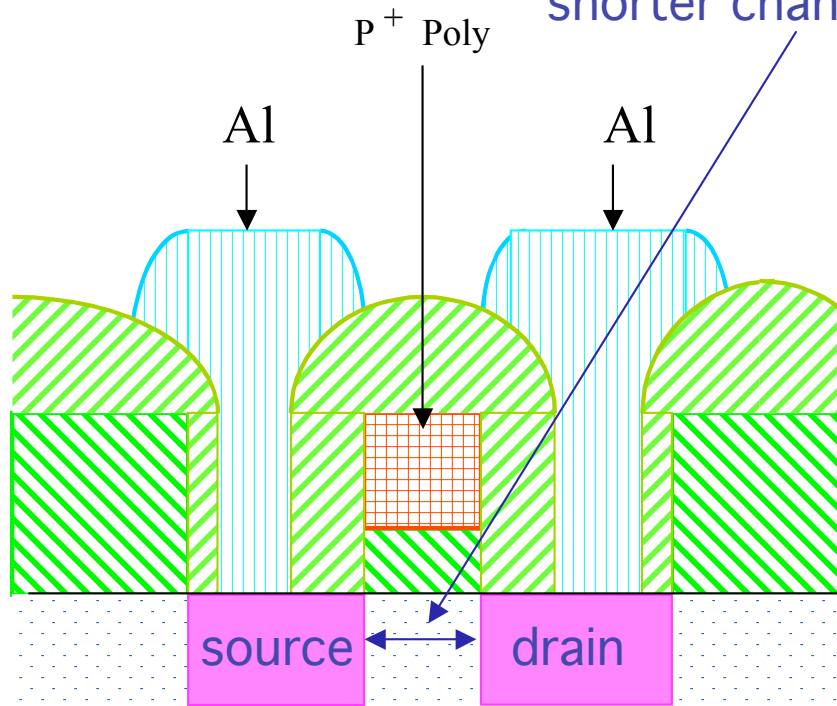


Doping and diffusion I

Motivation

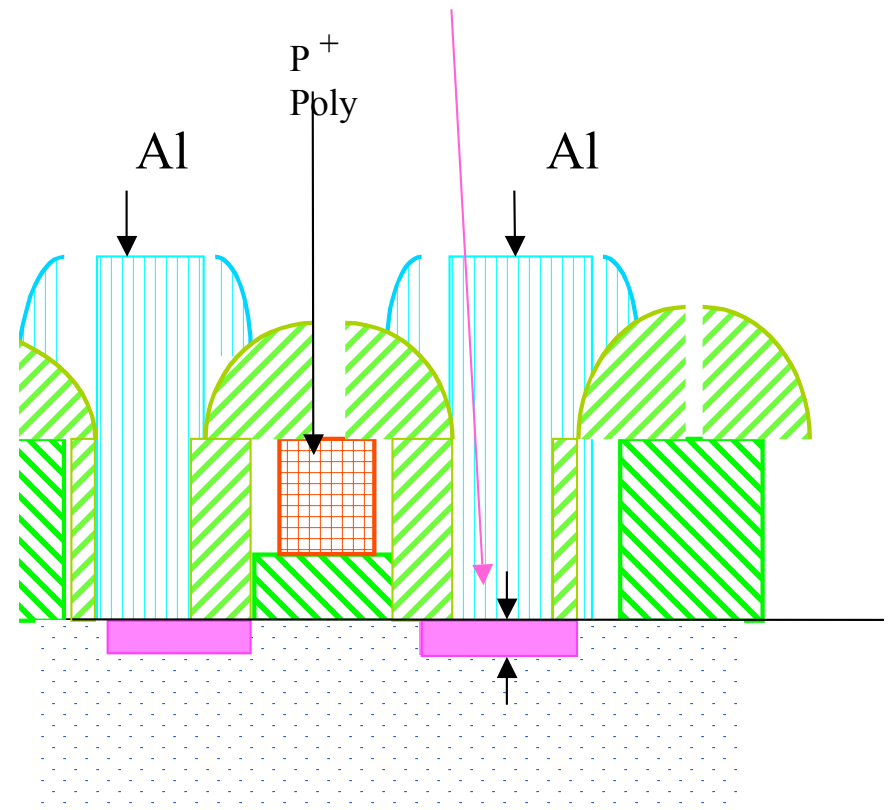
Faster MOSFET requires

shorter channel



Shorter channel but with same source, drain depth => drain field dominates gate field => "drain-induced barrier lowering" DIBL

Requires shallower source, drain

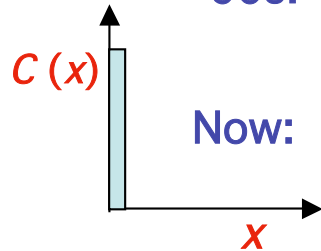


Shallower source, drain depth demands better control in doping & diffusion. CHANNEL ASPECT RATIO => ρ_s

How are shallow doped layers made?

1) Predeposition: controlled number of dopant species at surface

'60s: film or gas phase of dopant at surface



Surface concentration is limited by equilib . solubility

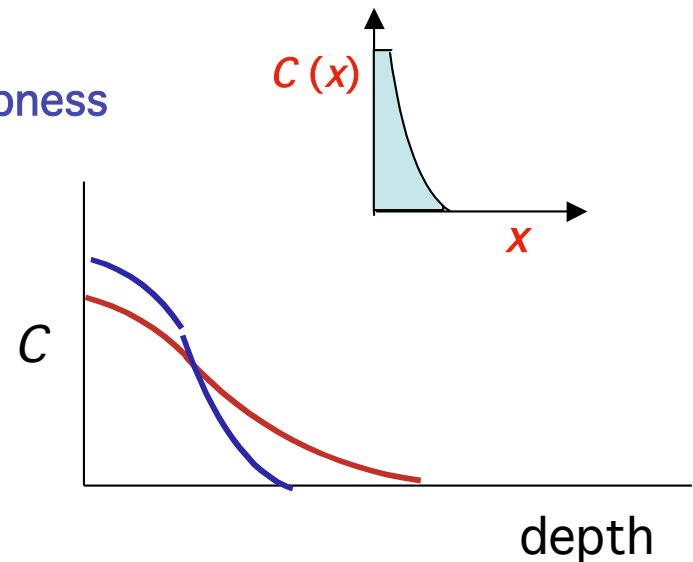
Now: Ion implant (non-equilibrium) , heat substrate to diffuse dopant

but ions damage target...requires anneal, changes doping, $C(z)$

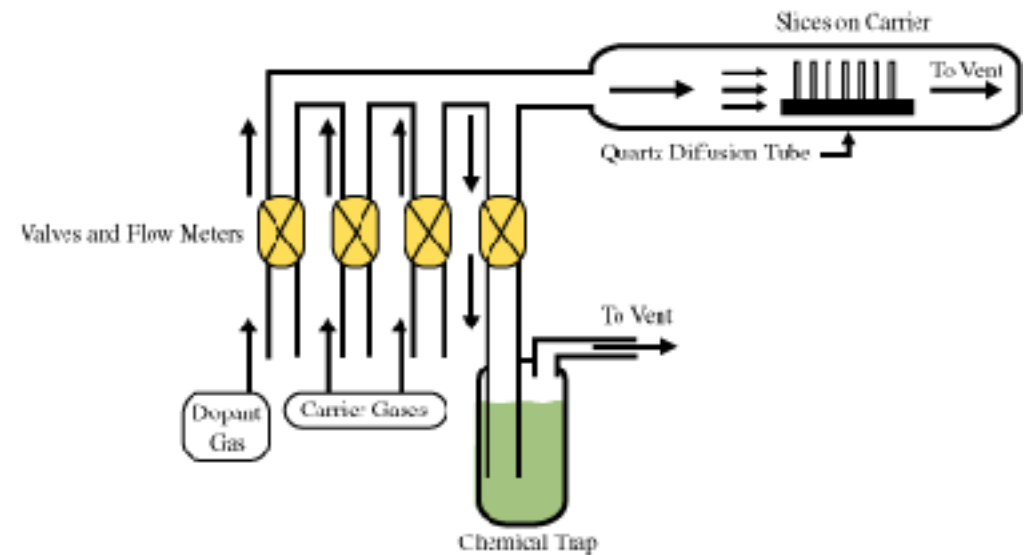
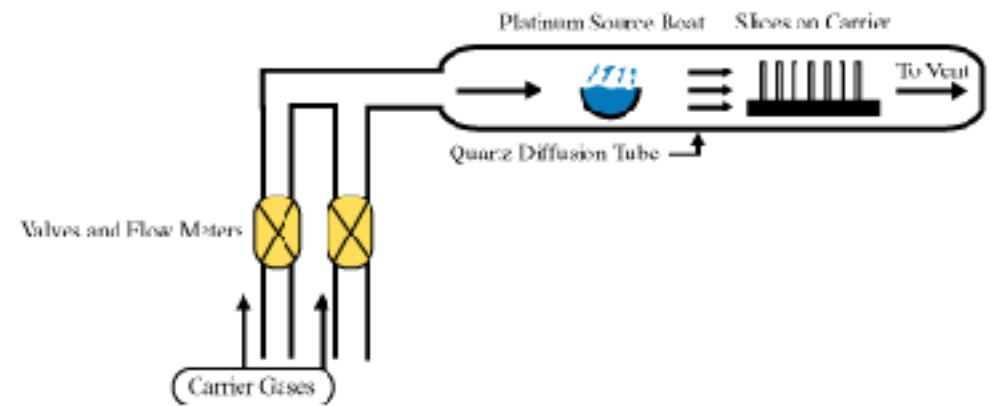
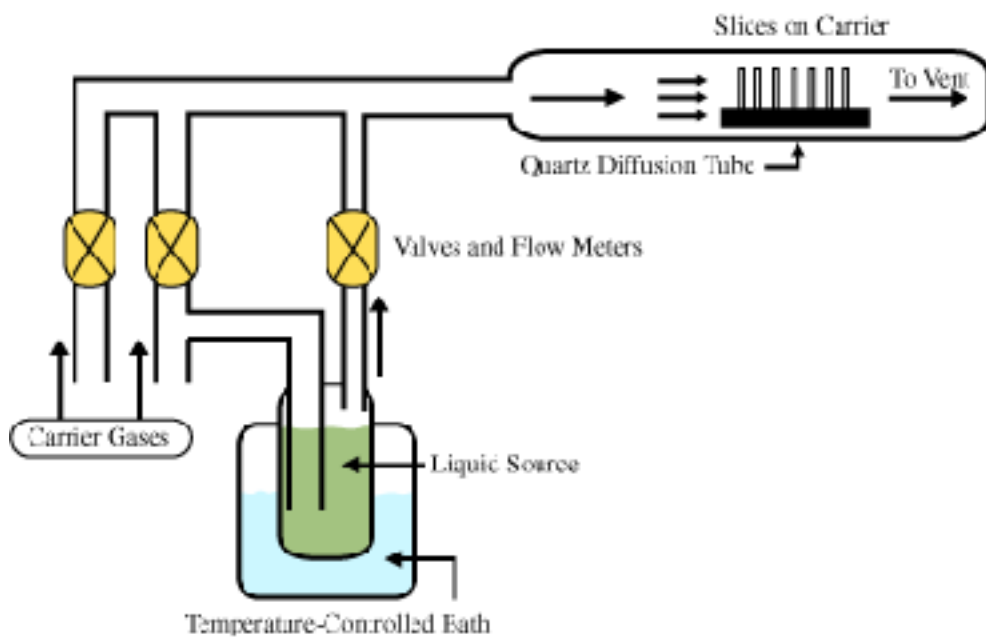
Soon: film or gas phase of dopant at surface

2) Drive-in process: heat substrate+predep, diffusion determines junction depth, sharpness

Need
sharper diffusion profiles:



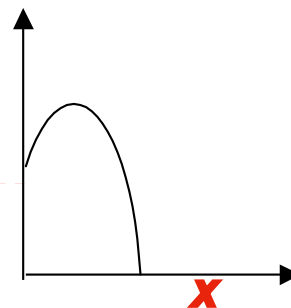
Doping and diffusion apparatus



**Later...
Ion Implantation**



6.155/ 3.155J 9/29/03



Doping, Diffusion I

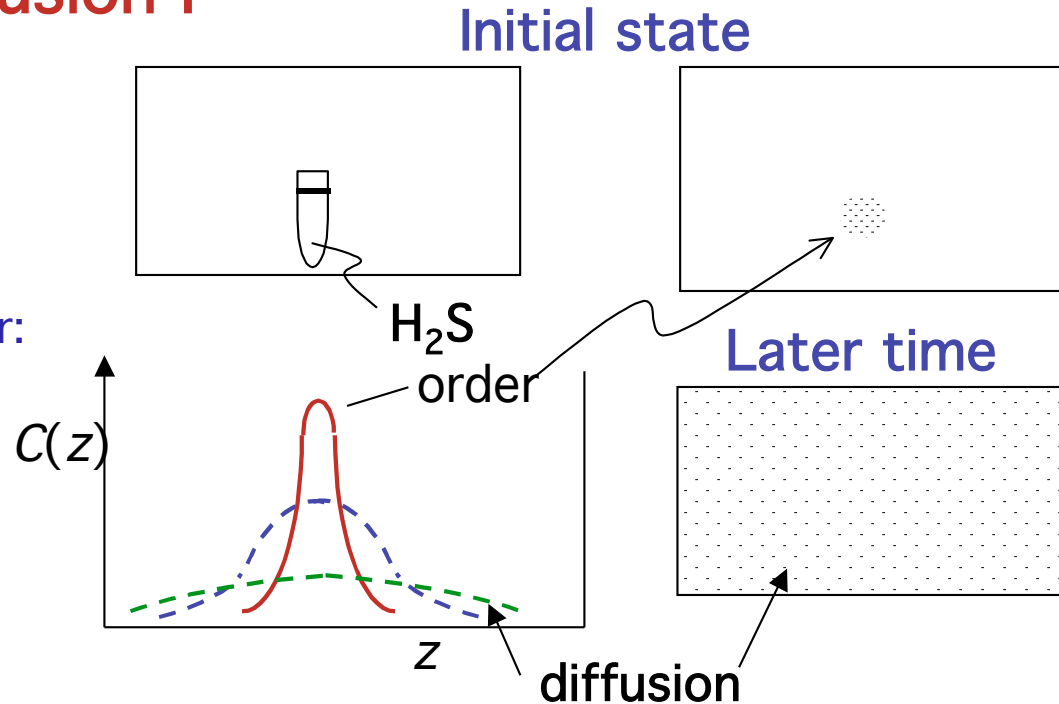
a) Gas diffusion

$$F = U - T S.$$

If no chem'l interaction with air:

$$F = - T S$$

Gas disperses, fills all possible states randomly.

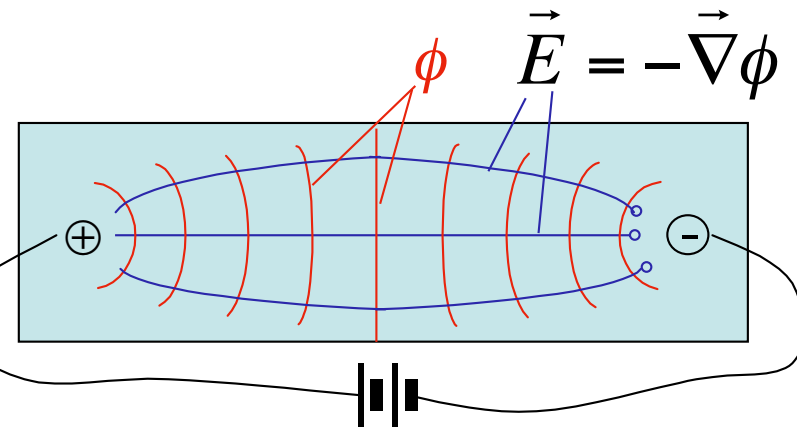


$$b) I = \frac{V}{R} \quad J = \sigma E = \sigma \left(-\frac{\partial \phi}{\partial z} \right)$$

Electric potential gradient
 \Rightarrow charge flow

Electrons drift down potential gradient:

here ϕ is imposed from outside

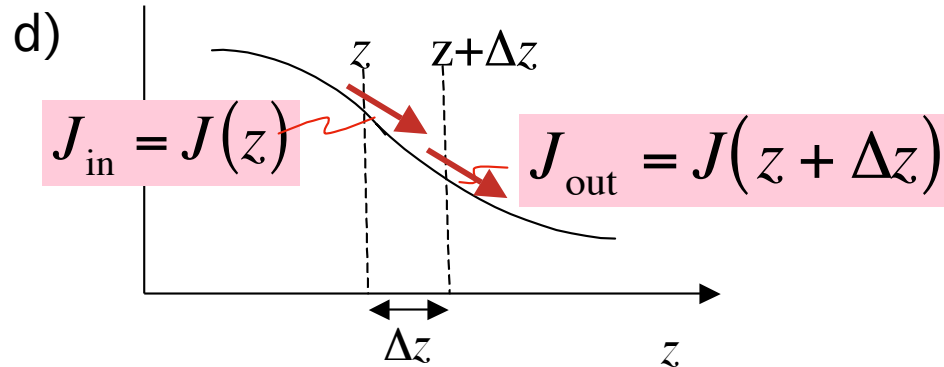
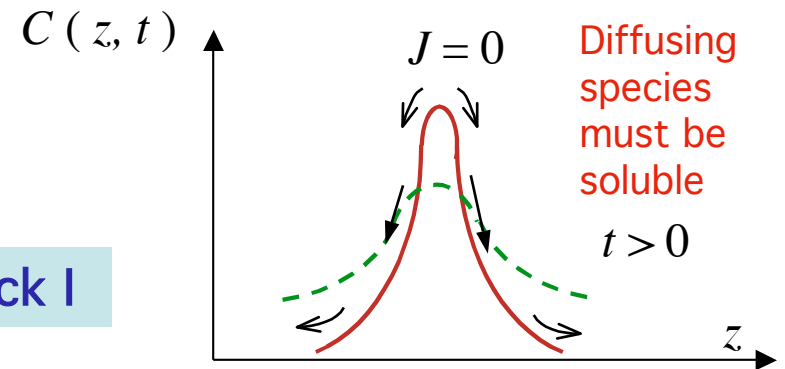


what about solids...

- c) Mass (or heat) flow J ,
due to **concentration** gradient

$$J \left(\frac{\#}{\text{area} \cdot t} \right) = D \left(- \frac{\partial C}{\partial z} \right)$$

Fick I



$$\frac{dC(z)}{dt} \Delta z = +J(z) - J(z + \Delta z) \frac{\#}{\text{area} \cdot t}$$

$$\frac{dC}{dt} = \frac{J(z) - J(z + \Delta z)}{\Delta z} \xrightarrow{\Delta z \rightarrow 0} - \frac{dJ}{dz}$$

$$\frac{dC(z)}{dt} = - \frac{d}{dz} D \left(- \frac{\partial C}{\partial z} \right)$$

Fick II

...or if D is constant

$$\frac{dC(z, t)}{dt} = D \nabla^2 C(z, t)$$

Time dep. Schrödinger Eq.

$$+i\hbar \frac{\partial \psi}{\partial t} = - \frac{\hbar^2}{2m} \nabla^2 \psi + V\psi$$

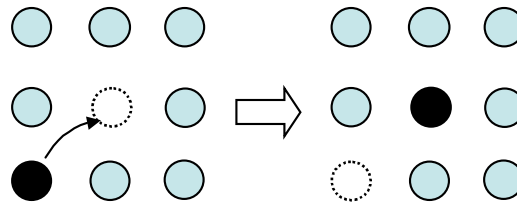
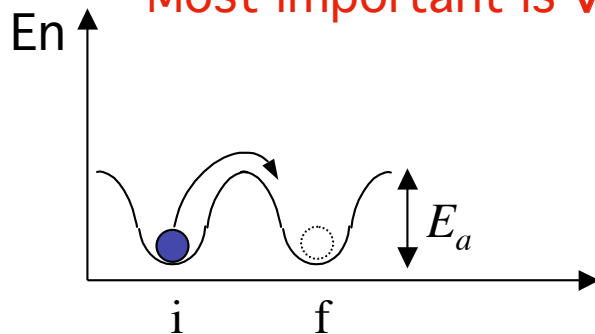
These Eqs => time evolution of some initial conditions, boundary conditions

Atomistic picture of diffusion

See web site for movies:

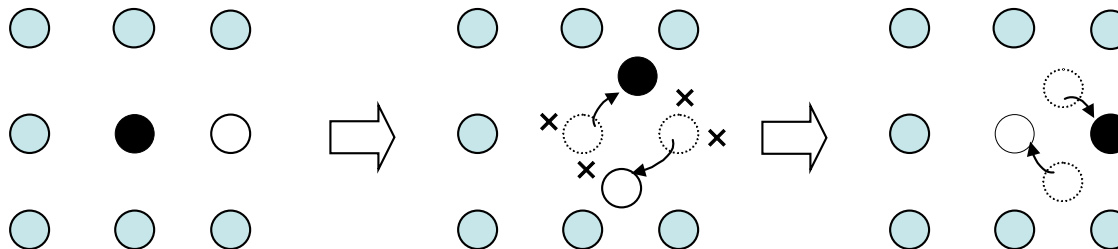
http://www.tf.uni-kiel.de/matwis/amat/def_en/index.html

Most important is vacancy diffusion.



Initial and final states have same energy

Also possible is direct exchange (x = broken bond)



Higher energy barrier or break more bonds => lower value of $D = D_0 \exp\left(-\frac{E}{kT}\right)$

Atoms that bond with Si are

substitutional impurities P, B, As, Al, Ga, Sb, Ge

Atomistic picture of diffusion

2 steps

for diffusion: 1) create vacancy

2) achieve energy E_a

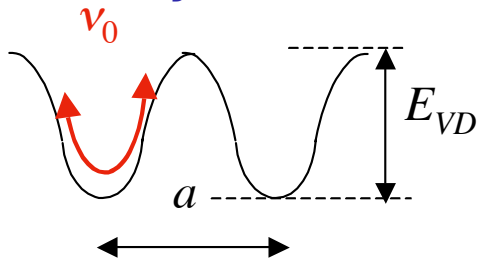
$$n_v = \frac{N_v}{N_0} = \exp\left[-\frac{2.6}{kT}\right]$$

$$\nu_v = \nu_0 \exp\left(-\frac{E_a}{kT}\right)$$

$$\left(e^{-\frac{\Delta G}{kT}} \rightarrow e^{-\frac{E_{VF} - TS}{kT}} = e^{\frac{S}{k}} e^{-\frac{E_{VF}}{kT}} \right)$$

$$D \sim a \times \nu = a^2 \nu_0 \underbrace{\exp\left[-\frac{E_v + E_a}{kT}\right]}_{\left(\frac{cm^2}{s}\right)}$$

Vacancy diffusion



$$D = D_0 \exp\left[-\frac{E_{VD}}{kT}\right]$$

Contains $\nu_0 \approx$ Debye frequency

$$\approx \frac{3}{2} \frac{k_B T}{h} = 9 \times 10^{12} s^{-1} \approx 10^{13} s^{-1}$$

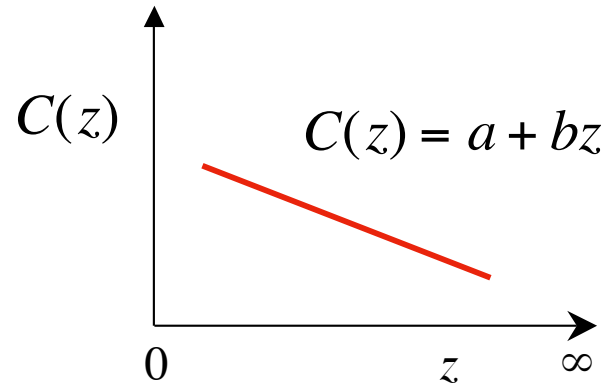
Analytic Solution to Diffusion Equations,

Fick II:

$$\frac{\partial C}{\partial t} = D \frac{\partial^2 C}{\partial z^2}$$

Steady state, $dC/dt = 0$

Conversely,
if $C(z)$ is curved,
 $dC/dt \neq 0$.



We assumed this to be the case in oxidation:

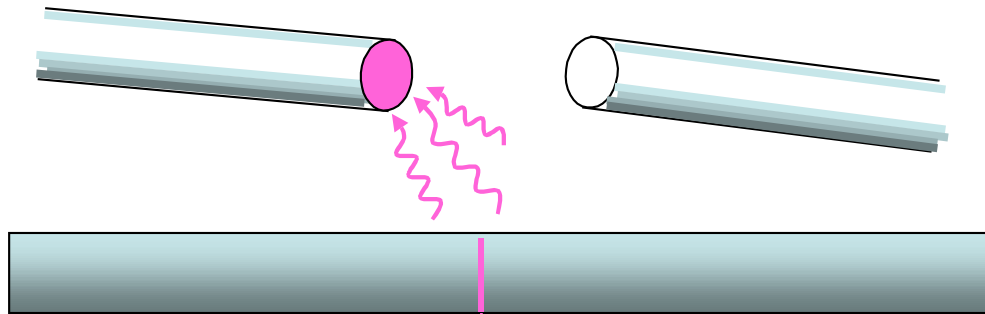
O_2 diffusion through SiO_2 , where

flux, $J = -D \frac{\partial C}{\partial z} = -Db$, is same everywhere

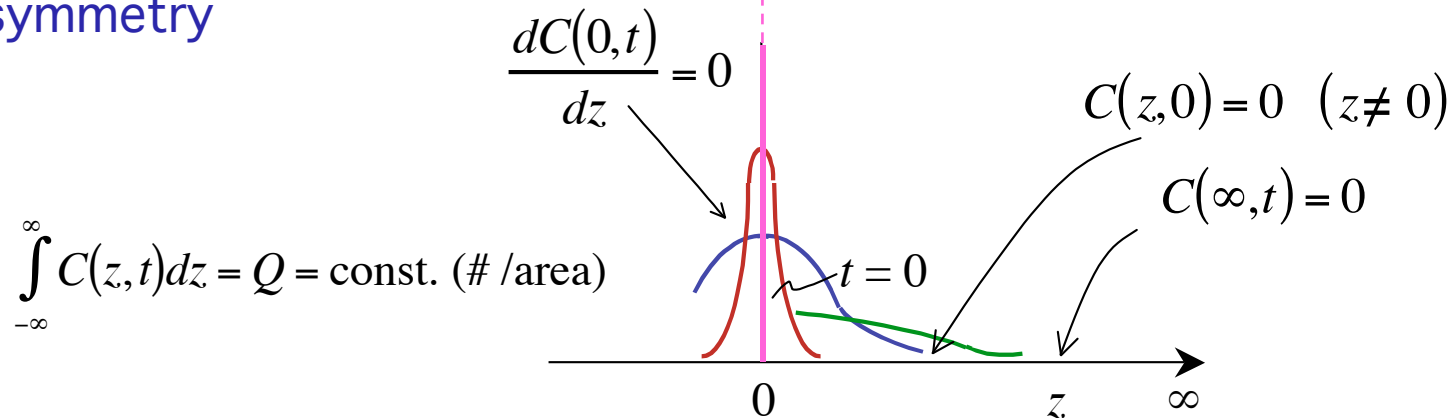
For other solutions, consider classical experiment:

Diffusion couple: thin dopant layer on rod face,
press 2 identical pieces together, heat.

Then study diffusion profile in sections.



symmetry



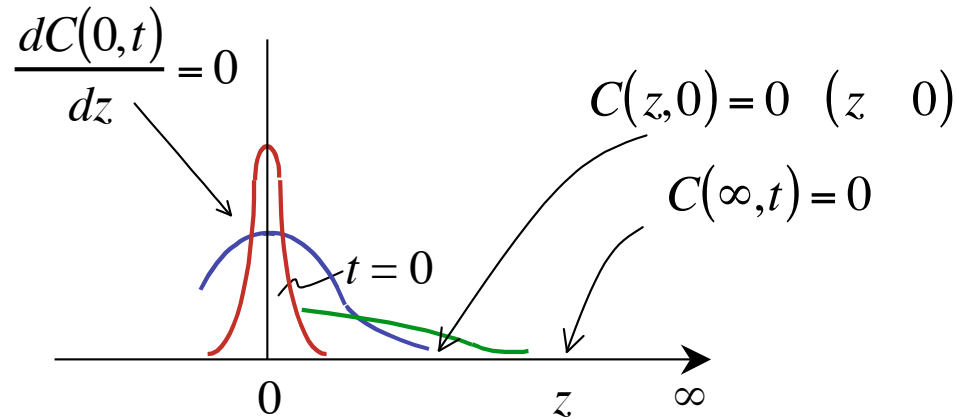
Analytic Solution to Diffusion Equations

$$J = -D \frac{\partial C}{\partial z},$$

$$\frac{\partial C}{\partial t} = D \frac{\partial^2 C}{\partial z^2}$$

I. “ Drive in” of *small*, fixed amount of dopant, solution is Gaussian

Predeposition is
delta function, $\delta(z)$.



$$C(z,t) = \frac{Q}{\sqrt{\pi D t}} \exp\left[-\frac{z^2}{4 D t}\right] \quad t > 0$$

Units

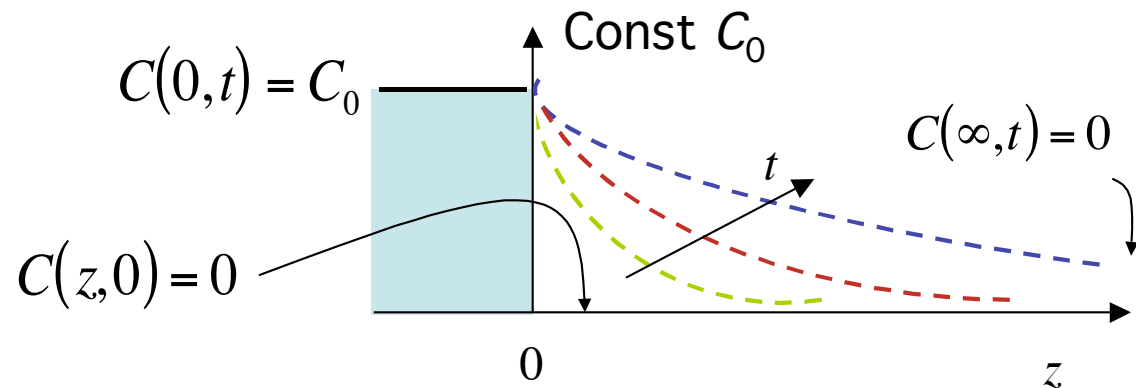
$\frac{1}{2}$ Width of Gaussian = $a = 2\sqrt{Dt}$ = diffusion length a
(a is large relative to width of predeposition)

Dose, Q , amount of dopant in sample, is constant.

Solutions for other I.C./B.C. can be obtained by superposition:

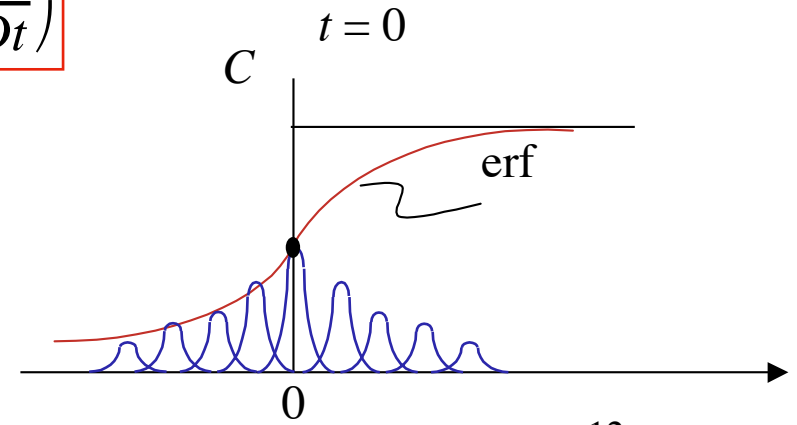
II. Predeposition

(Limitless source of dopant)

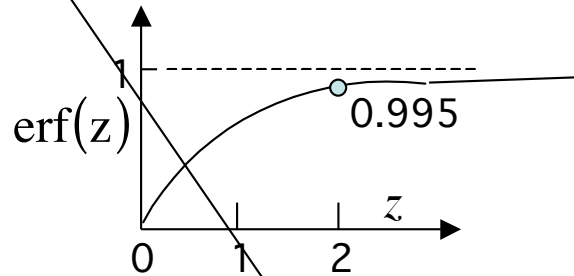


$$C_{\text{imp}}(z,t) = \frac{2}{\sqrt{\pi}} \int_0^{\frac{z}{2\sqrt{Dt}}} \exp[-\xi^2] d\xi \equiv \text{erf}(u) = \text{erf}\left(\frac{z}{2\sqrt{Dt}}\right)$$

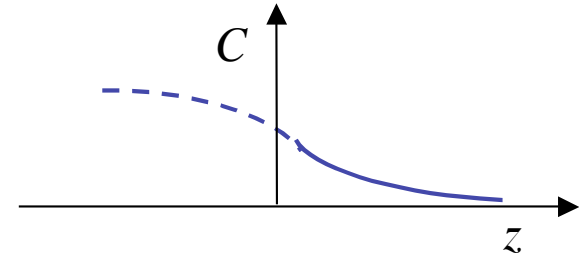
$$\xi^2 = \frac{z^2}{4Dt} \rightarrow \frac{(z - z_0)^2}{4Dt}$$



Other I.C./B.C. (cont.):



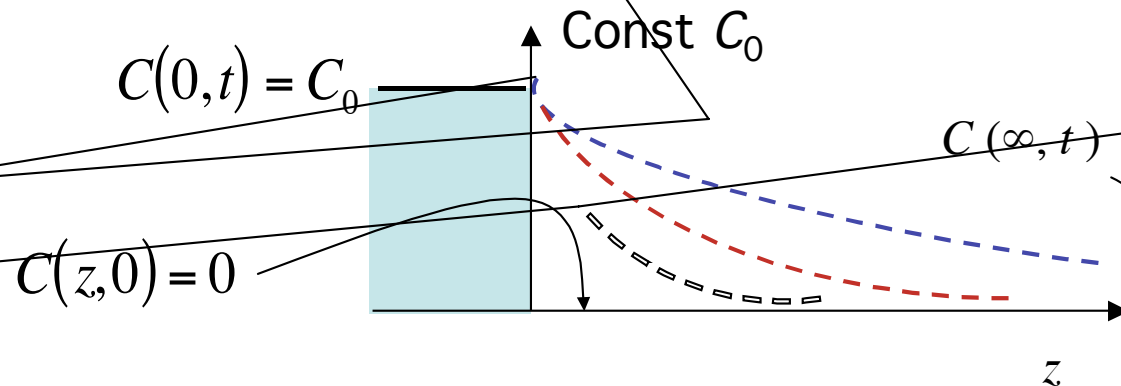
$$\text{erfc}(u) = 1 - \text{erf}(u)$$



$$C(z, t) = C_{\text{surf}} \text{erfc}\left[\frac{z}{2\sqrt{Dt}}\right], \quad t > 0$$

$$a = \text{diffusion length} = 2\sqrt{Dt}$$

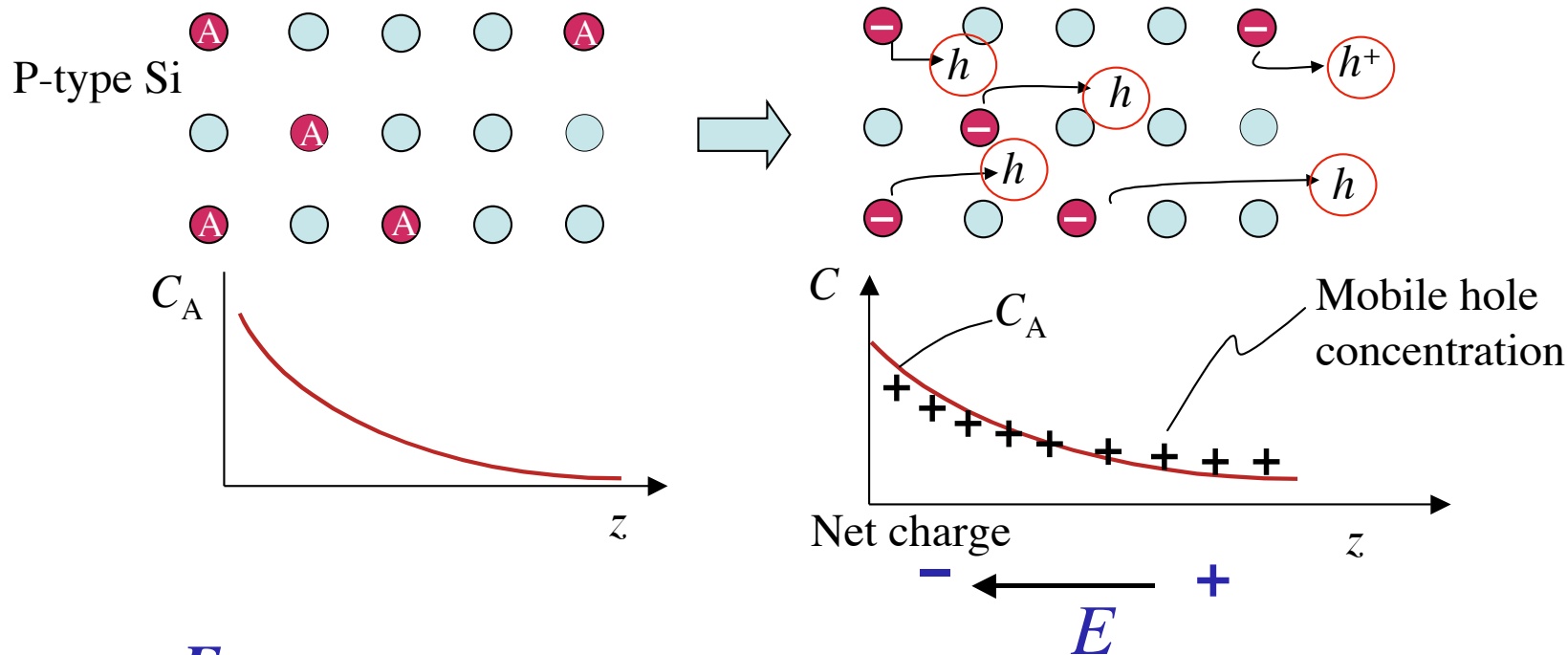
$$(D \approx 10^{-15}) \times (t = 10^3) \Rightarrow a \approx 0.2 \mu\text{m}$$



Internal E fields alter Fick's Law

Heavily doped layer can generate its own field

due to displacement of mobile carriers from ionized dopants:



E enhances diffusion of A^- to right, (also down concentration gradient).

$$J_{\text{mass}} = \underbrace{-D \frac{\partial C}{\partial z}}_{\text{diffusion}} + \underbrace{C \mu \vec{E}}_{A^- \text{ drift}} \equiv D \left[-\frac{\partial C}{\partial z} + \frac{C q \vec{E}}{kT} \right]$$

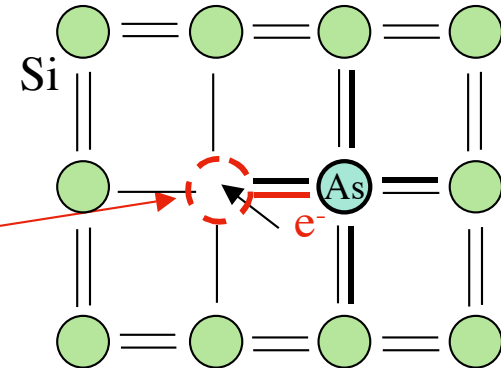
$$\left[\mu = \frac{Dq}{kT} \quad \begin{array}{l} \text{Einstein relation} \\ \text{from} \\ \text{Brownian motion} \end{array} \right]$$

Neutral and charged Impurities, dopants

If impurity is Gp. IV (e.g. Ge) uncharged, no e or h

But if imp. = B, P As... it will be charged:

So vacancies can be charged



For small dopant concentration, different diffusion processes are independent:

$$D_0 e^{\frac{E_a}{kT}} = D \Rightarrow \underbrace{D^0}_{\text{electrons}} + D^{1-} \frac{n}{n_i} + D^{2-} \left(\frac{n}{n_i} \right)^2 + \dots \quad D^+ \left(\frac{p}{p_i} \right) + D^{2+} \left(\frac{p}{p_i} \right)^2 + \dots$$

electrons **holes**

(these D^0 are NOT same as single activation energy values)

Intrinsic Diffusivities and Activation Energies of Substitutional Diffusers in Silicon^a

		P	As	Sb	B	Al	Ga
D_i^0	D_0	3.85	0.066	0.214	0.037	1.385	0.374
	E_0	3.66	3.44	3.65	3.46	3.41	3.39
D_i^+	D_0	—	—	—	0.76	2480	28.5
	E_0	—	—	—	3.46	4.20	3.92
D_i^-	D_0	4.44	22.9	13	—	—	—
	E_0	4.0	4.1	4.0	—	—	—
D_i^2	D_0	44.2	—	—	—	—	—
	E_0	4.37	—	—	—	—	—

^a D_0 in cm^2/s ; E_0 in eV.

[Higher activation energy for charged vacancy diffusion]

“What is n ?”

$$D^{\text{eff}} = D^0 + D^- \left(\frac{n}{n_i} \right) + D^{2-} \left(\frac{n}{n_i} \right)^2 + \dots + D^+ \left(\frac{p}{n_i} \right) + D^{2+} \left(\frac{p}{n_i} \right)^2 + \dots$$

n is free electron concentration. For strong donor doping $n > n_i$

So clearly, $D^{\text{eff}} = D^0 + D^-(n/n_i) + \dots$ can be $\gg D = D_0 \exp(-E_{\text{VD}}/kT)$

For intrinsic semiconductor or $N_D < n_i$, $n = p = n_i$

$$D^{\text{eff}} = D^0 + D^-(1) + \dots$$

See example p. 412 Plummer

$$n_i = 7.14 \times 10^{18}$$

$$D_{\text{As}}^{\text{eff}} = D^0 + D^-(n/n_i) +$$

$$\underbrace{2.67 \times 10^{-16} + 1.17 \times 10^{-15}(n/n_i)}$$

$$N_D = 10^{18}: D_{\text{As}}^{\text{eff}} = 1.43 \times 10^{-15}$$

$$N_D = 10^{20}: D_{\text{As}}^{\text{eff}} = 16.6 \times 10^{-15}$$

(Single-activation-energy value: $D = 1.5 \times 10^{-15}$)

Exercise

Calculate diffusivity of P in Si at 1000° C for

a) $C_p < n_i$ b) $C_p = 4 \times 10^{19} \text{ cm}^{-3}$

c) compare diffusion length b) with uncharged estimate

a) $C_p < n_i = 10^{19}$

from F 1.16

Exercise

Calculate diffusivity of P in Si at 1000° C for

a) $C_p < n_i$ b) $C_p = 4 \times 10^{19} \text{ cm}^{-3}$

c) compare diffusion length b) with uncharged estimate

a) $C_p < n_i = 10^{19}$

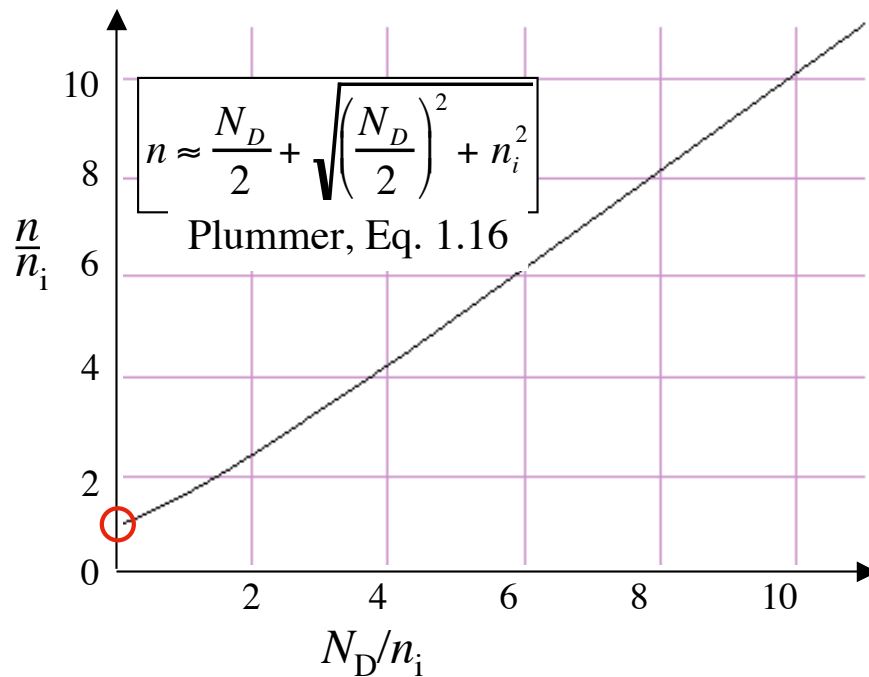
Diffusion of P in Si

D_0	E_a	D_0^-	E_a^-
(cm ² /s)	(eV)	(cm ² /s)	(eV)
3.85	3.66	4.4	4.0

$$D_p^0 = 3.85 \exp\left[-\frac{3.66}{kT}\right] = 1.3 \times 10^{-14} (\text{cm}^2 \text{s}^{-1})$$

$$D_p^- = 4.4 \exp\left[-\frac{4}{kT}\right] = 6.63 \times 10^{-16} (\text{cm}^2 \text{s}^{-1})$$

$$D = D_p^0 + D_p^- \left(\frac{n}{n_i}\right) = 1.37 \times 10^{-14} (\text{cm}^2 \text{s}^{-1})$$



Better than single-activation-energy:

$$D_p = 4.7 \exp\left[-\frac{3.68}{kT}\right] = 1.3 \times 10^{-14} (\text{cm}^2 \text{s}^{-1})$$

Exercise

Calculate diffusivity of P in Si at 1000° C for

a) $C_p < n_i$ b) $C_p = 4 \times 10^{19} \text{ cm}^{-3}$

c) compare diffusion length b) with uncharged estimate

b) $C_p = N_D = 4 \times 10^{19}$
$$n \approx \frac{N_D}{2} + \sqrt{\left(\frac{N_D}{2}\right)^2 + n_i^2} = 10^{19} + \sqrt{4 \times 10^{38} + 10^{38}} = 3.24 \times 10^{19} \text{ cm}^{-3}$$

Plummer, Eq. 1.16

$$D = D_P^0 + D_P^- \left(\frac{n}{n_i} \right) = 1.3 \times 10^{-14} + 6.63 \times 10^{-16} \left(\frac{3.24}{1} \right) = 1.5 \times 10^{-14} (\text{cm}^2 \text{s}^{-1}) \quad \text{vs } 1.37$$

c) $a = 2\sqrt{Dt}$, 1 hr $\Rightarrow a_0 = 2\sqrt{1.37 \times 10^{-14} \times 3600} = 0.14 \text{ } \mu\text{m}$
 $a_p = 2\sqrt{1.51 \times 10^{-14} \times 3600} = 0.147 \text{ } \mu\text{m}$

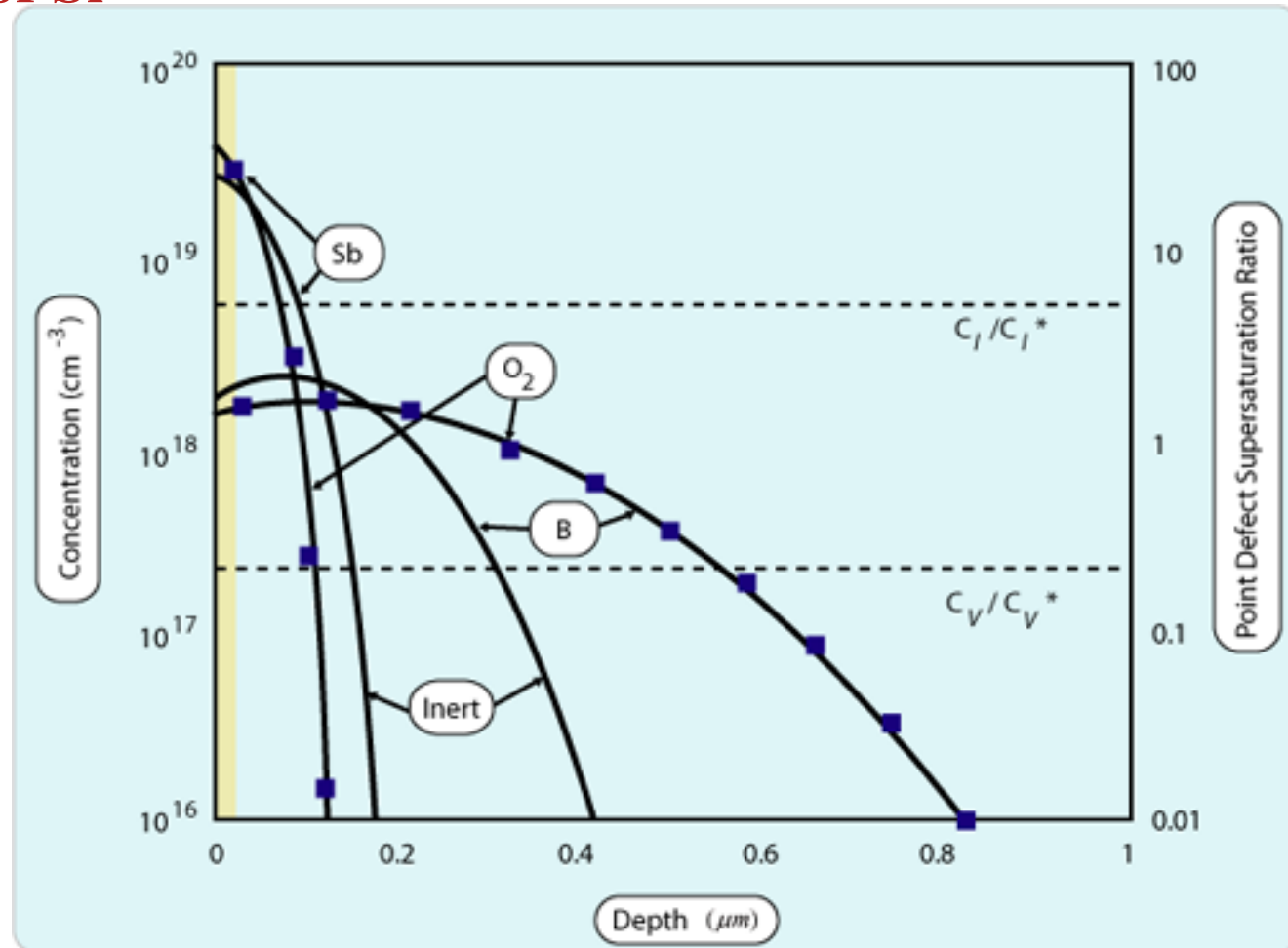
Consequence:

Diffusion is enhanced
at high dopant
concentrations
⇒ Sharper
diffusion profile

Effect of oxidation of Si on diffusion

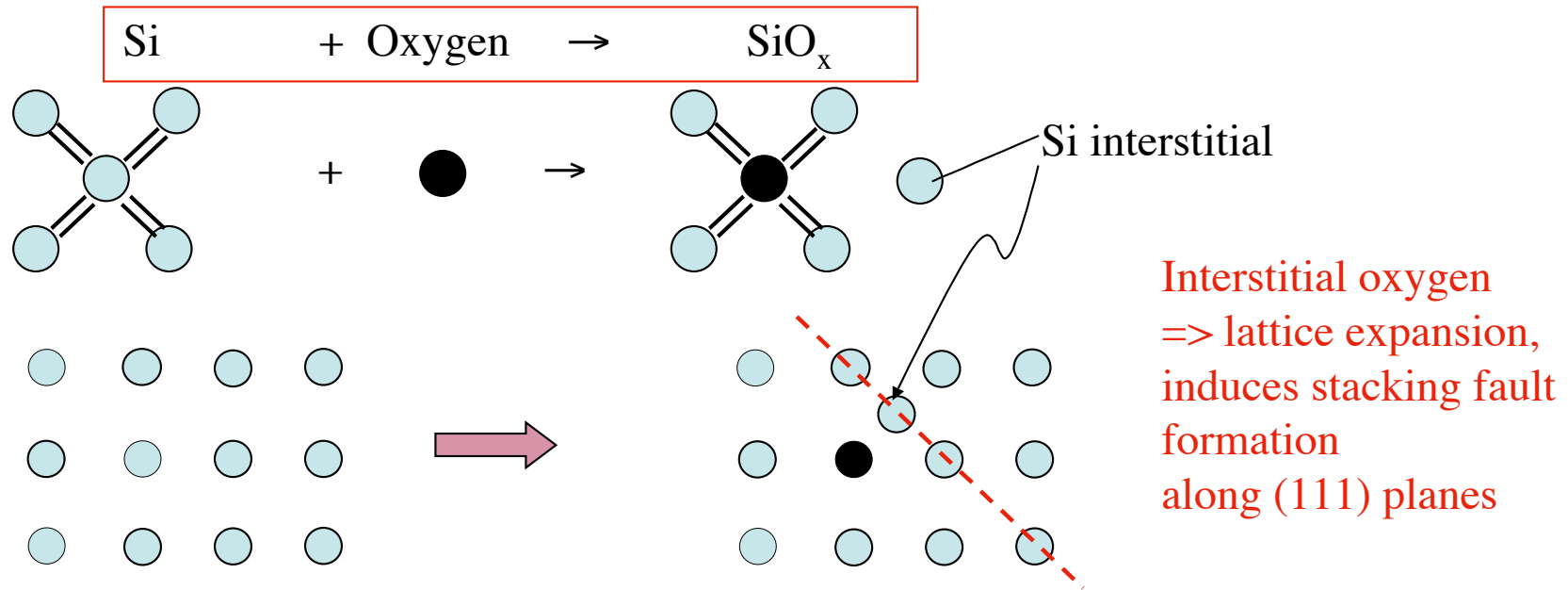
B and P
observed to diffuse faster
when Si surface is oxidized,
Sb slower?

So far
we have concentrated on
diffusion
by vacancy mechanism



Different behavior of B and Sb under oxidation suggests
a different mechanism may dominate in these two dopants

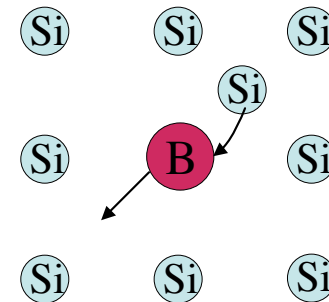
Effect of oxidation on diffusion in Si



Because B and P can diffuse via vacancies as well as interstitial process their diffusion is enhanced by oxidation.

But Sb is large and diffuses only by vacancies.

Si interstitials created by oxidation, recombine and reduce concentration of vacancies suppressing diffusion of Sb atoms.

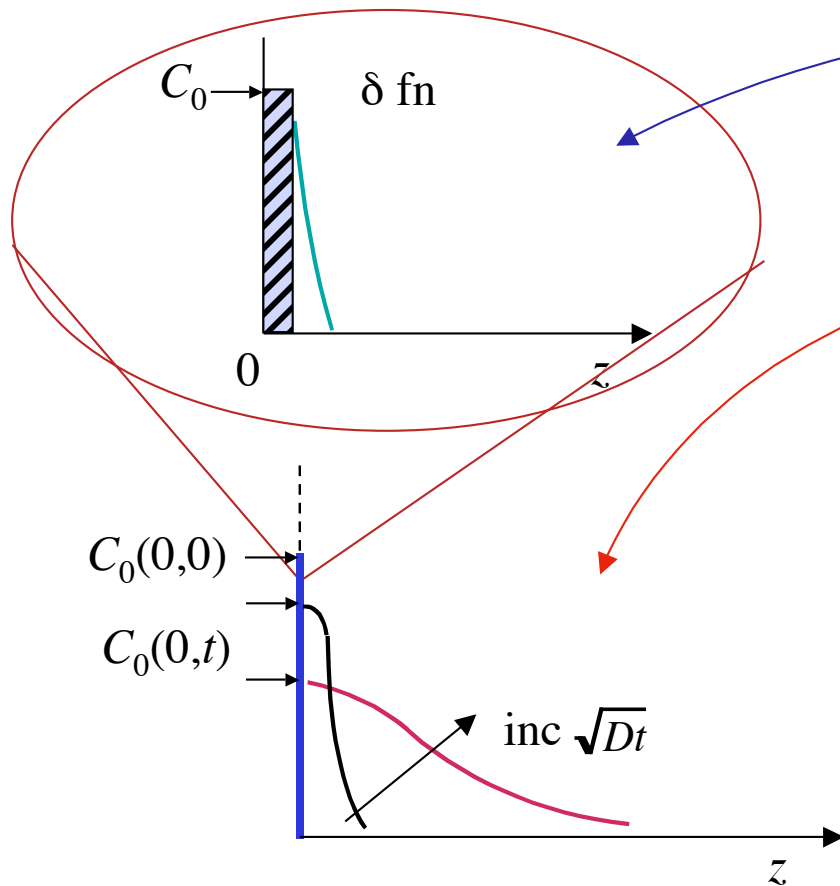


Review: Doping and diffusion, *small dose*

$$\frac{dC(z,t)}{dt} = \frac{d}{dz} \left(D \frac{dC}{dz} \right)$$

Plus I.C. and B.C.s

If “predeposition” is *small dose*,
followed by a higher T ,
larger t (larger $a \sim \sqrt{Dt}$)
“drive-in” process.



1) I.C. $C(z, 0) = 0 \quad z > 0$

2) B.C. $C(\infty, t) = 0$

3) **Fixed** dose $Q = \frac{a}{\sqrt{\pi}} c_0$

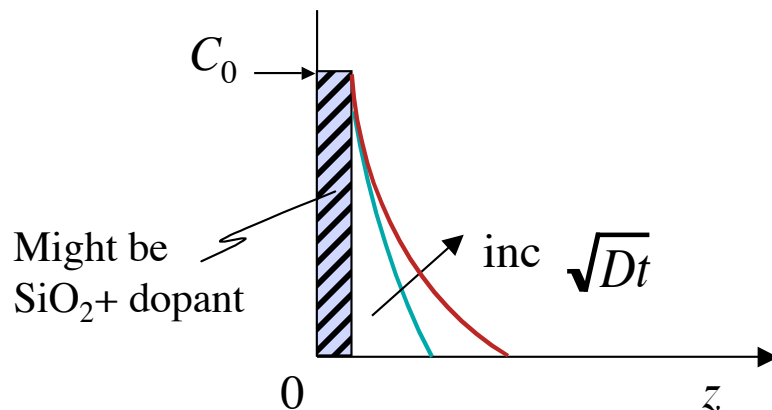
$$C(z,t) = \frac{Q}{\sqrt{\pi Dt}} \exp \left[-\left(\frac{z}{a} \right)^2 \right]$$

$$C(0,t) = \frac{Q}{\sqrt{\pi Dt}} \quad \text{decreases like } t^{-1/2}$$

Review: Doping and diffusion, *large dose*

Diffusion preceded by “pre-deposition” to deliver a *large amount* of impurity.

If pre-dep is *inexhaustible* or equivalently, if $a \sim \sqrt{Dt}$ is small, then



$$1) \text{ I.C. } C(z, 0) = 0 \quad z > 0$$

$$2) \text{ B.C. } C(\infty, t) = 0$$

$$3) \text{ B.C. } C(0, t) = C_0$$

$$C(z, t) = C_0 \operatorname{erfc} \left[\frac{z}{a} \right] \quad a = 2\sqrt{Dt}$$

$$\text{Dose} \equiv Q = \int_0^{\infty} C(z, t) dz = \frac{2\sqrt{Dt}}{\sqrt{\pi}} C_0 = \frac{a}{\sqrt{\pi}} C_0$$

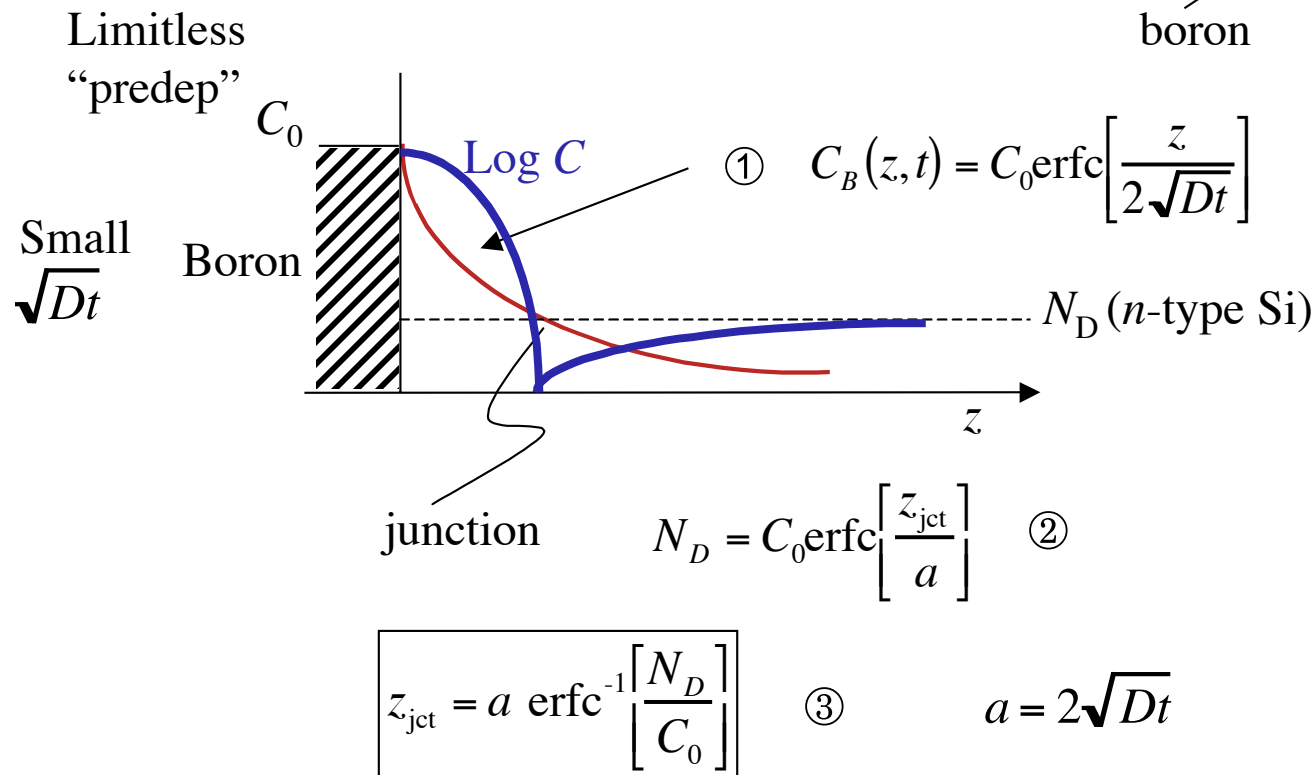
C_0 limited by solid solubility

Junctions between different doped regions

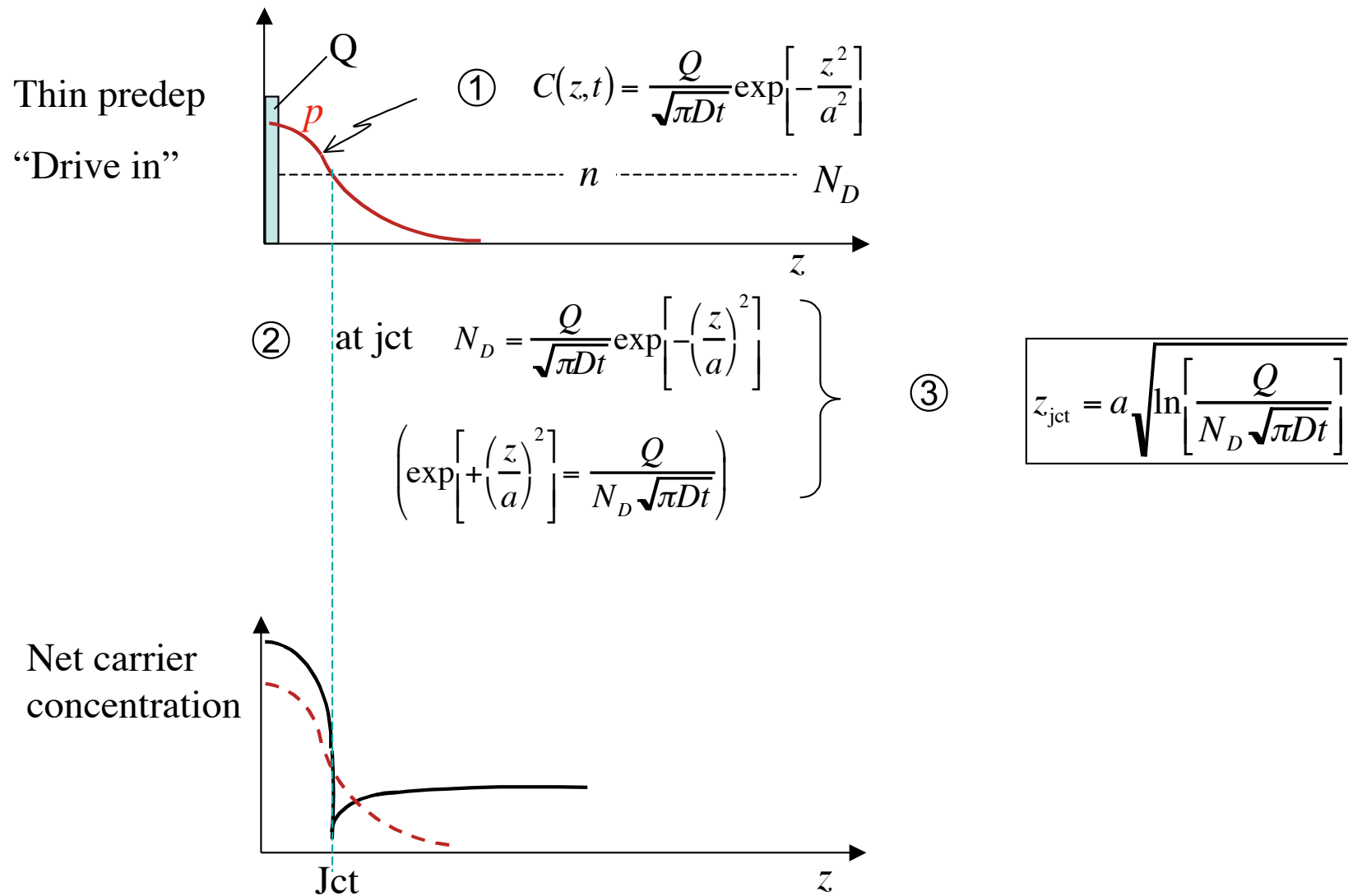
Diffuse B at high concentration, into n-type Si, (uniformly doped, N_D , with P).

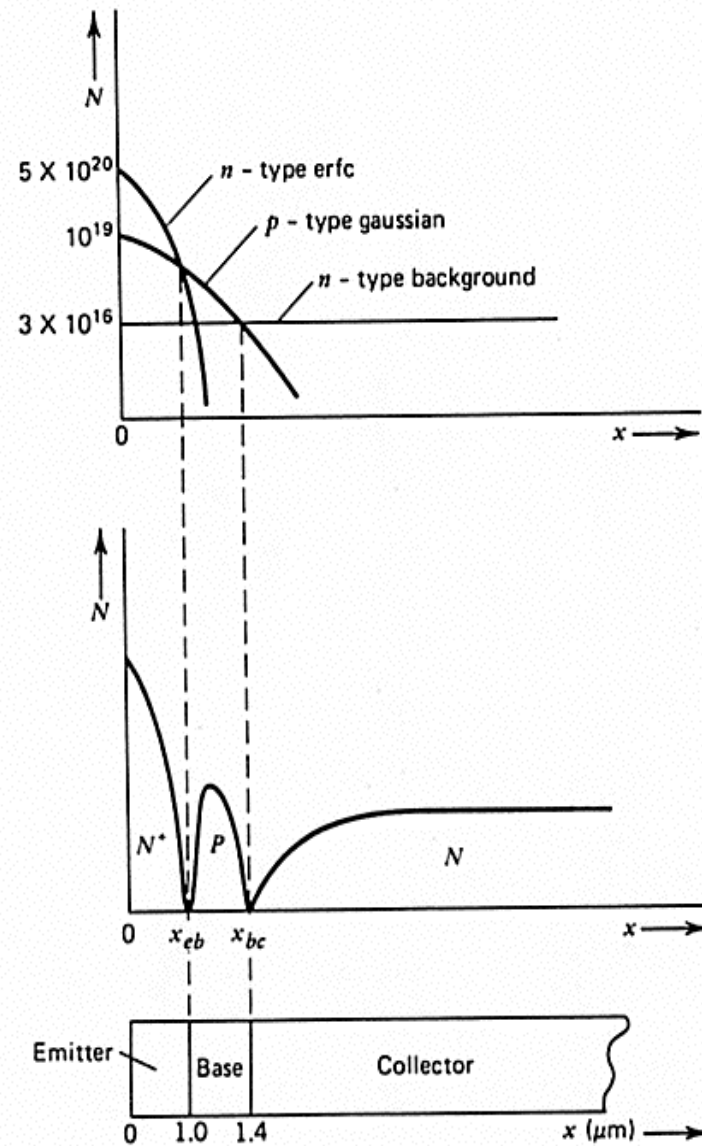
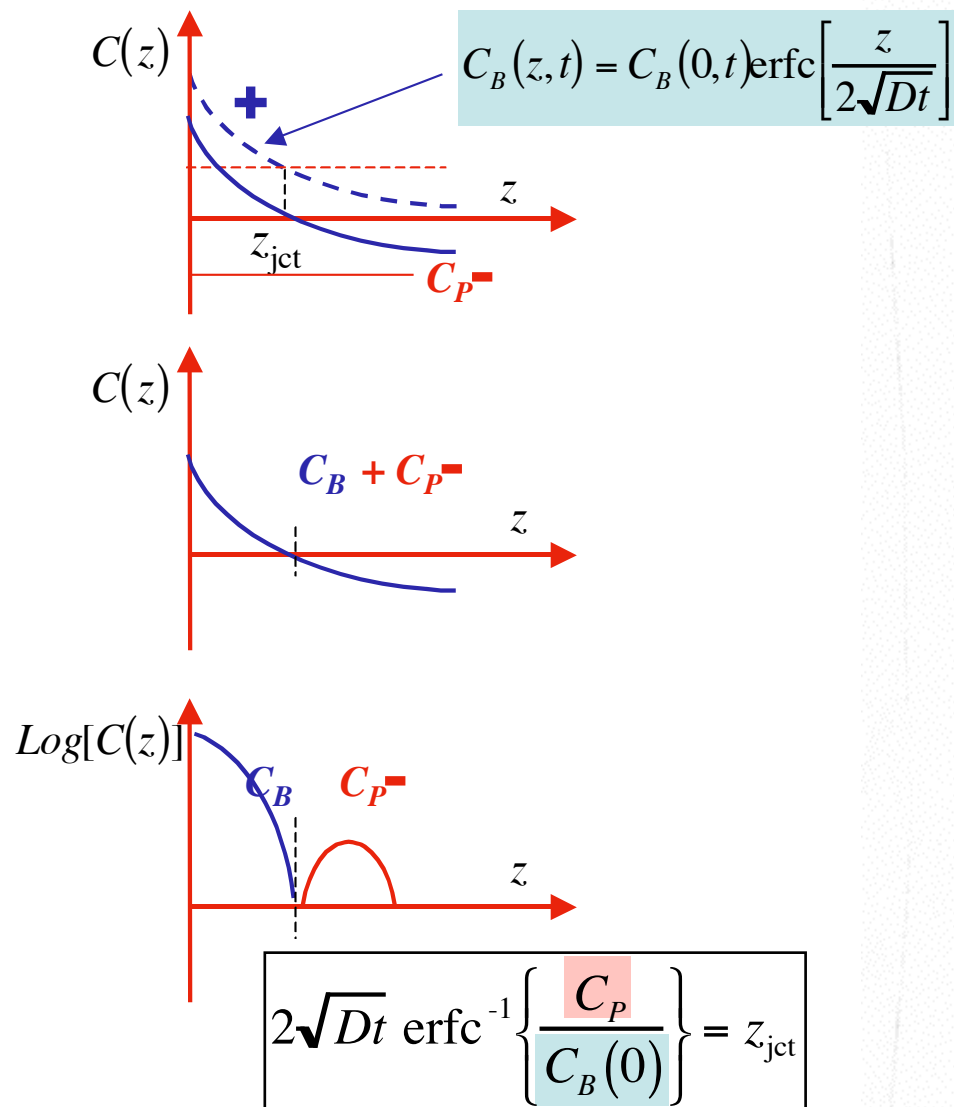
Want to know depth of p.n. junction ($N_A = N_D$)

\nearrow boron \nwarrow phosphorus



Junctions between different doped regions

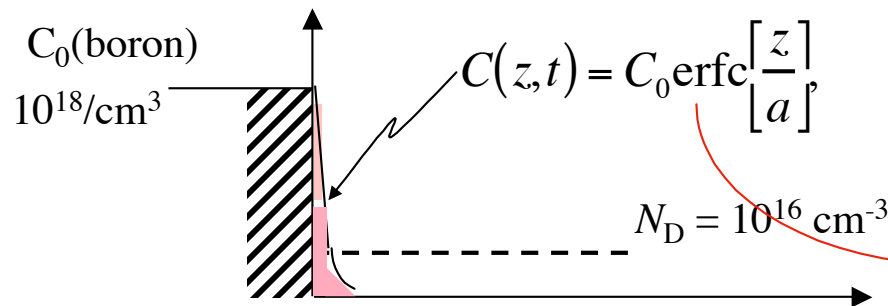




Exercise

N -type Si, $N_D = 10^{16} \text{ cm}^{-3}$ is doped with boron by a “predep”

from a const source with C_0 (boron) = 10^{18} cm^{-3}



Question:

If predep is done at 1000°C for 1 hr,
what is junction depth?

$$z_{\text{jct}} = a \operatorname{erfc}^{-1} \left[\frac{N_D}{C_0} \right] = 2\sqrt{Dt} \operatorname{erfc}^{-1} [10^{-2}]$$

Let $\operatorname{erfc}^{-1} [10^{-2}] = x$, $\operatorname{erfc}[x] = 0.01 = 1 - \operatorname{erf}[x]$, $\operatorname{erf}[x] = 0.99$.

From appendix, $x = 1.82$

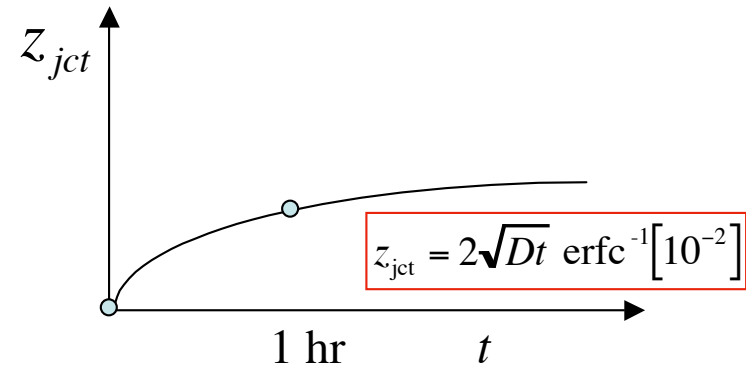
$$D(\text{boron}) = 0.037 \exp \left[-\frac{3.46}{kT} \right] \xrightarrow{1273 \text{ K}} 7.6 \times 10^{-16} \text{ cm}^2/\text{s}$$

$$a = 2\sqrt{Dt} = 3.31 \times 10^{-6} \text{ cm} = 0.033 \mu\text{m}$$

$$z_{\text{jct}} = 0.033 \times 1.82 = 0.06 \mu\text{m}$$

$$z_{\text{jct}} = 0.033 \times 1.82 = 0.06 \mu\text{m}$$

From $z_{\text{jct}}(t)$ and $z_{\text{jct}}(0)$
you can calculate
junction depth
at different time:



Question: Now surface film (const. source) is removed
and this dose, $C(z, 1\text{hr})$, is “driven in” for 1 hr at 1100°C .

Now where is junction?

$$Q = \int C(z, 1\text{hr}) dz = \frac{aC_0}{\sqrt{\pi}} = 1.87 \times 10^{12} \text{cm}^{-2}$$

$$\text{D (boron)} \xrightarrow{1373 \text{ K}} 7.57 \times 10^{-15} \text{cm}^2/\text{s} \quad \sqrt{Dt} = 5.22 \times 10^{-6} \text{cm}$$

$$z_{\text{jct}} = a \sqrt{\ln\left(\frac{Q}{N_D \sqrt{\pi Dt}}\right)} = 1.8 \times 10^{-5} \text{cm} = 0.18 \mu\text{m}$$

Measuring diffusion profiles

Resistance

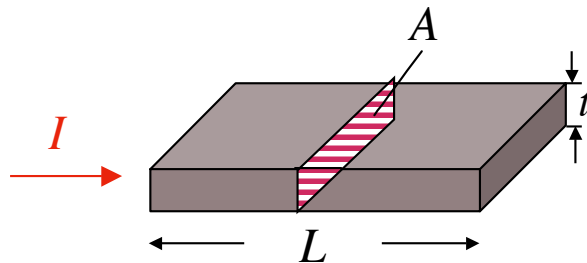
$$R = \rho \frac{L}{A} (\Omega),$$

resistivity

$$\rho = \frac{RA}{L} (\Omega m)$$

conductivity

$$\sigma = \frac{1}{\rho} = nq\mu$$



But n, μ are functions of position due to doping

$$\langle \sigma \rangle = \frac{q}{t} \int_0^t n(z) \mu(n) dz$$

$$\langle \rho \rangle = \frac{1}{\langle \sigma \rangle} = \frac{t}{q \int n \mu dz}$$

Define

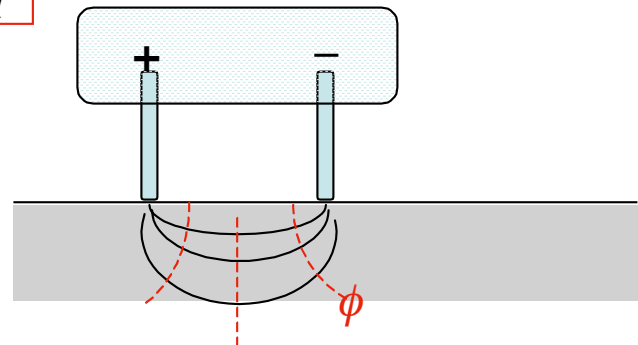
sheet resistance

$$\frac{\rho}{t} \equiv R_s = \frac{RA}{Lt} = R \frac{W}{L} \left(\frac{\Omega}{sq} \right)$$

an average measurement of n

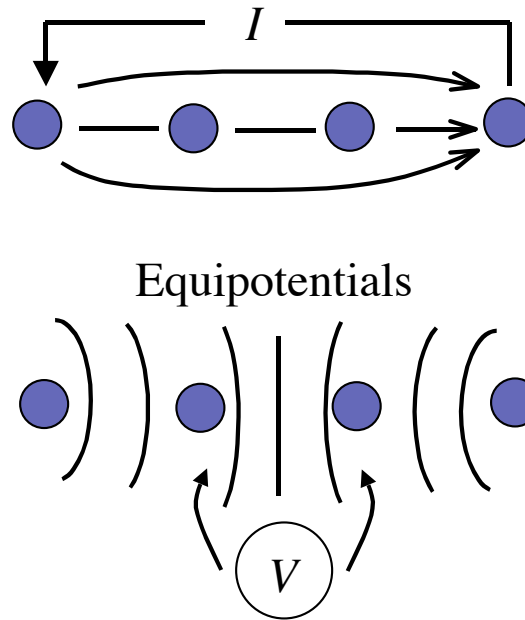
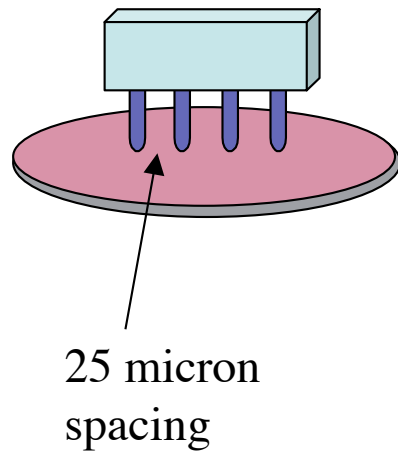
Spreading resistance probe:

(Developed at Bell Labs in '40s)

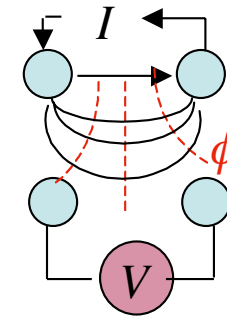


Measuring diffusion profiles

4-point probe

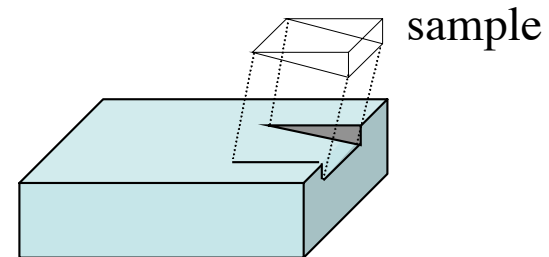


Also square array
(Van der Pauw method)

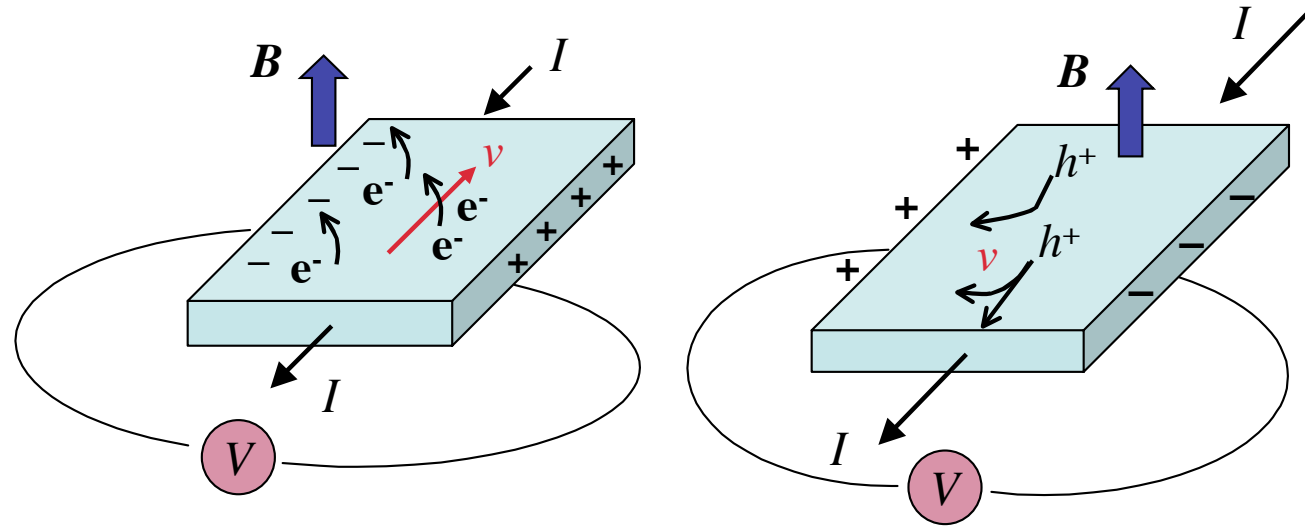


These \Rightarrow average n if done from surface.

These are most useful if done on beveled wafer:



Hall effect: electrical transport in magnetic field.

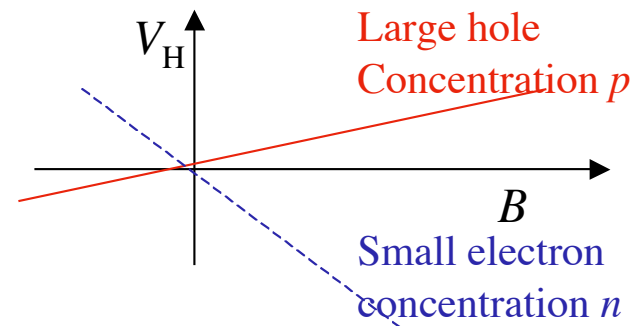


$$\left. \begin{aligned} F &= q\langle v \rangle \times B \\ J &= nq\langle v \rangle \end{aligned} \right\} \frac{F}{q} = E_H = \frac{J}{nq} B \quad \boxed{E_H = R_H (J \times B)}$$

Hall coefficient => charge sign
and concentration

R_H is slope of V vs B data

$$\boxed{R_H = \frac{1}{nq}}$$



Again an average measurement

Capacitance

Use MOS structure,
gate & substrate
are electrodes

$$C = \frac{\epsilon A}{d}$$

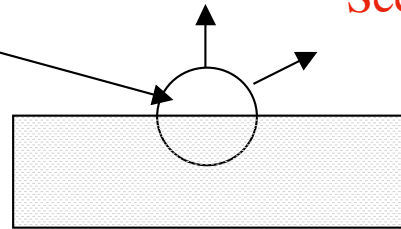
Useful for lightly doped regions

Depletion width

SIMS

(Secondary ion
mass spectroscopy)

Ion source
1 - 5 k eV
Sputters
surface



Secondary ions
to mass spectrometer

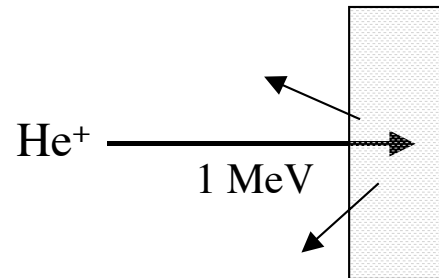
Depth profile

RBS

(Rutherford back scattering)

Backscatter energy

depends on depth and impurities



Ions penetrate

Backscatter intensity $\propto (\text{mass impurities})^2$