05

05

06

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05

03

97

Turn Over

## R.S.A.

## QP Code: 31061

(03 Hours)

Total Marks: 80

b)

- 1) Question Number 1 is Compulsory
- 2) Attempt any Three questions from the remaining Five questions
- 3) Assumptions made should be clearly stated. 4) Use of normal table is permitted
- Answer the following

  - For an LTI system with stochastic input prove that autocorrelation of output is given by convolution of cross-correlation (between input-output) and LTI system impulse response.
- Suppose that a pair of fair dice are tossed and let the RV X denote the sum of the points. Obtain probability mass function and cumulative distribution function for X.
- c) If Z = X + Y and if X and Y are independent then derive pdf of Z as convolution of pdf of X and Y.
- d) Write a note on the Markov chains.
- Define and Explain moment generating function in detail. 2a)
- The joint cdf of a bivariate r.v. (X, Y) is given by

Let Z = X/Y. Determine  $f_Z(z)$ 

## $F_{XY}(x,y) = (1 - e^{-\alpha x})(1 - e^{-\beta y}), x \ge 0, y \ge 0, \alpha, \beta > 0$

- D Find the marginal cdf's of X & Y.
- ii) Show that X & Y are independent. iii) Find P(X≤1, Y≤1), P(X≤1), P(Y>1) & P(X>x, Y>y)
- Explain strong law of large numbers and weak law of large numbers.
- 05 Write a note on birth and death queuing models. b) A distribution with unknown mean µ has variance equal to 1.5. Use central limit theorem to find how large a sample should be taken from the distribution in order that the probability will be at least 0.90 that the
- sample mean will be within 0.5 of the population mean. State and prove Chapman-Kolmogorov equation.
- b) State and prove Bayes theorem.
- State any three properties of power spectral density. If the spectral density of a WSS process is given by (ii)  $S(i\theta) = b(a-|i\theta|)/a, |i\theta| \le a$

, |w|>a -0 Find the autocorrelation function of the process.

FW-Con.8961-16.

## **QP Code: 31061**

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5a)	The joint probability function of two discrete $r.v.^*s.X$ and $F$ is given by $f(x,y) = c(Xx + y)$ , where $x$ and $y$ can assume all integers such that $0 \le x \le 2$ , $0 \le y \le 3$ and $f(x,y) = 0$ otherwise. Find $E(X)$ , $E(Y)$ , $E(XY)$ ,			
b)	Prove that if input LTI system is WSS the output is also WSS. What is ergodic process?			
6a)	The transition probability matrix of Markov Chain is			

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Find the limiting probabilities.

An information source generates symbols at random from a four letter alphabet (a, b, c, d) with probabilities

P(a) = 1/2, P(b) = ½ and P(c) = P(d) = 1/8. A coding scheme encodes these symbols into binary codes as follows:

b 10 c 110

d 111

Let X be the random variable denoting the length of the code, ie, the number of binary symbols.

1) What is the range of X?

ii) Sketch the cdf F<sub>X</sub>(x) of X, and specify the type of X.
 iii) Find P(X≤1), P(1<X≤2), P(X>1) & P(1≤X≤2).

Write notes on the following:

i) Block diagram and explanation of single & multiple server queuing system

ii) M/M/1/∞ queuing system

----End-----