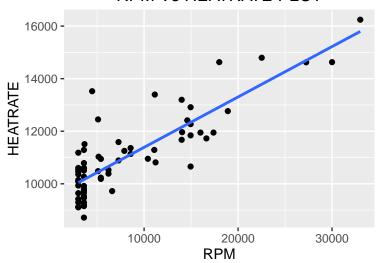
CSC 423 Homework 4

Akhil Kumar Ramasagaram April 30, 2016

5.8 Cooling method for gas turbines.

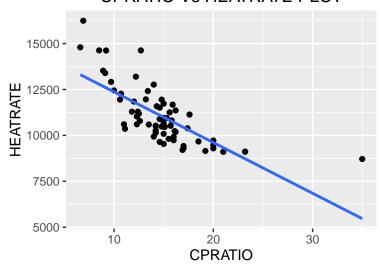
```
library(ggplot2)
library(gridExtra)
load("rdata/GASTURBINE.Rdata")
ggplot(GASTURBINE, aes( x = RPM, y = HEATRATE)) + geom_point() +
  geom_smooth(method = "lm", se = F) + ggtitle("RPM Vs HEATRATE PLOT")
```

RPM Vs HEATRATE PLOT



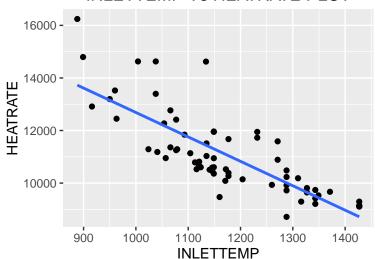
```
ggplot(GASTURBINE, aes( x = CPRATIO, y = HEATRATE)) + geom_point() +
geom_smooth(method = "lm", se = F) + ggtitle("CPRATIO Vs HEATRATE PLOT")
```

CPRATIO Vs HEATRATE PLOT



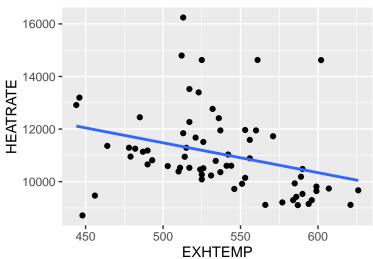
```
ggplot(GASTURBINE, aes( x = INLETTEMP, y = HEATRATE)) + geom_point() +
geom_smooth(method = "lm", se = F) + ggtitle("INLETTEMP Vs HEATRATE PLOT")
```

INLETTEMP Vs HEATRATE PLOT

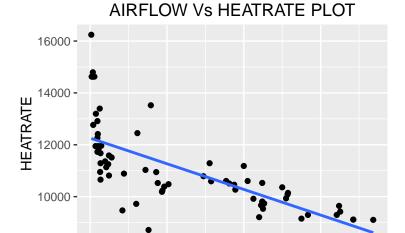


```
ggplot(GASTURBINE, aes( x = EXHTEMP, y = HEATRATE)) + geom_point() +
geom_smooth(method = "lm", se = F) + ggtitle("EXHTEMP Vs HEATRATE PLOT")
```

EXHTEMP Vs HEATRATE PLOT



```
ggplot(GASTURBINE, aes( x = AIRFLOW, y = HEATRATE)) + geom_point() +
geom_smooth(method = "lm", se = F) + ggtitle("AIRFLOW Vs HEATRATE PLOT")
```



400

AIRFLOW

A linear model can be used to predict the heat rate using RPM but for other variables the linear model doesn't capture the pattern. I think a polynomial model will be a better option for the remaining variables.

600

5.19 Cooling method for gas turbines.

200

- a) A second order model using RPM & CPRATIO can be written as. $Heatrate = \beta_0 + \beta_1 * RPM + \beta_2 * CPRATIO + \beta_3 * (RPM)^2 + \beta_4 * (CPRATIO)^2$
- b) Below is the fit.

Ö

```
full_lm_model <- lm(HEATRATE ~ RPM + CPRATIO, data = GASTURBINE)
reduced_lm_model <- lm(HEATRATE ~ poly(RPM, 2) + poly(CPRATIO, 2), data = GASTURBINE)
summary(reduced_lm_model)</pre>
```

```
##
## Call:
##
  lm(formula = HEATRATE ~ poly(RPM, 2) + poly(CPRATIO, 2), data = GASTURBINE)
##
## Residuals:
##
        Min
                  1Q
                       Median
                                    3Q
                                            Max
  -1126.51 -293.22
                       -42.15
                                291.84
                                        1932.16
##
##
##
  Coefficients:
##
                     Estimate Std. Error t value Pr(>|t|)
## (Intercept)
                     11066.43
                                   68.64 161.220 < 2e-16 ***
## poly(RPM, 2)1
                      6941.98
                                  711.56
                                           9.756 3.84e-14 ***
## poly(RPM, 2)2
                      -744.40
                                  582.93
                                          -1.277
                                                    0.206
## poly(CPRATIO, 2)1 -6134.29
                                  662.54
                                          -9.259 2.68e-13 ***
## poly(CPRATIO, 2)2
                      2776.16
                                  638.09
                                           4.351 5.16e-05 ***
##
## Signif. codes: 0 '***' 0.001 '**' 0.05 '.' 0.1 ' ' 1
##
## Residual standard error: 561.9 on 62 degrees of freedom
## Multiple R-squared: 0.8834, Adjusted R-squared: 0.8759
## F-statistic: 117.5 on 4 and 62 DF, p-value: < 2.2e-16
```

c)

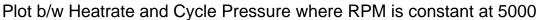
```
anova(full_lm_model, reduced_lm_model)
```

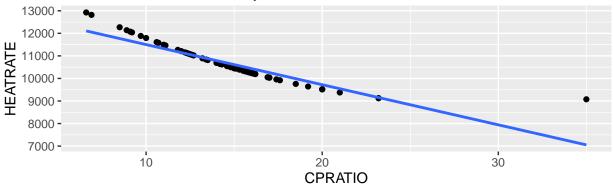
```
## Analysis of Variance Table
##
## Model 1: HEATRATE ~ RPM + CPRATIO
## Model 2: HEATRATE ~ poly(RPM, 2) + poly(CPRATIO, 2)
## Res.Df RSS Df Sum of Sq F Pr(>F)
## 1 64 25553200
## 2 62 19572351 2 5980848 9.4729 0.0002571 ***
## ---
## Signif. codes: 0 '***' 0.001 '**' 0.05 '.' 0.1 ' ' 1
```

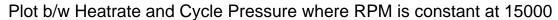
As the p-value is significant, we will reject the H_o that $\beta_3 = \beta_4 = 0$ and conclude that the quadratic terms are significant.

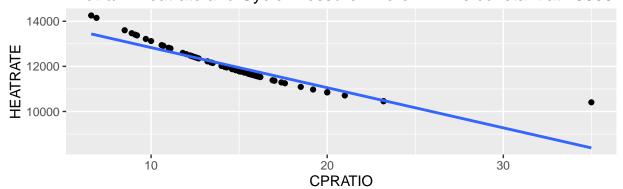
```
d), e) & f)
```

```
graph_prediction <- function(x){
   predictions = predict(reduced_lm_model, newdata = data.frame(RPM = x, CPRATIO = GASTURBINE$CPRATIO))
   new_data = data.frame("HEATRATE" = predictions, "CPRATIO" = GASTURBINE$CPRATIO)
   ggplot(new_data, aes(x = CPRATIO, y = HEATRATE)) + geom_point() + geom_smooth(method = "lm", se = F)
}
grid.arrange(graph_prediction(5000), graph_prediction(15000), ncol = 1)</pre>
```









```
predict(reduced_lm_model, newdata = data.frame(RPM = 15000, CPRATIO = GASTURBINE$CPRATIO)) -
predict(reduced_lm_model, newdata = data.frame(RPM = 5000, CPRATIO = GASTURBINE$CPRATIO))
                           3
                                             5
## 1331.631 1331.631 1331.631 1331.631 1331.631 1331.631 1331.631
##
                 10
                          11
                                   12
                                            13
                                                     14
                                                              15
## 1331.631 1331.631 1331.631 1331.631 1331.631 1331.631 1331.631
                                   20
                 18
                                            21
                                                     22
                                                              23
##
        17
                          19
## 1331.631 1331.631 1331.631 1331.631 1331.631 1331.631 1331.631
                 26
##
        25
                          27
                                   28
                                            29
                                                     30
                                                              31
                                                                       32
## 1331.631 1331.631 1331.631 1331.631 1331.631 1331.631 1331.631
                 34
                          35
                                   36
                                            37
                                                     38
                                                              39
                                                                       40
## 1331.631 1331.631 1331.631 1331.631 1331.631 1331.631 1331.631
                 42
                          43
                                   44
                                            45
                                                     46
## 1331.631 1331.631 1331.631 1331.631 1331.631 1331.631 1331.631
##
                 50
                          51
                                   52
                                            53
                                                     54
## 1331.631 1331.631 1331.631 1331.631 1331.631 1331.631 1331.631
                 58
                          59
                                   60
                                            61
                                                     62
## 1331.631 1331.631 1331.631 1331.631 1331.631 1331.631 1331.631
        65
                 66
## 1331.631 1331.631 1331.631
Although the graphs are similar the predictions are off by 1331.631. This can be interpreted for 10,000
increase in RPM the heat rate is expected to increase by 1331.631.
```

5.20 Tire wear and pressure.

```
load("rdata/TIRES2.Rdata")

a) The equation using coding system for pressure is u=(x-\bar{x})/s_x
b)

TIRES2$U <- (TIRES2$X_PSI - mean(TIRES2$X_PSI))/sd(TIRES2$X_PSI)

TIRES2$U

## [1] -1.3887301 -0.9258201 -0.4629100 0.0000000 0.4629100 0.9258201

## [7] 1.3887301

TIRES2$U2 <- TIRES2$U^2

TIRES2$U2

## [1] 1.9285714 0.8571429 0.2142857 0.0000000 0.2142857 0.8571429 1.9285714

c) & d)

cor(TIRES2$X_PSI, TIRES2$X_PSI^2)
```

```
cor(TIRES2$U, TIRES2$U2)
```

[1] 0

The variable are highly correlated in part c where as in part d it is 0 as they are standardized.

e)

```
lm_model <- lm(Y_THOUS ~ U + U2, TIRES2)
summary(lm_model)</pre>
```

```
##
## Call:
## lm(formula = Y THOUS ~ U + U2, data = TIRES2)
##
## Residuals:
##
        1
                2
                        3
                                        5
                                                6
   1.0714 -1.4286 -0.6429 0.4286 0.7857 0.4286 -0.6429
##
## Coefficients:
##
              Estimate Std. Error t value Pr(>|t|)
## (Intercept) 37.5714 0.6455 58.205 5.22e-07 ***
## U
                           0.4564 -1.014 0.367854
               -0.4629
                          0.5693 -9.369 0.000723 ***
## U2
               -5.3333
## ---
## Signif. codes: 0 '***' 0.001 '**' 0.05 '.' 0.1 ' ' 1
## Residual standard error: 1.118 on 4 degrees of freedom
## Multiple R-squared: 0.9569, Adjusted R-squared: 0.9353
## F-statistic: 44.4 on 2 and 4 DF, p-value: 0.001858
```

The equation can be written as $E(y) = 37.5714 - 0.4629 * U - 5.333 * U^2$. So for a unit increase in U mileage decreases by 0.46 units.

5.27 Quality of Bordeaux wine.

lets create a dummy dataset with 100 observations a)

```
##
## Call:
## lm(formula = quality ~ method * soil, data = wine_data)
##
```

```
## Residuals:
##
       Min
                10
                    Median
                                 30
                                        Max
   -4.9160 -1.9917
##
                    0.0256
                            1.8275
                                     5.6033
##
##
  Coefficients:
##
                            Estimate Std. Error t value Pr(>|t|)
## (Intercept)
                             4.39800
                                        0.70562
                                                   6.233 1.29e-08 ***
## methodmanual
                            -0.28133
                                        0.95542
                                                 -0.294
                                                          0.76905
## soilclay
                             2.70800
                                        0.99790
                                                   2.714
                                                          0.00792 **
## soilgravel
                            -0.01133
                                        0.89950
                                                 -0.013
                                                          0.98997
## methodmanual:soilclay
                            -0.69252
                                        1.39434
                                                 -0.497
                                                          0.62058
  methodmanual:soilgravel
                            0.92681
                                        1.32570
                                                  0.699
                                                          0.48621
##
                   0 '***' 0.001 '**' 0.01 '*' 0.05 '.' 0.1 ' ' 1
## Signif. codes:
##
## Residual standard error: 2.733 on 94 degrees of freedom
## Multiple R-squared: 0.1379, Adjusted R-squared: 0.09207
## F-statistic: 3.008 on 5 and 94 DF, p-value: 0.01457
```

- b) when a wine is made from grape which are picked automatically and grown on sand soil have a score of 4.39.
- c) β_0 is the intercept, β_1 is manual\$, β_2 is clay, β_3 is gravel, β_4 is manual&clay interaction & β_5 is manual&soil interaction. Since our base levels are automatic and sand, if the picking method is manual instead of automatic the wine quality is expected to decrease by 0.28 when everything is held at constant. If grapes are grown on a clay soil instead of sand soil we expect an 2.7 increase in wine quality when everything is held at constant.
- d) Its 0.28 units lower. This can be concluded from the β_1 estimate and from the below table.

```
aggregate(quality ~ method + soil, wine_data, mean)
```

```
##
     method
              soil quality
              sand 4.398000
## 1
       auto
## 2 manual
              sand 4.116667
## 3
       auto
              clay 7.106000
              clay 6.132143
## 4
    manual
## 5
       auto gravel 4.386667
## 6 manual gravel 5.032143
```

5.29 Impact of flavor name on consumer choice.

```
a) E(y) = \beta_0 + \beta_1 * x_1 + \beta_2 * x_2 + \beta_3 * (x_1 * x_2)
```

- b) β_0 will be the intercept which is the number of jelly's taken when flavour is ambiguous and cognitive load is high β_1 is the unit increase in jelly's taken when flavor is common and everything is held constant. β_2 is unit increase in jelly's taken when cognitive load is low and everything is held constant.
- c) We can find out the impact by just building a model with only flavor and then build another model by introducing it and compare the adjusted R squared, if it changed then there is an impact.

5.35 Lead in fern moss

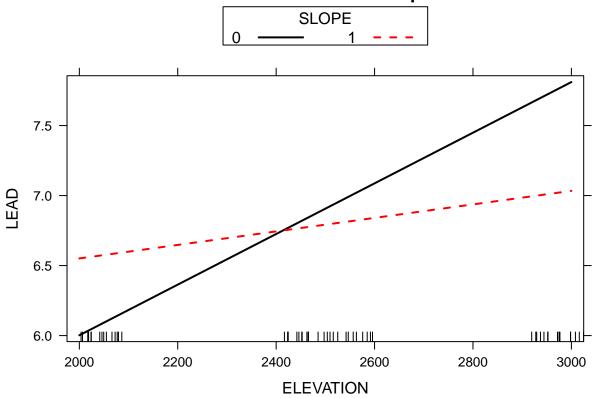
a)

The equation for first order model can be written as $E(y) = \beta_0 + \beta_1 * ELEVATION + \beta_2 * SLOPE + \beta_3 * (ELEVATION * SLOPE)$

b)

```
library(effects)
## Warning: package 'effects' was built under R version 3.2.4
load("rdata/LEADMOSS.Rdata")
lm_model <- lm(LEAD ~ ELEVATION*SLOPE, data = LEADMOSS)</pre>
summary(lm_model)
##
## Call:
## lm(formula = LEAD ~ ELEVATION * SLOPE, data = LEADMOSS)
##
## Residuals:
##
                1Q Median
                                3Q
       Min
                                       Max
## -4.8108 -2.8437 -1.2154 0.4023 22.3417
##
## Coefficients:
                    Estimate Std. Error t value Pr(>|t|)
##
## (Intercept)
                    2.384866
                               5.393140
                                          0.442
                                                   0.660
                    0.001809
                               0.002141
                                                   0.401
## ELEVATION
                                          0.845
## SLOPE
                    3.201458
                               7.669876
                                          0.417
                                                   0.678
## ELEVATION:SLOPE -0.001326
                               0.003028 -0.438
                                                   0.663
## Residual standard error: 5.132 on 66 degrees of freedom
## Multiple R-squared: 0.01151,
                                   Adjusted R-squared:
## F-statistic: 0.2562 on 3 and 66 DF, p-value: 0.8567
mean = mean(LEADMOSS$SLOPE)
sd = sd(LEADMOSS\$SLOPE)
plot(effect("ELEVATION:SLOPE", lm_model,, list(SLOPE=c(0,1))), multiline=TRUE)
```

ELEVATION*SLOPE effect plot



- c) For every one foot increase in elevation the lead level increase by 0.001809.
- d) As our p-value is 0.85 which is very high, at $\alpha=0.1$ we conclude that the above model is not significant to predict the lead level
- e) $E(y) = \beta_0 + \beta_1 * elevation + \beta_2 * elevation^2 + \beta_3 * slope + \beta_4 * slope^2$