

## Assignment 8 (noted graded)      Solutions

1. State which of the following schedules  $S_1$ ,  $S_2$ , and  $S_3$  over transactions  $T_1$ ,  $T_2$ , and  $T_3$  are conflict-serializable, and for each of the schedules that is serializable, given a serial schedule with which that schedule is conflict-equivalent.

(a)  $S_1 = R_1(x)R_2(y)R_1(z)R_2(x)R_1(y)$ .

**Solution:** This schedule consists of just read operations. Thus, there are no conflicting pairs and thus all  $T_1$  operations can be swapped with all  $T_2$  operations and as such the schedule  $S_1$  can be transformed to the serial schedule  $R_1(x)R_1(z)R_1(y)R_2(y)R_2(x)$ , i.e. the schedule  $T_1; T_2$ .

(b)  $S_2 = R_1(x)W_2(y)R_1(z)R_3(z)W_2(x)R_1(y)$ .

**Solution:** The precedence graph  $P(S_2) = \{(T_1, T_2), (T_2, T_1)\}$  which is cyclic. Thus,  $S_2$  is not serializable.

(c)  $S_3 = R_1(z)W_2(x)R_2(z)R_2(y)W_1(x)W_3(z)W_1(y)R_3(x)$ .

**Solution:** The precedence graph  $P(S_3) = \{(T_1, T_3), (T_2, T_1), (T_2, T_3)\}$  which is acyclic. Thus,  $S_3$  is serializable.

Using topological sort on this graph,  $S_3$  is equivalent with the serial schedule  $T_2; T_1; T_3$ .

2. Given 3 transactions  $T_1$ ,  $T_2$ ,  $T_3$  and a serializable schedule  $S$  on these transactions whose precedence graph (i.e. serialization graph) consists of the edges  $(T_1, T_2)$  and  $(T_1, T_3)$ . Give 2 serial schedules that are conflict-equivalent with  $S$ .

**Solution:** One of these serial schedules is  $T_1; T_2; T_3$ . Another is  $T_1; T_3; T_2$ .

3. Give 3 transactions  $T_1$ ,  $T_2$ ,  $T_3$  and a schedule  $S$  on these transactions whose precedence graph (i.e. serialization graph) consists of the edges  $(T_1, T_2)$ ,  $(T_2, T_3)$ , and  $(T_1, T_3)$ .

$$T_1 = R_1(x)R_1(z)$$

**Solution:**  $T_2 = W_2(x)W_2(y)$

$$T_3 = W_3(y)W_3(z)$$

$$S = R_1(x)R_1(z)W_2(x)W_2(y)W_3(y)W_3(z).$$

4. Give 3 transactions  $T_1$ ,  $T_2$ ,  $T_3$  and a schedule  $S$  on these transactions whose precedence graph (i.e. serialization graph) consists of the edges  $(T_1, T_2)$ ,  $(T_2, T_1)$ ,  $(T_1, T_3)$ ,  $(T_3, T_2)$ .

$$T_1 = R_1(u)R_1(x)R_1(z)$$

**Solution:**  $T_2 = W_2(u)W_2(x)W_2(w)$

$$T_3 = W_3(w)W_3(z)$$

$$S = W_2(u)R_1(u)R_1(x)R_1(z)W_2(x)W_3(w)W_3(z)W_2(w).$$

5. Give 3 transactions  $T_1$ ,  $T_2$ , and  $T_3$  that each involve read and write operations and a schedule  $S$  that is conflict-equivalent with **all** serial schedules over  $T_1$ ,  $T_2$ , and  $T_3$ .

**Solution:** We could pick the following transactions

$$T_1 = R_1(x)W_1(x)$$

$$T_2 = R_2(y)W_2(y)$$

$$T_3 = R_3(z)W_3(z)$$

In this example there are no conflicting pairs and therefore any schedule over  $T_1$ ,  $T_2$ , and  $T_3$  can be transformed into any serial schedule using appropriate swap operations of non-conflicting operations.

6. Consider the following transactions:

```
T1:  read(A);
      read(B);
      if A = 0 then B := B+1;
      write(B).
```

```
T2:  read(B);
      read(A);
      if B = 0 then A := A+1;
      write(A).
```

Let the consistency requirement be  $A = 0 \vee B = 0$ , and let  $A = B = 0$  be the initial values.

- (a) Show that each serial schedule involving transactions  $T_1$  and  $T_2$  preserves the consistency requirement of the database.

**Solution:**

For the serial schedule  $T_1; T_2$  the value for  $A = 0$  and that for  $B = 1$ .

For the serial schedule  $T_2; T_1$  the value for  $A = 1$  and that for  $B = 0$ .

- (b) Construct a schedule on  $T_1$  and  $T_2$  that produces a non-serializable schedule.

**Solution:**

T1	T2
R(A)	
	R(B)
	R(A)
	if B= 0 then A := A+1
	W(A)
R(B)	
if A = 0 then B := B+1	
W(B)	

The precedence graph consists of the edges  $(T_1, T_2)$  and  $(T_2, T_1)$ . This is a cyclic graph so this schedule is not serializable.

- (c) Is there a non-serial schedule on  $T_1$  and  $T_2$  that produces a serializable schedule. If so, give an example.

**Solution:**

The answer is no.

Assume that the schedule begins with  $R1(A)$ . Observe that this action conflicts with  $W2(A)$ .

Assume that we consider the partial schedule  $R1(A) R2(B)$ . Observe that  $R2(B)$  conflicts with  $W1(B)$ . So if we start the schedule with  $R1(A)R2(B)$  we get a cyclic precedence graph. Consequently, if we begin the schedule with  $R1(A)$  then the next action must be  $R1(B)$ . So we must have  $R1(A)R1(B)$ . We could now consider  $R2(B)$ . But this will again create a cycle in the precedence graph. Thus we are required to do " $R1(A)R1(B)$  if  $A = 0$  then  $B := B + 1$ ". Given this if we consider  $R2(B)$  we again have a problem since we will get a cyclic precedence graph. Thus we conclude that if we begin our schedule with  $R1(A)$ , then we must execute the serial schedule  $T_1; T_2$ .

Now assume that we begin the schedule with  $R2(B)$ . A similar analysis as above shows that if we want a serializable schedule, then we need to execute the serial schedule  $T_2; T_1$ .

- (d) i. Add lock and unlock instructions to  $T_1$  and  $T_2$ , so that they observe the two-phase locking protocol, but in such a way that interleaving between operations in  $T_1$  and  $T_2$  is still possible.

**Solution** By the previous argument, this can not be done.

- ii. Can the execution of these transactions result in a deadlock? If so, give an example.

**Solution.**

Yes this can happen. Notice the following initial segment of a possible schedule  $l_1(A)l_2(B)r_1(A)r_2(B)$  at this point (1)  $T_1$  wants to read  $B$  but  $T_2$  has a lock on  $B$  and (2)  $T_2$  wants to read  $A$  but  $T_1$  has a lock on  $A$ . So this schedule deadlocks.