

ICS904/CD2IC : Cell Design For Digital Integrated Circuits

L2 : Structural design of digital circuits
(1/2))

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Outline

Introduction

MOS complementary logic (CMOS)

Pass Transistor Logic



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Integrated logic

- How to build logic functions with electronic components ?
- Many possible implementations ...
 - derived from the manipulation of logical expressions.
 - derived from component properties (MOS transistors, bipolar ...)
- Arbitrary choice of a physical variable to represent the logic states
- Many paths explored in the years 70-90
- Major classes of solutions stabilized since.
- But research still continues ...

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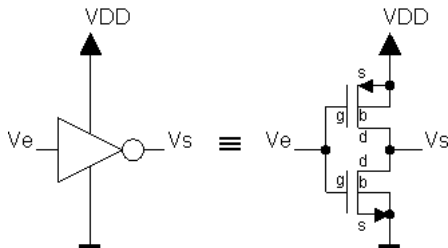
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MOS complementary logic (CMOS)

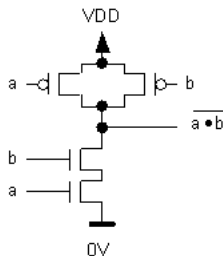
Pass Transistor Logic

CMOS inverter

- The selected supply voltage is the reference for defining the Boolean signal
- Harnessing the symmetrical behavior of NMOS and PMOS transistors.



The 2 input NAND gate



a	b	Output
0	0	1
0	1	1
1	0	1
1	1	0

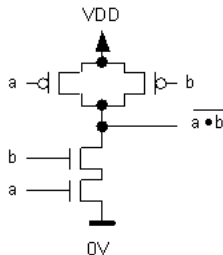
NMOS network

- ON if the two NMOS transistors are "ON"
- OFF if one of the two NMOS transistors is "OFF"

PMOS network

- ON if one of the two PMOS transistors is "ON"
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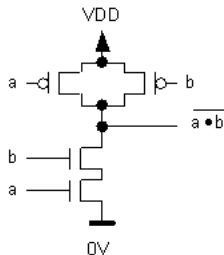
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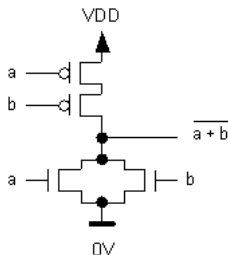
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PMOS network

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The two input NOR gate



a	b	Output
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0	1	0
1	0	0
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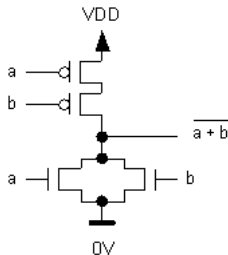
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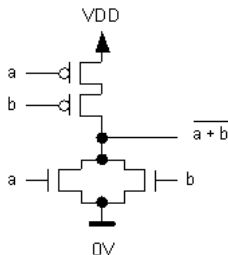
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CMOS logic

Generalization to other boolean functions

- Given the truth-table of boolean function.
- PMOS networks are used for the logic ones of the boolean function.
- NMOS networks are used for the logic zeros of the boolean function.
- A one to one NMOS/PMOS structure
- Implementable gates have a function of the form
$$F(x_0, x_1, \dots, x_n) = \sum \prod \overline{x_i}$$
- Other boolean functions are assemblies of these primitive gates.

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Construction methods for functions of the form $F = \sum \prod x_i$

■ First, build the NMOS network :

- Express the $\overline{F}(x_0, x_1, \dots, x_n)$ function in the form $\sum \prod x_i$
- Perform any factorisation/simplification.
- Remaining \prod match with series of NMOS transistors (or network of NMOS transistors).
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■ Two remarks :

- Simplest CMOS gates are inverting gates (NAND is smaller than AND)
- Dual PMOS and NMOS networks may be used :
 - Use parallel PMOS network when series of NMOS networks are used
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- This latter method often leads to a non optimal gate (from electrical point of view)

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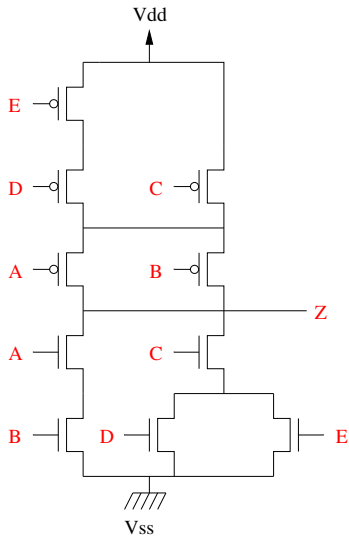
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$$Z = \overline{A \cdot B + C \cdot (D + E)}$$



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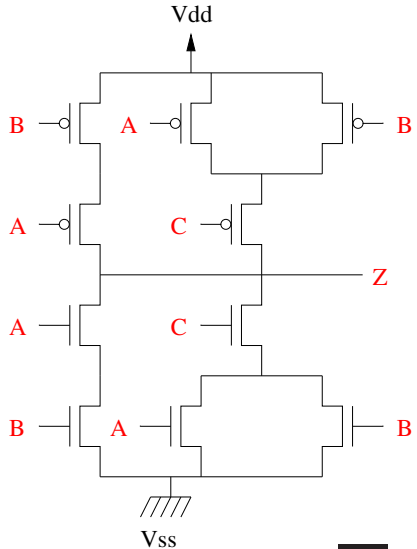
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- **Q1** : Build the gate using optimum optimisation methods
- **Q2** : Exchange "C" NMOS transistor with "A/B" NMOS network : Does it make any difference ?
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- **Q4** : What are the potentials flaws of this later gate ?

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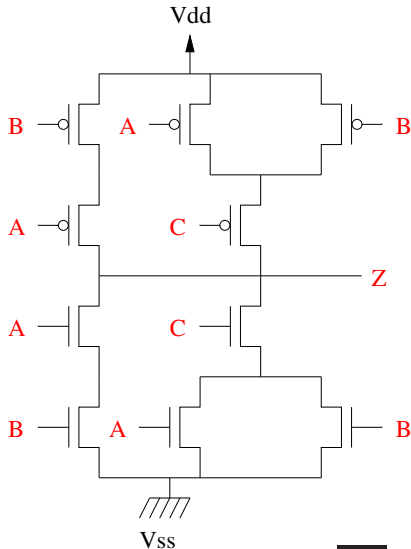
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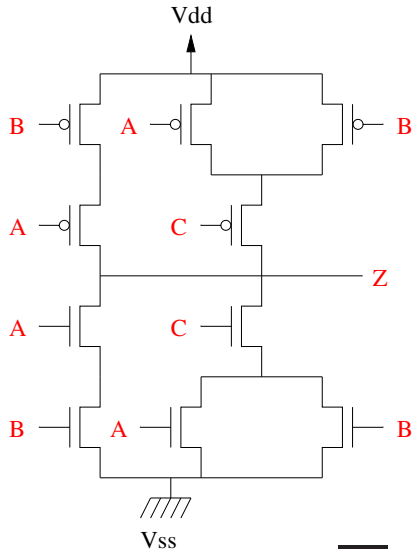
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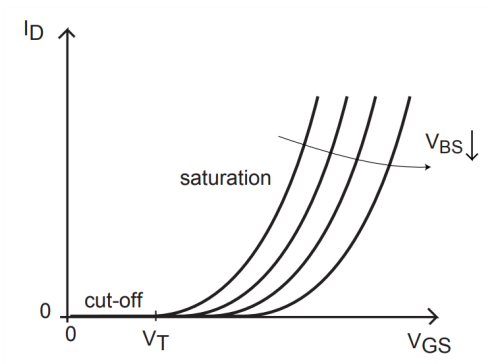
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Low/High input counts

- Series of transistors : the body effect (see lecture L1) leads to slow high V_t transistors.

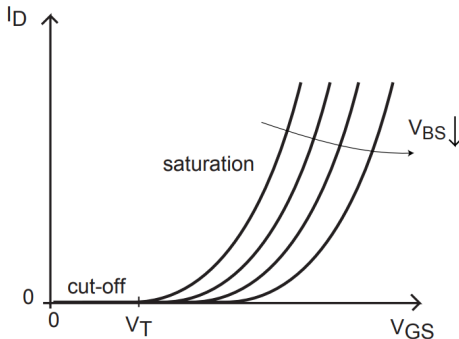


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Low/High input counts : The NAND6 example

- AND6 gate example, 28nm process, 1v supply voltage, all NMOS transistors of equal size, $w_p/w_n = 1.6$, no output load.
- Test cases : (1) All inputs change, (2) One input changes.

■ NAND6+INV

■ $Tp1R = 53ps$

■ $Tp1F = 18ps$

■ $Tp2R = 33ps$

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■ NAND3+NOR2

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non complementary PMOS/NMOS networks

- NMOS and PMOS networks may be simultaneously OFF.
- Usage : Input/Output trceivers for external busses.
- Tristate invertor.

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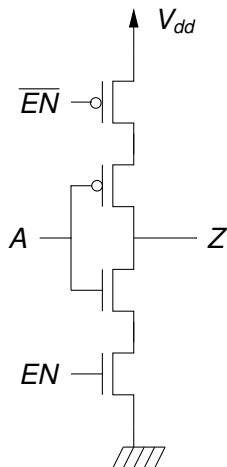
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- Only for full custom design (not included in automated methods)

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0	1	forbidden case
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CMOS logic

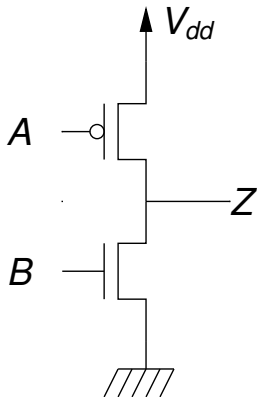
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- Only one boolean function but two transistor networks ...
- Truth table of the boolean function :
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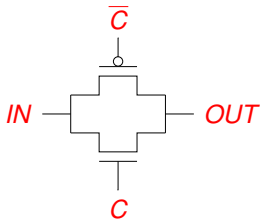
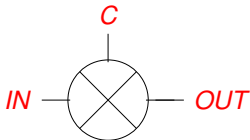
Introduction

MOS complementary logic (CMOS)

Pass Transistor Logic

Pass Transistor Logic

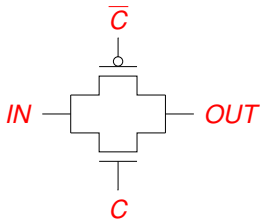
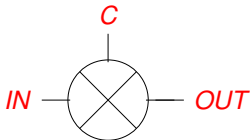
An ideal switch



- NMOS transistor efficient for falling transitions.
- PMOS transistor efficient for rising transitions.
- Warning : Passive circuit, no signal regeneration along the path "IN" to "OUT"

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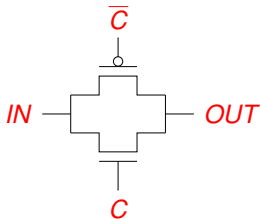
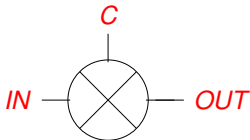
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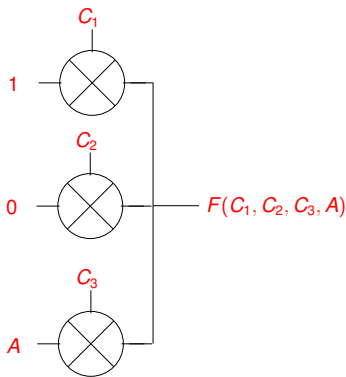
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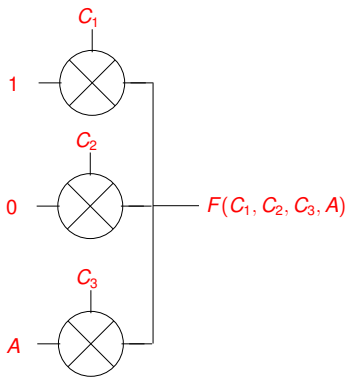
Input signals may be constants or variables



- Input is a constant : CMOS logic
- Input is a variable : Pass logic
- Combination of conditions and inputs should not lead to short-circuits.
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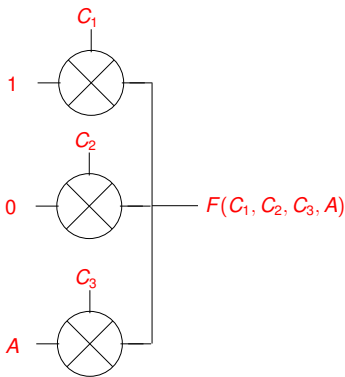
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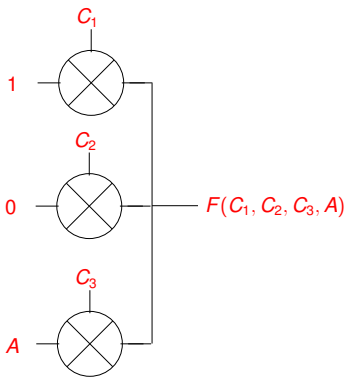
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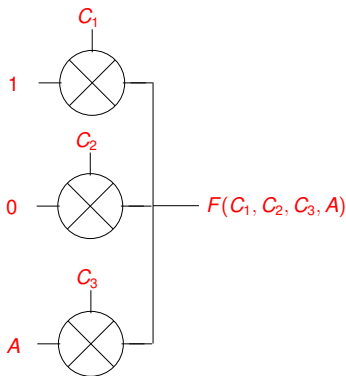
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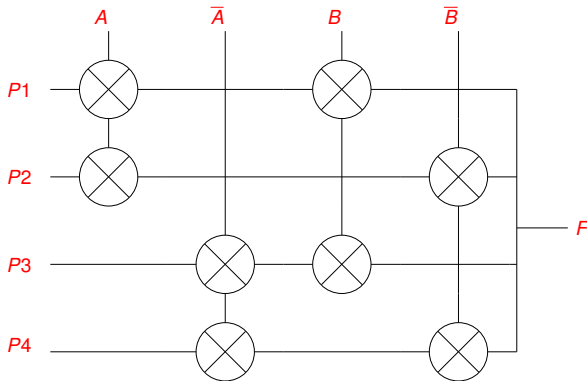
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Pass Transistor Logic

Full decoding

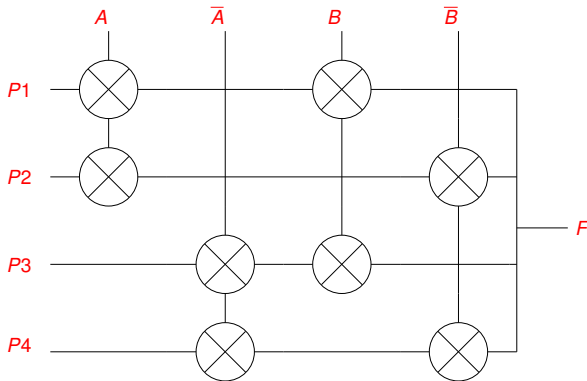


■
$$F = P_1 \cdot A \cdot B + P_2 \cdot A \cdot \bar{B} + P_3 \cdot \bar{A} \cdot B + P_4 \cdot \bar{A} \cdot \bar{B}$$

- Division of the truth table into four sub-tables (P1,P2,P3,P4) based on the full decoding of the 2 inputs A and B.

Pass Transistor Logic

Full decoding

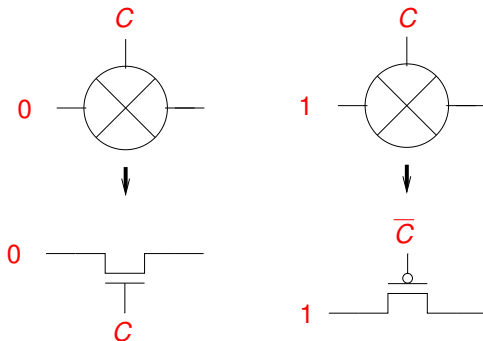


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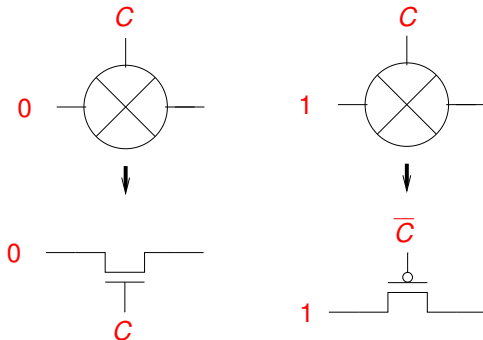
Area minimization for constant inputs



- Constant zero is a connection to V_{ss}
- Constant one is a connection to V_{dd}
- Beware the inverted condition for the PMOS transistor

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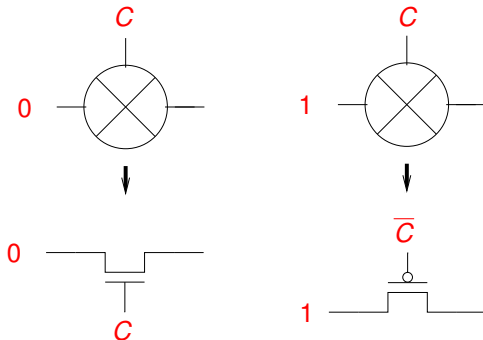
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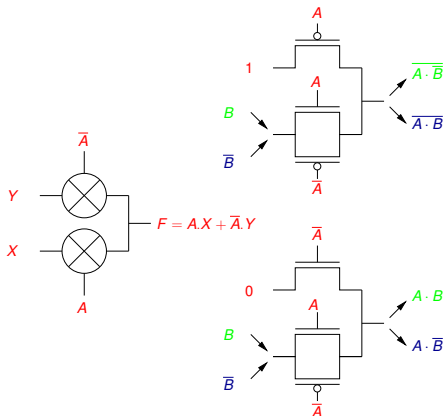
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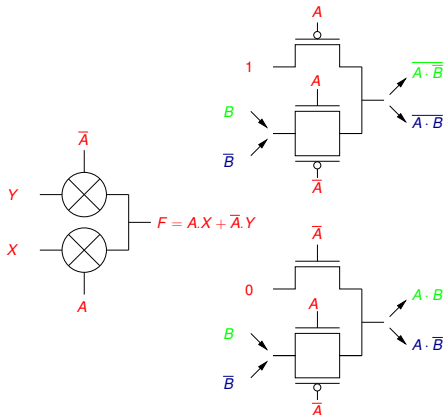
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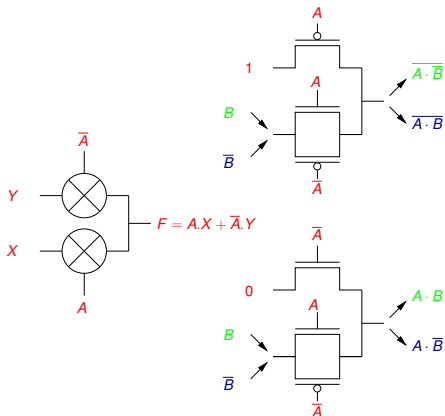
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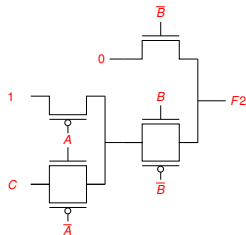
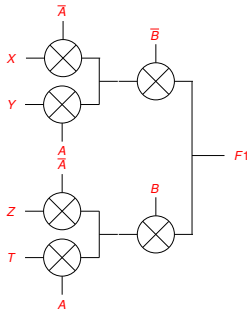
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Pass Transistor Logic

Trees of muxes



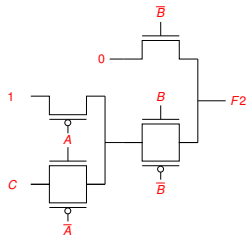
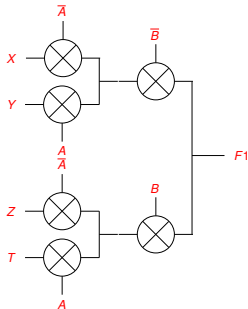
■ $F1 = \bar{B} \cdot (\bar{A} \cdot X + A \cdot Y) + B \cdot (\bar{A} \cdot Z + A \cdot T)$

■ $F2 = B \cdot A \cdot C + B \cdot \bar{A}$

- Less transistors than Pass Transistor Logic using decoders.
- But less simplifications (branch sharing)
- Heavily used for look-up tables (LUTs) in FPGAs.

Pass Transistor Logic

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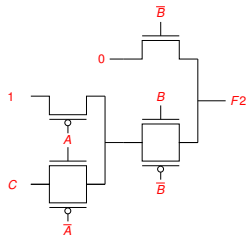
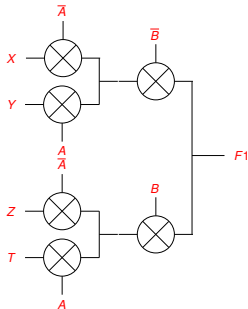
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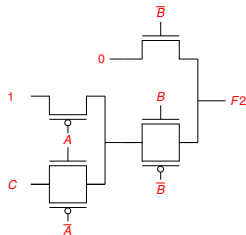
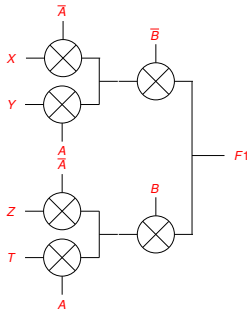
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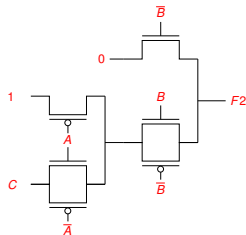
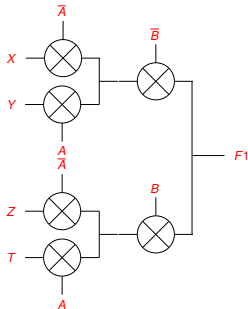
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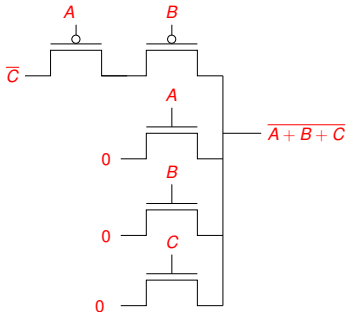
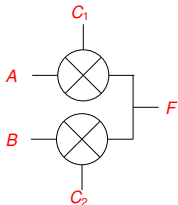
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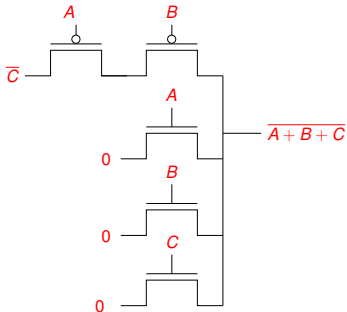
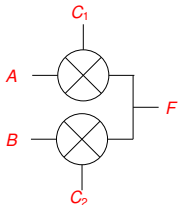
Non exclusive conditions



- Several branches may be simultaneously ON.
- Short circuits and High Impedance state should be avoided.
- $F : (C_1 = C_2) \Rightarrow A = B$

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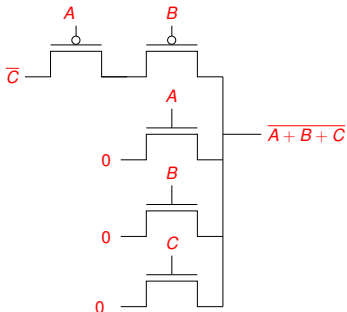
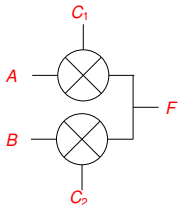
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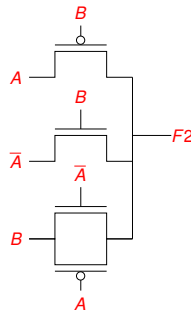
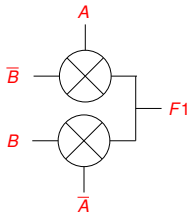
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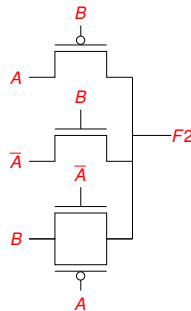
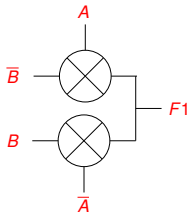
Two inputs XOR gate



- $\text{XOR} : A \cdot \bar{B} + \bar{A} \cdot B$
- F1 : Classical pass transistor logic XOR gate (8 transistors including invertors)
- F2 : Pass transistor logic XOR gate using non exclusive branches (6 transistors including invertors)

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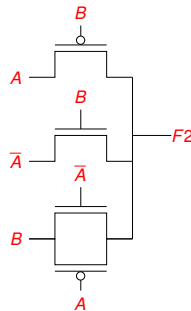
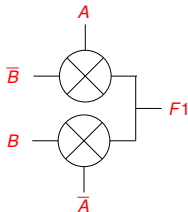
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Pass Transistor Logic

Chains of pass transistor logic / versus chain of invertors

- Passive propagation.
- RC time accumulation
- Test condition : CMOS 28nm, $V_{DD} = 1V$.
- Test case 1 : 2 invertors separated by N pass gates.
- Test case 2 : 2 invertors separated by N invertors.

N	1	2	3	4	5	6	7
Tp pass chain (ps)	7	11	17	24	32	42	53
Tp inv chain (ps)	7	12	18	23	29	35	41

- Increasing delta propagation time (cumulative RC)
- Use invertors every 2 or 3 pass gate.

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■ Q1 : Design of a 2 inputs XOR gate

- Q1.1 : How many transistors in CMOS logic.
- Q1.2 : Compare with pass transistor logic.

■ Q2 : Ripple carry adder.

- Q2.1 : Design the boolean function computing the output carry of a "Full adder" using CMOS logic.
- Q2.2 : Optimize the carry propagation of a 2N-bits ripple carry adder.
- In a full-adder, the output carry may be calculated as follows :
 - $C_{OUT} = G + P \cdot C_{IN}$
 - With G (carry generation) : $G = A \cdot B$
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 - **Q2.2** : Optimize the carry propagation of a 2N-bits ripple carry adder.
 - In a full-adder, the output carry may be calculated as follows :
 - $C_{OUT} = G + P \cdot C_{IN}$
 - With G (carry generation) : $G = A \cdot B$
 - With P (carry propagation) : $P = A \oplus B$
 - **Q2.3** : Design a boolean function computing the output carry using previous equations and pass transistor logic

Pass Transistor Logic

Summary

- Requires less transistors than CMOS logic ...
- Partially passive logic...
 - Requires buffers every 2 to 4 paths...
 - Performances of a gate alone are difficult to assess :
Performance evaluation at the assembly level...
- Gate inputs are not only transistor Gates but also transistor Drains or Sources.
 - Input capacitor depends from the state of the pass gate...
- Preferred Use :
 - Big "full-custom" digital blocs optimized for speed...
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