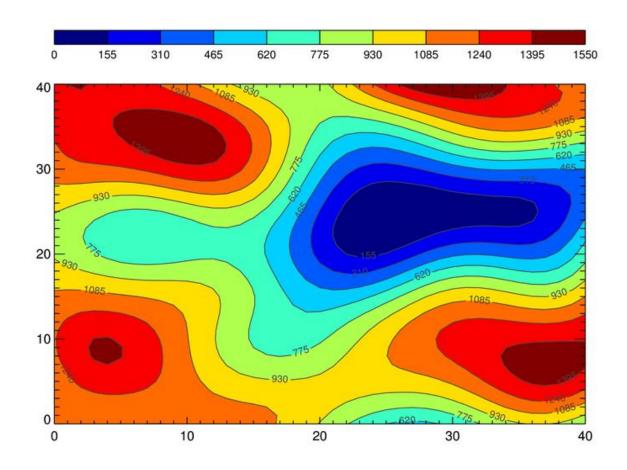
BAYES CLASSIFICATION FOR MULTIVARIATE GAUSSIAN DISTRIBUTION of MULTIPLE CLASSES



Introduction

The main objective of the assignment is to built Bayes Classifier from various given datasets which includes both linearly and nonlinearly separable data. For each dataset the task to generate Bayes classifier and Bayes decision boundary between each possible combination of classes with certain assumptions which can be listed as:

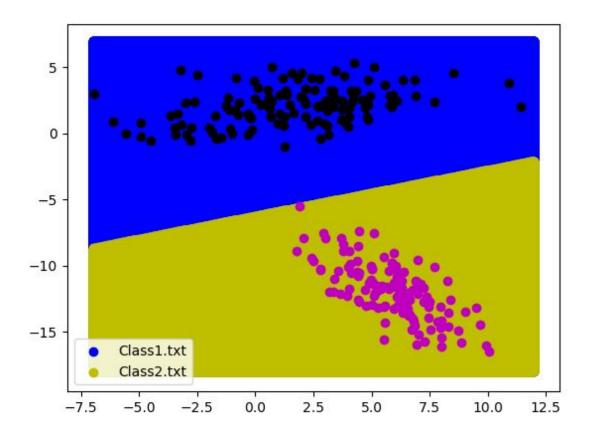
1) Covariance matrix for each class is same and is equal to sigma2 I.For this we first take average of covariance matrix of all classes and then averaging the value of all variances.

- 2) Full Covariance matrix for all the classes is the same and is sigma. Here covariance matrix is obtained by taking average of all covariance matrices.
- 3) Covariance matrix is diagonal and is different for each class
- 4) Full Covariance matrix for each class is different

Additionally we also have to generate contour plots of different classes from discriminant functions of each class.

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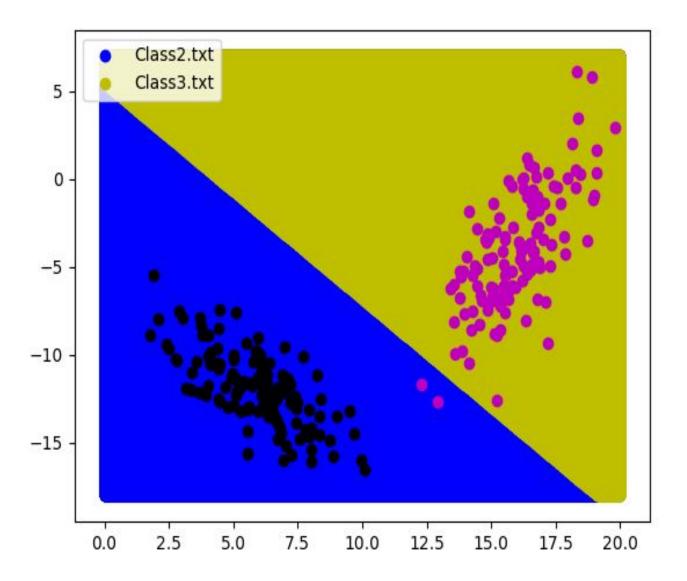
Case 1



- 1) This case corresponds to define Bayes Classifier and decision boundary between two classes when the classes are linearly separable.
- 2) In this case covariance matrix is σ ^2 I.
- 3) The dataset consisted of feature vector having dimensions and these features are statistically independent.

Confusion Matrix	For Class1 Class2
.250	0.1
11.0	124

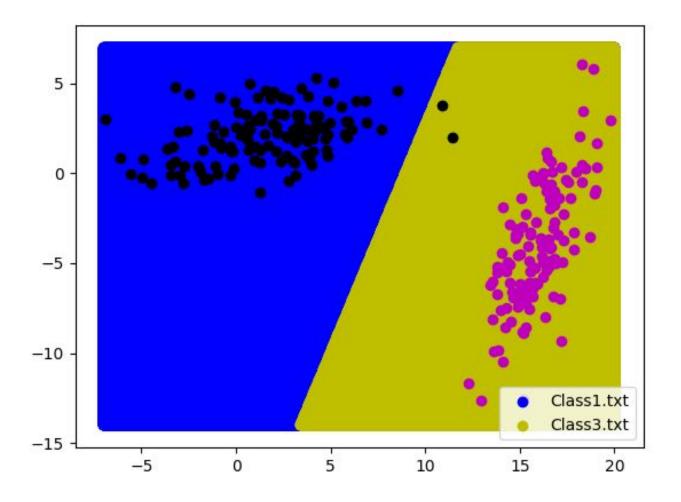
TITLE	VALUE
F-measure for Class1	0.996
F-measure for Class2	0.996
Accuracy of Classification	0.996
Mean recall	0.996
Mean precision	0.996
Mean F-measure	0.996
Recall for class Class1	0.992
Recall for class Class2	1.0
Precision for Class1	1.0
Precision for Class2	0.992



- 1) This plot also corresponds to data set which contains linearly separable data.
- 2) The decision boundary is a straight line.
- 3) As we can see that there is some error associated with the classifier which is shown as two data points which belong to pink class are classified as of black class.
- 4) Such details about the classifier are exposed in the below tables by various parameters.

Confusion Matrix	For Class2 Class3
125.0	0.0
2.0	123.0

TITLE	VALUE
F-measure for Class2	0.992
F-measure for Class3	0.992
Accuracy of Classification	0.992
Mean recall	0.992
Mean precision	0.992
Mean F-measure	0.992
Recall for Class2.	0.984
Recall for Class3	1.0
Precision for Class2	1.0
Precision for Class3	0.984

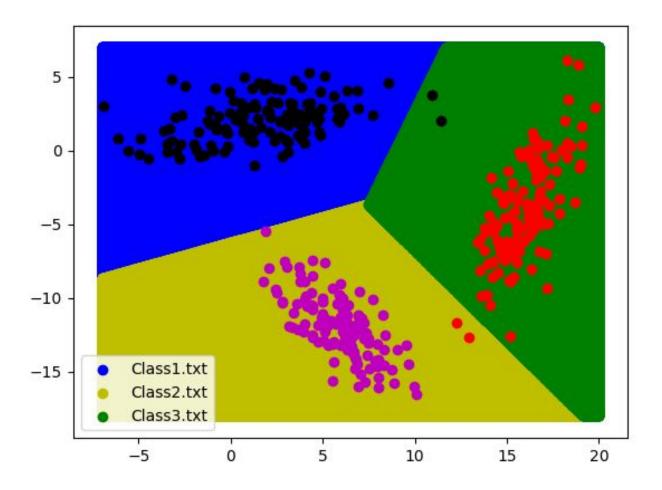


- 1) The 2d plot corresponds to data with feature vector having two dimensions.
- 2) Data is linearly separable and hence the decision boundary is linear.
- 3) There is some error associated with the classification as shown in the figure with wrong classification of two points.

GENERALIZATION FOR D-DIMENSIONS: If covariance matrices for two distributions are equal and proportional to the identity matrix, then the distributions are spherical in d-dimensions and the boundary is a generalized hyperplane in d-1 dimensions, perpendicular to the line joining the means.

Confusion Matrix	For Class1 Class3
123.0	2.0
0.0	125.0

TITLE	VALUE
F-measure for Class1	0.992
F-measure for Class3	0.992
Accuracy of Classification	0.992
Mean recall	0.992
Mean precision	0.992
Mean F-measure	0.992
Recall for Class1	0.984
Recall for Class3	1.0
Precision for Class1	1.0
Precision for Class3	0.984

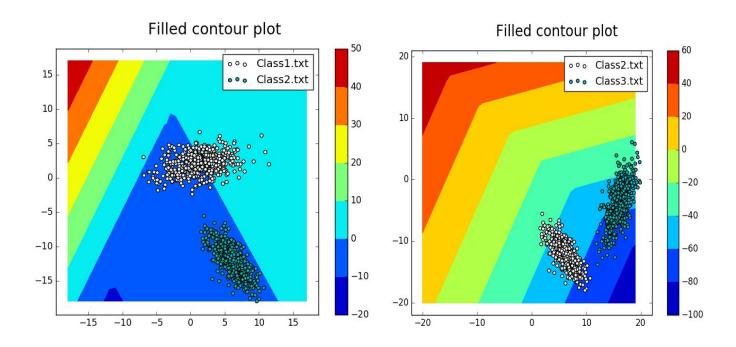


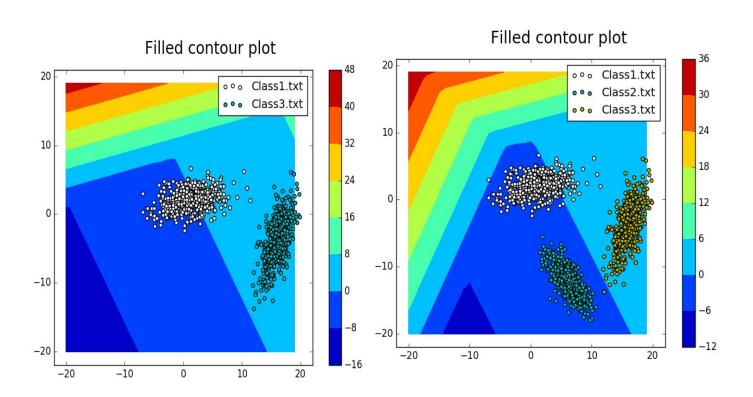
1) This plot shows formulation of decision boundary between three classes simultaneously and here also the data is linearly separable.

Confusion Matrix For Class1 Class2 Class3		
123.0	0.0	2.0
1.0	124.0	0.0
0.0	2.0	123.0

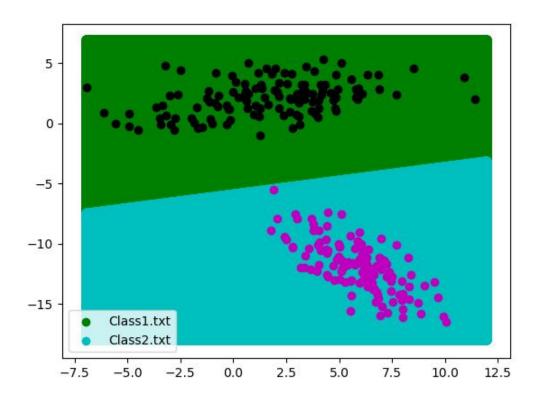
TITLE	VALUE
F-measure for Class1	0.988
F-measure for Class2	0.988
F-measure for Class3	0.984
Accuracy of Classification	0.987
Mean recall	0.987
Mean precision	0.987
Mean F-measure	0.987
Recall for Class1	0.992
Recall for Class2	0.984
Recall for Class3	0.984
Precision for Class1	0.984
Precision for Class2	0.992
Precision for Class3	0.984

Contour Plots for Dataset 1





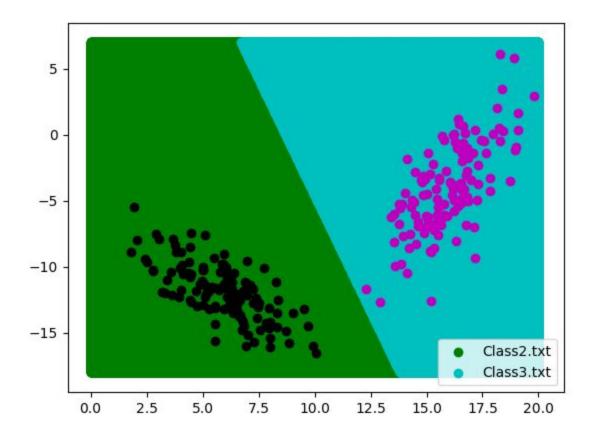
Case 2: Full covariance matrix for each class is same and is Σ .



- 1) This case corresponds to defining Bayes Classifier and decision boundary between two classes which are linearly separable but here the covariance matrix for all classes is considered same (by averaging all the covariance matrices of all classes) but it is arbitrary.
- 2) Decision boundary is this case is also a line which bisects the line joining the centre of means of two classes but unlike the previous case the decision boundary is not orthogonal to the line joining means of two classes.
- 3) It is more refined than the previous case as it is more flexible and gives better result like in the figure above the decision boundary perfectly separates data of two classes.
- 4) The several features of a feature vector are not statistically independent in this case.

Confusion Matrix	For Class1 Class2
125.0	0.0
0.0	125.0

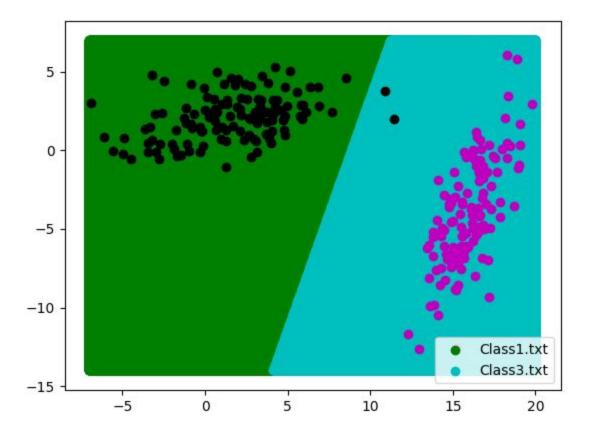
TITLE	VALUE
F-measure for Class1	1.0
F-measure for Class2	1.0
Accuracy of Classification	1.0
Mean recall	1.0
Mean precision	1.0
Mean F-measure	1.0
Recall for class Class1	1.0
Recall for class Class2	1.0
Precision for Class1	1.0
Precision for Class2	1.0



- 1) This plot corresponds to data set which contains linearly separable data.
- 2) The decision boundary is straight line.
- 3) As we can see that there is some error associated with the classifier which is shown as two data points which belong to pink class are classified as of black class.
- 4) These results can be improved if we apply a nonlinear classifier on this same dataset.

Confusion Matrix	For Class2 Class3
125.0	0.0
2.0	123.0

TITLE	VALUE
F-measure for Class2	1.0
F-measure for Class3	1.0
Accuracy of Classification	1.0
Mean recall	1.0
Mean precision	1.0
Mean F-measure	1.0
Recall for Class2.	1.0
Recall for Class3	1.0
Precision for Class2	1.0
Precision for Class3	1.0



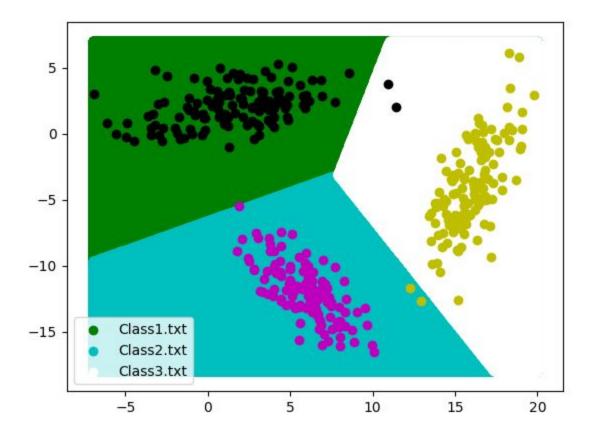
- 1) Data consists of features with feature vector having two dimensions.
- 4) Data is linearly separable and hence the decision boundary is linear.
- 5) There is some error associated with the classification as shown in the figure with wrong classification of two points.

GENERALIZATION FOR D-DIMENSIONS:

If the covariance matrix is arbitrary but is same for all the classes then in d-dimensional space (when feature vector will have d dimensions) the decision hyperplane will not be orthogonal to the line joining their means.

Confusion Matrix	For Class1 Class3
123.0	2.0
0.0	125.0

TITLE	VALUE
F-measure for Class1	0.992
F-measure for Class3	0.992
Accuracy of Classification	0.992
Mean recall	0.992
Mean precision	0.992
Mean F-measure	0.992
Recall for Class1	1.0
Recall for Class3	0.984
Precision for Class1	0.984
Precision for Class3	1.0

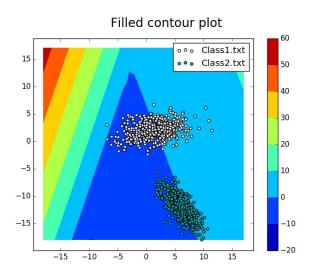


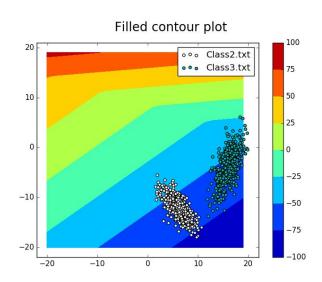
- 2) This plot shows formulation of decision boundary between all the classes simultaneously.
- 3) Confusion matrix is shown below which shows the accuracy of prediction of this classifier.

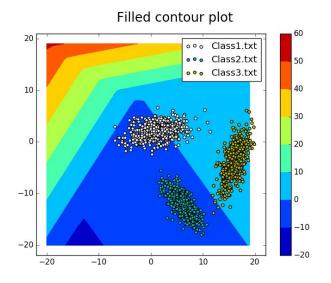
Confusion Matrix For Class1 Class2 Class3		
123.0	0.0	2.0
1.0	124.0	0.0
0.0	2.0	123.0

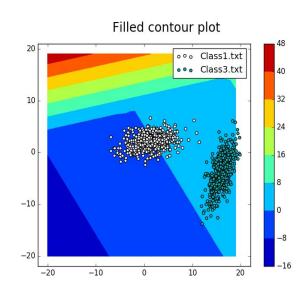
TITLE	VALUE
F-measure for Class1	0.988
F-measure for Class2	0.988
F-measure for Class3	0.984
Accuracy of Classification	0.987
Mean recall	0.987
Mean precision	0.987
Mean F-measure	0.987
Recall for Class1	0.992
Recall for Class2	0.984
Recall for Class3	0.984
Precision for Class1	0.984
Precision for Class2	0.992
Precision for Class3	0.984

Case 2 Contour Plots of Various Classes

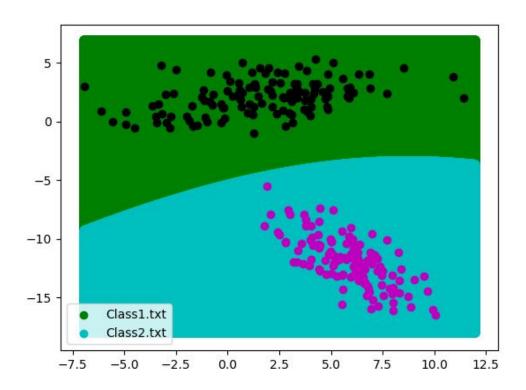








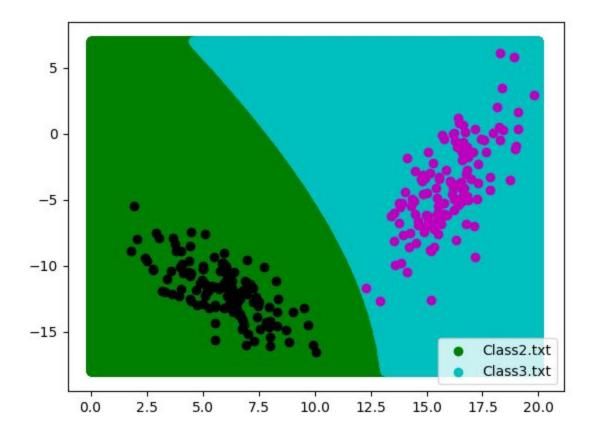
Case 3: Covariance Matrix is diagonal and different for each class.



- 1) Here we consider the case when covariance matrix is diagonal but is different for different classes.
- 2) As the covariance matrix is diagonal we can say the the features involved in feature vector are statistically independent.
- 3) Decision boundary between the classes is nonlinear and specifically by looking at the discriminant function we can infer that it is quadratic which is verified from the above plot also.
- 4) As dataset 1 consisted of data which was linearly separable but defining a nonlinear boundary gave us better results in terms of accuracy but involves a bit more computation.

Confusion Matrix	For Class1 Class2
125.0	0.0
0.0	125.0

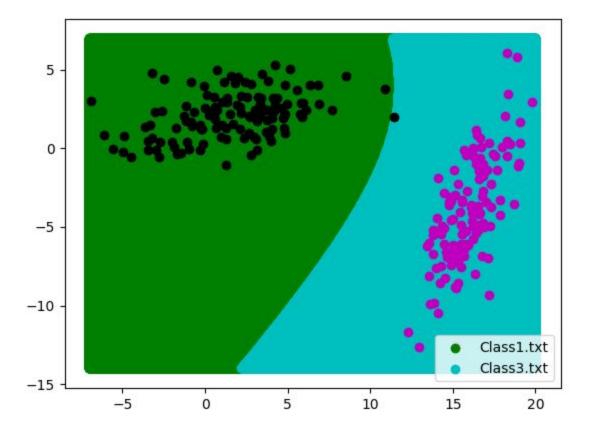
TITLE	VALUE
F-measure for Class1	1.0
F-measure for Class2	1.0
Accuracy of Classification	1.0
Mean recall	1.0
Mean precision	1.0
Mean F-measure	1.0
Recall for class Class1	1.0
Recall for class Class2	1.0
Precision for Class1	1.0
Precision for Class2	1.0



- 5) This plot corresponds to Dataset 1 in which it was given that dataset is linearly separable and we applied a nonlinear decision boundary over it.
- 6) As we can see that it acts better than linear machine in performance and for the above case it gives full accuracy but as the data distribution becomes more complicated like a parabolic distribution then this type of decision boundary will not suffice.
- 7) Various details about the classifier are exposed in the below tables by various parameters.

Confusion Matrix	For Class2 Class3
125.0	0.0
2.0	123.0

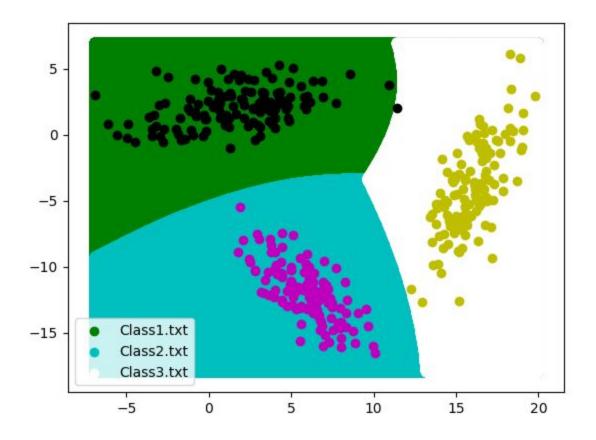
TITLE	VALUE
F-measure for Class2	1.0
F-measure for Class3	1.0
Accuracy of Classification	1.0
Mean recall	1.0
Mean precision	1.0
Mean F-measure	1.0
Recall for Class2.	1.0
Recall for Class3	1.0
Precision for Class2	1.0
Precision for Class3	1.0



- 1) This is also a case of data with feature vector having two dimensions.
- 2) Data is linearly separable and hence the decision boundary is linear.
- 3) There is some error associated with the classification as shown in the figure with wrong classification of two points.

Confusion Matrix	For Class1 Class3
125.0	0.0
0.0	125.0

TITLE	VALUE
F-measure for Class1	1.0
F-measure for Class3	1.0
Accuracy of Classification	1.0
Mean recall	1.0
Mean precision	1.0
Mean F-measure	1.0
Recall for Class1	1.0
Recall for Class3	1.0
Precision for Class1	1.0
Precision for Class3	1.0

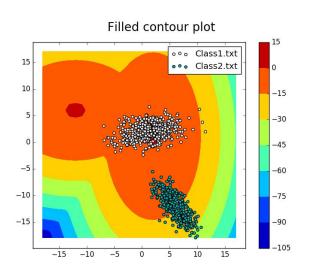


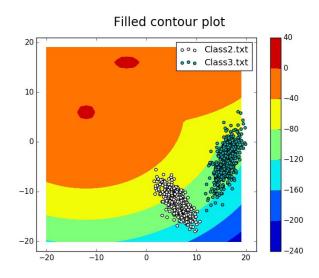
4) This plot shows formulation of decision boundary between three classes simultaneously.

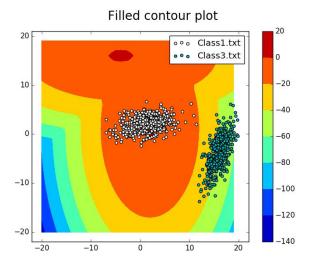
Confusion Matrix For Class1 Class2 Class3		
123.0	0.0	2.0
1.0	124.0	0.0
0.0	2.0	123.0

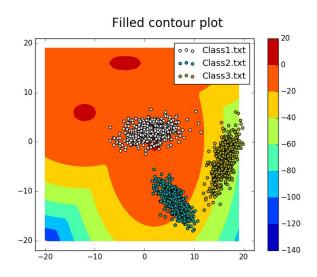
TITLE	VALUE
F-measure for Class1	1.0
F-measure for Class2	1.0
F-measure for Class3	1.0
Accuracy of Classification	1.0
Mean recall	1.0
Mean precision	1.0
Mean F-measure	1.0
Recall for Class1	1.0
Recall for Class2	1.0
Recall for Class3	1.0
Precision for Class1	1.0
Precision for Class2	1.0
Precision for Class3	1.0

Case 3 Contour

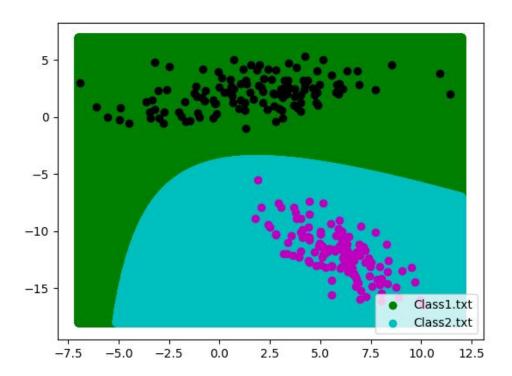








Case 4: Full Covariance Matrix is Different for each class

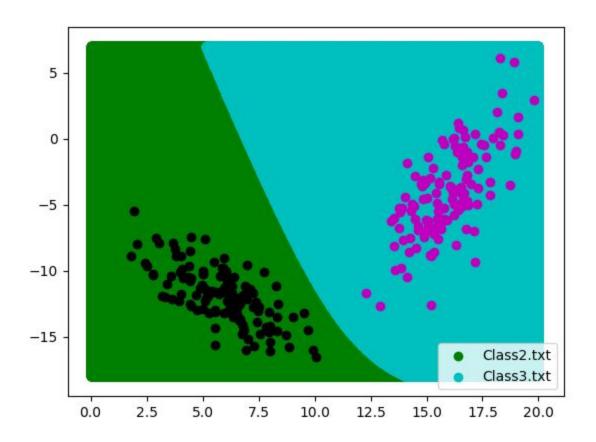


SUMMARISING POINTS:

4) This case corresponds to defining Bayes Classifier and decision boundary between two classes which are linearly separable.

Confusion Matrix For Class1 Class2	
125.0	0.0
0.0	125.0

TITLE	VALUE
F-measure for Class1	1.0
F-measure for Class2	1.0
Accuracy of Classification	1.0
Mean recall	1.0
Mean precision	1.0
Mean F-measure	1.0
Recall for class Class1	1.0
Recall for class Class2	1.0
Precision for Class1	1.0
Precision for Class2	1.0

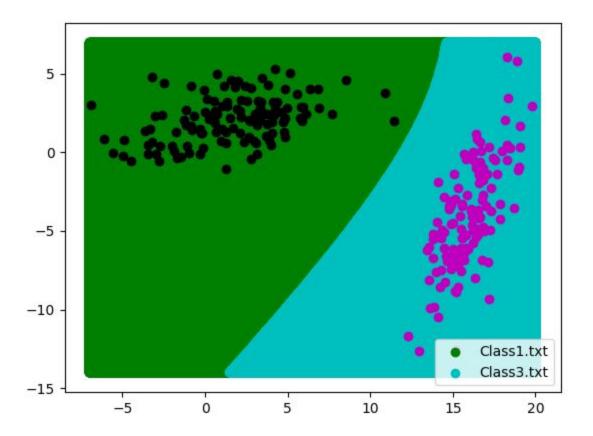


SUMMARISING POINTS:

- 1) This plot corresponds to data set which contains linearly separable data.
- 2) The decision boundary is parabolic.
- 3) As we can see that there is some error associated with the classifier which is shown as two data points which belong to pink class are classified as of black class.
- 4) Such details about the classifier are exposed in the below tables by various measures.

Confusion Matrix For Class2 Class3	
125.0	0.0
0.0	123.0

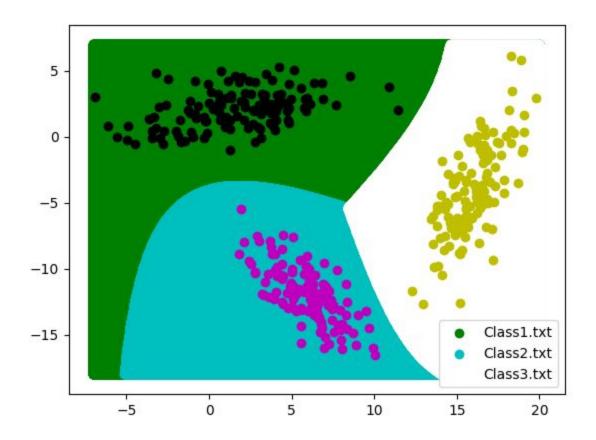
TITLE	VALUE
F-measure for Class2	1.0
F-measure for Class3	1.0
Accuracy of Classification	1.0
Mean recall	1.0
Mean precision	1.0
Mean F-measure	1.0
Recall for Class2.	1.0
Recall for Class3	1.0
Precision for Class2	1.0
Precision for Class3	1.0



- 1) Feature vector have two dimensions.
- 2) Data is linearly separable but the Bayes classifier applied is nonlinear (as of case 4).
- 3) The features of feature vector are not statistically independent.
- 4) The results have high accuracy in this case.

Confusion Matrix For Class1 Class3	
125.0	0.0
0.0	125.0

TITLE	VALUE
F-measure for Class1	1.0
F-measure for Class3	1.0
Accuracy of Classification	1.0
Mean recall	1.0
Mean precision	1.0
Mean F-measure	1.0
Recall for Class1	1.0
Recall for Class3	1.0
Precision for Class1	1.0
Precision for Class3	1.0



This plot shows formulation of parabolic decision boundary between three classes simultaneously

Confusion Matrix For Class1 Class2 Class3		
125.0	0.0	0.0
0.0	125.0	0.0
0.0	0.0	125.0

TITLE	VALUE
F-measure for Class1	1.0
F-measure for Class2	1.0
F-measure for Class3	1.0
Accuracy of Classification	1.0
Mean recall	1.0
Mean precision	1.0
Mean F-measure	1.0
Recall for Class1	1.0
Recall for Class2	1.0
Recall for Class3	1.0
Precision for Class1	1.0
Precision for Class2	1.0
Precision for Class3	1.0

Case 4 Contour

