```
In [1]: import pandas as pd
import numpy as np
import matplotlib.pyplot as plt
import seaborn as sns
plt.rcParams['figure.figsize'] = [8,5]
plt.rcParams['font.size'] = 14
plt.rcParams['font.weight'] = 'bold'
plt.style.use('seaborn-whitegrid')
```

/var/folders/20/prf96pn926n0x2yzn\_v2yhbr0000gn/T/ipykernel\_17464/356 1387198.py:8: MatplotlibDeprecationWarning: The seaborn styles shipped by Matplotlib are deprecated since 3.6, as they no longer correspond to the styles shipped by seaborn. However, they will remain available as 'seaborn-v0\_8-<style>'. Alternatively, directly use the seaborn API instead.

plt.style.use('seaborn-whitegrid')

```
In [2]: df = pd.read_csv("/Users/akheruddinahmed/ML/insurance.csv")
    print('\nNumber of rows and columns in the data set: ',df.shape)
    print('')
    df.head()
```

Number of rows and columns in the data set: (1338, 7)

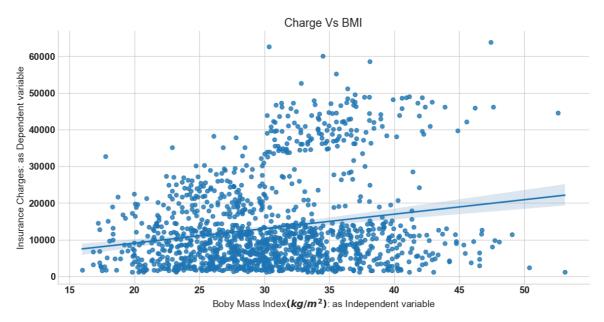
### Out[2]:

	age	sex	bmi	children	smoker	region	charges
0	19	female	27.900	0	yes	southwest	16884.92400
1	18	male	33.770	1	no	southeast	1725.55230
2	28	male	33.000	3	no	southeast	4449.46200
3	33	male	22.705	0	no	northwest	21984.47061
4	32	male	28.880	0	no	northwest	3866.85520

## In [3]: """ for our visualization purpose will fit line using seaborn library and charges as dependent variable""" sns.lmplot(x='bmi',y='charges',data=df,aspect=2,height=6) plt.xlabel('Boby Mass Index\$(kg/m^2)\$: as Independent variable') plt.ylabel('Insurance Charges: as Dependent variable') plt.title('Charge Vs BMI');

/Users/akheruddinahmed/anaconda3/lib/python3.11/site-packages/seabor n/axisgrid.py:118: UserWarning: The figure layout has changed to tig ht



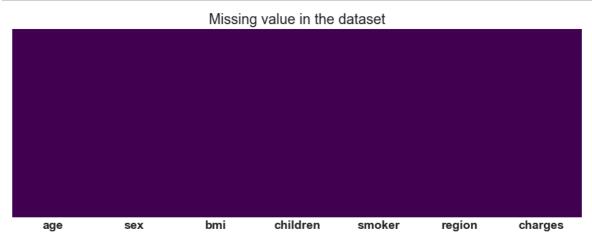


In [4]: df.describe()

## Out[4]:

	age	bmi	children	charges
count	1338.000000	1338.000000	1338.000000	1338.000000
mean	39.207025	30.663397	1.094918	13270.422265
std	14.049960	6.098187	1.205493	12110.011237
min	18.000000	15.960000	0.000000	1121.873900
25%	27.000000	26.296250	0.000000	4740.287150
50%	39.000000	30.400000	1.000000	9382.033000
75%	51.000000	34.693750	2.000000	16639.912515
max	64.000000	53.130000	5.000000	63770.428010

```
In [5]: plt.figure(figsize=(12,4))
    sns.heatmap(df.isnull(),cbar=False,cmap='viridis',yticklabels=False)
    plt.title('Missing value in the dataset');
```



```
In [6]: # correlation plot
    corr = df.corr()
    sns.heatmap(corr, cmap = 'Wistia', annot= True);
```

\_\_\_\_\_\_

```
ValueError
                                           Traceback (most recent cal
l last)
Cell In[6], line 2
      1 # correlation plot
----> 2 corr = df<sub>•</sub>corr()
      3 sns.heatmap(corr, cmap = 'Wistia', annot= True)
File ~/anaconda3/lib/python3.11/site-packages/pandas/core/frame.py:1
0054, in DataFrame.corr(self, method, min_periods, numeric_only)
  10052 cols = data_columns
  10053 idx = cols.copy()
> 10054 mat = data.to_numpy(dtype=float, na_value=np.nan, copy=Fals
e)
  10056 if method == "pearson":
            correl = libalgos.nancorr(mat, minp=min periods)
  10057
File ~/anaconda3/lib/python3.11/site-packages/pandas/core/frame.py:1
838, in DataFrame.to_numpy(self, dtype, copy, na_value)
   1836 if dtype is not None:
            dtype = np.dtype(dtype)
-> 1838 result = self._mgr.as_array(dtype=dtype, copy=copy, na_value
=na value)
   1839 if result.dtype is not dtype:
            result = np.array(result, dtype=dtype, copy=False)
File ~/anaconda3/lib/python3.11/site-packages/pandas/core/internals/
managers.py:1732, in BlockManager.as array(self, dtype, copy, na val
ue)
                arr.flags.writeable = False
   1730
   1731 else:
-> 1732
            arr = self._interleave(dtype=dtype, na_value=na_value)
   1733
            # The underlying data was copied within _interleave, so
no need
            # to further copy if copy=True or setting na_value
   1734
   1736 if na_value is not lib.no_default:
File ~/anaconda3/lib/python3.11/site-packages/pandas/core/internals/
managers.py:1794, in BlockManager._interleave(self, dtype, na_value)
   1792
            else:
   1793
                arr = blk get values(dtype)
-> 1794
            result[rl.indexer] = arr
            itemmask[rl.indexer] = 1
   1795
   1797 if not itemmask.all():
ValueError: could not convert string to float: 'female'
```

```
In [7]: f= plt.figure(figsize=(12,4))

ax=f.add_subplot(121)
sns.distplot(df['charges'],bins=50,color='r',ax=ax)
ax.set_title('Distribution of insurance charges')

ax=f.add_subplot(122)
sns.distplot(np.log10(df['charges']),bins=40,color='b',ax=ax)
ax.set_title('Distribution of insurance charges in $log$ sacle')
ax.set_xscale('log');
```

/var/folders/20/prf96pn926n0x2yzn\_v2yhbr0000gn/T/ipykernel\_17464/111
9713767.py:4: UserWarning:

`distplot` is a deprecated function and will be removed in seaborn v 0.14.0.

Please adapt your code to use either `displot` (a figure-level funct ion with

similar flexibility) or `histplot` (an axes-level function for histo grams).

For a guide to updating your code to use the new functions, please see

https://gist.github.com/mwaskom/de44147ed2974457ad6372750bbe5751 (https://gist.github.com/mwaskom/de44147ed2974457ad6372750bbe5751)

sns.distplot(df['charges'],bins=50,color='r',ax=ax)
/var/folders/20/prf96pn926n0x2yzn\_v2yhbr0000gn/T/ipykernel\_17464/111
9713767.py:8: UserWarning:

`distplot` is a deprecated function and will be removed in seaborn v 0.14.0.

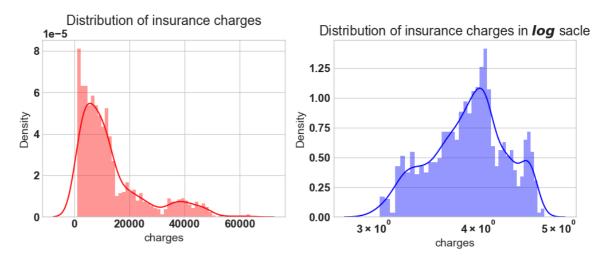
Please adapt your code to use either `displot` (a figure-level funct ion with

similar flexibility) or `histplot` (an axes-level function for histo
grams).

For a guide to updating your code to use the new functions, please s

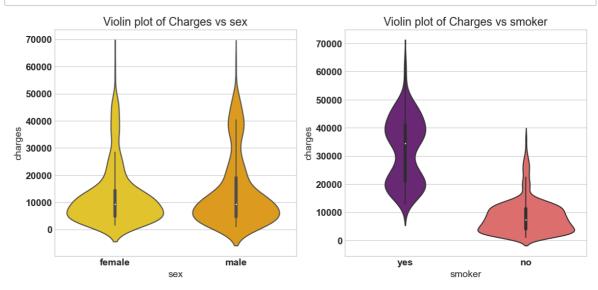
https://gist.github.com/mwaskom/de44147ed2974457ad6372750bbe5751 (https://gist.github.com/mwaskom/de44147ed2974457ad6372750bbe5751)

sns.distplot(np.log10(df['charges']),bins=40,color='b',ax=ax)

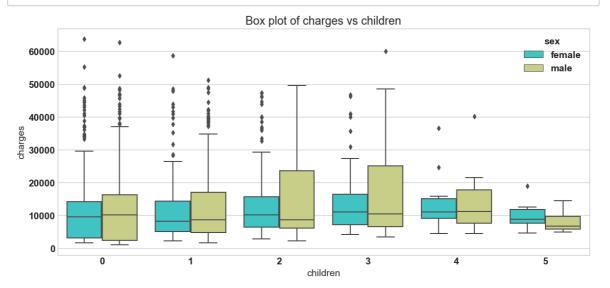


```
In [8]: f = plt.figure(figsize=(14,6))
    ax = f.add_subplot(121)
    sns.violinplot(x='sex', y='charges',data=df,palette='Wistia',ax=ax)
    ax.set_title('Violin plot of Charges vs sex')

ax = f.add_subplot(122)
    sns.violinplot(x='smoker', y='charges',data=df,palette='magma',ax=ax)
    ax.set_title('Violin plot of Charges vs smoker');
```

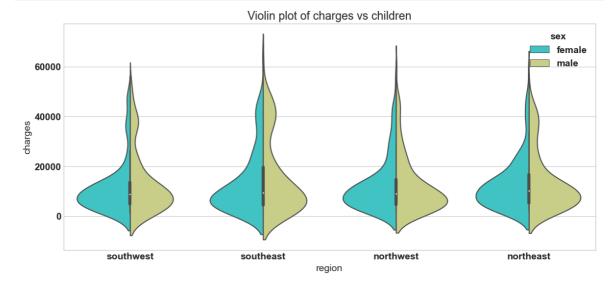


In [9]: plt.figure(figsize=(14,6))
 sns.boxplot(x='children', y='charges',hue='sex',data=df,palette='raint
 plt.title('Box plot of charges vs children');



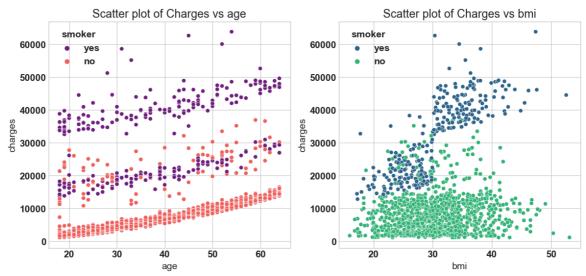
```
df.groupby('children').agg(['mean', 'min', 'max'])['charges']
In [10]:
          Sipyi40Z, in wrappeucythonopi_cython_op_nuim_compat(Seti,
         n_count, ngroups, comp_ids, mask, result_mask, **kwargs)
                      result_mask = result_mask[None, :]
          --> 482 res = self._call_cython_op(
             483
                      values2d,
             484
                      min count=min count,
             485
                      ngroups=ngroups,
                      comp_ids=comp_ids,
             486
             487
                      mask=mask,
             488
                      result_mask=result_mask,
             489
                      **kwarqs,
             490 )
             491 if res.shape[0] == 1:
```

In [11]: plt.figure(figsize=(14,6))
 sns.violinplot(x='region', y='charges',hue='sex',data=df,palette='rair
 plt.title('Violin plot of charges vs children');



```
In [12]: f = plt.figure(figsize=(14,6))
    ax = f.add_subplot(121)
    sns.scatterplot(x='age',y='charges',data=df,palette='magma',hue='smoke
    ax.set_title('Scatter plot of Charges vs age')

ax = f.add_subplot(122)
    sns.scatterplot(x='bmi',y='charges',data=df,palette='viridis',hue='smotax.set_title('Scatter plot of Charges vs bmi')
    plt.savefig('sc.png');
```



```
In [14]: # Lets verify the dummay variable process
print('Columns in original data frame:\n',df.columns.values)
print('\nNumber of rows and columns in the dataset:',df.shape)
print('\nColumns in data frame after encoding dummy variable:\n',df_er
print('\nNumber of rows and columns in the dataset:',df_encode.shape)
```

Number of rows and columns in the dataset: (1338, 13)

```
Columns in original data frame:
  ['age' 'sex' 'bmi' 'children' 'smoker' 'region' 'charges']

Number of rows and columns in the dataset: (1338, 7)

Columns in data frame after encoding dummy variable:
  ['age' 'bmi' 'charges' 'OHE_male' 'OHE_1' 'OHE_2' 'OHE_3' 'OHE_4'
'OHE_5'
  'OHE_yes' 'OHE_northwest' 'OHE_southeast' 'OHE_southwest']
```

```
In [15]: from scipy.stats import boxcox
         y_bc,lam, ci= boxcox(df_encode['charges'],alpha=0.05)
         #df['charges'] = y_bc
         # it did not perform better for this model, so log transform is used
         ci.lam
Out[15]: ((-0.01140290617294196, 0.0988096859767545), 0.043649053770664956)
In [16]: ## Log transform
         df encode['charges'] = np.log(df encode['charges'])
In [17]: from sklearn.model selection import train test split
         X = df_encode.drop('charges',axis=1) # Independet variable
         y = df_encode['charges'] # dependent variable
         X_train, X_test, y_train, y_test = train_test_split(X,y,test_size=0.3,
In [18]: \# Step 1: add x0 = 1 to dataset
         X_train_0 = np.c_[np.ones((X_train.shape[0],1)),X_train]
         X \text{ test } 0 = \text{np.c } [\text{np.ones}((X \text{ test.shape}[0],1)), X \text{ test}]
         # Step2: build model
         theta = np.matmul(np.linalg.inv( np.matmul(X_train_0.T,X_train_0) ), r
In [19]: # The parameters for linear regression model
         parameter = ['theta_'+str(i) for i in range(X_train_0.shape[1])]
         columns = ['intersect:x_0=1'] + list(X.columns.values)
         parameter df = pd.DataFrame({'Parameter':parameter,'Columns':columns,
```

# In [20]: # Scikit Learn module from sklearn.linear\_model import LinearRegression lin\_reg = LinearRegression() lin\_reg.fit(X\_train,y\_train) # Note: x\_0 =1 is no need to add, sklearn #Parameter sk\_theta = [lin\_reg.intercept\_]+list(lin\_reg.coef\_) parameter\_df = parameter\_df.join(pd.Series(sk\_theta, name='Sklearn\_theparameter\_df

## Out [20]:

	Parameter	Columns	theta	Sklearn_theta
0	theta_0	intersect:x_0=1	7.059171	7.059171
1	theta_1	age	0.033134	0.033134
2	theta_2	bmi	0.013517	0.013517
3	theta_3	OHE_male	-0.067767	-0.067767
4	theta_4	OHE_1	0.149457	0.149457
5	theta_5	OHE_2	0.272919	0.272919
6	theta_6	OHE_3	0.244095	0.244095
7	theta_7	OHE_4	0.523339	0.523339
8	theta_8	OHE_5	0.466030	0.466030
9	theta_9	OHE_yes	1.550481	1.550481
10	theta_10	OHE_northwest	-0.055845	-0.055845
11	theta_11	OHE_southeast	-0.146578	-0.146578
12	theta_12	OHE_southwest	-0.133508	-0.133508

```
In [21]: # Normal equation
y_pred_norm = np.matmul(X_test_0,theta)

#Evaluvation: MSE
J_mse = np.sum((y_pred_norm - y_test)**2)/ X_test_0.shape[0]

# R_square
sse = np.sum((y_pred_norm - y_test)**2)
sst = np.sum((y_test - y_test.mean())**2)
R_square = 1 - (sse/sst)
print('The Mean Square Error(MSE) or J(theta) is: ',J_mse)
print('R square obtain for normal equation method is:',R_square)
```

The Mean Square Error(MSE) or J(theta) is: 0.18729622322981962 R square obtain for normal equation method is: 0.779568754505531

```
In [22]: # sklearn regression module
y_pred_sk = lin_reg.predict(X_test)

#Evaluvation: MSE
from sklearn.metrics import mean_squared_error
J_mse_sk = mean_squared_error(y_pred_sk, y_test)

# R_square
R_square
R_square_sk = lin_reg.score(X_test,y_test)
print('The Mean Square Error(MSE) or J(theta) is: ',J_mse_sk)
print('R square obtain for scikit learn library is:',R_square_sk)
```

The Mean Square Error(MSE) or J(theta) is: 0.18729622322981904 R square obtain for scikit learn library is: 0.7795687545055316

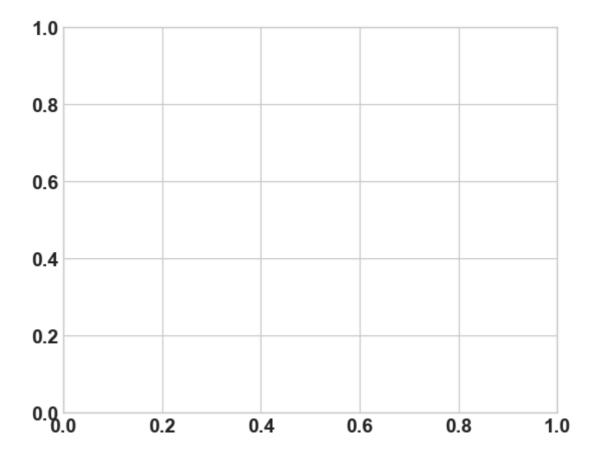
```
In [23]: # Check for Linearity
f = plt.figure(figsize=(14,5))
ax = f.add_subplot(121)
sns.scatterplot(y_test,y_pred_sk,ax=ax,color='r')
ax.set_title('Check for Linearity:\n Actual Vs Predicted value')

# Check for Residual normality & mean
ax = f.add_subplot(122)
sns.distplot((y_test - y_pred_sk),ax=ax,color='b')
ax.axvline((y_test - y_pred_sk).mean(),color='k',linestyle='--')
ax.set_title('Check for Residual normality & mean: \n Residual eror');
```

\_\_\_\_\_

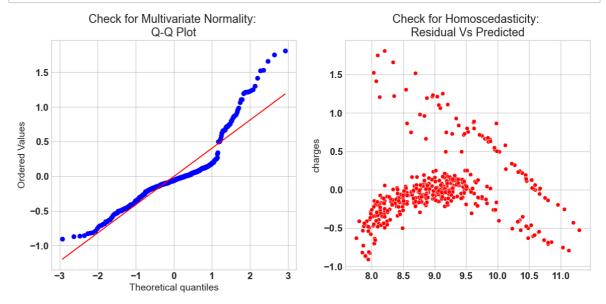
```
TypeError
l last)
Cell In[23], line 4
        2 f = plt.figure(figsize=(14,5))
        3 ax = f.add_subplot(121)
----> 4 sns.scatterplot(y_test,y_pred_sk,ax=ax,color='r')
        5 ax.set_title('Check for Linearity:\n Actual Vs Predicted value')
        7 # Check for Residual normality & mean
```

TypeError: scatterplot() takes from 0 to 1 positional arguments but
2 positional arguments (and 1 keyword-only argument) were given



```
In [24]: # Check for Multivariate Normality
# Quantile-Quantile plot
f,ax = plt.subplots(1,2,figsize=(14,6))
import scipy as sp
__,(_,_,r)= sp.stats.probplot((y_test - y_pred_sk),fit=True,plot=ax[0])
ax[0].set_title('Check for Multivariate Normality: \nQ-Q Plot')

#Check for Homoscedasticity
sns.scatterplot(y = (y_test - y_pred_sk), x= y_pred_sk, ax = ax[1],colax[1].set_title('Check for Homoscedasticity: \nResidual Vs Predicted')
```



In [25]: # Check for Multicollinearity
#Variance Inflation Factor
VIF = 1/(1- R\_square\_sk)
VIF

Out[25]: 4.536561945911133

In [ ]: