

## **Chapter : 18. AREA OF CIRCLE, SECTOR AND SEGMENT**

### **Exercise : 18A**

#### **Question: 1**

The difference between the circumference and the radius of circle = 37 cm

#### **Solution:**

Given:

Difference between the circumference and the radius of circle = 37 cm

Let the radius of the circle be 'r'.

Circumference of the circle =  $2\pi r$

So, Difference between the circumference and the radius of the circle =  $2\pi r - r = 37$

$$2\pi r - r = 37$$

$$2 \times \frac{22}{7} \times r - r = 37$$

$$\frac{44}{7} \times r - r = 37$$

$$r \left( \frac{44}{7} - 1 \right) = 37$$

$$\frac{37}{7} \times r = 37$$

$$r = 37 \times \frac{7}{37}$$

$$r = 7 \text{ cm}$$

$$\therefore \text{Circumference of circle} = 2 \times \frac{22}{7} \times 7$$

$$= 2 \times 22$$

$$= 44 \text{ cm}$$

Hence the circumference of the circle is 44 cm.

#### **Question: 2**

The circumference = 22 cm

#### **Solution:**

Given:

Circumference of circle = 22 cm

Let the radius of the circle be 'r'.

$\therefore$  Circumference of circle =  $2\pi r$

$$\therefore 22 = 2 \times \pi \times r$$

$$\Rightarrow 22 = 2 \times \frac{22}{7} \times r$$

$$\Rightarrow 22 \times \frac{7}{22} \times \frac{1}{2} = r \text{ or } \frac{7}{2} = r$$

$$\text{or } r = \frac{7}{2}$$

$$\therefore \text{Area of circle} = \pi r^2$$

$$\therefore \text{Area of its quadrant} = \frac{1}{4} \pi r^2$$

$$\begin{aligned}
 &= \frac{1}{4} \times \frac{22}{7} \times \frac{7}{2} \times \frac{7}{2} \\
 &= \frac{77}{8}
 \end{aligned}$$

Hence the area of the quadrant of the circle is  $\frac{77}{8}$  cm.

### Question: 3

What is the diameter

#### Solution:

Given:

Let the two circles be  $C_1$  and  $C_2$  with diameters 10 cm and 24 cm respectively.

$$\text{Area of circle, } C = \text{Area of } C_1 + \text{Area of } C_2 \dots \text{ (i)}$$

$$\because \text{Diameter} = 2 \times \text{radius}$$

$$\therefore \text{Radius of } C_1, r_1 = \frac{10}{2} = 5 \text{ cm}$$

$$\text{and Radius of } C_2, r_2 = \frac{24}{2} = 12 \text{ cm}$$

$$\because \text{Area of circle} = \pi r^2 \dots \text{ (ii)}$$

$$\therefore \text{Area of } C_1 = \pi r_1^2$$

$$= \frac{22}{7} \times 5 \times 5$$

$$= \frac{22}{7} \times 25$$

$$= \frac{550}{7} \text{ cm}^2$$

$$\text{Similarly, Area of } C_2 = \pi r_2^2$$

$$= \frac{22}{7} \times 12 \times 12$$

$$= 22/7 \times 144$$

$$= \frac{3168}{7} \text{ cm}^2$$

$\therefore$  Using equation (i), we have

$$\text{Area of } C = \frac{550}{7} + \frac{3168}{7}$$

$$= \frac{3718}{7} \text{ cm}^2$$

Now, using equation (ii), we have

$$\pi r^2 = \frac{3718}{7}$$

$$\frac{22}{7} \times r^2 = \frac{3718}{7}$$

$$r^2 = \frac{3718}{7} \times \frac{7}{22}$$

$$r^2 = 169$$

$$r = \sqrt{169}$$

$$r = 13 \text{ cm}$$

$$\Rightarrow \text{Diameter} = 2 \times r$$

$$= 2 \times 13$$

= 26 cm

Hence, the diameter of the circle is 26 cm.

**Question: 4**

If the area of a

**Solution:**

Given:

Area of circle =  $2 \times$  Circumference of circle ..... (i)

Let the radius of the circle be 'r'.

Then, the area of the circle =  $\pi r^2$

and the circumference of the circle =  $2\pi r$

Using (i), we have

$$\pi r^2 = 2 \times 2\pi r$$

$$\pi r^2 = 4\pi r$$

$$r = 4 \text{ cm}$$

$\therefore$  Diameter =  $2 \times$  radius

$$\therefore \text{Diameter} = 2 \times 4$$

$$= 8 \text{ cm}$$

Hence, the diameter of the circle is 8 cm.

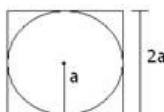
**Question: 5**

What is the perim

**Solution:**

Given:

Perimeter of square circumscribes a circle of radius 'a'.



Side of square = Diameter of circle

Diameter of circle =  $2 \times$  radius

$$= 2a$$

So, Side of square =  $2a$

$\therefore$  Perimeter of square =  $4 \times$  side

$$\therefore \text{Perimeter of square} = 4 \times 2a$$

$$= 8a$$

Hence, the perimeter of the square is  $8a$ .

**Question: 6**

Find the length o

**Solution:**

Given:

Diameter of circle = 42 cm

$$\Rightarrow \text{Radius of circle} = \frac{42}{2} \text{ cm} = 21 \text{ cm}$$

Angle subtended at the centre =  $60^\circ$

$$\therefore \text{Length of arc} = \frac{\theta}{360} \times 2\pi r$$

$$= \frac{60}{360} \times 2 \times \frac{22}{7} \times 21$$

$$= 22 \text{ cm}$$

Hence, the length of the arc is 22 cm.

**Question: 7**

Find the diameter

**Solution:**

Given:

Let the two circles with radii 4 cm and 3 cm be  $C_1$  and  $C_2$  respectively.

$$\Rightarrow r_1 = 4 \text{ cm and } r_2 = 3 \text{ cm}$$

Area of circle,  $C = \text{Area of } C_1 + \text{Area of } C_2 \dots \text{(i)}$

$$\therefore \text{Area of circle} = \pi r^2 \dots \text{(ii)}$$

$$\therefore \text{Area of } C_1 = \pi r_1^2$$

$$= \frac{22}{7} \times 4 \times 4$$

$$= \frac{22}{7} \times 16 = \frac{352}{7} \text{ cm}^2$$

Similarly, Area of  $C_2 = \pi r_2^2$

$$= \frac{22}{7} \times 3 \times 3$$

$$= \frac{22}{7} \times 9 = \frac{198}{7} \text{ cm}^2$$

So, using (i), we have

$$\text{Area of } C = \frac{352}{7} + \frac{198}{7} = \frac{550}{7} \text{ cm}^2$$

Now, using (ii), we have

$$\pi r^2 = \frac{550}{7}$$

$$\frac{22}{7} \times r^2 = \frac{550}{7}$$

$$r^2 = \frac{550}{7} \times \frac{7}{22} = 25$$

$$r = \sqrt{25} = 5$$

$$r = 5 \text{ cm}$$

$$\therefore \text{Diameter} = 2 \times \text{radius}$$

$$\therefore \text{Diameter} = 2 \times 5 = 10 \text{ cm}$$

Hence, diameter of the circle with area equal to the sum of two circles of radii 4 cm and 3cm is 10 cm.

**Question: 8**

Find the area of

**Solution:**

Given:

$$\text{Circumference of circle} = 8\pi$$

$$\therefore \text{Circumference of a circle} = 2\pi r$$

$$\therefore 8\pi = 2\pi r$$

$$r = 4$$

$$\therefore \text{Area of circle} = \pi r^2$$

$$\therefore \text{Area of circle} = \pi \times 4 \times 4$$

$$= 16\pi$$

Hence, the area of the circle is  $16\pi$ .

**Question: 9**

Find the perimeter

**Solution:**

Given:

$$\text{Diameter of the semicircular protractor} = 14 \text{ cm}$$

$$\text{Radius of the protractor} = \frac{14}{2} \text{ cm} = 7 \text{ cm}$$

$$\therefore \text{Perimeter of semicircle} = \pi r + d$$

$$\therefore \text{Perimeter of semicircular protractor} = \frac{22}{7} \times 7 + 14 = 22 + 14$$

$$= 36 \text{ cm}$$

Hence, the perimeter of the semicircular protractor is 36 cm.

**Question: 10**

Find the radius o

**Solution:**

Given:

$$\text{Perimeter of circle} = \text{Area of circle} \dots\dots \text{(i)}$$

$$\therefore \text{Perimeter of circle} = 2\pi r \text{ and Area of circle} = \pi r^2$$

$\therefore$  Using (i), we have

$$2\pi r = \pi r^2$$

$$2 = \frac{\pi r^2}{2\pi r}$$

$$2 = r \text{ or } r = 2$$

Hence, the radius of the circle is 2 cm.

**Question: 11**

The radii of two

**Solution:**

Given:

$$\text{Radius of one of the circles, } C_1 = 19 \text{ cm} = r_1$$

$$\text{Radius of the other circle, } C_2 = 9 \text{ cm} = r_2$$

Let the other circle be C with radius 'r'.

$$\text{Circumference of C} = \text{Circumference of } C_1 + \text{Circumference of } C_2 \dots\dots \text{(i)}$$

$\therefore$  Circumference of circle =  $2\pi r$

$$\therefore \text{Circumference of } C_1 = 2\pi r_1 = 2 \times \frac{22}{7} \times 19 = \frac{836}{7}$$

$$\text{and Circumference of } C_2 = 2\pi r_2 = 2 \times \frac{22}{7} \times 9 = \frac{396}{7}$$

Using (i), we have

$$2\pi r = \frac{836}{7} + \frac{396}{7} = \frac{1232}{7}$$

$$2 \times \frac{22}{7} \times r = \frac{1232}{7}$$

$$r = \frac{1232}{7} \times \frac{7}{22} \times \frac{1}{2} = 28$$

$$r = 28 \text{ cm}$$

Hence, the radius of the circle is 28 cm.

### Question: 12

The radii of two

#### Solution:

Given:

Radius of one of the circles,  $C_1 = 8 \text{ cm} = r_1$

Radius of the other circle,  $C_2 = 6 \text{ cm} = r_2$

Let the other circle be C with radius 'r'.

Area of C = Area of  $C_1 +$  Area of  $C_2 \dots \text{(i)}$

$\therefore$  Area of circle =  $\pi r^2$

$$\therefore \text{Area of } C_1 = \pi r_1^2 = \frac{22}{7} \times 8 \times 8 = \frac{1408}{7}$$

$$\text{and Area of } C_2 = \pi r_2^2 = \frac{22}{7} \times 6 \times 6 = \frac{792}{7}$$

Using (i), we have

$$\pi r^2 = \frac{1408}{7} + \frac{792}{7} = \frac{2200}{7}$$

$$\frac{22}{7} \times r^2 = \frac{2200}{7}$$

$$r^2 = \frac{2200}{7} \times \frac{7}{22} = 100$$

$$r^2 = 100$$

$$r = \sqrt{100} = 10 \text{ or } r = 10$$

Hence, the radius of the circle is 10 cm.

### Question: 13

Find the area of

#### Solution:

Given:

Radius of circle = 6 cm

Angle of the sector =  $30^\circ$

$$\therefore \text{Area of sector} = \frac{\theta}{360} \times \pi r^2$$

$$= \frac{30}{360} \times 3.14 \times 6 \times 6$$

$$= 3 \times 3.14 = 9.42 \text{ cm}^2$$

Hence, the area of the sector is 9.42 cm<sup>2</sup>.

### Question: 14

In a circle of ra

#### Solution:

Given:

Radius of circle = 21 cm

Angle subtended by the arc = 60°

$$\therefore \text{Length of arc} = \frac{\theta}{360} \times 2\pi r$$

$$= \frac{60}{360} \times 2 \times \frac{22}{7} \times 21 = 22 \text{ cm}$$

Hence, the length of the arc is 22 cm.

### Question: 15

The circumference

#### Solution:

Given:

Ratio of circumferences of two circles = 2:3

Let the two circles be C<sub>1</sub> and C<sub>2</sub> with radii 'r<sub>1</sub>' and 'r<sub>2</sub>'.

∴ Circumference of circle = 2πr

∴ Circumference of C<sub>1</sub> = 2πr<sub>1</sub>

and Circumference of C<sub>2</sub> = 2πr<sub>2</sub>

$$\Rightarrow \frac{2\pi r_1}{2\pi r_2} = \frac{2}{3}$$

$$\Rightarrow \frac{r_1}{r_2} = \frac{2}{3}$$

Squaring both sides, we get

$$\Rightarrow \frac{r_1^2}{r_2^2} = \frac{2^2}{3^2}$$

Multiplying both sides by 'π', we get

$$\Rightarrow \frac{\pi r_1^2}{\pi r_2^2} = \frac{4}{9}$$

∴ Area of circle = πr<sup>2</sup>

$$\Rightarrow \frac{\text{Area of } C_1}{\text{Area of } C_2} = \frac{4}{9}$$

Hence, the ratio between the areas of C<sub>1</sub> and C<sub>2</sub> is 4:9.

### Question: 16

The areas of two

#### Solution:

Given:

Ratio of areas of two circles = 2:3

Let the two circles be C<sub>1</sub> and C<sub>2</sub> with radii 'r<sub>1</sub>' and 'r<sub>2</sub>'.

$\therefore$  Area of circle =  $\pi r^2$

$\therefore$  Area of  $C_1 = \pi r_1^2$

and Area of  $C_2 = \pi r_2^2$

$$\Rightarrow \frac{\pi r_1^2}{\pi r_2^2} = \frac{4}{9}$$

$$\Rightarrow \frac{r_1^2}{r_2^2} = \frac{4}{9}$$

Taking square root on both sides, we get

$$\Rightarrow \frac{r_1}{r_2} = \frac{\sqrt{4}}{\sqrt{9}}$$

$$\Rightarrow \frac{r_1}{r_2} = \frac{2}{3}$$

Multiplying and dividing L.H.S. by ' $\pi$ ', we get

$$\Rightarrow \frac{\pi r_1}{\pi r_2} = \frac{2}{3}$$

Multiplying and dividing L.H.S. by '2', we get

$$\Rightarrow \frac{2\pi r_1}{2\pi r_2} = \frac{2}{3}$$

As Circumference of circle =  $2\pi r$

$$\Rightarrow \frac{\text{Circumference of } C_1}{\text{Circumference of } C_2} = \frac{2}{3}$$

Hence, the ratio between the circumferences of  $C_1$  and  $C_2$  is 2:3.

### Question: 17

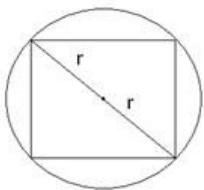
A square is inscr

#### Solution:

Given:

A square is inscribed in a circle.

Let the radius of circle be 'r' and the side of the square be 'x'.



$\Rightarrow$  The length of the diagonal =  $2r$

$$\therefore \text{Length of side of square} = \frac{\text{Length of diagonal}}{\sqrt{2}}$$

$$\therefore \text{Length of side of square} = \frac{2r}{\sqrt{2}} = \sqrt{2}r$$

$$\text{Area of square} = \text{side} \times \text{side} = x \times x = \sqrt{2}r \times \sqrt{2}r = 2r^2$$

$$\text{Area of circle} = \pi r^2$$

$$\text{Ratio of areas of circle and square} = \frac{\text{Area of circle}}{\text{Area of square}} = \frac{\pi r^2}{2r^2} = \frac{\pi}{2}$$

Hence, the ratio of areas of circle and square is  $\pi:2$ .

### Question: 18

The circumference

**Solution:**

Given:

Circumference of circle = 8 cm

Central angle =  $72^\circ$

$\therefore$  Circumference of a circle =  $2\pi r$

$$\therefore 2\pi r = 8$$

$$2 \times \frac{22}{7} \times r = 8$$

$$r = 8 \times \frac{7}{22} \times \frac{1}{2}$$

$$r = \frac{14}{11} \text{ cm}$$

$$\therefore \text{Area of sector} = \frac{\theta}{360} \times \pi r^2$$

$$= \frac{72}{360} \times \pi \times \frac{14}{11} \times \frac{14}{11}$$

$$= 1.02 \text{ cm}^2$$

**Question: 19**

A pendulum swings

**Solution:**

Given:

Angle made by the pendulum =  $30^\circ$

Length of the arc made by the pendulum = 8.8 cm

Then the length of the pendulum is equal to the radius of the sector made by the pendulum.

Let the length of the pendulum be 'r'.

$$\therefore \text{Length of arc} = \frac{\theta}{360} \times 2\pi r$$

$\therefore$  We have,

$$\frac{\theta}{360} \times 2\pi r = 8.8$$

$$\frac{30}{360} \times 2 \times 3.14 \times r = 8.8$$

$$r = 8.8 \times \frac{360}{30} \times \frac{1}{2} \times \frac{1}{3.14}$$

$$r = 16.8 \text{ cm}$$

Hence, the length of the pendulum is 16.8 cm.

**Question: 20**

The minute hand o

**Solution:**

Given:

Length of minute hand = 15 cm

Here, the length of the minute hand is equal to the radius of the sector formed by the minute hand.

$$\text{Angle made by the minute hand in 1 minute} = \frac{360}{60} = 6^\circ$$

$$\text{Angle made by the minute hand in 20 minutes} = 20 \times 6 = 120^\circ$$

Here, the area swept by the minute hand is equal to the area of the corresponding sector made.

$$\begin{aligned}\therefore \text{Area of sector} &= \frac{\theta}{360} \times \pi r^2 \\ &= \frac{120}{360} \times 3.14 \times 15 \times 15 = 235.5 \text{ cm}^2\end{aligned}$$

Hence, the area swept by it in 20 minutes is  $235.5 \text{ cm}^2$ .

**Question: 21**

A sector of  $56^\circ$ ,

**Solution:**

Given:

Angle of the sector =  $56^\circ$

Area of the sector =  $17.6 \text{ cm}^2$

Let the radius of the circle be 'r'.

$$\therefore \text{Area of sector} = \frac{\theta}{360} \times \pi r^2$$

$$\therefore 17.6 = \frac{56}{360} \times \frac{22}{7} \times r^2$$

$$r^2 = \frac{360}{56} \times \frac{7}{22} \times 17.6$$

$$r^2 = 36$$

$$r = \sqrt{36}$$

$$r = 6 \text{ cm}$$

Hence, the radius of the circle is 6 cm.

**Question: 22**

The area of the s

**Solution:**

Given:

Radius of the circle =  $10.5 \text{ cm}$

Area of the sector =  $69.3 \text{ cm}^2$

$$\therefore \text{Area of the sector} = \frac{\theta}{360} \times \pi r^2$$

$$\therefore 69.3 = \frac{\theta}{360} \times \frac{22}{7} \times 10.5 \times 10.5$$

$$\theta = 69.3 \times 360 \times \frac{7}{22} \times \frac{1}{10.5} \times \frac{1}{10.5}$$

$$\theta = 72^\circ$$

Hence, the central angle is  $72^\circ$ .

**Question: 23**

The perimeter of

**Solution:**

Given:

Radius of circle =  $6.5 \text{ cm}$

Perimeter of sector =  $31 \text{ cm}$

Now, Perimeter of sector =  $2 \times \text{radius} + \text{Length of arc}$

$$\therefore \text{Length of arc} = \frac{\theta}{360} \times 2r \times 2\pi r$$

$$\therefore \text{Perimeter of sector} = 2 \times r + \frac{\theta}{360} \times 2r \times \pi$$

$$= 2r \times [1 + \frac{\theta}{360} \times \pi]$$

$$31 = 2 \times 6.5 \times [1 + \frac{\theta}{360} \times \frac{22}{7}]$$

$$31 = 13 \times [1 + \frac{\theta}{360} \times \frac{22}{7}]$$

$$\frac{31}{13} = 1 + \frac{\theta}{360} \times \frac{22}{7}$$

$$\frac{31}{13} - 1 = \frac{\theta}{360} \times \frac{22}{7}$$

$$\frac{18}{13} = \frac{\theta}{360} \times \frac{22}{7}$$

$$\therefore \text{Area of sector} = \frac{\theta}{360} \times \pi r^2$$

$\therefore$  using (i), we have

$$\text{Area} = \frac{18}{13} \times 360 \times \frac{7}{22} \times \frac{1}{360} \times \frac{22}{7} \times 6.5 \times 6.5$$

$$= 18 \times 3.25 = 58.5 \text{ cm}^2$$

Hence, the area of the sector is  $58.5 \text{ cm}^2$ .

## **Question: 24**

The radius of a c

### Solution:

Given:

Radius of circle = 17.5 cm

Length of arc = 44 cm

$$\therefore \text{Length of arc} = \frac{\theta}{360^\circ} \times 2\pi r$$

$$\therefore 44 = \frac{0}{360} \times 2 \times \frac{22}{7} \times 17.5$$

$$\theta = 44 \times 360 \times \frac{1}{2} \times \frac{7}{22} \times \frac{10}{175}$$

$$\theta = \frac{2520}{17.5} = 144^\circ$$

Now, Area of sector =  $\frac{\theta}{360} \times \pi r^2$

$$= \frac{144}{260} \times \frac{22}{7} \times 17.5 \times 17.5 = 385 \text{ cm}^2$$

Hence, the area of the sector is  $385 \text{ cm}^2$

### Question: 25

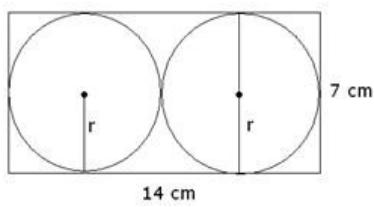
## Two circular pieces

**Solution:**

Given:

Length of the rectangular cardboard = 14 cm

Breadth of the rectangular cardboard = 7 cm



$\therefore$  Area of rectangle = length  $\times$  breadth

$$\therefore \text{Area of cardboard} = 14 \times 7 = 98 \text{ cm}^2$$

Let the two circles with equal radii and maximum area have a radius of 'r' cm each.

$$\text{Then, } 2r = 7$$

$$r = \frac{7}{2} \text{ cm}$$

$$\therefore \text{Area of circle} = \pi r^2$$

$$\therefore \text{Area of two circular cut outs} = 2 \times \pi r^2$$

$$= 2 \times \frac{22}{7} \times \frac{7}{2} \times \frac{7}{2}$$

$$= 11 \times 7 = 77 \text{ cm}^2$$

$$\text{Thus, the area of remaining cardboard} = 98 - 77 = 21 \text{ cm}^2$$

Hence, the area of remaining cardboard is 21 cm<sup>2</sup>.

### Question: 26

In the given figure

#### Solution:

Given:

Side of the square = 4 cm

Radius of the quadrants at the corners = 1 cm

Radius of the circle in the centre = 1 cm

$$\therefore 4 \text{ quadrants} = 1 \text{ circle}$$

$\therefore$  There are 2 circles of radius 1 cm

Area of square = side  $\times$  side

$$= 4 \times 4 = 16 \text{ cm}^2$$

Area of 2 circles =  $2 \times \pi r^2$

$$= 2 \times \frac{22}{7} \times 1 \times 1 = \frac{44}{7} \text{ cm}^2$$

$\therefore$  Area of shaded region = Area of square - Area of 2 circles

$$= 16 - \frac{44}{7}$$

$$= \frac{112-44}{7} = \frac{68}{7} \text{ cm}^2 = 9.7 \text{ cm}^2$$

Hence, the area of shaded region is 9.72 cm<sup>2</sup>.

### Question: 27

From a rectangular

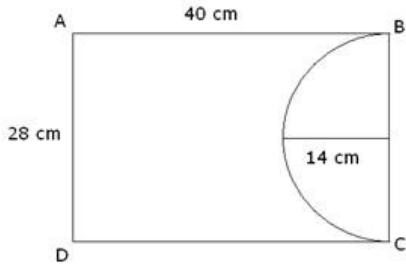
#### Solution:

Given:

Length of rectangular sheet of paper = 40 cm

Breadth of rectangular sheet of paper = 28 cm

Radius of the semicircular cut out = 14 cm



$\therefore$  Area of rectangle = length  $\times$  breadth

$$\therefore \text{Area of rectangular sheet of paper} = 40 \times 28$$

$$= 1120 \text{ cm}^2$$

$$\therefore \text{Area of semicircle} = \frac{1}{2}\pi r^2$$

$$\therefore \text{Area of semicircular cut out} = \frac{1}{2} \times \frac{22}{7} \times 14 \times 14$$

$$= 22 \times 14 = 308 \text{ cm}^2$$

Thus, the area of remaining sheet of paper = Area of rectangular sheet of paper - Area of semicircular cut out

$$= 1120 - 308 = 812 \text{ cm}^2$$

Hence, the area of remaining sheet of paper is  $812 \text{ cm}^2$ .

### Question: 28

In the given figure

#### Solution:

Given:

Side of square = 7 cm

Radius of the quadrant = 7 cm

Area of square = side  $\times$  side

$$= 7 \times 7 = 49 \text{ cm}^2$$

$$\therefore \text{Area of circle} = \pi r^2$$

$$\therefore \text{Area of a quadrant} = \frac{1}{4} \pi r^2$$

$$= \frac{1}{4} \times \frac{22}{7} \times 7 \times 7$$

$$= \frac{77}{2} = 38.5 \text{ cm}^2$$

Thus, the area of shaded region = Area of square - Area of quadrant

$$= 49 - 38.5 = 10.5 \text{ cm}^2$$

Hence, the area of the shaded region is  $10.5 \text{ cm}^2$ .

### Question: 29

In the given figure

#### Solution:

Given:

Radius of circle = 7 cm

Let the sectors with central angles  $80^\circ$ ,  $60^\circ$  and  $40^\circ$  be  $S_1$ ,  $S_2$ , and  $S_3$  respectively.

Then, the area of shaded region = Area of  $S_1$  + Area of  $S_2$  + Area of  $S_3$  .....(i)

$$\therefore \text{Area of sector} = \frac{\theta}{360} \times \pi r^2$$

$$\therefore \text{Area of } S_1 = \frac{80}{360} \times \frac{22}{7} \times 7 \times 7$$

$$= \frac{308}{9} \text{ cm}^2$$

$$\text{Similarly, Area of } S_2 = \frac{60}{360} \times \frac{22}{7} \times 7 \times 7$$

$$= \frac{154}{6} \text{ cm}^2$$

$$\text{and Area of } S_3 = \frac{40}{360} \times \frac{22}{7} \times 7 \times 7$$

$$= \frac{154}{9} \text{ cm}^2$$

Thus, using (i), we have

$$\text{Area of shaded region} = \frac{308}{9} + \frac{154}{6} + \frac{154}{9}$$

$$= \frac{616 + 462 + 308}{18}$$

$$= \frac{1386}{18} = 77 \text{ cm}^2$$

Hence, the area of shaded region is  $77 \text{ cm}^2$ .

### Question: 30

In the given figure

#### Solution:

Given:

Radius of inner circle = 3.5 cm

Radius of outer circle = 7 cm

$\angle POQ = 30^\circ$

Let the sector made by the arcs PQ and AB be  $S_1$  and  $S_2$  respectively.

Then, Area of shaded region = Area of  $S_1$  - Area of  $S_2$  .....(i)

$$\therefore \text{Area of sector} = \frac{\theta}{360} \times \pi r^2$$

$$\therefore \text{Area of } S_1 = \frac{30}{360} \times \frac{22}{7} \times 7 \times 7$$

$$= \frac{71}{6} \text{ cm}^2$$

$$\text{Similarly, Area of } S_2 = \frac{30}{360} \times \frac{22}{7} \times 3.5 \times 3.5$$

$$= \frac{77}{24} \text{ cm}^2$$

Thus, using (i), we have

$$\text{Area of shaded region} = \frac{71}{6} - \frac{77}{24}$$

$$= \frac{308 - 77}{24}$$

$$= \frac{231}{24} = \frac{77}{8} \text{ cm}^2$$

Hence, the area of shaded region is  $\frac{77}{8}$  cm<sup>2</sup>.

**Question: 31**

In the given figure

**Solution:**

Given:

Side of square = 14 cm

Diameter of each semicircle = 14 cm

Radius of each semicircle =  $\frac{14}{2} = 7$  cm

∴ Both the semicircles have same radius.

∴ We consider one circle of radius 7 cm.

Area of shaded region = Area of square - Area of circle ..... (i)

Area of square = side × side

$$= 14 \times 14 = 196 \text{ cm}^2$$

Area of circle =  $\pi r^2$

$$= \frac{22}{7} \times 7 \times 7 = 22 \times 7 = 154 \text{ cm}^2$$

Thus, using (i), we have

$$\text{Area of shaded region} = 196 - 154 = 42 \text{ cm}^2$$

Hence, the area of shaded region is 42 cm<sup>2</sup>.

**Question: 32**

In the given figure

**Solution:**

Given:

Radius of the circle = 42 cm

Central angle of the sector = ∠AOB = 90°

Perimeter of the top of the table = Length of the major arc AB + 2 × radius ..... (i)

Length of major arc AB =  $\frac{(360-90)}{360} \times 2\pi r$

$$= \frac{(360-90)}{360} \times 2 \times \frac{22}{7} \times 42$$

$$= \frac{270}{360} \times 2 \times 22 \times 6$$

$$= \frac{3}{4} \times 264 = 3 \times 66 = 198 \text{ cm}$$

Thus, using (i), we have

Perimeter of the top of the table = 198 + 2 × 42

$$= 198 + 84 = 282 \text{ cm}$$

Hence, the perimeter of the top of the table is 282 cm.

**Question: 33**

In the given figure

**Solution:**

Given:

Side of square = 7 cm

Radius of each quadrant = 7 cm

Area of square = side × side =  $7 \times 7 = 49 \text{ cm}^2$

$$\therefore \text{Area of quadrant} = \frac{1}{4} \pi r^2$$

$$\therefore \text{Area of 2 quadrants} = 2 \times \frac{1}{4} \times \pi r^2$$

$$= \frac{1}{2} \times \frac{22}{7} \times 7 \times 7$$

$$= 77 \text{ cm}^2$$

Area of shaded region = Area of 2 quadrants - Area of square

$$= 77 - 49 = 28 \text{ cm}^2$$

Hence, the area of shaded region is  $28 \text{ cm}^2$ .

### Question: 34

In the given figure

#### Solution:

Given:

Radius of Circle = 3.5 cm

OD = 2 cm

$$\therefore \text{Area of Quadrant} = \frac{1}{4} \pi r^2$$

$$\therefore \text{Area of Quadrant OABC} = \frac{1}{4} \times \frac{22}{7} \times 3.5 \times 3.5$$

$$= 9.625 \text{ cm}^2$$

$$\therefore \text{Area of Triangle} = \frac{1}{2} \times \text{Base} \times \text{Height}$$

$$\therefore \text{Area of } \triangle COD = \frac{1}{2} \times 3.5 \times 2$$

$$= 3.5 \text{ cm}^2$$

Area of Shaded Region = Area of Quadrant OABC - Area of  $\triangle COD$

$$= 9.625 - 3.5 = 35 \text{ cm}^2$$

Hence, the area of shaded region is  $35 \text{ cm}^2$ .

### Question: 35

Find the perimeter

#### Solution:

Given:

Side of square = 14 cm

Diameter of semi circle = 14 cm

$$\Rightarrow \text{Radius of semi circle} = \frac{14}{2} = 7 \text{ cm}$$

$\therefore$  There are 2 semi circles of same radius.

$\therefore$  We consider it as one circle with radius 7 cm.

So,

Perimeter of 2 semicircles = Perimeter of circle =  $2\pi r$

$$= 2 \times \frac{22}{7} \times 7$$

$$= 2 \times 22 = 44 \text{ cm}$$

Perimeter of shaded region = Perimeter of 2 semicircles + 2 × Side of Square =  $44 + 2 \times 14 = 44 + 28 = 72 \text{ cm}$

Hence, the area of the shaded region is 72 cm.

**Question: 36**

In a circle of radius 7 cm

**Solution:**

Given:

Radius of the circle = 7 cm

Diameter of the circle = 14 cm

Here, diagonal of square = 14 cm

$$\therefore \text{Side of a square} = \frac{\text{diagonal}}{\sqrt{2}}$$

$$\Rightarrow \text{Side} = \frac{14}{\sqrt{2}} = 7\sqrt{2} \text{ cm}$$

$\Rightarrow$  Area of square = side × side

$$= 7\sqrt{2} \times 7\sqrt{2}$$

$$= 49 \times 2 = 98 \text{ cm}^2$$

Area of circle =  $\pi r^2$

$$= \frac{22}{7} \times 7 \times 7 = 22 \times 7 = 154 \text{ cm}^2$$

Thus, the area of the circle outside the square

$$= \text{Area of circle} - \text{Area of square} = 154 - 98 = 56 \text{ cm}^2$$

Hence, the area of the required region is 56 cm<sup>2</sup>.

**Question: 37**

In the given figure

**Solution:**

(i) Given:

Diameter of semicircles APB and CQD = 7 cm

$$\Rightarrow \text{Radius of semicircles APB and CQD} = \frac{7}{2} \text{ cm} = r_1$$

Diameter of semicircles ARC and BSD = 14 cm

$$\Rightarrow \text{Radius of semicircles ARC and BSD} = \frac{14}{2} \text{ cm} = 7 \text{ cm} = r_2$$

Perimeter of APB = Perimeter of CQD

Area of APB = Area of CQD ..... (i)

Perimeter of ARC = Perimeter of BSD

Area of ARC = Area of BSD ..... (ii)

$\therefore$  Perimeter of semicircle =  $\pi r$  ..... (iii)

$\therefore$  Perimeter of APB =  $\pi r_1$

$$= \frac{22}{7} \times \frac{7}{2} = 11 \text{ cm}$$

Then, using (i), we have

Perimeter of CQD = 11 cm

Now, using (iii), we have

Perimeter of ARC =  $\pi r_2$

$$= \frac{22}{7} \times 7 = 22 \text{ cm}$$

Then, using (ii), we have

Perimeter of BSD = 22 cm

Perimeter of shaded region

$$= (\text{Perimeter of ARC} + \text{Perimeter of APB}) + (\text{Perimeter of BSD} + \text{Perimeter of CQD})$$

$$= (22 + 11) + (22 + 11) = 33 + 33 = 66 \text{ cm}$$

Hence, the perimeter of the shaded region is 66 cm.

(ii) Now,

$$\therefore \text{Area of semicircle} = \frac{1}{2} \pi r^2 \dots \dots \dots \text{(iv)}$$

$$\therefore \text{Area of APB} = \frac{1}{2} \pi r_1^2$$

$$= \frac{1}{2} \times \frac{22}{7} \times \frac{7}{2} \times \frac{7}{2} = \frac{77}{4} \text{ cm}^2$$

Then, using (i), we have

$$\text{Area of CQD} = \frac{77}{4} \text{ cm}^2$$

Now, using (iv), we have

$$\text{Area of ARC} = \frac{1}{2} \pi r_2^2$$

$$= \frac{1}{2} \times \frac{22}{7} \times 7 \times 7 = 11 \times 7 = 77 \text{ cm}^2$$

Then, by using (ii), we have

$$\text{Area of BSD} = 77 \text{ cm}^2$$

Area of shaded region

$$= (\text{Area of ARC} - \text{Area of APB}) + (\text{Area of BSD} - \text{Area of CQD})$$

$$= (77 - \frac{77}{4}) + (77 - \frac{77}{4})$$

$$= (\frac{308-77}{4}) + (\frac{308-77}{4}) = \frac{231}{4} + \frac{231}{4} = \frac{462}{4} = 115.5 \text{ cm}^2$$

Hence, the area of the shaded region is 115.5 cm<sup>2</sup>.

### Question: 38

In the given figure

#### Solution:

Given:

Diameter of semicircle PSR = 10 cm

$$\Rightarrow \text{Radius of semicircle PSR} = \frac{10}{2} = 5 \text{ cm} = r_1$$

Diameter of semicircle RTQ = 3 cm

$$\Rightarrow \text{Radius of semicircle RTQ} = \frac{3}{2} = 1.5 \text{ cm} = r_2$$

Diameter of semicircle PAQ = 7 cm

$$\Rightarrow \text{Radius of semicircle PAQ} = \frac{7}{2} = 3.5 \text{ cm} = r_3$$

$\therefore$  Perimeter of semicircle =  $\pi r$

$$\therefore \text{Perimeter of semicircle PSR} = \pi r_1$$

$$= 3.14 \times 5 = 15.7 \text{ cm}$$

Similarly, Perimeter of semicircle RTQ =  $\pi r_2$

$$= 3.14 \times 1.5 = 4.71 \text{ cm}$$

and Perimeter of semicircle PAQ =  $\pi r_3$

$$= 3.14 \times 3.5 = 10.99 \text{ cm}$$

Perimeter of shaded region = Perimeter of semicircle PSR

$$+ \text{Perimeter of semicircle RTQ}$$

$$+ \text{Perimeter of semicircle PAQ}$$

$$= 15.7 + 4.71 + 10.99 = 31.4 \text{ cm}$$

Hence, the perimeter of the shaded region is 31.4 cm.

### Question: 39

In the given figure

#### Solution:

Given:

OA = Side of square OABC = 20 cm

$\therefore$  Area of square = Side  $\times$  Side

$$\therefore \text{Area of square OABC} = 20 \times 20 = 400 \text{ cm}^2$$

Now,

$\therefore$  Length of diagonal of square =  $\sqrt{2} \times$  Side of Square

$$\therefore \text{Length of diagonal of square OABC} = \sqrt{2} \times 20 = 20\sqrt{2} \text{ cm}$$

$\Rightarrow$  Radius of the quadrant =  $20\sqrt{2}$  cm

$$\therefore \text{Area of quadrant} = \frac{1}{4} \pi r^2$$

$$\therefore \text{Area of quadrant OPBQ} = \frac{1}{4} \times 3.14 \times 20\sqrt{2} \times 20\sqrt{2}$$

$$= \frac{3.14}{4} \times 400 \times 2$$

$$= 3.14 \times 200 = 628 \text{ cm}^2$$

$$\text{Area of shaded region} = \text{Area of quadrant OPBQ} - \text{Area of square OABC} = 628 - 400 = 228 \text{ cm}^2$$

Hence, the area of the shaded region is 228 cm<sup>2</sup>.

### Question: 40

In the given figure

#### Solution:

Given:

$$AO = OB$$

Perimeter of the figure = 40 cm.....(i)

Let the diameters of semicircles AQO and APB be ' $x_1$ ' and ' $x_2$ ' respectively.

Then, using (1), we have

$$AO = OB$$

$$\text{Also, } AB = AO + OB = AO + AO = 2AO$$

$$\Rightarrow x_2 = 2x_1$$

So, diameter of APB =  $2x_1$

and diameter of AQO =  $x_1$

Radius of APB =  $x_1$

and Radius of AQO =  $\frac{x_1}{2}$  .....(ii)

Perimeter of shaded region = perimeter of AQO + perimeter APB + diameter of APB  
.....(iii)

$\therefore$  Perimeter of semicircle =  $\pi r$

$$\therefore \text{Perimeter of semicircle AQO} = \frac{22}{7} \times \frac{x_1}{2} = \frac{11x_1}{7} \text{ cm}$$

$$\text{Perimeter of semicircle APB} = \frac{22}{7} \times x_1 = \frac{22x_1}{7} \text{ cm}$$

Now, using (iii), we have

$$40 = \frac{11x_1}{7} + \frac{22x_1}{7} + x_1$$

$$40 = \frac{11x_1 + 22x_1 + 7x_1}{7}$$

$$40 \times 7 = 40x_1$$

$$280 = 40x_1$$

$$x_1 = \frac{280}{40} = 7 \text{ cm}$$

$\therefore$  using (ii), we have

Radius of APB = 7 cm =  $r_1$

And Radius of AQO =  $\frac{7}{2}$  cm = 3.5 cm =  $r_2$

Now,

$\therefore$  Area of semicircle =  $\frac{1}{2} \pi r^2$

$\therefore$  Area of semicircle APB =  $\frac{1}{2} \pi r_1^2$

$$= \frac{1}{2} \times \frac{22}{7} \times 7 \times 7 = 11 \times 7 = 77 \text{ cm}^2$$

Similarly,

Area of semicircle APB =  $\frac{1}{2} \pi r_2^2$

$$= \frac{1}{2} \times \frac{22}{7} \times 3.5 \times 3.5 = 19.25 \text{ cm}^2$$

Thus, Area of shaded region = Area of APB + Area of AQO

$$= 77 + 19.25 = 96.25 \text{ cm}^2$$

Hence, the area of the shaded region is 96.25 cm<sup>2</sup>.

**Question: 41**

Find the area of

**Solution:**

Given:

Circumference of circle = 44 cm

Let the radius of the circle be 'r' cm

$\therefore$  Circumference of circle =  $2\pi r$

$$\therefore 44 = 2\pi r$$

$$\frac{44}{2} = \frac{22}{7} \times r$$

$$r = 22 \times \frac{7}{22} = 7 \text{ cm}$$

Now, Area of quadrant =  $\frac{1}{4} \times \pi r^2$

$$= \frac{1}{4} \times \frac{22}{7} \times 7 \times 7$$

$$= \frac{11 \times 7}{2} = \frac{22}{7} = 38.5 \text{ cm}^2$$

Hence, the area of the quadrant is  $38.5 \text{ cm}^2$ .

**Question: 42**

In the given figure

**Solution:**

Given:

Side of square = 14 cm

Let the radius of each circle be 'r' cm

Then,  $2r + 2r = 14 \text{ cm}$

$$4r = 14 \text{ cm}$$

$$r = \frac{14}{4} = \frac{7}{2}$$

Area of square = side  $\times$  side =  $14 \times 14 = 196 \text{ cm}^2$

$\therefore$  Area of circle =  $\pi r^2$

$\therefore$  Area of 4 circles =  $4 \times \pi r^2$

$$= 4 \times \frac{22}{7} \times \frac{7}{2} \times \frac{7}{2}$$

$$= 22 \times 7 = 154 \text{ cm}^2$$

Area of shaded region = Area of the square - Area of 4 circles

$$= 196 - 154$$

$$= 42 \text{ cm}^2$$

Hence, the area of the shaded region is  $42 \text{ cm}^2$ .

**Question: 43**

Find the area of

**Solution:**

Given:

Length of rectangle = 8 cm

Breadth of rectangle = 6 cm

Area of rectangle = length × breadth

$$= 8 \times 6 = 48 \text{ cm}^2$$

Consider  $\triangle ABC$ ,

By Pythagoras theorem,

$$AC^2 = AB^2 + BC^2$$

$$= 8^2 + 6^2 = 64 + 36 = 100$$

$$AC = \sqrt{100} = 10 \text{ cm}$$

$\Rightarrow$  Diameter of circle = 10 cm

$$\text{Thus, radius of circle} = \frac{10}{2} = 5 \text{ cm}$$

Let the radius of circle be  $r = 5 \text{ cm}$

Then, Area of circle =  $\pi r^2$

$$= \frac{22}{7} \times 5 \times 5 = \frac{22 \times 25}{7} = \frac{550}{7} = 78.57 \text{ cm}^2$$

Area of shaded region = Area of circle - Area of rectangle

$$= 78.57 - 48$$

$$= 30.57 \text{ cm}^2$$

Hence, the area of shaded region is  $30.57 \text{ cm}^2$ .

#### Question: 44

A wire is bent to

#### Solution:

Given:

Perimeter of square = Circumference of circle ..... (i)

Area of Square =  $484 \text{ m}^2$

Let the side of square be 'x' cm.

$\therefore$  Area of Square = side × side

$$\therefore 484 = x \times x$$

$$x^2 = 484$$

$$x = \sqrt{484} = 22 \text{ cm}$$

$\therefore$  Perimeter of square =  $4 \times$  side

$$= 4 \times 22 = 88 \text{ cm}$$

$\therefore$  Using (i), we have

Circumference of circle = 88 cm

Also, Circumference of Circle =  $2\pi r$

$$2\pi r = 88$$

$$2 \times \frac{22}{7} \times r = 88$$

$$r = 88 \times \frac{1}{2} \times \frac{7}{22}$$

$$r = 2 \times 7 = 14 \text{ cm}$$

$$\text{Area of Circle} = \pi r^2 = \frac{22}{7} \times 14 \times 14$$

$$= 22 \times 2 \times 14 = 616 \text{ cm}^2$$

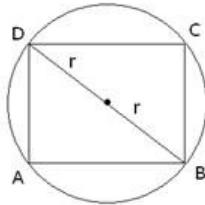
Hence, the area of Circle is  $616 \text{ cm}^2$ .

**Question: 45**

A square ABCD is

**Solution:**

Given: Radius of circle =  $r$



$$\text{Diagonal of Square} = 2r$$

$$\therefore \text{Side of Square} = \frac{\text{length of diagonal}}{\sqrt{2}}$$

$$\therefore \text{Side} = \frac{2r}{\sqrt{2}} = \sqrt{2}r$$

$$\text{Area of Square} = \text{Side} \times \text{Side}$$

$$= \sqrt{2}r \times \sqrt{2}r$$

$$= 2r^2$$

Hence, the area of square is ' $2r^2$ ' square units.

**Question: 46**

The cost of fencing

**Solution:**

Given:

Rate of fencing a circular field = Rs. 25/m

Cost of fencing a circular field = Rs. 5500

Rate of ploughing the field = 50p/m<sup>2</sup> = Rs. 0.5/m<sup>2</sup>

Let the radius of circular field be 'r' and the length of the field fenced be 'x' m.

Then,  $25 \times x = 5500$

$$x = \frac{5500}{25} = 220 \text{ m}$$

$\therefore$  Circumference of circular field =  $2\pi r$

$$\therefore 220 = 2\pi r$$

$$220 = 2 \times \frac{22}{7} \times r$$

$$r = \frac{220 \times 7}{2 \times 22}$$

$$r = 35 \text{ m}$$

Area of the circular field =  $\pi r^2$

$$= \frac{22}{7} \times 35 \times 35$$

$$= 22 \times 5 \times 35$$

$$= 3850 \text{ m}^2$$

Now, cost of ploughing the field = Rate of ploughing the field  $\times$  Area of the field =  $0.5 \times 3850$

$$= \text{Rs. } 1925$$

Hence, the cost of Ploughing the field is Rs. 1925.

**Question: 47**

A park is in the

**Solution:**

Given:

$$\text{Length of the rectangular park} = 120 \text{ m}$$

$$\text{Breadth of the rectangular park} = 90 \text{ m}$$

$$\text{Area of the park excluding the circular lawn} = 2950 \text{ m}^2$$

$$\text{Area of the rectangular park} = \text{length} \times \text{breadth}$$

$$= 120 \times 90$$

$$= 10800 \text{ m}^2$$

$$\text{Area of circular lawn} = \text{Area of rectangular park} - \text{Area of park excluding the lawn}$$

$$= 10800 - 2950$$

$$= 7850 \text{ m}^2$$

$$\therefore \text{Area of circle} = \pi r^2$$

$$\therefore 7850 = 3.14 \times r^2$$

$$r^2 = \frac{7850}{3.14} = 2500$$

$$r = \sqrt{2500} = 50 \text{ m}$$

Hence, the radius of the circular lawn is 50m.

**Question: 48**

In the given figure

**Solution:**

Given:

$$OP = 21 \text{ m} = r_1$$

$$OR = 14 \text{ m} = r_2$$

Let the quadrants made by outer and inner circles be  $Q_1$  and  $Q_2$ , with radius  $r_1$  and  $r_2$  respectively.

Then, Area of flower bed = Area of  $Q_1$  - Area of  $Q_2$

$$\therefore \text{Area of Quadrant} = \frac{1}{4} \pi r^2$$

$$\therefore \text{Area of } Q_1 = \frac{1}{4} \pi r_1^2$$

$$= \frac{1}{4} \times \frac{22}{7} \times 21 \times 21$$

$$= \frac{693}{2} \text{ m}^2$$

$$\text{Similarly, Area of } Q_2 = \frac{1}{4} \pi r_2^2$$

$$= \frac{1}{4} \times \frac{22}{7} \times 14 \times 14$$

$$= \frac{308}{2} \text{ m}^2$$

$$\text{Thus, Area of flower bed} = \frac{693}{2} - \frac{308}{2}$$

$$= \frac{385}{2} = 192.5 \text{ m}^2$$

Hence, the area of the flower bed is 192.5 m<sup>2</sup>.

### Question: 49

In the given figure

#### Solution:

Given:

$$AC = 54 \text{ cm}$$

$$BC = 10 \text{ cm}$$

$$\Rightarrow AB = AC - BC = 54 - 10 = 44 \text{ cm}$$

$$\text{Radius of bigger circle} = \frac{AC}{2} = \frac{54}{2} = 27 \text{ cm} = r_1$$

$$\text{Radius of Smaller circle} = \frac{AB}{2} = \frac{44}{2} = 22 \text{ cm} = r_2$$

$$\therefore \text{Area of Circle} = \pi r^2$$

$$\therefore \text{Area of Bigger Circle} = \pi r_1^2$$

$$= \frac{22}{7} \times 27 \times 27$$

$$= \frac{16038}{7} \text{ cm}^2$$

$$\text{Similarly, Area of Smaller Circle} = \pi r_2^2$$

$$= \frac{22}{7} \times 22 \times 22$$

$$= \frac{10648}{7} \text{ cm}^2$$

$$\text{Area of shaded region} = \text{Area of Bigger Circle} - \text{Area of Smaller Circle} = \frac{16038}{7} - \frac{10648}{7} = \frac{5390}{7} = 770 \text{ cm}^2$$

Hence, Area of Shaded Region is 770 cm<sup>2</sup>.

### Question: 50

From a thin metal

#### Solution:

Given:

$$AB \parallel CD$$

$$\angle BCD = 90^\circ$$

$$AB = BC = 3.5 \text{ cm} = EC$$

$$DE = 2 \text{ cm}$$

$$DC = DE + EC = 2 + 3.5 = 5.5 \text{ cm}$$

$$\text{Area of Trapezium} = \frac{1}{2} \times \text{Sum of Parallel Sides} \times h$$

$$= \frac{1}{2} \times (AB + DC) \times BC$$

$$= \frac{1}{2} \times (3.5 + 5.5) \times 3.5$$

$$= \frac{1}{2} \times 9 \times 3.5$$

$$= 15.75 \text{ cm}^2$$

$$\text{Area of Quadrant BFEC} = \frac{1}{4} \times \pi r^2 = \frac{1}{4} \times \frac{22}{7} \times 3.5 \times 3.5$$

$$= 9.625 \text{ cm}^2$$

Thus, Area of remaining part of metal sheet

$$= \text{Area of Trapezium} - \text{Area of Quadrant BFEC}$$

$$= 15.75 - 9.625 = 6.125 \text{ cm}^2$$

Hence, the area of the remaining part of metal sheet is 6.125 cm<sup>2</sup>.

### Question: 51

Find the area of

#### Solution:

Given:

Radius of Circle = 35 cm

$\angle AOB = 90^\circ$

$$\therefore \text{Area of Sector} = \frac{\theta}{360^\circ} \times \pi r^2$$

$$= \frac{90}{360} \times \frac{22}{7} \times 35 \times 35$$

$$= \frac{1925}{2} \text{ cm}^2$$

$\because \Delta AOB$  is right-angled triangle.

$$\therefore \text{Area of } \Delta AOB = \frac{1}{2} \times OA \times OB$$

$$= \frac{1}{2} \times 35 \times 35$$

$$= \frac{1225}{2} \text{ cm}^2$$

Now, Area of Minor Segment ACB

$$= \text{Area of Sector} - \text{Area of } \Delta AOB$$

$$= \frac{1925}{2} - \frac{1225}{2} = \frac{700}{2} = 350 \text{ cm}^2$$

Area of Circle =  $\pi r^2$

$$= \frac{22}{7} \times 35 \times 35$$

$$= 22 \times 5 \times 35$$

$$= 3850 \text{ cm}^2$$

Thus, Area of Major Segment = Area of Circle - Area of Minor Segment =  $3850 - 350 = 3500 \text{ cm}^2$

Hence, the area of the major segment is 3500 cm<sup>2</sup>.

## Exercise : 18B

### Question: 1

The circumference

**Solution:**

In order to solve such type of questions we basically need to find the radius of the give circle and simply use it to find the area of the given circle.

Given the circumference or perimeter of the circle = 39.6 cm.

And we know, Perimeter or circumference of circle =  $2\pi r$

Where,  $r$  = Radius of the circle

Therefore,  $2\pi r = 39.6$

$$\Rightarrow r = \frac{39.6}{2\pi}$$

(put value of  $\pi = 22/7$ )

$$\Rightarrow r = \frac{39.6}{2 \times \frac{22}{7}}$$

On rearranging we get,

$$\Rightarrow r = \frac{39.6 \times 7}{2 \times 22}$$

$$\Rightarrow r = \frac{277.2}{44}$$

$$\Rightarrow r = 6.3 \text{ cm}$$

So, the radius of the circle = 6.3 cm

And we also know, Area of the circle =  $\pi r^2$

Where,  $r$  = radius of the circle

$$\Rightarrow \text{Area of the circle} = \pi(6.3)^2$$

(putting value of  $r$ )

$$= \frac{22}{7}(6.3^2)$$

$$= \frac{22}{7}(6.3 \times 6.3)$$

$$= \frac{22}{7} \times 39.69$$

$$= 22 \times 5.67$$

$$= 124.74 \text{ cm}^2$$

The area of the circle = 124.74 cm<sup>2</sup>.

**Question: 2**

In order to solve such type of questions we basically need to find the radius of the give circle and simply use it to find the are circumference or perimeter of the given circle.

Given the area of the circle = 98.56 cm<sup>2</sup>

And we also know, Area of the circle =  $\pi r^2$

Therefore,  $\pi r^2 = 98.56$

$$\Rightarrow r^2 = \frac{98.56}{\pi}$$

(put value of  $\pi = 22/7$ )

$$\Rightarrow r^2 = \frac{98.56}{\frac{22}{7}}$$

On rearranging we get,

$$\Rightarrow r^2 = \frac{98.56 \times 7}{22}$$

$$\Rightarrow r^2 = \frac{689.92}{22}$$

$$\Rightarrow r^2 = 31.36$$

$$\Rightarrow r = \sqrt{31.36}$$

$$\Rightarrow r = 5.6 \text{ cm}$$

So, the radius of the circle = 5.6 cm

And we know, Perimeter of circle =  $2\pi r$

(put value of r)

$$\Rightarrow \text{Circumference or Perimeter of circle} = 2\pi(5.6)$$

$$= 2 \times \frac{22}{7} \times 5.6 \text{ (put } \pi = \frac{22}{7})$$

$$= \frac{2 \times 22 \times 5.6}{7}$$

$$= \frac{246.4}{7}$$

$$= 35.2 \text{ cm}$$

The circumference or perimeter of the circle is 35.2 cm

### Question: 3

Given, the circumference of a circle exceeds its diameter by 45 cm.

$$\Rightarrow \text{Circumference of circle} = \text{Diameter of circle} + 45$$

Let 'd' = diameter of the circle

$$\Rightarrow \text{Circumference} = d + 45 \rightarrow \text{eqn1}$$

And we know, Circumference of a circle =  $2\pi r \rightarrow \text{eqn2}$

Where  $r$  = radius of circle

Also, we know that the radius of the circle is half of its diameter.

$$\Rightarrow r = \frac{d}{2} \rightarrow \text{eqn3}$$

Put value of circumference in equation 1 from equation 2

$$\Rightarrow 2\pi r = d + 45 \rightarrow \text{eqn4}$$

Put value of  $r$  in equation 4 from equation 3

$$\Rightarrow 2\pi \left(\frac{d}{2}\right) = d + 45$$

$$\Rightarrow \pi d = d + 45$$

$$\Rightarrow \pi d - d = 45$$

$$\Rightarrow (\pi - 1)d = 45 \text{ (taking } d \text{ common from L.H.S)}$$

$$\Rightarrow d = \frac{45}{\pi - 1} \text{ (now put } \pi = \frac{22}{7})$$

$$\Rightarrow d = \frac{45}{\frac{22}{7} - 1}$$

$$\Rightarrow d = \frac{45}{\frac{22-7}{7}} \text{ (taking 7 as LCM in denominator)}$$

$$\Rightarrow d = \frac{45}{\frac{15}{7}}$$

On rearranging, we get

$$\Rightarrow d = \frac{45 \times 7}{15}$$

$$\Rightarrow d = \frac{315}{15}$$

$$\Rightarrow d = 21 \text{ cm}$$

Therefore, the diameter of the circle is 21 cm.

Thus, the radius of the circle  $r = \frac{d}{2}$  (from equation 3)

$$\therefore r = \frac{21}{2}$$

$$\Rightarrow r = 10.5 \text{ cm}$$

Now put the value of  $r$  in equation 2, we get

$$\Rightarrow \text{Circumference or Perimeter of circle} = 2\pi(10.5) \text{ (put } \pi = \frac{22}{7})$$

$$= 2 \times \frac{22}{7} \times 10.5$$

$$= \frac{2 \times 22 \times 10.5}{7}$$

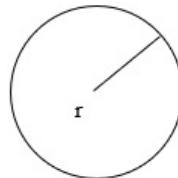
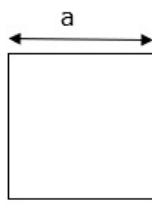
$$= \frac{462}{7}$$

$$= 66 \text{ cm}$$

The circumference of the circle is 66 cm.

#### Question: 4

In this question the wire is first bent in the shape of square and then same wire is bent to form a circle. The point to be noticed is that the same wire is used both the times which implies that the perimeter of square and that of circle will be equal.



Let the square be of side 'a' cm and radius of the circle be 'r'

Given the area enclosed by the square =  $484 \text{ cm}^2$

Also, we know that Area of square = Side  $\times$  Side

Area of the square =  $a^2$

$$\Rightarrow a^2 = 484$$

$$\Rightarrow a = \sqrt{484}$$

$$\Rightarrow a = 22 \text{ cm}$$

Therefore, side of square, 'a' is 22 cm.

Also, circumference of the circle = Perimeter of square  $\rightarrow$  eqn1

Perimeter of square =  $4 \times$  side

Perimeter of square =  $4 \times 22$

$\Rightarrow$  Perimeter of square = 88 cm  $\rightarrow$  eqn2

Also, we know, Circumference of circle =  $2\pi r \rightarrow$  eqn3

Put values in equation 1 from equation 2 & 3, we get

$$2\pi r = 88$$

$$\Rightarrow r = \frac{88}{2\pi} \text{ (put } \pi = \frac{22}{7} \text{)}$$

$$\Rightarrow r = \frac{88}{2 \times \frac{22}{7}}$$

On rearranging,

$$\Rightarrow r = \frac{88 \times 7}{2 \times 22}$$

$$\Rightarrow r = \frac{616}{44}$$

$$\Rightarrow r = 14 \text{ cm}$$

So, the radius 'r' of the circle is 14 cm.

$$\text{Area of circle} = \pi r^2$$

Where  $r$  = radius of the circle

$$= \pi(14^2)$$

$$= \frac{22}{7} \times 14 \times 14 \text{ (put } \pi = \frac{22}{7} \text{)}$$

$$= \frac{22 \times 14 \times 14}{7}$$

$$= 4312/7$$

$$= 616 \text{ cm}^2$$

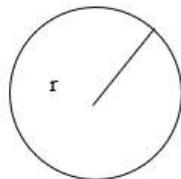
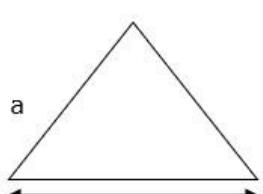
Area of the circle is  $616 \text{ cm}^2$ .

### Question: 5

A wire when

#### Solution:

In this question the wire is first bent in the shape of equilateral triangle and then same wire is bent to form a circle. The point to be noticed is that the same wire is used both the times which implies that the **perimeter of equilateral triangle and that of circle will be equal**.



Let the equilateral triangle be of side 'a' cm and radius of the circle be 'r'.

Given: Area enclosed by equilateral triangle =  $123\sqrt{3}$  cm<sup>2</sup>

Also, we know that Area of equilateral triangle =  $\frac{\sqrt{3}}{4}a^2$

Where 'a' = side of equilateral triangle

$$\Rightarrow \frac{\sqrt{3}}{4}a^2 = 123\sqrt{3}$$

$$\Rightarrow a^2 = \frac{123\sqrt{3} \times 4}{\sqrt{3}}$$

$$\Rightarrow a^2 = \frac{484\sqrt{3}}{\sqrt{3}}$$

$$\Rightarrow a = \sqrt{484}$$

$$\Rightarrow a = 22 \text{ cm}$$

Therefore, side of equilateral triangle, 'a' is 22 cm.

Also, circumference of the circle = Perimeter of equilateral triangle  $\rightarrow$  eqn1

Perimeter of equilateral triangle =  $3 \times$  side

$$= 3 \times 22$$

$$= 66 \text{ cm} \rightarrow \text{eqn2}$$

Also, we know Circumference of circle =  $2\pi r \rightarrow$  eqn3

Put values in equation 1 from equation 2 & 3, we get

$$2\pi r = 66$$

$$\Rightarrow r = \frac{66}{2\pi}$$

(put  $\pi = 22/7$ )

$$\Rightarrow r = \frac{66}{2 \times \frac{22}{7}}$$

On rearranging,

$$\Rightarrow r = \frac{66 \times 7}{2 \times 22}$$

$$\Rightarrow r = \frac{462}{44}$$

$$\Rightarrow r = 10.5 \text{ cm}$$

So, the radius 'r' of the circle is 10.5 cm.

Area of circle =  $\pi r^2$

Where  $r$  = radius of the circle

$$\Rightarrow \text{Area of circle} = \pi(10.5^2)$$

$$\Rightarrow \text{Area of circle} = \frac{22}{7} \times 10.5 \times 10.5 \text{ (put } \pi = \frac{22}{7})$$

$$= \frac{22 \times 10.5 \times 10.5}{7}$$

$$= \frac{2425.5}{7}$$

$$= 346.5 \text{ cm}^2$$

**Area of the circle is 346.5 cm<sup>2</sup>.**

### Question: 6

In this question the length of chain used as boundary of the semicircular park is the perimeter of the semicircular park. By using this we will first calculate the radius of the semicircular park and then area of semicircle consequently.

Length of chain = 108 m

Length of chain = Perimeter or circumference of semicircle

Therefore, Circumference or Perimeter of semicircle = 108 m

Also, Circumference or Perimeter of semicircle =  $\pi r$

Where  $r$  = radius of semicircle

$$\Rightarrow \pi r = 108$$

$$\Rightarrow r = \frac{108}{\pi}$$

(put  $\pi = 22/7$ )

$$\Rightarrow r = \frac{\frac{108}{22}}{7}$$

On rearranging,

$$\Rightarrow r = \frac{108 \times 7}{22}$$

$$\Rightarrow r = \frac{756}{22}$$

$$\Rightarrow r = 34.46 \text{ m}$$

Therefore, radius of semicircle is 34.36 m

As, Area of semicircle =  $\frac{\pi r^2}{2} \rightarrow \text{eqn1}$

Put value of 'r' in equation 1, we get

$$\text{Area of semicircle} = \frac{\pi(34.36^2)}{2}$$

(put  $\pi = 22/7$ )

$$= \frac{\frac{22}{7} \times 34.36 \times 34.36}{2}$$

On rearranging,

$$= \frac{22 \times 34.36 \times 34.36}{7 \times 2}$$

$$= \frac{25973.4112}{14}$$

$$= 1855.63 \text{ m}^2$$

The area of the semicircular park is 1855.63 m<sup>2</sup>.

**Question: 7**

Given Sum of the radius of the circles = 7 cm

the difference of their circumference = 8 cm

Let the radius one circle be ' $r_1$ ' cm and other be ' $r_2$ ' cm and circumference be ' $C_1$ ' and ' $C_2$ ' respectively.

Also, circumference of circle =  $2\pi r$

Where  $r$  = radius of the circle

$$C_1 = 2\pi r_1 \text{ and } C_2 = 2\pi r_2$$

$$r_1 + r_2 = 7 \rightarrow \text{eqn1}$$

$$C_1 - C_2 = 8 \rightarrow \text{eqn2}$$

(Note: Here it is considered that  $r_1 > r_2$ )

We can rewrite equation 2 as,

$$2\pi r_1 - 2\pi r_2 = 8$$

$$\Rightarrow 2\pi(r_1 - r_2) = 8$$

(taking  $2\pi$  common from L.H.S)

$$\Rightarrow r_1 - r_2 = \frac{8}{2\pi} \rightarrow \text{eqn3}$$

$$\Rightarrow r_1 - r_2 = \frac{8}{2 \times \frac{22}{7}}$$

$$\Rightarrow r_1 - r_2 = \frac{8 \times 7}{44}$$

$$\Rightarrow r_1 - r_2 = \frac{56}{44}$$

$$\Rightarrow r_1 - r_2 = \frac{14}{11}$$

$$\Rightarrow r_1 = \frac{14}{11} + r_2 \rightarrow \text{eqn3}$$

Put the value of  $r_1$  from equation 3 in equation 1

$$\frac{14}{11} + r_2 + r_2 = 7$$

$$\Rightarrow \frac{14}{11} + 2r_2 = 7$$

$$\Rightarrow 2r_2 = 7 - \frac{14}{11}$$

$$\Rightarrow 2r_2 = \frac{77 - 14}{11}$$

(taking 11 as LCM on R.H.S)

$$\Rightarrow 2r_2 = \frac{63}{11}$$

$$\Rightarrow r_2 = \frac{63}{2 \times 11}$$

$$\Rightarrow r_2 = \frac{63}{22} \text{ cm}$$

Put value of  $r_2$  in equation 3

$$\therefore r_1 = \frac{14}{11} + \frac{63}{22} \text{ (from equation 3)}$$

$$\Rightarrow r_1 = \frac{28+63}{22} \text{ (taking 22 as LCM on R.H.S)}$$

$$\Rightarrow r_1 = \frac{91}{22} \text{ cm}$$

$$\therefore C_1 = 2\pi \left( \frac{91}{22} \right)$$

(by putting value of  $r_1$ )

$$\Rightarrow C_1 = 2 \times \frac{22}{7} \times \frac{91}{22}$$

$$= \frac{2 \times 22 \times 91}{7 \times 22}$$

$$= \frac{2 \times 91}{7}$$

$$= 182/7$$

$$= 26 \text{ cm}$$

$$C_2 = 2\pi \left( \frac{63}{22} \right) \text{ (by putting value of } r_2)$$

$$\Rightarrow C_1 = 2 \times \frac{22}{7} \times \frac{63}{22}$$

$$= \frac{2 \times 22 \times 63}{7 \times 22}$$

$$= \frac{2 \times 63}{7}$$

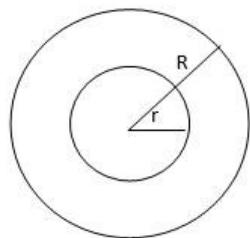
$$= 126/7$$

$$= 18 \text{ cm}$$

The circumference of circles are 26 cm and 18 cm.

### Question: 8

Consider the ring as shown in the figure below,



The inner radius of ring is ' $r$ ' and the outer radius is ' $R$ '.

$$\text{Area of inner Circle} = \pi r^2 \text{ and Area of outer Circle} = \pi R^2$$

$$\text{Where } r = 12 \text{ cm and } R = 23 \text{ cm}$$

$$\text{Area of ring} = \text{Area of outer circle} - \text{Area of inner circle}$$

$$\text{Area of ring} = \pi R^2 - \pi r^2 \text{ (put values of } r \text{ & } R)$$

$$\Rightarrow \text{Area of ring} = \pi(23^2) - \pi(12^2)$$

$$\Rightarrow \text{Area of ring} = \pi(23^2 - 12^2) \text{ (taking } \pi \text{ common from R.H.S)}$$

$$\Rightarrow \text{Area of ring} = \pi(529 - 144)$$

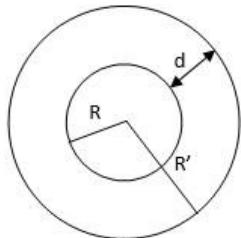
$$= \frac{22 \times 385}{7}$$

$$= \frac{8470}{7}$$

$$= 1210 \text{ cm}^2$$

Area of ring is  $1210 \text{ cm}^2$ .

**Question: 9**



Given radius of circular park =  $R = 17 \text{ m}$

Width of the circular path outside the park =  $d = 8 \text{ m}$

Therefore, the radius of the outer circle =  $R' = R + d$

Outer radius =  $R' = 17 + 8$

$R' = 25 \text{ m}$

Area of inner circle =  $\pi R^2$  and,

Area of outer circle =  $\pi R'^2$

Area of path = Area of outer circle - Area of inner circle

$$= \pi R'^2 - \pi R^2 \text{ (put values of } R' \text{ & } R\text{)}$$

$$= \pi(25^2) - \pi(17^2)$$

$$= \pi(25^2 - 17^2) \text{ (taking } \pi \text{ common from R.H.S)}$$

$$= \pi(625 - 289)$$

$$\Rightarrow \text{Area of path} = \frac{22}{7} \times 336$$

(put  $\pi = 22/7$ )

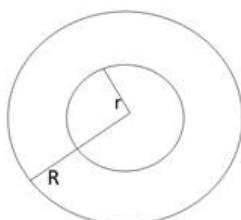
$$= 7392/7$$

$$= 1056 \text{ m}^2$$

The area of the path is  $1056 \text{ m}^2$ .

**Question: 10**

Consider the race track as shown below,



The inner and outer radius of track is ' $r$ ' cm and ' $R$ ' cm respectively.

Let inner and outer circumference be ' $C_1$ ' and ' $C_2$ ' respectively.

$C_1 = 352 \text{ m}$  and  $C_2 = 396 \text{ m}$ .

We know,

$$\text{Circumference of circle} = 2\pi r$$

Where  $r$  = radius of the circle

$$C_1 = 2\pi r \text{ and } C_2 = 2\pi R$$

$$\Rightarrow 2\pi r = 352 \text{ and } 2\pi R = 396$$

$$\Rightarrow r = \frac{352}{2\pi} \text{ and } R = \frac{396}{2\pi} \left(\text{put } \pi = \frac{22}{7}\right)$$

$$\Rightarrow r = \frac{352}{2 \times \frac{22}{7}} \text{ and } R = \frac{396}{2 \times \frac{22}{7}}$$

On rearranging,

$$\Rightarrow r = \frac{352 \times 7}{2 \times 22} \text{ and } R = \frac{396 \times 7}{2 \times 22}$$

$$\Rightarrow r = \frac{2464}{44} \text{ and } R = \frac{2772}{44}$$

$$\Rightarrow r = 56 \text{ m and } R = 63 \text{ m}$$

So, the width of the race track =  $R - r$ ,

$$\Rightarrow \text{Width of the race track} = 63 - 56$$

$$\Rightarrow \text{Width of the race track} = 7 \text{ m}$$

Area of race track = area of outer circle - area of inner circle

$$\Rightarrow \text{Area of track} = \pi R^2 - \pi r^2 \text{ (put values of } r \text{ and } R\text{)}$$

$$\Rightarrow \text{Area of track} = \pi(63^2) - \pi(56^2)$$

$$\Rightarrow \text{Area of track} = \pi(63^2 - 56^2) \text{ (taking } \pi \text{ common from R.H.S)}$$

$$\Rightarrow \text{Area of track} = \pi(3969 - 3136)$$

$$\Rightarrow \text{Area of track} = \pi \times 833$$

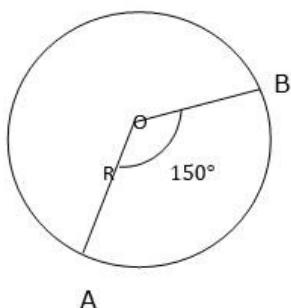
$$\Rightarrow \text{Area of track} = \frac{22}{7} \times 833 \text{ (put } \pi = \frac{22}{7}\text{)}$$

$$= 22 \times 119$$

$$= 2618 \text{ m}^2$$

The width of track is 7 m and area of track is  $2618 \text{ m}^2$ .

**Question: 11**



Consider the circle shown above,

Given radius of the circle =  $R = 21 \text{ cm} \rightarrow \text{eqn1}$

And angle of the sector =  $\theta = 150^\circ \rightarrow \text{eqn2}$

$$\text{Length of arc of a sector} = \frac{\theta}{360} \times 2\pi R \rightarrow \text{eqn3}$$

Where 'R' = radius of sector (or circle)

$\theta$  = angle subtended by the arc on the centre of the circle

Put the values of R and  $\theta$  from equation 1 and 2 in equation 3

$$\Rightarrow \text{Length of arc} = \frac{150}{360} \times 2\pi(21) \text{ (put } \pi = \frac{22}{7})$$

$$= \frac{150}{360} \times 2 \times \frac{22}{7} \times 21$$

$$= \frac{150 \times 2 \times 22 \times 21}{360 \times 7}$$

$$= 138600/2520$$

$$= 55 \text{ cm}$$

$$\text{Area of a sector} = \frac{\theta}{360} \times \pi R^2 \rightarrow \text{eqn4}$$

Where 'R' = radius of sector (or circle)

$\theta$  = angle subtended by the arc on the centre of the circle

Put the values of R and  $\theta$  from equation 1 and 2 in equation 3

$$\Rightarrow \text{Area of sector} = \frac{150}{360} \times \pi(21^2) \text{ (put } \pi = \frac{22}{7})$$

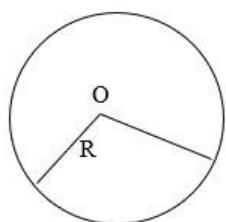
$$= \frac{150 \times 22 \times 21 \times 21}{360 \times 7}$$

$$= 1455300/2520$$

$$= 577.5 \text{ cm}^2$$

The length of arc is 55 cm and area of sector is 577.5 cm<sup>2</sup>.

### Question: 12



Consider the circle shown above,

$$\text{We know, Area of sector} = \frac{\theta}{360} \times \pi R^2 \rightarrow \text{eqn1}$$

Where R = radius of the circle and  $\theta$  = central angle

Given R = 10.5 cm and Area of sector = 69.3 cm<sup>2</sup>

Let the angle subtended at centre =  $\theta$

Put the values of R and area of sector in equation 1

$$\Rightarrow 69.3 = \frac{\theta}{360} \times \pi(10.5^2) \text{ (put } \pi = \frac{22}{7})$$

$$\Rightarrow 69.3 = \frac{\theta}{360} \times \frac{22}{7} \times 10.5 \times 10.5$$

$$\Rightarrow 69.3 = \frac{\theta \times 22 \times 10.5 \times 10.5}{360 \times 7}$$

$$\Rightarrow 69.3 = \frac{\theta \times 2425.5}{2520}$$

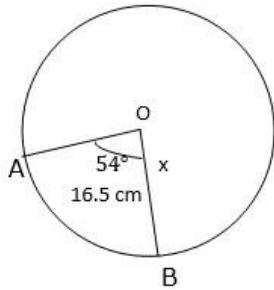
$$\Rightarrow \frac{69.3 \times 2520}{2425.5} = \theta$$

$$\Rightarrow \frac{174636}{2425.5} = \theta$$

$$\Rightarrow \theta = 72^\circ$$

The central angle of the sector is  $72^\circ$ .

### Question: 13



Consider the Circle shown above,

$$\text{We know, Length of arc of sector} = \frac{\theta}{360} \times 2\pi R \rightarrow \text{eqn1}$$

Where  $R$  = radius of circle and  $\theta$  = central angle of the sector

Given, Length of arc =  $l = 16.5$  cm and  $\theta = 54^\circ$ . Let the radius be  $x$  cm

Put the values of  $l$  and  $\theta$  in equation 1

$$\Rightarrow 16.5 = \frac{54}{360} \times 2\pi x \left(\text{put } \pi = \frac{22}{7}\right)$$

$$\Rightarrow 16.5 = \frac{54 \times 2 \times 22 \times x}{360 \times 7}$$

$$\Rightarrow 16.5 = \frac{2376 \times x}{2520}$$

On rearranging

$$\Rightarrow \frac{16.5 \times 2520}{2376} = x$$

$$\Rightarrow \frac{41580}{2376} = x$$

$$\Rightarrow x = 17.5 \text{ cm}$$

Also, we know circumference of the circle =  $2\pi R$

$\Rightarrow$  Circumference of the circle =  $2\pi x$  (put value of  $x$  in this equation)

$\Rightarrow$  Circumference of the circle =  $2\pi(17.5)$

$$\Rightarrow \text{Circumference of the circle} = 2 \times \frac{22}{7} \times 17.5 \left(\text{put } \pi = \frac{22}{7}\right)$$

$$= \frac{2 \times 22 \times 17.5}{7}$$

$$= \frac{770}{7}$$

$\Rightarrow$  Circumference of the circle = 110 cm

Also, we know Area of the circle =  $\pi R^2$

$$\Rightarrow \text{Area of the circle} = \pi r^2$$

$$\Rightarrow \text{Area of the circle} = \pi(17.5^2)$$

$$\Rightarrow \text{Area of the circle} = \frac{22}{7} \times 17.5 \times 17.5 \text{ (put } \pi = \frac{22}{7})$$

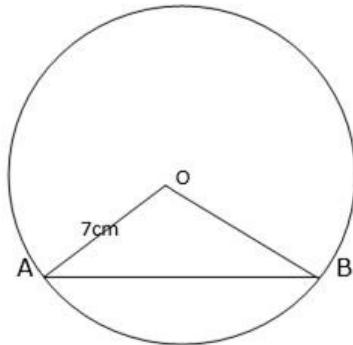
$$\Rightarrow \text{Area of the circle} = \frac{22 \times 17.5 \times 17.5}{7}$$

$$\Rightarrow \text{Area of the circle} = \frac{6737.5}{7}$$

$$\Rightarrow \text{Area of the circle} = 962.5 \text{ cm}^2$$

The radius of circle is 17.5 cm, circumference is 110 cm and area is 962.5 cm<sup>2</sup>

#### Question: 14



Consider the above figure,

From here we can conclude that the portion or the segment below the chord AB is the minor segment and the segment above AB is major segment.

Also we know,

$$\text{Area of minor segment} = \text{Area of sector} - \text{Area of } \triangle AOB \rightarrow \text{eqn1}$$

$$\text{Now, Area of sector} = \frac{\theta}{360} \times \pi R^2 \rightarrow \text{eqn2}$$

Where R = radius of the circle and  $\theta$  = central angle of the sector

Given, R = 7 cm and  $\theta = 90^\circ$

Putting these values in the equation 2, we get

$$\text{Area of sector} = \frac{90}{360} \times \pi(7^2) \text{ (put } \pi = \frac{22}{7})$$

$$= \frac{90}{360} \times \frac{22}{7} \times 7 \times 7$$

$$= \frac{90 \times 22 \times 7 \times 7}{360 \times 7}$$

$$= \frac{97020}{2520}$$

$$\Rightarrow \text{Area of sector} = 38.5 \text{ cm}^2 \rightarrow \text{eqn3}$$

$$\text{Area of } \triangle AOB = \frac{1}{2} \times \text{base} \times \text{height}$$

$$\text{NOTE : In general Area of } \triangle AOB = \frac{1}{2} \times OA \times OB \times \sin \theta$$

As triangle is isosceles therefore height and base both are 7 cm.

$$\Rightarrow \text{Area of } \triangle AOB = \frac{1}{2} \times 7 \times 7 = \frac{49}{2}$$

$$= 24.5 \text{ cm}^2 \rightarrow \text{eqn4}$$

Putting values of equation 2 and 4 in equation 1 we get

$$\text{Area of minor segment} = 38.5 - 24.5$$

$$\Rightarrow \text{Area of minor segment} = 14 \text{ cm}^2$$

$$\text{Area of major segment} = \pi R^2 - \text{Area of minor segment} \rightarrow \text{eqn5}$$

Put the value of R, and Area of minor segment in equation 5

$$= \pi(7^2) - 14$$

$$= 49\pi - 14$$

$$\Rightarrow \text{Area of major segment} = \frac{22}{7} \times 49 - 14 \left(\text{put } \pi = \frac{22}{7}\right)$$

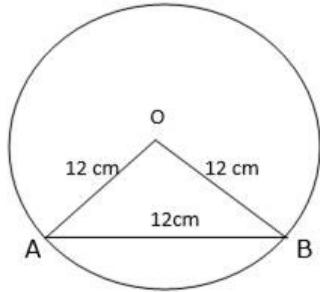
$$= (22 \times 7) - 14$$

$$= 154 - 14$$

$$= 140 \text{ cm}^2$$

Area of minor segment is  $14 \text{ cm}^2$  and of major segment is  $140 \text{ cm}^2$ .

### Question: 15



Consider the figure shown above.

In this, the triangle AOB is an equilateral triangle as all the sides are equal; therefore, it is obvious that the central angle of the sector is 60 degrees. Now by simply applying the formula of length of an arc, we can easily calculate the length of arc of the sector AOB.

Given Radius of circle =  $R = 12 \text{ cm}$ ,

Length of chord AB =  $12 \text{ cm}$

$\therefore$  Central angle =  $\theta = 60^\circ$  ( $\because \triangle AOB$  is an equilateral triangle)

$$\text{Length of arc} = \frac{\theta}{360} \times 2\pi(R) \rightarrow \text{eqn1}$$

Where  $R$  = radius of the circle and  $\theta$  = central angle of the sector

Put the values of  $R$  and  $\theta$  in equation 1

$$\Rightarrow \text{Length of minor arc} = \frac{60}{360} \times 2\pi(12) \left(\text{put } \pi = 3.14\right)$$

$$= \frac{60}{360} \times 2 \times 3.14 \times 12$$

$$= \frac{60 \times 2 \times 3.14 \times 12}{360}$$

$$= \frac{2 \times 3.14 \times 12}{6}$$

$$= 2 \times 3.14 \times 2$$

$$= 12.56 \text{ cm}$$

Now, Length of major arc =  $2\pi R$  - Length of minor arc

$$\Rightarrow \text{Length of major arc} = 2\pi(12) - 12.56 \text{ (put } \pi = 3.14)$$

$$\Rightarrow \text{Length of major arc} = (2 \times 3.14 \times 12) - 12.56$$

$$\Rightarrow \text{Length of major arc} = 75.36 - 12.56$$

$$\Rightarrow \text{Length of major arc} = 62.8 \text{ cm}$$

Now, Area of minor segment = Area of sector - Area of triangle  $\rightarrow$  eqn1

$$\therefore \text{Area pf sector} = \frac{\theta}{360} \times \pi R^2 \text{ (put the values of } R \text{ and } \theta)$$

$$= \frac{60}{360} \times \pi(12^2)$$

$$= \frac{60}{360} \times 3.14 \times 144$$

$$= 75.36 \text{ cm}^2 \rightarrow \text{eqn2}$$

$$\text{Area of triangle} = \frac{\sqrt{3}}{4} \times a^2 \text{ (put } a = 12 \text{ cm)}$$

$$= \frac{\sqrt{3}}{4} \times (12^2)$$

$$\Rightarrow \text{Area of triangle} = \frac{\sqrt{3}}{4} \times 144$$

$$\Rightarrow \text{Area of triangle} = 1.73 \times 36$$

$$\Rightarrow \text{Area of triangle} = 62.28 \text{ cm}^2 \rightarrow \text{eqn3}$$

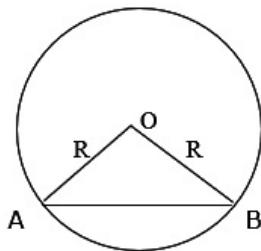
Put the values of equation 2 and 3 in equation 1,

$$\therefore \text{Area of minor segment} = 75.36 - 62.28$$

$$= 13.08 \text{ cm}^2$$

Length of major arc is 62.8 cm and of minor arc is 12.56 cm and area of minor segment is 13.08 cm<sup>2</sup>.

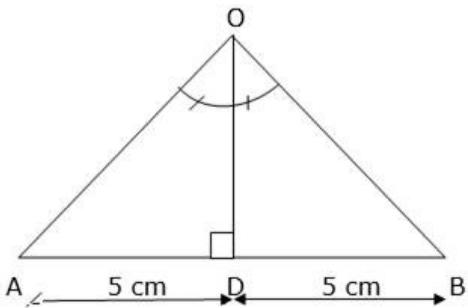
### Question: 16



Consider the figure shown above.

In this, the triangle AOB is an isosceles triangle. So here we will construct a perpendicular bisector from O on AB and as this triangle is isosceles therefore this perpendicular will also act as median and angle bisector.

Therefore,



Draw a perpendicular bisector from O which meets AB at D and bisects AB, as ABO is an isosceles triangle therefore OD acts as a median.

So, consider right angle triangle AOD right angled at D

$$\sin \theta = \frac{\text{Perpendicular}}{\text{Hypotenuse}}$$

Let  $\angle AOD = \theta \Rightarrow \text{Perpendicular} = AD \text{ and Hypotenuse} = AO = R$

Given Radius of circle =  $R = 5\sqrt{2}$  cm

Length of chord AB = 10 cm, AD = 5 cm

$$\sin \theta = \frac{AD}{AO} \text{ (put values of AD and AO)}$$

$$\Rightarrow \sin \theta = \frac{5}{5\sqrt{2}} = \frac{1}{\sqrt{2}}$$

$$\Rightarrow \sin \theta = \sin 45^\circ$$

$$(\text{as } \sin 45^\circ = \frac{1}{\sqrt{2}})$$

$$\Rightarrow \theta = 45^\circ$$

$$\therefore \angle AOD = 45^\circ$$

Thus we can say  $\angle AOB = 90^\circ$  (As  $\angle AOD = \frac{1}{2}\angle AOB$ )

Area of minor segment = Area of sector - Area of right angle triangle

$\rightarrow$  eqn1

$$\text{Area of sector} = \frac{\theta}{360} \times \pi R^2$$

Where R = radius of the circle and  $\theta$  = central angle of the sector

$$\text{Area of sector} = \frac{90}{360} \times \pi ((5\sqrt{2})^2) \text{ (put } \pi = 3.14)$$

$$= \frac{90}{360} \times 3.14 \times 50$$

$$= \frac{3.14 \times 50}{4}$$

$$\therefore \text{Area of sector} = 39.25 \text{ cm}^2$$

Area of right angle triangle =  $1/2 \times \text{base} \times \text{height}$

As this is isosceles right-angle triangle

$$\therefore \text{height} = \text{base} = 5\sqrt{2} \text{ cm}$$

$$\text{Area of right angle triangle} = 1/2 \times 5\sqrt{2} \times 5\sqrt{2} = \frac{50}{2} = 25 \text{ cm}^2$$

Put the value of area of sector and area of right angle triangle in equation 1,

$$\Rightarrow \text{Area of minor segment} = 39.25 - 25$$

$$= 14.25 \text{ cm}^2$$

$$\text{Area of major segment} = \pi R^2 - \text{area of minor segment}$$

$$\text{Area of major segment} = \pi((5\sqrt{2})^2) - 14.25$$

$$= 3.14 \times 5\sqrt{2} \times 5\sqrt{2} - 14.25$$

$$\Rightarrow \text{Area of major segment} = 157 - 14.25 = 142.75 \text{ cm}^2$$

Area of major segment is  $142.75 \text{ cm}^2$  and of minor segment is  $14.25 \text{ cm}^2$ .

### Question: 17

Given  $R = 42 \text{ cm}$  and central angle of sector  $= 120^\circ$

Area of minor segment = Area of sector - Area of triangle  $\rightarrow$  eqn1

$$\text{Area of sector} = \frac{\theta}{360} \times \pi R^2$$

Where  $R$  = radius of the circle and  $\theta$  = central angle of the sector

$$\text{Area of sector} = \frac{120}{360} \times \pi(42^2) \quad (\text{put } \pi = \frac{22}{7})$$

$$= \frac{120}{360} \times \frac{22}{7} \times 1764$$

$$\therefore \text{Area of sector} = 1848 \text{ cm}^2$$

Area of right angle triangle  $= \frac{1}{2} \times \text{base} \times \text{height} \times \sin \theta$

Where  $\theta$  = central angle of the sector

$$\text{Area of triangle} = \frac{1}{2} \times 42 \times 42 \times \sin 120^\circ$$

$$(\text{put the value } \sin 120^\circ = \frac{\sqrt{3}}{2})$$

$$\text{Area of triangle} = \frac{1}{2} \times 42 \times 42 \times \frac{\sqrt{3}}{2}$$

$$\text{Area of triangle} = (42 \times 42 \times \sqrt{3})/4$$

$$(\text{put } \sqrt{3} = 1.73)$$

$$\text{Area of triangle} = \frac{42 \times 42 \times 1.73}{4}$$

$$= 762.93 \text{ cm}^2$$

Put the values of area of triangle and area of sector in equation 1

$$\Rightarrow \text{Area of minor segment} = 1848 - 762.93$$

$$= 1085.07 \text{ cm}^2$$

$$\text{Area of major segment} = \pi R^2 - \text{Area of minor segment}$$

Put the value of area of minor segment and  $R$  in above equation

$$= \pi(42^2) - 1085.07$$

$$\Rightarrow \text{Area of major segment} = 22/7 \times 42 \times 42 - 1085.07$$

$$(\text{put } \pi = 22/7)$$

$$\Rightarrow \text{Area of major segment} = 5544 - 1085.07$$

$$\therefore \text{Area of major segment} = 4458.93 \text{ cm}^2$$

Area of major segment is  $4458.93 \text{ cm}^2$  and of minor segment is  $1085.07 \text{ cm}^2$ .

**Question: 18**

Area of minor segment = Area of sector - Area of triangle  $\rightarrow$  eqn1

$$\text{Area of sector} = \frac{\theta}{360} \times \pi R^2$$

Where  $R$  = radius of the circle and  $\theta$  = central angle of the sector

$$\text{Area of sector} = \frac{60}{360} \times \pi(30^2) \text{ (put } \pi = 3.14)$$

$$\text{Area of sector} = \frac{60}{360} \times 3.14 \times 900$$

$$\text{Area of sector} = \frac{3.14 \times 900}{6}$$

$$\therefore \text{Area of sector} = 471 \text{ cm}^2$$

$$\text{Area of right angle triangle} = \frac{\sqrt{3}}{4} \times a^2$$

Where  $a$  = side of the triangle

$$\text{Area of triangle} = \sqrt{3}/4 \times 30 \times 30$$

$$\text{Area of triangle} = \sqrt{3}/4 \times 900$$

$$\text{Area of triangle} = (900 \times \sqrt{3})/4$$

$$(\text{put } \sqrt{3} = 1.732)$$

$$\text{Area of triangle} = (1.732 \times 900)/4$$

$$\therefore \text{Area of triangle} = 389.7 \text{ cm}^2$$

Put the values of area of triangle and area of sector in equation 1

$$\text{Area of minor segment} = 471 - 389.7$$

$$\Rightarrow \text{Area of minor segment} = 81.3 \text{ cm}^2$$

$$\text{Area of major segment} = \pi R^2 - \text{Area of minor segment}$$

Put the value of area of minor segment and  $R$  in above equation

$$\Rightarrow \text{Area of major segment} = \pi \times (30^2) - 81.3 \text{ (put } \pi = 3.14)$$

$$\Rightarrow \text{Area of major segment} = 3.14 \times 30 \times 30 - 81.3$$

$$\Rightarrow \text{Area of major segment} = 2826 - 81.3$$

$$= 2744.7 \text{ cm}^2$$

Area of major segment is  $2744.7 \text{ cm}^2$  and of minor segment is  $81.3 \text{ cm}^2$ .

**Question: 19**

In a circle of ra

**Solution:**

Given radius of circle =  $R = 10.5 \text{ cm}$

Let the area of major sector be ' $A_1$ ' and that of minor sector be ' $A_2$ '

$$\therefore A_2 = \frac{A_1}{5} \rightarrow \text{eqn1}$$

We know, Area of circle = Area of major sector + Area of minor sector

$$\Rightarrow \text{Area of circle} = A_1 + A_2$$

$$\Rightarrow \text{Area of circle} = A_1 + \frac{A_1}{5} \rightarrow \text{eqn2 (from equation 1)}$$

We also know, Area of circle =  $\pi R^2$

Where  $R$  = radius of circle, put value of area of circle in equation 2.

$$\Rightarrow \pi(10.5^2) = \frac{5A_1 + A_1}{5}$$

(taking 5 as L.C.M on R.H.S)

$$\Rightarrow \pi \times 10.5 \times 10.5 = \frac{6A_1}{5}$$

$$\Rightarrow \frac{22}{7} \times 10.5 \times 10.5 = \frac{6A_1}{5}$$

$$\Rightarrow \frac{22 \times 10.5 \times 10.5}{7} = \frac{6A_1}{5}$$

$$\Rightarrow 22 \times 10.5 \times 1.5 = \frac{6A_1}{5}$$

$$\Rightarrow 346.5 = \frac{6A_1}{5}$$

$$\Rightarrow \frac{5 \times 346.5}{6} = A_1$$

$$= 288.75 \text{ cm}^2$$

The area of major sector is  $288.75 \text{ cm}^2$ .

### Question: 20

In an hour the minute hand completes one rotation therefore in 24 hours the minute hand will complete 24 rotations similarly the hour hand completes one rotation in 12 hours therefore in 24 hours it will complete 2 rotations. Now we have to just calculate the perimeter of the circle traced by minute hand and hour hand and multiply it with the number of rotations of minute hand and hour hand in 2 days respectively.

Length of short/hour hand =  $r = 4 \text{ cm}$

Length of long/minute hand =  $R = 6 \text{ cm}$

$\therefore$  The perimeter of circle traced by short hand =  $p = 2\pi r \rightarrow \text{eqn1}$

$\therefore$  The perimeter of circle traced by Long hand =  $P = 2\pi R \rightarrow \text{eqn2}$

Now put the value of ' $r$ ' and ' $R$ ' in the equation 1 and 2 respectively.

$$\Rightarrow p = 2\pi(4) \text{ & } P = 2\pi(6) \text{ (put } \pi = 3.14)$$

$$\Rightarrow p = 2 \times 3.14 \times 4 \text{ & } P = 2 \times 3.14 \times 6$$

$$\therefore p = 25.12 \text{ cm & } P = 37.68 \text{ cm}$$

Therefore, distance covered by short hand in one rotation =  $25.12 \text{ cm}$

Distance covered by long hand in one rotation =  $37.68 \text{ cm}$

Number of rotation of short hand in one day = 2

Number of rotation of long hand in one day = 24

Therefore number of rotation of small hand in two days = 4

Number of rotation of long hand in two days = 48

Total distance covered by long hand in 2 days =  $P \times \text{no. of rotations in 2 days}$

$$\Rightarrow \text{Total distance covered by long hand in 2 days} = 37.68 \times 48$$

$\Rightarrow$  Total distance covered by long hand in 2 days = 1808.64 cm  $\rightarrow$  eqn3

Total distance covered by short hand in 2 days =  $p \times$  no. of rotations in 2 days

$\Rightarrow$  Total distance covered by short hand in 2 days =  $25.12 \times 24$

$\Rightarrow$  Total distance covered by short hand in 2 days = 100.48 cm  $\rightarrow$  eqn4

Now total distance covered by tip of both hands in 2 days = eqn3 + eqn4

$\Rightarrow$  Total distance covered by both hands in 2 days = 1808.64 + 100.48

$\Rightarrow$  Total distance covered by both hands in 2 days = 1909.12 cm

The distance covered by both hands tip in 2 days is 1909.12 cm

### Question: 21

Quadrant is a sector in which the central angle is 90 degrees, and this is the key to solve this question. As we know the central angle of the sector so we can easily calculate the area of quadrant by first calculating the radius of the circle as the circumference of the circle is given and then applying the formula of area of sector.

So, we know Circumference of a circle =  $2\pi R \rightarrow$  eqn1

Where  $R$  = radius of the circle

Given Circumference of the circle = 88 cm,  $\theta = 90^\circ$

Put the given values in equation 1

$$88 = 2 \times \frac{22}{7} \times R (\pi = \frac{22}{7})$$

$$\Rightarrow 88 = \frac{2 \times 22 \times R}{7}$$

$$\Rightarrow 88 = (44 \times R)/7$$

$$\Rightarrow 88 = 44R/7$$

$$\Rightarrow (88 \times 7)/44 = R$$

$$\Rightarrow 616/44 = R$$

$$\Rightarrow R = 14 \text{ cm}$$

$$\text{Now we know Area of a sector} = \frac{\theta}{360} \times \pi R^2$$

Put the values of  $R$  and  $\theta$  in the above equation

$$\Rightarrow \text{Area of quadrant} = \frac{90}{360} \times \pi(14^2)$$

$$= \frac{90}{360} \times \frac{22}{7} \times 14 \times 14$$

$$= \frac{90 \times 22 \times 14 \times 14}{360 \times 7}$$

$$= \frac{22 \times 14 \times 14}{4 \times 7} = \frac{4312}{28}$$

$$= 154 \text{ cm}^2.$$

The area of quadrant is 154 cm<sup>2</sup>.

### Question: 22

Here the increase in the length of the rope simply means that there is increase in the radius of the circle within which cow can graze. Now to find the additional area available for grazing can be easily be found by simply subtracting the initial area available for grazing from the new area available.

Initial radius =  $r = 16$  cm

Increased radius =  $R = 23$  cm

Additional ground available = Area of new ground - Initial area  $\rightarrow$  eqn1

Initial area of ground =  $\pi(r^2)$

$\Rightarrow$  Initial area of ground =  $\pi(16^2)$

$\Rightarrow$  Initial area of ground =  $256\pi \rightarrow$  eqn2

Area of new ground =  $\pi R^2$

$\Rightarrow$  Area of new ground =  $\pi(23^2)$

$\Rightarrow$  Area of new ground =  $529\pi \rightarrow$  eqn3

Now put the values of equation 2 and 3 in equation 1

$\Rightarrow$  Additional area of ground available =  $529\pi - 256\pi$

$\Rightarrow$  Additional area available =  $(529 - 256)\pi$  (Taking  $\pi$  common)

$\Rightarrow$  Additional ground available =  $273\pi$

$\Rightarrow$  Additional ground available =  $273 \times \frac{22}{7}$

(put  $\pi = \frac{22}{7}$ )

$= (22 \times 273)/7$

$= 6006/7$

$= 858 \text{ cm}^2$

The additional ground available is  $858 \text{ cm}^2$ .

### Question: 23

Here the horse is tethered to one corner implies or means that the area available for grazing is a quadrant of radius 21 m. Now we need to find the area of this quadrant to find out the area available for grazing and then subtract it from the total area of the rectangular field to obtain the area left ungrazed.

Given length of rectangular field =  $l = 70$  m

Breadth of rectangular field =  $b = 52$  m

$\therefore$  Area of the field =  $l \times b$

$\Rightarrow$  Area of the field =  $70 \times 52$

$\Rightarrow$  Area of the field =  $3640 \text{ m}^2$

We know in a rectangle all the angles are 90 degrees.

$\therefore$  Area available for grazing = area of quadrant

$\Rightarrow$  Area of quadrant/sector =  $\frac{\theta}{360} \times \pi R^2$

Where  $R$  = radius of circle &  $\theta$  = central angle

Given  $R = 21$  m and  $\theta = 90^\circ$

$\Rightarrow$  Area available for grazing =  $\frac{\theta}{360} \times \pi R^2$

Put the given values in the above equation,

$\Rightarrow$  Area available for grazing =  $\frac{90}{360} \times \pi(21^2)$

(put  $\pi = 22/7$ )

$$= \frac{90}{360} \times \frac{22}{7} \times 441$$

$$= \frac{90 \times 22 \times 441}{360 \times 7}$$

$$= (22 \times 63)/4$$

$$= 1386/4$$

$$\Rightarrow \text{Area available for grazing} = 346.5 \text{ m}^2$$

Area left ungrazed = Area of field - Area available for grazing

$$\Rightarrow \text{Area left ungrazed} = 3640 - 346.5$$

$$\Rightarrow \text{Area left ungrazed} = 3293.5 \text{ m}^2$$

The area available for grazing is  $346.5 \text{ m}^2$  and area left ungrazed is  $3293.5 \text{ m}^2$ .

#### Question: 24

Here the horse is tethered to one corner implies or means that the area available for grazing is a sector of radius 21 m with central angle as 60 degrees as the field is in shape of equilateral triangle. Now we need to find the area of this sector to find out the area available for grazing and then subtract it from the total area of the triangular field to obtain the area left ungrazed.

Given the side of field =  $a = 12 \text{ m}$

$\therefore$  Area of field = Area of equilateral triangle

$$\Rightarrow \text{Area of field} = \frac{\sqrt{3}}{4} \times a^2$$

$$\Rightarrow \text{Area of field} = \frac{1.732}{4} \times (12^2)$$

$$\Rightarrow \text{Area of field} = \frac{1.732 \times 144}{4}$$

$$\Rightarrow \text{Area of field} = 62.352 \text{ m}^2$$

We know in an equilateral triangle all the angles are 60 degrees.

$\therefore$  Area available for grazing = Area of the sector

$$\text{Area of quadrant/sector} = \frac{\theta}{360} \times \pi R^2$$

Where  $R$  = radius of circle and  $\theta$  = central angle of sector

Given  $R = 7 \text{ m}$  and  $\theta = 60^\circ$

Put the given values in the above equation,

$$\Rightarrow \text{Area available for grazing} = \frac{60}{360} \times \pi(7^2) \left( \text{put } \pi = \frac{22}{7} \right)$$

$$\Rightarrow \text{Area available for grazing} = \frac{60}{360} \times \frac{22}{7} \times 49$$

$$\Rightarrow \text{Area available for grazing} = \frac{60 \times 22 \times 49}{360 \times 7}$$

$$\Rightarrow \text{Area available for grazing} = \frac{22 \times 7}{6}$$

$$\Rightarrow \text{Area available for grazing} = \frac{154}{6}$$

$$\Rightarrow \text{Area available for grazing} = 25.666 \text{ m}^2$$

Area that cannot be grazed = Area of field - Area available for grazing

$$\Rightarrow \text{Area that cannot be grazed} = 62.352 - 25.666$$

$$\Rightarrow \text{Area that cannot be grazed} = 36.686 \text{ m}^2$$

The area that cannot be grazed is  $36.686 \text{ m}^2$ .

### Question: 25

Here the 4 cows are tethered to each corner implies or means that the area available for grazing is a quadrant of radius 25 m with central angle as 60 degrees as the field is in shape of square . Now we need to find the area of this sector to find out the area available for grazing for all the cows and then subtract it from the total area of the square field to obtain the area left ungrazed.

The reason why we have taken the radius as 25 m is , basically we have considered that each cow is tethered to a rope which is equal to half of the side of the square as we had to maximize the area each cow gets to graze without sharing thus the maximum radius within which a cow can graze maximum unshared area is simply the half of the side of square.

Given the side of field which is in shape of square =  $a = 50 \text{ m}$

$\therefore$  Area of the field = Area of Square

$$\Rightarrow \text{Area of field} = a^2$$

$$\Rightarrow \text{Area of field} = (50^2)$$

$$\Rightarrow \text{Area of field} = 2500 \text{ m}^2$$

We know in an square all the angles are 90 degrees.

$\therefore$  Area available for grazing for one cow = area of sector/quadrant

$$\text{Area of quadrant/sector} = \frac{\theta}{360} \times \pi R^2$$

Where  $R$  = radius of circle &  $\theta$  = central angle of sector

Given  $R = 25 \text{ m}$  &  $\theta = 90^\circ$

$$\Rightarrow \text{Area available for grazing for one cow} = \frac{\theta}{360} \times \pi R^2$$

Put the given values in the above equation,

$$\Rightarrow \text{Area available for grazing for one cow} = \frac{90}{360} \times \pi(25^2) \text{ (put } \pi = 3.14\text{)}$$

$$\Rightarrow \text{Area available for grazing for one cow} = \frac{90}{360} \times 3.14 \times 625$$

$$\Rightarrow \text{Area available for grazing for one cow} = \frac{90 \times 3.14 \times 625}{360}$$

$$\Rightarrow \text{Area available for grazing for one cow} = \frac{3.14 \times 625}{4}$$

$$\Rightarrow \text{Area available for grazing for one cow} = \frac{1962.5}{4}$$

$$\Rightarrow \text{Area available for grazing for one cow} = 490.625 \text{ m}^2$$

$$\Rightarrow \text{Area available for 4 cows} = 4 \times \text{Area available for one cow}$$

$$\Rightarrow \text{Area available for 4 cows} = 4 \times 490.625$$

$$\Rightarrow \text{Area available for 4 cows} = 1962.5 \text{ m}^2$$

Area left ungrazed = Area of field - Area available for grazing for 4 cows

$$\Rightarrow \text{Area that cannot be grazed} = 2500 - 1962.5$$

$$\Rightarrow \text{Area that cannot be grazed} = 2500 - 1962.5$$

$\Rightarrow$  Area that cannot be grazed =  $537.5 \text{ m}^2$

The area left ungrazed is  $537.5 \text{ m}^2$ .

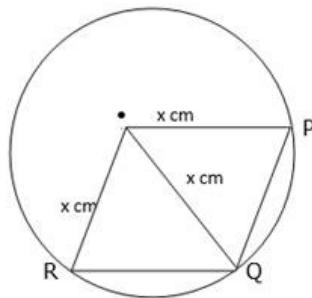
### Question: 26

Here in the given figure 'O' is the centre of circle on which three vertices of rhombus lie, this implies that OP, OR are both radius of the circle. Also we know that in rhombus all the 4 sides are equal in length. Thus OP, OR, PQ, RQ, they all are radii of circle. Also OQ is equal to radius of circle. Now rhombus being a parallelogram therefore diagonal OQ will divide the rhombus into two equal halves this means that the area of triangle OQR will be equal to half of the area of rhombus. Also we can see that triangle OQR is an equilateral triangle and hence we can easily calculate its area in terms of radius of circle and equate it to half of the area of rhombus and calculate the radius of given circle.

$$\text{Given Area of OPQR} = 32\sqrt{3} \text{ cm}^2$$

Let the radius of the circle =  $x \text{ cm}$

Now join OQ



Consider  $\Delta OQR$ ,

$$OQ = OR = RQ = x \text{ cm}$$

$\Rightarrow \Delta OQR$  is an equilateral triangle

$$\therefore \text{Area of } \Delta OQR = \text{Area of an equilateral triangle} = \frac{\sqrt{3}}{4} \times a^2 \rightarrow \text{eqn 1}$$

Where  $a$  = side of equilateral triangle

Also we know OQ is a diagonal of rhombus OPQR and as in a parallelogram diagonal divides it into two equal area or halves , similarly OQ is also dividing the rhombus into two equal areas therefore,

$$\Rightarrow \text{Area of } \Delta OQR = \text{Area of } \Delta OPQ \rightarrow \text{eqn2}$$

$$\text{Area of OPQR} = \text{Area of } \Delta OQR + \text{Area of } \Delta OPQ$$

$$\text{Area of OPQR} = 2 \times \text{Area of } \Delta OQR \text{ (from eqn2)} \rightarrow \text{eqn3}$$

Put the values of area of OPQR and equation 1 in equation 3

$$\Rightarrow 32\sqrt{3} = 2 \times \frac{\sqrt{3}}{4} \times a^2 \text{ (put } a = x)$$

$$\Rightarrow 32\sqrt{3} = \frac{2\sqrt{3}}{4} \times x^2$$

$$\Rightarrow 32\sqrt{3} = \frac{\sqrt{3}}{2} \times x^2$$

$$\Rightarrow \frac{32\sqrt{3} \times 2}{\sqrt{3}} = x^2$$

$$\Rightarrow 64 = x^2$$

$$\Rightarrow x = \pm\sqrt{64}$$

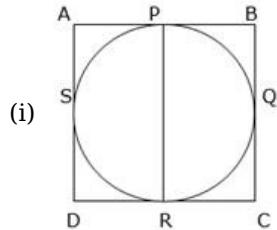
$$\Rightarrow x = \pm 8$$

As every quadratic equation has two roots, similarly  $x^2 = 64$  also have two roots i.e.  $x = 8$  and  $x = -8$ . As we know that 'x' represents radius of circle therefore it cannot be a negative value, hence we discard the negative root.

Therefore radius of the circle =  $x = 8$  cm.

The radius of circle is 8 cm.

**Question: 27**



Consider the above figure, Join PR,

Now PR = Diameter of the inscribed circle

Also, PR = BC = 10 cm.

So, PR = 10 cm

$$\therefore \text{radius of inscribed circle} = r = \frac{PR}{2}$$

$$\Rightarrow r = \frac{10}{2}$$

$$\Rightarrow r = 5 \text{ cm}$$

$\therefore$  Area of inscribed circle =  $\pi r^2$  (put value of r in this equation)

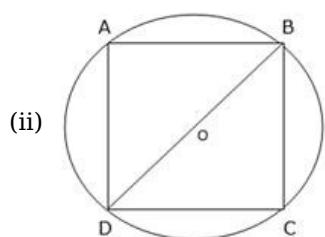
$$\Rightarrow \text{Area of inscribed circle} = \pi(5^2)$$

$$\Rightarrow \text{Area of inscribed circle} = \frac{22}{7} \times 25 \text{ (put } \pi = \frac{22}{7})$$

$$\Rightarrow \text{Area of inscribed circle} = \frac{22 \times 25}{7}$$

$$\Rightarrow \text{Area of inscribed circle} = 78.57 \text{ cm}^2$$

The area of inscribed circle is  $78.57 \text{ cm}^2$ .



Consider the above figure, O is the centre of circle and ABCD is a square inscribed. Now OB and OD are radii of circle.

Consider  $\triangle DBC$  right angled at C (as C is a vertex of square)

$\therefore$  Apply Pythagoras theorem in triangle DBC

$$\text{Hypotenuse}^2 = \text{Perpendicular}^2 + \text{Base}^2$$

In triangle DBC, hypotenuse = DB,

perpendicular = BC and

base = DC

$$\Rightarrow BD^2 = BC^2 + DC^2$$

Put the values of BC and DC i.e. 10 cm

$$\Rightarrow BD^2 = 10^2 + 10^2$$

$$\Rightarrow BD^2 = 200$$

$$\Rightarrow BD = \sqrt{200}$$

$$\Rightarrow BD = 10\sqrt{2} \text{ cm}$$

Now radius of circle = half of BD

$$\therefore \text{radius of circle} = r = \frac{BD}{2}$$

$$\Rightarrow r = (10\sqrt{2})/2$$

$$\Rightarrow r = 5\sqrt{2} \text{ cm}$$

Hence Area of circumscribing circle =  $\pi r^2$

$$\Rightarrow \text{Area of circumscribing circle} = 3.14 \times 5\sqrt{2} \times 5\sqrt{2}$$

(put  $\pi = 3.14$  and  $r = 5\sqrt{2} \text{ cm}$ )

$$\Rightarrow \text{Area of circumscribing circle} = 3.14 \times 50$$

$$\Rightarrow \text{Area of circumscribing circle} = 157 \text{ cm}^2$$

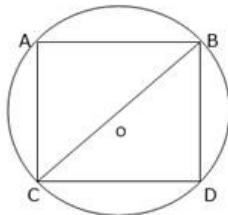
Area of circumscribing circle is  $157 \text{ cm}^2$ .

### Question: 28

Consider the figure shown below where O is centre of circle, join BC which passes through O, let the side of square be 'a' and radius of circle be 'r'.

Now we know OB and OC are radius of circle

$$\text{So, } OB = OC = r$$



Consider  $\triangle BDC$  right angled at D

$$\therefore H^2 = P^2 + B^2 \text{ (Pythagoras theorem)}$$

$$\Rightarrow BC^2 = BD^2 + DC^2 \rightarrow \text{eqn1}$$

And we know  $BC = OC + OB$

$BC = 2r$  and  $BD = DC = a$  (put these values in eqn1)

$$\Rightarrow (2r)^2 = a^2 + a^2$$

$$\Rightarrow 4r^2 = 2a^2$$

$$\Rightarrow r^2 = \frac{2a^2}{4}$$

$$\Rightarrow r^2 = \frac{a^2}{2} \rightarrow \text{eqn2}$$

Area of inscribed square = side  $\times$  side

Area of inscribed square =  $a \times a$

Area of inscribed square =  $a^2 \rightarrow$  eqn3

Area of circumscribing circle =  $\pi R^2$  where  $R$  = radius of circle

$\Rightarrow$  Area of circumscribing circle =  $\pi r^2 \rightarrow$  eqn4

Ratio of area of circumscribing circle to that of inscribed circle  
 $= \frac{\text{area of circle}}{\text{area of square}}$

Put the values from equation 3 & 4 in above equation

$$\text{Ratio} = \frac{\pi r^2}{a^2}$$

$$\Rightarrow \text{Ratio} = \frac{\pi \times \frac{a^2}{2}}{a^2}$$

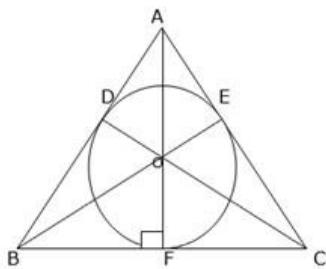
(from eqn 2)

$$\Rightarrow \text{Ratio} = \frac{\pi \times a^2}{2 \times a^2} = \frac{\pi}{2}$$

So, Ratio is  $\pi : 2$

The ratio is  $\pi : 2$

### Question: 29



Consider the figure shown above, AF, BE and CD are perpendicular bisector.

Now we know that the point at which all three perpendiculars meet is called incentre, so O is the incentre, thus O divides all three perpendiculars in a ratio 2:1.

Let  $AB = BC = CA = a$  cm

Therefore let  $AF = h$  cm

$$\Rightarrow \angle AFC = 90^\circ \text{ and } OF = \frac{1}{3} \times AF$$

$$\Rightarrow OF = \frac{h}{3} \text{ cm (putting value of OF)}$$

$$\Rightarrow h = 3 \times OF \rightarrow \text{eqn1}$$

And we can see from figure that  $OF = \text{radius of circle}$

Now let radius of circle be =  $r$  cm

$$\therefore \text{Area of circle} = \pi R^2$$

where  $R = \text{radius of circle}$

Given area of circle =  $154 \text{ cm}^2$

$$\Rightarrow \pi r^2 = 154$$

$$\Rightarrow \frac{22}{7} \times r^2 = 154 \text{ (put } \pi = \frac{22}{7})$$

$$\Rightarrow r^2 = \frac{154 \times 7}{22}$$

$$\Rightarrow r^2 = 49$$

$$\Rightarrow r = 7 \text{ cm}$$

Therefore OF = 7 cm

$$\Rightarrow h = 3 \times 7 \text{ (from eqn 1)}$$

$$\Rightarrow h = 21 \text{ cm}$$

we know area of an equilateral triangle =  $\frac{\sqrt{3}}{4} \times a^2$

where  $a$  = side of triangle

Also, Area of triangle =  $1/2 \times \text{base} \times \text{height}$

Equating both the areas we get,

$$\frac{\sqrt{3}}{4} \times a^2 = \frac{1}{2} \times BC \times AF$$

Put the values of BC and AF

$$\Rightarrow \frac{\sqrt{3}}{4} \times a^2 = \frac{1}{2} \times a \times h$$

$$\Rightarrow \frac{\sqrt{3}}{4} \times a^2 = \frac{1}{2} \times a \times 21$$

(putting value of  $h = 21 \text{ cm}$ )

$$\Rightarrow \frac{\sqrt{3}}{4} \times a = \frac{21}{2}$$

$$\Rightarrow a = \frac{21 \times 4}{2 \times \sqrt{3}}$$

(rationalize it)

$$\Rightarrow a = \frac{21 \times 4 \times \sqrt{3}}{2 \times \sqrt{3} \times \sqrt{3}}$$

$$\Rightarrow a = \frac{42 \times \sqrt{3}}{3}$$

$$\Rightarrow a = 14\sqrt{3} \text{ cm}$$

$\therefore$  Perimeter of equilateral triangle =  $3 \times \text{side of triangle}$

$$\Rightarrow \text{Perimeter of } \Delta ABC = 3 \times 14\sqrt{3} \text{ (put } \sqrt{3} = 1.73\text{)}$$

$$\Rightarrow \text{Perimeter of } \Delta ABC = 42 \times 1.73$$

$$\Rightarrow \text{Perimeter of } \Delta ABC = 72.66 \text{ cm}$$

The perimeter of triangle is 72.66 cm

### Question: 30

In one revolution a wheel will cover a distance equal to its circumference, so in order to find the number of revolutions we have to first calculate the circumference of the wheel and then divide it with the total distance covered to find out the total number of revolutions

Given radius of wheel =  $r = 42 \text{ cm}$

Circumference of wheel =  $2\pi R$  where  $R$  = radius of the wheel

$$= 2\pi(42) \text{ (putting value of } r\text{)}$$

$$\text{Circumference of wheel} = \frac{2 \times 22 \times 42}{7} = 264 \text{ cm}$$

Therefore distance covered in one revolution = 264 cm

Total distance covered = 19.8 km = 1980000 cm

Total number of revolutions = n

Distance covered on 1 revolution  $\times$  no. of revolutions = Total distance

$$264 \times n = 1980000$$

$$\Rightarrow n = \frac{1980000}{264}$$

$$\Rightarrow n = 7500$$

Total number of revolutions is 7500.

### Question: 31

Given radius of wheel = R = 2.1m

Number of revolutions in one minute = 75

Number of revolutions in 1 hour =  $75 \times 60$

Number of revolutions in 1 hour = 45000

Distance covered in one revolution = Circumference of wheel

Distance covered in 1 revolution =  $2\pi R$  (where R = radius of wheel)

Distance covered in 1 revolution =  $2\pi(2.1)$

$$\text{Distance covered in one revolution} = 2 \times \frac{22}{7} \times 2.1 \text{ (put } \pi = \frac{22}{7})$$

$$= 13.2 \text{ m}$$

So, distance covered in 4500 revolutions =  $4500 \times$  distance covered in 1

Distance covered in 4500 revolutions =  $4500 \times 13.2$

Distance covered in 4500 revolutions = 59400 m = 59.4 km

$\therefore$  Distance covered in 1 hour = 59.4 km

Hence speed of the locomotive = 59.4 km/hr

The speed of locomotive is 59.4 km/hr

### Question: 32

Let the diameter of the wheel be 'd' cm

Total distance covered in 250 revolutions = 49.5 km = 495000 m

$$\text{distance covered in one revolution} = \frac{495000}{250}$$

$\Rightarrow$  Distance covered in one revolution = 198 cm  $\rightarrow$  eqn1

Also, Distance covered in one revolution = circumference of wheel

$\therefore$  Distance covered in one revolution =  $\pi D$  where d = diameter of wheel

$$\text{Distance covered in one revolution} = \frac{22 \times d}{7} \rightarrow \text{eqn2 (put } \pi = \frac{22}{7})$$

Equate equation 1 and 2 we get,

$$\frac{22 \times d}{7} = 198$$

$$\Rightarrow d = \frac{198 \times 7}{22}$$

$$\Rightarrow d = 9 \times 7$$

$$\Rightarrow d = 63 \text{ cm}$$

The diameter of the wheel is 63 cm.

### Question: 33

Given diameter of wheel =  $d = 60 \text{ cm}$

Number of revolutions in one minute = 140

Number of revolutions in one hour =  $140 \times 60$

Number of revolutions in one hour = 8400

Distance covered in one revolution = circumference of wheel

$\Rightarrow$  Distance covered in one revolution =  $\pi d$

$$\text{Distance covered in one revolution} = \frac{22}{7} \times 60 \text{ (put } \pi = \frac{22}{7} \text{ and value of } d)$$

$$= 188.57 \text{ cm}$$

Distance covered in one hour = Distance in 1 revolution  $\times$  no. of revolutions

$\Rightarrow$  Total distance covered in one hour =  $188.57 \times 8400$

$\Rightarrow$  Total distance covered in one hour = 1583988 cm = 15.839 km

$\therefore$  speed with which boy is cycling = 15.839 km/hr

The speed with which boy is cycling is 15.839 km/hr

### Question: 34

Given diameter of wheel of bus =  $d = 140 \text{ cm}$

$$\text{So radius of wheel} = R = \frac{d}{2} = \frac{140}{2} = 70 \text{ cm}$$

Speed of bus = 72.6 km/hr

$\therefore$  Distance covered by bus in one hour = 72.6 km = 7260000 cm

$$\text{So distance covered by wheels in one minute} = \frac{7260000}{60}$$

Distance covered in one minute = 121000 cm  $\rightarrow$  eqn1

Let the number of revolutions made by wheel per minute =  $x$

Distance covered by wheel in one revolution = circumference of wheel =  $2\pi R$

Distance covered by wheel in one revolution =  $2\pi(70)$

(putting value of  $R$ )

$$= 2 \times \frac{22}{7} \times 70 \left( \text{putting value of } R \text{ and } \pi = \frac{22}{7} \right)$$

$$= \frac{2 \times 22 \times 70}{7}$$

$$= 2 \times 22 \times 10 = 440 \text{ cm}$$

$\therefore$  Total distance = No. of revolution  $\times$  Distance covered in 1 revolution

On putting the required values we get,

$$121000 = 440 \times (x)$$

$$\Rightarrow x = \frac{121000}{440}$$

$$\Rightarrow x = 275$$

Number of revolutions made per minute is 275.

### Question: 35

Given diameter of front wheel =  $d = 80 \text{ cm}$

so, Radius of front wheel =  $r = d/2 = 80/2 = 40 \text{ cm}$

Diameter of rear wheel =  $D = 2 \text{ m} = 200 \text{ cm}$

$$\text{so, Radius of front wheel} = R = \frac{D}{2} = \frac{200}{2} = 100 \text{ cm}$$

Distance covered by wheel in 1 revolution = Circumference of wheel

$$\Rightarrow \text{Distance covered by front wheel} = 2\pi r = 2\pi(40)$$

$$\Rightarrow \text{Distance covered by front wheel} = 80\pi$$

$$\therefore \text{Distance covered by front wheel in 800 revolutions} = 80\pi \times 800$$

$$\Rightarrow \text{Distance covered by front wheel in 800 revolutions} = 6400\pi \rightarrow \text{eqn1}$$

Similarly

$$\Rightarrow \text{Distance covered by rear wheel} = 2\pi R = 2\pi(100)$$

$$\Rightarrow \text{Distance covered by rear wheel} = 200\pi \rightarrow \text{eqn2}$$

Let the number of revolutions made by rear wheel to cover  $6400\pi \text{ cm}$  be "x"

$$\therefore (x) \times 200\pi = 6400\pi \text{ (from eqn1 and eqn2)}$$

$$\Rightarrow x = \frac{6400\pi}{200\pi}$$

$$\Rightarrow x = 6400/200$$

$$\Rightarrow x = 320$$

Number of revolution made by rear wheel to cover the distance covered by front wheel in 800 revolutions is 320.

### Question: 36

Here the distance between the center of circles touching each other is equal to the side of the square. Therefore, we can say that the radius of ach circle is equal to the half of the side of the square. Now by simply calculating the area of the 4 quadrants and then subtracting it from the area of the square we can easily calculate the area of the shaded region.

Given side of square =  $a = 14 \text{ cm}$

Central angle of each sector formed at corner =  $\theta = 90^\circ$

So, radius of 4 equal circles =  $r = a/2 = 14/2$

$\therefore$  Radius of 4 circles =  $r = 7 \text{ cm}$

$$\text{Area of quadrant formed at each corner} = \frac{\theta}{360} \times \pi R^2$$

where  $R$  = radius of circle

$$\Rightarrow \text{Area of one quadrant} = \frac{90}{360} \times \pi(7^2)$$

$$= \frac{49\pi}{4} \text{ cm}^2 \rightarrow \text{eqn1}$$

Area of all the 4 quadrant =  $4 \times \text{Area of one quadrant}$

$$= 4 \times \frac{49\pi}{4} \text{ (from eqn 1)}$$

$$\Rightarrow \text{Area of all 4 quadrants} = 49\pi \rightarrow \text{eqn2}$$

Also, Area of square = side × side =  $a \times a = a^2 = 14^2$  (putting value of side of square)

$$\Rightarrow \text{Area of square} = 196 \text{ cm}^2 \rightarrow \text{eqn3}$$

$\therefore$  Area of shaded region = Area of square - Area of all 4 quadrants

$$\Rightarrow \text{Area of shaded region} = 196 - 49\pi \text{ (from eqn3 and eqn2)}$$

$$\Rightarrow \text{Area of shaded region} = 196 - \left(49 \times \frac{22}{7}\right) \text{ (put } \pi = \frac{22}{7})$$

$$= 196 - (7 \times 22)$$

$$= 196 - 154$$

$$= 42 \text{ cm}^2$$

The area of shaded region is  $42 \text{ cm}^2$ .

### Question: 37

Here, first we join the center of all adjacent circles then the distance between the center of circles touching each other is equal to the side of the square formed by joining the center of adjacent circles. Therefore, we can say that the side of the square equal to the twice of the radius of circle. Now by simply calculating the area of the 4 quadrants and then subtracting it from the area of the square we can easily calculate the area of the shaded region.

Given radius of each circle =  $r = 5 \text{ cm}$

Central angle of each sector formed at corner =  $\theta = 90^\circ$

Side of square ABCD =  $a = 2 \times r = 2 \times 5 = 10 \text{ cm}$

$$\text{Area of quadrant formed at each corner} = \frac{\theta}{360} \times \pi R^2$$

where  $R$  = radius of circle

$$\Rightarrow \text{Area of one quadrant} = \frac{90}{360} \times \pi (5^2)$$

(putting value of  $r$  and  $\theta$ )

$$= \frac{25\pi}{4} \text{ cm}^2 \rightarrow \text{eqn1}$$

Area of all 4 quadrants =  $4 \times$  Area of one quadrant

$$= 4 \times \frac{25\pi}{4} \text{ (from eqn 1)}$$

$$\Rightarrow \text{Area of all 4 quadrants} = 25\pi \rightarrow \text{eqn2}$$

Area of square = side × side =  $a \times a = a^2$

$$\Rightarrow \text{Area of square} = 10^2 \text{ (putting value of side of square)}$$

$$\Rightarrow \text{Area of square} = 100 \text{ cm}^2 \rightarrow \text{eqn3}$$

Area of shaded region = Area of square - Area of all 4 quadrants

$$\text{Area of shaded region} = 100 - 25\pi \text{ (from eqn3 and eqn2)}$$

$$= 100 - (25 \times 3.14) \text{ (put } \pi = 3.14)$$

$$= 100 - 78.5$$

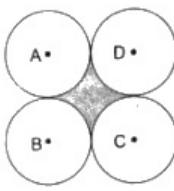
$$= 21.5 \text{ cm}^2$$

The area of shaded region is  $21.5 \text{ cm}^2$ .

### Question: 38

Four equal circle

**Solution:**



Here, first we join the centre of all adjacent circles then the distance between the centre of circles touching each other is equal to the side of the square formed by joining the centre of adjacent circles. Therefore, we can say that the side of the square equal to the twice of the radius of circle. Now by simply calculating the area of the 4 quadrants and then subtracting it from the area of the square we can easily calculate the area of the shaded region.

Given radius of each circle = "a" units

Central angle of each sector formed at corner =  $\theta = 90^\circ$

Side of square ABCD =  $2 \times a$  units

$$\text{Area of quadrant formed at each corner} = \frac{\theta}{360} \times \pi R^2$$

where  $R$  = radius of circle

$$\Rightarrow \text{Area of one quadrant} = \frac{90}{360} \times \pi(a^2)$$

$$\Rightarrow \text{Area of one quadrant} = \frac{\pi a^2}{4} \text{ sq. units} \rightarrow \text{eqn1}$$

$\therefore$  Area all 4 quadrants =  $4 \times$  Area of one quadrant

$$\Rightarrow \text{Area of all the 4 quadrant} = 4 \times \frac{\pi a^2}{4} \text{ (from eqn 1)}$$

$$= \pi a^2 \text{ sq. units} \rightarrow \text{eqn2}$$

$$\text{Area of square} = \text{side} \times \text{side} = 2a \times 2a = 4a^2$$

$$\Rightarrow \text{Area of square} = 4a^2 \text{ sq. units} \rightarrow \text{eqn3}$$

$$\text{Area of shaded region} = \text{Area of square} - \text{Area of all 4 quadrants}$$

$$\Rightarrow \text{Area of shaded region} = 4a^2 - \pi a^2 \text{ (from eqn3 and eqn2)}$$

$$\Rightarrow \text{Area of shaded region} = 4a^2 - \left( a^2 \times \frac{22}{7} \right) \text{ (put } \pi = \frac{22}{7})$$

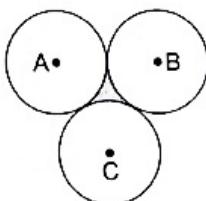
$$\Rightarrow \text{Area of the shaded region} = 4a^2 - \frac{22a^2}{7}$$

$$\Rightarrow \text{Area of shaded region} = \frac{28a^2 - 22a^2}{7}$$

$$\Rightarrow \text{Area of shaded region} = \frac{6a^2}{7} \text{ sq. units}$$

$$\text{Area of shaded region is } \frac{6a^2}{7} \text{ sq. units}$$

**Question: 39**



Consider the above figure,

Here, first we join the center of all adjacent circles then the distance between the center of circles touching each other is equal to the side of an equilateral triangle formed by joining the center of adjacent circles. Therefore, we can say that the side of the equilateral triangle is equal to twice of the radius of circle. Now by simply calculating the area of the 3 sectors and then subtracting it from the area of the equilateral triangle we can easily calculate the area of the enclosed region.

Given radius of each circle =  $r = 6 \text{ cm}$

Central angle of each sector =  $\theta = 60^\circ$  ( $\because \Delta ABC$  is equilateral)

Side of equilateral  $\Delta ABC = a = 2 \times r = 2 \times 6$

$\therefore$  Side of equilateral  $\Delta ABC = a = 12 \text{ cm}$

$$\begin{aligned} \text{Area of sector formed at each corner} &= \frac{\theta}{360} \times \pi R^2 \text{ where } R \\ &= \text{radius of circle} \end{aligned}$$

$$\Rightarrow \text{Area of one sector} = \frac{60}{360} \times \pi(6^2)$$

$$\Rightarrow \text{Area of one sector} = \frac{36\pi}{6} \text{ cm}^2$$

$$\Rightarrow \text{Area of one sector} = 6\pi \text{ cm}^2 \rightarrow \text{eqn1}$$

Area of all the 3 sector =  $3 \times \text{Area of one sector}$

$$= 3 \times 6\pi \text{ (from eqn1)}$$

$$= 18\pi \text{ cm}^2 \rightarrow \text{eqn2}$$

$$\text{Area of equilateral } \Delta ABC = \frac{\sqrt{3}}{4} \times a^2 = \frac{\sqrt{3}}{4} \times (12^2)$$

$$\Rightarrow \text{Area of equilateral } \Delta ABC = \frac{\sqrt{3} \times 144}{4}$$

$$\Rightarrow \text{Area of equilateral } \Delta ABC = 36\sqrt{3} \text{ cm}^2 \rightarrow \text{eqn3}$$

Area of enclosed region = Area of equilateral  $\Delta ABC$  - Area of all 3 sectors

$$\Rightarrow \text{Area of enclosed region} = 36\sqrt{3} - 18\pi \text{ (from eqn 3 and eqn 2)}$$

$$\Rightarrow \text{Area of enclosed region} = (36 \times 1.732) - (18 \times 3.14)$$

(put  $\pi = 3.14$  &  $\sqrt{3} = 1.732$ )

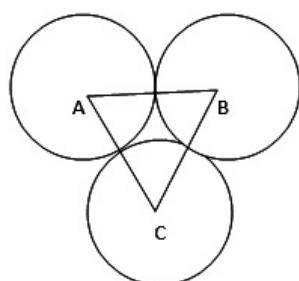
$$= 62.352 - 56.52$$

$$= 5.832 \text{ cm}^2$$

The area of enclosed region is  $5.832 \text{ cm}^2$ .

#### Question: 40

Consider the figure shown below



Here, first we join the center of all adjacent circles then the distance between the center of circles touching each other is equal to the side of an equilateral triangle formed by joining the

center of adjacent circles. Therefore, we can say that the side of the equilateral triangle is equal to the twice of the radius of circle. Now by simply calculating the area of the 3 sectors and then subtracting it from the area of the equilateral triangle we can easily calculate the area of the enclosed region.

Given radius of each circle = "a" units

Central angle of each sector =  $\theta = 60^\circ$  ( $\because \Delta ABC$  is equilateral)

Side of equilateral  $\Delta ABC = 2 \times a$  units

$$\text{Area of sector formed at each corner} = \frac{\theta}{360} \times \pi R^2$$

$$\Rightarrow \text{Area of one sector} = \frac{60}{360} \times \pi(a^2)$$

$$\Rightarrow \text{Area of one sector} = \frac{\pi a^2}{6} \text{ sq. units} \rightarrow \text{eqn1}$$

$\therefore$  Area of all 3 sectors =  $3 \times \text{Area of one sector}$

$$\Rightarrow \text{Area of all the 3 sector} = 3 \times \frac{\pi a^2}{6} \text{ (from eqn 1)}$$

$$= \frac{\pi a^2}{2} \text{ sq. units} \rightarrow \text{eqn2}$$

$$\text{Area of equilateral } \Delta ABC = \frac{\sqrt{3}}{4} \times (2a)^2$$

$$= \frac{\sqrt{3} \times 4a^2}{4}$$

$$= a^2 \sqrt{3} \text{ sq. units} \rightarrow \text{eqn3}$$

Area of enclosed region = Area of equilateral  $\Delta ABC$  - Area of all 3 sectors

$$\Rightarrow \text{Area of enclosed region} = a^2 \sqrt{3} - \frac{\pi a^2}{2} \text{ (from eqn 3 and eqn 2)}$$

$$= a^2 \times 1.73 - \frac{3.14 \times a^2}{2}$$

$$= \frac{a^2 \times 1.73 \times 2 - 3.14 \times a^2}{2}$$

$$= \frac{(3.46 - 3.14)a^2}{2}$$

(taking  $a^2$  common)

$$\Rightarrow \text{Area of the enclosed region} = \frac{0.32a^2}{2}$$

$$= \frac{32a^2}{200}$$

$$= \frac{4a^2}{25} \text{ sq. units}$$

Area of the enclosed region is  $\frac{4a^2}{25}$  sq. units

### Question: 41

In the give

### Solution:

Here in order to find the area of the shaded region we have to calculate the area, or the quadrant shown and subtract it from the area of the trapezium. And in order to find the area of the

quadrant we have to calculate the radius of the sector EAB by the area of trapezium.

Given Area of trapezium ABCD = 24.5 cm<sup>2</sup> → eqn1

AD || BC, AD = 10 cm, BC = 4 cm, ∠DAB = 90°

We also now Area of trapezium =  $\frac{1}{2} \times (\text{sum of parallel sides}) \times \text{height}$

Area of trapezium =  $\frac{1}{2} \times (AD + BC) \times AB \rightarrow \text{eqn2}$

Putting the values in equation 2, we get,

$$24.5 = \frac{1}{2} \times (10 + 4) \times AB$$

$$\Rightarrow 24.5 = \frac{14 \times AB}{2}$$

$$\Rightarrow 24.5 = 7AB$$

$$\Rightarrow AB = \frac{24.5}{7}$$

$$\Rightarrow AB = 3.5 \text{ cm}$$

Therefore radius of the sector EAB = r = 3.5 cm

Area of quadrant EAB =  $\frac{\theta}{360} \times \pi R^2$  where R = radius of the sector

$$\Rightarrow \text{Area of quadrant EAB} = \frac{90}{360} \times \pi(3.5^2) \left(\text{put } \pi = \frac{22}{7}\right)$$

$$\Rightarrow \text{Area of the quadrant} = \frac{90}{360} \times \frac{22}{7} \times 3.5 \times 3.5$$

$$\Rightarrow \text{Area of the quadrant EAB} = \frac{22 \times 3.5 \times 3.5}{4 \times 7}$$

$$\Rightarrow \text{Area of the quadrant EAB} = \frac{269.5}{28}$$

$$\Rightarrow \text{Area of the quadrant EAB} = 9.625 \text{ cm}^2 \rightarrow \text{eqn3}$$

∴ Area of shaded region = Area of trapezium - Area of quadrant EAB

$$\Rightarrow \text{Area of shaded region} = 24.5 - 9.625 \text{ (putting values from eqn1 and eqn3)}$$

$$\Rightarrow \text{Area of shaded region} = 14.875 \text{ cm}^2$$

### Question: 42

Here in order to find the area of the shaded region we have to calculate the area, or the quadrant shown and subtract it from the area of the trapezium. And in order to find the area of the quadrant we have to calculate the radius of the sector EAB by the area of trapezium.

Given AB = 30 m, AD = 55 m, BC = 45 m

$\theta_A = 90^\circ$ ,  $\theta_B = 90^\circ$ ,  $\theta_C = 120^\circ$ ,  $\theta_D = 60^\circ$

Radius of each sector = r = 14 m

(i) total area of 4 sectors

$$\text{Area of sector} = \frac{\theta_i}{360} \times \pi R^2 \rightarrow \text{eqn1}$$

$$= \frac{\theta_A}{360} \times \pi R^2$$

$$\text{Area of sector at corner A} = \frac{90}{360} \times \pi \times 14^2 \text{ (putting values in eqn 1)}$$

$$\text{Area of sector at corner A} = \frac{196\pi}{4}$$

$$\text{Area of sector at corner A} = 49\pi \text{ m}^2 \rightarrow \text{eqn2}$$

As we know that central angle at A and B are both 90 degrees and radius is also same i.e. 14 m therefore the area of the sector at B will be exactly same as that of sector at A.

$$\therefore \text{Area of sector at corner B} = \text{Area of sector at corner A}$$

$$\Rightarrow \text{Area of sector at corner B} = 49\pi \rightarrow \text{eqn3}$$

Similarly,

$$\text{Area of sector} = \frac{\theta_C}{360} \times \pi R^2$$

$$\text{Area of sector at corner C} = \frac{120}{360} \times \pi \times 14^2 \text{ (putting values in eqn 1)}$$

$$\text{Area of sector at corner C} = \frac{196\pi}{3}$$

$$\text{Area of sector at corner C} = 65.33\pi \text{ m}^2 \rightarrow \text{eqn4}$$

Similarly,

$$\text{Area of sector} = \frac{\theta_D}{360} \times \pi R^2$$

$$\text{Area of sector at corner D} = \frac{60}{360} \times \pi \times 14^2 \text{ (putting values in eqn 1)}$$

$$\text{Area of sector at corner D} = \frac{196\pi}{6}$$

$$\text{Area of sector at corner D} = 32.67\pi \rightarrow \text{eqn5}$$

$$\text{Total area of 4 sectors} = \text{eqn2} + \text{eqn3} + \text{eqn4} + \text{eqn5}$$

$$\Rightarrow \text{Total area of 4 sectors} = 49\pi + 49\pi + 65.33\pi + 32.67\pi$$

$$\Rightarrow \text{Total area of 4 sectors} = 196\pi$$

$$\text{Total area of 4 sectors} = 196\pi$$

$$\text{Total area of 4 sectors} = 196 \times \frac{22}{7} \left( \text{put } \pi = \frac{22}{7} \right)$$

$$\therefore \text{Total area of 4 sectors} = 616 \text{ m}^2$$

$$\text{Total area of 4 sectors is } 616 \text{ m}^2.$$

(ii) Area of the remaining portion

Here in order to find the area of the remaining portion of the trapezium we have to subtract the area of the 4 sectors from the area of the trapezium.

$$\text{Area of trapezium} = \frac{1}{2} \times (\text{sum of parallel sides}) \times \text{height}$$

$$\text{Area of trapezium} = \frac{1}{2} \times (AD + BC) \times AB$$

On putting the values,

$$\text{Area of trapezium} = \frac{1}{2} \times (55 + 45) \times 30$$

$$= \frac{100 \times 30}{2}$$

$$= 50 \times 30$$

Area of trapezium =  $1500 \text{ m}^2 \rightarrow \text{eqn1}$

Area of remaining portion = Area of trapezium - Area of the 4 sectors

$\Rightarrow$  Area of remaining portion =  $1500 - 616$  (from eqn1 and part (i))

$\therefore$  Area of remaining portion =  $884 \text{ m}^2$

The area of the remaining portion is  $884 \text{ m}^2$ .

### Question: 43

Area of shaded region can be calculated by subtracting the area of minor sector at vertex B from the sum of areas of the major sector at O and area of equilateral triangle.

Given Radius of circle at O =  $r = 6 \text{ cm}$

Side of equilateral triangle =  $a = 12 \text{ cm}$

Central angle at O =  $360 - 60 = 300^\circ$

Central angle at B =  $60^\circ$

Area of the equilateral triangle =  $\frac{\sqrt{3}}{4} \times a^2$

where  $a$  = side of equilateral triangle

Area of the equilateral triangle =  $\sqrt{3}/4 \times (12)^2$  (putting the value of  $a$ )

Area of the equilateral triangle =  $(144 \times \sqrt{3})/4$

Area of the equilateral triangle =  $36\sqrt{3} \text{ cm}^2 \rightarrow \text{eqn1}$

Area of sector =  $\theta/360 \times \pi R^2$  where  $r$  = radius of the sector

Area of minor sector at B =  $60/360 \times \pi \times (6^2)$  (given)

$\therefore$  Area of minor sector at B =  $6\pi \text{ cm}^2 \rightarrow \text{eqn2}$

Similarly,

Area of major sector at O =  $\frac{300}{360} \times \pi(6^2)$

$\therefore$  Area of major sector at O =  $30\pi \text{ cm}^2 \rightarrow \text{eqn3}$

Area of shaded region = eqn1 + eqn3 - eqn2

On putting values

$\Rightarrow$  Area of shaded region =  $36\sqrt{3} + 30\pi - 6\pi$

Area of shaded region =  $36\sqrt{3} + 24\pi$

(put  $\pi = 3.14$  and  $\sqrt{3} = 1.73$

$\therefore$  Area of shaded region =  $(36 \times 1.73) + (24 \times 3.14)$

$\Rightarrow$  Area of shaded region =  $62.28 + 75.36$

$\therefore$  Area of shaded region =  $137.64 \text{ cm}^2$

Area of the shaded region is  $137.64 \text{ cm}^2$ .

### Question: 44

Here in order to find the area of the shaded region we have to subtract the area of the semicircle and the triangle from the area of the rectangle.

Given AB = 80 cm, BC = 70 cm, DE = 42 cm,  $\angle AED = 90^\circ$

Here we see that the triangle AED is right angle triangle, therefore, we can apply Pythagoras theorem i.e.

$$H^2 = P^2 + B^2 \text{ (pythagoras theorem)}$$

$$AD^2 = DE^2 + AE^2$$

$$\Rightarrow 70^2 = 42^2 + AE^2 \text{ (putting the given values)}$$

$$= 4900 = 1764 + AE^2$$

$$= 4900 - 1764 = AE^2$$

$$= 3136 = AE^2$$

$$AE = \sqrt{3136}$$

$$\therefore AE = 56 \text{ cm}$$

$$\text{Area of } \Delta AED = 1/2 \times AE \times DE$$

$$(\text{Area of triangle} = 1/2 \times \text{base} \times \text{height})$$

On putting values we get,

$$\text{Area of } \Delta AED = 1/2 \times 56 \times 42$$

$$\Rightarrow \text{Area of } \Delta AED = 28 \times 42$$

$$\therefore \text{Area of } \Delta AED = 1176 \text{ cm}^2 \rightarrow \text{eqn1}$$

$$\text{Area of semicircle} = \frac{\pi R^2}{2}$$

$$\text{Here radius of semicircle} = \frac{BC}{2} = \frac{70}{2}$$

$$R = 35 \text{ cm}$$

$$\therefore \text{Area of semicircle} = \frac{\pi \times 35^2}{2}$$

$$\text{Area of semicircle} = \frac{22 \times 1225}{2 \times 7} \text{ (putting } \pi = \frac{22}{7} \text{)}$$

$$\Rightarrow \text{Area of semicircle} = 11 \times 175$$

$$\therefore \text{Area of semicircle} = 1925 \text{ cm}^2 \rightarrow \text{eqn2}$$

$$\text{Area of rectangle} = l \times b \text{ ( } l \text{ = length of rectangle, } b \text{ = breadth of rectangle)}$$

$$\Rightarrow \text{Area of rectangle} = 80 \times 70 = 5600 \text{ cm}^2 \rightarrow \text{eqn3}$$

$$\text{Area of shaded region} = \text{Area of rectangle} - \text{Area of semicircle} - \text{Area of } \Delta$$

$$\Rightarrow \text{Area of shaded region} = 5600 - 1925 - 1176 \text{ (from eqn1, eqn2 and eqn3)}$$

$$\therefore \text{Area of shaded region} = 2499 \text{ cm}^2$$

Area of the shaded region is 2499 cm<sup>2</sup>.

### Question: 45

Here in order to find the area of the shaded region (region excluding the triangle) we have to subtract the area of the triangle from the area of the rectangle and then add the area of the semicircle.

Given AB = 20 cm, DE = 12 cm, AE = 9 cm and  $\angle AED = 90^\circ$

Here we see that the triangle AED is right angle triangle, therefore, we can apply Pythagoras theorem i.e.

$$H^2 = P^2 + B^2 \text{ (pythagoras theorem)}$$

$$AD^2 = DE^2 + AE^2$$

$$AD^2 = DE^2 + AE^2$$

$$AD^2 = 12^2 + 9^2 \text{ (putting given values)}$$

$$\Rightarrow AD^2 = 144 + 81$$

$$\Rightarrow AD^2 = 225$$

$$\Rightarrow AD = \sqrt{225}$$

$$\therefore AD = 15 \text{ cm}$$

$$\text{Area of } \Delta AED = 1/2 \times AE \times DE$$

$$(\text{Area of triangle} = 1/2 \times \text{base} \times \text{height})$$

On putting values we get,

$$\text{Area of } \Delta AED = \frac{1}{2} \times 9 \times 12$$

$$\Rightarrow \text{Area of } \Delta AED = 9 \times 6$$

$$\therefore \text{Area of } \Delta AED = 54 \text{ cm}^2 \rightarrow \text{eqn1}$$

$$\text{Area of semicircle} = \frac{\pi R^2}{2}$$

$$\text{Here radius of semicircle} = BC/2 = 15/2$$

$$\Rightarrow R = 7.5 \text{ cm}$$

$$\therefore \text{Area of semicircle} = \frac{\pi \times 7.5^2}{2}$$

$$\text{Area of semicircle} = \frac{3.14 \times 56.25}{2} \text{ (putting } \pi = 3.14)$$

$$\Rightarrow \text{Area of semicircle} = 1.07 \times 56.25$$

$$\therefore \text{Area of semicircle} = 88.3125 \text{ cm}^2 \rightarrow \text{eqn2}$$

$$\text{Area of rectangle} = l \times b$$

$$(l = \text{length of rectangle}, b = \text{breadth of rectangle})$$

$$\Rightarrow \text{Area of rectangle} = 20 \times 15$$

$$(\text{putting the values of } l \text{ & } b)$$

$$\therefore \text{Area of rectangle} = 300 \text{ cm}^2 \rightarrow \text{eqn3}$$

$$\text{Area of shaded region} = \text{Area of rectangle} + \text{Area of semicircle} - \text{Area of } \Delta$$

$$\Rightarrow \text{Area of shaded region} = 300 + 88.3125 - 53 \text{ (from eqn1, eqn2, eqn3)}$$

$$\therefore \text{Area of shaded region} = 334.3125 \text{ cm}^2$$

$$\text{Area of shaded region is } 334.3125 \text{ cm}^2.$$

#### Question: 46

Here in order to find the area of the shaded region (region excluding the area of segment AC and quadrant OCD) can be calculated by subtracting the area of triangle and quadrant OBD from the area of the circle.

$$\text{Given } AC = 24 \text{ cm, } AB = 7 \text{ cm and } \angle BOD = 90^\circ$$

Here we see that the triangle ACB is right angle triangle, therefore, we can apply Pythagoras theorem i.e.

$$H^2 = P^2 + B^2 \text{ (pythagoras theorem)}$$

$$BC^2 = AC^2 + AB^2$$

$$\Rightarrow BC^2 = 24^2 + 7^2 \text{ (putting the given values)}$$

$$\Rightarrow BC^2 = 576 + 49$$

$$\Rightarrow BC^2 = 625$$

$$BC = \sqrt{625}$$

$$\therefore BC = 25 \text{ cm}$$

Area of  $\Delta ACB = 1/2 \times AB \times AC$  (Area of triangle =  $1/2 \times \text{base} \times \text{height}$ )

On putting values we get,

$$\text{Area of } \Delta ACB = \frac{1}{2} \times 7 \times 24$$

$$\Rightarrow \text{Area of } \Delta AED = 7 \times 12$$

$$\therefore \text{Area of } \Delta AED = 84 \text{ cm}^2 \rightarrow \text{eqn1}$$

Area of circle =  $\pi R^2$  ( $R$  = radius of circle)

$$\text{Here radius of circle} = \frac{BC}{2} = \frac{25}{2} \text{ (because ABCD is a rectangle)}$$

$$\Rightarrow R = 12.5 \text{ cm}$$

$$\therefore \text{Area of circle} = \pi \times 12.5^2$$

$$\Rightarrow \text{Area of circle} = 156.25 \times 3.14 \text{ (put } \pi = 3.14)$$

$$\therefore \text{Area of circle} = 490.625 \text{ cm}^2 \rightarrow \text{eqn2}$$

$$\text{Area of quadrant OBD} = \frac{\theta}{360} \times \pi R^2$$

$$\text{Area of quadrant OBD} = \frac{90}{360} \times \pi \times 12.5^2 \text{ (put } \pi = 3.14)$$

$$\text{Area of quadrant} = \frac{3.14 \times 156.25}{4}$$

$$\Rightarrow \text{Area of quadrant OBD} = 122.65625 \text{ cm}^2 \rightarrow \text{eqn3}$$

Area of shaded region = Area of circle - Area of quadrant - Area of  $\Delta$

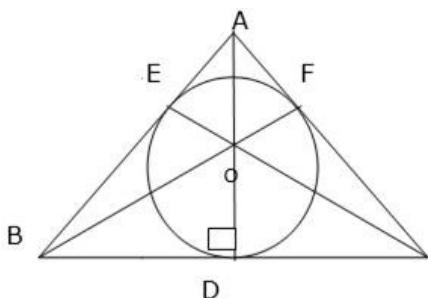
$$\Rightarrow \text{Area of shaded region} = 490.625 - 84 - 122.65625 \text{ (from eqn1, 2 and 3)}$$

$$\Rightarrow \text{Area of shaded region} = 283.96875 \text{ cm}^2$$

Area of shaded region is  $283.96875 \text{ cm}^2$ .

#### Question: 47

Here we will draw median from all the vertices of the equilateral triangle and the point at which they intersect will be the incircle of the triangle and that will be the centre of the circle. Then with the help of which we will find out the height of the triangle and subsequently the radius of the circle and ultimately the area of the shaded region (region of equilateral triangle excluding the area of circle inscribed).



As  $AD = BF = CE = h$

Consider  $\Delta ADB$ ,  $\angle ADB = 90^\circ$ ,  $BD = 6 \text{ cm}$

$$AB^2 = AD^2 + BD^2 \text{ (Phythagoras theorem)}$$

$$12^2 = AD^2 + 6^2 \text{ (putting the given values)}$$

$$144 = AD^2 + 36$$

$$144 - 36 = AD^2$$

$$AD^2 = 108$$

$$AD = \sqrt{108}$$

$$AD = \sqrt{9 \times 3 \times 4}$$

$$AD = 6\sqrt{3} \text{ cm}$$

$$\text{so, } h = 6\sqrt{3} \text{ cm}$$

We also know that a point O will divide each median in a ratio of 2:1

$$\text{So, } OD = \frac{h}{3}$$

$$OD = \frac{6\sqrt{3}}{3}$$

$$OD = 2\sqrt{3} \text{ cm}$$

$$\therefore \text{radius of the circle} = r = 2\sqrt{3} \text{ cm}$$

$$\text{Area of the circle} = \pi r^2$$

$$\text{Area of the circle} = \pi \times (2\sqrt{3})^2 \text{ (putting the value of } r)$$

$$\therefore \text{Area of the circle} = 12\pi \text{ cm}^2 \rightarrow \text{eqn1}$$

$$\text{Area of } \Delta ABC = \frac{\sqrt{3}}{4} \times a^2 \text{ where } a = \text{side of equilateral triangle}$$

$$\text{Area of } \Delta ABC = \frac{\sqrt{3}}{4} \times 12^2$$

$$\text{Area of } \Delta ABC = \frac{144 \times \sqrt{3}}{4}$$

$$\text{Area of } \Delta ABC = 36\sqrt{3} \text{ cm}^2 \rightarrow \text{eqn2}$$

$$\text{Area of shaded region} = \text{area of triangle} - \text{area of circle}$$

$$\text{Area of the shaded region} = 36\sqrt{3} - 12\pi \text{ (put } \pi = 3.14 \text{ & } \sqrt{3} = 1.73)$$

$$\Rightarrow \text{Area of the shaded region} = (36 \times 1.73) - (12 \times 3.14)$$

$$\Rightarrow \text{Area of the shaded region} = 62.28 - 37.68$$

$$\therefore \text{Area of the shaded region} = 24.6 \text{ cm}^2$$

The radius of the circle is  $2\sqrt{3}$  cm and area of shaded region is  $24.6 \text{ cm}^2$ .

#### Question: 48

Here we will first find the sides of equilateral triangle and then subtract the area of the triangle from the area of the circle.

Given radius of circle =  $r = 42 \text{ cm}$

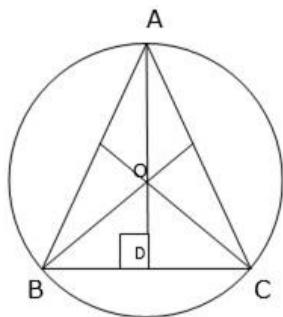
$$\therefore \text{Area of the circle} = \pi R^2, \text{ where } R = \text{radius of the circle}$$

$$\Rightarrow \text{Area of the circle} = \pi(42^2)$$

$$\therefore \text{Area of circle} = \frac{22}{7} \times 1764 \left(\text{putting } \pi = \frac{22}{7}\right)$$

$\Rightarrow$  Area of the circle =  $22 \times 252$

$\therefore$  Area of the circle =  $5544 \text{ cm}^2 \rightarrow \text{eqn1}$



Consider the figure shown,

In  $\triangle ABD$ ,  $\angle ADB = 90^\circ$

$$\therefore AB^2 = AD^2 + BD^2 \rightarrow \text{eqn2 (Pythagoras theorem)}$$

Let the sides of the equilateral triangle = a cm

And as we know AD is a median therefore it will bisect the side BC into two equal parts i.e.

$$BD = DC \rightarrow \text{eqn3}$$

$$\text{Also, } BC = BD + DC$$

$$\Rightarrow BC = BD + BD \text{ (from eqn3)}$$

$$\Rightarrow a = 2BD \text{ (BC = a)}$$

$$BD = \frac{a}{2} \text{ cm}$$

$$\text{So, } a^2 = AD^2 + \left(\frac{a}{2}\right)^2 \text{ (putting values of AC and BD in eqn2)}$$

$$\Rightarrow a^2 = AD^2 + \frac{a^2}{4}$$

$$\Rightarrow a^2 - \frac{a^2}{4} = AD^2$$

$$\Rightarrow \frac{4a^2 - a^2}{4} = AD^2$$

$$\Rightarrow \frac{3a^2}{4} = AD^2$$

$$\Rightarrow AD = \sqrt{\frac{3a^2}{4}}$$

$$\Rightarrow AD = \frac{a\sqrt{3}}{2} \text{ cm} \rightarrow \text{eqn4}$$

Now, we also know that the point 'O' which is the intersection of all the three medians i.e. centroid of the triangle. Also we know that the centroid divides the median in the ratio 2:1.

$$\text{So, we can say that } AO = \frac{2AD}{3}$$

Also, we know  $AO = \text{radius} = r = 42 \text{ cm}$

$$\therefore 42 = \frac{2AD}{3}$$

$$\Rightarrow \frac{42 \times 3}{2} = AD$$

$$\Rightarrow AD = 63 \text{ cm}$$

Putting the value in equation 4,

$$63 = \frac{a\sqrt{3}}{2}$$

$$\Rightarrow \frac{63 \times 2}{\sqrt{3}} = a$$

$$\Rightarrow \frac{126}{\sqrt{3}} = a$$

$$\Rightarrow \frac{126 \times \sqrt{3}}{\sqrt{3} \times \sqrt{3}} = a \text{ (rationalizing L.H.S)}$$

$$\Rightarrow \frac{126\sqrt{3}}{3} = a$$

$$\Rightarrow a = 42\sqrt{3} \text{ cm}$$

$$o, \text{area of equilateral triangle } ABC = \frac{\sqrt{3}}{4} \times a^2 \text{ (where } a = \text{ side of triangle)}$$

$$\Rightarrow \text{Area of triangle } ABC = \frac{\sqrt{3}}{4} \times (42\sqrt{3})^2 \text{ (putting the value of } a)$$

$$\Rightarrow \text{Area of triangle } ABC = \frac{\sqrt{3}}{4} \times (1764 \times 3)$$

$$\Rightarrow \text{Area of triangle } ABC = \frac{\sqrt{3}}{4} \times 5292$$

$$\Rightarrow \text{Area of triangle } ABC = 1323\sqrt{3} \text{ cm}^2 \rightarrow \text{eqn5}$$

Area of covered by design = Area of circle - Area of triangle ABC

$$\text{Area covered by design} = 5544 - 1323\sqrt{3} \text{ (from eqn1 and eqn5)}$$

$$\Rightarrow \text{Area covered by design} = 5544 - (1323 \times 1.73) \text{ (putting } \sqrt{3} = 1.73)$$

$$\Rightarrow \text{Area covered by design} = 5544 - 2288.79$$

$$\therefore \text{Area covered by design} = 3255.21 \text{ cm}^2$$

Area covered by design is 3255.21 cm<sup>2</sup>.

### Question: 49

We know perimeter of a sector = Length of its arc + 2R → eqn1

Where R = radius of the sector.

Perimeter = 25 cm

$$\text{Also, length of arc of sector} = \frac{\theta}{360} \times 2\pi R$$

$$\theta = 90^\circ$$

$$\therefore 25 = \frac{90}{360} \times 2\pi R + 2R \text{ (putting the values in eqn1)}$$

$$\Rightarrow 25 = \frac{2\pi R}{4} + 2R$$

$$\Rightarrow 25 = \frac{\pi R}{2} + 2R$$

$$\Rightarrow 25 = \frac{\pi R + 4R}{2} \text{ (taking 2 as L.C.M on R.H.S)}$$

$$\Rightarrow 25 \times 2 = (\pi + 4)R \text{ (taking R common)}$$

$$\Rightarrow 50 = \left(\frac{22}{7} + 4\right)R \text{ (putting } \pi = \frac{22}{7})$$

$$\Rightarrow 50 = \left(\frac{22 + 28}{7}\right)R \text{ (taking 7 as L.C.M on R.H.S)}$$

$$\Rightarrow 50 \times 7 = 50R$$

$$\Rightarrow \frac{50 \times 7}{50} = R$$

$$\Rightarrow R = 7 \text{ cm} \rightarrow \text{eqn2}$$

$$\text{Area of a sector} = \frac{\theta}{360} \times \pi R^2$$

$$\Rightarrow \text{Area of quadrant} = \frac{90}{360} \times \pi(7^2) \text{ (putting the value of } \theta \text{ and } R)$$

$$\Rightarrow \text{Area of the quadrant} = \frac{49\pi}{4} \text{ (put } \pi = \frac{22}{7})$$

$$\Rightarrow \text{Area of the quadrant} = \frac{49 \times 22}{4 \times 7}$$

$$\Rightarrow \text{Area of the quadrant} = \frac{7 \times 11}{2}$$

$$\therefore \text{Area of the quadrant} = 38.5 \text{ cm}^2$$

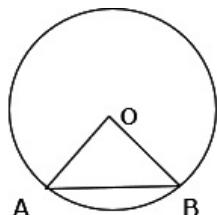
Area of the quadrant is  $38.5 \text{ cm}^2$ .

### Question: 50

Given the radius of the circle = 42 cm

Central angle of the sector =  $\theta = 90^\circ$

Area of the minor segment = Area of sector - area of the right angle triangle



$$\text{Area of the sector} = \frac{\theta}{360} \times \pi R^2$$

$$\text{Area of the sector} = \frac{90}{360} \times \pi(10^2) \text{ (putting the values of } \theta \text{ and } R)$$

$$\Rightarrow \text{Area of the sector} = \frac{100\pi}{4} \text{ (put } \pi = 3.14)$$

$$\Rightarrow \text{Area of the sector} = \frac{100 \times 3.14}{4}$$

$$\Rightarrow \text{Area of the sector} = 25 \times 3.14$$

$$\therefore \text{Area of the sector} = 78.5 \text{ cm}^2 \rightarrow \text{eqn1}$$

$$\text{Area of triangle} = \frac{1}{2} \times \text{base} \times \text{height}$$

$$\Rightarrow \text{Area of triangle} = \frac{1}{2} \times 10 \times 10$$

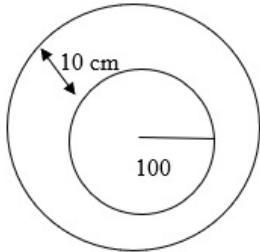
$$\therefore \text{Area of triangle} = 50 \text{ cm}^2 \rightarrow \text{eqn2}$$

$$\text{Area of the minor segment} = 78.5 - 50 \text{ (from eqn1, eqn2)}$$

$$\therefore \text{Area of the minor segment} = 28.5 \text{ cm}^2$$

Area of the minor segment is  $28.5 \text{ cm}^2$ .

### **Question: 51**



Here we will first find out the area of the road running around the circular garden and then multiplying it with rate per square meter to calculate the cost of leveling.

Here we see in the figure there are two concentric circles so,

$$\text{Area of road} = \text{Area of outer circle} - \text{Area of circular garden}$$

$$\text{Area of circle} = \pi R^2 \text{ (where } R = \text{radius of circle)} \rightarrow \text{eqn1}$$

$$\text{Let the radius of inner circle} = r = 100 \text{ m}$$

$$\text{Also, radius of outer circle} = R = 110 \text{ m} \text{ (} R = r + 10 \text{)}$$

$$\text{Area of outer circle} = \pi(110)^2 \rightarrow \text{eqn2 (putting } R \text{ in eqn1)}$$

$$\text{Area of inner circle} = \pi(100)^2 \rightarrow \text{eqn2 (putting } r \text{ in eqn1)}$$

$$\therefore \text{Area of road} = \pi(110)^2 - \pi(100)^2 \text{ (from eqn2 and 3)}$$

$$\Rightarrow \text{Area of road} = \pi(12100 - 10000)$$

$$\Rightarrow \text{Area of road} = 2100 \pi \text{ (put } \pi = 3.14)$$

$$\Rightarrow \text{Area of road} = 2100 \times 3.14$$

$$\therefore \text{Area of road} = 6594 \text{ m}^2$$

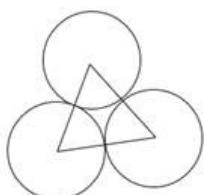
$$\text{Cost of leveling} = \text{Rate of leveling} \times \text{Area of road}$$

$$\Rightarrow \text{Cost of leveling} = 20 \times 6594$$

$$\therefore \text{Cost of leveling} = \text{Rs.}131880$$

Area of road is  $6594 \text{ m}^2$  and cost of leveling is  $\text{Rs.}131880$ .

### **Question: 52**



$$\text{Area of equilateral triangle} = 49\sqrt{3} \text{ cm}^2$$

$$\text{Each angle of triangle} = \theta = 60^\circ$$

Area of triangle not included in circles = Area of triangle - Area of all sectors

Area of all 3 sectors area equal as all the three circles are having same radius which is equal to the half of the side of the equilateral triangle.

Let the side of equilateral triangle be = a cm

$$\text{also, area of equilateral triangle} = \frac{\sqrt{3}}{4} \times a^2 \quad (a = \text{side of triangle})$$

$$49\sqrt{3} = \frac{\sqrt{3}}{4} \times a^2 \quad (\text{equating the value of area to the above equation})$$

$$\Rightarrow \frac{49\sqrt{3} \times 4}{\sqrt{3}} = a^2$$

$$\Rightarrow a^2 = 49 \times 4$$

$$\Rightarrow a = \sqrt{49 \times 4}$$

$$\Rightarrow a = 7 \times 2$$

$$\Rightarrow a = 14 \text{ cm}$$

So radius of the circles = 7 cm

$$\text{Area of sector} = \frac{\theta}{360} \times \pi R^2$$

$$\text{Area of sector} = \frac{60}{360} \times \pi(7)^2$$

$$\text{Area of sector} = \frac{22 \times 49}{6 \times 7} \left(\text{put } \pi = \frac{22}{7}\right)$$

$$\text{Area of sector} = \frac{11 \times 7}{3}$$

$$\text{Area of sector} = \frac{77}{3} \text{ cm}^2$$

Area of 3 sector = 3 × area of one sector

$$\text{Area of 3 sector} = 3 \times \frac{77}{3}$$

∴ Area of all 3 sectors = 77 cm<sup>2</sup> → eqn1

Area of triangle not included in circles

$$= 49\sqrt{3} - 77 \quad (\text{putting value of area of triangle and sector})$$

$$\text{Area of triangle not included} = (49 \times 1.73) - 77$$

$$\Rightarrow \text{Area of triangle not included} = 84.77 - 77$$

$$\therefore \text{Area of triangle not included} = 7.77 \text{ cm}^2$$

Area of triangle not included in circles is 7.77 cm<sup>2</sup>.

### Question: 53

Area of whole figure = ar || ABCD + ar || FGHI + ar DCIF + ar ΔDEF + area semicircle

CD = 8 cm, BP = HQ = 4 cm, DE = EF = 5 cm, CI = 8 cm

ar || ABCD = ar || FGHI = base × height

ar || ABCD = ar || FGHI = BP × DC

ar || ABCD = ar || FGHI = 4 × 8

ar || ABCD = ar || FGHI = 32 cm<sup>2</sup> → eqn1 and eqn2

ar DCIF = area of square = side×side

ar DCIF = DC×CI

ar DCIF = 8×8

ar DCIF = 64 cm<sup>2</sup>→ eqn3

Consider ΔDEF, EF⊥DF and ΔDEF is isosceles

So, FL = LD

$$FL = LD = \frac{DF}{2}$$

$$FL = LD = \frac{8}{2}$$

$$FL = LD = 4 \text{ cm}$$

In ΔDEL, ∠DLE = 90°

$$ED^2 = EL^2 + LD^2 \text{ (Pythagoras theorem)}$$

$$5^2 = EL^2 + 4^2 \text{ (putting the values)}$$

$$25 = EL^2 + 16$$

$$25 - 16 = EL^2$$

$$\Rightarrow EL^2 = 9$$

$$EL = \sqrt{9}$$

$$\therefore EL = 3 \text{ cm}$$

$$\text{Area of } \Delta \text{ DEF} = \frac{1}{2} \times \text{base} \times \text{height}$$

$$\text{Area of } \Delta \text{DEF} = \frac{1}{2} \times DF \times EL$$

$$\text{Area of } \Delta \text{DEF} = \frac{1}{2} \times 8 \times 3$$

$$\Rightarrow \text{Area of } \Delta \text{DEF} = 4 \times 3$$

$$\therefore \text{Area of } \Delta \text{DEF} = 12 \text{ cm}^2 \rightarrow \text{eqn4}$$

$$\text{Area of semicircle} = \frac{\pi R^2}{2} \text{ where } R = \text{radius of the semicircle}$$

$$R = 4 \text{ cm}$$

$$\text{Area of semicircle} = \frac{\pi(4)^2}{2} \text{ (put } \pi = 3.14)$$

$$\text{Area of semicircle} = \frac{3.14 \times 16}{2}$$

$$\Rightarrow \text{Area of semicircle} = 3.14 \times 8$$

$$\therefore \text{Area of semicircle} = 25.12 \text{ cm}^2 \rightarrow \text{eqn5}$$

$$\text{Area of whole figure} = \text{eqn1} + \text{eqn2} + \text{eqn3} + \text{eqn4} + \text{eqn5}$$

$$\Rightarrow \text{Area of whole figure} = 32 + 32 + 64 + 12 + 25.12$$

$$\therefore \text{Area of whole figure} = 165.12 \text{ cm}^2$$

Area of the whole figure is 165.12 cm<sup>2</sup>.

**Question: 54**

$$A \theta_1 = 90^\circ, \theta_2 = 120^\circ, \theta_3 = 150^\circ$$

Radius of circle =  $r = 6 \text{ cm}$

$$\text{Area of sector} = \frac{\theta}{360} \times \pi R^2 \rightarrow \text{eqn1}$$

$$\text{Area of circle} = \pi R^2$$

$$\Rightarrow \text{Area of circle} = \pi \times 6^2$$

$$\Rightarrow \text{Area of circle} = 36\pi \rightarrow \text{eqn2}$$

$$\text{Area of sector}(\theta_3) = \frac{150}{360} \pi \times 6^2 \text{ (from eqn1)}$$

$$\text{Area of sector}(\theta_3) = \frac{15\pi}{36} \times 36$$

$$\text{Area of sector}(\theta_3) = \frac{15}{36} \times 36\pi$$

$$\text{Area of sector}(\theta_3) = \frac{15}{36} \times \text{Area of circle} \text{ (from eqn2)}$$

$$\text{Area of sector}(\theta_3) = \frac{5}{12} \times \text{Area of circle}$$

$$\text{Also, Area of sector}(\theta_3) = 15\pi \text{ cm}^2$$

$$\text{Area of sector}(\theta_2) = \frac{120}{360} \times \pi 6^2 \text{ (putting values in eqn 1)}$$

$$\text{Area of sector}(\theta_2) = \frac{12}{36} \times 36\pi$$

$$\text{Area of sector}(\theta_2) = 12\pi \text{ cm}^2 \rightarrow \text{eqn3}$$

$$\text{Area of sector}(\theta_1) = \frac{90}{360} \times \pi 6^2 \text{ (putting values in eqn 1)}$$

$$\text{Area of sector}(\theta_1) = \frac{9}{36} \times 36\pi$$

$$\text{Area of sector}(\theta_1) = 9\pi \text{ cm}^2 \rightarrow \text{eqn4}$$

Ratio of three sectors ::  $9\pi : 12\pi : 15\pi$

Ratio of three sectors :: 3:4:5

$$\text{Area of sector}(\theta_3) \text{ is } \frac{5}{12} \times \text{Area of circle} \text{ and Ratio of three sectors :: 3 : 4 : 5}$$

### Question: 55

Total area of design = Area of all the minor segments

Here we will find out the area of one segment and then multiply it with 6 to get the total area of design. And as the figure inscribed in the circle is a regular hexagon this implies that it will be having all edges of same length. Therefore we can say that the angle subtended by each chord which are actually the edges of regular hexagon are equal(theorem).

Let angle subtended by chord AB on centre O be  $\theta$

$$\text{So, angle subtended} = \theta = \frac{360}{6}$$

$$\therefore \text{Angle subtended} = \theta = 60^\circ$$

$$\text{Radius of circle} = 35 \text{ cm}$$

$$\text{Area of sector} = \frac{\theta}{360} \times \pi R^2 \rightarrow \text{eqn1}$$

$$\text{Area of one sector} = \frac{60}{360} \times \pi(35)^2 \text{ (putting values in eqn1)}$$

$$\text{Area of one sector} = \frac{1225\pi}{6} \text{ cm}^2$$

$$\text{Area of } \Delta OAB = \frac{1}{2} \times OA \times OB \times \sin \theta \text{ (where } \theta = \text{ central angle of sector)}$$

$$\text{Area of } \Delta OAB = \frac{1}{2} \times 35 \times 35 \times \sin 60$$

$$\text{Area of } \Delta OAB = \frac{1}{2} \times 1225 \times \frac{\sqrt{3}}{2} \left( \sin 60 = \frac{\sqrt{3}}{2} \right)$$

$$\text{Area of } \Delta OAB = \frac{1225\sqrt{3}}{4} \text{ cm}^2$$

$$\text{Area of minor segment OAB} = \text{Area of sector} - \text{Area of } \Delta OAB$$

$$\text{Area of minor segment OAB}$$

$$= \frac{1225\pi}{6} - \frac{1225\sqrt{3}}{4} \text{ (put } \pi = 3.14 \text{ & } \sqrt{3} = 1.732)$$

$$\text{Area of minor segment OAB} = \frac{1225 \times 3.14}{6} - \frac{1225 \times 1.732}{4}$$

$$\text{Area of minor segment OAB} = \frac{3846.5}{6} - \frac{2121.7}{4}$$

$$\text{Area of minor segment OAB} = 641.0833333 - 530.425$$

$$\therefore \text{Area of minor segment OAB} = 110.6583333 \text{ cm}^2 \rightarrow \text{eqn2}$$

$$\text{Total area of design} = 6 \times \text{Area of minor segment OAB}$$

$$\Rightarrow \text{Total area of design} = 6 \times 110.6583333 \text{ (from eqn2)}$$

$$\therefore \text{Total area of design} = 663.95 \text{ cm}^2$$

$$\text{Total area of design is } 663.95 \text{ cm}^2.$$

### Question: 56

Here we will subtract the area of right angle triangle PQR and semicircle from the area of entire circle.

Given PQ = 24 cm, PR = 7 cm

Consider  $\Delta PQR$ ,  $\angle QPR = 90^\circ$

$$RQ^2 = PQ^2 + PR^2 \text{ (Pythagoras theorem)}$$

$$RQ^2 = 24^2 + 7^2$$

$$\Rightarrow RQ^2 = 576 + 49$$

$$\Rightarrow RQ^2 = 625$$

$$\Rightarrow RQ = \sqrt{625}$$

$$\therefore RQ = 25 \text{ cm}$$

Therefore Radius of the circle = half of RQ

Let radius be 'r'

$$r = \frac{25}{2}$$

$\therefore r = 12.5 \text{ cm}$

$$\text{Area } \Delta PQR = \frac{1}{2} \times \text{base} \times \text{height}$$

$$\text{Area of } \Delta PQR = \frac{1}{2} \times PR \times PQ$$

$$\text{Area of } \Delta PQR = \frac{1}{2} \times 7 \times 24$$

$$\text{Area of } \Delta PQR = 7 \times 12$$

$$\therefore \text{Area of } \Delta PQR = 84 \text{ cm}^2 \rightarrow \text{eqn1}$$

$$\text{Area of semicircle} = \frac{\pi r^2}{2}$$

$$\text{Area of semicircle} = \frac{3.14 \times (12.5^2)}{2} \text{ (putting } \pi = 3.14)$$

$$\text{Area of semicircle} = \frac{3.14 \times 156.25}{2}$$

$$\therefore \text{Area of semicircle} = 245.3125 \text{ cm}^2 \rightarrow \text{eqn2}$$

$$\text{Area of circle} = \pi r^2$$

$$\text{Area of circle} = \pi(12.5^2)$$

$$\Rightarrow \text{Area of circle} = 3.14 \times 156.25 \text{ (putting } \pi = 3.14)$$

$$\therefore \text{Area of circle} = 490.625 \text{ cm}^2 \rightarrow \text{eqn3}$$

$$\text{Area of shaded region} = \text{eqn3} - \text{eqn2} - \text{eqn1}$$

$$\Rightarrow \text{Area of shaded region} = 490.625 - 245.3125 - 84$$

$$\therefore \text{Area of shaded region} = 161.3125 \text{ cm}^2$$

Area of shaded region is 161.3125 cm<sup>2</sup>.

### Question: 57

Given AB = 6 cm, BC = 10 cm

Consider  $\triangle ABC$ ,  $\angle BAC = 90^\circ$

$$BC^2 = AB^2 + AC^2 \text{ (Pythagoras theorem)}$$

$$\Rightarrow 10^2 = 6^2 + AC^2 \text{ (putting given values)}$$

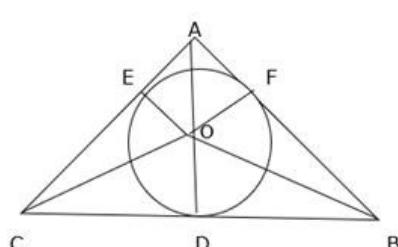
$$\Rightarrow 100 = 36 + AC^2$$

$$\Rightarrow 100 - 36 = AC^2$$

$$\Rightarrow AC^2 = 64$$

$$AC = \sqrt{64}$$

$$\therefore AC = 8 \text{ cm}$$



Join OB, OA, OC, OE, OF, OD

Here  $OE = OF = OD$  = radius of circle =  $r$  cm

$\angle OEC = \angle ODB = \angle OFB = 90^\circ$  (angle at the point of contact of radius & tangent)

Area  $\Delta ABC$  = Area of  $\Delta OAC$  + Area of  $\Delta OCB$  + Area of  $\Delta OAB \rightarrow$  eqn1

$$\text{Area of } \Delta OAC = \frac{1}{2} \times OE \times AC$$

$$\text{Area of } \Delta OAC = \frac{1}{2} \times r \times 8$$

$\therefore$  Area of  $\Delta OAC = 4r \rightarrow$  eqn2

$$\text{Area of } \Delta OCB = \frac{1}{2} \times OD \times BC$$

$$\text{Area of } \Delta OCB = \frac{1}{2} \times r \times 10$$

$\therefore$  Area of  $\Delta OCB = 5r \rightarrow$  eqn3

$$\text{Area of } \Delta OAB = \frac{1}{2} \times OF \times AB$$

$$\text{Area of } \Delta OAB = \frac{1}{2} \times r \times 6$$

$\therefore$  Area of  $\Delta OAB = 3r \rightarrow$  eqn4

$$\text{Area of } \Delta ABC = \frac{1}{2} \times AB \times AC$$

$$\text{Area of } \Delta ABC = \frac{1}{2} \times 6 \times 8$$

$\Rightarrow$  Area of  $\Delta ABC = 3 \times 8$

$\therefore$  Area of  $\Delta ABC = 24 \text{ cm}^2 \rightarrow$  eqn5

Putting all the values in equation we get;

$$\Rightarrow 24 = 4r + 5r + 3r$$

$$\Rightarrow 24 = 12r$$

$$r = \frac{24}{12}$$

$$\therefore r = 2 \text{ cm}$$

$$\text{Area of circle} = \pi r^2$$

Put the value of  $r$ , we get,

$$\Rightarrow \text{Area of circle} = \pi \times 2^2$$

$$\Rightarrow \text{Area of circle} = 3.14 \times 4 \text{ (putting } \pi = 3.14\text{)}$$

$$\therefore \text{Area of circle} = 12.56 \text{ cm}^2 \rightarrow \text{eqn6}$$

Area of shaded region = Area of triangle - Area of circle

$$\Rightarrow \text{Area of shaded region} = 24 - 12.56 \text{ (from eqn5 and eqn6)}$$

$$\therefore \text{Area of shaded region} = 11.44 \text{ cm}^2$$

Area of shaded region is  $11.44 \text{ cm}^2$ .

### Question: 58

Here we will first find out the area of semicircle whose diameter is BC and then subtract the area of right angle triangle ABC from it and then we will subtract this result from the area of semicircles whose diameters are AB and AC.

Consider  $\triangle ABC$ ,  $\angle BAC = 90^\circ$

$$BC^2 = AC^2 + AB^2 \text{ (Pythagoras theorem)}$$

$$\Rightarrow BC^2 = 4^2 + 3^2$$

$$\Rightarrow BC^2 = 16 + 9$$

$$\Rightarrow BC^2 = 25$$

$$BC = \sqrt{25}$$

$$\therefore BC = 5 \text{ cm}$$

$$\text{Area of semicircle} = \frac{\pi r^2}{2} \rightarrow \text{eqn1 where } r = \text{radius of the semicircle}$$

Area of semicircle whose diameter is AC

$$\text{Radius} = \frac{AC}{2}$$

$$\text{Radius} = \frac{4}{2}$$

$$\therefore \text{Radius} = 2 \text{ cm}$$

$$\text{Area of semicircle} = \frac{\pi(2)^2}{2} \text{ (from eqn1)}$$

$$\therefore \text{Area of semicircle} = 2\pi \text{ cm}^2 \rightarrow \text{eqn2}$$

Area of semicircle whose diameter is AB

$$\text{Radius} = \frac{AB}{2}$$

$$\text{Radius} = \frac{3}{2}$$

$$\therefore \text{Radius} = 1.5 \text{ cm}$$

$$\text{Area of semicircle} = \frac{\pi(1.5)^2}{2} \text{ (from eqn1)}$$

$$\therefore \text{Area of semicircle} = 1.125\pi \text{ cm}^2 \rightarrow \text{eqn3}$$

Area of semicircle whose diameter is BC

$$\text{Radius} = \frac{BC}{2}$$

$$\text{Radius} = \frac{5}{2}$$

$$\therefore \text{Radius} = 2.5 \text{ cm}$$

$$\text{Area of semicircle} = \frac{\pi(2.5)^2}{2} \text{ (from eqn1)}$$

$$\therefore \text{Area of semicircle} = 3.125\pi \text{ cm}^2 \rightarrow \text{eqn4}$$

$$\text{Area of triangle PQR} = \frac{1}{2} \times AB \times AC$$

$$\text{Area of triangle PQR} = \frac{1}{2} \times 3 \times 4$$

$$\Rightarrow \text{Area of triangle PQR} = 3 \times 2$$

$$\therefore \text{Area of triangle PQR} = 6 \text{ cm}^2 \rightarrow \text{eqn5}$$

Now subtract equation 5 from equation 4,

$\Rightarrow$  Area of semicircle excluding  $\Delta ABC = \text{eqn4} - \text{eqn5}$

$\Rightarrow$  Area of semicircle excluding  $\Delta ABC = 3.125\pi - 6$

$$\Rightarrow \text{Area of semicircle excluding } \Delta ABC = 3.125 \times \frac{22}{7} - 6 \text{ cm}^2$$

$$\Rightarrow \text{Area of semicircle excluding } \Delta ABC = \frac{3.125 \times 22}{7} - 6$$

$$\Rightarrow \text{Area of semicircle excluding } \Delta ABC = \frac{68.75 - 42}{7}$$

$$\Rightarrow \text{Area of semicircle excluding } \Delta ABC = \frac{26.75}{7}$$

$\therefore$  Area of semicircle excluding  $\Delta ABC = 3.8214 \text{ cm}^2 \rightarrow \text{eqn6}$

Area of shaded region = eqn3 + eqn2 - eqn6

$\Rightarrow$  Area of shaded region =  $2\pi + 1.125\pi - 3.8214$

$\Rightarrow$  Area of shaded region =  $3.125\pi - 3.8214$

$$\text{Area of shaded region} = 3.125 \times \frac{22}{7} - 3.8214$$

$$\text{Area of shaded region} = \frac{68.75}{7} - 3.8214$$

$\Rightarrow$  Area of shaded region =  $9.8214 - 3.8214$

$\therefore$  Area of shaded region =  $6 \text{ cm}^2$

Area of shaded region  $6 \text{ cm}^2$ .

### Question: 59

Here we will subtract the area of semicircle whose diameter is QS from the area of the semicircle whose diameter PS and add the area of semicircle whose diameter is PQ so as to find out the area of the shaded region.

Given PS = 12 cm

Radius of the circle = 6 cm

PQ = QR = RS

So let PQ = QR = RS = k cm

Also, PQ + QR + RS = PS

$\Rightarrow k + k + k = 12$

$\Rightarrow 3k = 12$

$$k = \frac{12}{3}$$

$\therefore k = 4 \text{ cm}$

So, PQ = QR = RS = 4 cm

$$\text{Area of semicircle} = \frac{\pi r^2}{2} \rightarrow \text{eqn1 where } r = \text{radius of the semicircle}$$

Area and perimeter of semicircle whose diameter is PS

$$\text{Radius} = \frac{PS}{2}$$

$$\text{Radius} = \frac{12}{2}$$

∴ Radius = 6 cm

$$\text{Area of semicircle} = \frac{\pi(6)^2}{2} \text{ (from eqn1)}$$

∴ Area of semicircle =  $18\pi \text{ cm}^2 \rightarrow \text{eqn2}$

Perimeter of semicircle =  $\pi r$

⇒ Perimeter of semicircle =  $\pi \times 6$

∴ Perimeter of semicircle =  $6\pi \text{ cm} \rightarrow \text{eqn3}$

Area of semicircle whose diameter is QS

$$\text{Radius} = \frac{QS}{2}$$

$$\text{Radius} = \frac{8}{2}$$

⇒ Radius = 4 cm

$$\text{Area of semicircle} = \frac{\pi(4)^2}{2} \text{ (from eqn1)}$$

∴ Area of semicircle =  $8\pi \text{ cm}^2 \rightarrow \text{eqn4}$

Perimeter of semicircle =  $\pi r$

⇒ Perimeter of semicircle =  $\pi \times 4$

∴ Perimeter of semicircle =  $4\pi \text{ cm} \rightarrow \text{eqn5}$

Area of semicircle whose diameter is PQ

$$\text{Radius} = \frac{PQ}{2}$$

$$\text{Radius} = \frac{4}{2}$$

∴ Radius = 2 cm

$$\text{Area of semicircle} = \frac{\pi(2)^2}{2} \text{ (from eqn1)}$$

∴ Area of semicircle =  $2\pi \text{ cm}^2 \rightarrow \text{eqn6}$

Perimeter of semicircle =  $\pi r$

⇒ Perimeter of semicircle =  $\pi \times 2$

∴ Perimeter of semicircle =  $2\pi \text{ cm} \rightarrow \text{eqn7}$

Area of the shaded region = eqn2 - eqn4 + eqn6

Area of shaded region =  $18\pi - 8\pi + 2\pi$

⇒ Area of shaded region =  $12\pi$

⇒ Area of shaded region =  $12 \times 3.14$  (putting  $\pi = 3.14$ )

∴ Area of shaded region =  $37.68 \text{ cm}^2$

Perimeter of shaded region = eqn3 - eqn5 + eqn7

⇒ Perimeter of shaded region =  $6\pi - 4\pi + 2\pi$

⇒ Perimeter of shaded region =  $4\pi$

⇒ Perimeter of shaded region =  $4 \times 3.14$  (put  $\pi = 3.14$ )

∴ Perimeter of shaded region =  $12.56 \text{ cm}$

Perimeter of the shaded region is 12.56 cm and Area of shaded region is 37.68 cm<sup>2</sup>.

**Question: 60**

Consider the figure as a combination of two semicircles on the ends of the rectangle

Let the length of rectangle be 'L' m and breadth be 'B' cm

Given L = 90 m, W = 14 m

Perimeter of running track = 400 m

Perimeter of inside of running track = 2L + Arc of two semicircles → eqn1

Arc length of a semicircle =  $\pi r$  where r = radius

$$\Rightarrow 400 = (2 \times 90) + (2 \times \pi r) \text{ (putting values in eqn1)}$$

$$\Rightarrow 400 = 180 + 2\pi r$$

$$\Rightarrow 400 - 180 = 2\pi r$$

$$\Rightarrow 220 = 2\pi r$$

$$220 = 2 \times \frac{22}{7} \times r \left( \pi = \frac{22}{7} \right)$$

$$220 = \frac{44}{7} \times r$$

$$\frac{220 \times 7}{44} = r$$

$$\therefore r = 35 \text{ m}$$

Area of inner of running track = Area of rectangle + 2×area of semicircles → eqn2

Area of rectangle = L×B

Here B = 2r

B = 70 m

$$\Rightarrow \text{Area of inner rectangle} = 90 \times 70$$

$$\therefore \text{Area of inner rectangle} = 6300 \text{ m}^2 \rightarrow \text{eqn3}$$

$$\text{Area of inner semicircles} = 2 \times \frac{\pi r^2}{2}$$

$$\text{Area of inner semicircles} = 2 \times \frac{\pi (35)^2}{2}$$

$$\Rightarrow \text{Area of inner semicircles} = 1225\pi$$

$$\text{Area of inner semicircles} = 1225 \times \frac{22}{7}$$

$$\Rightarrow \text{Area of inner semicircle} = 175 \times 22$$

$$\therefore \text{Area of inner semicircle} = 3850 \text{ m}^2 \rightarrow \text{eqn4}$$

Area of inner of running track = 6300 + 3850 (from3&4)

$$\therefore \text{Area of inner of running track} = 10150 \text{ m}^2$$

Now radius of semicircles of outer of the running track = R = r + W

$$\Rightarrow R = 35 + 14$$

$$\therefore R = 49 \text{ m}$$

$$\text{Area of outer semicircles} = 2 \times \frac{\pi R^2}{2}$$

$$\text{Area of outer semicircles} = 2 \times \frac{\pi(49)^2}{2}$$

$$\Rightarrow \text{Area of outer semicircles} = 2401\pi$$

$$\Rightarrow \text{Area of outer semicircles} = 2401 \times \frac{22}{7}$$

$$\Rightarrow \text{Area of outer semicircles} = 343 \times 22$$

$$\therefore \text{Area of outer semicircle} = 7546 \text{ m}^2 \rightarrow \text{eqn5}$$

$$\text{Breadth of outer running track} = B' = 2R$$

$$\Rightarrow B' = 2 \times 49$$

$$\therefore B' = 98 \text{ m}$$

$$\text{Area of outer rectangle} = L \times B'$$

$$\Rightarrow \text{Area of outer rectangle} = 90 \times 98$$

$$\therefore \text{Area of outer rectangle} = 8820 \text{ m}^2 \rightarrow \text{eqn6}$$

$$\text{Area of entire ground} = 8820 + 7546 \text{ (from 5&6)}$$

$$\therefore \text{Area of entire ground} = 16366 \text{ m}^2$$

$$\text{Area of running track} = \text{Area of entire ground} - \text{Area of inner ground}$$

$$\Rightarrow \text{Area of running track} = 16366 - 10150$$

$$\therefore \text{Area of running track} = 6216 \text{ m}^2$$

$$\text{Perimeter of outer boundary} = 2L + \text{Arc of outer semicircles}$$

$$\text{Arc length of an outer semicircle} = \pi R, \text{ where } R = \text{outer radius}$$

**Perimeter of outer boundary**

$$= (2 \times 90) + \left( 2 \times \frac{22}{7} \times 49 \right) \text{ (putting values)}$$

$$\Rightarrow \text{Perimeter of outer boundary} = 180 + (2 \times 22 \times 7)$$

$$\Rightarrow \text{Perimeter of outer boundary} = 180 + 308$$

$$\therefore \text{Perimeter of outer boundary} = 488 \text{ m}$$

Area of running track is 6216 m<sup>2</sup> and perimeter of outer boundary is 488 m.

## **Exercise : MULTIPLE CHOICE QUESTIONS (MCQ)**

### **Question: 1**

Let the radius if circle be r

Given, Area of circle = 38.5 cm<sup>2</sup>

Area of circle =  $\pi r^2$

$$\Rightarrow \pi r^2 = 38.5$$

Since  $\pi = 22/7$

$$\Rightarrow 22/7 \times r^2 = 38.5$$

$$\Rightarrow r^2 = 38.5 \times (7/22)$$

$$\Rightarrow r^2 = 12.25$$

$$\Rightarrow r = \sqrt{12.25} = 3.5 \text{ cm}$$

$$\therefore \text{Radius of circle} = 3.5 \text{ cm}$$

Circumference of circle =  $2\pi r$

$$= 2 \times 22/7 \times 3.5 \text{ cm}$$

$$= 22 \text{ cm}$$

$\therefore$  Circumference of the circle is 22 cm

Let the radius if circle be  $r$

Given, Area of circle =  $38.5 \text{ cm}^2$

Area of circle =  $\pi r^2$

$$\pi r^2 = 38.5$$

$$\text{Since } = 22/7$$

$$\therefore \pi r^2 = 38.5$$

$$\Rightarrow 22/7 \times r^2 = 38.5$$

$$\Rightarrow r^2 = 12.25$$

$$\Rightarrow r = \sqrt{12.25} = 3.5 \text{ cm}$$

$\therefore$  Radius of circle = 3.5 cm

Circumference of circle =  $2\pi r$

$$= 2 \times 22/7 \times 3.5$$

$$= 22 \text{ cm}$$

$\therefore$  Circumference of the circle is 22 cm

### Question: 2

The area of a cir

### Solution:

Let the radius if circle be  $r$

Given, Area of circle =  $49\pi \text{ cm}^2$

Area of circle =  $\pi r^2$

$$\pi r^2 = 49\pi$$

$$\text{Since } = 22/7$$

$$\therefore \pi r^2 = 49\pi$$

$$\Rightarrow r^2 = 49$$

$$\Rightarrow r = \sqrt{49} = 7 \text{ cm}$$

$\therefore$  Radius of circle = 7 cm

Circumference of circle =  $2\pi r$

$$= 2 \times \pi \times 7 \text{ cm}$$

$$= 14\pi \text{ cm}$$

$\therefore$  Circumference of the circle is  $14\pi \text{ cm}$

### Question: 3

The difference be

### Solution:

Let the radius if circle be  $r$

Circumference of circle =  $2\pi r$

Difference between the circumference and radius of a circle = 37 cm

$$\Rightarrow 2\pi r - r = 37 \text{ cm}$$

$$\Rightarrow 2 \times 22/7 \times r - r = 37 \text{ cm}$$

$$\Rightarrow 44/7 \times r - r = 37 \text{ cm}$$

$$\Rightarrow (44/7 - 1) \times r = 37 \text{ cm}$$

$$\Rightarrow 37/7 \times r = 37 \text{ cm}$$

$$\Rightarrow r = 37 \times 7/37$$

$$\Rightarrow r = 7 \text{ cm}$$

Area of circle =  $\pi r^2$

$$= 22/7 \times 7 \times 7 \text{ cm}^2$$

$$= 22/7 \times 49 \text{ cm}^2 = 22 \times 7 \text{ cm}^2 = 154 \text{ cm}^2$$

$\therefore$  Area of the circle is  $154 \text{ cm}^2$

#### Question: 4

The perimeter of

#### Solution:

Let the radius of circular field be  $r$

Perimeter of circular field =  $2\pi r$

Perimeter of circular field = 242 m

$$\Rightarrow 2\pi r = 242 \text{ m}$$

$$\Rightarrow 2 \times 22/7 \times r = 242 \text{ m}$$

$$\Rightarrow r = 242 \times 1/2 \times 7/22 = 38.5 \text{ m}$$

$\therefore$  Radius of circular field = 38.5 m

Area of the field =  $\pi r^2$

$$= 22/7 \times 38.5^2 \text{ m}^2$$

$$= 22/7 \times 1482.5 \text{ m}^2 = 4658.5 \text{ m}^2$$

$\therefore$  Area of the field =  $4658.5 \text{ m}^2$

#### Question: 5

On increasing the

#### Solution:

Let the radius of circle be  $r$

Area of circle =  $A = \pi r^2$

Radius increases by 40%

So, New Radius  $r' = r + 40/100 \times r = 1.4r$

$$\text{New Area of circle} = A' = \pi r'^2 = \pi \times (1.4r)^2$$

$$= 1.96\pi r^2$$

$$\text{Percentage increase in area} = \frac{A' - A}{A} \times 100$$

$$= \frac{1.96\pi r^2 - \pi r^2}{\pi r^2} \times 100 = .96 \times 100 = 96$$

$\therefore$  Increase in area = 96%

### Question: 6

On decreasing the

#### Solution:

Let the radius if circle be  $r$

$$\text{Area of circle} = A = \pi r^2$$

Radius decreases by 30%

$$\text{So, New Radius } r' = r - 30/100 \times r = 0.7r$$

$$\text{New Area of circle} = A' = \pi r'^2 = \pi \times (0.7r)^2$$

$$= .49\pi r^2$$

$$\text{Percentage decrease in area} = \frac{A - A'}{A} \times 100$$

$$= \frac{\pi r^2 - .49\pi r^2}{\pi r^2} \times 100 = .51 \times 100 = 51$$

$\therefore$  Decrease in area = 51%

### Question: 7

The area of a square

#### Solution:

Let the length of the side of the square be  $a$

Let the radius if circle be  $r$

$$\text{Area of a square} = a^2$$

$$\text{Area of circle} = \pi r^2$$

Area of a square = Area of a circle

$$a^2 = \pi r^2$$

$$a = \sqrt{\pi} \times r$$

$$\text{Perimeter of circle} = 2\pi r$$

$$\text{Perimeter of square} = 4a$$

$$= 4\sqrt{\pi} r$$

$$\frac{\text{Perimeter of square}}{\text{Perimeter of circle}} = \frac{4\sqrt{\pi} r}{2\pi r}$$

$$\frac{\text{Perimeter of circle}}{\text{Perimeter of square}} = \frac{\sqrt{\pi}}{2}$$

$$\text{Ratio of perimeter of circle and square} = \sqrt{\pi} : 2$$

### Question: 8

The circumference

#### Solution:

Let the bigger circle be  $C_1$  and other circles be  $C_2$  and  $C_3$

$$\text{Radius of circle } C_1 = r_1$$

Diameter of circle  $C_2 = 36$  cm

Radius of circle  $C_2 = r_2 = 36/2$  cm = 18cm

Diameter of circle  $C_3 = 20$  cm

Radius of circle  $C_3 = r_3 = 20/2$  cm = 10 cm

Circumference of circle  $C_2 = 2\pi r_2$

$$= 2 \times \pi \times 18 \text{ cm} = 36\pi \text{ cm}$$

Circumference of circle  $C_3 = 2\pi r_3$

$$= 2 \times \pi \times 10 \text{ cm} = 20\pi \text{ cm}$$

Circumference of circle  $C_1$  = Circumference of circle  $C_2$  + Circumference of circle  $C_3$

$$\Rightarrow 2\pi r_1 = 2\pi r_2 + 2\pi r_3$$

$$\Rightarrow 2\pi r_1 = 36\pi + 20\pi$$

$$\Rightarrow 2\pi r_1 = 56\pi$$

$$\Rightarrow r_1 = 28 \text{ cm}$$

Radius of circle  $C_1 = r_1 = 28$  cm

### Question: 9

The area of a cir

### Solution:

Let the bigger circle be  $C_1$  and other circles be  $C_2$  and  $C_3$

Radius of circle  $C_1 = r_1$

Radius of circle  $C_2 = r_2 = 24$  cm

Radius of circle  $C_3 = r_3 = 7$  cm

Area of circle  $C_2 = \pi r_2^2$

$$= \pi \times 24^2 = 576\pi$$

Area of circle  $C_3 = \pi r_3^2$

$$= \pi \times 7^2 = 49\pi$$

Area of circle  $C_1$  = Area of circle  $C_2$  + Area of circle  $C_3$

$$\pi r_1^2 = \pi r_2^2 + \pi r_3^2$$

$$\pi r_1^2 = 576\pi + 49\pi$$

$$\pi r_1^2 = 625\pi$$

$$r_1 = 25 \text{ cm}$$

Diameter of new circle =  $25 \times 2$  cm = 50cm

### Question: 10

If the perimeter

### Solution:

Let the length of the side of the square be a

Let the radius if circle be r

Perimeter of circle =  $2\pi r$

Perimeter of square =  $4a$

Perimeter of circle = Perimeter of square

$$\Rightarrow 2\pi r = 4a$$

$$a = \pi \times r/2$$

Area of a square =  $a^2$

Area of circle =  $\pi r^2$

$$\frac{\text{Area of square}}{\text{Area of circle}} = \frac{a^2}{\pi r^2}$$

$$\frac{\text{Area of square}}{\text{Area of circle}} = \frac{\left(\frac{\pi r}{4}\right)^2}{\pi r^2}$$

$$\frac{\text{Area of square}}{\text{Area of circle}} = \frac{\pi^2 r^2}{4\pi r^2}$$

$$\frac{\text{Area of square}}{\text{Area of circle}} = \frac{\pi}{4}$$

Ratio of area of square to circle =  $\pi : 4$

### Question: 11

If the sum of the

#### Solution:

Let three circles be  $C_1$ ,  $C_2$  and  $C$

Area of circle  $C$  = Area of circle  $C_1$  + Area of circle  $C_2$

$$\pi R^2 = \pi R_1^2 + \pi R_2^2$$

$$R_1^2 + R_2^2 = R^2$$

### Question: 12

Let three circles be  $C_1$ ,  $C_2$  and  $C$

Circumference of circle  $C$  = Circumference of circle  $C_1$  + Circumference of circle  $C_2$

$$\Rightarrow 2\pi R = 2\pi R_1 + 2\pi R_2$$

$$R = R_1 + R_2$$

### Question: 13

If the circumference

#### Solution:

Let the length of the side of the square be  $a$

Let the radius of circle be  $r$

Perimeter of circle =  $2\pi r$

Perimeter of square =  $4a$

Perimeter of circle = Perimeter of square

$$2\pi r = 4a$$

$$a = \pi \times r/2$$

Area of a square =  $a^2$

$$= (\pi \times r/2)^2 = \pi/4 \times \pi r^2$$

Area of circle =  $\pi r^2$

Seeing the co-efficient of  $\pi r^2$

$$1 > \frac{\pi}{4} \therefore \pi r^2 > \frac{\pi}{4} \times \pi r^2$$

So, (area of the circle) > (area of the square)

**Question: 14**

The radii of two

**Solution:**



Radius of circle 1 =  $r_1 = 19$  cm

Radius of circle 2 =  $r_2 = 16$  cm

$$\text{Area of Ring} = \pi(r_1^2 - r_2^2)$$

$$= \pi(19^2 - 16^2) \text{ cm}^2$$

$$= 22/7 \times 105$$

$$= 330 \text{ cm}^2$$

**Question: 15**

The areas of two

**Solution:**

Let the radius of circle 1 & 2 be  $R_1$  and  $R_2$  respectively

$$\text{Area of circle 1} = 1386 \text{ cm}^2$$

$$\pi R_1^2 = 1386 \text{ cm}^2$$

$$22/7 \times R_1^2 = 1386 \text{ cm}^2$$

$$R_1^2 = 1386 \times 7/22 \text{ cm}^2 = 441 \text{ cm}^2$$

$$R_1 = 21 \text{ cm}$$

$$\text{Area of circle 2} = 962.5 \text{ cm}^2$$

$$\pi R_2^2 = 962.5 \text{ cm}^2$$

$$22/7 \times R_2^2 = 962.5 \text{ cm}^2$$

$$R_2^2 = 962.5 \times 7/22 \text{ cm}^2 = 306.25 \text{ cm}^2$$

$$R_2 = 17.5 \text{ cm}$$

$$\text{Width of the ring} = R_1 - R_2 = 21 - 17.5 = 3.5 \text{ cm}$$

**Question: 16**

The circumference

**Solution:**

$$\text{Circumference of circle } C_1 = 2\pi r_1$$

Circumference of circle C<sub>2</sub> = 2πr<sub>2</sub>

$$\frac{\text{Circumference of circle C1}}{\text{Circumference of circle C2}} = \frac{2\pi r_1}{2\pi r_2} = \frac{3}{4}$$

$$\frac{r_1}{r_2} = \frac{3}{4}$$

$$\frac{\text{Area of circle C1}}{\text{Area of circle C2}} = \frac{\pi r_1^2}{\pi r_2^2} = \frac{r_1^2}{r_2^2} = \left(\frac{3}{4}\right)^2 = \frac{9}{16}$$

∴ Ratio of two circles = 9: 16

### Question: 17

The areas of two

#### Solution:

$$\text{Area of circle C}_1 = \pi r_1^2$$

$$\text{Area of circle C}_2 = \pi r_2^2$$

$$\frac{\text{Area of circle C1}}{\text{Area of circle C2}} = \frac{\pi r_1^2}{\pi r_2^2} = \frac{r_1^2}{r_2^2} = \frac{9}{4}$$

$$\frac{r_1}{r_2} = \frac{3}{2}$$

$$\frac{\text{Circumference of circle C1}}{\text{Circumference of circle C2}} = \frac{2\pi r_1}{2\pi r_2} = \frac{r_1}{r_2} = \frac{3}{2}$$

Ratio of their circumferences = 3: 2

### Question: 18

The radius of a w

#### Solution:

$$\text{Radius of wheel} = r = 0.25 \text{ m}$$

$$\text{Distance the wheel travels} = 11 \text{ km} = 11000 \text{ m}$$

In 1 revolution wheel travels  $2\pi r$  distance

$$\text{No. of revolutions a wheel makes} = \frac{\text{distance travelled by the wheel}}{2\pi r}$$

$$= \frac{11000}{2\pi \times 0.25} = \frac{11000}{2 \times \frac{22}{7} \times 0.25} = \frac{11000 \times 7}{2 \times 22 \times 0.25}$$

$$= 7000 \text{ revolutions}$$

### Question: 19

The diameter of a

#### Solution:

$$\text{Diameter of wheel} = 40 \text{ cm}$$

$$\text{Radius of wheel} = r = 40/2 \text{ cm} = 20 \text{ cm}$$

$$\text{Distance the wheel travels} = 176 \text{ m} = 17600 \text{ cm}$$

In 1 revolution wheel travels  $2\pi r$  distance

$$\text{No. of revolutions a wheel makes} = \frac{\text{distance travelled by the wheel}}{2\pi r}$$

$$= \frac{17600}{2\pi \times 20} = \frac{17600}{2 \times \frac{22}{7} \times 20} = \frac{17600 \times 7}{2 \times 22 \times 20}$$

= 140 revolutions

### Question: 20

In making 1000 re

#### Solution:

Distance the wheel travels = 88 km = 88000 m

In 1 revolution wheel travels  $2\pi r$  distance

$$\text{No. of revolutions a wheel makes} = \frac{\text{distance travelled by the wheel}}{2\pi r}$$

No. of revolutions a wheel makes = 1000

$$r = \frac{\text{distance travelled by the wheel}}{2\pi \times \text{No. of revolutions a wheel makes}} = \frac{88000}{2 \times \frac{22}{7} \times 1000}$$
$$= \frac{88000 \times 7}{2 \times 22 \times 1000}$$

$$r = 14 \text{ m}$$

Radius of wheel = 14 m

Diameter of wheel =  $2 \times 14 \text{ m} = 28 \text{ m}$

### Question: 21

The area of a sec

#### Solution:

Area of a sector of angle  $\theta^\circ$  of a circle with radius R = area of circle  $\times \frac{\theta}{360}$

$$= \frac{\pi R^2 \theta}{360}$$

### Question: 22

The length of an

#### Solution:

Length of an arc of a sector of angle  $\theta^\circ$  of a circle with radius R

$$= \text{Circumference of circle} \times \frac{\theta}{360}$$

$$= \frac{2\pi R \theta}{360}$$

### Question: 23

The length of the

#### Solution:

Length of the minute hand of a clock = 21 cm

$$\therefore \text{Radius} = R = 21 \text{ cm}$$

In 1 minute, minute hand sweeps  $6^\circ$

So, in 10 minutes, minute hand will sweep  $10 \times 6^\circ = 60^\circ$

Area swept by minute hand in 10 minutes = Area of a sector of angle  $\theta^\circ$  of a circle with radius R

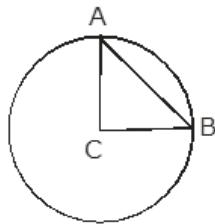
$$= \frac{\pi R^2 \theta}{360} = 22/7 \times 21 \times 21 \times 60/360 = 231 \text{ cm}^2$$

### Question: 24

A chord of a circle

**Solution:**

Radius of Circle = R = 10 cm



Area of minor Segment = Area of sector subtending 90° - Area of triangle ABC

$$\text{Area of sector subtending } 90^\circ = \frac{\pi R^2 \theta}{360} = 3.14 \times 10 \times 10 \times 90/360 \text{ cm}^2$$

$$= 78.5 \text{ cm}^2$$

$$\text{Area of triangle ABC} = 1/2 \times AC \times BC$$

$$= 1/2 \times 10 \times 10 \text{ cm}^2 = 50 \text{ cm}^2$$

$$\text{Area of Minor segment} = 78.5 \text{ cm}^2 - 50 \text{ cm}^2$$

$$= 28.5 \text{ cm}^2$$

**Question: 25**

In a circle of radius 21 cm

**Solution:**

Radius of Circle = R = 21 cm

Angle Subtended by the arc = 60°

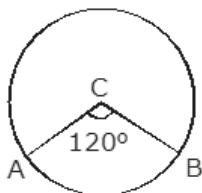
$$\text{Length of an arc of a sector of angle } \theta^\circ \text{ of a circle with radius } R = \frac{2\pi R \theta}{360}$$

$$\text{Length of arc} = 2 \times 22/7 \times 21 \times 60/360 \text{ cm} = 22 \text{ cm}$$

**Question: 26**

In a circle of radius 14 cm

**Solution:**



Radius of Circle = R = 14 cm

Angle Subtended by the arc = θ = 120°

$$\text{Area of sector subtending } 120^\circ = \frac{\pi R^2 \theta}{360} = 22/7 \times 14 \times 14 \times 120/360 \text{ cm}^2$$

$$= 205.33 \text{ cm}^2$$

In Triangle ABC

AC = BC = 14 cm = R

Area of triangle ABC = 1/2 × base × height

$$\begin{aligned}
 &= 2 \times 1/2 \times R \sin \theta/2 \times R \times \cos \theta/2 \\
 &= 2 \times 1/2 \times 14 \times 14 \times \sin 60^\circ \times \cos 60^\circ \\
 &= 84.77 \text{ cm}^2
 \end{aligned}$$

Area of Segment = Area of sector subtending  $120^\circ$  - Area of triangle ABC  
 $= 205.33 - 84.77 \text{ cm}^2 = 120.56 \text{ cm}^2$

## Exercise : FORMATIVE ASSESSMENT (UNIT TEST)

### Question: 1

In the given figure

#### Solution:

Length of side of square = OA = 20 cm

Radius of Quadrant = OB =  $\sqrt{20^2 + 20^2}$  cm =  $20\sqrt{2}$  cm

Area of Quadrant =  $\pi R^2 \times \theta/360 = 3.14 \times 20\sqrt{2} \times 20\sqrt{2} \times 90/360 = 628 \text{ cm}^2$

Area of Square =  $a^2 = 20^2 \text{ cm}^2 = 400 \text{ cm}^2$

Area of Shaded region = Area of Quadrant - Area of Square

$$= 628 \text{ cm}^2 - 400 \text{ cm}^2$$

$$= 228 \text{ cm}^2$$

### Question: 2

The diameter of a

#### Solution:

Diameter of wheel = 84 cm

Radius of wheel = r =  $84/2 \text{ cm} = 42 \text{ cm}$

Distance the wheel travels = 792 m = 79200 cm

In 1 revolution wheel travels  $2\pi r$  distance

$$\begin{aligned}
 \text{No. of revolutions a wheel makes} &= \frac{\text{distance travelled by the wheel}}{2\pi r} \\
 &= \frac{79200}{2\pi \times 42} = \frac{79200}{2 \times \frac{22}{7} \times 42} = \frac{79200 \times 7}{2 \times 22 \times 42} \\
 &= 300 \text{ revolutions}
 \end{aligned}$$

### Question: 3

The area of a sector

#### Solution:

$$\begin{aligned}
 \text{Area of a sector of angle } \theta^\circ \text{ of a circle with radius } R &= \text{area of circle} \times \frac{\theta}{360} \\
 &= \pi r^2 \times \frac{\theta}{360^\circ}
 \end{aligned}$$

### Question: 4

In the given figure

#### Solution:

Given:

Length of rectangle = 8 cm

Breadth of rectangle = 6 cm

Area of rectangle = length × breadth

$$= 8 \times 6 = 48 \text{ cm}^2$$

Consider  $\triangle ABC$ ,

By Pythagoras theorem,

$$AC^2 = AB^2 + BC^2$$

$$= 8^2 + 6^2 = 64 + 36 = 100$$

$$AC = \sqrt{100} = 10 \text{ cm}$$

$\Rightarrow$  Diameter of circle = 10 cm

$$\text{Thus, radius of circle} = \frac{10}{2} = 5 \text{ cm}$$

Let the radius of circle be  $r = 5 \text{ cm}$

Then, Area of circle =  $\pi r^2$

$$= \frac{22}{7} \times 5 \times 5 = \frac{22 \times 25}{7} = \frac{550}{7} = 78.57 \text{ cm}^2$$

Area of shaded region = Area of circle - Area of rectangle

$$= 78.57 - 48$$

$$= 30.57 \text{ cm}^2$$

Hence, the area of shaded region is  $30.57 \text{ cm}^2$ . [None of the option is correct]

### Question: 5

The circumference

#### Solution:

Let the radius if circle be  $r$

Circumference of circle = 22 cm

$$2\pi r = 22 \text{ cm}$$

$$2 \times 22/7 \times r = 22 \text{ cm}$$

$$r = 22 \times 1/2 \times 7/22 \text{ cm}$$

$$r = 3.5 \text{ cm}$$

Area of Circle =  $\pi r^2$

$$= 22/7 \times 3.5 \times 3.5 \text{ cm}^2$$

$$= 38.5 \text{ cm}^2$$

$$\therefore \text{Area of Circle} = 38.5 \text{ cm}^2$$

### Question: 6

In a circle of ra

#### Solution:

Radius of circle =  $R = 21 \text{ cm}$

Angle subtended by arc =  $60^\circ$

Length of an arc of a sector of angle  $\theta^\circ$  of a circle with radius  $R$

= Circumference of circle  $\times \theta/360$

$$= \frac{2\pi R\theta}{360}$$

Length of arc =  $2 \times 22/7 \times 21 \times \theta/360$  cm = 22 cm

Length of arc = 22 cm

**Question: 7**

The minute hand o

**Solution:**

Length of the minute hand of a clock = 12 cm

$\therefore$  Radius = R = 12 cm

In 1 minute, minute hand sweeps  $6^\circ$

So, in 35 minutes, minute hand will sweep  $35 \times 6^\circ = 210^\circ$

Area swept by minute hand in 35 minutes = Area of a sector of angle  $\theta^\circ$  of a circle with radius R

$$= \frac{\pi R^2 \theta}{360} = 22/7 \times 12 \times 12 \times 60^\circ/360^\circ = 264 \text{ cm}^2$$

Area swept by minute hand in 35 minutes =  $264 \text{ cm}^2$

**Question: 8**

The perimeter of

**Solution:**

Radius of circle = 5.6 cm

Perimeter of a sector of a circle =  $2R + \text{Circumference of circle} \times \theta/360$

$$= 2R + \frac{2\pi R\theta}{360}$$

Perimeter of a sector of a circle =  $2 \times 5.6 + 2 \times 22/7 \times 5.6 \times \theta/360$  cm

= 27.2 cm

$\Rightarrow 2 \times 22/7 \times 5.6 \times \theta/360 = 27.2 - 11.2$  cm = 16 cm

$\Rightarrow \theta = 16 \times 1/2 \times 1/5.6 \times 7/22$

$\Rightarrow \theta = 163.63^\circ$

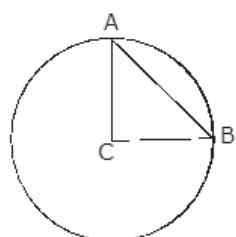
Area of Sector =  $\pi r^2 \times \theta/360 = 22/7 \times 5.6 \times 5.6 \times 163.63/360 = 44.8 \text{ cm}^2$

$\therefore$  Area of Sector =  $44.8 \text{ cm}^2$

**Question: 9**

A chord of a circ

**Solution:**



Chord AB subtends an angle of  $90^\circ$  at the centre of the circle

Radius of Circle = R = 14 cm

$$\text{Area of sector of circle of radius } R = \frac{\pi R^2 \theta}{360}$$

$$= 22/7 \times 14 \times 14 \times 90/360 \text{ cm}^2 = 154 \text{ cm}^2$$

**Question: 10**

In the given figure

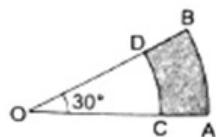
**Solution:**

Given,

$$\text{Radius of smaller circle} = R_1 = 3.5 \text{ cm}$$

$$\text{Radius of bigger circle} = R_2 = 7 \text{ cm}$$

$$\text{Angle subtended} = 30^\circ$$



$$\text{Area of Shaded region} = \frac{\pi R_2^2 \theta}{360} - \frac{\pi R_1^2 \theta}{360} = \pi (R_2^2 - R_1^2) \frac{\theta}{360}$$

$$= 22/7 \times (7^2 - 3.5^2) \times 30/360 \text{ cm}^2$$

$$= 22/7 \times (49 - 12.25) \times 30/360 \text{ cm}^2$$

$$= 9.625 \text{ cm}^2$$

$$\therefore \text{Area of shaded region} = 9.625 \text{ cm}^2$$

**Question: 11**

A wire when bent

**Solution:**

Let the sides of equilateral triangle be  $a$  cm

$$\text{Area of equilateral triangle} = 121\sqrt{3} \text{ cm}^2$$

$$\text{Area of equilateral triangle} = \sqrt{3}/4 \times a^2$$

$$\Rightarrow \sqrt{3}/4 a^2 = 121\sqrt{3}$$

$$\Rightarrow a^2 = 121\sqrt{3} \times 4/\sqrt{3} = 121 \times 4 \text{ cm}^2$$

$$\Rightarrow a^2 = 484 \text{ cm}^2$$

$$\Rightarrow a = 22 \text{ cm}$$

$$\text{Perimeter of equilateral triangle} = 3a$$

$$= 3 \times 22 \text{ cm} = 66 \text{ cm}$$

$$\text{Perimeter of equilateral triangle} = \text{Circumference of circle}$$

$$\text{Circumference of circle} = 66 \text{ cm}$$

Let the radius of circle be  $r$

$$\text{Circumference of circle} = 2\pi r$$

$$\Rightarrow 2\pi r = 66 \text{ cm}$$

$$\Rightarrow 2 \times 22/7 \times r = 66 \text{ cm}$$

$$\Rightarrow r = 66 \times 1/2 \times 7/22 \text{ cm}$$

$$\Rightarrow r = 10.5 \text{ cm}$$

$$\begin{aligned}\text{Area of circle} &= \pi r^2 = 22/7 \times 22/7 \times 10.5 \times 10.5 \text{ cm}^2 \\ &= 346.5 \text{ cm}^2\end{aligned}$$

**Question: 12**

Diameter of the wheel = 84 cm

Let the radius of the wheel be R cm

Radius of the wheel =  $84/2 \text{ cm} = 42 \text{ cm}$

No. of revolutions wheel makes = 5 rev/sec

Since, 1 revolution =  $2\pi R$

Speed of the wheel =  $5 \times 2\pi R \text{ rev/sec}$

$$= 5 \times 2 \times 22/7 \times 42 = 1320 \text{ cm/sec}$$

$$= 13.20 \text{ m/sec}$$

$$= 13.20 \times 3600/1000 \text{ km/h}$$

$$= 47.52 \text{ km/h}$$

Since, 1 m/sec = 3600/1000 km/h

**Question: 13**

OACB is a quadrant

**Solution:**

Radius of circle = R = 3.5 cm

OD = 2 cm

OA = OB = R = 3.5 cm

Since, OACB is a quadrant of a circle  $\therefore$  angle subtended by it at the centre =  $90^\circ$

$$\begin{aligned}\text{(i) Area of quadrant} &= \frac{\pi R^2 \theta}{360} \\ &= 22/7 \times 3.5 \times 3.5 \times 90^\circ/360^\circ \text{ cm}^2 \\ &= 9.625 \text{ cm}^2\end{aligned}$$

(ii) Area of shaded region = Area of quadrant - Area of triangle OAD

Area of triangle OAD =  $1/2 \times \text{base} \times \text{height}$

$$= 1/2 \times OA \times OD$$

$$= 1/2 \times 3.5 \times 2 \text{ cm}^2$$

$$= 3.5 \text{ cm}^2$$

Area of shaded region =  $9.625 \text{ cm}^2 - 3.5 \text{ cm}^2$

$$= 6.125 \text{ cm}^2$$

**Question: 14**

In the given figure

**Solution:**

Length of the sides of square = 28 cm

Area of square =  $a^2 = 28^2 \text{ cm}^2$

$$= 784 \text{ cm}^2$$

Since, all the circles are identical so, they have same radius

Let the radius of circle be R cm

From the figure  $2R = 28$  cm

$$R = 28/2 \text{ cm}$$

$$R = 14 \text{ cm}$$

Quadrant of a circle subtends  $90^\circ$  at the centre.

$$\text{Area of quadrant of circle} = \frac{\pi R^2 \theta}{360}$$

$$= 22/7 \times 14 \times 14 \times 90^\circ/360^\circ \text{ cm}^2 = 154 \text{ cm}^2$$

$$\text{Area of 4 quadrants of circle} = 154 \times 4 \text{ cm}^2 = 616 \text{ cm}^2$$

Area of shaded region = Area of square - Area of 4 quadrants of circle

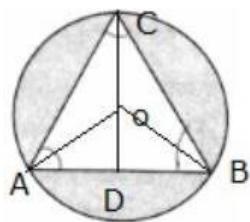
$$= 784 \text{ cm}^2 - 616 \text{ cm}^2$$

$$= 168 \text{ cm}^2$$

### Question: 15

In the given figure

**Solution:**



Radius of circle = R = 4 cm

OD perpendicular to AB is drawn

$\triangle ABC$  is equilateral triangle,

$$\angle A = \angle B = \angle C = 60^\circ$$

$$\angle OAD = 30^\circ$$

$$OD/AO = \sin 30^\circ$$

$$AO = 4 \text{ cm}$$

$$\frac{OD}{AO} = \frac{1}{2}$$

$$OD = 1/2 \times 4 \text{ cm}$$

$$OD = 2 \text{ cm}$$

$$AD^2 = OA^2 - OD^2$$

$$= 4^2 - 2^2 = 16 - 4 = 12 \text{ cm}^2$$

$$AD = 2\sqrt{3} \text{ cm}$$

$$AB = 2 \times AD$$

$$= 2 \times 2\sqrt{3} \text{ cm} = 4\sqrt{3} \text{ cm}$$

$$\text{Area of triangle } ABC = \sqrt{3}/4 \times AB^2$$

$$= \sqrt{3}/4 \times 4\sqrt{3} \times 4\sqrt{3}$$

$$= 20.71 \text{ cm}^2$$

$$\text{Area of circle} = \pi R^2$$

$$= 3.14 \times 4 \times 4 \text{ cm}^2$$

$$= 50.24 \text{ cm}^2$$

$$\text{Area of shaded region} = 29.53 \text{ cm}^2$$

**Question: 16**

The minute hand o

**Solution:**

$$\text{Length of minute hand} = 7.5 \text{ cm}$$

In a clock, length of minute hand = radius

$$\text{Radius} = R = 7.5 \text{ cm}$$

In 1 minute, minute hand moves  $6^\circ$

So, in 56 minutes, minute hand moves  $56 \times 6^\circ = 336^\circ$

$$\text{Area described by minute hand} = \frac{\pi R^2 \theta}{360^\circ}$$

$$= 22/7 \times 7.5 \times 7.5 \times 336^\circ / 360^\circ \text{ cm}^2$$

$$= 165 \text{ cm}^2$$

**Question: 17**

A racetrack is in

**Solution:**

Let the inner radius be  $R_1$  and outer radius be  $R_2$

$$\text{Inner circumference} = 2\pi R_1 = 352 \text{ m}$$

$$\Rightarrow 2 \times 22/7 \times R_1 = 352 \text{ m}$$

$$\Rightarrow R_1 = 352 \times 1/2 \times 7/22$$

$$\Rightarrow R_1 = 56 \text{ m}$$

$$\text{Outer Circumference} = 2\pi R_2 = 396 \text{ m}$$

$$\Rightarrow 2 \times 22/7 \times R_2 = 396 \text{ m}$$

$$\Rightarrow R_2 = 396 \times 1/2 \times 7/22 \text{ m}$$

$$\Rightarrow R_2 = 63 \text{ m}$$

$$\text{Width of the track} = R_2 - R_1 = 63 \text{ m} - 56 \text{ m} = 7 \text{ m}$$

$$\text{Area of track} = \pi(R_2^2 - R_1^2) = 22/7 \times (63^2 - 56^2)$$

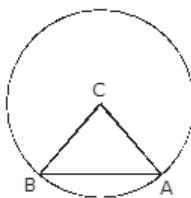
$$= 22/7 \times (3969 - 3136) \text{ m}^2$$

$$= 22/7 \times 833 \text{ m}^2 = 2618 \text{ m}^2$$

**Question: 18**

A chord of a circ

**Solution:**



$$\angle ACB = 60^\circ$$

Chord AB subtends an angle of  $60^\circ$  at the centre

$$\text{Radius} = 30 \text{ cm}$$

Let Radius be R

In triangle ABC, AC = BC

$$\text{So, } \angle CAB = \angle CBA$$

$$\angle ACB + \angle CAB + \angle CBA = 180^\circ$$

$$60^\circ + 2\angle CAB = 180^\circ$$

$$2\angle CAB = 180^\circ - 60^\circ = 120^\circ$$

$$\angle CAB = 120^\circ/2 = 60^\circ$$

$$\angle CAB = \angle CBA = 60^\circ$$

$\therefore \Delta ABC$  is an equilateral triangle

Length of side of an equilateral triangle = radius of circle = 30 cm

$$\text{Area of equilateral triangle} = \sqrt{3}/4 \times \text{side}^2 = 1.732/4 \times 30 \times 30 \text{ cm}^2$$

$$= 389.7 \text{ cm}^2$$

$$\text{Area of sector } ACB = \frac{\pi R^2 \theta}{360} = 3.14 \times 30 \times 30 \times 60^\circ/360^\circ = 471.45 \text{ cm}^2$$

Area of minor Segment = Area of sector ACB - Area of  $\Delta ABC$

$$= 471.45 \text{ cm}^2 - 389.7 \text{ cm}^2 = 81.75 \text{ cm}^2$$

$$\text{Area of circle} = \pi R^2 = 3.14 \times 30 \times 30 \text{ cm}^2 = 2828.57 \text{ cm}^2$$

Area of major segment = Area of circle - Area of minor segment

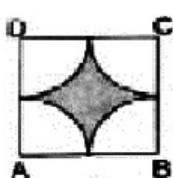
$$= 2826 \text{ cm}^2 - 81.75 \text{ cm}^2$$

$$= 2744.25 \text{ cm}^2$$

### Question: 19

Four cows are tethered

**Solution:**



From the figure we see that cows are tethered at the corners of the square so while grazing they form four quadrants as shown in the figure

$$\text{Length of side of square} = 50 \text{ m}$$

$$\text{Length of side of square} = 2 \times \text{Radius of quadrant}$$

$$\text{Radius of quadrant} = R = 50/2 \text{ m}$$

$$= 25 \text{ m}$$

$$\text{Area of square} = \text{side}^2$$

$$= 50^2 \text{ m}^2 = 2500 \text{ m}^2$$

$$\text{Area of quadrant} = 1/4 \pi R^2 = 1/4 \times 3.14 \times 25 \times 25 \text{ m}^2$$

$$= 490.625 \text{ m}^2$$

$$\text{Area of 4 quadrants} = 4 \times 490.625 \text{ m}^2$$

$$= 1962.5 \text{ m}^2$$

$$\text{Area left ungrazed} = \text{Area of shaded part}$$

$$= \text{Area of square} - \text{Area of 4 quadrants}$$

$$= 2500 \text{ m}^2 - 1962.5 \text{ m}^2$$

$$= 537.5 \text{ m}^2$$

### Question: 20

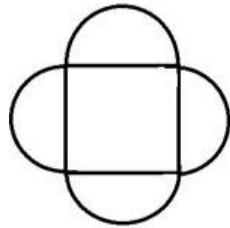
A square tank has

#### Solution:

Let the length of side of the square tank be a

$$\text{Area of square tank} = a^2 = 1600 \text{ m}^2$$

$$\Rightarrow a = \sqrt{1600} \text{ m} = 40 \text{ m}$$



Let the radius of semicircle be R

From the figure we can see that

Length of the side of the square = Diameter of semicircle

$$40 \text{ m} = 2 \times R$$

$$R = 40/2 \text{ m}$$

$$R = 20 \text{ m}$$

$$\text{Area of semi-circle} = 1/2 \pi R^2 = 1/2 \times 3.14 \times 20 \times 20 \text{ m}^2$$

$$= 628 \text{ m}^2$$

$$\text{Area of 4 semi-circles} = 4 \times 628 \text{ m}^2$$

$$= 2512 \text{ m}^2$$

$$\text{Cost of turfing the plots} = \text{Rs. } 12.50 \text{ per m}^2$$

$$\text{Cost of Turfing} = \text{Cost of turfing per m}^2 \times \text{Area of 4 semicircle}$$

$$= \text{Rs. } 12.50 \times 2512$$

$$= \text{Rs. } 31400$$