

# Assignment 1

## Task 1

Base Joint=(0,0)

### Elbow Joint

$$x_1 = l_1 \cos q_1 = \cos q_1$$

$$y_1 = l_1 \sin q_1 = \sin q_1$$

### End-Effector Joint

$$x_2 = x_1 + l_2 \cos(q_1 + q_2) = \cos q_1 + \cos(q_1 + q_2)$$

$$y_2 = y_1 + l_2 \sin(q_1 + q_2) = \sin q_1 + \sin(q_1 + q_2)$$

## Task2

```
import numpy as np
```

```
import matplotlib.pyplot as plt
```

```
l1 = l2 = 1
```

```
def forward_kinematics(q1, q2):
```

```
    x1 = l1 * np.cos(q1)
```

```
    y1 = l1 * np.sin(q1)
```

```
    x2 = x1 + l2 * np.cos(q1 + q2)
```

```
    y2 = y1 + l2 * np.sin(q1 + q2)
```

```
    return (0, 0), (x1, y1), (x2, y2)
```

```
configs = {  
    "Straight Arm": (0, 0),  
    "Bent Elbow": (np.pi/4, np.pi/4),  
    "Folded Arm": (np.pi/6, -2*np.pi/6)  
}
```

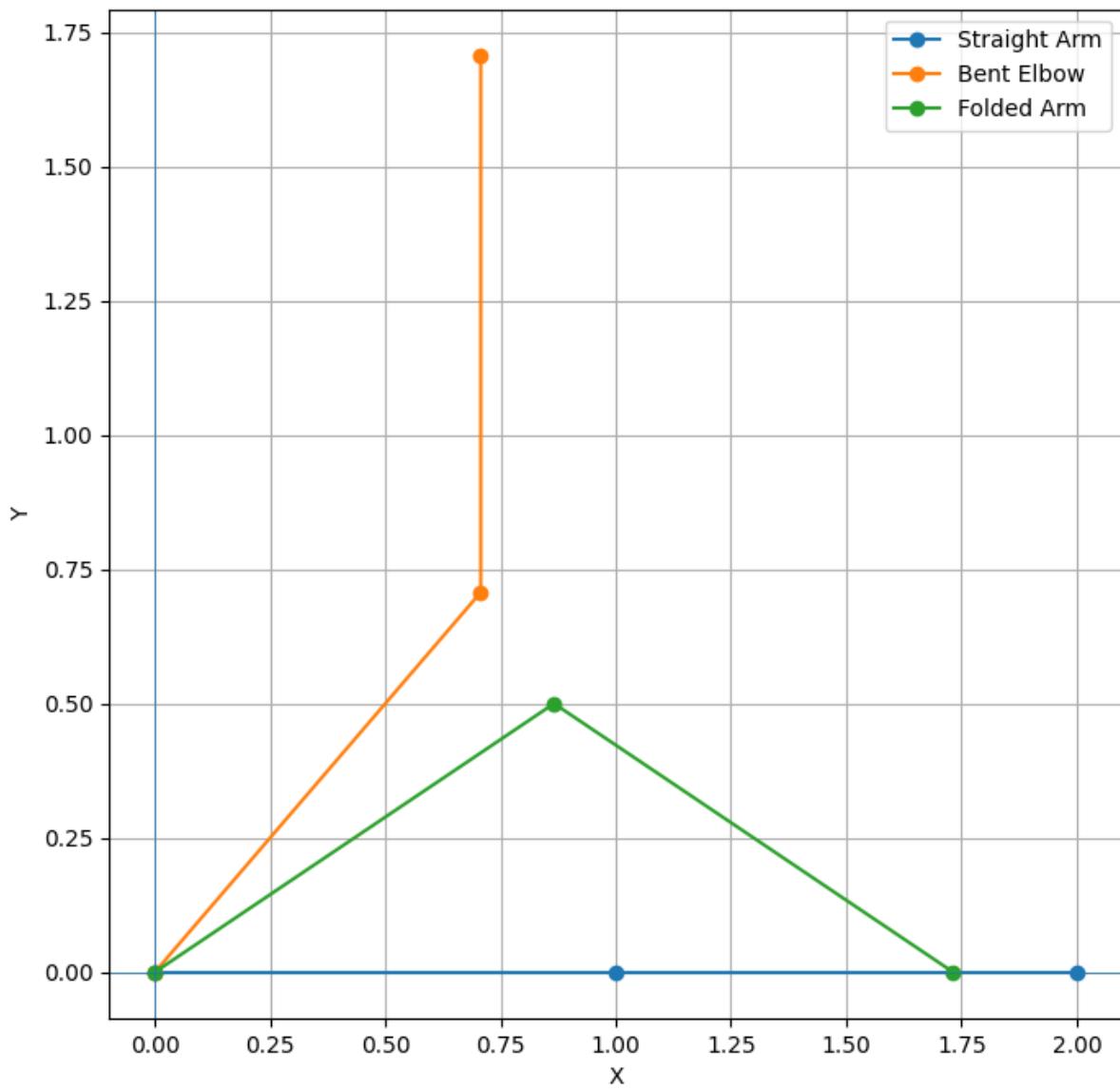
```
plt.figure(figsize=(8, 8))
```

```
for name, (q1, q2) in configs.items():  
    base, elbow, end_eff = forward_kinematics(q1, q2)
```

```
    x = [base[0], elbow[0], end_eff[0]]  
    y = [base[1], elbow[1], end_eff[1]]
```

```
    plt.plot(x, y, '-o', label=name)
```

```
plt.axhline(0, linewidth=0.5)  
plt.axvline(0, linewidth=0.5)  
plt.grid(True)  
plt.legend()  
plt.xlabel("X")  
plt.ylabel("Y")  
plt.show()
```



### Role of q1

Rotates the entire arm about the base.

Changes the orientation of the workspace

### Role of q2

Controls the relative bend at the elbow

Determines whether the arm is fully extended, bent or folded back.

Maximum reach =  $|l_1 + l_2| = 2$

Minimum reach =  $|l_1 - l_2| = 0$

Workspace is circle of radius 2 with origin as center.

