



Loop parallelization issues

- Not all loops can be safely parallelized
- If there are inter-iteration dependencies, race conditions can appear
- Simple example the Fibonacci sequence:

```
for (int i = 2; i < K; i++) {
  a[i] = a[i - 1] + a[i - 2];
}</pre>
```

• This situation is an example of the data dependency: the iteration i needs data produced by previous iterations (i - 1) and (i - 2)



Dependencies in loops

1. Data dependency:

- Current iteration needs data produced by the previous iterations
- Also knows as RAW Read After Write
- Example:

```
a[i] = a[i - 2] * a[i - 1];
```



Dependencies in loops

2. Anti-dependency:

- Current iteration must use data before it is updated by the next iterations
- Also known as WAR Write After Read
- Example:

```
a[i] = a[i + 1] + a[i + 2];
```



Dependencies in loops

3. Output dependency:

- Different iterations write to the same addresses
- Also known as WAW Write After Write
- Example:

```
a[i] = 2 * a[i + 1];

a[i + 2] = 3 * a[i];
```

- Iteration 0: update a [0] and a [2]
- Iteration 1: update a [1] and a [3]
- Iteration 2: update a [2] and a [4], etc.



Dealing with dependencies

- Loops should not be parallelized if the program logic contains dependencies
- Loops with output dependency or anti-dependency are inherently sequential
- Loops with data dependency have race conditions that could be fixed with locks:
 - But in this case, the loop likely becomes sequential
 - The execution time will become slower than sequential due to locking overhead



Justifying the sample size (reminder)

The necessary sample size for a random variable with a normal distribution:

$$n_p = \left\lceil \frac{u_\alpha^2 \cdot \sigma^2}{\varepsilon^2} \right\rceil$$

- α is a significance level ($\alpha = 0.05$)
- u_{α} is the value of a random variable with standard normal distribution (N:0,1), such that $\mathrm{Prob}\{-u_{\alpha} < U < u_{\alpha}\} = 1-\alpha$
- ϵ is a permissible maximum error of the estimated mean value: $\epsilon = \mu \cdot \alpha$
- μ and σ are the parameters of the normally distributed variable (expected value and standard deviation)



Inverting nested loops

Consider the nested loop:

```
for (i = 1; i < n; i++) for (i = 1; i < n; i++)
 for (j = 1; j < m; j++) #pragma parallel for
   a[i][j] = a[i - 1][j];
```

Slow parallelized version:

```
for (j = 1; j < m; j++)
 a[i][j] = a[i - 1][j];
```

Fast parallelized version:

```
#pragma parallel for
for (j = 1; j < m; j++)
  for (i = 1; i < n; i++)
    a[i][j] = a[i - 1][j];
```



Conditionally parallelized loops

The if clause syntax:

#pragma omp parallel for if (expression)

If the *expression* evaluates to true, the loop will be executed in parallel

- The if clause allows the compiler to insert code that determines at run-time whether the loop should be executed in parallel
- In some cases, the sequential execution could be more effective than the parallel version: e.g., if a loop does not have enough iterations, the time for forking and joining threads may exceed the time saved by dividing the loop iterations among threads



Justifying the parallelization

- To create an effective parallel code, the preliminary study of the program execution time may be needed
- The list of the input factors that may affect the execution time should be identified
- The plan of a full-factor experiment should be prepared:
 - the plan consists of the experiment series
 - the execution time for the unique combination of the input factors is studied in each series
 - in series, the studied function should be launched multiple times to guarantee the statistically significant results of measurements
- Based on the experiment results, the condition expression for the if clause is defined



Scheduling loops

- In some loops, the execution time for different iterations may vary considerably
- In such cases, the maximum possible speedup cannot be achieved by dividing the iterations among threads evenly: some threads will complete the job earlier and remain idle
- To avoid these situations, the schedule clause is used to specify how the iterations of a loop should be allocated to threads:

#pragma omp parallel for schedule(type[, chunk])

- type is one of static, dynamic, guided, or runtime
- chunk is the number of iterations assigned to a thread



Static scheduling

- The static schedule (default type) means the allocation of approximately the same number of contiguous iterations to each thread before the loop iterations start executing
- If the chunk size is provided for static scheduling, the chunk of iterations is allocated to threads in turns
- Increasing the chunk size can reduce overhead. Reducing the chunk size can allow finer balancing of workloads
- Static schedules have low overhead but may exhibit high load imbalance



Dynamic and guided scheduling

- In a dynamic schedule, only some of iterations are allocated to threads at the beginning of the loop execution
- Threads that completed the assigned iterations may get additional work
- Dynamic schedules have higher overhead but can reduce load imbalance
- In a guided schedule, a dynamic allocation of iterations to tasks is performed using the guided self-scheduling heuristics
- Guided self-scheduling begins by allocating a large chunk size to each thread and responds to further requests for chunks by allocating chunks of decreasing size
- The size of the chunks in guided schedules decreases exponentially to a minimum size of chunk (by default chunk=1 for guided schedules)



The runtime type of scheduling

- If the runtime parameter is provided, the schedule is chosen at run-time based on the value of the environment variable OMP SCHEDULE:
 - In csh-like shells:

```
setenv OMP_SCHEDULE "static,1"
```

In bash-like shells:

```
export OMP SCHEDULE="static,1"
```



Assignment #4

- Prepare the parallelized version of the provided sequential code
- Study the execution time of the parallelized code for different combinations of input parameters (N \in [50; 300], M \in [50; 300])
- Maximize the speedup of your parallelized version (you may justify your decisions in commentaries to your code)
- The solution must satisfy the following conditions:
 - The program must not contain race conditions
 - The parallelized version must be as fast as possible (certainly faster than the sequential version)
 - The result returned by the parallelized version must be the same as for the sequential version for any combination of the input parameters N and M