Project 2

Ex1

1. The BC can be defined as follows: X' = (X-C)C[+9] + Y'

Multiplying by Pt & det sunding.

=> x'= (n-c) (1+9) Pt + E'

\$ n' = (n-c) (1+9) t E'

2. V(X) z max { u(c) + BE+ V(X')}

=> V(X) = max &u(C) + B EtV(X) Pttl }

> V(n)= max {u(c) + B Et Vt+1 (nt+1). Pt+1 }

=> V(x) = Pt 1-0 [1-0 (t -0 + BEE VEHI (Ne+1) Pt 1-0]

=> V(n) = [- + B (1+9) = V++1 (74+1)]

091 V (n) = max { u (c) + B (1+9) + 6 E V' (n') }

3. -> These totansformation one useful sincer now we our gramove a state voorable & solve the partier using only cash in hand making it ordatively easier.

> If we solve for Fox we get:

Therefore, for convergence we seem that: $\frac{\beta R}{(1+9)^9} < 1.$

- We require $S=N-C_{0},0$ gind now we have a condition for pareoutrosing sawings.

Therefore at some point in the life ayole the housheld would like to borrow more than his sawings. This is not possible according to the bandget constraint.

Therefore, the household will sespond by decreasing their consumption.

$E_X 2$

- 1. Psuedo code:
- a) Set original paremeters of the model.
- b) Set an evenly spaced grud for carsh in hand, such that n>, p + c. The code instead of using a equidistant grid space uses taiple exponential grid.
- Solve for the eulean Equation & Horate making sure we do not violate the BC.
- d) This iteration involves intempolating over in and since c appears on both sides we have to use a nonlinear Solver.
- e) Finally we an check for convergence & update the function to solve the problem.

The simulation allows us to observe the dynamics over time. In particular we can check the evolution of our consumption policy & the eulers error which permits us to make bether approximation.

The eulers error is the arror generated at Cach simulation; where

Et = 1 - BR Et [(SCHI LICHI) - 6]

Therefore, by tetter estimating the earn't term we can get more pareose approximations.

As we increase there, the household becomes more stick average, hence the perecautionary savings increases leading to a joil in consumbion today; changing the consumption policy over time,

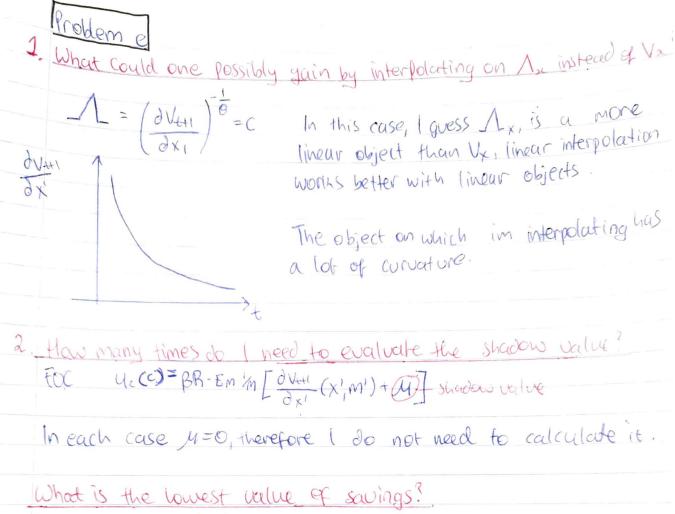
Therefore, consumption is different over time and has a higher volatility. This happens since now the uncertainty is higher in the cornerny inducing higher consumptions and a similar effect in n.

3. If we change the good size the culous equation ceause falls considerably. This is expected since, increasing the grid points we are approximating over more points making are estimation more prease. On average the Coras fall from 0.0266 to 6.114. The time taken by using 50 grid points its approximately 4 seconds more. Lastly increasing there, Increases the average

Egoroa, Since as agents one more such aware the culeus equation would show a greater dy prence in Ct & Ct+I Therefore incorporing the careful.

tx 3

2 a) Howards Heration converges much jastes than Fire Value junction Heration. This happons since now we use the policy function to Iterate and this deasion sule applies jor all pegiods, while in value jundion Heration we assume that the obcision suite is only for 2 periods. This is the meason for quicker convergence. The main difference between these methods the the way we iterate to find convergence. In VF1 Loe make initial guess of our value function at 1 Penad T and sales Herate backwoods. In Howards Improvement we identify our policy junction and identify a value junction given the dedsion Shule, while in the outers method sugurious orequoies that FOC is supposent to some the peroblem. The thouse methods are related Since they all Grequese the satisfaction of the For. the maximization paroblem with the BC. They all use the Bell man equation to find the southern to the peroblem.



Rewriting the budget constraint as. $0^1 \ge -0$ $0^1 \ge -0$ $0^1 \ge -\infty$ $0^1 \ge -\infty$

Therefore, S must be ≥ 0 , and the minimum value is S=0 at period T.

what's the highest possible value of savings?

If we assume households will always consume the minimum value of E and save the rest. We also assume that in each period they draw the best possible realisation of income shocks, therefore we can calculate the maximum amount of asset. And ultimately an afternative is to set an arbitrary x and then simulate the model. It x exceess the simulations we must increase x.

Problem e

Exagenous and method: Using the endagenous method consumption is in the right hard side of the manginal utility equation, therefore this method is quite costly, once we have to use non-linear systems of equations, using the exagenous method we can remove this problem, since consumption does a not show on the right hand side of the equation, so the problem is no larger non-linear. Moreover, we know the lowest point in the squing grid where $S = -\emptyset$. Furthermore we know for the

of $C \in LE, x+\Phi I$, cis linear.

"Consumption over the Lifecycle" Gourinchas and Parker (2002).

This paper estimates a structural model of optimal life-cycle consumption expenditures the presence of realistic labor income uncertainty. Additionally, it estimates a dynamic stochastic model of the life-cycle saving behaviour of households when they face exogenous, stochastic, labor income processes. In their model, the optimal choice of consumption depends not only on lifetime resources, the real interest rate, and the discount factor, but also on the expected growth rate of income, so that consumer behaviour may vary systematically as households age. They focus on estimation of structural preference parameters and upon characterizing optimal behaviour when households face exogenous, stochastic, labor income processes.

Using weak identifying assumptions they construct average total consumption and income profiles across the working lives of households of five different educational attainments and four different occupational groupings, using high quality household-level data on consumption and income from a sample of roughly 40,000 households from the Consumer Expenditure Survey from 1980 to 1993.

They use the Consumer Expenditure Survey to construct life-cycle profiles of consumption and income. The Consumer Expenditure Survey contains information about consumption expenditures, demographics, income and assets, for a large sample of the US population. They use the household survey data alongside simulation techniques to estimate a structural model of inter-temporal consumption choice with realistic levels of income uncertainty. Each household contributes one data point to the sample. For each household they construct a measure of household income and consumption. Based on the characteristics of the household, they assign the household to an occupation group, an education group, a birth cohort, an interview year and a Census region.

The paper yields four main findings:

- 1. The fitted model matches the correlation between consumption and income at young ages and the general concavity of the profile that is observed in the data.
- 2. They find reasonable estimates of the preference parameters. The average household has a discount rate of 4%-4.5% and a coefficient of relative risk aversion varying between 0.5%-1.4%.
- The paper contributes to the debate on the determinants of wealth accumulation. In our model, the relative shapes of the consumption and income profiles reveal the relative roles of precautionary and retirement motives for accumulating liquid assets.
- 4. They find strikingly different consumption behaviour for households at different ages: households behave like "buffer-stock" consumers early in the working lives and more like certainty-equivalent life-cycle hypothesis model households as retirement nears.

The model does much better in an economic sense than the certainty-equivalent life-cycle hypothesis model. In two places however, the model fit is not good. First, actual consumption exceeds simulated consumption early in life. Second, the actual consumption profile is slightly flatter and peaks slightly later.

They authors developed a new method for estimating household consumption behaviour in their mode. They model consumer behaviour in the presence of realistic levels of uninsurable income uncertainty and estimate preference parameters and household consumption behaviour using the Method of Simulated Moments. The model fits well and yields tight estimates of the discount rate and intertemporal elasticity of substitution.

Their results indicate that small holding of liquid assets by young households is an optimal response to expected income growth and the riskiness of future labor income over the life cycle. Until their early forties, household consumption behaviour, while fully optimal, appears short-sighted within the context of the certainty-equivalent life-cycle hypothesis model. Their results also imply that older households save actively for retirement purposes and behave in a manner more consistent with the certainty-equivalent life-cycle hypothesis model.