



COE/EE152: Basic Electronics

Lecture 7 Andrew Selasi Agbemenu

<https://sites.google.com/site/agbemenu/courses/ee-coe-152>



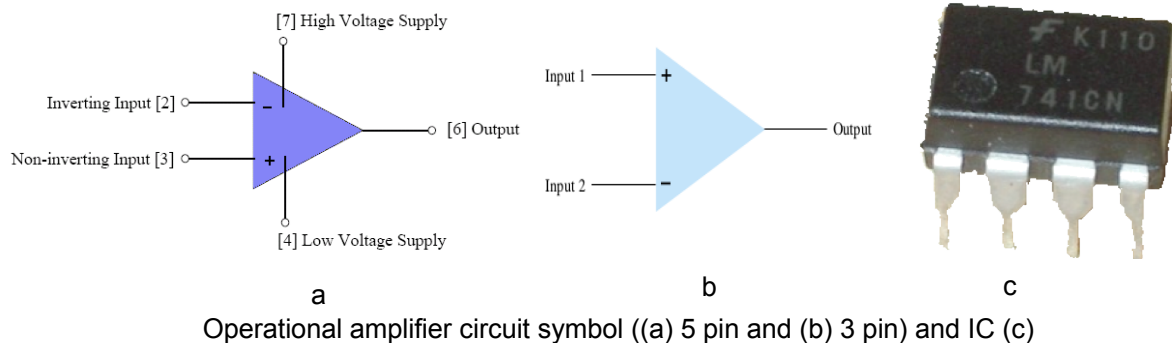
Outline

- Introduction to operational Amplifiers
- Operational Amplifiers



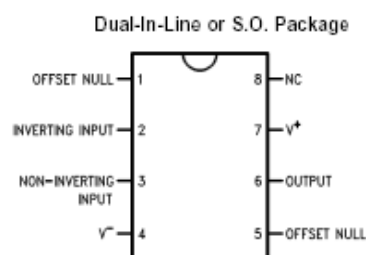
Operational Amplifiers

- Low cost integrated circuit which is able to amplify signals due to an external DC power supply
- The op-amp is a very high gain amplifier



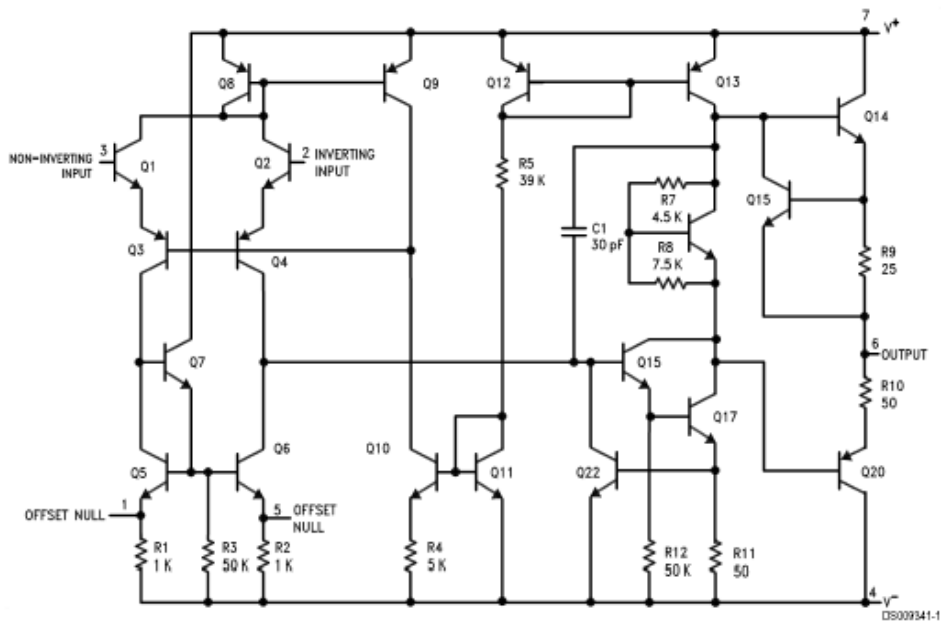
LM741

- The most popular operational amplifier IC is LM741 by National semiconductor
- The internal circuitry is shown I the next slide but beyond the scope of this course





Internal Circuitry of LM741



Properties of Op-amps

- Ideal op-amp
 - Infinite input impedance
 - Will not load any source
 - Zero output impedance
 - Will drive any load
- Real Op-amps
 - Gain $\sim 10^6$
 - Input Impedance $\sim 100 \text{ M}\Omega$
 - Output Impedance $\sim 100 \Omega$



Ideal Op-amp

Characteristics of an ideal op-amp

$R_{in} = \text{infinity}$

$R_{out} = 0$

$A_{vo} = \text{infinity}$ (A_{vo} is the open-loop gain, sometimes A or A_v of the op-amp)

Bandwidth = infinity (amplifies all frequencies equally)

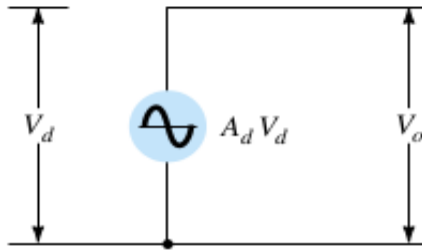


Summary of Characteristics

Parameter	Ideal Op-Amp	Typical Op-Amp
G_{OL}	∞	$10^5 - 10^9$
Common Mode Gain	0	10^{-5}
Bandwidth	∞	1-20 MHz
Input Impedance	∞	$10^6 \Omega$ (bipolar) $10^9 - 10^{12} \Omega$ (FET)
Output Impedance	0	100-1000 Ω



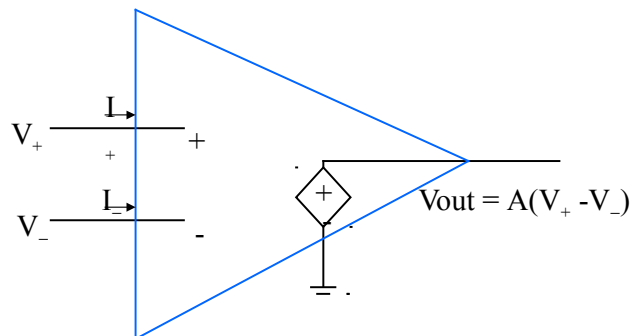
Ideal Op-amp Model



$$V_d = V_+ - V_- \quad (\text{Differential Voltage})$$
$$A_d = \text{open-loop differential mode gain} (A_v)$$
$$A_d = A = A_v = \frac{V_o}{V_d}$$

Important op-amp behaviour

$$V_+ = V_-$$
$$I_+ = I_- = 0$$



Op-amp Gain

- Op-amps have very high gain. They can be connected in **open-loop** or **closed-loop**
 - **Open-loop** refers to a configuration where there is no feedback from output to the input. The gain is usually in excess of 10,000. In this mode the slightest noise is greatly amplified
 - **Closed-loop** configuration reduces gain. The gain is controlled by *negative feedback* which improves the characteristics of the op-amp

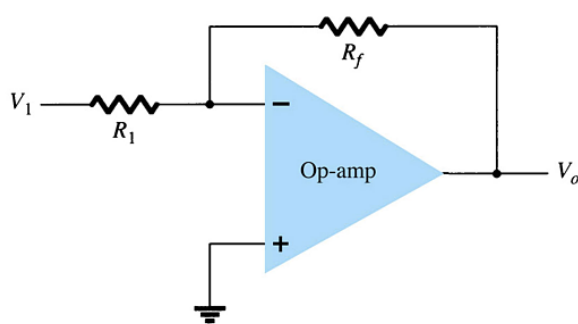


Op-Amp Applications

- Amplifier
 - Inverting Amplifier
 - The output signal is an amplified inversion of the input signal
 - Non-inverting Amplifier
 - The input signal is not inverted at the output but only amplified
 - Unity Follower (Buffer)
- Operations (Mathematical)
 - Summation
 - Difference
 - Integration
 - Differentiation
- Op-amps are also used for:
 - Filters (High, Low and Band Pass)
 - Comparator
 - A/D converters



Inverting Amplifier

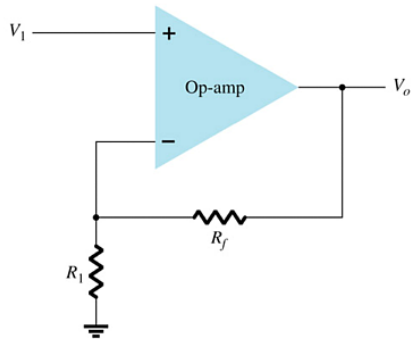


$$\begin{aligned} R_1 \text{ current} &= R_f \text{ current} \\ \frac{V_1 - V_-}{R_1} &= \frac{V_- - V_0}{R_f} \\ V_- &= V_+ = 0 \\ \frac{V_1}{R_1} &= \frac{V_0}{R_f} \\ A_v &= \frac{V_0}{V_1} = -\frac{R_f}{R_1} \end{aligned}$$

Negative sign shows 180° phase shift of input



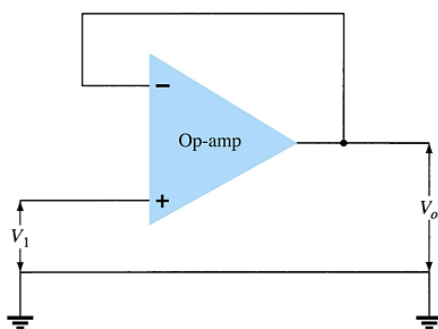
Non-inverting Amplifier



$$\begin{aligned} R_1 \text{ current} &= R_f \text{ current} \\ \frac{0 - V_-}{R_1} &= \frac{V_- - V_o}{R_f} \\ V_- &= V_+ = V_1 \\ \frac{V_1}{R_1} &= \frac{V_1 - V_o}{R_f} \\ A_V &= \frac{V_o}{V_1} = 1 + \frac{R_f}{R_1} \end{aligned}$$



Unity Follower

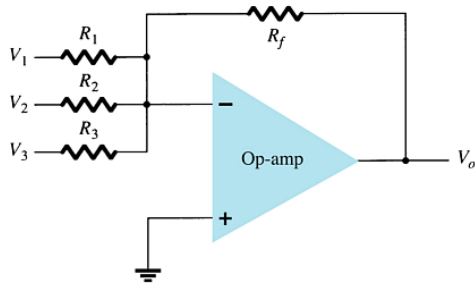


$$\begin{aligned} V_o &= V_- \\ V_- &= V_+ = V_1 \\ \Rightarrow V_o &= V_1 \end{aligned}$$

Input voltage is regenerated at the output
The gain here is unity



Summation



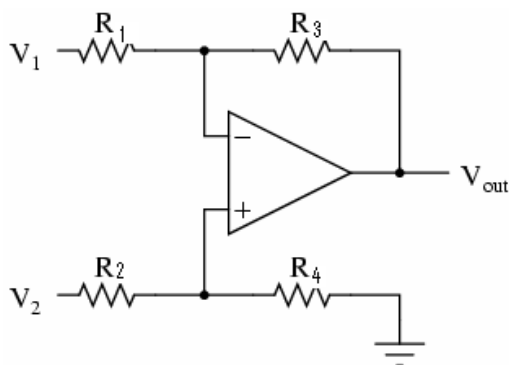
Because the op-amp has a high input impedance, the multiple inputs are treated as separate inputs.

$$\frac{V_1}{R_1} + \frac{V_2}{R_2} + \frac{V_3}{R_3} = -\frac{V_o}{R_f}$$

$$V_o = -\left(\frac{R_f}{R_1}V_1 + \frac{R_f}{R_2}V_2 + \frac{R_f}{R_3}V_3\right)$$



Difference



$$\frac{V_1 - V_-}{R_1} = \frac{V_- - V_{out}}{R_3}$$

$$\frac{V_2 - V_+}{R_2} = \frac{V_+}{R_4}$$

$$V_- = V_+$$

Solving:

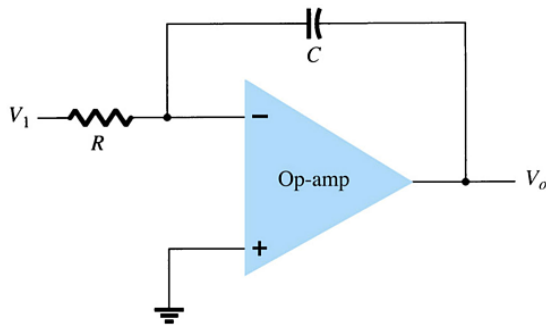
$$V_{out} = \frac{V_2(R_3 + R_1)R_4}{(R_4 + R_2)R_1} - \frac{V_1R_3}{R_1}$$

if all resistors are equal:

$$V_{out} = V_2 - V_1$$



Integration: Integrator



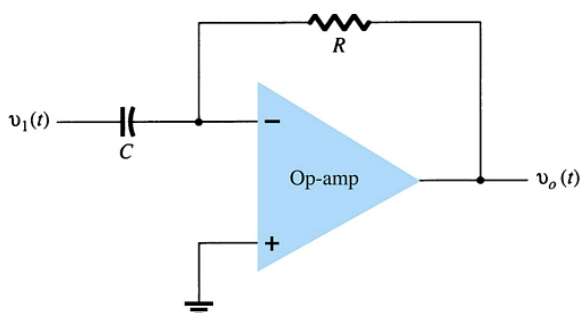
$$\begin{aligned}\frac{v_1}{R} &= -\frac{dv_0}{dt}C \\ dv_0 &= -\frac{1}{RC}v_1 \cdot dt \\ v_0 &= -\frac{1}{RC} \int v_1 \cdot dt\end{aligned}$$

The output is the integral of the input. Integration is the operation of summing the area under a waveform or curve over a period of time. This circuit is useful in low-pass filter circuits and sensor conditioning circuits.

v_0 and v_1 are functions of time



Differentiation: Differentiator



$$\begin{aligned}C \frac{dv_1}{dt} &= -\frac{v_0}{R} \\ v_0 &= -RC \frac{dv_1}{dt}\end{aligned}$$

The differentiator takes the derivative of the input. This circuit is useful in high-pass filter circuits.

v_0 and v_1 are functions of time

