Chapter one, Assignment 2

1. Compute the partial derivatives with respect to x and with respect to y for the following fuctions.

a.
$$f(x,y) = y^2 e^{3x}$$

b.
$$z = (3xy + 2x)^5$$

c.
$$q(x,y) = e^{x+3y} \sin(xy)$$

2. Let $f(x,y) = \frac{x^2}{y+1}$. Find $f_y(3,2)$ algebraically.

Find the indicated partial derivatives for the following problems. Assume the variable are restricted to a domain on which the function is defined.

3.
$$z_y$$
 if $z = \frac{3x^2y^7 - y^2}{15xy - 8}$

4.
$$z_x$$
 if $z = \frac{1}{2x^2ay} + \frac{3x^5abc}{y}$

$$5. \ \frac{\partial}{\partial \lambda} (\frac{x^2 y \lambda - 3 \lambda^5}{\sqrt{\lambda^2 - 3\lambda + 5}})$$

$$6. \ \frac{\partial}{\partial w}(\sqrt{2\pi xyw - 13x^7y^3v})$$

7.
$$\frac{\partial \alpha}{\partial \beta}$$
 if $\alpha = \frac{e^{x\beta - 3}}{2y\beta + 5}$

8.
$$\frac{\partial}{\partial w} \left(\frac{x^2 y w - x y^3 w^7}{w - 1} \right)^{\frac{-7}{2}}$$

9. Find the equation of the tangent plane at the given point for the functions below.

a.
$$z = e^y + x + x^2 + 6$$
 at the point $(1, 0, 9)$

b.
$$z = \frac{1}{2}(x^2 + 4y^2)$$
 at the point $(2, 1, 4)$.

- 10. Find the differential of $h(x,t) = e^{-3t} \sin(x+5t)$
- 11. Find the differential of $g(x,t) = x^2 \sin(2t)$ at the point $(2,\frac{\pi}{4})$

12. Find
$$\frac{\partial z}{\partial u}$$
 and $\frac{\partial z}{\partial v}$ of $z = xe^{-y} + ye^{-x}, x = u\sin v, y = v\cos u$

13. Find $\frac{dz}{dt}$ of $z = \sin(\frac{x}{y}), x = 2t, y = 1 - t^2$ using the chain rule.

Calculate all the four second-order partial derivatives of the functions below and show that $f_{xy} = f_{yx}$.

14.
$$f(x,y) = \sin(x^2 + y^2)$$

15.
$$f(x,y) = \sin(\frac{x}{y})$$