

Homework - 2

① 1. for example,

$$3^2 \equiv 1 \pmod{8}$$

$$5^2 \equiv 1 \pmod{8}$$

proof:- for all odd squares $\rightarrow (2n+1)^2$
 $n \in \text{whole numbers}$

$$(2n+1)^2 = 8m+1$$

$$4n^2 + 4n + 1 = 8m + 1$$

$$n^2 + n = 2m$$

$$n(n+1) = 2m$$

\rightarrow If n is odd, $n+1$ is even

It is a factor of 2

\rightarrow If n is even, automatically we have a factor of 2

2. For example,

$$2^2 \equiv \pmod{8} \rightarrow 4$$

$$4^2 \equiv \pmod{8} \rightarrow 0$$

$$6^2 \equiv \pmod{8} \rightarrow 4$$

$$8^2 \equiv \pmod{8} \rightarrow 0$$

proof:- $(2n)^2 \rightarrow$ for all even squares

$$(2n)^2 = 8m + 1$$

$$4n^2 = 8m + 1$$

→ n belongs to whole numbers

→ When $n = 0$

$$0 = 8m + 1 \quad \text{Not possible,}$$

③ * $O(1)$:- constant time complexity.

→ This operation ↓ depend on size of input data. does not

→ small input data (or) Large input data
↓
It takes same time to execute.

* $O(n)$: Linear time complexity

→ The operation grows linearly with the size of the input data.

→ If the input data size increases, operation takes more time.

* $O(\log n)$: Logarithmic time complexity

→ The operation grows logarithmically with the size of input data.

→ If the input size increases, the time to complete increases at a decreasing rate.