

# Sparse Logit Sampling: Accelerating Knowledge Distillation in LLMs

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Paper  
& code!

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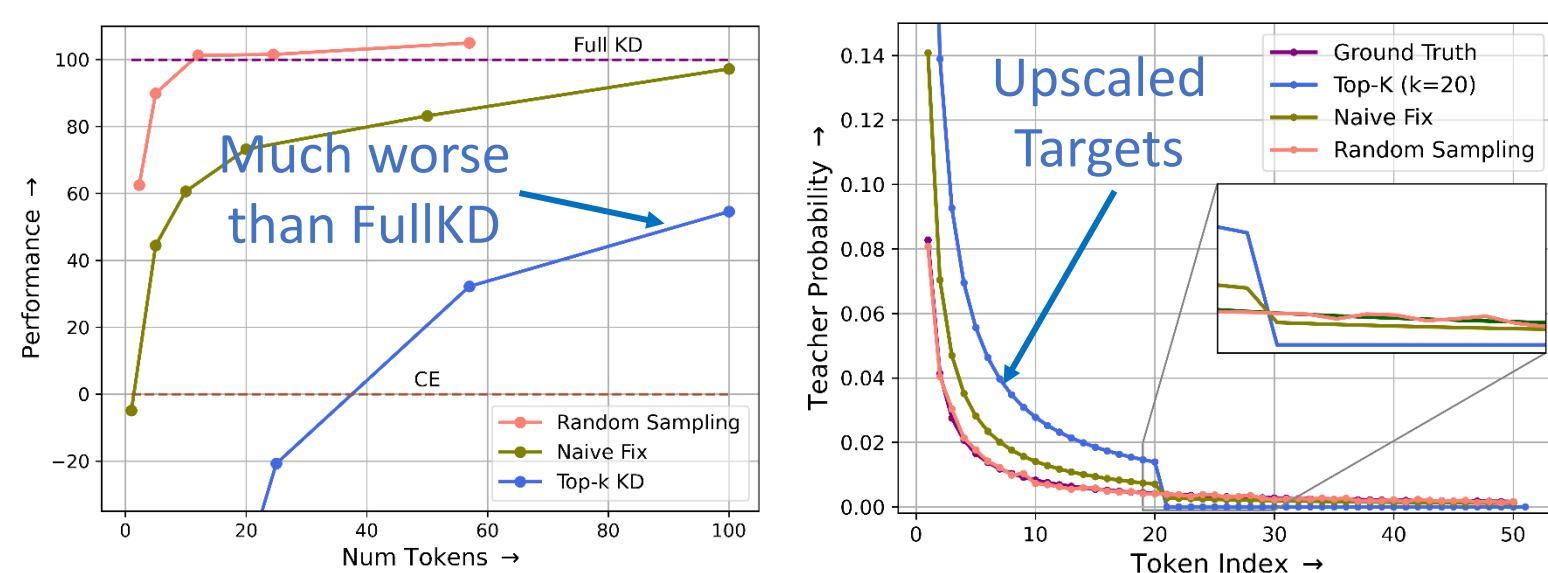
Samsung Research

## 1. Contributions

1. Run teacher once for KD for pre-training/SFT, pre-compute/store **teacher soft-labels**
2. Unlike top-K methods, provides **unbiased estimate** of teacher probs
3. Preserves KL Divergence **gradients** in expectation and empirically

## 3. Vanilla Top-K Distillation

1. Store only Top- $K$  largest probs, eg. Top-100
2. Using KLD loss,  $L = \sum_{i=1}^{|V|} t_i \log \frac{t_i}{p_i}$ ,  
student learns **upscaled targets** -  $p_i = \frac{t_i}{\sum t_i}$
3. Missing any supervision in the tail
4. **Worse than no KD for Top-25!**  
60% of performance of Full-KD at Top-100



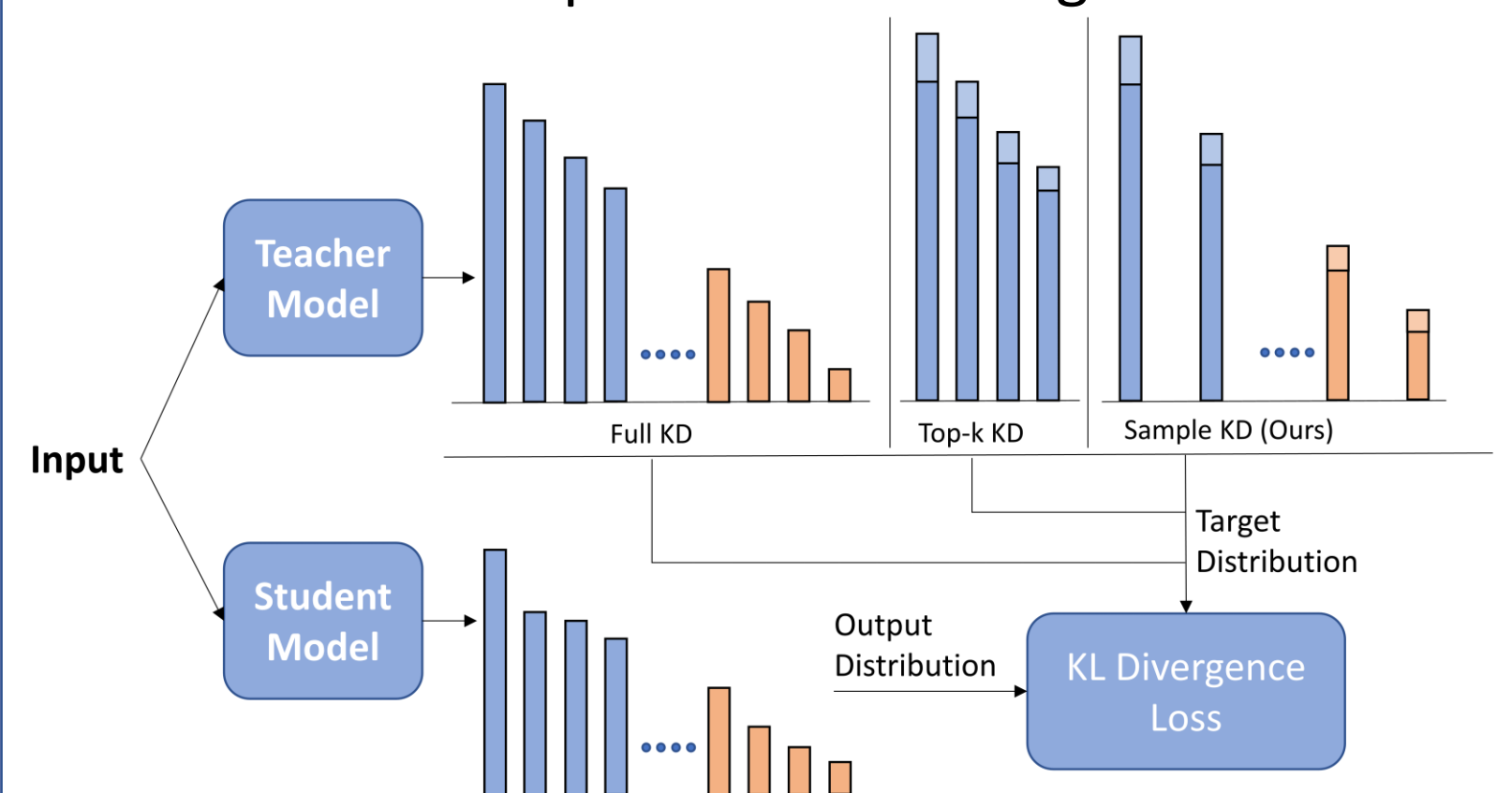
## 2. Advantages

1. Store only **12 soft-labels/token**, < 10% compute overhead
2. Comparable performance to using Full KD
3. The student is **well-calibrated**, improves 0-shot, IF scores, speculative decoding
4. 300M to 3B student, for 10B to 1T train tokens

## 4. Proposed: Random Sampling KD

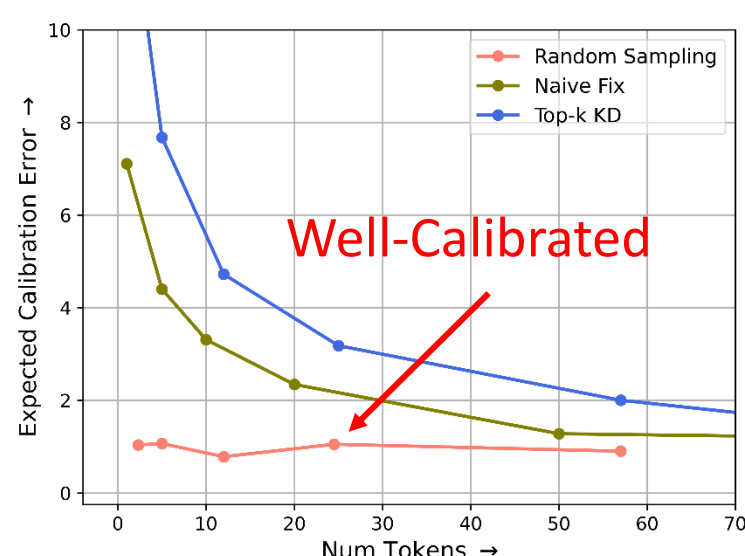
**Don't truncate to top- $K$ , sample instead!**

1. **Sample tokens** (with replacement) from teacher probability dist. for  $N$  rounds
2. For each token  $i$ , save **sampled freqs**  $\frac{\text{count}_i}{N}$
3. Use saved freqs as soft label targets for KLD.



## 5. Random Sampling KD Analysis

1. Saved labels very sparse – 12 for  $N = 50$
2. Only  $\approx 36\text{GB}$  of storage for 1B training tokens.
3. 2 – 3x compute savings of teacher
4. **Well-calibrated** student!
5. Mini-batch **gradient perfectly matches** FullKD



Method	$\Delta$ Angle $\downarrow$	Norm Ratio
Top-K 12	58°	2.4
Top-K 50	48°	1.8
Top-K 300	30°	1.3
Ours12	4°	1.0

No Grad Error

## 6. Results

Unique Tokens	LM Loss $\downarrow$	ECE % $\downarrow$	Speculative Accept % $\uparrow$	0-shot Score $\uparrow$
CE	2.81	0.4	59.95	40.4
2.4	2.77	1.0	61.47	42.1
5.0	2.75	1.1	61.83	42.6
12.1	2.75	0.8	61.85	43.0
24.5	2.75	1.1	61.93	43.1
57.0	2.74	0.9	61.97	42.9
FullKD	2.75	0.7	62.02	42.1

$\approx 12$  labels  
sufficient  
3B  $\rightarrow$  300M

Method	LM Loss $\downarrow$	ECE % $\downarrow$	Speculative Accept % $\uparrow$	0-shot Score $\uparrow$	IF SFT Score $\uparrow$
CE	2.37	0.3	71.1	55.6	54.5
Top-K 12	2.50	4.7	73.0	56.6	57.7
Top-K 50	2.40	1.8	73.1	57.1	58.3
Ours (12)	2.35	0.2	73.2	57.5	59.4
FullKD	2.34	0.2	73.4	57.5	58.4

8B  $\rightarrow$  3B

## 7. Future Work

1. Larger Scale, Continual Pre-training, SFT/IF
2. Better sampling (without replacement?)  
Optimal sampling depends on student perf..
3. Cross-tokenizer Offline KD – Vocab mismatch?
4. Offline KD of Hidden States – Invert LM Head and Softmax?

<https://github.com/akhilmedia/RandomSamplingKD>

Dataset	CE	Top-K 12	Top-K 50	Ours 12	FullKD
Dolly	64.2	59.0	65.4	71.3	66.1
SelfInst	64.6	60.9	63.4	73.1	66.1
Vicuna	49.1	48.9	53.1	58.2	56.9
S-NI	62.4	63.4	62.6	63.8	60.7
UnNI	60.4	58.0	58.3	61.4	61.0
Avg	60.2	58.0	60.6	65.6	62.2

**Better than FullKD for NLG**

Sampling noise  
=Regularization?