$$g_i(\mathbf{x}) = P(\omega_i | \mathbf{x}) = \frac{p(\mathbf{x} | \omega_i) P(\omega_i)}{\sum\limits_{j=1}^{c} p(\mathbf{x} | \omega_j) P(\omega_j)}$$
$$g_i(\mathbf{x}) = p(\mathbf{x} | \omega_i) P(\omega_i)$$
$$g_i(\mathbf{x}) = \ln p(\mathbf{x} | \omega_i) + \ln P(\omega_i),$$