

# Tables

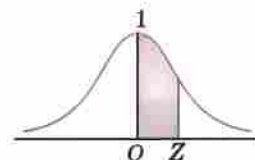
Table I : Gamma Function,  $\Gamma(\alpha) = \int_0^{\infty} e^{-t} t^{\alpha-1} dt$

$\alpha$	$\Gamma(\alpha)$	$\alpha$	$\Gamma(\alpha)$	$\alpha$	$\Gamma(\alpha)$	$\alpha$	$\Gamma(\alpha)$
1.00	1.000000	1.26	0.904397	1.52	0.887039	1.78	0.926227
1.01	0.994326	1.27	0.902503	1.53	0.887568	1.79	0.928767
1.02	0.988844	1.28	0.900719	1.54	0.888178	1.80	0.931384
1.03	0.983550	1.29	0.899042	1.55	0.888869	1.81	0.934076
1.04	0.978438	1.30	0.897471	1.56	0.889639	1.82	0.936845
1.05	0.973504	1.31	0.896004	1.57	0.890490	1.83	0.939690
1.06	0.968744	1.32	0.894640	1.58	0.891420	1.84	0.942612
1.07	0.964152	1.33	0.893378	1.59	0.892428	1.85	0.945611
1.08	0.959725	1.34	0.892215	1.60	0.893516	1.86	0.948687
1.09	0.955459	1.35	0.891151	1.61	0.894681	1.87	0.951840
1.10	0.951351	1.36	0.890184	1.62	0.895924	1.88	0.955071
1.11	0.947395	1.37	0.889313	1.63	0.897244	1.89	0.958380
1.12	0.943590	1.38	0.888537	1.64	0.898642	1.90	0.961766
1.13	0.939931	1.39	0.887854	1.65	0.900117	1.91	0.965231
1.14	0.936416	1.40	0.887264	1.66	0.901668	1.92	0.968774
1.15	0.933041	1.41	0.886764	1.67	0.903296	1.93	0.972397
1.16	0.929803	1.42	0.886356	1.68	0.905001	1.94	0.976099
1.17	0.926700	1.43	0.886036	1.69	0.906782	1.95	0.979881
1.18	0.923728	1.44	0.885805	1.70	0.908639	1.96	0.983742
1.19	0.920885	1.45	0.885661	1.71	0.910572	1.97	0.987685
1.20	0.918169	1.46	0.885604	1.72	0.912580	1.98	0.991708
1.21	0.915577	1.47	0.885633	1.73	0.914665	1.99	0.995813
1.22	0.913106	1.48	0.885747	1.74	0.916826	2.00	1.000000
1.23	0.910755	1.49	0.885945	1.75	0.919062		
1.24	0.908521	1.50	0.886227	1.76	0.921375		
1.25	0.906403	1.51	0.886592	1.77	0.923763		

Table II : Bessel Functions

$x$	$J_0(x)$	$J_1(x)$	$x$	$J_0(x)$	$J_1(x)$
0.0	1.0000	0.0000	3.0	-0.2601	0.3991
0.1	0.9975	0.0499	3.1	-0.2921	0.3009
0.2	0.9900	0.0995	3.2	-0.3202	0.2613
0.3	0.9776	0.1483	3.3	-0.3443	0.2207
0.4	0.9604	0.1960	3.4	-0.3643	0.1792
0.5	0.9385	0.2423	3.5	-0.3801	0.1374
0.6	0.9120	0.2867	3.6	-0.3918	0.0955
0.7	0.8812	0.3290	3.7	-0.3992	0.0538
0.8	0.8463	0.3688	3.8	-0.4026	0.0128
0.9	0.8075	0.4059	3.9	-0.4018	-0.0272
1.0	0.7652	0.4401	4.0	-0.3971	-0.0660
1.1	0.7196	0.4709	4.1	-0.3887	-0.1033
1.2	0.6711	0.4983	4.2	-0.3766	-0.1386
1.3	0.6201	0.5220	4.3	-0.3610	-0.1719
1.4	0.5669	0.5419	4.4	-0.3423	-0.2028
1.5	0.5118	0.5579	4.5	-0.3205	-0.2311
1.6	0.4554	0.5699	4.6	-0.2961	-0.2566
1.7	0.3980	0.5778	4.7	-0.2693	-0.2791
1.8	0.3400	0.5815	4.8	-0.2404	-0.2985
1.9	0.2818	0.5812	4.9	-0.2097	-0.3147
2.0	0.2239	0.5767	5.0	-0.1776	-0.3276
2.1	0.1666	0.5683	5.1	-0.1443	-0.3371
2.2	0.1104	0.5560	5.2	-0.1103	-0.3432
2.3	0.0555	0.5399	5.3	-0.0758	-0.3460
2.4	0.0025	0.5202	5.4	-0.0412	-0.3453
2.5	-0.0484	0.4971	5.5	-0.0068	-0.3414
2.6	-0.0968	0.4708	5.6	0.0270	-0.3343
2.7	-0.1424	0.4416	5.7	0.0599	-0.3241
2.8	-0.1850	0.4097	5.8	0.0917	-0.3110
2.9	-0.2243	0.3754	5.9	0.1220	-0.2951

Table III : Area under the Normal curve



$z$	0	1	2	3	4	5	6	7	8	9
0.0	0.0000	0.0040	0.0080	0.0120	0.0160	0.0199	0.0239	0.0279	0.0319	0.0359
0.1	0.0398	0.0438	0.0478	0.0517	0.0557	0.0596	0.0636	0.0675	0.0714	0.0754
0.2	0.0793	0.0832	0.0871	0.0910	0.0948	0.0987	0.1026	0.1064	0.1103	0.1141
0.3	0.1179	0.1217	0.1255	0.1293	0.1331	0.1368	0.1406	0.1443	0.1480	0.1517
0.4	0.1554	0.1591	0.1628	0.1664	0.1700	0.1736	0.1772	0.1808	0.1844	0.1879
0.5	0.1915	0.1950	0.1985	0.2019	0.2054	0.2088	0.2123	0.2157	0.2190	0.2224
0.6	0.2258	0.2291	0.2324	0.2357	0.2389	0.2422	0.2454	0.2486	0.2518	0.2549
0.7	0.2580	0.2612	0.2642	0.2673	0.2704	0.2734	0.2764	0.2794	0.2823	0.2852
0.8	0.2881	0.2910	0.2939	0.2967	0.2996	0.3023	0.3051	0.3078	0.3106	0.3133
0.9	0.3159	0.3186	0.3212	0.3238	0.3264	0.3289	0.3315	0.3340	0.3365	0.3389
1.0	0.3413	0.3438	0.3461	0.3485	0.3508	0.3531	0.3554	0.3577	0.3599	0.3621
1.1	0.3643	0.3665	0.3686	0.3708	0.3729	0.3749	0.3770	0.3790	0.3810	0.3830
1.2	0.3849	0.3869	0.3888	0.3907	0.3925	0.3944	0.3962	0.3980	0.3997	0.4015
1.3	0.4032	0.4049	0.4066	0.4082	0.4099	0.4115	0.4131	0.4147	0.4162	0.4177
1.4	0.4192	0.4207	0.4222	0.4236	0.4251	0.4265	0.4279	0.4292	0.4306	0.4319
1.5	0.4332	0.4345	0.4357	0.4370	0.4382	0.4394	0.4406	0.4418	0.4429	0.4441
1.6	0.4452	0.4463	0.4474	0.4484	0.4495	0.4505	0.4515	0.4525	0.4535	0.4545
1.7	0.4554	0.4564	0.4573	0.4582	0.4591	0.4599	0.4608	0.4616	0.4625	0.4633
1.8	0.4641	0.4649	0.4656	0.4664	0.4671	0.4678	0.4686	0.4693	0.4699	0.4706
1.9	0.4713	0.4719	0.4726	0.4732	0.4738	0.4744	0.4750	0.4756	0.4761	0.4767
2.0	0.4772	0.4778	0.4783	0.4788	0.4793	0.4798	0.4803	0.4808	0.4812	0.4817
2.1	0.4821	0.4826	0.4830	0.4834	0.4838	0.4842	0.4846	0.4850	0.4854	0.4857
2.2	0.4861	0.4864	0.4868	0.4871	0.4875	0.4878	0.4881	0.4884	0.4887	0.4890
2.3	0.4893	0.4896	0.4898	0.4901	0.4904	0.4906	0.4909	0.4911	0.4913	0.4916
2.4	0.4918	0.4920	0.4922	0.4925	0.4927	0.4929	0.4931	0.4932	0.4934	0.4936
2.5	0.4938	0.4940	0.4941	0.4943	0.4945	0.4946	0.4948	0.4949	0.4951	0.4952
2.6	0.4953	0.4955	0.4956	0.4957	0.4959	0.4960	0.4961	0.4962	0.4963	0.4964
2.7	0.4965	0.4966	0.4967	0.4968	0.4969	0.4970	0.4971	0.4972	0.4973	0.4974
2.8	0.4974	0.4975	0.4976	0.4977	0.4977	0.4978	0.4979	0.4979	0.4980	0.4981
2.9	0.4981	0.4982	0.4982	0.4983	0.4984	0.4984	0.4985	0.4985	0.4986	0.4986
3.0	0.4987	0.4987	0.4987	0.4988	0.4988	0.4989	0.4989	0.4989	0.4990	0.4990
3.1	0.4990	0.4991	0.4991	0.4991	0.4992	0.4992	0.4992	0.4992	0.4993	0.4993



Table IV : Values of  $|t|$  with probability  $P$  and degrees of freedom  $v$ 

$P \backslash v$	0.50	0.10	0.05	0.02	0.01
1	1.000	6.34	12.71	31.82	63.66
2	0.816	2.92	4.30	6.96	9.92
3	0.765	2.35	3.18	4.54	5.84
4	0.741	2.13	2.78	3.75	4.60
5	0.727	2.02	2.57	3.36	4.03
6	0.718	1.94	2.45	3.14	3.71
7	0.711	1.90	2.36	3.00	3.50
8	0.706	1.86	2.31	2.90	3.36
9	0.703	1.83	2.26	2.82	3.25
10	0.700	1.81	2.23	2.76	3.17
11	0.697	1.80	2.20	2.72	3.11
12	0.695	1.78	2.18	2.68	3.06
13	0.694	1.77	2.16	2.65	3.01
14	0.692	1.76	2.14	2.62	2.98
15	0.691	1.75	2.13	2.60	2.95
16	0.690	1.75	2.12	2.58	2.92
17	0.689	1.74	2.11	2.57	2.90
18	0.688	1.73	2.10	2.55	2.88
19	0.688	1.73	2.09	2.54	2.86
20	0.687	1.72	2.09	2.53	2.84
21	0.686	1.72	2.08	2.52	2.83
22	0.686	1.72	2.07	2.51	2.82
23	0.685	1.71	2.07	2.50	2.81
24	0.685	1.71	2.06	2.49	2.80
25	0.684	1.71	2.06	2.48	2.79
26	0.684	1.71	2.06	2.48	2.78
27	0.684	1.70	2.05	2.47	2.77
28	0.683	1.70	2.05	2.47	2.76
29	0.683	1.70	2.04	2.46	2.76
30	0.683	1.70	2.04	2.46	2.75

Table V : Values of  $\chi^2$  with probability  $P$  and df  $v$ 

$P \backslash v$	0.99	0.95	0.50	0.30	0.20	0.10	0.05	0.01
1	0.0002	0.004	0.46	1.07	1.64	2.71	3.84	6.64
2	0.020	0.103	1.39	2.41	3.22	4.60	5.99	9.21
3	0.115	0.35	2.37	3.66	4.64	6.25	7.82	11.34
4	0.30	0.71	3.36	4.88	5.99	7.78	9.49	13.28
5	0.55	1.14	4.35	6.06	7.29	9.24	11.07	15.09
6	0.87	1.64	5.35	7.23	8.56	10.64	12.59	16.81
7	1.24	2.17	6.35	8.38	9.80	12.02	14.07	18.48
8	1.65	2.73	7.34	9.52	11.03	13.36	15.51	20.09
9	2.09	3.32	8.34	10.66	12.24	14.68	16.92	21.67
10	2.56	3.94	9.34	11.78	13.44	15.99	18.31	23.21
11	3.05	4.58	10.34	12.90	14.63	17.28	19.68	24.72
12	3.57	5.23	11.34	14.01	15.81	18.55	21.03	26.22
13	4.11	5.89	12.34	15.12	16.98	19.81	22.36	27.69
14	4.66	6.57	13.34	16.22	18.15	21.06	23.68	29.14
15	5.23	7.26	14.34	17.32	19.31	22.31	25.00	30.58
16	5.81	7.96	15.34	18.42	20.46	23.54	26.30	32.00
17	6.41	8.67	16.34	19.51	21.62	24.77	27.59	33.41
18	7.02	9.39	17.34	20.60	22.76	25.99	28.87	34.80
19	7.63	10.12	18.34	21.69	23.90	27.20	30.14	36.19
20	8.26	10.85	19.34	22.78	25.04	28.41	31.41	37.57
21	8.90	11.59	20.34	23.86	26.17	29.62	32.67	38.93
22	9.54	12.34	21.34	24.94	27.30	30.81	33.92	40.29
23	10.20	13.09	22.34	26.02	28.43	32.01	35.17	41.64
24	10.86	13.85	23.34	27.10	29.55	33.20	36.42	42.98
25	11.52	14.61	24.34	28.17	30.68	34.68	37.65	44.31
26	12.20	15.38	25.34	29.25	31.80	35.56	38.88	45.64
27	12.88	16.15	26.34	30.32	32.91	36.74	40.11	46.96
28	13.56	16.93	27.34	31.39	34.03	37.92	41.34	48.28
29	14.26	17.71	28.34	32.46	35.14	39.09	42.56	49.59
30	14.95	18.49	29.34	33.53	36.25	40.26	43.77	50.89

Table VI : 5% and 1% points of F

$v_1 \backslash v_2$	1	2	3	4	5	6	8	12	24	$\infty$
2	18.51 98.49	19.00 99.00	19.16 99.17	19.25 99.25	19.30 99.30	19.32 99.33	19.37 99.36	19.41 99.42	19.45 99.46	19.50 99.50
3	10.13 34.12	9.55 30.82	9.28 29.46	9.12 28.71	9.01 28.24	8.94 27.91	8.84 27.49	8.74 27.05	8.64 26.60	8.53 26.12
4	7.71 21.20	6.94 18.00	6.59 16.69	6.39 15.98	6.26 15.52	6.16 15.21	6.04 14.80	5.91 14.37	5.77 13.93	5.63 13.46
5	6.61 16.26	5.79 13.27	5.41 12.06	5.19 11.39	5.05 10.97	4.95 10.67	4.82 10.27	4.68 9.89	4.53 9.47	4.36 9.02
6	5.99 13.74	5.14 10.92	4.76 9.78	4.53 9.15	4.39 8.75	4.28 8.47	4.15 8.10	4.00 7.72	3.84 7.31	3.67 6.88
7	5.59 12.25	4.74 9.55	4.35 8.45	4.12 7.85	3.97 7.46	3.87 7.19	3.73 6.84	3.57 6.47	3.41 6.07	3.23 5.65
8	5.32 11.26	4.46 8.65	4.07 7.59	3.84 7.01	3.69 6.63	3.58 6.37	3.44 6.03	3.28 5.67	3.12 5.28	2.93 4.86
9	5.12 10.56	4.26 8.02	3.86 6.99	3.63 6.42	3.48 6.06	3.37 5.80	3.23 5.47	3.07 5.11	2.90 4.73	2.71 4.31
10	4.96 10.04	4.10 7.56	3.71 6.55	3.48 5.99	3.33 5.64	3.22 5.39	3.07 5.06	2.91 4.71	2.74 4.33	2.54 3.91
12	4.75 9.23	3.88 6.93	3.49 5.95	3.26 5.41	3.11 5.06	3.00 4.82	2.85 4.50	2.69 4.16	2.50 3.78	2.30 3.36
14	4.60 8.86	3.74 6.51	3.34 5.56	3.11 5.03	2.96 4.69	2.85 4.46	2.70 4.14	2.53 3.80	2.35 3.43	2.13 3.00
16	4.49 8.53	3.63 6.23	3.24 5.29	3.01 4.77	2.85 4.44	2.74 4.20	2.59 3.89	2.42 3.55	2.24 3.18	2.01 2.75
18	4.41 8.28	3.55 6.01	3.16 5.09	2.93 4.58	2.77 4.25	2.66 4.01	2.51 3.71	2.34 3.37	2.15 3.01	1.92 2.57
20	4.35 8.10	3.49 5.85	3.10 4.94	2.87 4.43	2.71 4.10	2.60 3.87	2.45 3.56	2.28 3.23	2.08 2.86	1.84 2.42
25	4.24 7.77	3.38 5.57	2.99 4.68	2.76 4.18	2.60 3.86	2.49 3.63	2.34 3.32	2.16 2.99	1.96 2.62	1.71 2.17
30	4.17 7.56	3.32 5.39	2.92 4.51	2.69 4.02	2.53 3.70	2.42 3.47	2.27 3.17	2.09 2.84	1.89 2.47	1.62 2.01
40	4.08 7.31	3.23 5.18	2.84 4.31	2.61 3.83	2.45 3.51	2.34 3.29	2.18 2.99	2.00 2.66	1.79 2.29	1.51 1.81
60	4.00 7.08	3.15 4.98	2.76 4.13	2.52 3.65	2.37 3.34	2.25 3.12	2.10 2.82	1.92 2.50	1.70 2.12	1.39 1.60