compare_v2

April 16, 2023

```
[]: import numpy as np
     from numba import jit
     from numpy.random import default_rng as rg
     rng = rg(12345)
     from tqdm import tqdm
     import sys
     sys.path.append('../core')
     %matplotlib inline
[]: import torch
     torch.manual seed(0)
     import torch.optim as optim
[]: from FLDojo import dojo
     from FL import FL
     from DNN_R import DNN
     from display2 import*
[]: Xs = np.linspace(-1,1,40000)
     Ys0 = Xs**2 - 0.7*Xs
     # derivative is 2x - 0.7, which has a absval max of 2.7 (which is the Lipshitz \Box
      ⇔constant)
     Ys1 = np.sin(Xs*8*np.pi)
     # note derivative is 8 pi \cos(8 \text{ pi x}), which has a max of 8 pi (which is the
      →Lipshitz constant)
     Ys2 = np.sin(Xs*4*np.pi) + np.exp(-4*Xs)
     print(np.max(np.abs(4*np.pi*np.cos(4*np.pi*Xs) - 4*np.exp(-4*Xs))))
     # derivative has a max of ~205 (which is the Lipshitz constant)
     from matplotlib import pyplot as plt
     fig,axs = plt.subplots(1,3,figsize=(15,5))
     axs[0].plot(Xs,Ys0)
     axs[1].plot(Xs,Ys1)
     axs[2].plot(Xs,Ys2)
     # We will use the same network for all three functions
     ks = [2.7,8*np.pi,205]
     dnn_sizes = [1,102,101,1] # so # of weights is 102*1 + 102*102 + 102*1 = 10608
```

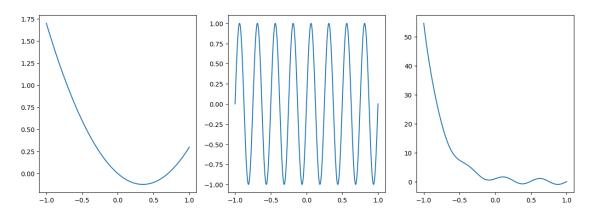
```
fl_sizes = [1,100,100] # so # of weights is 1*a + a*1 + a*a + a*1 = 10300, forusa = 100

fl_sizes2 = [1,25,25] # so # of weights is 1*a + a*1 + a*a + a*1 = 700, for aux = 25

dnn_sizes2 = [1,26,26,1] # so # of weights is 26*1 + 26*26 + 26*1 = 728

# a three layer nn can represent any multivariate function (continuous orusalisation) https://arxiv.org/abs/2012.03016
```

205.826229518



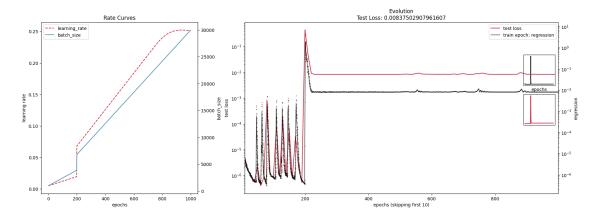
```
device = torch.device("cuda:0" if torch.cuda.is_available() else "cpu")
p = np.random.permutation(len(Xs))
Xs = Xs[p]
X = torch.from_numpy(Xs).float().unsqueeze(1).to(device)
split = 0.75
train_X = X[:int(split*len(X))]
test_X = X[int(split*len(X)):]

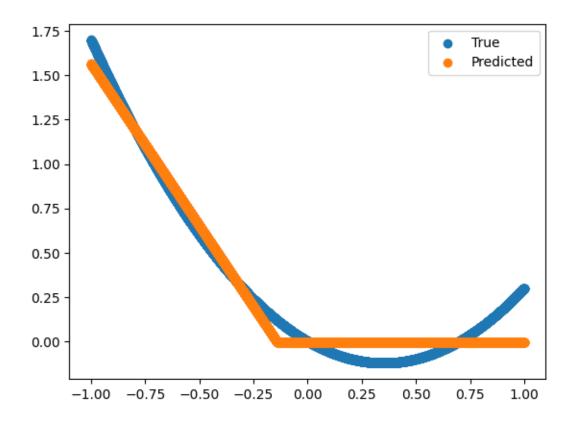
def update_y(Ys):
    y = torch.from_numpy(Ys[p]).float().unsqueeze(1).to(device)
    train_y = y[:int(split*len(y))]
    test_y = y[int(split*len(y)):]
    return train_y, test_y
train_y,test_y = update_y(Ys0)
```

1 Function 0

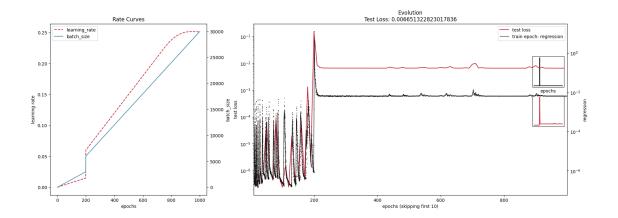
1.1 DNN 0

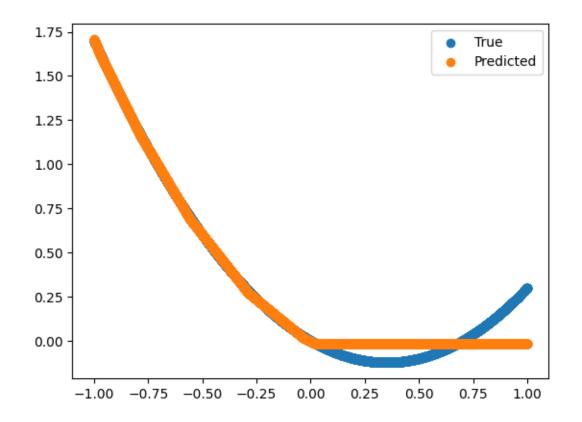
100%| | 1000/1000 [00:12<00:00, 81.81it/s]





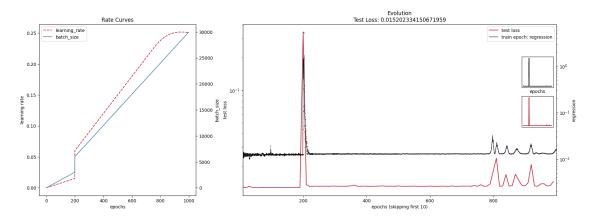
100% | 1000/1000 [00:34<00:00, 29.24it/s]

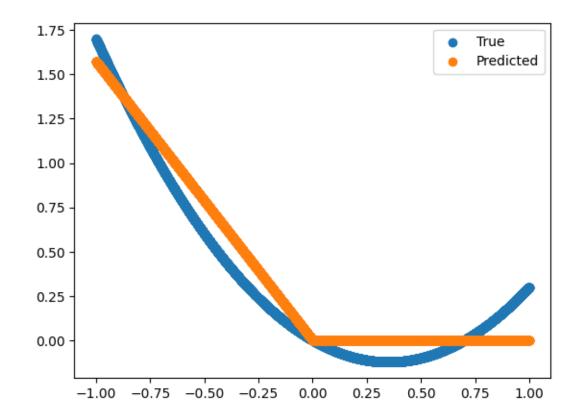




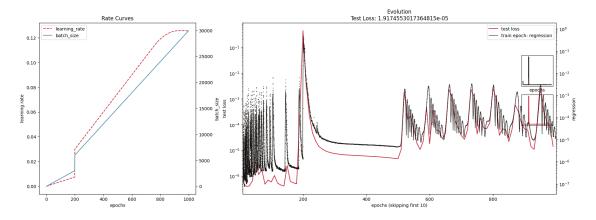
```
act = torch.nn.ReLU()
net = DNN(device, dnn_sizes, opttype=opt, act = act, bias=False) # expect 1.6%
error rate
report = D.train(net, train_X, train_y, test_X, test_y, start_batch_size=10)
ecran(net, test_X, test_y, report, classification=False)
plt.scatter(test_X.detach().cpu().numpy(),test_y.detach().cpu().
numpy(),label='True')
```

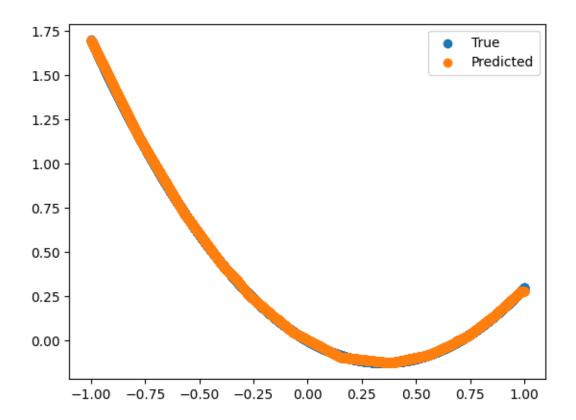
100%| | 1000/1000 [00:23<00:00, 42.29it/s]





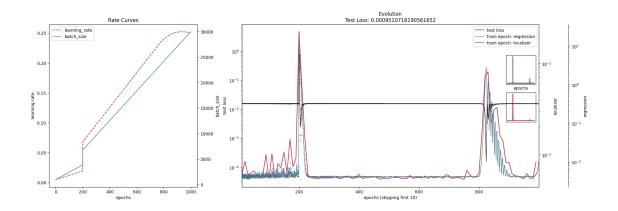
100%| | 1000/1000 [00:37<00:00, 26.85it/s]

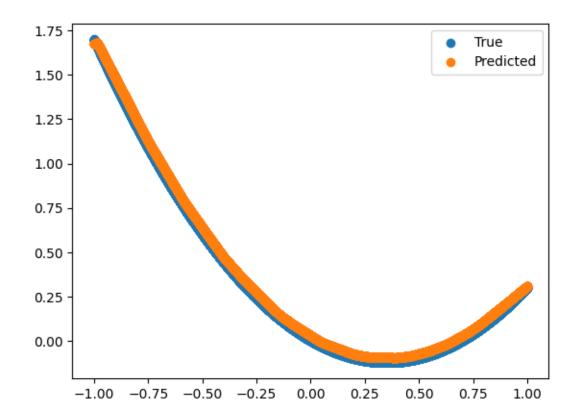




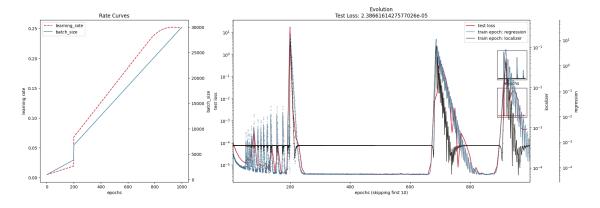
1.2 FL 0

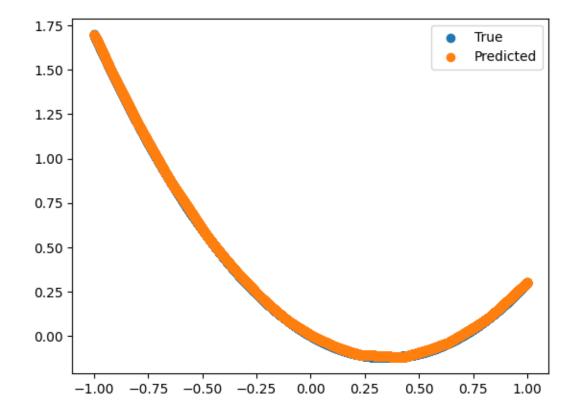
100% | 1000/1000 [00:45<00:00, 22.14it/s]



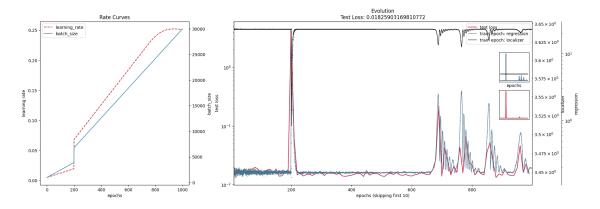


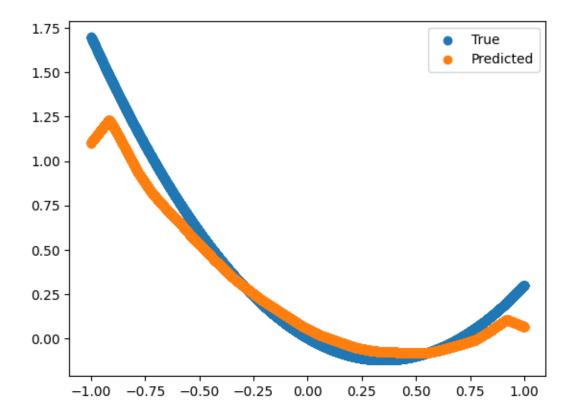
100%| | 1000/1000 [00:43<00:00, 23.22it/s]





100% | 1000/1000 [00:43<00:00, 22.89it/s]





[]:

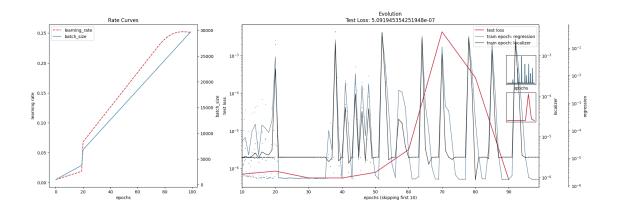
1.3 FL 0 Greedy

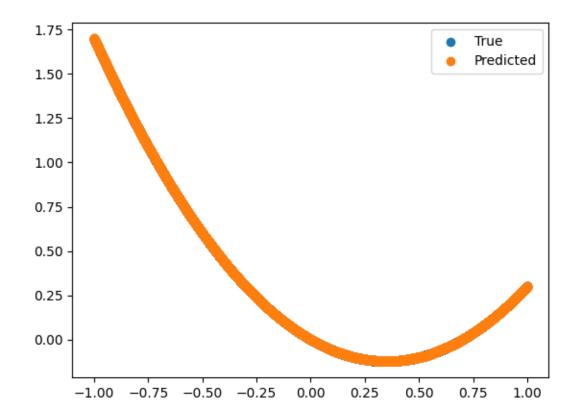
```
[]: act = torch.nn.ReLU()
     delta = np.array([1]*len(fl_sizes))*0.00005
     k = [ks[1]]*len(fl_sizes)
     net = FL(device, fl_sizes, delta, k, opttype=opt, act = act, bias=True) #__
     ⇔expect 1.6% error rate
     D.epochs = 100
     report = D.train(net, train_X, train_y, test_X, test_y, start_batch_size=1000,__
     →repeat_epochs=40)
     D.epochs = 1000
     ecran(net, test_X, test_y, report, classification=False)
     plt.scatter(test_X.detach().cpu().numpy(),test_y.detach().cpu().

¬numpy(),label='True')

     plt.scatter(test_X.detach().cpu().numpy(),net(test_X).detach().cpu().
      →numpy(),label='Predicted')
     plt.legend()
     plt.show()
```

100% | 100/100 [02:55<00:00, 1.75s/it]



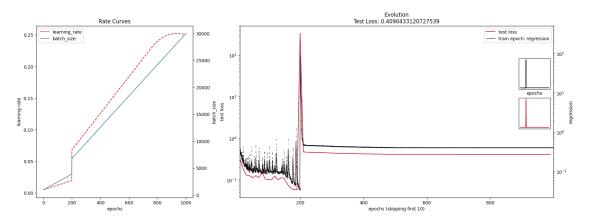


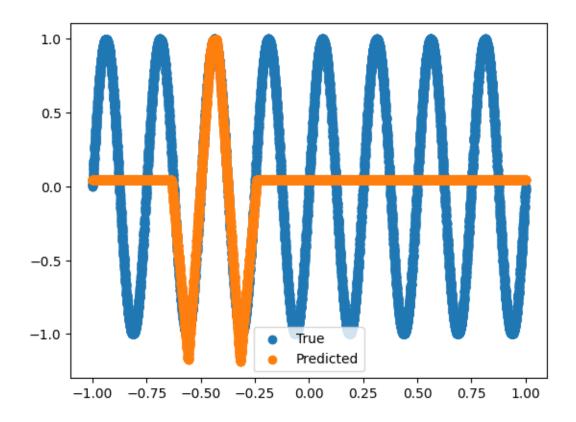
2 Function 1

```
[ ]: train_y, test_y = update_y(Ys1)
```

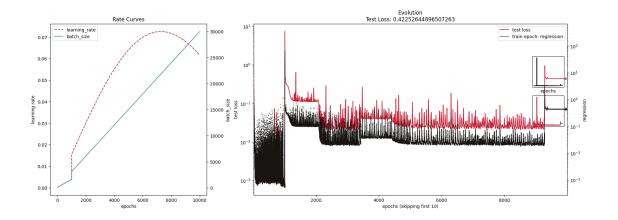
2.1 DNN 1

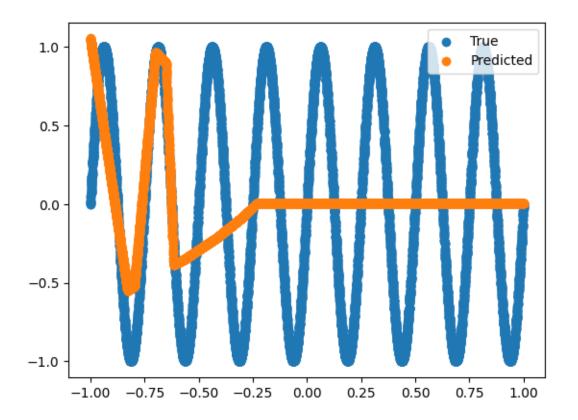
100% | 1000/1000 [00:11<00:00, 85.92it/s]





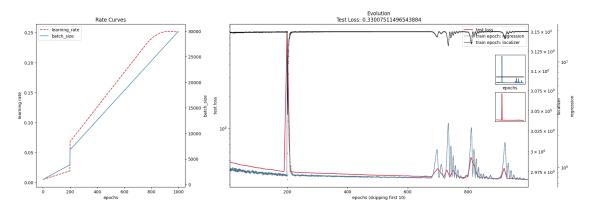
100% | 10000/10000 [03:15<00:00, 51.10it/s]

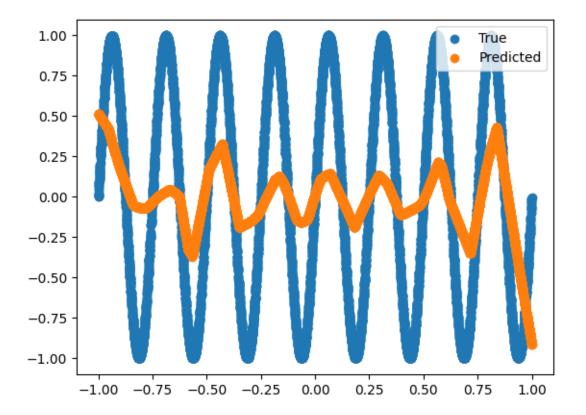




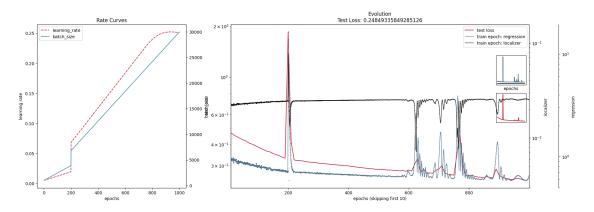
2.2 FL 1

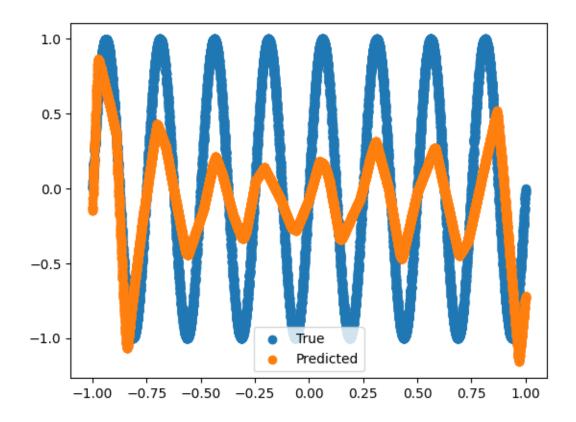
100%| | 1000/1000 [00:42<00:00, 23.80it/s]



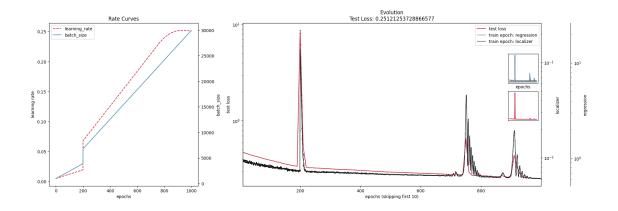


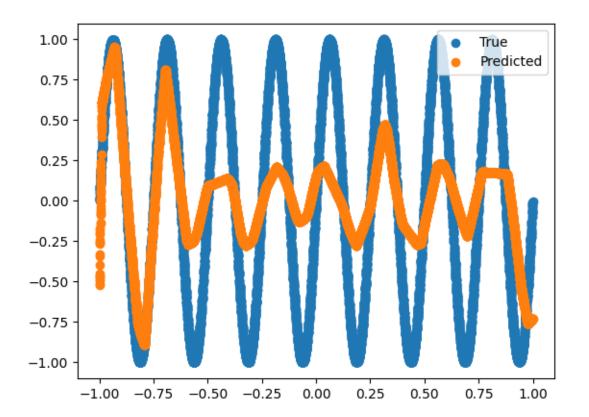
100% | 1000/1000 [00:43<00:00, 23.15it/s]



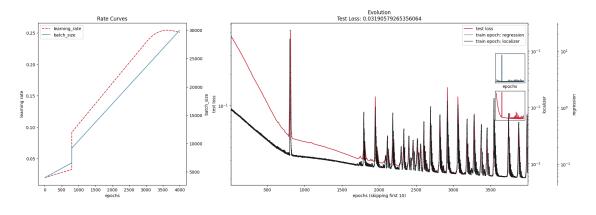


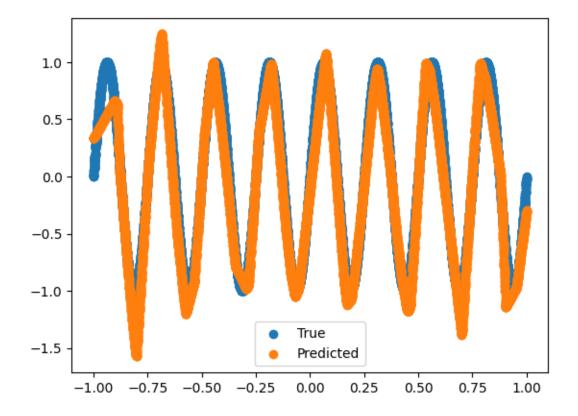
100% | 1000/1000 [00:45<00:00, 21.94it/s]



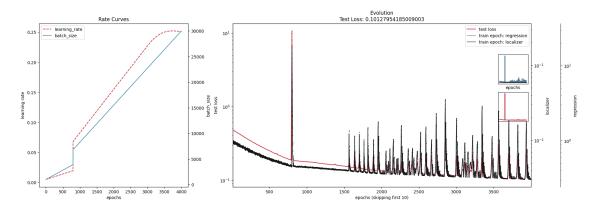


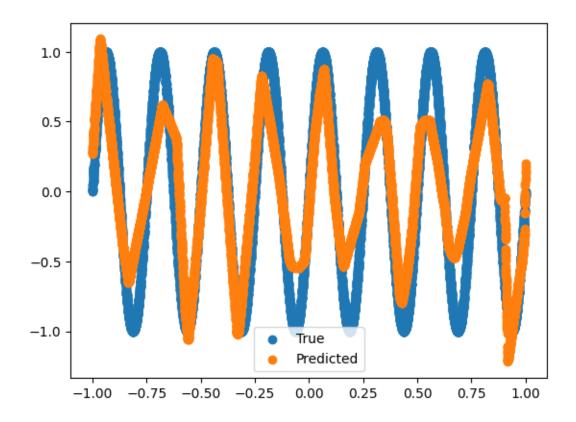
100%| | 4000/4000 [02:12<00:00, 30.12it/s]





100%| | 4000/4000 [03:04<00:00, 21.71it/s]

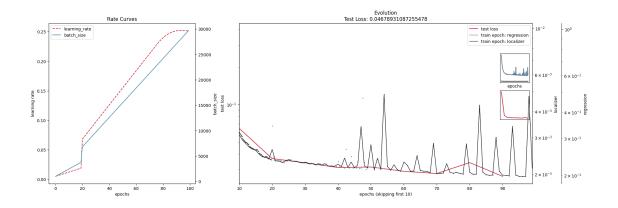


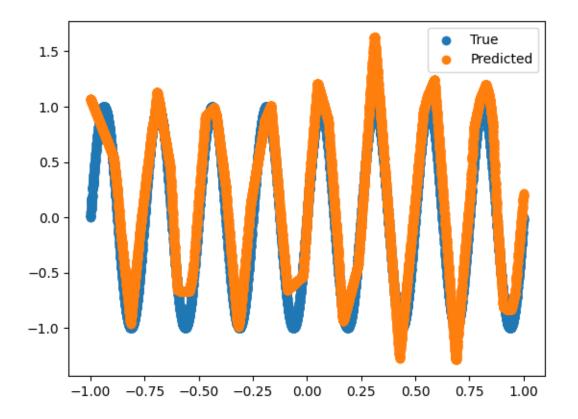


2.3 FL 1 Greedy

```
[]: act = torch.nn.ReLU()
     delta = np.array([1]*len(fl_sizes))*0.00005
     k = [ks[1]]*len(fl_sizes)
     net = FL(device, fl_sizes, delta, k, opttype=opt, act = act, bias=True) #__
      ⇔expect 1.6% error rate
     D.epochs = 100
     report = D.train(net, train_X, train_y, test_X, test_y, start_batch_size=1000,_
      →repeat_epochs=40)
     D.epochs = 1000
     ecran(net, test_X, test_y, report, classification=False)
     plt.scatter(test_X.detach().cpu().numpy(),test_y.detach().cpu().
      →numpy(),label='True')
     plt.scatter(test_X.detach().cpu().numpy(),net(test_X).detach().cpu().
      →numpy(),label='Predicted')
     plt.legend()
    plt.show()
```

100%| | 100/100 [03:02<00:00, 1.82s/it]



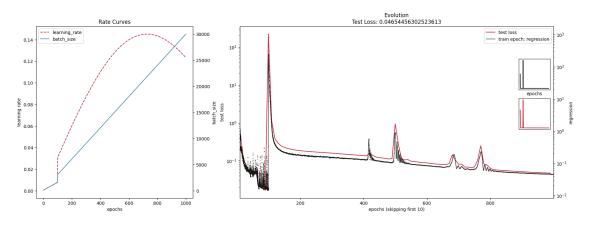


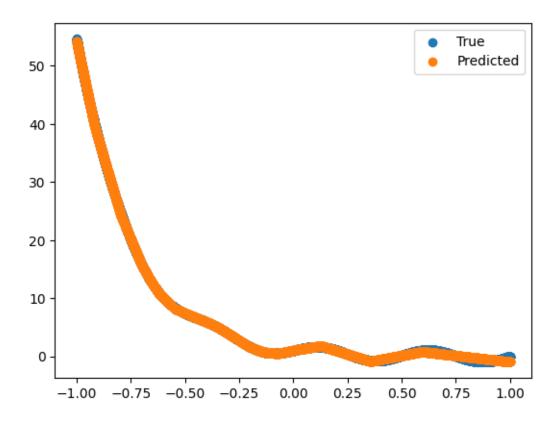
3 Function 2

[]: train_y, test_y = update_y(Ys2)

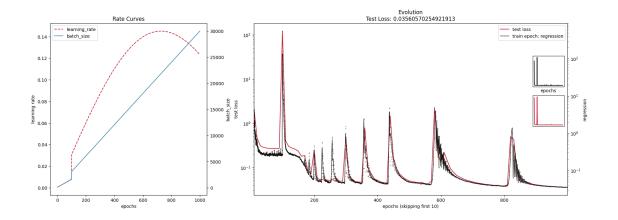
3.1 DNN 2

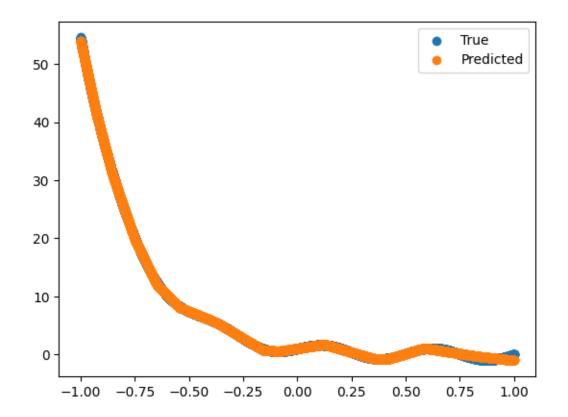
100% | 1000/1000 [00:17<00:00, 55.89it/s]



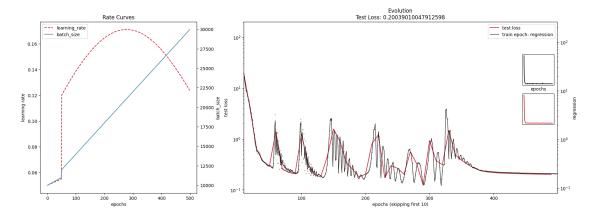


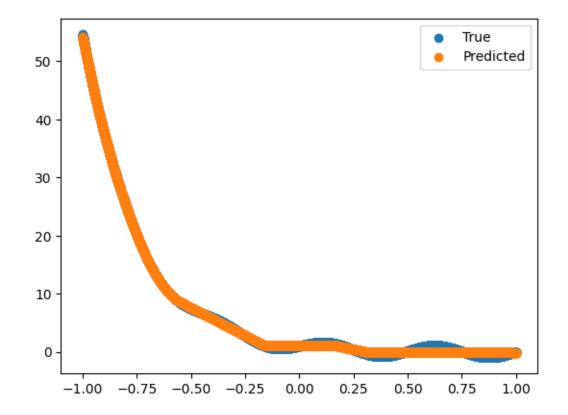
100%| | 1000/1000 [00:22<00:00, 44.51it/s]





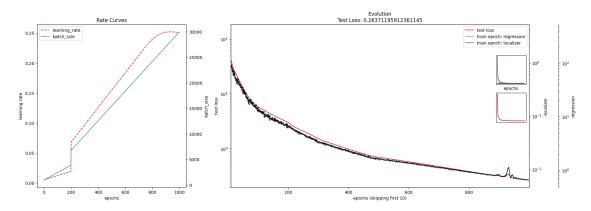
100%| | 500/500 [00:02<00:00, 216.71it/s]

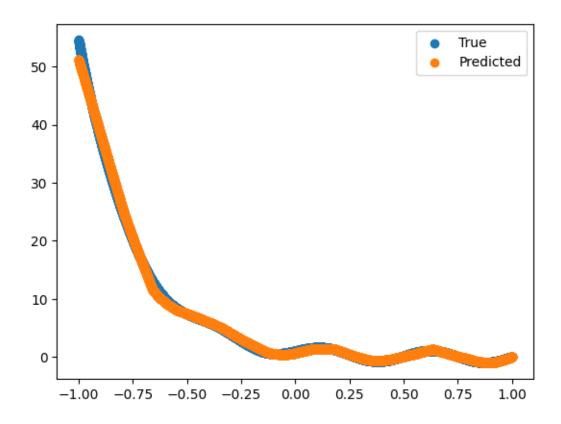




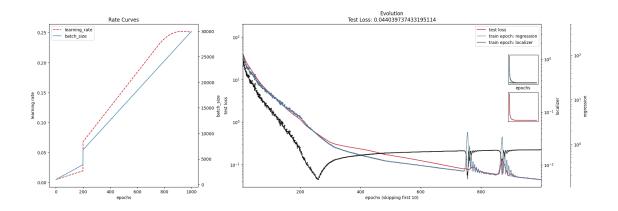
3.2 FL 2

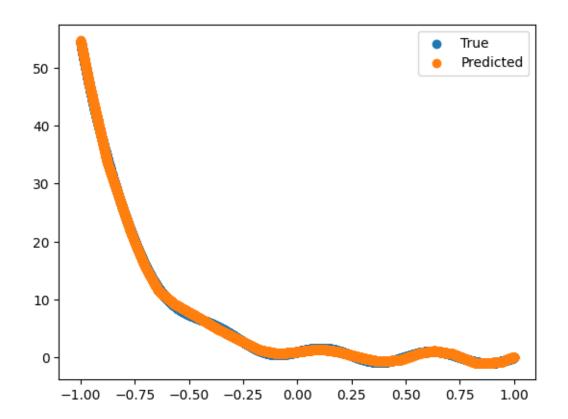
100% | 1000/1000 [00:46<00:00, 21.69it/s]



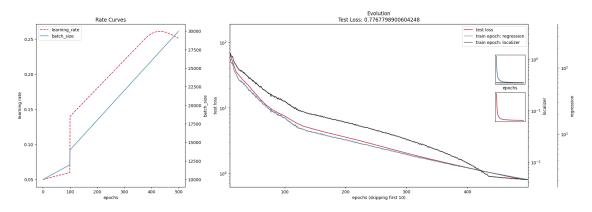


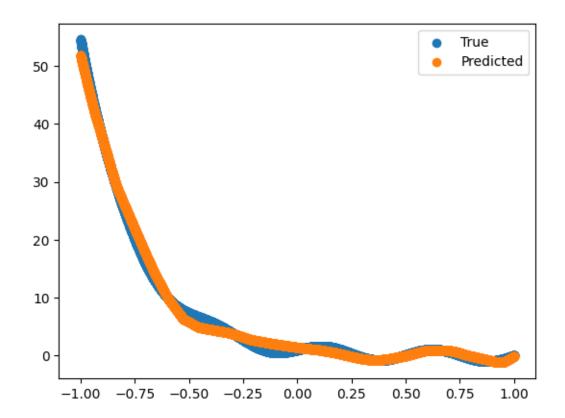
100% | 1000/1000 [00:45<00:00, 22.21it/s]





100%| | 500/500 [00:14<00:00, 33.68it/s]





[]:

3.3 FL 2 Greedy

```
[]: act = torch.nn.ReLU()
     delta = np.array([1]*len(fl_sizes))*0.00005
    k = [ks[1]]*len(fl_sizes)
     net = FL(device, fl_sizes, delta, k, opttype=opt, act = act, bias=True) #__
     ⇔expect 1.6% error rate
     D.epochs = 100
     report = D.train(net, train_X, train_y, test_X, test_y, start_batch_size=1000,__
      →repeat_epochs=40)
     D.epochs = 1000
     ecran(net, test_X, test_y, report, classification=False)
     plt.scatter(test_X.detach().cpu().numpy(),test_y.detach().cpu().
      →numpy(),label='True')
    plt.scatter(test_X.detach().cpu().numpy(),net(test_X).detach().cpu().
      →numpy(),label='Predicted')
     plt.legend()
     plt.show()
```

100% | 100/100 [02:58<00:00, 1.78s/it]

