## 1 Rewrite the algorithm

## Algorithm 1 FJ source code

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Inputs: k_{\min}, k_{\max}, \epsilon, initial parameters \hat{\boldsymbol{\theta}} = \{\hat{\boldsymbol{\theta}}_1, \dots, \hat{\boldsymbol{\theta}}_{k_{\max}}, \hat{\alpha}_1, \dots, \hat{\alpha}_{k_{\max}}\}
Output: Mixture model in \hat{\boldsymbol{\theta}}_{\text{best}}
   1: t \leftarrow 0, k_{nz} \leftarrow k_{\max}, \mathcal{L}_{\min} \leftarrow +\infty
    2: u_m^{(i)} \leftarrow p(\boldsymbol{y}^{(i)}|\hat{\boldsymbol{\theta}}_m), for m = 1, \dots, k_{\text{max}}, and i = 1, \dots, n
   3: while k_{nz} \ge k_{\min} do
                  repeat
   4:
                           t \leftarrow t + 1
   5:
                          for m = 1 to k_{\text{max}} do
w_m^{(i)} \leftarrow \hat{\alpha}_m u_m^{(i)} \left( \sum_{j=1}^{k_{\text{max}}} \hat{\alpha}_j u_j^{(i)} \right)^{-1}, \text{ for } i = 1, \dots, n
\hat{\alpha}_m \leftarrow \max \left\{ 0, \left( \sum_{i=1}^n w_m^{(i)} \right) - \frac{N}{2} \right\} / n
   6:
   7:
   8:
                                  \{\hat{\alpha}_1, \dots, \hat{\alpha}_{k_{\max}}\} \leftarrow \{\hat{\alpha}_1, \dots, \hat{\alpha}_{k_{\max}}\} \left(\sum_{m=1}^{k_{\max}} \hat{\alpha}_m\right)^{-1}
   9:
                                  if \hat{\alpha}_m > 0 then
 10:
                                         \hat{\boldsymbol{\theta}}_m \leftarrow \operatorname*{arg\,max} \log p(\mathcal{Y}, \mathcal{W} | \boldsymbol{\theta})
 11:
                                        u_m^{(i)} \leftarrow p(\mathbf{y}^{(i)}|\hat{\boldsymbol{\theta}}_m) \text{ for } i = 1, \dots, n
 12:
 13:
                                          k_{nz} \leftarrow k_{nz} - 1
 14:
                                  end if
 15:
                           end for

\hat{\boldsymbol{\theta}}(t) \leftarrow \{\hat{\boldsymbol{\theta}}_1, \dots, \hat{\boldsymbol{\theta}}_{k_{\text{max}}}, \hat{\alpha}_1, \dots, \hat{\alpha}_{k_{\text{max}}}\} 

L(t) \leftarrow \sum_{i=1}^n \log \sum_{m=1}^k \hat{\alpha}_m u_n^{(i)} 

\mathbf{until} \ |L(t) - L(t-1)| < \epsilon |L(t-1)| 

\mathcal{L}[\hat{\boldsymbol{\theta}}(t), \mathcal{Y}] \leftarrow \frac{N}{2} \sum_{m: \hat{\alpha}_m > 0} \log \hat{\alpha}_m + \frac{1}{2}k(N+1)\log n - L(t)

 17:
 18:
 19:
 20:
                   if \mathcal{L}[\hat{\boldsymbol{\theta}}(t), \mathcal{Y}] \leq \mathcal{L}_{\min} then
 21:
                          \mathcal{L}_{\min} \leftarrow \mathcal{L}[\hat{\boldsymbol{\theta}}(t), \mathcal{Y}]
 22:
                          \hat{\boldsymbol{\theta}}_{\text{best}} \leftarrow \hat{\boldsymbol{\theta}}(t)
 23:
 24:
                   end if
                   m^* \leftarrow \arg\min\{\hat{\alpha}_m > 0\}, \, \hat{\alpha}_{m^*} \leftarrow 0, \, k_{nz} \leftarrow k_{nz} - 1
 25:
                   \{\hat{\alpha}_1, \dots, \hat{\alpha}_{k_{\max}}\} \leftarrow \{\hat{\alpha}_1, \dots, \hat{\alpha}_{k_{\max}}\} \left(\sum_{m=1}^{k_{\max}} \hat{\alpha}_m\right)^{-1}
27: end while
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