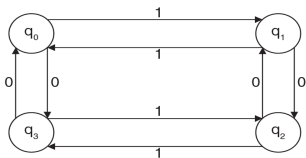


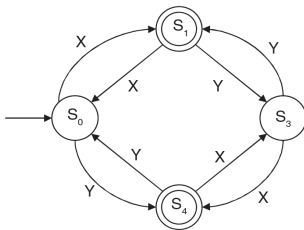
2. Consider the transitional system.



Which of the states are to be marked as starting state and final state, respectively, so as to turn the above system into a DFA that accepts all strings having odd number of zeros and even number of 1's?

- a)  $q_0, q_2$       b)  $q_0, q_1$       c)  $q_1, q_2$       d) None of these

3. Consider the following DFA in which  $S_0$  is the start state and  $S_1$  and  $S_3$  are the final states. Which one is true?

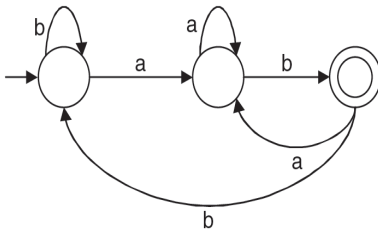


- a) All strings of  $x$  and  $y$ .
- b) All strings of  $x$  and  $y$  which have either an even number of  $x$  and even number of  $y$  or an odd number of  $x$  and odd number of  $y$ .
- c) All strings of  $x$  and  $y$  which have an equal number of  $x$  and  $y$ .
- d) All strings of  $x$  and  $y$  which have either an even number of  $x$  and odd number of  $y$  or an odd number of  $x$  and even number of  $y$ .

4. Let N be an NFA with  $n$  states and let M be the minimized DFA with  $m$  states recognizing the same language. Which of the following is NECESSARILY true?

- a)  $m \leq 2^n$       b)  $n \leq m$       c) M has one accept state      d)  $m = 2^n$

5. If the final state and non-final states in the following DFA are interchanged, then which of the following languages over the alphabet  $(a, b)$  will be accepted by the new DFA?



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- a) Set of all strings that do not end with ab
- b) Set of all strings that begin with either an a or a b.
- c) Set of all strings that do not contain the substring ab.
- d) The set described by the regular expression  $b^*aa^*(ba)^*b^*$

6. A finite state machine with the following state table has a single input x and a single output z.

Present State	Next State,z	
	X=0	X=1
A	D, 0	B, 0
B	B, 1	C, 1
C	B, 0	D, 1
D	B, 1	C, 0

If the initial state is unknown, then the shortest input sequence to reach the final state C is:

- a)01      b)10      c) 101      d)110

7. Which of the following sets can be recognized by a deterministic finite state automaton?

- a) The numbers  $1, 2, 4, 8, \dots, 2^n$  written in binary.
- b) The numbers  $1, 2, 4, \dots, 2^n$  written in unary.
- c) The set of binary string in which the number of zeros is the same as the number of ones.
- d) The set  $\{1, 101, 11011, 1110111, \dots\}$

8. Consider the regular expression  $(0 + 1)(0 + 1)\dots N$  times. The minimum state FA that recognizes the language represented by this regular expression contains

- a)  $n$  states      b)  $(n + 1)$  states      c)  $(n + 2)$  states      d) None of the above

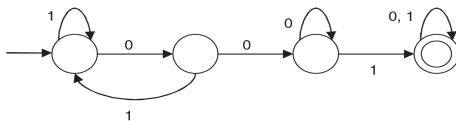
9. What can be said about a regular language  $L$  over  $\{a\}$  whose minimal finite state automaton has two states?

- a)  $L$  must be  $\{an \mid n \text{ is odd}\}$       b)  $L$  must be  $\{an \mid n \text{ is even}\}$   
 c)  $L$  must be  $\{an \mid n \geq 0\}$       d) Either  $L$  must be  $\{an \mid n \text{ is odd}\}$  or  $L$  must be  $\{an \mid n \text{ is even}\}$

10. The smallest FA which accepts the language  $\{x \mid \text{length of } x \text{ is divisible by } 3\}$  has

- a) 2 states      b) 3 states      c) 4 states      d) 5 states

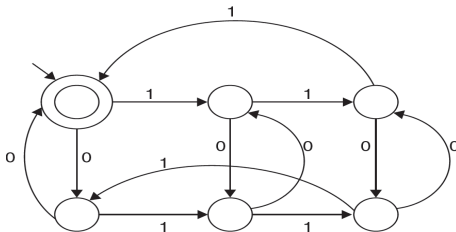
11. Consider the following deterministic finite state automaton  $M$ .



Let  $S$  denote the set of seven-bit binary strings in which the first, fourth, and last bits are 1. The number of strings in  $S$  that are accepted by  $M$  is

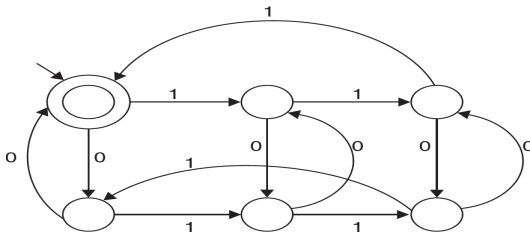
- a) 1      b) 5      c) 7      d) 8

12. The following finite state machine accepts all those binary strings in which the number of 1's and 0's are, respectively,



- a) divisible by 3 and 2      b) odd and even  
c) even and odd      d) divisible by 2 and 3

13. Consider the machine M.



The language recognized by M is:

- a)  $\{w \in \{a, b\}^* \mid \text{every } a \text{ in } w \text{ is followed by exactly two } b\text{'s}\}$
- b)  $\{w \in \{a, b\}^* \mid \text{every } a \text{ in } w \text{ is followed by at least two } b\text{'s}\}$
- c)  $\{w \in \{a, b\}^* \mid w \text{ contains the substring 'abb'}\}$
- d)  $\{w \in \{a, b\}^* \mid w \text{ does not contain 'aa' as a substring}\}$



14. A minimum state deterministic FA accepting the language  $L = \{w | w \in \{0, 1\}^*\}$  where number of 0's and 1's in  $w$  are divisible by 3 and 5, respectively, has

- a) 15 states      b) 11 states      c) 10 states      d) 9 states

Y:

	a	b
$\rightarrow 1$	1	2
2(F)	2	1

Z:

	a	b
$\rightarrow 1$	2	2
2(F)	1	1

Which of the following represents the product automaton  $Z \times Y$ ?

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a)

	a	b
$\rightarrow P$	S	R
Q	R	S
R(F)	Q	P
S	Q	P

b)

	a	b
$\rightarrow P$	S	Q
Z	R	S
R(F)	Q	P
S	P	Q

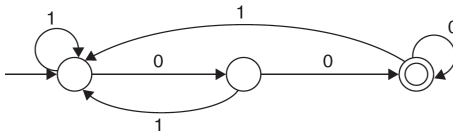
c)

	a	b
$\rightarrow P$	Q	S
Q	R	S
R(F)	Q	P
S	Q	P

d)

	a	b
$\rightarrow P$	S	Q
Q	S	R
R(F)	Q	P
S	Q	P

16.



The given DFA accepts the set of all strings over  $\{0, 1\}$  that

- a) begin either with 0 or 1.                      b) end with 0  
c) end with 00.                                      d) contain the substring 00.

17. Let  $w$  be any string of length  $n$  in  $\{0, 1\}^*$ . Let  $L$  be the set of all substrings of  $w$ . What is the minimum number of states in a non-deterministic FA that accepts  $L$ ?

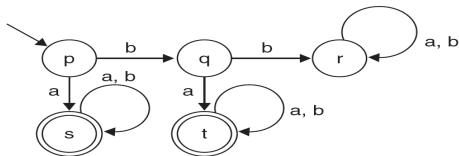
- a)  $n - 1$       b)  $n$       c)  $n + 1$       d)  $2^{n-1}$

18. Definition of a language  $L$  with alphabet  $\{a\}$  is given as following  $\{a^{nk} | k > 0 \text{ and } n \text{ is a positive integer constant}\}$

What is the minimum number of states needed in a DFA to recognize  $L$ ?

- a)  $k + 1$       b)  $n + 1$       c)  $2^{n+1}$       d)  $2^{k+1}$

19. A deterministic finite automation (DFA)  $D$  with alphabet  $\Sigma = \{a, b\}$  is given as follows:



Which of the following finite state machines is a valid minimal DFA which accepts the same language as  $D$ ?

