Homework 1

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Question 1 We will let H denote a heads and T denote a tails.

- (a) The sample space is given by $\mathcal{S} = \{HHH, HHT, HTH, HTT, THH, THT, TTH, TTT\}.$
- (b) We have
 - 1. $A = \text{at least two heads} = \{\text{HHH}, \text{HHT}, \text{HTH}, \text{THH}\}.$
 - 2. $B = \text{the first two tosses are heads} = \{\text{HHH}, \text{HHT}\}.$
 - 3. $C = \text{the last toss is a tail} = \{\text{HHT}, \text{HTT}, \text{THT}, \text{TTT}\}.$
- (c) We have
 - 1. $A^c = \{HTT, THT, TTH, TTT\}.$
 - 2. $A \cap B = \{HHH, HHT\} = B \text{ (since } B \subset A).$
 - 3. $A \cup C = \{HHH, HHT, HTH, HTT, THH, THT, TTT\}.$

Question 2