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Name: Gulam Rabbani Rifat

Roll: 19201041

1. In Diffuse Reflection given the value of $I_p=10$, $K_d=0.5$ and angle between the \vec{L} and \vec{n} vector is 120 degree. Find out the value of Diffuse Reflection (D). (4)

$$\begin{aligned} D &= I_p K_d \max(\cos \theta, 0) \\ &= 10 \times 0.5 \max\left(-\frac{1}{2}, 0\right) \\ &= 0 \end{aligned}$$

2. In Specular Reflection 2 vectors \vec{V} and \vec{R} is given.

$$\vec{V} = 2\hat{i} + 3\hat{j} + 5\hat{k} \text{ and } \vec{R} = \hat{i} + 2\hat{j} + \hat{k}$$

Find out the value of $\cos(\alpha)$. [Here α means the angle between the vector \vec{V} and \vec{R}] (7)

$$\vec{V} = 2\hat{i} + 3\hat{j} + 5\hat{k} \quad \vec{R} = \hat{i} + 2\hat{j} + \hat{k}$$

$$\vec{V} \cdot \vec{R} = 2 + 6 + 5 = 13$$

$$|\vec{V}| = \sqrt{2^2 + 3^2 + 5^2} = 6.16$$

$$|\vec{R}| = \sqrt{1^2 + 2^2 + 1^2} = 2.45$$

$$\begin{aligned} \cos(\alpha) &= \hat{V} \cdot \hat{R} = \frac{\vec{V} \cdot \vec{R}}{|\vec{V}| \cdot |\vec{R}|} = \frac{13}{6.16 \times 2.45} \\ &= 0.861 \end{aligned}$$

3. Write the Orthographic Projection Matrix if we project the (x,y,z) point on ZX plane where y=-5. [No Derivation required just write the matrix of 4*4 shape] (3)

3

$$\begin{bmatrix} 1 & 0 & 0 & 0 \\ 0 & 0 & 0 & -5 \\ 0 & 0 & 1 & 0 \\ 0 & 0 & 0 & 1 \end{bmatrix} \begin{bmatrix} x \\ y \\ z \\ 1 \end{bmatrix} = \begin{bmatrix} x \\ -5 \\ z \\ 1 \end{bmatrix} \quad (\text{Ans})$$

4. Suppose a Oblique Projection on xy plane where z=0. Given, $\Phi=30$ degree and $\alpha=60$ degree. Input point is A (3, 5, 7) Find out the new co-ordinate of point A after projection. [Use Oblique Projection matrix to solve the math] (6)

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$$\begin{bmatrix} 1 & 0 & \frac{\cos \Phi}{\tan \alpha} & 0 \\ 0 & 1 & \frac{\sin \Phi}{\tan \alpha} & 0 \\ 0 & 0 & 0 & 0 \\ 0 & 0 & 0 & 1 \end{bmatrix} \begin{bmatrix} 3 \\ 5 \\ 7 \\ 1 \end{bmatrix}$$

here,

$$\Phi = 30^\circ$$

$$\alpha = 60^\circ$$

$$= \begin{bmatrix} 3 + 7 \left(\frac{\cos 30}{\tan 60} \right) \\ 5 + 7 \left(\frac{\sin 30}{\tan 60} \right) \\ 0 \\ 1 \end{bmatrix} = \begin{bmatrix} 6.5 \\ 7.02 \\ 0 \\ 1 \end{bmatrix} \quad (\text{Ans})$$