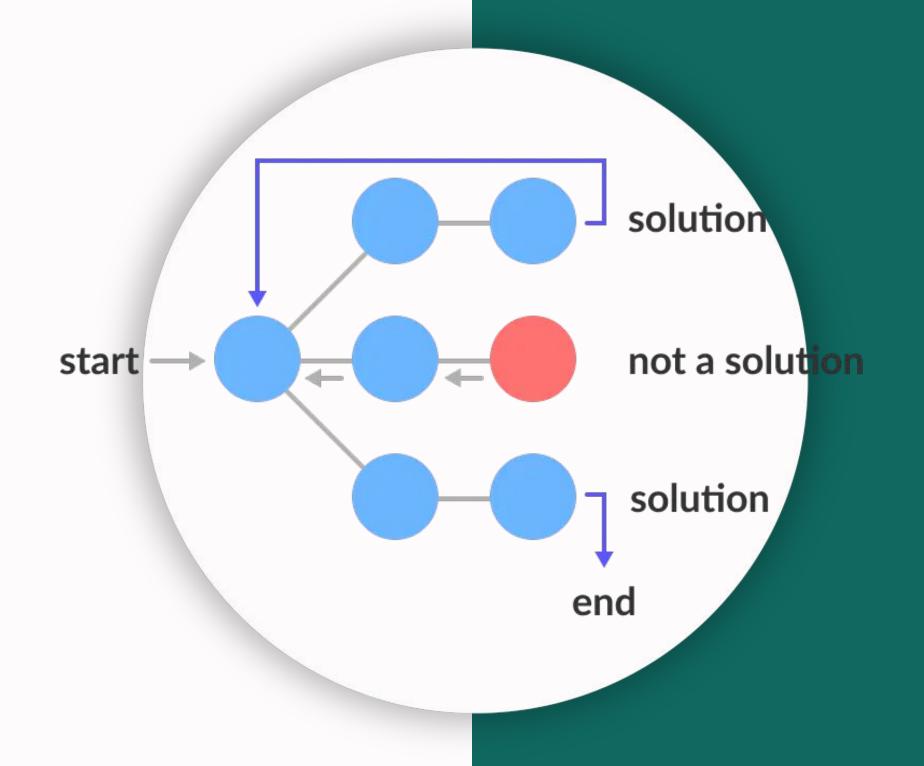


# IMPROVMENT OF BACKTRACKING

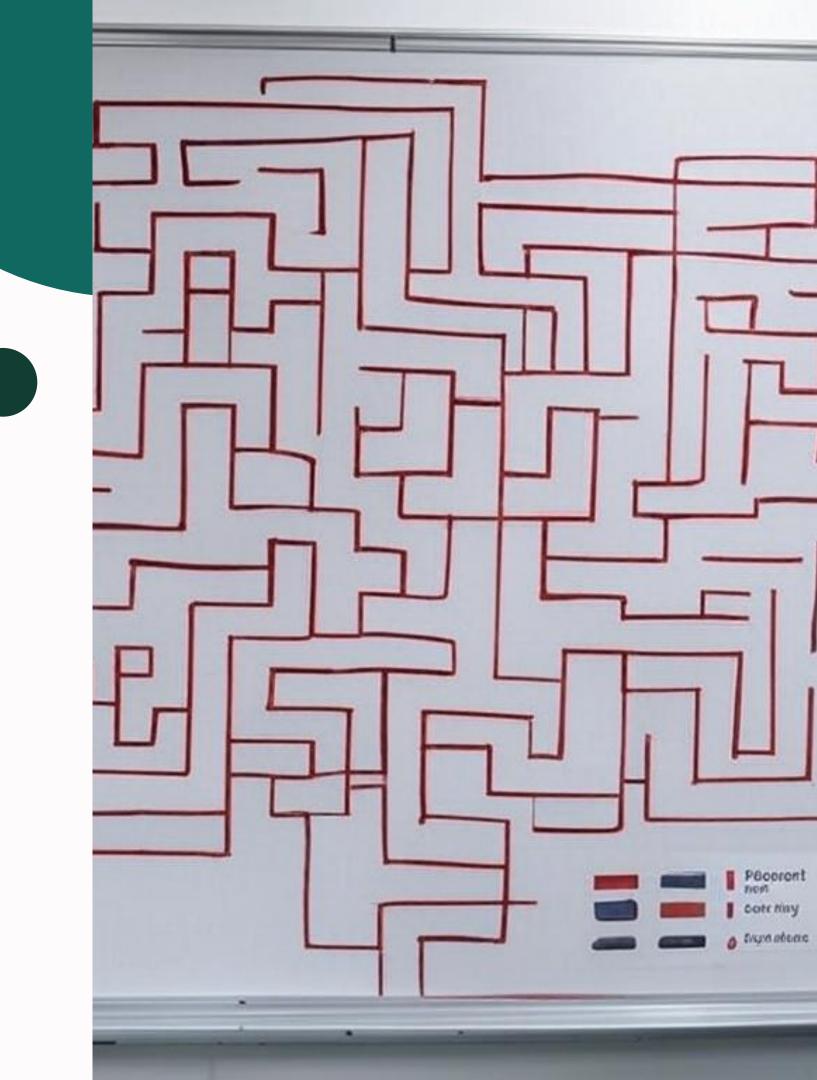


# Improving Backtracking with Arc Consistency (AC-3)

A More Efficient Approach to

**Constraint Satisfaction** 

Problems (CSPs)





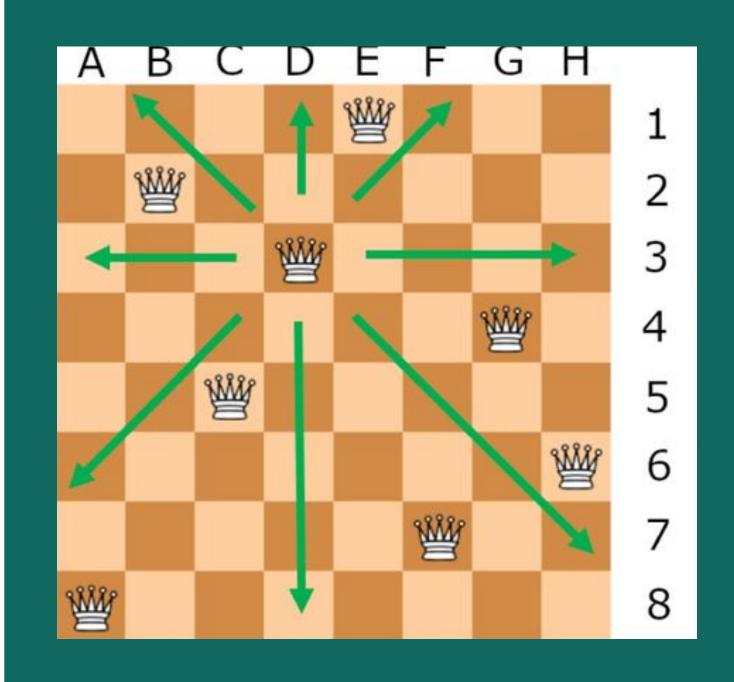
- - Backtracking alone is inefficient in CSPs with large search spaces.
  - - It often leads to unnecessary re-exploration of inconsistent paths.
  - - Solution? Arc Consistency (AC-3) helps reduce the

# What is Arc Consistency?

 - AC-3 is a constraint propagation algorithm.

 - It removes values that cannot be part of a consistent solution before search begins.

 - Works with binary constraints (relations between two



#### **How AC-3 Works?**

Convert each binary constraint into two arcs.

2 Add all arcs to an agenda (queue).

While the agenda is not empty:

 Take an arc (Xi, Xj) and check for consistency.

Remove values from Xi that don't satisfy the constraint with any value of X

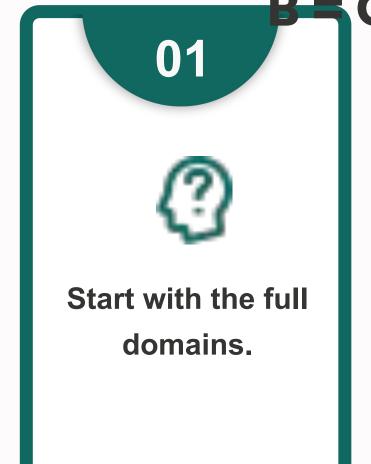
- If Xi is modified, add arcs (Xk, Xi) back to the agenda.

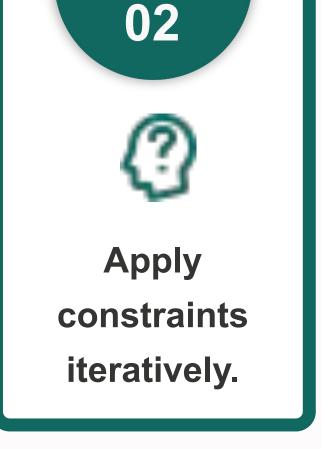
#### **AC-3 in Action**

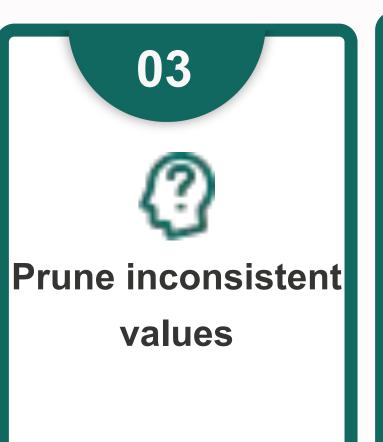
## (Example) Given variables and constraints:

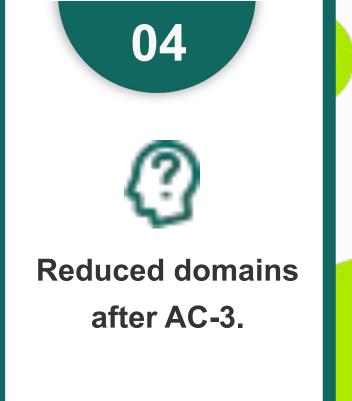
- Domains: {1,2,3,4} for A, B, and C
- - Constraints:

**A > B** 









### Solution

#### Problem Statement

$$\bullet A = \{1,2,3,4\}$$

$$\bullet B = \{1,2,3,4\}$$

$$\cdot C = \{1,2,3,4\}$$

•

- •Constraints:
- •1. A > B (A should be a proper superset of B)
- •2. B = C (B and C are equal sets)

#### Initial Domains and

• 
$$A = \{1,2,3,4\}, B = \{1,2,3,4\}, C = \{1,2,3,4\}$$

ets:

- •2. Apply constraints:
- B = C → No change in values.
- A > B → A must only contain values strictly greater than B.

Removing not larger

value exists in B).

• 
$$\rightarrow A = \{2,3,4\}$$

- •2. B = C remains unchanged for now.
- •3. Adjust B and C to maintain consistency:
- Since A > B, the
   largest B can have is 3
   (to ensure at least one
   element in A is greater
   than B).

Final Domain after arc Consistency

•Final Domains:

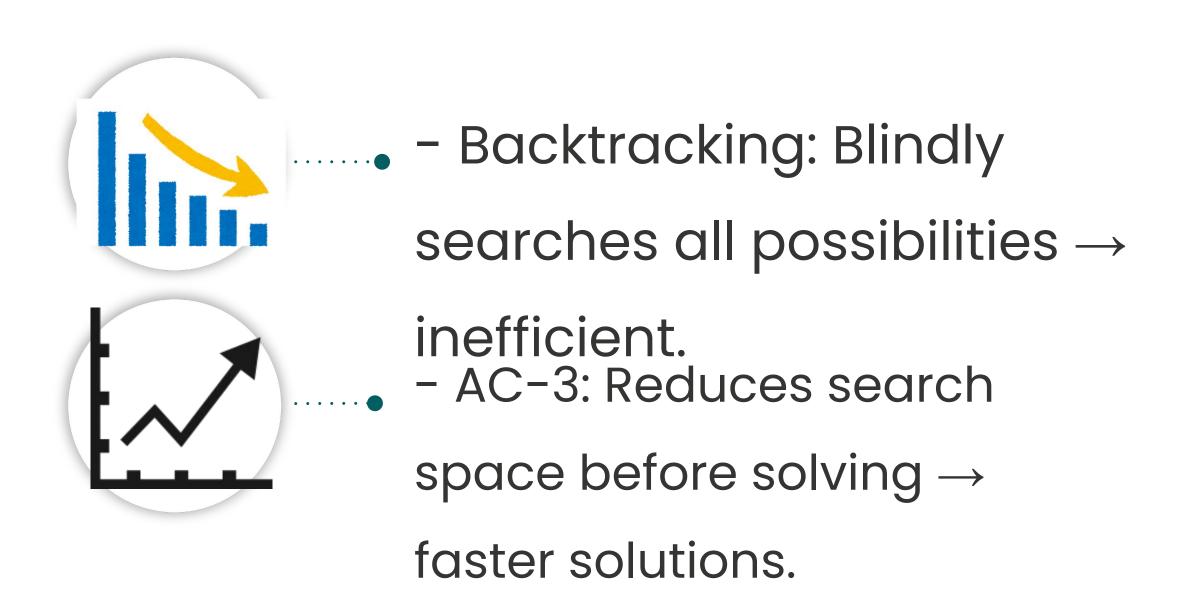
$$\bullet A = \{2,3,4\}$$

$$\bullet B = \{1,2,3\}$$

$$\cdot C = \{1,2,3\}$$

#### AC-3 vs.

### Backtracking





### Summary

AC-3 makes backtracking faster by eliminating inconsistent values before searching.

- Works best for binary constraints in CSPs.

Reduces unnecessary search space, leading to more efficient problem-solving.

