

Size n of relation S	Avg execution time to scan S(in ms)	Avg execution time to sort S (in ms)
10	0.028	0.044
100	0.056	0.091
1000	0.290	0.688
10000	2.031	7.511
100000	26.252	166.614
1000000	202.440	1342.876
10000000	2220.582	16748.270
100000000	14,756.498	81476.678

3.a The above table determines the query plan for scanning and sorting as per the observation. Execution time for scanning is less compared to that of the execution time for sorting. The scanning and sorting time increases as the size n of the relation S increases.

3.b As the size of the relation S increases the execution time for sorting increases.

3.c Yes, it conforms with the formal time complexity of external sorting as it takes $O(n \log n)$ time. The file is subdivided into subparts of B blocks and each of these subfiles will be sorted in a parallel way and will be Merged. We will need to merge B Sorted files which will add up to $2N(\log_B(N))$. Hence it conforms with the formal time complexity of external sorting.

3.d Set work_mem='64kB'

Size n of relation S	Avg execution time to scan S(in ms)	Avg execution time to sort S (in ms)
10	0.036	0.026
100	0.041	0.074
1000	0.232	1.406
10000	2.183	10.324

100000	23.916	128.327
1000000	256.360	1079.581
10000000	2882.076	11936.966
100000000	14,882.586	112318.732

Set work_mem='1GB'

Size n of relation S	Avg execution time to scan S(in ms)	Avg execution time to sort S (in ms)
10	0.016	0.034
100	0.038	0.085
1000	0.212	0.847
10000	1.883	7.004
100000	20.081	82.512
1000000	193.151	926.272
10000000	2064.654	10366.519
100000000	15018.812	114788.745

3.e

Size n of relation S	Avg execution to create index indexedS(in ms)	Avg execution time for range query (in ms)
10	0.613	0.55
100	3.77	5.5
1000	28.7	30.23
10000	109	104.88
100000	800.34	700.55
1000000	9000	2300
10000000	88780	16450

100000000	970455	21340
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Average execution time for range query decreases compared to other above algorithms when using b+ indexing.

7. a. Size of node n can be calculated using the below

$$N \leq (\text{Block_size} - |\text{blockaddress}|) / (|\text{blockaddress}| + |\text{key}|)$$

$$N \leq (4096 - 9) / (9 + 8)$$

$$N \leq 4087 / 17$$

$$N \leq 240$$

$$N = N + 1 = 241 \text{ (adding 1 to N)}$$

Because each block can fit a maximum of 240 records.

$$\text{Minimum Time :- } ([\log_{241}(10^9 + 1)] + 1) * 10\text{ms}$$

$$= (9 (\log_{241} 10 + 1) + 1) * (10)\text{ms}$$

$$= 4 * 10 \text{ ms}$$

$$= 40 \text{ ms}$$

b. Calculating the maximum time to insert a record with a key will be taken when branching factor is minimum.

$$(240/2) + 1 = 121$$

$$\text{Height of the tree} = \log_{121}(10^9 + 1) * 10\text{ms}$$

$$= 5 * 10\text{ms} = 50\text{ms}$$

c. For Two Levels it will be= $4096 + (241 * 4096)$

$$= 991232 \text{ bytes}$$

$$= 1\text{MB}$$

For Three Levels it will be= $1\text{MB} + (241)^2 * 4096$

$$= 238899768$$

$$= 238\text{MB}$$

10. Size = 400

Execution-Time: 0.280 ms

Size = 4000

Execution-Time: 1.280 ms

Size = 40000

Execution-Time: 8.258 ms

11. Size = 400

Execution-Time: 0.426 ms

Size = 4000

Execution-Time: 3.175 ms

Size = 40000

Execution-Time: 13.755 ms

12. Size = 400

Execution-Time: 0.285 ms

Size = 4000

Execution-Time: 0.963 ms

Size = 40000

Execution-Time: 4.052 ms

13. **For Join Or IN**

Size = 400

Execution-Time: 0.484 ms

Size = 4000

Execution-Time: 5.066 ms

Size = 40000

Execution-Time: 30.397 ms

For Anti-Join Or Not-IN

Size = 400

Execution-Time: 0.614 ms

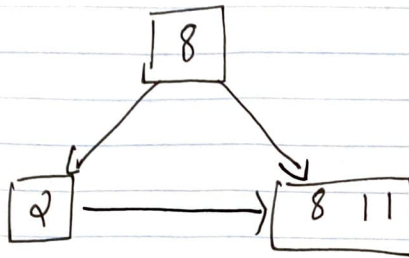
Size = 4000

Execution-Time: 9.029 ms

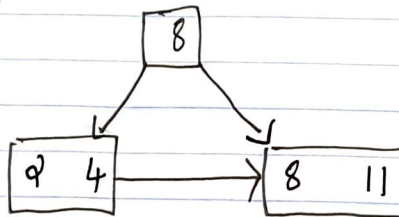
Size = 40000

Execution-Time: 30.805 ms

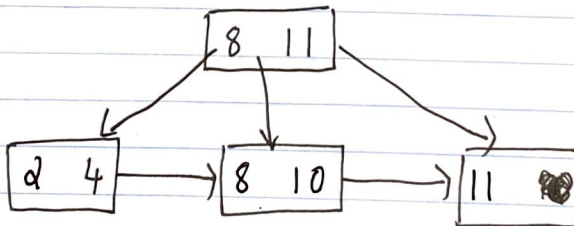
8]



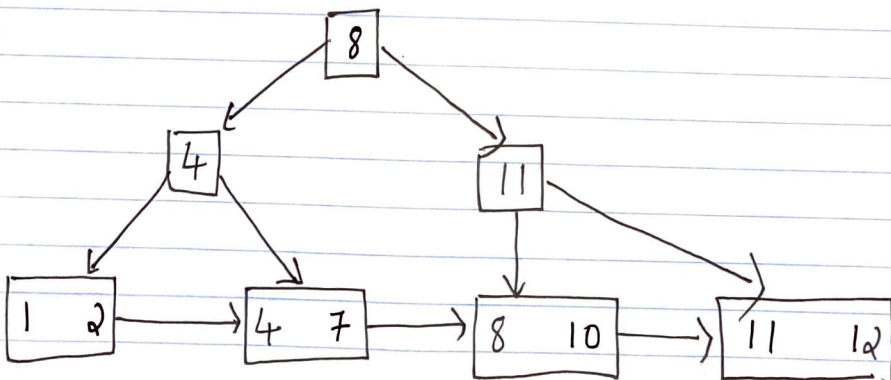
a) Inserting 4



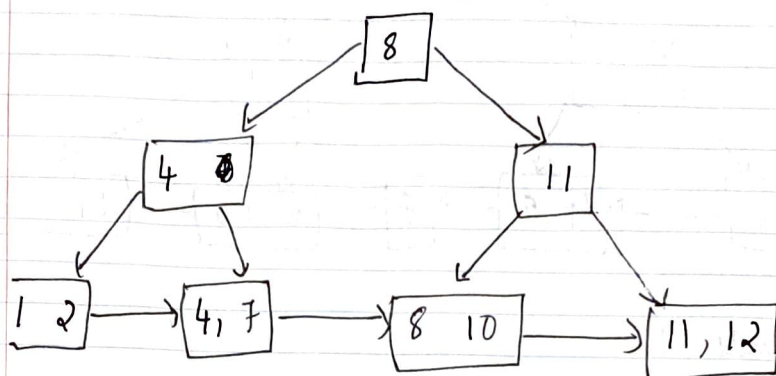
Insert 10



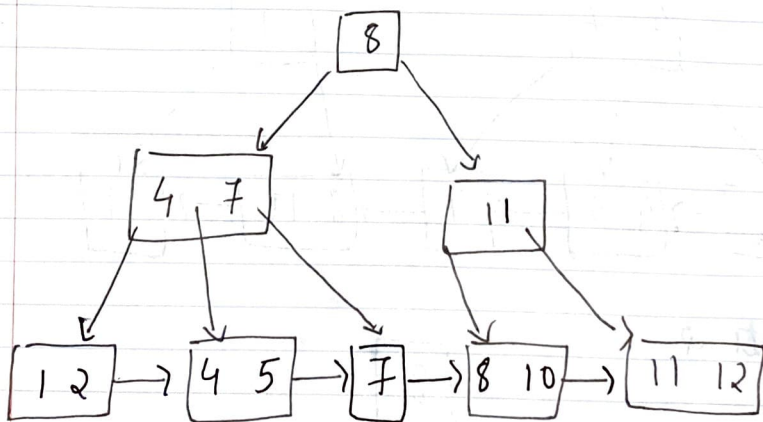
Insert 12 and 1



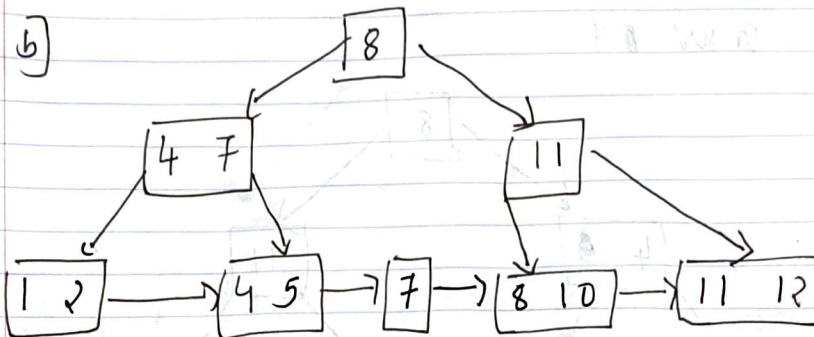
Insert 7



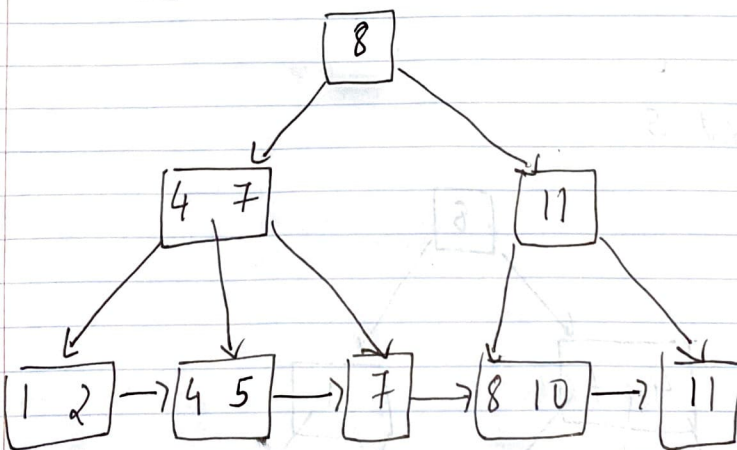
Insert 5



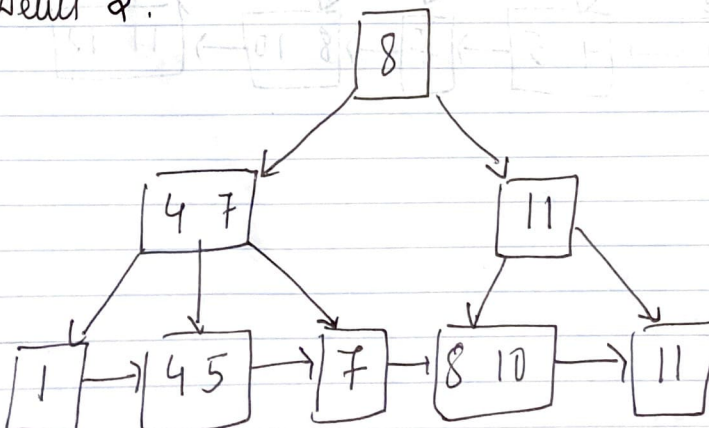
8) 6)



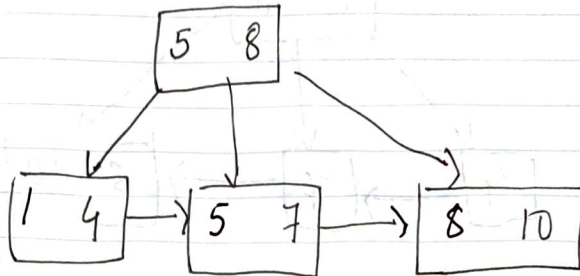
Delete 12



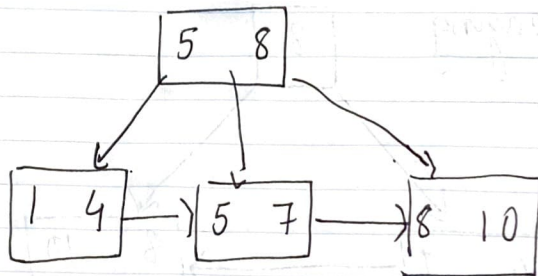
Delete 2:



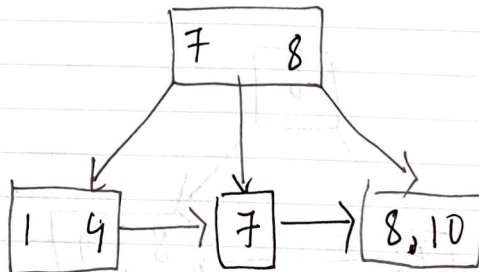
Delete 11



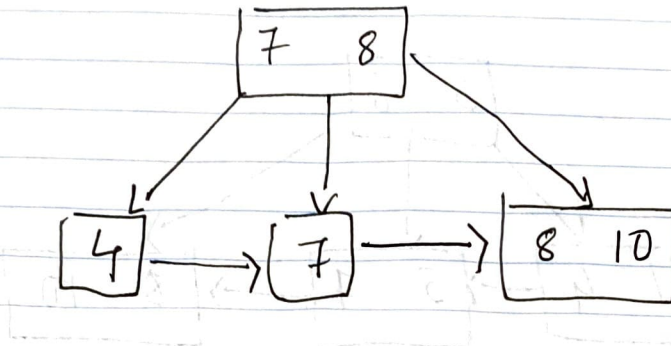
[8] C



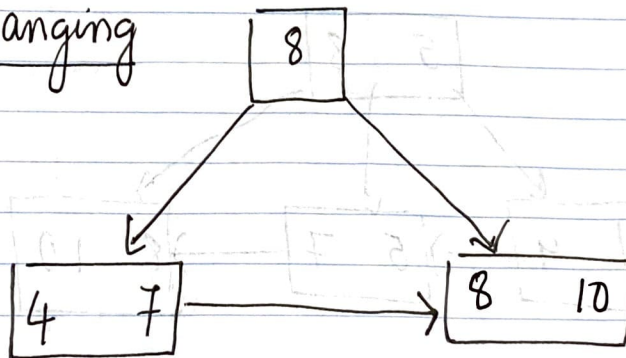
Delete 5



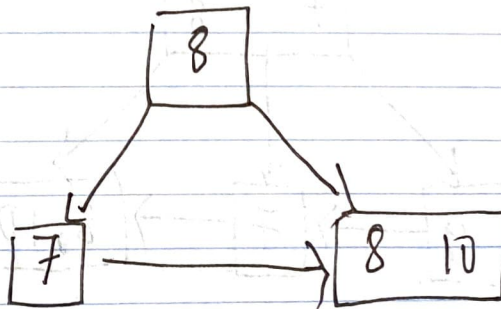
Delete 1



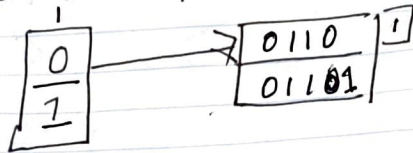
Rearranging



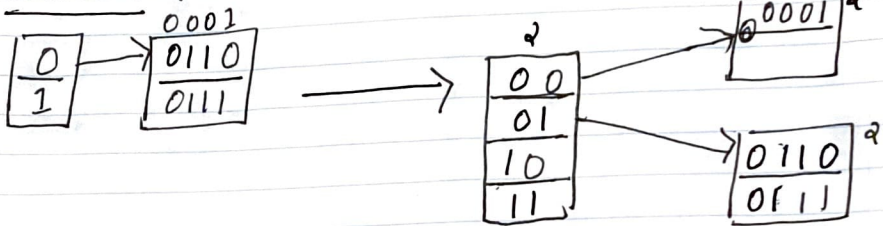
Delete 4



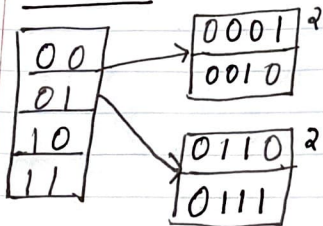
q) Insert 6 & 7



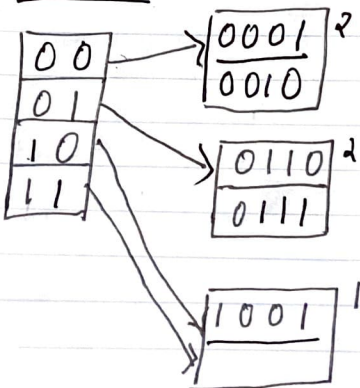
Insert 7 & 1

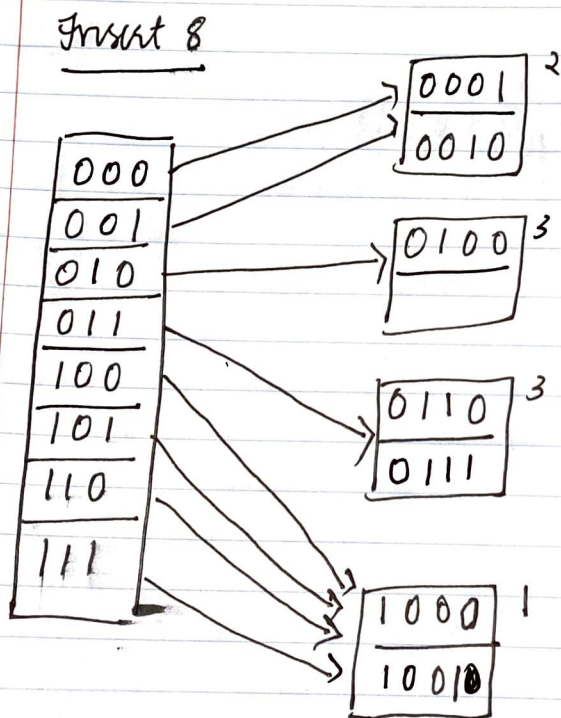
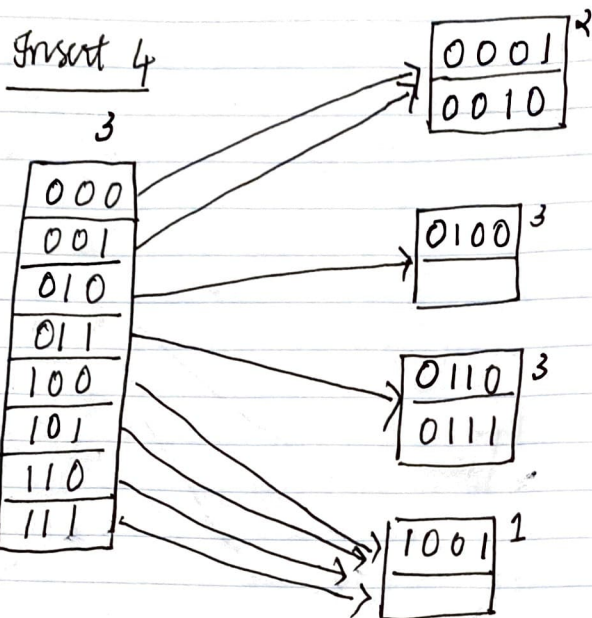


Insert 2

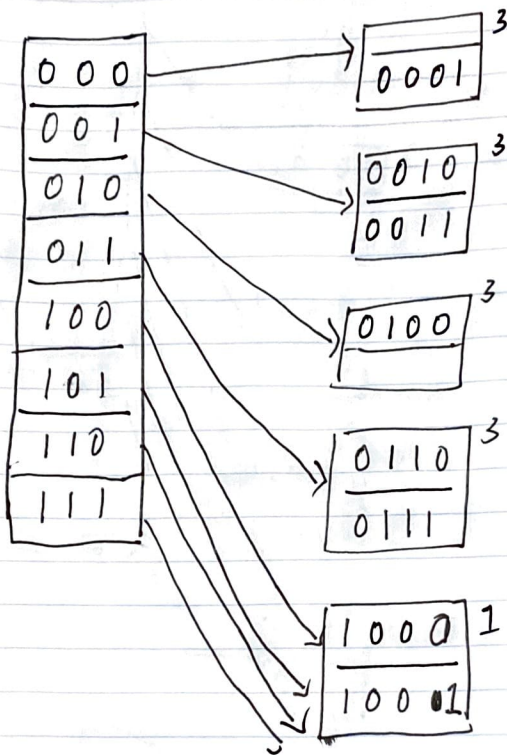


Insert 9

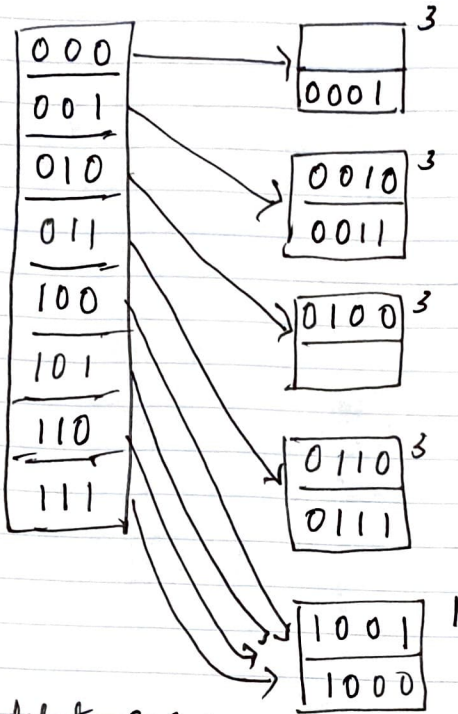




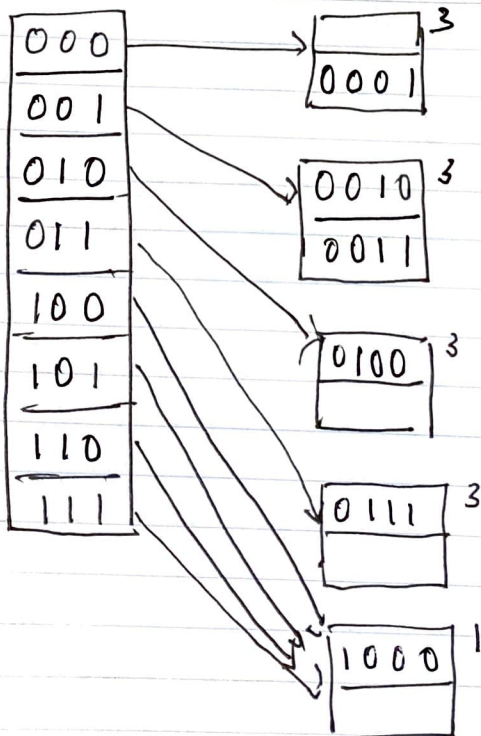
Insert 3



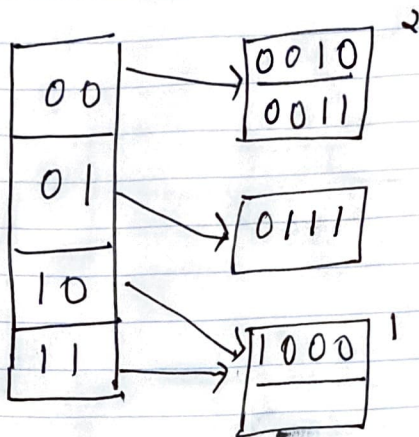
9) 5



delete 9 & 6



Delete 4 and 11



Delete 2 and 8

