7/2, 4)$$

Now for BC

$$-7/2 = (m_1 x_2 + m_2 x_1) / m_1 + m_2$$

$$-7/2 = (1 \times x + 1x (-5)) / 1 + 1$$

$$-7/2 = (x - 5) / 2$$

$$-7 = x - 5$$

$$-7 + 5 = x$$

$$\Rightarrow x = -2$$

$$4 = (m_1 y_2 + m_2 y_1) / m_1 + m_2$$

$$4 = (1 \times y + 1x 2) / 2$$

$$4 = (y + 2) / 2$$

$$8 = y + 2$$

$$\Rightarrow y = 6$$

$$\text{Hence, } C(-2, 6)$$

Question: 23

Find the third vertex

Solution:

Coordinate of D on median on BC

$$x = (m_1 x_2 + m_2 x_1) / m_1 + m_2$$

$$x = (1 \times 0 + 1x (-3)) / 1 + 1$$

$$x = (0 - 3) / 2$$

$$x = -3/2$$

$$y = (m_1 y_2 + m_2 y_1) / m_1 + m_2$$

$$y = (1 \times (-2) + 1x 1) / 2$$

$$y = (-2 + 1) / 2$$

$$2y = -1$$

$$y = -1/2$$

$$D(-3/2, -1/2)$$

Now for AD we have D(-3/2, -1/2) and Centroid C(0,0)

$$0 = (m_1x_2 + m_2x_1) / m_1 + m_2$$

$$0 = (2 \times (-3/2) + 1 \times x) / 2 + 1$$

$$0 = (-3 + x) / 3$$

$$-3 + x = 0$$

$$x = 3$$

$$0 = (m_1y_2 + m_2y_1) / m_1 + m_2$$

$$0 = (2 \times (-1/2) + 1 \times y) / 2 + 1$$

$$0 = (-1 + y) / 3$$

$$-1 + y = 0$$

$$y = 1$$

Hence, A(3, 1)

Question: 24

Show that the poi

Solution:

We know that if diagonals of a quadrilateral bisect each other, then the quadrilateral is parallelogram

Given, A(3, 1), B(0, -2), C(1, 1) and D(4, 4) are coordinates of a quadrilateral

So, If ABCD is a parallelogram, the coordinates of the mid-point of the AC = Coordinates of the mid-point of the BD

We know, midpoint formula that if P is mid point of A(x₁, y₁) and B(x₂, y₂) $P = \left(\frac{x_1 + x_2}{2}, \frac{y_1 + y_2}{2} \right)$

Coordinates of mid-point of AC

$$= \left(\frac{3+1}{2}, \frac{1+1}{2} \right) = (2, 1)$$

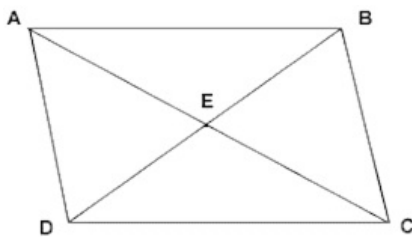
$$\text{Coordinates of mid-point of BD} = \left(\frac{0+4}{2}, \frac{-2+4}{2} \right) = (2, 1)$$

Hence, ABCD is a parallelogram.

Question: 25

If the points P(a

Solution:



We know that the diagonals of a parallelogram bisect each other

So the coordinates of the mid - point of the PR = Coordinates of the mid - point of the QS

$$\{(2 + a)/2, (15 - 11)/2\} = \{(5 + 1)/2, (b + 1)/2\}$$

$$2 + a = 6$$

$$a = 4$$

$$15 - 11 = b + 1$$

$$4 = b + 1$$

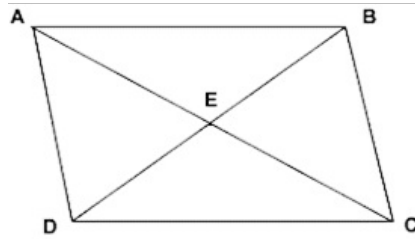
$$b = 3$$

Hence, $a = 4$, $b = 3$

Question: 26

If three consecut

Solution:



Coordinate of mid - point of AC = $\{(1 + 5)/2, (-2 + 10)/2\}$

implies (3,4)

This is equal to the coordinates of mid - point of BD

$$3 = (3 + x)/2$$

$$6 = 3 + x$$

$$x = 3$$

$$4 = (6 + y)/2$$

$$8 = (6 + y)$$

$$y = 2$$

Hence, D(3, 2)

Question: 27

In what ratio doe

Solution:

Let the coordinate of the point on y axis be (0,y)

$$0 = (m_1x_2 + m_2x_1)/ m_1 + m_2$$

$$0 = (m_13 + m_2(-4))/ m_1 + m_2$$

$$0 = (3m_1 - 4m_2)/ m_1 + m_2$$

$$(3m_1 - 4m_2) = 0$$

$$3m_1 = 4m_2$$

$$m_1: m_2 = 4:3$$

Question: 28

If the point

Solution:

Given: The points P(1/2, y) lies on the line AB.

Then,

$$1/2 = (m_1x_2 + m_2x_1)/ m_1 + m_2$$

$$1/2 = (m_1(-7) + m_2 3) / m_1 + m_2$$

$$1/2 = (-7m_1 + 3m_2) / m_1 + m_2$$

$$(m_1 + m_2) = -14m_1 + 6m_2$$

$$15m_1 = 5m_2$$

$$m_1 : m_2 = 3:5$$

$$y = (m_1 y_2 + m_2 y_1) / m_1 + m_2$$

$$y = (3 \times 9 + 5 \times (-5)) / 3 + 5$$

$$y = (27 - 25) / 8$$

$$y = 2/8$$

$$y = 1/4$$

Question: 29

Find the ratio in

Solution:

Let the coordinate of the point on x axis be (x,0)

$$0 = (m_1 y_2 + m_2 y_1) / m_1 + m_2$$

$$0 = (m_1 7 + m_2(-3)) / m_1 + m_2$$

$$0 = (7m_1 - 3m_2) / m_1 + m_2$$

$$7m_1 - 3m_2 = 0$$

$$7m_1 = 3m_2$$

$$m_1 : m_2 = 3:7$$

$$x = (m_1 x_2 + m_2 x_1) / m_1 + m_2$$

$$x = (3 \times (-2) + 7 \times 3) / 10$$

$$x = (-6 + 21) / 10$$

$$x = 15/10$$

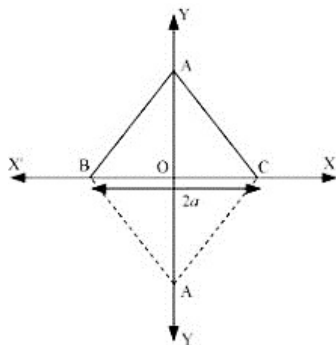
$$x = 3/2$$

Hence the coordinate of the point be (3/2, 0)

Question: 30

The base QR of an

Solution:



Let QR be the base

Since origin is mid - point O(0,0) of QR

Then the coordinates of R(x,y) is given by

$$(-4 + x)/2 = 0$$

$$x = 4$$

$$(0 + y)/2 = 0$$

$$y = 0$$

$$R(4,0)$$

$$\text{Distance of QR} = \sqrt{(4 + 4)^2 + 0}$$

$$QR = 8$$

$$\therefore PR = 8$$

Let P(x,y)

$$8 = \sqrt{(4 - x)^2 + (0 - y)^2}$$

$$64 = 16 + x^2 - 8x + y^2$$

Since it will lie on x axis

$$\therefore y = 0$$

$$64 = 16 + y^2$$

$$48 = y^2$$

$$y = 4\sqrt{3} \text{ or } -4\sqrt{3}$$

Hence,

$$P(0, 4\sqrt{3}) \text{ or } P(0, -4\sqrt{3}) \text{ and } R(4, 0)$$

Question: 31

The base BC of an

Solution:

Given: The base (BC) of the equilateral triangle ABC lies on y - axis, where, C has the coordinates: (0, -3). The origin is the midpoint of the base.

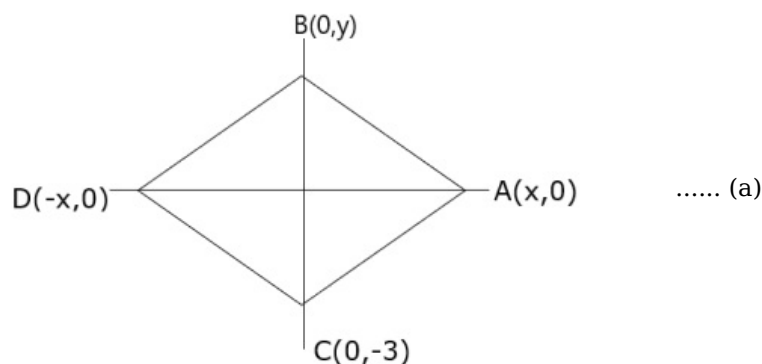
To find: The coordinates of the points A and B. Also, the coordinates of another point D such that ABCD is a rhombus. **Solution:**

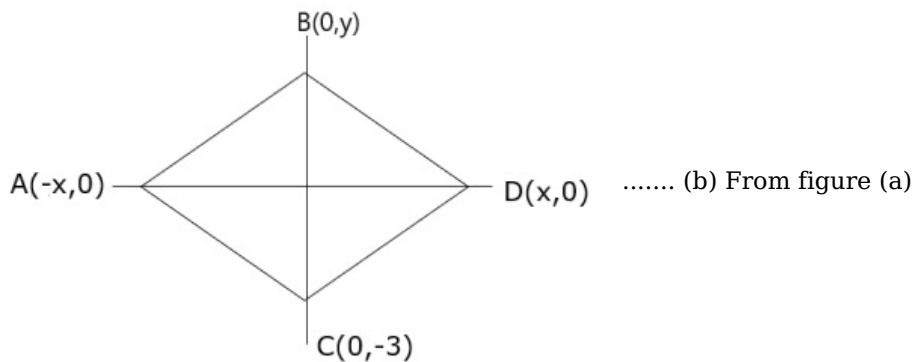
Now, ΔABC is an equilateral triangle

$\therefore AB = AC = BC$... (1) By symmetry the coordinate A lies on x axis. Also D is another point such that ABCD is rhombus and every side of rhombus is equal to each other. So For this condition to be possible D will also lie on x axis. Now, Let coordinates of A be (x,0), B be (0,y) and D be (-x,0).

or coordinates of A be (-x,0), B be (0,y) and D be (x,0).

The figures are shown below:





$$BC = \sqrt{(0 - 0)^2 + (-3 - y)^2} \Rightarrow BC = \sqrt{0 + 9 + y^2 + 6y} \Rightarrow BC = \sqrt{9 + y^2 + 6y}$$

$$\text{Now, } AC = \sqrt{(0 - x)^2 + (-3 - 0)^2}$$

$$\Rightarrow AC = \sqrt{x^2 + (-3)^2} \Rightarrow AC = \sqrt{x^2 + 9}$$

And

$$AB = \sqrt{(0 - x)^2 + (y - 0)^2}$$

$\Rightarrow AB = \sqrt{x^2 + y^2}$ From (1) $AB = AC \Rightarrow \sqrt{x^2 + y^2} = \sqrt{x^2 + 9}$ Taking square on both sides we get, $x^2 + y^2 = x^2 + 9 \Rightarrow y^2 = 9 \Rightarrow y = \pm 3$ Since B lies in positive y direction. \therefore The coordinates of B are (0,3) Now from (1) $AB = BC \Rightarrow \sqrt{x^2 + y^2} = \sqrt{9 + y^2 + 6y}$ Take square on both sides $\Rightarrow x^2 + y^2 = 9 + y^2 + 6y \Rightarrow x^2 = 9 + 6y$ Put the value of y to get, $\Rightarrow x^2 = 9 + 6(3) \Rightarrow x^2 = 9 + 18 \Rightarrow x^2 = 27 \Rightarrow x = \pm 3\sqrt{3}$ Hence the coordinates of A can be $(3\sqrt{3}, 0)$ or $(-3\sqrt{3}, 0)$ Also, ABCD is a rhombus. $\Rightarrow AB = BC = DC = BD$ So coordinates of D will be $(-3\sqrt{3}, 0)$ or $(3\sqrt{3}, 0)$ Hence coordinates are A $(3\sqrt{3}, 0)$, B(0,3), D $(-3\sqrt{3}, 0)$ Or coordinates are A $(-3\sqrt{3}, 0)$, B(0,3), D $(3\sqrt{3}, 0)$

Question: 32

Find the ratio in

Solution:

$$-1 = (m_1x_2 + m_2x_1) / m_1 + m_2$$

$$-1 = (m_16 + m_2(-3)) / m_1 + m_2$$

$$-1 = (6m_1 - 3m_2) / m_1 + m_2$$

$$(6m_1 - 3m_2) = -m_1 - m_2$$

$$7m_1 = 2m_2$$

$$m_1 : m_2 = 2 : 7$$

$$y = (m_1y_2 + m_2y_1) / m_1 + m_2$$

$$= (2x(-8) + 7 \times 10) / 9$$

$$= (-16 + 70) / 9$$

$$= 54 / 9$$

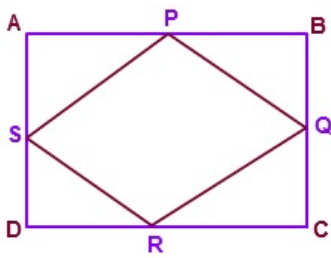
$$y = 6$$

Question: 33

ABCD is a rectang

Solution:

The figure is shown below:



$$P(x,y) = (-1 - 1)/2, (4 - 1)/2$$

$$= (-1, 3/2)$$

$$Q(x,y) = (5 - 1)/2, (4 + 4)/2$$

$$= (2, 4)$$

$$R(x,y) = (5 + 5)/2, (-1 + 4)/2$$

$$= (5, 3/2)$$

$$S(x,y) = (5 - 1)/2, (-1 - 1)/2$$

$$= (2, -1)$$

Coordinates of mid - point of PR = Coordinates of mid - point of QS

$$\text{Coordinates of mid - point of PR} = \{(5 - 1)/2, (3/2 + 3/2)/2\} = (2, 3/2)$$

$$\text{Coordinates of mid - point of QS} = \{(2 + 2)/2, (-1 + 4)/2\} = (2, 3/2)$$

Hence PQRS is a Rhombus.

Question: 34

The midpoint P of

Solution:

For P(x,y)

$$X = (-10 - 2)/2 = -6$$

$$Y = (4 + 0)/2 = 2$$

Thus, P(-6,2)

Now

$$-6 = (m_1x_2 + m_2x_1)/m_1 + m_2$$

$$-6 = (m_1(-4) + m_2(-9))/m_1 + m_2$$

$$-6 = (-4m_1 - 9m_2)/m_1 + m_2$$

$$-6(m_1 + m_2) = -4m_1 - 9m_2$$

$$-2m_1 = -3m_2$$

$$m_1:m_2 = 3:2,$$

$$2 = (m_1y_2 + m_2y_1)/m_1 + m_2$$

$$2 = (3 \times y + 2 \times (-4))/5$$

$$2 = (3y - 8)/5$$

$$10 = 3y - 8$$

$$3y = 18$$

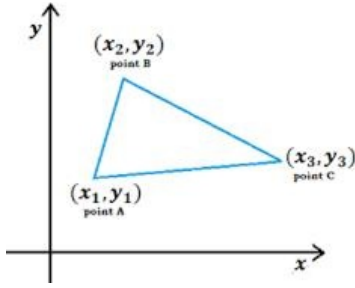
$$y = 6$$

Exercise : 16C

Question: 1 A

Find the area of

Solution:



Area of triangle

$$= 1/2(x_1(y_2 - y_3) + x_2(y_3 - y_1) + x_3(y_1 - y_2))$$

$$= 1/2(1(-2 + 3) - 2(-4 - 2) - 3(2 - 3))$$

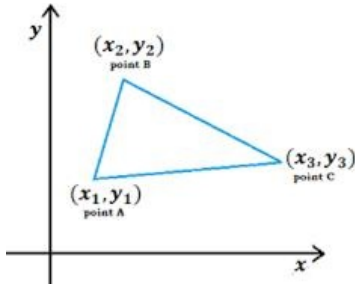
$$= 1/2(1 + 12 + 3)$$

$$= 8 \text{ sq units}$$

Question: 1 B

Find the area of

Solution:



Area of triangle

$$= 1/2(x_1(y_2 - y_3) + x_2(y_3 - y_1) + x_3(y_1 - y_2))$$

$$= 1/2(-5(-5 - 5) - 4(5 - 7) + 4(7 + 5))$$

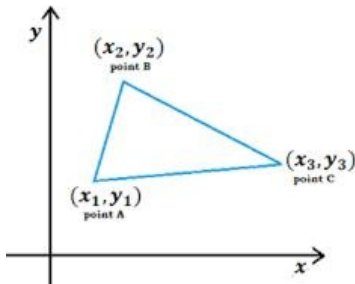
$$= 1/2(-50 + 8 + 48)$$

$$= 5 \text{ sq units}$$

Question: 1 C

Find the area of

Solution:



Area of triangle

$$= 1/2(x_1(y_2 - y_3) + x_2(y_3 - y_1) + x_3(y_1 - y_2))$$

$$= 1/2(3(2 + 1) - 4(-1 - 8) + 5(8 - 2))$$

$$= 1/2(9 + 36 + 30)$$

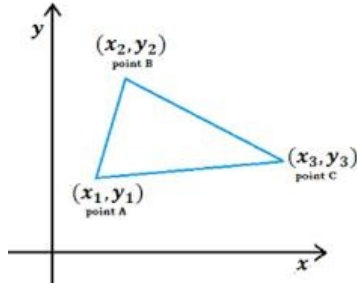
$$= 1/2(75)$$

$$= 37.5 \text{ sq units}$$

Question: 1 D

Find the area of

Solution:



Area of triangle

$$= 1/2(x_1(y_2 - y_3) + x_2(y_3 - y_1) + x_3(y_1 - y_2))$$

$$= 1/2(10(5 - 3) + 2(3 + 6) - 1(-6 - 5))$$

$$= 1/2(20 + 18 + 11)$$

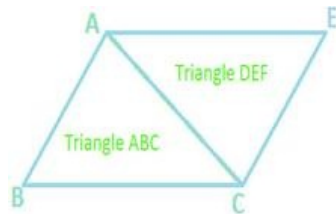
$$= 1/2(49)$$

$$= 24.5 \text{ sq units}$$

Question: 2

Find the area of

Solution:



For triangle ABC

Area of triangle

$$= 1/2(x_1(y_2 - y_3) + x_2(y_3 - y_1) + x_3(y_1 - y_2))$$

$$= 1/2(3(-5 - 0) + 9(0 + 1) + 14(-1 + 5))$$

$$= 1/2(-15 + 9 + 56)$$

$$= 1/2(50)$$

$$= 25$$

For triangle ACD

Area of triangle

$$= 1/2(x_1(y_2 - y_3) + x_2(y_3 - y_1) + x_3(y_1 - y_2))$$

$$= 1/2(3(0 - 19) + 14(19 + 1) + 9(-1 - 0))$$

$$= 1/2(-57 + 280 - 9)$$

$$= 1/2(214)$$

$$= 107$$

$$\text{Area of ABCD} = \text{Area of ABC} + \text{Area of ACD}$$

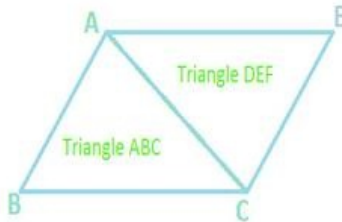
$$= 25 + 107$$

$$= 132 \text{ sq units}$$

Question: 3

Find the area of

Solution:



For triangle PQR

Area of triangle

$$= 1/2(x_1(y_2 - y_3) + x_2(y_3 - y_1) + x_3(y_1 - y_2))$$

$$= 1/2(-5(-6 + 3) - 4(-3 + 3) + 2(-3 + 6))$$

$$= 1/2(15 + 0 + 6)$$

$$= 1/2(21)$$

For triangle PRS

Area of triangle

$$= 1/2(x_1(y_2 - y_3) + x_2(y_3 - y_1) + x_3(y_1 - y_2))$$

$$= 1/2(-5(-3 - 2) + 2(2 - (-3)) + 1(-3 + 3))$$

$$= 1/2(25 + 10 + 0)$$

$$= 1/2(35)$$

$$\text{Area of ABCD} = \text{Area of ABC} + \text{Area of ACD}$$

$$= 21/2 + 35/2$$

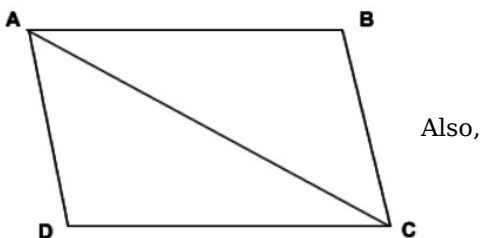
$$= 28 \text{ sq units}$$

Question: 4

Find the area of

Solution:

We divide quadrilateral in two triangles, such that $\text{Area of ABCD} = \text{Area of } \triangle ABC + \text{Area of } \triangle ACD$



We know area of a triangle, if it's coordinates are $A(x_1, y_1)$, $B(x_2, y_2)$ and $C(x_3, y_3)$ is

$$\text{Area} = \frac{1}{2}(x_1(y_2 - y_3) + x_2(y_3 - y_1) + x_3(y_1 - y_2)) \text{ Therefore, Area of ABC}$$

$$= \left| \frac{1}{2}[-3(-1 + 4) - 2(-1 + 1) + 4(-1 + 4)] \right|$$

$$= \left| \frac{1}{2}(-9 - 12) \right|$$

$$= \frac{21}{2}$$

$$= \frac{1}{2}[-3(-1 - 4) + 4(4 + 1) + 3(-1 + 1)]$$

$$\text{Area of ACD} = \frac{1}{2}(15 + 20)$$

$$\text{Area of ABCD} = \text{Area of ABC} + \text{Area of}$$

$$= \frac{35}{2}$$

ACD

$$= \frac{21}{2} + \frac{35}{2}$$

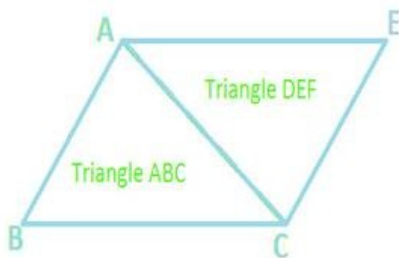
$$= 28 \text{ sq units}$$

$$= \frac{56}{2}$$

Question: 5

Find the area of

Solution:



For triangle ABC

Area of triangle

$$= 1/2(x_1(y_2 - y_3) + x_2(y_3 - y_1) + x_3(y_1 - y_2))$$

$$= 1/2(-5(-5 + 6) - 4(-6 - 7) - 1(7 + 5))$$

$$= 1/2(-5 + 52 - 12)$$

$$= 1/2(35)$$

For triangle ACD

Area of triangle

$$= 1/2(x_1(y_2 - y_3) + x_2(y_3 - y_1) + x_3(y_1 - y_2))$$

$$= 1/2(-5(-6 - 5) - 1(5 - 7) + 4(7 + 6))$$

$$= 1/2(-55 + 2 + 52)$$

$$= 1/2(1)$$

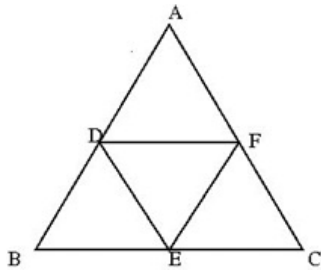
$$\text{Area of ABCD} = \text{Area of ABC} + \text{Area of ACD}$$

$$= 18 \text{ sq units}$$

Question: 6

Find the area of

Solution:



By applying section formula we get the coordinates of mid points of AB,BC and AC.

Mid point of AB = P = $\{(2 + 4)/2, (1 + 3)/2\}$

P = (3,2)

Mid point of BC = Q = $\{(4 + 2)/2, (3 + 5)/2\}$

Q = (3,4)

Mid point of AC = R = $\{(2 + 2)/2, (1 + 5)/2\}$

R = (2,3)

For triangle PQR

Area of triangle

$$= 1/2(x_1(y_2 - y_3) + x_2(y_3 - y_1) + x_3(y_1 - y_2))$$

$$= 1/2(3(4 - 3) + 3(3 - 2) + 2(2 - 4))$$

$$= 1/2(3 + 3 - 4)$$

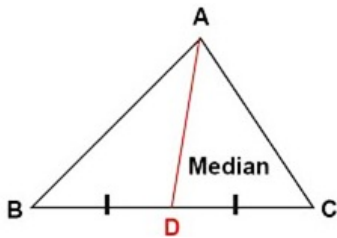
$$= 1/2(2)$$

$$= 1 \text{ sq unit}$$

Question: 7

A(7, -3), B(5, 3)

Solution:



$$D = \{(3 + 5)/2, (3 - 1)/2\} = (4, 1)$$

For triangle ABD

Area of triangle

$$= 1/2(x_1(y_2 - y_3) + x_2(y_3 - y_1) + x_3(y_1 - y_2))$$

$$= 1/2(7(3 - 1) + 5(1 + 3) + 4(-3 - 3))$$

$$= 1/2(14 + 20 - 24)$$

$$= 1/2(10)$$

$$= 5 \text{ sq unit}$$

For triangle ACD

Area of triangle

$$= 1/2(x_1(y_2 - y_3) + x_2(y_3 - y_1) + x_3(y_1 - y_2))$$

$$= 1/2(7(-1 - 1) + 3(1 + 3) + 4(-3 + 1))$$

$$= 1/2(-14 + 12 - 8)$$

$$= 1/2(10)$$

$$= 5 \text{ sq unit}$$

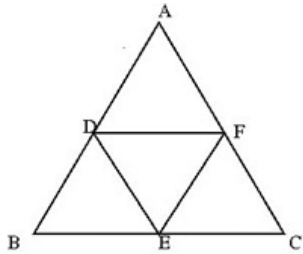
Hence area of triangle ABD and ACD is equal.

Question: 8

Find the area of

Solution:

The diagram is given below:



Coordinates of B

$$2 = (1 + x)/2 \text{ [by section formula]}$$

$$4 = 1 + x$$

$$X = 3$$

$$-1 = (-4 + y)/2$$

$$-2 = (-4 + y)$$

$$Y = 2$$

∴ the coordinates of B(3,2)

Coordinates of C [by section formula]

$$0 = (1 + x)/2$$

$$0 = (1 + x)$$

$$x = -1$$

$$-1 = (-4 + y)/2$$

$$-2 = (-4 + y)$$

$$Y = 2$$

∴ the coordinates of point C are (-1,2)

Now, Area of triangle ABC

$$= 1/2(x_1(y_2 - y_3) + x_2(y_3 - y_1) + x_3(y_1 - y_2))$$

$$= 1/2(1(2 - 2) + 3(2 + 4) - 1(-4 - 2))$$

$$= 1/2(0 + 18 + 6)$$

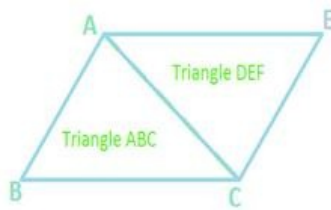
$$= 1/2(24)$$

$$= 12 \text{ sq unit}$$

Question: 9

A(6, 1), B(8, 2)

Solution:



Let (x, y) be the coordinates of D and (x', y') be the coordinates of E. since the diagonals of a parallelogram bisect each other at the same point, therefore

$$(x + 8)/2 = (6 + 9)/2$$

$$X = 7$$

$$(y + 2)/2 = (1 + 4)/2$$

$$Y = 3$$

Thus, the coordinates of D are $(7, 3)$

E is the midpoint of DC,

therefore

$$x' = (7 + 9)/2 = 8$$

$$y' = (3 + 4)/2 = 7/2$$

Thus, the coordinates of E are $(8, 7/2)$

Let $A(x_1, y_1) = A(6, 1)$, $E(x_2, y_2) = (8, 7/2)$ and $D(x_3, y_3) = D(7, 3)$

Now Area

$$= 1/2(x_1(y_2 - y_3) + x_2(y_3 - y_1) + x_3(y_1 - y_2))$$

$$= 1/2(6(7/2 - 3) + 8(3 - 1) + 7(1 - 7/2))$$

$$= 1/2(3/2)$$

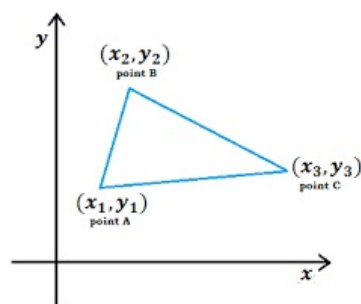
$$= 3/4 \text{ sq unit}$$

Hence, the area of the triangle $\triangle ADE$ is $3/4$ sq. units.

Question: 10

If the vertices o

Solution:



$$\text{Area} = 15$$

$$= \Delta = 1/2(x_1(y_2 - y_3) + x_2(y_3 - y_1) + x_3(y_1 - y_2))$$

$$15 = 1/2(x_1(y_2 - y_3) + x_2(y_3 - y_1) + x_3(y_1 - y_2))$$

$$15 = 1/2(1(p - 7) + 4(7 + 3) - 9(-3 - p))$$

$$15 = 1/2(10p + 16)$$

$$|10p + 16| = 30$$

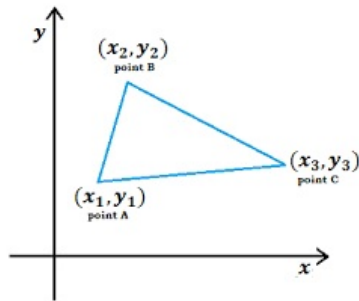
$$10p + 16 = 30 \text{ or } -30$$

Hence, $p = -9$ or $p = -3$.

Question: 11

Find the value of

Solution:



$$\Delta = 6$$

$$= \Delta = 1/2 \{x_1(y_2 - y_3) + x_2(y_3 - y_1) + x_3(y_1 - y_2)\}$$

$$6 = 1/2(x_1(y_2 - y_3) + x_2(y_3 - y_1) + x_3(y_1 - y_2))$$

$$6 = 1/2(k + 1(-3 + k) + 4(-k - 1) + 7(1 + 3))$$

$$6 = 1/2(k^2 - 2k - 3 - 4k - 4 + 28)$$

$$k^2 - 6k + 9 = 0$$

$$k = 3$$

Question: 12

For what value of

Solution:

Given the area of triangle, $\Delta = 53$

$$= \Delta = 1/2 \{x_1(y_2 - y_3) + x_2(y_3 - y_1) + x_3(y_1 - y_2)\}$$

$$53 = 1/2 \{-2(-4 - 10) + k(10 - 5) + 2k + 1(5 + 4)\}$$

$$53 = 1/2 \{28 + 5k + 9(2k + 1)\}$$

$$106 = (28 + 5k + 18k + 9)$$

$$37 + 3k = 106$$

$$23k = 69$$

$$k = 3$$

Question: 13 A

Show that the fol

Solution:

To show that the points are collinear, we show that the area of triangle is equilateral $= 0$

Given, the area of the triangle, $\Delta = 0$

$$= \Delta = 1/2(x_1(y_2 - y_3) + x_2(y_3 - y_1) + x_3(y_1 - y_2))$$

$$= \Delta = 1/2 \{2(8 - 4) + (-3)(4 + 2) - 1(2 - 8)\}$$

$$= \Delta = 1/2 \{8 - 18 + 10\}$$

$$= \Delta = 0$$

Hence the points A(2, - 2), B(-3, 8) and C(-1, 4) are collinear.

Question: 13 B

Show that the fol

Solution:

To show that the points are collinear, we show that the area of triangle is equilateral = 0

$$= \Delta = 1/2 \{ (x_1(y_2 - y_3) + x_2(y_3 - y_1) + x_3(y_1 - y_2)) \}$$

$$= \Delta = 1/2 \{ -5(5 - 7) + 5(7 - 1) + 10(1 - 5) \}$$

$$= \Delta = 1/2 \{ 10 + 30 - 40 \}$$

$$= \Delta = 0$$

Hence collinear.

Question: 13 C

Show that the fol

Solution:

To show that the points are collinear, we show that the area of triangle is equilateral = 0

$$\Delta = 0$$

$$\Delta = 1/2 \{ x_1(y_2 - y_3) + x_2(y_3 - y_1) + x_3(y_1 - y_2) \}$$

$$= \Delta = 1/2 \{ 5(-1 - 4) + 1(4 - 1) + 11(1 + 1) \}$$

$$= 1/2 \{ -25 + 3 + 22 \}$$

$$= 0$$

Hence collinear

Question: 13 D

Show that the fol

Solution:

A(8, 1), B(3, -4) and C(2, -5)

To show that the points are collinear, we show that the area of triangle is equilateral = 0

$$\Delta = 0$$

$$\Delta = 1/2 \{ x_1(y_2 - y_3) + x_2(y_3 - y_1) + x_3(y_1 - y_2) \}$$

$$= 1/2 \{ 8(-4 + 5) + 3(-5 - 1) + 2(1 + 4) \}$$

$$= 1/2 \{ 8 - 18 + 10 \}$$

$$= 0$$

Hence collinear.

Question: 14

Find the value of

Solution:

To show that the points are collinear, we show that the area of triangle is equilateral = 0

$$\Delta = 0$$

$$\Delta = 1/2 \{ x_1(y_2 - y_3) + x_2(y_3 - y_1) + x_3(y_1 - y_2) \}$$

$$= \Delta = 1/2 \{ x(-4 + 5) - 3(-5 - 2) + 7(2 + 4) \} = 0$$

$$= \Delta = 1/2\{x + 21 + 42\} = 0$$

$$x = -63$$

Question: 15

For what value of

Solution:

To show that the points are collinear, we show that the area of triangle is equilateral = 0

$$\Delta = 0$$

$$\Delta = 1/2\{x_1(y_2 - y_3) + x_2(y_3 - y_1) + x_3(y_1 - y_2)\}$$

$$= \Delta = 1/2\{-3(6-9) + 7(9-12) + x(12-6)\} = 0$$

$$= (-3)(-3) + 7(-3) + 6x = 0$$

$$= 9 - 21 + 6x = 0$$

$$6x = 12$$

$$x = 2$$

Question: 16

For what value of

Solution:



Collinear points P, Q, and R.

To show that the points are collinear, we show that the area of triangle is equilateral = 0

$$\Delta = 0$$

$$\Delta = 1/2\{x_1(y_2 - y_3) + x_2(y_3 - y_1) + x_3(y_1 - y_2)\}$$

$$= \Delta = 1/2\{1(y-16) + 3(16-4) - 3(4-y)\} = 0$$

$$= y - 16 + 36 - 12 + 3y = 0$$

$$= 8 + 4y = 0$$

$$= 4y = -8$$

$$y = -2$$

Question: 17

Find the value of

Solution:

To show that the points are collinear, we show that the area of triangle is equilateral = 0

$$\Delta = 0$$

$$\Delta = 1/2\{x_1(y_2 - y_3) + x_2(y_3 - y_1) + x_3(y_1 - y_2)\}$$

$$= \Delta = 1/2\{-3(y+5) + 2(-5-9) + 4(9-y)\} = 0$$

$$= -3y - 15 - 28 + 36 - 4y = 0$$

$$= 7y = 36 - 43$$

$$y = -1$$

Question: 18

For what values of

Solution:

To show that the points are collinear, we show that the area of triangle is equilateral = 0

$$\Delta = 0$$

$$\Delta = 1/2\{x_1(y_2-y_3) + x_2(y_3-y_1) + x_3(y_1-y_2)\}$$

$$= \Delta = 1/2\{8(-2k+5) + 3(-5-1) + k(1+2k)\} = 0$$

$$= -16k + 40 - 18 + k + 2k^2 = 0$$

$$= 2k^2 + 15k + 22 = 0$$

$$= 2k^2 - 11k - 14k + 22 = 0$$

$$= K(2k-11) - 2(2k-11) = 0$$

$$k = 2 \text{ or } k = \frac{11}{2}$$

Question: 19

Find a relation b

Solution:

To show that the points are collinear, we show that the area of triangle is equilateral = 0

$$\Delta = 0$$

$$\Delta = 1/2\{x_1(y_2-y_3) + x_2(y_3-y_1) + x_3(y_1-y_2)\}$$

$$= \Delta = 1/2\{2(y-5) + x(5-1) + 7(1-y)\}$$

$$= 2y - 10 + 4x - 7 - 7y = 0$$

$$= 4x - 5y - 3 = 0$$

Question: 20

Find a relation b

Solution:

To show that the points are collinear, we show that the area of triangle is equilateral = 0

$$\Delta = 0$$

$$\Delta = 1/2\{x_1(y_2-y_3) + x_2(y_3-y_1) + x_3(y_1-y_2)\}$$

$$= \Delta = 1/2\{x(7-5) + (-5)(-5-y) - 4(y-7)\}$$

$$= 7x - 5x - 25 + 5y - 4y + 28 = 0$$

$$= 2x + y + 3 = 0$$

Question: 21

Prove that the po

Solution:

To show that the points are collinear, we show that the area of triangle is equilateral = 0

$$\Delta = 0$$

$$\Delta = 1/2\{x_1(y_2-y_3) + x_2(y_3-y_1) + x_3(y_1-y_2)\} = 0$$

$$= \Delta = 1/2\{a(b-1) + 0(1-0) + 1(0-b)\} = 0$$

$$= (ab - a - b) = 0$$

Dividing the equation by ab .

$$1 - 1/b - 1/a$$

$$1 - (1/a + 1/b)$$

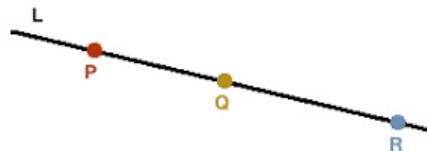
$$1 - 1 = 0$$

Hence collinear.

Question: 22

If the points P(-

Solution:



Collinear points P, Q, and R.

To show that the points are collinear, we show that the area of triangle is equilateral = 0

$$\Delta = 0$$

$$\Delta = 1/2 \{x_1(y_2 - y_3) + x_2(y_3 - y_1) + x_3(y_1 - y_2)\}$$

$$= \Delta = 1/2 \{-3(b + 5) + a(-5 - 9) + 4(9 - b)\} = 0$$

$$= -3b - 150 - 14a + 36 - 4b = 0$$

$$2a + b = 3$$

Now solving $a + b = 1$ and $2a + b = 3$ we get $a = 2$ and $b = -1$.

Hence $a = 2$, $b = -1$

Exercise : 16D

Question: 1

Points A(-1, y) a

Solution:

The distance of any point which lies on the circumference of the circle from the centre of the circle is called radius.

$\therefore OA = OB = \text{Radius of given Circle}$

taking square on both sides, we get-

$$OA^2 = OB^2$$

$$= (-1 - 2)^2 + [y - (-3y)]^2 = (5 - 2)^2 + [7 - (-3y)]^2$$

[using distance formula, the distance between points (x_1, y_1) and (x_2, y_2) is equal to

$$\sqrt{(x_1 - x_2)^2 + (y_1 - y_2)^2} \text{ units.}]$$

$$= 9 + 16y^2 = 9 + (7 + 3y)^2$$

$$= 16y^2 = 49 + 42y + 9y^2$$

$$= 7y^2 - 42y - 49 = 0$$

$$= 7(y^2 - 6y - 7) = 0$$

$$= y^2 - 7y + y - 7 = 0$$

$$= y(y-7) + 1(y-7) = 0$$

$$= (y + 1)(y-7) = 0$$

$$\therefore y = 7 \text{ or } y = -1$$

Thus, possible values of y are 7 or -1.

Question: 2

If the point A(0,

Solution:

According to question-

$$AB = AC$$

taking square on both sides, we get-

$$AB^2 = AC^2$$

$$= (0-3)^2 + (2-p)^2 = (0-p)^2 + (2-5)^2$$

[using distance formula, the distance between points (x_1, y_1) and (x_2, y_2) is equal to

$$\sqrt{(x_1 - x_2)^2 + (y_1 - y_2)^2} \text{ units.}]$$

$$= 9 + 4 + p^2 - 4p = p^2 + 9$$

$$= 4p - 4 = 0$$

$$= 4p = 4$$

$$\therefore p = 1$$

Thus, the value of p is 1.

Question: 3

ABCD is a rectang

Solution:

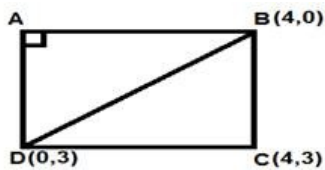


fig.1

Clearly from fig.1, One of the diagonals of the rectangle ABCD is BD.

Length of diagonal BD is given by-

$$BD = \sqrt{(4 - 0)^2 + (0 - 3)^2}$$

$$= \sqrt{4^2 + (-3)^2}$$

$$= \sqrt{16 + 9}$$

$$= \sqrt{25}$$

$$= 5 \text{ units}$$

Question: 4

If the point P(k

Solution:

According to question-

$$AP = BP$$

taking square on both sides, we get-

$$AP^2 = BP^2$$

$$= (k-4)^2 + (2-k)^2 = (-1)^2 + (2-5)^2$$

[using distance formula, the distance between points (x_1, y_1) and (x_2, y_2) is equal to $\sqrt{(x_1 - x_2)^2 + (y_1 - y_2)^2}$ units.]

$$= k^2 - 8k + 16 + 4 + k^2 - 4k = 1 + 9$$

$$= 2k^2 - 12k + 20 = 10$$

$$= 2k^2 - 12k + 10 = 0$$

$$= 2(k^2 - 6k + 5) = 0$$

$$= (k^2 - 5k - k + 5) = 0$$

$$= k(k-5) - 1(k-5) = 0$$

$$= (k-1)(k-5) = 0$$

$$\therefore k = 1 \text{ or } k = 5$$

Thus, the value of k is 1 or 5.

Question: 5

Find the ratio in

Solution:

Let the point P(x, 2) divides the join of A(12, 5) and B(4, -3) in the ratio of m:n.

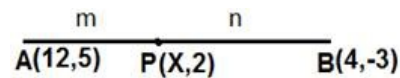


fig.2

Recall that if $(x, y) \equiv (a, b)$ then $x = a$ and $y = b$

\therefore assume that

$$(x, y) \equiv (x, 2)$$

$$(x_1, y_1) \equiv (12, 5)$$

$$\text{and, } (x_2, y_2) \equiv (4, -3)$$

Now, Using Section Formula-

$$y = \frac{my_2 + ny_1}{m + n}$$

$$\Rightarrow 2 = \frac{m \times (-3) + n \times (5)}{m + n}$$

$$\Rightarrow 2m + 2n = -3m + 5n$$

$$\Rightarrow 5m = 3n$$

$$\therefore m:n = 3:5$$

Thus, the required ratio is 3:5.

Question: 6

Prove that the di

Solution:

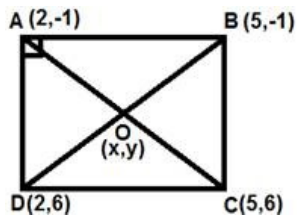


fig.3

Length of diagonal AC is given by-

$$AC = \sqrt{(2 - 5)^2 + (-1 - 6)^2}$$

$$= \sqrt{(-3)^2 + (-7)^2}$$

$$= \sqrt{9 + 49}$$

$$= \sqrt{58} \text{ units}$$

Length of diagonal BD is given by-

$$BD = \sqrt{(5 - 2)^2 + (-1 - 6)^2}$$

$$= \sqrt{3^2 + (-7)^2}$$

$$= \sqrt{9 + 49}$$

$$= \sqrt{58} \text{ units}$$

Clearly, the length of the diagonals of the rectangle ABCD are equal.

Mid-point of Diagonal AC is given by

$$= \left(\frac{2 + 5}{2}, \frac{-1 + 6}{2} \right)$$

$$= \left(\frac{7}{2}, \frac{5}{2} \right)$$

Similarly, Mid-point of Diagonal BD is given by

$$= \left(\frac{5 + 2}{2}, \frac{-1 + 6}{2} \right)$$

$$= \left(\frac{7}{2}, \frac{5}{2} \right)$$

Clearly, the coordinates of mid-point of both the diagonals coincide i.e. diagonals of the rectangle bisect each other.

Question: 7

Find the lengths

Solution:

A **median of a triangle** is a line segment joining a vertex to the midpoint of the opposing side, bisecting it.

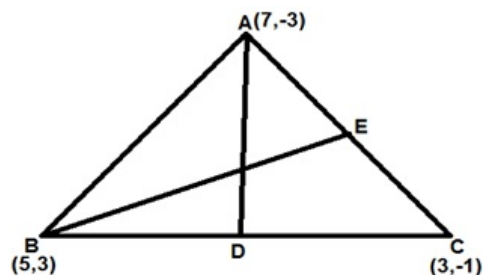


fig.4

Mid-point of side BC opposite to vertex A i.e. coordinates of point D is given by-

$$\begin{aligned} &= \left(\frac{5 + 3}{2}, \frac{3 - 1}{2} \right) \\ &= \left(\frac{8}{2}, \frac{2}{2} \right) \\ &= (4, 1) \end{aligned}$$

Mid-point of side AC opposite to vertex B i.e. coordinates of point E is given by-

$$\begin{aligned} &= \left(\frac{7 + 3}{2}, \frac{-3 - 1}{2} \right) \\ &= \left(\frac{10}{2}, \frac{-4}{2} \right) \\ &= (5, -2) \end{aligned}$$

Length of Median AD is given by-

$$\begin{aligned} AD &= \sqrt{(7 - 4)^2 + (-3 - 1)^2} \\ &= \sqrt{(3)^2 + (-4)^2} \\ &= \sqrt{9 + 16} \\ &= \sqrt{25} \\ &= 5 \text{ units} \end{aligned}$$

Length of Median BE is given by-

$$\begin{aligned} BD &= \sqrt{(5 - 5)^2 + (3 - (-2))^2} \\ &= \sqrt{0^2 + (3 + 2)^2} \\ &= \sqrt{0 + 5^2} \\ &= \sqrt{25} \\ &= 5 \text{ units} \end{aligned}$$

Thus, Length of Medians AD and BE are same which is equal to 5 units.

Question: 8

If the point C(k,

Solution:

Given that point C(k, 4) divides the join of A(2, 6) and B(5, 1) in the ratio 2 : 3.

$$\therefore m:n = 2:3$$

Recall that if $(x, y) \equiv (a, b)$ then $x = a$ and $y = b$

$$\text{Let } (x, y) \equiv (k, 4)$$

$$(x_1, y_1) \equiv (2, 6)$$

$$\text{and, } (x_2, y_2) \equiv (5, 1)$$

Now, Using Section Formula-

$$x = \frac{mx_2 + nx_1}{m + n}$$

On dividing numerator and denominator of R.H.S by n, we get-

$$x = \frac{\frac{m}{n}x_2 + 1x_1}{\frac{m}{n} + 1}$$

$$\Rightarrow k = \frac{\frac{2}{3} \times (5) + 1 \times (2)}{\frac{2}{3} + 1}$$

$$\Rightarrow k = \frac{\frac{10 + 6}{3}}{\frac{5}{3}}$$

$$\therefore k = (16/5)$$

Thus the value of k is (16/5).

Question: 9

Find the point on

Solution:

Let the point on the x-axis which is equidistant from points A(-1,0) and B(5,0) i.e. the point which divides the line segment AB in the ratio 1:1 be C(x,0).

$$\therefore m:n = 1:1$$

Recall that if $(x,y) \equiv (a,b)$ then $x = a$ and $y = b$

Let $(x,y) \equiv (x,0)$

$(x_1,y_1) \equiv (-1,0)$

and $(x_2,y_2) \equiv (5,0)$

Using Section Formula,

$$x = \frac{1 \times (5) + 1 \times (-1)}{1 + 1}$$

$$\Rightarrow x = \frac{5 - 1}{2}$$

$$\Rightarrow x = (4/2) = 2$$

Thus, the point on the x-axis which is equidistant from points A(-1,0) and B(5,0) is P(2,0).

Question: 10

Find the distance

Solution:

The distance between the points $\left(\frac{-8}{5}, 2\right)$ and $\left(\frac{2}{5}, 2\right)$ is given by- $= \sqrt{\left(\frac{-8}{5} - \frac{2}{5}\right)^2 + (2 - 2)^2}$

[using distance formula, the distance between points (x_1,y_1) and (x_2,y_2) is equal to

$\sqrt{(x_1 - x_2)^2 + (y_1 - y_2)^2}$ units.]

$$= \sqrt{\left(\frac{-10}{5}\right)^2 + (0)^2}$$

$$= \sqrt{(-2)^2 + 0}$$

$$= \sqrt{4}$$

$$= 2 \text{ units}$$

Question: 11

Find the value of

Solution:

Since the point (3, a) lies on the line represented by $2x - 3y = 5$

Thus, the point (3,a) will satisfy the above linear equation

$$\therefore 2 \times (3) - 3 \times (a) = 5$$

$$\Rightarrow 3a = 6-5$$

$$\Rightarrow 3a = 1$$

$$\therefore a = (1/3)$$

Thus, the value of a is (1/3).

Question: 12

If the points A(4

Solution:

The distance of any point which lies on the circumference of the circle from the centre of the circle is called radius.

$$\therefore OA = OB = \text{Radius of given Circle}$$

taking square on both sides, we get-

$$OA^2 = OB^2$$

$$\Rightarrow (2-4)^2 + (3-3)^2 = (2-x)^2 + (3-5)^2$$

[using distance formula, the distance between points (x_1, y_1) and (x_2, y_2) is equal to

$$\sqrt{(x_1 - x_2)^2 + (y_1 - y_2)^2} \text{ units.}]$$

$$\Rightarrow (-2)^2 + 0 = x^2 - 4x + 4 + (-2)^2$$

$$\Rightarrow x^2 - 4x + 4 = 0$$

$$\Rightarrow (x-2)^2 = 0$$

$$\therefore x = 2$$

Thus, the value of x is 2.

Question: 13

If P(x, y) is equ

Solution:

According to question-

$$AP = BP$$

taking square on both sides, we get-

$$AP^2 = BP^2$$

$$\Rightarrow (7-x)^2 + (1-y)^2 = (3-x)^2 + (5-y)^2$$

[using distance formula, the distance between points (x_1, y_1) and (x_2, y_2) is equal to

$$\sqrt{(x_1 - x_2)^2 + (y_1 - y_2)^2} \text{ units.}]$$

$$\Rightarrow x^2 - 14x + 49 + y^2 - 2y + 1 = x^2 - 6x + 9 + y^2 - 10y + 25$$

$$\Rightarrow -8x + 8y + 16 = 0$$

$$\Rightarrow -8(x-y-2) = 0$$

$$\Rightarrow x-y-2 = 0$$

$$\therefore x-y = 2$$

This is the required relation between x and y.

Question: 14

If the centroid o

Solution:

Every **triangle** has exactly three **medians**, one from each vertex, and they all intersect each other at a common point which is called **centroid**.

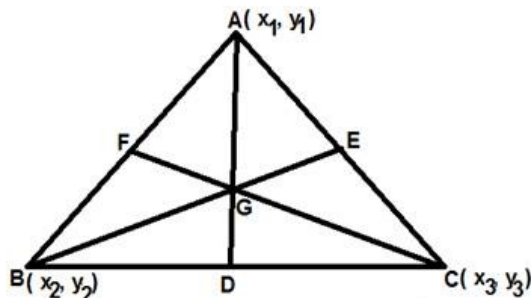


fig.5

In the fig.5, Let AD, BE and CF be the medians of ΔABC and point G be the centroid.

We know that-

Centroid of a Δ divides the medians of the Δ in the ratio 2:1.

Mid-point of side BC i.e. coordinates of point D is given by

$$= \left(\frac{x_2 + x_3}{2}, \frac{y_2 + y_3}{2} \right)$$

Let the coordinates of the centroid G be (x,y).

Since centroid G divides the median AD in the ratio 2:1 i.e.

$$AG:GD = 2:1$$

\therefore using section-formula, the coordinates of centroid is given by-

$$(x,y) \equiv \left(\frac{2 \left(\frac{x_2 + x_3}{2} \right) + 1(x_1)}{2 + 1}, \frac{2 \left(\frac{y_2 + y_3}{2} \right) + 1(y_1)}{2 + 1} \right)$$

$$\therefore (x,y) \equiv \left(\frac{x_1 + x_2 + x_3}{3}, \frac{y_1 + y_2 + y_3}{3} \right)$$

Now, according to question-

Centroid of ΔABC having vertices A(a, b), B(b, c) and C(c, a) is the origin.

$$\therefore \left(\frac{a + b + c}{3}, \frac{b + c + a}{3} \right) \equiv (0,0)$$

Thus, the value of a + b + c is 0.

Question: 15

Find the centroid

Solution:

The centroid of a Δ whose vertices are (x_1, y_1) , (x_2, y_2) and (x_3, y_3) is given by-

$$\left(\frac{x_1 + x_2 + x_3}{3}, \frac{y_1 + y_2 + y_3}{3} \right)$$

$$\therefore \text{centroid of the given } \Delta ABC \equiv \left[\frac{(2-4) + 5}{3}, \frac{(2-4-8)}{3} \right]$$

$$\equiv (1, -10/3)$$

Thus, the centroid of the given triangle ABC is $(1, -10/3)$.

Question: 16

In what ratio does

Solution:

Let the ratio in which the point C(4, 5) divides the join of A(2, 3) and B(7, 8) be $m:n$.

Recall that if $(x, y) \equiv (a, b)$ then $x = a$ and $y = b$

Let $(x, y) \equiv (4, 5)$

$(x_1, y_1) \equiv (2, 3)$

and, $(x_2, y_2) \equiv (7, 8)$

Now, Using Section Formula-

$$x = \frac{mx_2 + nx_1}{m + n}$$

$$\Rightarrow 4 = \frac{m(7) + n(2)}{m + n}$$

$$\Rightarrow 4m + 4n = 7m + 2n$$

$$\Rightarrow 3m = 2n$$

$$\therefore m:n = 2:3$$

Thus, the required ratio is 2:3.

Question: 17

If the points A(2

Solution:

If the three points are collinear then the area of the triangle formed by them will be zero.

Area of a ΔABC whose vertices are $A(x_1, y_1)$, $B(x_2, y_2)$ and $C(x_3, y_3)$ is given by-

$$\frac{1}{2} \sqrt{x_1(y_2 - y_3) + x_2(y_3 - y_1) + x_3(y_1 - y_2)} \text{ units}^2$$

$$\therefore \text{Area of given } \Delta ABC = 0$$

$$\Rightarrow \sqrt{2(k - (-3)) + 4(-3 - 3) + 6(3 - k)} = 0$$

squaring both sides, we get-

$$2(k + 3) + 4(-6) + 6(3 - k) = 0$$

$$\Rightarrow 2k + 6 - 24 + 18 - 6k = 0$$

$$\Rightarrow -4k + 24 - 24 = 0$$

$$\therefore k = 0$$

Thus, the value of k is zero.

Exercise : MULTIPLE CHOICE QUESTIONS (MCQ)

Question: 1

The distance of t

Solution:

The distance between any two points $P_1(x_1, y_1)$ and $P_2(x_2, y_2)$ is given by the following formula:

$$\text{Distance, } d = \sqrt{(x_2 - x_1)^2 + (y_2 - y_1)^2}$$

From the question we have,

$= P_1(x_1, y_1) = (0, 0)$co-ordinates of origin

$= P_2(x_2, y_2) = (-6, 8)$co-ordinates of point

$$= d = \sqrt{(-6 - 0)^2 + (8 - 0)^2}$$

$$= d = \sqrt{36 + 64}$$

$$= d = \sqrt{100}$$

$$= d = 10 \text{ units}$$

Therefore the distance between the point and origin is 10 units.

Question: 2

The distance of t

Solution:

The distance of any point from x-axis can be determined the modulus or absolute value of the y-coordinate of that point and in similar manner the distance of any point from y-axis can be determined the modulus or absolute value of the x-coordinate of that point

The modulus of y-coordinate is taken because distance cannot be negative.

In this case the y-coordinate is 4 and hence the distance of point from x-axis is 4 units.

Question: 3

The point on x-ax

Solution:

$=$ For the point to be equidistant, the point has to be the midpoint of the line joining the points A and B.

$=$ If $P(x, y)$ is the midpoint of the line joining AB then By Midpoint Formula we have,

$$= x = \frac{x_1 + x_2}{2} \text{ and } y = \frac{y_1 + y_2}{2}$$

Finding x co-ordinate of midpoint:

$$= x = \frac{-1 + 5}{2}$$

$$= x = \frac{4}{2}$$

$$= x = 2$$

Finding y- co-ordinate of midpoint:

$$= y = \frac{0 + 0}{2}$$

$$= y = 0$$

Therefore the point which is equidistant from A and B is $P(2,0)$.

Question: 4

If $R(5, 6)$ is the

Solution:

$=$ If $P(x, y)$ is the midpoint of the line joining AB then By Midpoint Formula we have,

$$= x = \frac{x_1 + x_2}{2} \text{ and } y = \frac{y_1 + y_2}{2}$$

Finding the value of y:

$$\Rightarrow y = \frac{y_1 + y_2}{2}$$

$$\Rightarrow 6 = \frac{5 + y}{2}$$

$$\Rightarrow 12 = 5 + y$$

$$\Rightarrow y = 12 - 5$$

$$\Rightarrow y = 7$$

Therefore the value of y is 7

Question: 5

If the point C(k,

Solution:

= If P(x, y) is the dividing point of the line joining AB then By Section Formula we have,

$$\Rightarrow x = \frac{mx_2 + nx_1}{m + n} \text{ and } y = \frac{my_2 + ny_1}{m + n}$$

where m and n is the ratio in which the point C divides the line AB

Finding the value of k:

$$\Rightarrow m = 2 \text{ and } n = 3$$

$$\Rightarrow k = \frac{2 \times 5 + 3 \times 2}{2 + 3}$$

$$\Rightarrow k = \frac{16}{5}$$

The value of k is 16/5.

Question: 6

The perimeter of

Solution:

The perimeter is the addition of lengths of all sides.

Let the points be A = (0, 4), B = (0, 0) and C = (3, 0).

The distance between any two points P₁(x₁, y₁) and P₂(x₂, y₂) is given by the following formula:

$$\Rightarrow \text{Distance, } d = \sqrt{(x_2 - x_1)^2 + (y_2 - y_1)^2}$$

$$\Rightarrow \text{Distance AB} = \sqrt{(0 - 0)^2 + (0 - 4)^2}$$

$$= \sqrt{4^2}$$

$$= 4$$

$$\Rightarrow \text{Distance BC} = \sqrt{(3 - 0)^2 + (0 - 0)^2}$$

$$= \sqrt{3^2}$$

$$= 3$$

$$\Rightarrow \text{Distance AC} = \sqrt{(3 - 0)^2 + (0 - 4)^2}$$

$$= \sqrt{9 + 16}$$

$$= \sqrt{25}$$

$$= 5$$

$$\therefore \text{Perimeter} = 3 + 4 + 5$$

$$= 12$$

Therefore the perimeter of triangle is 12.

Question: 7

If A(1, 3), B(-1,

Solution:

Since the given quadrilateral is a parallelogram, the length of parallel sides is equal.

So by distance formula,

$$= \text{Distance AB} = \sqrt{(-1-1)^2 + (2-3)^2}$$

$$= \sqrt{4 + 1}$$

$$= \sqrt{5}$$

$$= \text{Distance CD} = \sqrt{(x-2)^2 + (4-5)^2}$$

$$= \sqrt{(x-2)^2 + 1}$$

$$= \text{Distance CD} = \text{Distance AB}$$

$$= \sqrt{5} = \sqrt{(x-2)^2 + 1}$$

Squaring both sides

$$= 5 = (x-2)^2 + 1$$

$$= 4 = (x-2)^2$$

Taking square root of both sides

$$= 2 = x-2$$

$$= x = 4$$

or

$$= -2 = x-2$$

$$= x = 0$$

Therefore the value of x can be 0 or 4.

Question: 8

If the points A(x

Solution:

Three points A, B, C are said to be collinear if,

Area of triangle formed by three points is zero

The formula of Area of Triangle of three points is given as follows:

$$= A = \frac{1}{2} \begin{vmatrix} x_1 & x_2 & x_3 \\ y_1 & y_2 & y_3 \end{vmatrix} = 0$$

$$\frac{1}{2} \begin{vmatrix} x+3 & -3 & 7 \\ 2-(-4) & -4 & (-5) \end{vmatrix} = 0$$

$$= 1/2 \times \{[(x+3) \times 1] - [6 \times -10]\} = 0$$

$$= x + 3 + 60 = 0$$

$$= x = -63$$

Therefore the value of x is -63.

Question: 9

The area of a tri

Solution:

= Formula of Area of Triangle of three points is given as follows:

$$= \text{Area, } A = \frac{1}{2} \begin{vmatrix} x_1 - x_2 & x_2 - x_3 \\ y_1 - y_2 & y_2 - y_3 \end{vmatrix}$$

$$= \frac{1}{2} \begin{vmatrix} 5 - 8 & 8 - 8 \\ 0 - 0 & 0 - 4 \end{vmatrix}$$

$$= 1/2 \times \{[-3 \times -4] - 0\}$$

$$= 1/2 \times 12$$

$$= 6$$

Therefore the area of a triangle in square units is 6.

Question: 10

The area of $\triangle ABC$

Solution:

= Formula of Area of Triangle of three points is given as follows:

$$= \text{Area, } A = \frac{1}{2} \begin{vmatrix} x_1 - x_2 & x_2 - x_3 \\ y_1 - y_2 & y_2 - y_3 \end{vmatrix}$$

$$= \frac{1}{2} \begin{vmatrix} a - 0 & 0 - 0 \\ 0 - 0 & 0 - b \end{vmatrix}$$

$$= (ab)/2$$

Therefore the area of the triangle is $ab/2$.

Question: 11

If P(x, y) is the midpoint of the line joining AB then By Midpoint Formula we have,

$$\Rightarrow x = \frac{x_1 + x_2}{2} \text{ and } y = \frac{y_1 + y_2}{2}$$

$$\Rightarrow \frac{a}{2} = \frac{-6-2}{2}$$

$$\Rightarrow a = -8$$

Therefore the value of a is -8.

Question: 12

ABCD is a rectang

Solution:

Distance BD is the length of one of its diagonal.

= So by distance formula,

$$= \text{Distance BD} = \sqrt{(0-4)^2 + (0-3)^2}$$

$$= \sqrt{16 + 9}$$

$$= \sqrt{25}$$

$$= 5$$

Therefore the length of diagonal is 5 units.

Question: 13

The coordinates o

Solution:

If P(x, y) is the dividing point of the line joining AB then By Section Formula we have,

$$\Rightarrow x = \frac{mx_2 + nx_1}{m+n} \text{ and } y = \frac{my_2 + ny_1}{m+n}$$

where m and n is the ratio in which the point C divides the line AB

Finding the x-coordinate of P:

$$\Rightarrow x = \frac{2 \times 4 + 1 \times 1}{2 + 1}$$

$$\Rightarrow x = \frac{9}{3}$$

$$\Rightarrow x = 3$$

Finding the y-coordinate of P:

$$\Rightarrow y = \frac{2 \times 6 + 1 \times 3}{2 + 1}$$

$$\Rightarrow y = \frac{15}{3}$$

$$\Rightarrow y = 5$$

Therefore the coordinates of P is (3,5).

Question: 14

If the coordinate

Solution:

Since the center divides the diameter into two equal halves.

= Therefore by Midpoint Formula we have,

$$\Rightarrow x = \frac{x_1 + x_2}{2} \text{ and } y = \frac{y_1 + y_2}{2}$$

Finding the coordinates of another end of diameter:

Finding x-coordinate:

$$\Rightarrow -2 = \frac{2 + x_2}{2}$$

$$\Rightarrow -4 = 2 + x_2$$

$$\Rightarrow x_2 = -4 - 2$$

$$\Rightarrow x_2 = -6$$

Finding y-coordinate:

$$\Rightarrow 5 = \frac{3 + y_2}{2}$$

$$\Rightarrow 10 = 3 + y_2$$

$$\Rightarrow y_2 = 10 - 3$$

$$\Rightarrow y_2 = 7$$

Therefore the coordinates of another end of diameter are (-6, 7).

Question: 15

In the given figu

Solution:

From the given diagram, we come to know

$$\Rightarrow AP = PQ = QB$$

\Rightarrow Therefore the point P divides the line internally in the ratio 1:2 and Q divides the line in the ratio 2: 1

\Rightarrow Then by section formula the y-coordinate of point Q which divide the line AB is given as

$$\Rightarrow y = \frac{(-5 \times 2) + (1 \times -2)}{2 + 1}$$

$$\Rightarrow y = -12/3$$

$$\Rightarrow y = -4$$

Therefore the value of y is -4.

Question: 16

The midpoint of s

Solution:

\Rightarrow Therefore by Midpoint Formula we have,

$$\Rightarrow x = \frac{x_1 + x_2}{2} \text{ and } y = \frac{y_1 + y_2}{2}$$

Finding the coordinates of the end of A:

\Rightarrow Finding x-coordinate:

$$\Rightarrow 0 = \frac{-2 + x_2}{2}$$

$$\Rightarrow x_2 = 2$$

Finding y-coordinate:

$$\Rightarrow 4 = \frac{3 + y_2}{2}$$

$$\Rightarrow 8 = 3 + y_2$$

$$\Rightarrow y_2 = 8 - 3$$

$$\Rightarrow y_2 = 5$$

Therefore the coordinates of the end of A are (2, 5).

Question: 17

The point P which

Solution:

If P(x, y) is the dividing point of the line joining AB then By Section Formula we have,

$$\Rightarrow x = \frac{mx_2 + nx_1}{m + n} \text{ and } y = \frac{my_2 + ny_1}{m + n}$$

\Rightarrow where m and n is the ratio in which the point C divides the line AB

Finding the x-coordinate of P:

$$\Rightarrow x = \frac{2 \times 5 + 3 \times 2}{2 + 3}$$

$$\Rightarrow x = \frac{10 + 6}{5}$$

$$\Rightarrow x = 16/3$$

Finding the y-coordinate of P:

$$\Rightarrow y = \frac{2 \times 2 + 3 \times -5}{2 + 3}$$

$$= y = \frac{4-15}{3}$$

$$= y = -11/3$$

Therefore the coordinates of P is (16/3, -11/3).

Since in fourth quadrant x-coordinate is positive and y-coordinate is negative.

Therefore the point P lies in the fourth quadrant.

Question: 18

If A(-6, 7) and B

Solution:

$$= \text{Distance, } d = \sqrt{(x_2 - x_1)^2 + (y_2 - y_1)^2}$$

$$= \text{Distance AB} = \sqrt{(-1 - (-6))^2 + (-5 - 7)^2}$$

$$= \sqrt{(5)^2 + (-12)^2}$$

$$= \sqrt{(25 + 144)}$$

$$= \sqrt{169}$$

$$= 13$$

$$= \text{Distance } 2AB = 2 \times 13$$

$$= 26 \text{ units.}$$

Therefore the distance 2AB is 26 units.

Question: 19

Which point on th

Solution:

= Point on x-axis means its y-coordinate is zero.

= Let the point be P(x, 0)

Using the distance formula,

$$= \text{Distance, } d = \sqrt{(x_2 - x_1)^2 + (y_2 - y_1)^2}$$

$$= \text{Distance AP} = \text{Distance BP}$$

$$= (x-7)^2 + (0-6)^2 = (x+3)^2 + (0-4)^2 \Rightarrow x^2 + 49 - 14x + 36 = x^2 + 9 + 6x + 16$$

$$= 49 - 9 + 36 - 16 = 6x + 14x$$

$$= 40 + 20 = 20x$$

$$= x = 60/20$$

$$x = 3$$

Therefore the coordinate of P is (3,0).

Question: 20

The distance of P

Solution:

The distance of any point from x-axis can be determined the modulus or absolute value of the y-coordinate of that point and in a similar manner, the distance of any point from y-axis can be determined the modulus or absolute value of the x-coordinate of that point

The modulus of y-coordinate is taken because distance cannot be negative.

In this case, the y-coordinate is 4 and hence the distance of the point from x-axis is 4 units.

Question: 21

In what ratio doe

Solution:

= Let the ratio be k:1.

= Then by section formula the coordinates of point which divide the line AB is given as

$$\frac{5k + 2}{k + 1}, \frac{6k - 3}{k + 1}$$

= Since the point lies on x-axis its y-coordinate is zero.

$$= \frac{6k-3}{k+1} = 0$$

$$= 6k = 3$$

$$= k = 1/2$$

Therefore the ratio in which x-axis divide the line AB is 1:2.

Question: 22

In what ratio doe

Solution:

= Let the ratio be k:1.

= Then by section formula the coordinates of point which divide the line AB is given as

$$\frac{8k - 4}{k + 1}, \frac{3k + 2}{k + 1}$$

= Since the point lies on y-axis its x-coordinate is zero.

$$= \frac{8k-4}{k+1} = 0$$

$$= 8k = 4$$

$$= k = 1/2$$

Therefore the ratio in which x-axis divide the line AB is 1:2.

Question: 23

If P(-1, 1) is th

Solution:

∴ by Midpoint Formula we have,

$$= x = \frac{x_1 + x_2}{2} \text{ and } y = \frac{y_1 + y_2}{2}$$

Finding value of b:

$$= 1 = \frac{b + b + 4}{2}$$

$$= 2 = 2b + 4$$

$$= 2 - 4 = 2b$$

$$= b = -2/2$$

$$= b = -1$$

Therefore the value of b is -1.

Question: 24

The line $2x + y = 4$

Solution:

$$\Rightarrow 2x + y = 4 \quad \text{..... (1)}$$

Finding the equation of line formed by AB:

Finding slope:

$$= m = \frac{y_2 - y_1}{x_2 - x_1}$$

$$= m = \frac{7 - (-2)}{3 - 2}$$

$$= m = 9$$

The equation of line AB:

$$= y - y_1 = m(x - x_1)$$

$$= y - (-2) = 9(x - 2)$$

$$= y + 2 = 9x - 18$$

$$= 9x - y = 20 \quad \text{..... (2)}$$

When we solve the two equations simultaneously, we get point of intersection of two lines.

$$= \text{Adding (1) and (2)}$$

$$= 11x = 24$$

$$= x = 24/11$$

$$= \text{Substituting the value of } x \text{ in (1)}$$

$$= 2 \times 24/11 + y = 4$$

$$= y = 4 - 48/11$$

$$= y = -4/11$$

let us assume the line divides the segment AB in the ratio $k:1$

Then by section formula, the coordinates of point which divide the line AB is given as

$$\frac{3k + 2}{k + 1}, \frac{7k - 2}{k + 1}$$

Since we know x-coordinate of the point

$$= \frac{3k + 2}{k + 1} = \frac{24}{11}$$

$$= 33k + 22 = 24k + 24$$

$$= 9k = 2$$

$$= k = 2:9$$

Therefore the line $2x + y - 4 = 0$ divides the line segment AB into the ratio 2:9.

Question: 25

If A(4, 2), B(6,

Solution:

Since the AD is median, it divides the line BC into two equal halves. So D acts as the midpoint of line BC.

If D(x, y) is the midpoint of the line joining BC then By Midpoint Formula we have,

$$= x = \frac{x_1 + x_2}{2} \text{ and } y = \frac{y_1 + y_2}{2}$$

Finding x co-ordinate of midpoint:

$$\Rightarrow x = \frac{6+1}{2}$$

$$\Rightarrow x = \frac{7}{2}$$

$$\Rightarrow x = 7/2$$

Finding y- co-ordinate of midpoint:

$$\Rightarrow y = \frac{5+4}{2}$$

$$\Rightarrow y = 9/2$$

Therefore the point which is equidistant from A and B is P(7/2,9/2).

Question: 26

If A(-1, 0), B(5,

Solution:

Let P(x, y) be the centroid of the triangle

= Finding the x-coordinate of P:

$$\Rightarrow x = \frac{-1+5+8}{3}$$

$$\Rightarrow x = \frac{12}{3}$$

$$\Rightarrow x = 4$$

Finding the y-coordinate of P:

$$\Rightarrow y = \frac{0+2-2}{3}$$

$$\Rightarrow y = 0$$

Therefore the coordinates of P are (4, 0).

Question: 27

Two vertices of <

Solution:

Finding the x-coordinate of C:

$$\Rightarrow 0 = \frac{-1+5+x}{3}$$

$$\Rightarrow x = -4$$

Finding the y-coordinate of P:

$$\Rightarrow -3 = \frac{4+2+y}{3}$$

$$\Rightarrow -9 = 6 + y$$

$$\Rightarrow y = -15$$

Therefore the coordinates of P are (-4, -15).

Question: 28

The points A(-4,

Solution:

The distance between any two points $P_1(x_1, y_1)$ and $P_2(x_2, y_2)$ is given by the following formula:

$$= \text{Distance, } d = \sqrt{(x_2 - x_1)^2 + (y_2 - y_1)^2}$$

$$= \text{Distance AB} = \sqrt{(4 - (-4))^2 + (0 - 0)^2}$$

$$= \sqrt{8^2}$$

$$= 8$$

$$= \text{Distance BC} = \sqrt{(0 - 4)^2 + (3 - 0)^2}$$

$$= \sqrt{9 + 16}$$

$$= 5$$

$$= \text{Distance AC} = \sqrt{(0 - (-4))^2 + (3 - 4)^2}$$

$$= \sqrt{9 + 16}$$

$$= \sqrt{25}$$

$$= 5$$

Since the length of two sides is equal, given triangle is an isosceles triangle.

Question: 29

The points P(0, 6

Solution:

The distance between any two points $P_1(x_1, y_1)$ and $P_2(x_2, y_2)$ is given by the following formula:

$$= \text{Distance, } d = \sqrt{(x_2 - x_1)^2 + (y_2 - y_1)^2}$$

$$= \text{Distance AB} = \sqrt{(-5 - 0)^2 + (3 - 6)^2}$$

$$= \sqrt{25 + 9}$$

$$= \sqrt{34}$$

$$= \text{Distance BC} = \sqrt{(3 - (-5))^2 + (1 - 3)^2}$$

$$= \sqrt{64 + 4}$$

$$= \sqrt{68}$$

$$= \text{Distance AC} = \sqrt{(3 - 0)^2 + (1 - 6)^2}$$

$$= \sqrt{9 + 25}$$

$$= \sqrt{34}$$

Since the length of two sides is equal, given triangle is an isosceles triangle.

= The given triangle also satisfy Pythagoras Theorem in following way:

$$BC^2 = AC^2 + AB^2$$

Therefore the given triangle is also right-angled triangle.

Question: 30

If the points A(2

Solution:

Three points A, B, C are said to be collinear if,

Area of triangle formed by three points is zero

The formula of Area of Triangle of three points is given as follows:

$$\text{Area, } A = \frac{1}{2} \begin{vmatrix} x_1 - x_2 & x_2 - x_3 \\ y_1 - y_2 & y_2 - y_3 \end{vmatrix} = 0$$

$$= \frac{1}{2} \begin{vmatrix} 2 - 5 & 5 - 6 \\ 3 - k & k - 7 \end{vmatrix} = 0$$

$$= 1/2 \times \{[-3k + 21] - [-3 + k]\} = 0$$

$$= -4k + 21 + 3 = 0$$

$$= 4k = 24$$

$$= k = 6$$

Therefore the value of k is 6.

Question: 31

If the points A(1

Solution:

Three points A, B, C are said to be collinear if,

Area of triangle formed by three points is zero

= Formula of Area of Triangle of three points is given as follows:

$$= \text{Area, } A = \frac{1}{2} \begin{vmatrix} x_1 - x_2 & x_2 - x_3 \\ y_1 - y_2 & y_2 - y_3 \end{vmatrix} = 0$$

$$= \frac{1}{2} \begin{vmatrix} 1 - 0 & 0 - a \\ 2 - 0 & 0 - b \end{vmatrix} = 0$$

$$= 1/2 \times \{[-b \times 1] - [-a \times 2]\} = 0$$

$$= 2a - b = 0$$

$$= 2a = b$$

Hence Proved

Question: 32

The area of ΔABC

Solution:

The formula of Area of Triangle of three points is given as follows:

$$\text{Area, } A = \frac{1}{2} \begin{vmatrix} x_1 - x_2 & x_2 - x_3 \\ y_1 - y_2 & y_2 - y_3 \end{vmatrix}$$

$$= \frac{1}{2} \begin{vmatrix} 3 - 7 & 7 - 8 \\ 0 - 0 & 0 - 4 \end{vmatrix}$$

$$= 1/2 \times \{[-4 \times -4] - 0\}$$

$$= 8 \text{ sq. units}$$

Therefore the area of the triangle is 8 sq. units.

Question: 33

AOBC is a rectang

Solution:

Distance BD is the length of one of its diagonal.

So by distance formula,

$$\text{Distance AB} = \sqrt{(5 - 0)^2 + (0 - 3)^2}$$

$$= \sqrt{(25 + 9)}$$

$$= \sqrt{34} \text{ units}$$

Therefore the length of diagonal is $\sqrt{34}$ units.

Question: 34

If the distance b

Solution:

The distance between any two points $P_1(x_1, y_1)$ and $P_2(x_2, y_2)$ is given by the following formula:

$$\text{Distance, } d = \sqrt{(x_2 - x_1)^2 + (y_2 - y_1)^2}$$

= From the question we have,

$$= A = (4, p)$$

$$= B = (1, 0)$$

$$= d = 5$$

$$= 5 = \sqrt{(1 - 4)^2 + (0 - p)^2}$$

= Squaring both sides

$$= 25 = (-3)^2 + p^2$$

$$= 25 = 9 + p^2$$

$$= p^2 = 25 - 9$$

$$= p^2 = 16$$

$$= p = \pm 4$$

Therefore the value of p is ± 4 .