

Arrays

Data Structures: A Programming Approach with C, PHI,
Dharmender Singh Kushwaha & A.K.Misra

Outline

- Introduction
- One dimensional array
- Basic Operations on Array
- Multi Dimensional Array
- 3-Dimensional Array
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Introduction

- An array is a collection of elements of the same type
- Each element of the array is always stored in consecutive memory location.
- Each element is accessed using a subscript or index.
- int arr[100]; declares an array of 100 integers
- Indices for above arrays are 0 to 99.

Introduction

- Array name is actually a pointer to the first location of the memory block allocated to the name of the array.
- Examples
 - int arr[5]={1,2,3,21,11}
 - array arr is initialized with 5 values.

Introduction

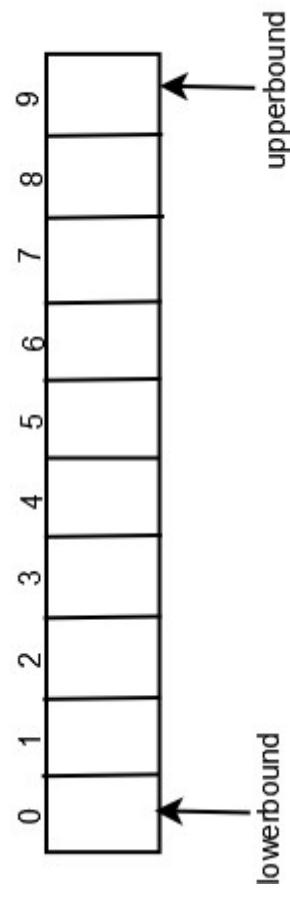
- Array name is actually a pointer to the first location of the memory block allocated to the name of the array.
- It can be initialized during declaration time only.
- Since there is no bound checking for array in C / C++, we have to check for upper bound of array

Example 1: Illustrating initialization of array

```
int[] marks; // marks is a reference name  
              // given to an array of integers  
  
marks = int[20]; // allocates OS storage for 20  
                  // integers  
  
int[] marks = int[20]; // combines the above into  
                      // one line  
  
marks[2] = 91; // gives the array element  
               // index 2 the value 91
```

One dimensional array

- A one dimensional array requires **only** one subscript specification.
- `int A[10];`



- The reference name given to the array is A and 'i' is the subscripted variable that is the index in the array.

One dimensional array

- 'i' can take values from 0 to 9.
- Size of the array is calculated as

$$\text{Size} = (\text{upperbound} - \text{lowerbound}) + 1$$

- Calculating memory requirement

$$\text{Size in byte} = \text{size of array} * \text{size of (element type)}$$

One dimensional array

```
float val[10];  
size = 10 * sizeof (float)  
      = 10 * 4  
      = 40 bytes
```

Sizeof operator gives the bytes required by that particular data type.

Implementation of 1- D Array in Memory

- Base address of the array is the address of first element of the array.
- Address of k^{th} element of the array $a[]$ is

$$a[k] = B + (S * k)$$

B=Base address of array.

S=Size of each element of array.

k=Index of the element.

Basic Operations on Array

► Some common operation types are:

- Traversal of array
- Inserting an element in the array
- Deleting an element from the array
- Merging two arrays

Traversal of Array

Traversal of an array is performed to:

- Read and access all elements one by one.
- To access the elements or
- To perform any other operation.

Pseudocode Traversal

- Let the array to be traversed be named as ‘arr’ containing ‘n’ elements such that:
 - element at position 0 is lowerbound ‘lb’ of the array and
 - the element at index position n be the upperbound ‘ub’ of the array.

Pseudocode Traversal

Initialize counter i

Set i at lb

Repeat

 for i=lb to ub

 visit element

 display arr[i]

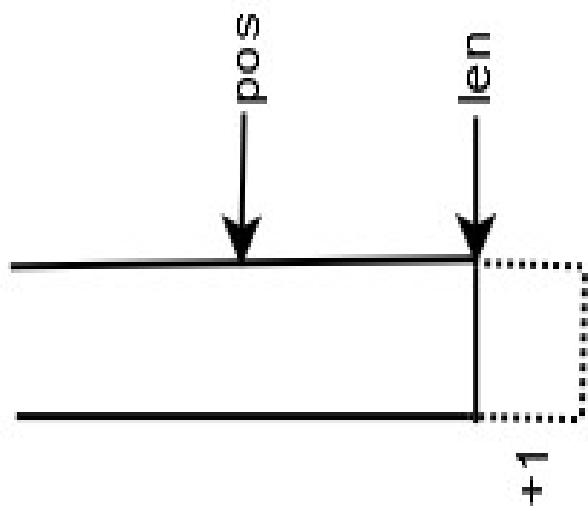
 end of loop

Exit

Inserting an element in 1-D Array

- Consider an array arr whose length is *len* and the elements in this array are stored from location 0 to *len*.
 - In order to insert an element ‘value’ in the array at some location LOC, we have to shift all the elements right from index pos till len by one.
 - The index of LOC is less than the index of len of the array.
 - This will vacate one memory location at pos so as to insert ‘value’. Let Insert be the function that does this job and the pseudo-code for this is given here.

Inserting an element in 1-D Array



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Pseudocode: Insert (arr, len, pos, value)

Initialize the value of i=length of the array arr.

Repeat

 for i = len down to pos

 set arr[i+1]=a[i] // shift the element down by 1 position
 end of loop

Insert element at required position

 set arr[pos]=value

 set len = len + 1 // Reset length of array

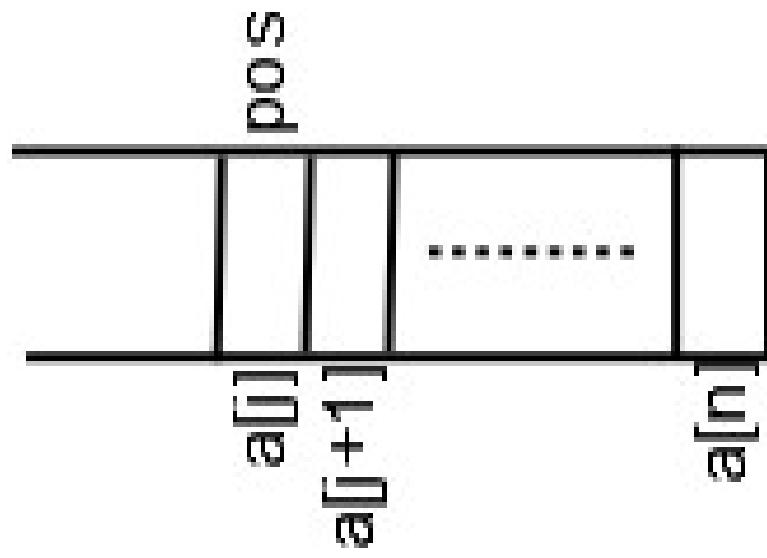
Display new list

End

Deleting an Element from 1-D Array

- Deletion of an element placed at the end of an array poses no problem.
- If last element is deleted, it simply reduces array length by one.
- Deleting an element placed in the middle of an array requires shifting all elements as to fill the space emptied by the just deleted element.

Deleting an Element from 1-D Array



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Pseudocode Delete (arr, pos, n)

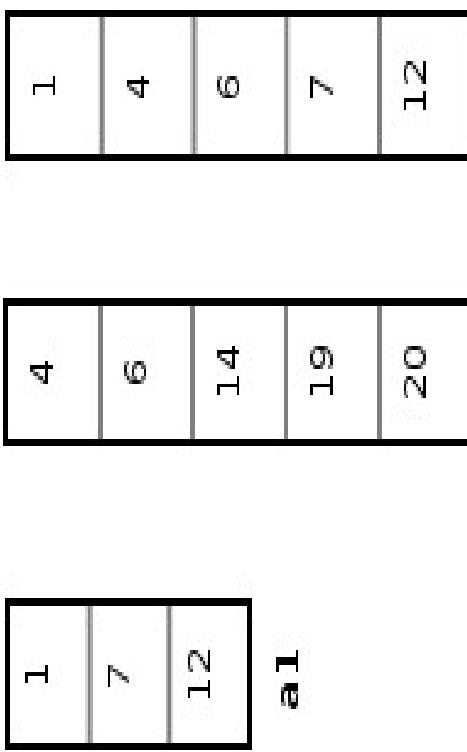
```
Set item =a [pos] //store the element to be deleted in  
a variable  
  
Repeat  
    for j = pos to n-1 //since there are n elements in the array  
        set a [j] = a [j+1] //shift elements one position leftwards /  
        upwards  
    end of loop  
    Reset number of elements in the array as n=n-1  
End
```

Merging two Arrays

- There are several applications where we have to merge the elements of two different arrays into one array.
- The elements in the two given arrays arr1 and arr2 may be in some sorted order.
- In the given pseudocode, the elements are arranged in ascending order and the resultant merged array arrmerge also has all its elements arranged in the ascending order.

Merging two Arrays

- The resultant merged array a3 also has all its elements arranged in the ascending order.



Merging two Arrays

- Create three array arr1[10], arr2[10] & arr3[20].
- Enter or arrange the element in ascending order in arr1 & arr2.
- Initialize the lower bounds lbar1, lbar2 & lbar3 to 0th position of the 3 arrays.

Check if

$$\text{arr1[lbar1]} \leq \text{arr2[lbar2]}$$

Merging two Arrays

```
If yes, assign elements of arr1 to arr3  
arr3 [lbarr3]= arr1[lbarr1]           // First element of  
                                         arr1 copied to arr3  
  
lbarr1++ //set lbarr1 = lbarr1 + 1  
lbarr3++ //set lbarr3 = lbarr3 + 1  
  
else  
    arr3[lbarr3] = arr2[lbarr2]        // assign  
                                         elements of arr2 to arr3
```

Merging two Arrays

```
lbarr2++ //set lbarr2 = lbarr2 + 1  
lbarr3++ //set lbarr3 = lbarr3 + 1  
end of loop
```

Repeat the above loop for remaining elements
of arr1, arr2 & arr3.
Display elements of arr3
End.

Character Array

```
#include <stdio.h>
main()
{
    static char chararr1[] = {'H','e','l','l','o'};
    static char chararr2[] = "Hello";
    printf("%s\n", name1);
    printf("%s\n", name2);
}
```

Sample Program Output

Helloxghifghjk (**some garbage value**)

Hello

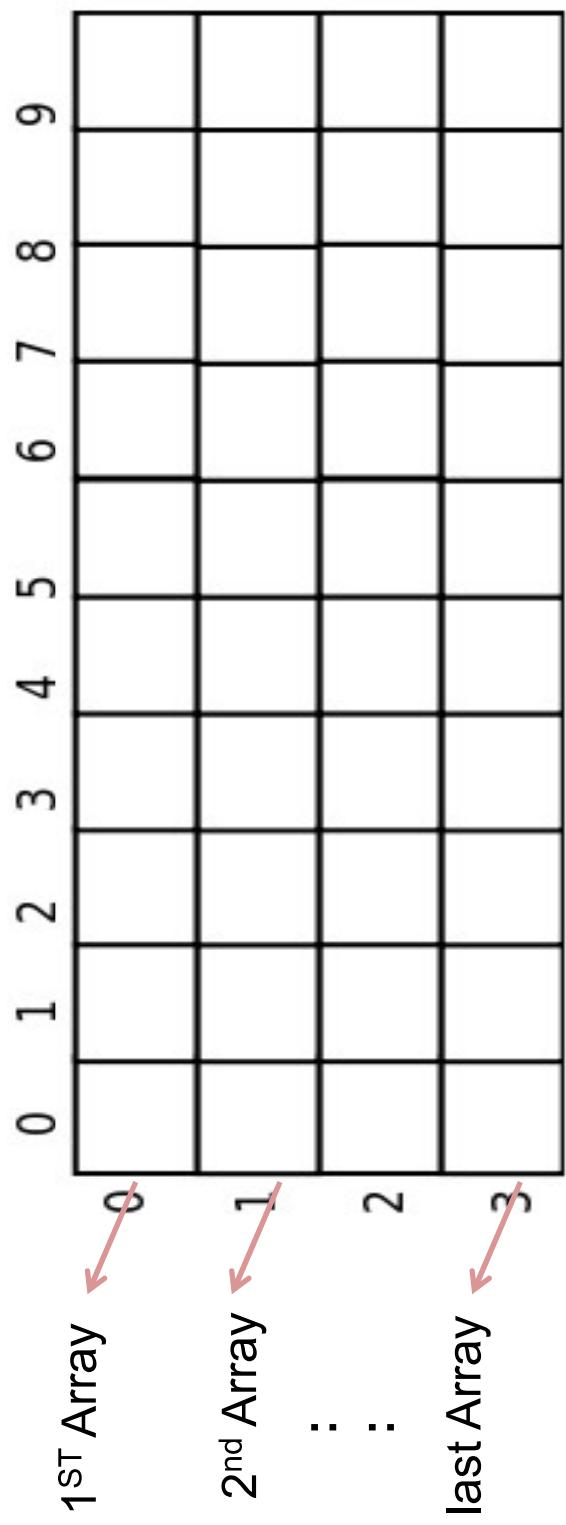
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Character Array

- The difference between the two arrays is that *chararr2 has a null placed at the end of the string, ie, in chararr2[5], while chararr1 doesn't.*
- *This often results in garbage characters being printed on the end.*
- To prevent this, we insert a null at the end of the *chararr1 array.*
- *The initialization now changes to:*
 - **static char chararr1[] = {"H",'e','l','l','o','\0'};**

Multi Dimensional Array

- If we place identical arrays adjacent to each other, what we have is a multidimensional array.



Multi Dimensional Array

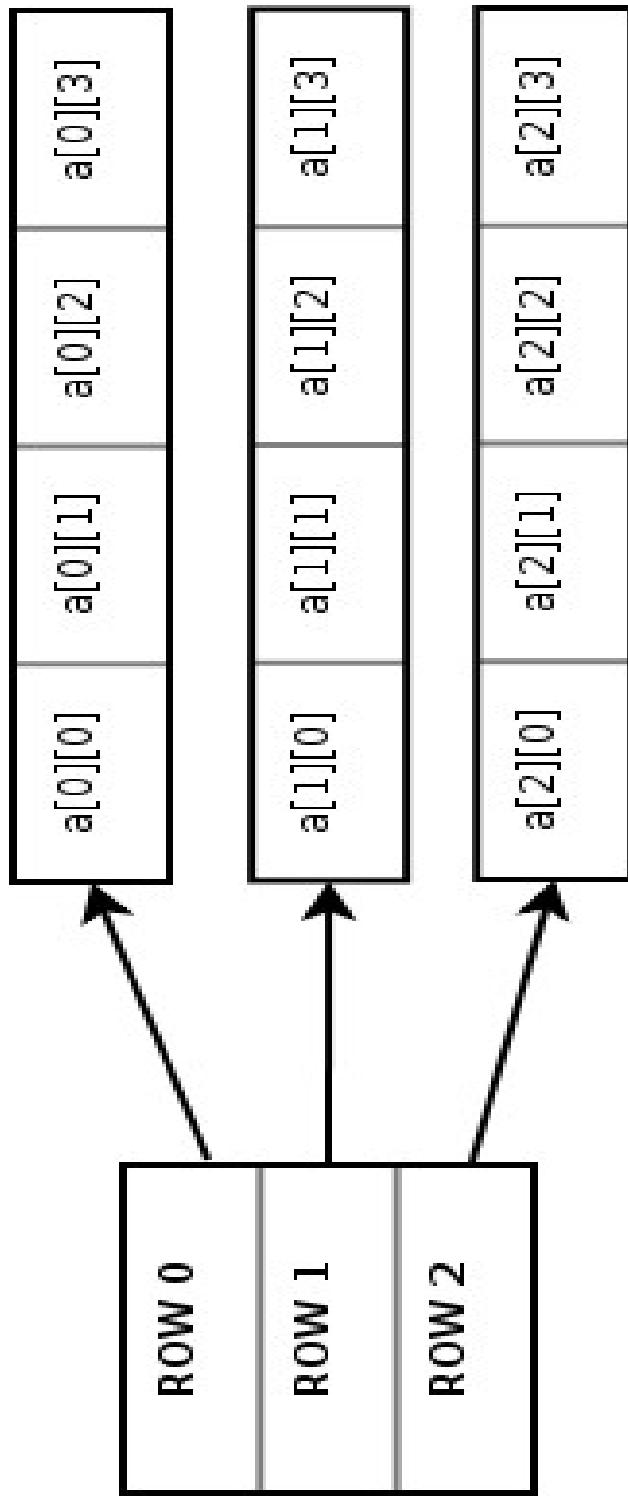
- All elements are homogeneous.
- A pair of indices specifies the desired element in a 2-dimensional array.

Example:

- `int a[3][4]`
- First index i.e. 3 represents the number of rows and second index i.e. 4 represents number of columns in array.

Multi Dimensional Array

- $A[0][0]$ is the first and $a[2][3]$ is the last element of the array.
- An element $a[i][j]$ refers to an element that is in i^{th} row and j^{th} column.



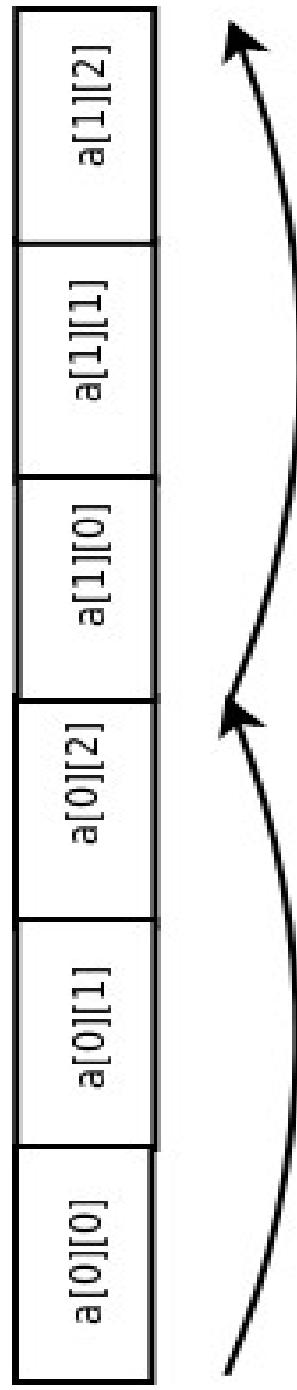
Multi Dimensional Array

- In memory, elements of a 2-dimensional array are stored in contiguous memory locations.
- 2 dimensional array can be initialized by specifying the position and value as follows:
 - $A[1][3]=32$ inserts 32 in 1st row and 3rd column.

Implementation of 2-D Array

Row major implementation

- Elements of an array are stored and accessed row wise.
- All the elements of row 1 are stored first and then the elements of row 2 and so on.



ROW 1

ROW 2

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Implementation of 2-D Array

Address of element $a[i][j] = [\text{base address}] + [\text{number of byte required by each element} * (\text{number of column } (i - \text{lbc of row}) + (j - \text{lbc of column}))]$

or

Add of $a[i][j]=B + nb [n * (i - lbr) + (j - lbc)]$ where:

B = base address of the array

nb = number of bytes occupied by each element of the array

i, j = index of element at $a[i,j]$ whose address is being computed

lbr = lower bound of row

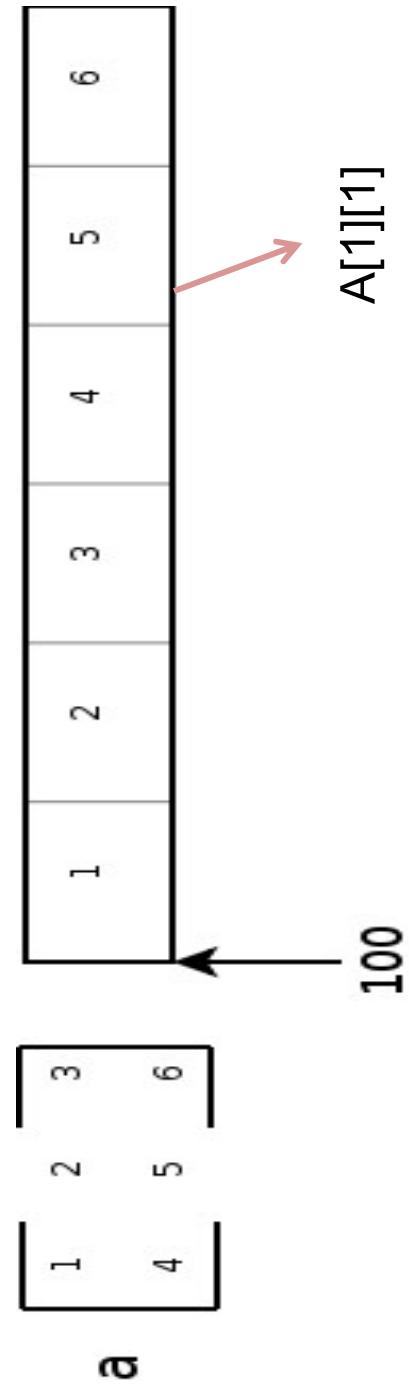
lbc = lower bound of column

m = number of rows in the array

n = number of columns in the array

Implementation of 2-D Array

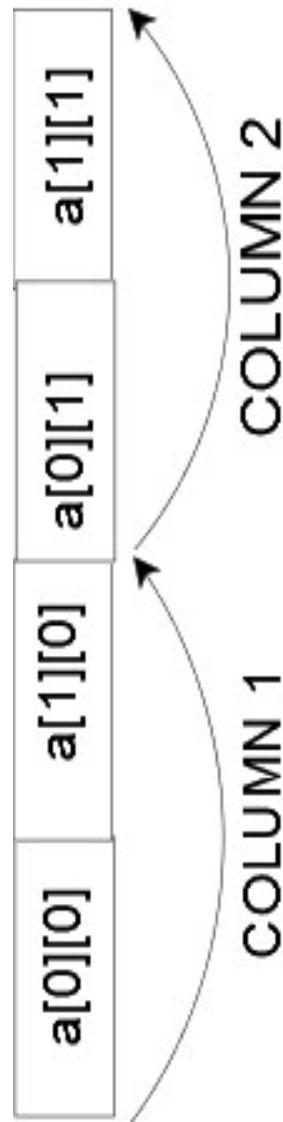
- Calculate address for $a[1][1]$.
- Here $B=100$, $nb=1$ byte, $i=1, j=1$,
- $lbr = 0, lbc = 0, n = 3$
- Add $a[1][1]=100 + 1 [3 (1 - 0) + (1 - 0)] = 104$



Implementation of 2-D Array

Column major implementation

- Elements of an array are stored and accessed column wise.
- All the elements of column 1 are stored first and then the elements of column 2 and so on.



Implementation of 2-D Array

Address of element $a[i][j] = [\text{base address}] + [\text{number of byte required by each element} * (\text{number of rows } (j - \text{lbc of col}) + (i - \text{lbc of row}))]$

or

add of $a[i][j] = B + nb [m * (j - lbc) + (i - lbr)]$ where:

B = base address of the array

nb = number of bytes occupied by each element of the array

i,j = index of element at $a[i,j]$ whose address is being computed

lbr = lower bound of row

lbc = lower bound of column

m = number of rows in the array

Example

- Given a 2-D array $\text{arr}[-10..20, 10..35]$ where each elements requires 1 bytes of storage and the array is column major implementation. Calculate the address of element stored at $\text{arr}[0, 30]$.
- The base address of the given array is 1010.

Example

- $B = 1010$
- $nb = 1$
- $i = 0$
- $j = 30$
- $lbr = -10$
- $lbc = 10$
- $m = 31$

Example

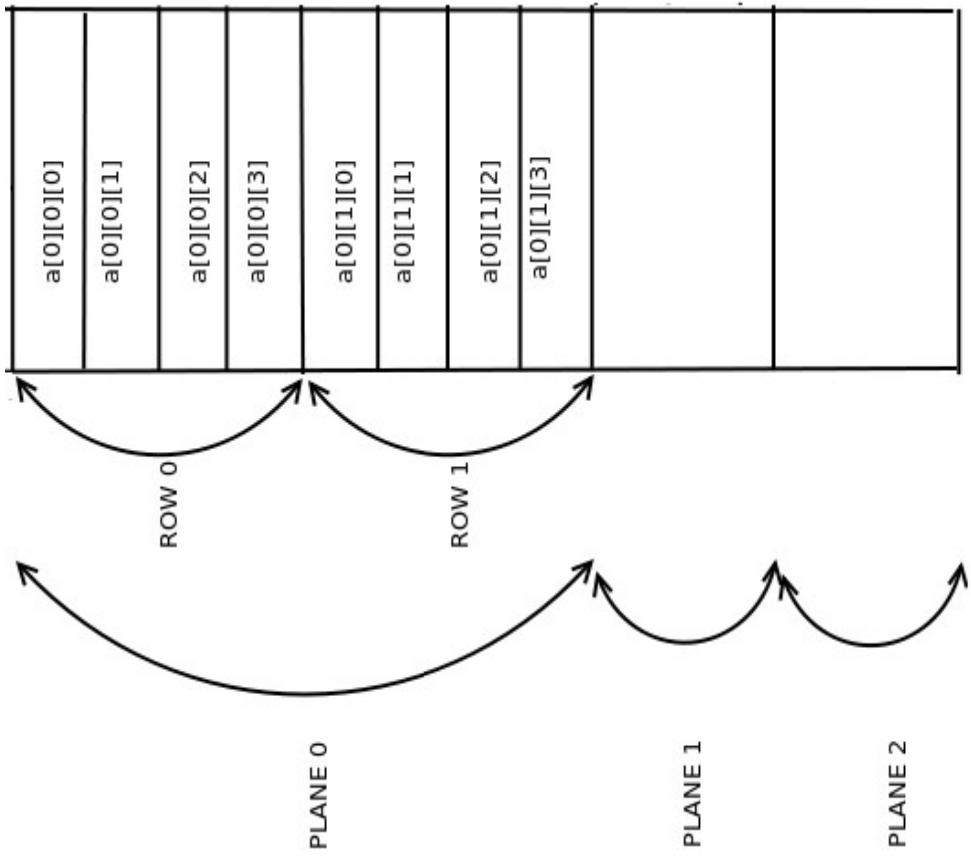
$$\begin{aligned}\text{Add of } a[0][30] &= 1010 + 1[31 * (30 - 10) + (0 - (-10))] \\&= 1010 + [31 * (20) + 10] \\&= 1010 + [620 + 20] \\&= 1010 + 640 \\&= 1650\end{aligned}$$

3-Dimensional Array

- A 3-dimensional array is modeled as a collection of identical 2-dimensional arrays placed one behind the other or one above.
- Three subscript are needed to access a particular element.
- First subscript specifies the plane, second subscript the row and the third subscript the column.

3-Dimensional Array

Representing a
3-dimensional array



Matrix Multiplication

- Given two matrices $A(m*n)$ and $B(x*y)$.
- Condition for multiplication is that $n==x$.
- If $n \neq x$, matrix multiplication is not possible.

Matrix Multiplication

$$\begin{array}{c} \text{MATRIX A} \\ \begin{array}{|c|c|c|} \hline & A & B & C \\ \hline D & & E & F \\ \hline G & H & I & \\ \hline \end{array} \end{array} \times \begin{array}{c} \text{MATRIX B} \\ \begin{array}{|c|c|c|} \hline & a & b & c \\ \hline d & & e & f \\ \hline g & h & i & \\ \hline \end{array} \end{array} = \begin{array}{c} \text{RESULTANT MATRIX} \\ \begin{array}{|c|c|c|} \hline & 1 & 2 & 3 \\ \hline 4 & & 5 & 6 \\ \hline 7 & 8 & 9 & \\ \hline \end{array} \end{array}$$

```
1=A.a+B.d+C.g  
2=A.b+B.e+C.h  
3=A.c+B.f+C.i  
4=D.a+E.d+F.g  
5=D.b+E.e+F.h  
6=D.c+E.f+F.i  
7=G.a+H.d+I.g  
8=G.b+H.e+I.h  
9=G.c+H.f+I.i
```

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Matrix Addition

MATRIX A

| | | |
|---|---|---|
| A | B | C |
| D | E | F |
| G | H | I |

MATRIX B

| | | |
|---|---|---|
| a | b | c |
| d | e | f |
| g | h | i |

RESULTANT MATRIX

+

| | | |
|---|---|---|
| 1 | 2 | 3 |
| 4 | 5 | 6 |
| 7 | 8 | 9 |

=

$$\begin{aligned}1 &= A + a \\2 &= B + b \\3 &= C + c\end{aligned}$$

$$\begin{aligned}4 &= D + d \\5 &= E + e \\6 &= F + f\end{aligned}$$

$$\begin{aligned}7 &= G + g \\8 &= H + h \\9 &= I + i\end{aligned}$$

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Matrix Transpose

| | | | |
|---|---|---|---|
| a | b | c | d |
| e | f | g | h |
| i | j | k | l |
| m | n | o | p |



| | | | |
|---|---|---|---|
| a | e | i | m |
| b | f | j | n |
| c | g | k | o |
| d | h | l | p |

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Pointer & 1-D Array

```
int array [s], *ip;           //pointer to int
ip= & array[3]                 //pointer points element of array

main()
{
    int n,*p;                // defines two variables
    p=&n;                     // pointer p has address of or points to variable n
    *p=0;                     // set n=0
    *p + =1;                  // increment what p point to
    (*p)+ +;                  // ----,----
}
```

Array of Pointers

- Suppose we have a declaration:
 - int *a[10] // array of pointers which are 10 in number.
- Let there be other array marks declared as:
 - int marks[10]={1,2,3,4,5,6,7,8,9,0};
- These 10 elements of the array marks will be stored in certain addresses.
- Now these add. can be stored in array of ptrs.
- Address of element 1 is the first element of int *a[] i.e. the first element of int marks[10] and so on. This is **array of pointer**.

Pointer to an Array

- Consider the declaration:
 - `int(*a)[10]` // here ‘a’ is a pointer to an array containing 10 integers.
- Now if we had the following lines of code:
 - `int marks[10];`
 - `a=&marks[10];`
- Here, we deference pointer a with '*' operator and we first get element of int `marks[10]` array that is `marks[0]` and so on.
- **This is pointer to array.**

Array within Structures: Complex Structure

- Structure can contains arrays or other structures so it is sometimes called complex structure.

struct address

```
{  
    int house_no;  
    char street_name [40];  
    char city_name [30];  
    int pin_code;  
};
```

Array of Structure

- Once we need to store the complex structures, the natural choice is array of structures.

Struct student

```
{     char name[12];  
     int rollno;  
     int percent_marks;  
};  
student studresult[60];
```

Summary

- Array is a data structure consisting of a collection of elements, each identified by at least one index.
- A one-dimensional is a type of linear array.
- Accessing its elements involves a single subscript which can either represent a row or column index.

Summary

- Static arrays have a size that is fixed at allocation time and consequently do not allow elements to be inserted or removed.
- Array stores values in contiguous memory location.
- Arrays take linear ($O(n)$) space in the number of elements n that they hold.