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# Symmetric and asymmetric tilt grain boundary structure and energy in Cu and Al (and transferability to other fcc metals)

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## Abstract

Symmetric and asymmetric tilt grain boundaries in Cu and Al were generated using molecular statics energy minimization in a classical molecular dynamics code with in-plane grain boundary translations and an atom deletion criterion. The following dataset (NIST repository, <http://hdl.handle.net/11256/358>) contains atomic coordinates for minimum energy grain boundaries in three-dimensional periodic simulation cells, facilitating their use in future simulations. This grain boundary dataset is used to show the relative transferability of grain boundary structures from one face-centered cubic system to another; in general, there is good agreement in terms of grain boundary energies ( $R^2 > 0.99$ ). Some potential applications and uses of this tilt grain boundary dataset in nanomechanics and materials science are discussed.

**Keywords:** Tilt grain boundaries; Grain boundary structure; Grain boundary energy; fcc; Molecular dynamics; Copper; Aluminum; LAMMPS; Face-centered cubic

## Data Description

### Introduction

The bulk properties of polycrystalline materials are heavily influenced by atomic details associated with the crystallography of the grains and the structure of grain boundaries [1]. While one route to achieving an improvement to the properties of polycrystalline materials is to engineer the texture of the material, another route that is being increasingly explored is to engineer the distribution of special grain boundaries in the polycrystal. This latter technique is motivated by the fact that different atomic structures at the grain boundary often lead to different properties or responses. Hence, the notion of “grain boundary engineering” [2] has evolved to increase the number density of grain boundaries with beneficial properties, while reducing the number density of boundaries that have detrimental properties. It can also refer to compromise trade-offs of distributions to achieve competing property sets. In practice, grain boundary (GB) engineering has largely referred to increasing the number of low- $\Sigma$  boundaries [3], e.g., increasing the number of coherent twin boundaries [4], which have properties that differ significantly from general high-angle grain boundaries. As computational techniques have improved, more researchers are turning to atomistic studies to quantify the influence of grain boundary structure on properties and collective responses at higher length and time scales. Many of the early studies (e.g., [5, 6]) focused on understanding the grain

boundary structure and energy. However, recent studies have expanded to address grain boundary sliding [7–10], migration and bulk dislocation slip transfer [11–13], grain boundary fracture [14–16] or spall [17–20], grain boundary segregation [21–23], phase transformations [24], grain boundary mobility [25, 26], etc. In many cases, grain boundary structures have to be recreated in order to assess properties, and it is unclear whether the minimum energy structure was used or a higher energy metastable structure; hence, openly publishing grain boundary datasets in materials repositories can aid in providing a common starting configuration for these studies.

The objective of this data descriptor article is to provide and describe datasets for minimum energy ( $\langle 100 \rangle$ ,  $\langle 110 \rangle$ ,  $\langle 111 \rangle$ ) symmetric and ( $\Sigma 3$ ,  $\Sigma 5$ ,  $\Sigma 9$ ,  $\Sigma 11$ ,  $\Sigma 13$ ) asymmetric tilt grain boundaries in Cu and Al [27], which have been previously used to explore structure-energy relationships [28–31] as well as dislocation nucleation at the grain boundary [32–37]. The grain boundary datasets for Al and Cu can support future studies of structure-property relations, as well as providing data to support multiscale models of various types [38].

### Simulation methods

The macroscopic grain boundary geometry is defined using five degrees of freedom (DOF) that fully describe the crystallographic orientation of one grain relative to the other (3 DOF) and the orientation of the boundary relative to one of the grains, i.e., the grain boundary plane (2 DOF). On a microscopic level, the translation between the two adjoining crystal lattices requires three additional DOF. Atomistic simulations are used to explore how the grain boundary DOF affect the structure and properties of particular grain boundaries.

A few terms are often used to describe the crystallography of grain boundaries: sigma values ( $\Sigma$ ), tilt versus twist, symmetric versus asymmetric boundaries, crystallographic directions for GB tilt/twist classification (e.g.,  $\langle 100 \rangle$ ,  $\langle 110 \rangle$ ,  $\langle 111 \rangle$ ), and specification of grain boundary planes. First, the  $\Sigma$  value is often used in conjunction with the coincident site lattice (CSL) model, which simply states that at certain orientations between two interpenetrating lattices there are a number of positions where the atoms are in coincidence. Boundaries with a large fraction of coincident sites may have properties different from more general grain boundaries with a much lower number of coincident points. In this context, the  $\Sigma$  value refers to the reciprocal of the density of coincident sites, i.e., a  $\Sigma 3$  boundary has 1/3 of the atoms in coincident sites, the  $\Sigma 13$  has 1/13, and so on. Tilt and twist boundaries arise from both crystal lattices having a shared lattice vector; in tilt boundaries, this lattice vector is contained within the grain boundary plane, and in twist boundaries, this lattice vector is orthogonal to the grain boundary plane. For most general grain boundaries, they are a combination of both tilt and twist. For pure tilt boundaries, they can be separated into symmetric and asymmetric boundaries based on their relationship to the grain boundary plane, i.e., the crystallographic directions of symmetric tilt boundaries are mirrored about the grain boundary plane. In terms of specifying lattice directions in this work, the tilt direction is often specified as  $\langle 100 \rangle$  or  $\langle 110 \rangle$  or  $\langle 111 \rangle$ , which specifies a family of crystallographically identical directions (i.e.,  $\langle 110 \rangle$  can refer to  $[110]$ ,  $[101]$ ,  $[011]$ , etc.). In the same manner, a family of planes can be referred to by  $\{210\}$ , for example, where this can denote the planes  $(210)$ ,  $(120)$ ,  $(012)$ , etc. Therefore, for tilt boundaries, a lattice direction is often given to

denote the shared tilt axis (e.g.,  $\langle 110 \rangle$ ) and either one (symmetric) or two (asymmetric) planes are given to fully characterize the grain boundary crystallography. For further information on the crystallography of grain boundaries and the coincident site lattice, the reader is referred to books such as by Randle [39].

The datasets for Al and Cu tilt grain boundaries [27] are generated using a computational cell with three-dimensional (3-D) periodic boundary conditions, which results in two grains and two grain boundaries. The crystal lattices for the two grains are created such that periodicity in all directions is maintained through the simulation cell boundaries. In the case of the direction perpendicular to the grain boundary plane, this periodic distance is selected to ensure that the two grain boundaries are identical in structure. The size of the computational cell is large enough to eliminate any interaction between the two grain boundaries while attempting to minimize the number of atoms in the cell. The two grain boundaries are separated by similar distances in terms of lattice units—a minimum distance of 12.0 nm in Cu and  $\sim 13.4$  nm in Al, corresponding to the simulated minimum energy lattice constants  $a_0 = 3.615 \text{ \AA}$  and  $a_0 = 4.032 \text{ \AA}$  with the present Cu and Al interatomic potentials, respectively. The minimum periodic distance is used for the orthogonal directions parallel to the grain boundary plane. This effectively minimizes the number of atoms required without affecting the 0 K grain boundary structure or energy. For calculating properties, replication in these dimensions may be required to ensure that simulation cell size effects are not affecting the results (e.g., suppressing dislocations on certain  $\{111\}$  systems).

The included scripts<sup>1</sup> for the 15 May 2015 version of the classical molecular dynamics code LAMMPS (Large-scale Atomic/Molecular Massively Parallel Simulator) [40] serve as an example of a brute force method for obtaining the local and global “minimum energy” grain boundary structures for a particular set of macroscopic DOF. Because of different translations of the grains with respect to each other and different densities of atoms at the interface, a single set of macroscopic DOF can produce a multitude of different grain boundary structures and energies. In practice, the minimum energy structure (from this distribution of different structures) correlates well with high-resolution TEM images of interface structures [34, 41]. There are multiple steps for obtaining the minimum energy structure: grain boundary initialization, rigid body translation, atom deletion criterion, and conjugate gradient energy minimization.

The *grain boundary initialization* step involves selecting the crystallographic orientations of the two lattices, defining the interatomic potential, calculating the lattice constant and periodic distances, defining the simulation cell bounds, and building the atom positions within the two grains. Next, the *rigid body translation* of one lattice with respect to the other is used to sample different starting configurations, thus improving the probability that a “global” minimum energy structure is obtained following energy minimization. In these datasets, a grid of translations was defined to sample the in-plane translations uniformly (minimum of four translations in the tilt direction and eight translations in the grain boundary period direction). Since atoms in the two lattices are built up to the GB plane, an *atom deletion criterion*—i.e., if atom  $a$  from lattice  $A$  is within a certain distance of atom  $b$  in lattice  $B$ , then delete atom  $a$ —is used to remove atoms that may physically lie too close to each other. Note that this criterion removes atoms identically at both grain boundaries. In these datasets, the atom deletion criterion uses distances between  $0.275a_0$  and  $0.700a_0$  in increments of  $0.005a_0$  at each

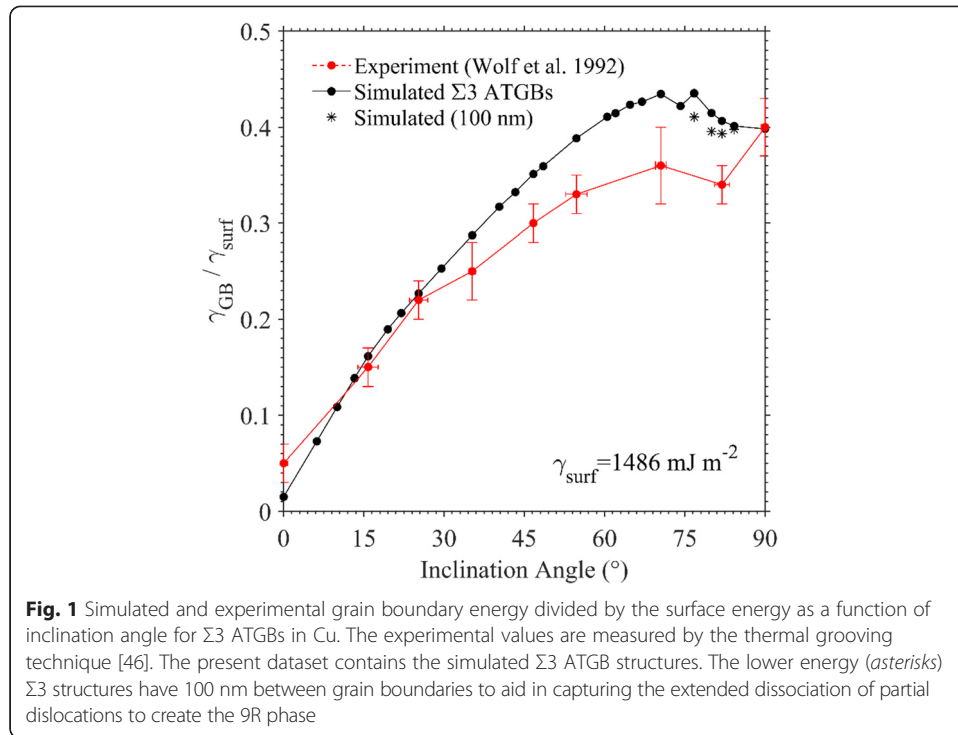
in-plane translation (for face-centered cubic (fcc), i.e., nearest neighbor distance is  $\sqrt{2}a_0$ ). Here, successive atom deletion criteria that do not reduce the number of atoms reproduce a previously examined structure and thus are ignored to improve computational efficiency. It should be noted that for asymmetric grain boundaries, the decision to delete an atom from lattice *A* or lattice *B* will give different starting configurations, so the number of configurations is doubled (e.g., 86 distances/starting configurations for symmetric GBs, 172 distances for asymmetric GBs). After the initial configuration is generated, *energy minimization* is used to obtain the final structure for a particular combination of the grain boundary crystallography, in-plane translations, and atom deletion distance. In this case, the nonlinear conjugate gradient algorithm employed the Polak-Ribiere formula and the secant method for calculating the new search direction (i.e., for atom movement) and the appropriate step size (magnitude of movement), respectively. The conjugate gradient algorithm terminates when the residual of the potential energy (i.e., the force vector) falls below a predefined value. Since there are no fixed regions of atoms in the computational cell, the crystal lattices can translate as appropriate and grain boundary atoms can move to obtain the final minimum energy structure. Further details can be found in Ref. [29].

In the present datasets, embedded atom method (EAM) potentials for Cu [42] and Al [43] were used to generate the minimum energy grain boundaries. These potentials were experimentally fit to give the correct physical properties for Cu and Al, including the equilibrium lattice parameter, the cohesive energy, three elastic constants, and the vacancy formation energy, to name a few. The calculated stacking fault energies (SFE) for these potentials are consistent with experimental data and ab initio calculations. The stable SFE determines the width of dislocation dissociation within both the lattice and the grain boundary. While these potentials were deemed valid for generating grain boundary structures and energies, it should be checked that their properties are suitable for capturing other grain boundary properties or responses.

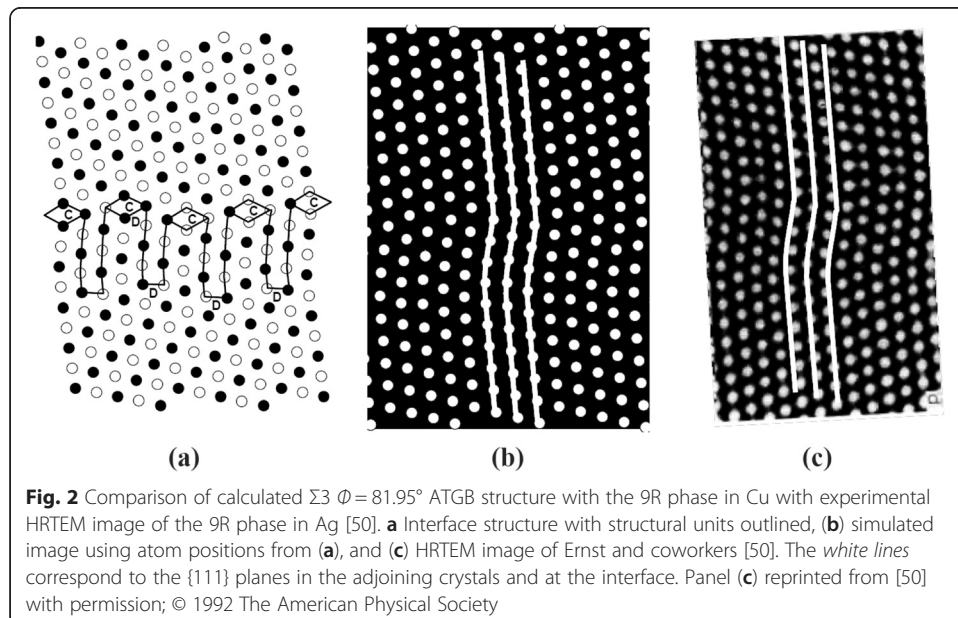
As an indication of the validity of the methods and potentials, the computed grain boundary energies are in good agreement with experimental energy curves for  $\langle 110 \rangle$  symmetric tilt grain boundaries [44] and for  $\Sigma 3$  asymmetric grain boundaries [45, 46]. For instance, Fig. 1 compares the computed grain boundary energies<sup>2</sup>, which have been normalized by the  $\{110\}$  surface energy, to experimentally measured energies. The grain boundary structures generated are also in good agreement with prior simulated grain boundary structures for low- and high-SFE materials [47, 48] as well as experimentally observed structures using high-resolution transmission electron microscopy [41, 49], which includes the observation of the 9R phase in low-SFE fcc metals [50–52], as shown in Fig. 2.

### Dataset description

The following dataset [27] contains 174 symmetric and asymmetric tilt grain boundaries in both Al and Cu (total of 348 grain boundaries) along with the corresponding inter-atomic potentials mentioned previously<sup>3</sup>. In this dataset, there are 68 symmetric tilt grain boundaries (STGBs), which include 29  $\langle 100 \rangle$  STGBs, 32  $\langle 110 \rangle$  STGBs, and 7  $\langle 111 \rangle$  STGBs. The remaining 106 grain boundaries in the dataset are asymmetric tilt grain boundaries (ATGBs), which include 26  $\Sigma 3$  ATGBs, 16  $\Sigma 5$  ATGBs, 27  $\Sigma 9$  ATGBs, 27  $\Sigma 11$  ATGBs, and 10  $\Sigma 13$  ATGBs. In the dataset, the coordinates of the simulation cell



and atoms for Al and Cu are provided in a LAMMPS data file format and can be accessed using the “read\_data” command within a LAMMPS input file. The data file names are in the following format: lammmps.#1.#2\_#3.dat where argument #1 is the element type (Cu or Al), argument #2 is the system (e.g., stgb001 for  $\langle 100 \rangle$  STGBs or sigma3 for  $\Sigma 3$  ATGBs), and argument #3 is a reference number that is sequentially numbered in order of increasing misorientation angle from a vector describing the GB plane (1, 2, 3, etc.). The reference number (argument #3) is used to identify the different GBs in the associated text file



(info.#4.txt, where argument #4 corresponds to the aforementioned argument #2), which contains the minimum information required to specify the orientations of the surrounding two crystal lattices (the lattice vector describing the GB plane, i.e.,  $x_1, y_1, z_1$  for lattice 1 and  $x_2, y_2, z_2$  for lattice 2), the computed grain boundary energies, and the sigma values for the symmetric tilt grain boundaries. Table 1 shows an example of the information within this text file for  $\Sigma 3$  asymmetric tilt grain boundaries. First, the misorientation angle is with reference to the  $\langle 110 \rangle \{112\}$  STGB (first boundary); if the reference is the  $\langle 110 \rangle \{111\}$  STGB (the 26th boundary), then all misorientation angles  $\theta$  would be  $90^\circ - \theta$ . Also,  $x_1, y_1, z_1$  and  $x_2, y_2, z_2$  refer to the grain boundary planes of lattices 1 and 2, respectively, in this dataset. Since the tilt direction is also known for the symmetric and asymmetric systems, the three orthogonal lattice vectors describing the complete lattice orientation can be calculated. For asymmetric tilt grain boundaries, both planes are necessary to completely describe the grain boundary, i.e., the  $\Sigma 3$  (110)/(114) ATGB.

In the ATGB systems, it should be noted that the two STGBs that bracket the asymmetric boundaries are also included. These are actually duplicates of grain boundaries in the STGB systems, and the text file “duplicate\_boundaries.txt” identifies the duplicate boundary file names. These duplicate boundaries were retained to enable easy

**Table 1** Inclination angle and grain boundary plane orientations for  $\Sigma 3$  tilt grain boundaries

#	Angle	Al_GBE	Cu_GBE	$x_1$	$y_1$	$z_1$	$x_2$	$y_2$	$z_2$
1	0.00	354.4	591.9	1	1	2	1	1	-2
2	5.77	361.6	596.3	8	8	13	2	2	-5
3	8.05	363.0	604.2	2	2	3	4	4	-11
4	10.02	364.0	616.3	5	5	7	1	1	-3
5	13.26	364.6	646.9	4	4	5	2	2	-7
6	15.79	363.0	627.3	7	7	8	1	1	-4
7	19.47	361.1	645.8	1	1	1	1	1	-5
8	22.99	357.0	633.8	8	8	7	2	2	-13
9	25.24	352.2	629.3	5	5	4	1	1	-8
10	27.94	346.8	616.2	7	7	5	1	1	-11
11	29.50	343.5	610.6	3	3	2	1	1	-14
12	35.26	329.0	577.3	2	2	1	0	0	1
13	41.47	312.5	533.9	3	3	1	1	1	13
14	43.31	305.8	521.8	7	7	2	1	1	10
15	46.69	296.2	493.7	5	5	1	1	1	7
16	49.68	285.3	471.1	8	8	1	2	2	11
17	54.74	267.1	427.0	1	1	0	1	1	4
18	60.50	243.6	375.6	-7	-7	1	1	1	3
19	64.76	225.5	337.0	-4	-4	1	2	2	5
20	68.00	211.8	306.7	-3	-3	1	5	5	11
21	70.53	197.7	281.5	-5	-5	2	1	1	2
22	74.21	176.8	239.9	-2	-2	1	4	4	7
23	76.74	161.6	206.0	-7	-7	4	5	5	8
24	79.98	141.5	161.7	-3	-3	2	7	7	10
25	83.79	116.8	108.5	-14	-14	11	4	4	5
26	90.00	75.2	22.2	-1	-1	1	1	1	1



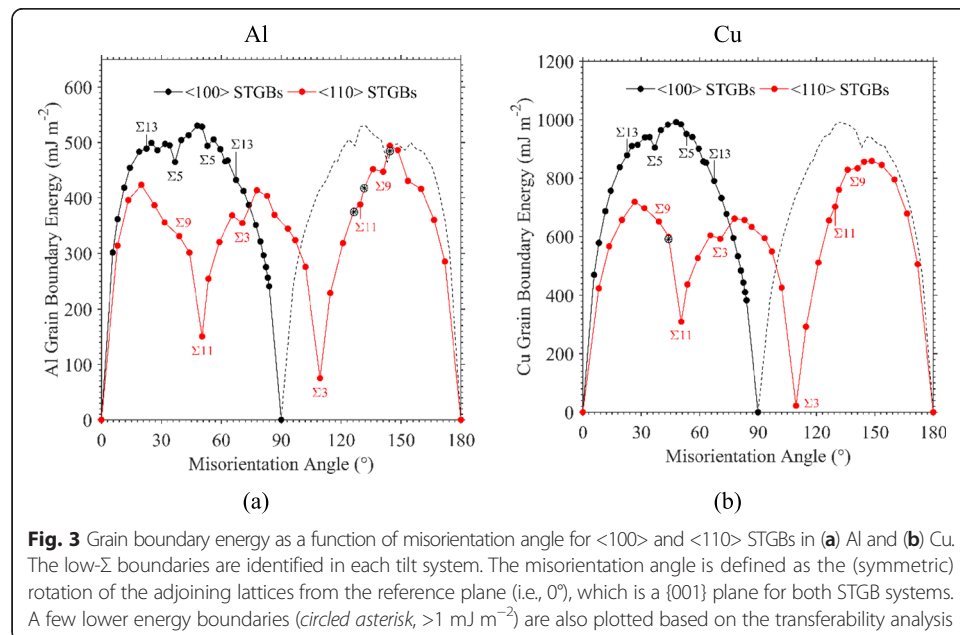
identification with the corresponding ATGBs. Therefore, there are 164 unique tilt grain boundaries in this dataset, with a fine sampling of low CSL ATGBs in the  $\langle 100 \rangle$  and  $\langle 110 \rangle$  tilt systems.

Figures 3 and 4 illustrate the grain boundary energies in different systems as a function of misorientation (inclination) angle for STGBs (ATGBs) in Al and Cu. Figure 3 follows the well-known grain boundary energy curves in  $\langle 100 \rangle$  and  $\langle 110 \rangle$  STGBs, where major energy cusps are the  $\Sigma 3\{111\}$  (i.e., coherent twin) and  $\Sigma 11\{113\}$  STGBs and minor cusps appear for the  $\Sigma 5\{310\}$  STGB. The low- $\Sigma$  boundaries ( $\Sigma \leq 13$ ) are identified, and there are two STGBs for each  $\Sigma$  value, i.e., the  $\Sigma 3\{111\}\theta = 109.47^\circ$  and the  $\Sigma 3\{112\}\theta = 70.53^\circ$  boundaries in the  $\langle 110 \rangle$  STGB system.

For each of these low- $\Sigma$  STGBs, the grain boundary plane can be rotated about the tilt direction to break the crystal symmetry and create an ATGB in that  $\Sigma$  system<sup>4</sup>. This rotation is termed the inclination angle. Figure 4 shows the change in grain boundary energy for low- $\Sigma$  systems in the  $\langle 100 \rangle$  and  $\langle 110 \rangle$  tilt systems as a function of inclination angle for Cu and Al. At  $90^\circ$  in ATGBs with a  $\langle 110 \rangle$  tilt axis (and  $45^\circ$  for  $\langle 100 \rangle$  tilt axis), the grain boundary reaches the other STGB in that  $\Sigma$  system. The dataset includes all STGBs and ATGBs in Figs. 3 and 4.

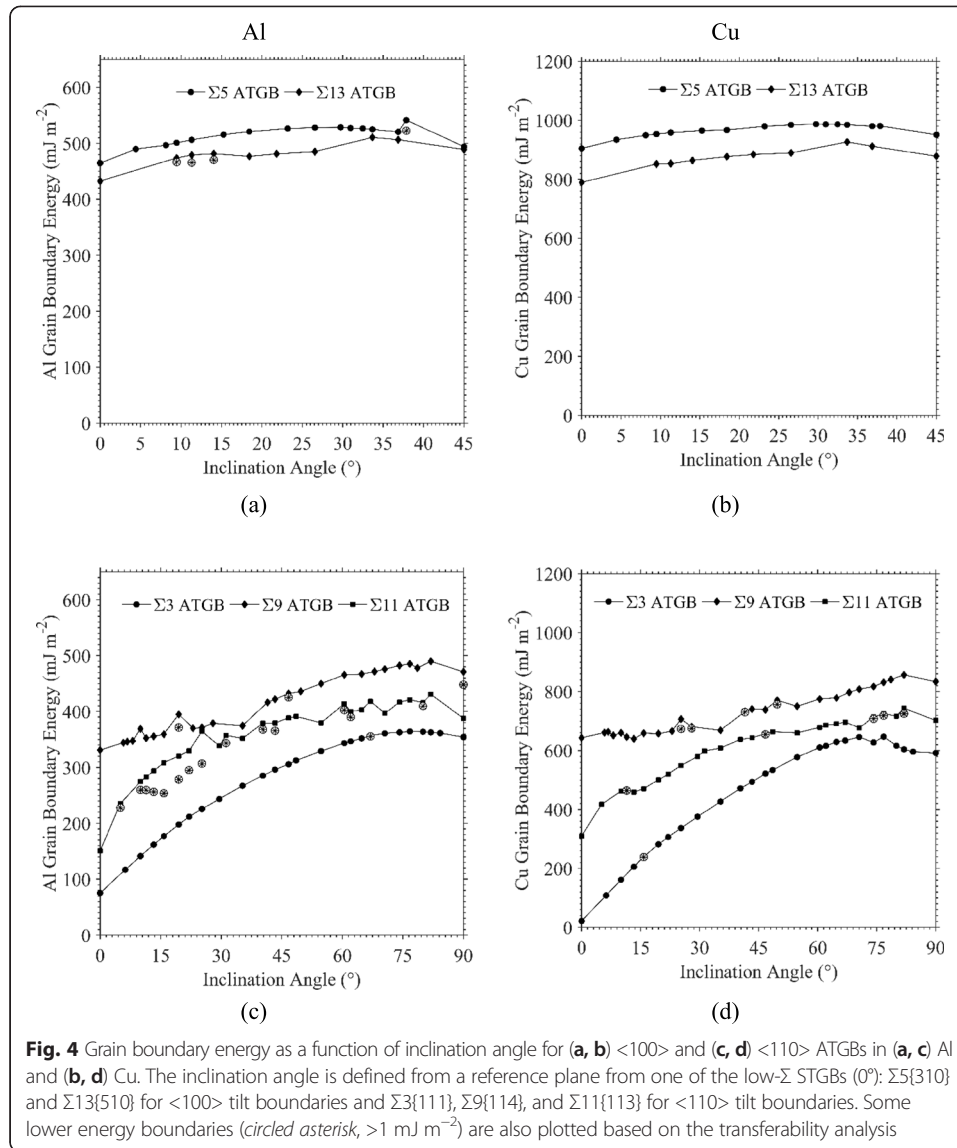
### Transferability

As a measure of transferability, the tilt grain boundaries in the dataset [27] are also tested to assess their utility in generating tilt grain boundary datasets for other fcc materials<sup>5</sup>. For example, consider transforming the Cu dataset to a new Al dataset, which can then be compared to the Al grain boundaries obtained through a large number of different starting configurations ( $>1000$ ). For each grain boundary in the Cu dataset, both the simulation cell and the atom coordinates are affinely displaced according to the ratio of the minimum energy lattice constants for the two interatomic potentials ( $a_{\text{Al}}/a_{\text{Cu}} = 4.050 \text{ \AA}/3.615 \text{ \AA} = 1.1204$ ); this correctly scales the simulation cell to ensure



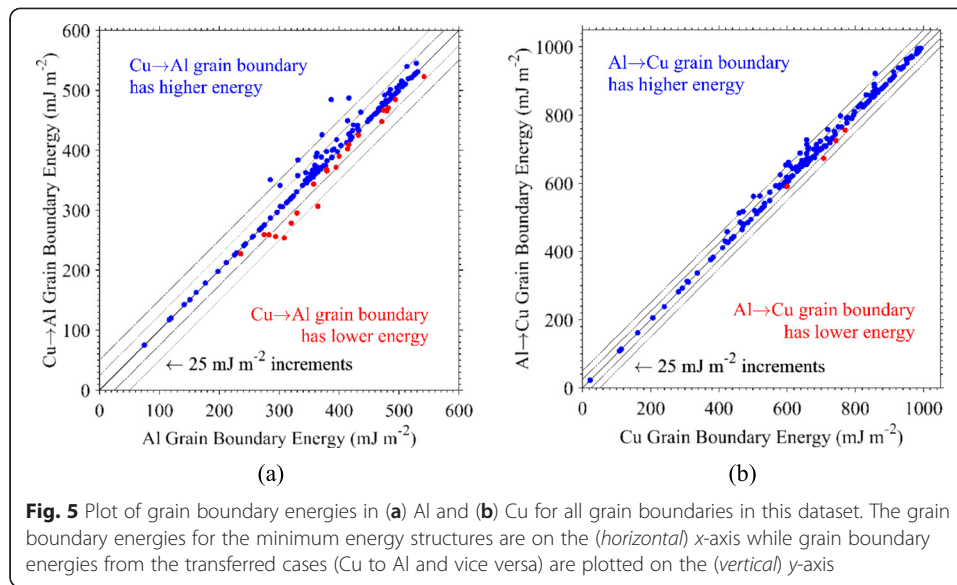
**Fig. 3** Grain boundary energy as a function of misorientation angle for  $\langle 100 \rangle$  and  $\langle 110 \rangle$  STGBs in (a) Al and (b) Cu. The low- $\Sigma$  boundaries are identified in each tilt system. The misorientation angle is defined as the (symmetric) rotation of the adjoining lattices from the reference plane (i.e.,  $0^\circ$ ), which is a  $\{001\}$  plane for both STGB systems. A few lower energy boundaries (circled asterisk,  $>1 \text{ mJ m}^{-2}$ ) are also plotted based on the transferability analysis





the correct bulk lattice constant for Al. Then, the conjugate gradient minimization routine is used to obtain the minimum energy structure at the grain boundary. This converted (Cu $\rightarrow$ Al) grain boundary dataset can then be directly compared to the energies obtained in the original Al dataset from the large number of in-plane translations and atom deletion.

The results are plotted in Fig. 5a for Al grain boundaries and in Fig. 5b for Cu grain boundaries. In general, the grain boundary energies agree well in Al ( $R^2 = 0.9868$ ) and agree even better in Cu ( $R^2 = 0.9971$ ). Figure 5 also highlights that not all grain boundaries agree in terms of energy, with some boundaries lying both above and below the  $45^\circ$  perfect correlation line. Interestingly, some of the converted grain boundaries exhibited lower grain boundary energies than the initial dataset (shown in red). This most likely stems from the fact that the in-plane translations were more coarsely sampled as the in-plane periodic distances increased, i.e., the more complex boundaries (higher  $\Sigma$  value resulting in larger grain boundary area) tended to have this issue. Hence, the



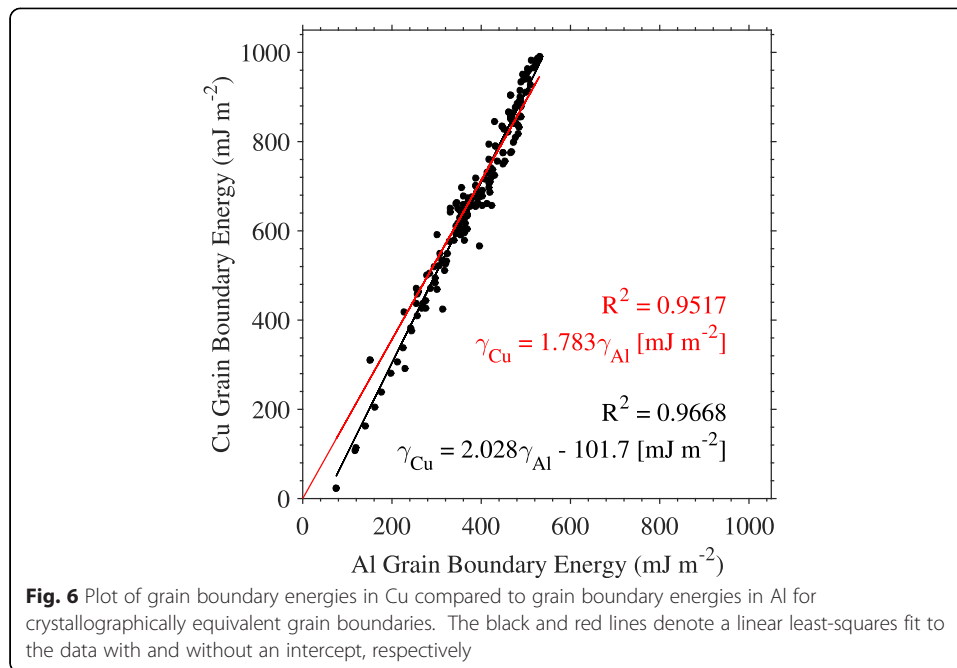
initial dataset includes data files for the lower energy grain boundary structures (in red) along with the original grain boundary structures. This results in an even greater agreement for Al and Cu ( $R^2 = 0.9918$  and  $R^2 = 0.9974$ , respectively), indicating that these datasets can be adequate predictors for minimum energy structures (and energies) in other fcc systems.

Several converted grain boundary energies, shown in Fig. 5, are substantially higher than those from the original dataset (by as much as 25 %). Because Cu has a much lower SFE than Al, the grain boundary structures are not expected to directly match when scaled by the lattice constant, i.e., partial dislocations in low-SFE materials will dissociate much more readily than in high-SFE materials, which tend to form more compact full dislocations. Hence, variation in grain boundary energy between the two fcc materials when transferred to a new system is perhaps expected.

Once one grain boundary dataset is transferred to a new system, other relationships between different fcc materials can be examined using the same structure. For instance, the grain boundary energies can be compared for two materials, as shown in Fig. 6. In the analysis that follows, the grain boundary energies in Cu are 1.78–2.03 times those in Al, depending on whether or not an intercept is applied to the linear model. It is hypothesized that the intercept value is a consequence of a large number of  $\Sigma 3$  ATGBs at the lower end of the energy distribution and is related to the SFE, i.e., the  $\Sigma 3$  coherent twin has a lower energy in Cu than in Al (22 versus 75  $\text{mJ m}^{-2}$ , respectively). Indeed, other studies have explored understanding the relationship between grain boundary energies using the ratio of a number of different element properties [53], including stable SFE, the  $C_{44}$  elastic constant, and the Voigt average shear modulus  $\mu$ .

#### Potential applications of this dataset

The present dataset [27] can be applied in various ways. First, it can serve as a reference set of tilt grain boundaries for exploring grain boundary properties as a function of grain boundary character. For example, this grain boundary set was first applied to the problem of dislocation nucleation in symmetric and asymmetric tilt grain boundaries



[32, 33, 35], of which an example input script is included<sup>6</sup>, but could easily be extended to any number of nanomechanical or materials science studies, atomistic or continuum in nature, including but not limited to the following:

1. Dislocation nucleation in unexplored asymmetric tilt grain boundary systems ( $\Sigma 5$ ,  $\Sigma 9$ ,  $\Sigma 11$ ,  $\Sigma 13$ ), similar to the previous study on  $\Sigma 3$  boundaries [33]
2. Grain boundary shear, shuffling, and sliding [7–10, 54–58] or dislocation interactions [11–13, 59–61]
3. Grain boundary mobility [25, 26]
4. Connecting grain boundary degrees of freedom or structure with energy [31, 62] and connecting grain boundary structure to experiments [63–65]
5. New techniques for examining grain boundary structure [66–69]
6. Fracture, fracture mechanisms [14, 15], and spall in grain boundaries [17–20]
7. Grain boundary structural mechanisms, including dissociation and faceting [70]
8. Interaction, diffusion, and precipitation of solutes [21, 22] and impurities [71, 72]
9. Interactions and diffusion of point defects [73–76]

Second, this dataset can serve as a starting point for exploring grain boundaries in other fcc systems (i.e., transferability). This transferability to minimum energy structures in other fcc systems can allow for exploring properties in other fcc systems based on a standard grain boundary representation as a starting point.

Third, this dataset can serve as a starting point for modification to explore metastable grain boundary states or even to obtain lower energy boundaries, if the global minimum energy boundary was not attained. For instance, by removing atoms at the boundary, different metastable (higher energy) or perhaps even lower boundaries could be obtained to understand how sensitive the grain boundary properties of a single grain boundary are to changes in grain boundary structure and energy, e.g., for examining

inelastic deformation in metastable boundaries [77] or the potential multiplicity of grain boundary structures [78, 79]. This includes the incorporation of additional elements as solutes or segregants.

Last, the structures and energies within this dataset can be used as reference data to compare results of more efficient computational techniques for obtaining minimum energy structures in fcc systems. As researchers explore methods to probe grain boundary DOE, more efficient techniques are required to efficiently probe this space. The dataset here utilized a brute force method with translations and atom deletion criteria; certainly, there are likely more efficient but perhaps more approximate methods to obtain minimum energy structures at a fraction of the computational cost.

### Availability and Requirements of Software Used

The 15 May 2015 version of the classical molecular dynamics code LAMMPS [40] was used in the following work. LAMMPS is distributed as an open source code under the terms of the GPL. LAMMPS is distributed by Sandia National Laboratories, a US Department of Energy laboratory, at <http://lammps.sandia.gov/>. All input scripts and data-files associated with the dataset are tested on the aforementioned version of LAMMPS.

### Availability of Supporting Data

The dataset is openly distributed through the NIST Material Measurement Laboratory data repository server at <https://materialsdata.nist.gov/>. Within this repository, the dataset [27] supporting the results of this article is available in the NIST Computational File Repository, Atomistic Simulations, at <http://hdl.handle.net/11256/358>.

### Endnotes

<sup>1</sup>In the directory “Grain Boundary Generation” of the dataset [27].

<sup>2</sup>Some of the 9R structures were computed with a larger spacing between the two grain boundaries and are included in the directory “lammps15May2015\_Cu\_9R” of the dataset [27].

<sup>3</sup>In the directories “lammps15May2015\_Al” and “lammps15May2015\_Cu” of the dataset [27].

<sup>4</sup>Since only the grain boundary plane is rotated, the rotation matrix describing the misorientation between the two crystal lattices does not change; hence, the  $\Sigma$  value is the same for these ATGBs.

<sup>5</sup>The LAMMPS input script for this transferability is included in the Al and Cu grain boundary directories in the dataset [27].

<sup>6</sup>In the directory “Grain Boundary Property” of the dataset *k*, which can be modified for different properties.

### Competing Interests

The authors declare that they have no competing interests.

### Authors' contributions

MT, SC, and DM conceived the idea for the manuscript, compiled the dataset, and wrote/edited the manuscript. All authors read and approved the final manuscript.

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