$$P(\mathbf{x}|\omega_1) = \prod_{i=1}^d p_i^{x_i} (1 - p_i)^{1 - x_i}$$