Chapter 1 INTRODUCTION AND BASIC CONCEPTS

Thermodynamics

- **1-1C** Classical thermodynamics is based on experimental observations whereas statistical thermodynamics is based on the average behavior of large groups of particles.
- **1-2C** On a downhill road the potential energy of the bicyclist is being converted to kinetic energy, and thus the bicyclist picks up speed. There is no creation of energy, and thus no violation of the conservation of energy principle.
- **1-3C** There is no truth to his claim. It violates the second law of thermodynamics.

Mass, Force, and Units

- **1-4C** Pound-mass lbm is the mass unit in English system whereas pound-force lbf is the force unit. One pound-force is the force required to accelerate a mass of 32.174 lbm by 1 ft/s². In other words, the weight of a 1-lbm mass at sea level is 1 lbf.
- **1-5**C Kg-mass is the mass unit in the SI system whereas kg-force is a force unit. 1-kg-force is the force required to accelerate a 1-kg mass by 9.807 m/s². In other words, the weight of 1-kg mass at sea level is 1 kg-force.
- **1-6**C There is no acceleration, thus the net force is zero in both cases.
- 1-7 A plastic tank is filled with water. The weight of the combined system is to be determined.

Assumptions The density of water is constant throughout.

Properties The density of water is given to be $\rho = 1000 \text{ kg/m}^3$.

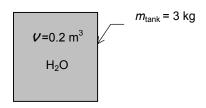
Analysis The mass of the water in the tank and the total mass are

$$m_w = \rho \mathbf{V} = (1000 \text{ kg/m}^3)(0.2 \text{ m}^3) = 200 \text{ kg}$$

 $m_{\text{total}} = m_w + m_{\text{tank}} = 200 + 3 = 203 \text{ kg}$

Thus,

$$W = mg = (203 \text{ kg})(9.81 \text{ m/s}^2) \left(\frac{1 \text{ N}}{1 \text{ kg} \cdot \text{m/s}^2}\right) = 1991 \text{ N}$$



1-8 The interior dimensions of a room are given. The mass and weight of the air in the room are to be determined.

Assumptions The density of air is constant throughout the room.

Properties The density of air is given to be $\rho = 1.16 \text{ kg/m}^3$.

Analysis The mass of the air in the room is

$$m = \rho V = (1.16 \text{ kg/m}^3)(6 \times 6 \times 8 \text{ m}^3) = 334.1 \text{ kg}$$

Thus,

$$W = mg = (334.1 \text{ kg})(9.81 \text{ m/s}^2) \left(\frac{1 \text{ N}}{1 \text{ kg} \cdot \text{m/s}^2}\right) = 3277 \text{ N}$$

ROOM AIR 6X6X8 m³

1-9 The variation of gravitational acceleration above the sea level is given as a function of altitude. The height at which the weight of a body will decrease by 1% is to be determined.

Analysis The weight of a body at the elevation z can be expressed as

$$W = mg = m(9.807 - 3.32 \times 10^{-6}z)$$

In our case,

$$W = 0.99W_s = 0.99mg_s = 0.99(m)(9.807)$$

Substituting,

$$0.99(9.81) = (9.81 - 3.32 \times 10^{-6} z) \longrightarrow z = 29,539 m$$



1-10E An astronaut took his scales with him to space. It is to be determined how much he will weigh on the spring and beam scales in space.

Analysis (a) A spring scale measures weight, which is the local gravitational force applied on a body:

$$W = mg = (150 \text{ lbm})(5.48 \text{ ft/s}^2) \left(\frac{1 \text{ lbf}}{32.2 \text{ lbm} \cdot \text{ft/s}^2} \right) = 25.5 \text{ lbf}$$

(b) A beam scale compares masses and thus is not affected by the variations in gravitational acceleration. The beam scale will read what it reads on earth,

$$W = 150 \, lbf$$

1-11 The acceleration of an aircraft is given in g's. The net upward force acting on a man in the aircraft is to be determined.

Analysis From the Newton's second law, the force applied is

$$F = ma = m(6 \text{ g}) = (90 \text{ kg})(6 \times 9.81 \text{ m/s}^2) \left(\frac{1 \text{ N}}{1 \text{ kg} \cdot \text{m/s}^2}\right) = 5297 \text{ N}$$

1-12 [Also solved by EES on enclosed CD] A rock is thrown upward with a specified force. The acceleration of the rock is to be determined.

Analysis The weight of the rock is

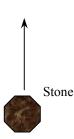
$$W = mg = (5 \text{ kg})(9.79 \text{ m/s}^2) \left(\frac{1 \text{ N}}{1 \text{ kg} \cdot \text{m/s}^2}\right) = 48.95 \text{ N}$$

Then the net force that acts on the rock is

$$F_{\text{net}} = F_{\text{up}} - F_{\text{down}} = 150 - 48.95 = 101.05 \text{ N}$$

From the Newton's second law, the acceleration of the rock becomes

$$a = \frac{F}{m} = \frac{101.05 \text{ N}}{5 \text{ kg}} \left(\frac{1 \text{ kg} \cdot \text{m/s}^2}{1 \text{ N}} \right) = 20.2 \text{ m/s}^2$$



1-13 EES Problem 1-12 is reconsidered. The entire EES solution is to be printed out, including the numerical results with proper units.

Analysis The problem is solved using EES, and the solution is given below.

W=m*g"[N]" m=5"[kg]" g=9.79"[m/s^2]"

"The force balance on the rock yields the net force acting on the rock as"

 $F_net = F_up - F_down"[N]"$ $F_up=150"[N]"$ $F_down=W"[N]"$

"The acceleration of the rock is determined from Newton's second law." F_net=a*m

"To Run the program, press F2 or click on the calculator icon from the Calculate menu"

SOLUTION a=20.21 [m/s^2] F_down=48.95 [N] F_net=101.1 [N] F_up=150 [N] g=9.79 [m/s^2] m=5 [kg] W=48.95 [N] **1-14** Gravitational acceleration g and thus the weight of bodies decreases with increasing elevation. The percent reduction in the weight of an airplane cruising at 13,000 m is to be determined.

Properties The gravitational acceleration g is given to be 9.807 m/s² at sea level and 9.767 m/s² at an altitude of 13,000 m.

Analysis Weight is proportional to the gravitational acceleration g, and thus the percent reduction in weight is equivalent to the percent reduction in the gravitational acceleration, which is determined from

%Reduction in weight = %Reduction in
$$g = \frac{\Delta g}{g} \times 100 = \frac{9.807 - 9.767}{9.807} \times 100 = 0.41\%$$

Therefore, the airplane and the people in it will weight 0.41% less at 13,000 m altitude.

Discussion Note that the weight loss at cruising altitudes is negligible.



Systems, Properties, State, and Processes

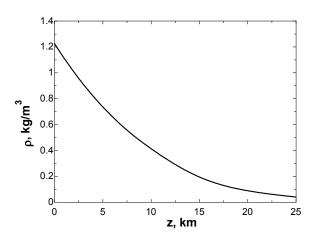
- 1-15C The radiator should be analyzed as an open system since mass is crossing the boundaries of the system.
- 1-16C A can of soft drink should be analyzed as a closed system since no mass is crossing the boundaries of the system.
- 1-17C Intensive properties do not depend on the size (extent) of the system but extensive properties do.
- **1-18C** For a system to be in thermodynamic equilibrium, the temperature has to be the same throughout but the pressure does not. However, there should be no unbalanced pressure forces present. The increasing pressure with depth in a fluid, for example, should be balanced by increasing weight.
- **1-19C** A process during which a system remains almost in equilibrium at all times is called a quasi-equilibrium process. Many engineering processes can be approximated as being quasi-equilibrium. The work output of a device is maximum and the work input to a device is minimum when quasi-equilibrium processes are used instead of nonquasi-equilibrium processes.
- **1-20**C A process during which the temperature remains constant is called isothermal; a process during which the pressure remains constant is called isobaric; and a process during which the volume remains constant is called isochoric.
- **1-21**C The state of a simple compressible system is completely specified by two independent, intensive properties.
- **1-22**C Yes, because temperature and pressure are two independent properties and the air in an isolated room is a simple compressible system.
- **1-23**C A process is said to be steady-flow if it involves no changes with time anywhere within the system or at the system boundaries.
- **1-24**C The **specific gravity**, or **relative density**, and is defined as the ratio of the density of a substance to the density of some standard substance at a specified temperature (usually water at 4°C, for which $\rho_{\rm H2O}$ = 1000 kg/m³). That is, SG = ρ / $\rho_{\rm H2O}$. When specific gravity is known, density is determined from ρ = SG × $\rho_{\rm H2O}$.

1-25 EES The variation of density of atmospheric air with elevation is given in tabular form. A relation for the variation of density with elevation is to be obtained, the density at 7 km elevation is to be calculated, and the mass of the atmosphere using the correlation is to be estimated.

Assumptions 1 Atmospheric air behaves as an ideal gas. 2 The earth is perfectly sphere with a radius of 6377 km, and the thickness of the atmosphere is 25 km.

Properties The density data are given in tabular form as

<i>r</i> , km	<i>z</i> , km	ρ , kg/m ³
6377	0	1.225
6378	1	1.112
6379	2	1.007
6380	3	0.9093
6381	4	0.8194
6382	5	0.7364
6383	6	0.6601
6385	8	0.5258
6387	10	0.4135
6392	15	0.1948
6397	20	0.08891
6402	25	0.04008



Analysis Using EES, (1) Define a trivial function rho= a+z in equation window, (2) select new parametric table from Tables, and type the data in a two-column table, (3) select Plot and plot the data, and (4) select plot and click on "curve fit" to get curve fit window. Then specify 2nd order polynomial and enter/edit equation. The results are:

$$\rho(z) = a + bz + cz^2 = 1.20252 - 0.101674z + 0.0022375z^2$$
 for the unit of kg/m³, (or, $\rho(z) = (1.20252 - 0.101674z + 0.0022375z^2) \times 10^9$ for the unit of kg/km³)

where z is the vertical distance from the earth surface at sea level. At z = 7 km, the equation would give $\rho = 0.60 \text{ kg/m}^3$.

(b) The mass of atmosphere can be evaluated by integration to be

$$m = \int_{V} \rho dV = \int_{z=0}^{h} (a+bz+cz^{2}) 4\pi (r_{0}+z)^{2} dz = 4\pi \int_{z=0}^{h} (a+bz+cz^{2}) (r_{0}^{2}+2r_{0}z+z^{2}) dz$$
$$= 4\pi \left[ar_{0}^{2}h + r_{0}(2a+br_{0})h^{2}/2 + (a+2br_{0}+cr_{0}^{2})h^{3}/3 + (b+2cr_{0})h^{4}/4 + ch^{5}/5 \right]$$

where $r_0 = 6377$ km is the radius of the earth, h = 25 km is the thickness of the atmosphere, and a = 1.20252, b = -0.101674, and c = 0.0022375 are the constants in the density function. Substituting and multiplying by the factor 10^9 for the density unity kg/km³, the mass of the atmosphere is determined to be

$$m = 5.092 \times 10^{18} \text{ kg}$$

Discussion Performing the analysis with excel would yield exactly the same results.

EES Solution for final result:

a=1.2025166 b=-0.10167 c=0.0022375 r=6377 h=25

m=4*pi*(a*r^2*h+r*(2*a+b*r)*h^2/2+(a+2*b*r+c*r^2)*h^3/3+(b+2*c*r)*h^4/4+c*h^5/5)*1E+9

Temperature

- **1-26**°C The zeroth law of thermodynamics states that two bodies are in thermal equilibrium if both have the same temperature reading, even if they are not in contact.
- **1-27**C They are celsius($^{\circ}$ C) and kelvin (K) in the SI, and fahrenheit ($^{\circ}$ F) and rankine (R) in the English system.
- **1-28**C Probably, but not necessarily. The operation of these two thermometers is based on the thermal expansion of a fluid. If the thermal expansion coefficients of both fluids vary linearly with temperature, then both fluids will expand at the same rate with temperature, and both thermometers will always give identical readings. Otherwise, the two readings may deviate.
- **1-29** A temperature is given in °C. It is to be expressed in K.

Analysis The Kelvin scale is related to Celsius scale by

$$T(K] = T(^{\circ}C) + 273$$

Thus, $T(K] = 37^{\circ}C + 273 = 310 \text{ K}$

1-30E A temperature is given in °C. It is to be expressed in °F, K, and R.

Analysis Using the conversion relations between the various temperature scales,

$$T(K] = T(^{\circ}C) + 273 = 18^{\circ}C + 273 = 291 \text{ K}$$

 $T(^{\circ}F] = 1.8T(^{\circ}C) + 32 = (1.8)(18) + 32 = 64.4^{\circ}F$
 $T(R] = T(^{\circ}F) + 460 = 64.4 + 460 = 524.4 \text{ R}$

1-31 A temperature change is given in °C. It is to be expressed in K.

Analysis This problem deals with temperature changes, which are identical in Kelvin and Celsius scales. Thus, $\Delta T(K) = \Delta T(^{\circ}C) = 15 \text{ K}$

1-32E A temperature change is given in °F. It is to be expressed in °C, K, and R.

Analysis This problem deals with temperature changes, which are identical in Rankine and Fahrenheit scales. Thus,

$$\Delta T(R) = \Delta T(\cdot F) = 45 R$$

The temperature changes in Celsius and Kelvin scales are also identical, and are related to the changes in Fahrenheit and Rankine scales by

$$\Delta T(K) = \Delta T(R)/1.8 = 45/1.8 = 25 \text{ K}$$

and $\Delta T(^{\circ}C) = \Delta T(K) = 25^{\circ}C$

1-33 Two systems having different temperatures and energy contents are brought in contact. The direction of heat transfer is to be determined.

Analysis Heat transfer occurs from warmer to cooler objects. Therefore, heat will be transferred from system B to system A until both systems reach the same temperature.

Pressure, Manometer, and Barometer

1-34C The pressure relative to the atmospheric pressure is called the *gage pressure*, and the pressure relative to an absolute vacuum is called *absolute pressure*.

1-35C The atmospheric pressure, which is the external pressure exerted on the skin, decreases with increasing elevation. Therefore, the pressure is lower at higher elevations. As a result, the difference between the blood pressure in the veins and the air pressure outside increases. This pressure imbalance may cause some thin-walled veins such as the ones in the nose to burst, causing bleeding. The shortness of breath is caused by the lower air density at higher elevations, and thus lower amount of oxygen per unit volume.

1-36C No, the absolute pressure in a liquid of constant density does not double when the depth is doubled. It is the *gage pressure* that doubles when the depth is doubled.

1-37C If the lengths of the sides of the tiny cube suspended in water by a string are very small, the magnitudes of the pressures on all sides of the cube will be the same.

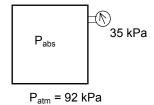
1-38C Pascal's principle states that the pressure applied to a confined fluid increases the pressure throughout by the same amount. This is a consequence of the pressure in a fluid remaining constant in the horizontal direction. An example of Pascal's principle is the operation of the hydraulic car jack.

1-39C The density of air at sea level is higher than the density of air on top of a high mountain. Therefore, the volume flow rates of the two fans running at identical speeds will be the same, but the mass flow rate of the fan at sea level will be higher.

1-40 The pressure in a vacuum chamber is measured by a vacuum gage. The absolute pressure in the chamber is to be determined.

Analysis The absolute pressure in the chamber is determined from

$$P_{\text{abs}} = P_{\text{atm}} - P_{\text{vac}} = 92 - 35 = 57 \text{ kPa}$$



1-41E The pressure in a tank is measured with a manometer by measuring the differential height of the manometer fluid. The absolute pressure in the tank is to be determined for the cases of the manometer arm with the higher and lower fluid level being attached to the tank.

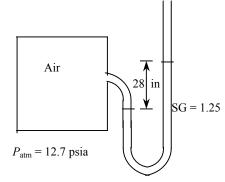
Assumptions The fluid in the manometer is incompressible.

Properties The specific gravity of the fluid is given to be SG = 1.25. The density of water at 32°F is 62.4 lbm/ft³ (Table A-3E)

Analysis The density of the fluid is obtained by multiplying its specific gravity by the density of water,

$$\rho = SG \times \rho_{H_2O} = (1.25)(62.4 \text{lbm/ft}^3) = 78.0 \text{lbm/ft}^3$$

The pressure difference corresponding to a differential height of 28 in between the two arms of the manometer is



$$\Delta P = \rho g h = (78 \,\text{lbm/ft}^3)(32.174 \,\text{ft/s}^2)(28/12 \,\text{ft}) \left(\frac{1 \,\text{lbf}}{32.174 \,\text{lbm} \cdot \text{ft/s}^2}\right) \left(\frac{1 \,\text{ft}^2}{144 \,\text{in}^2}\right) = 1.26 \,\text{psia}$$

Then the absolute pressures in the tank for the two cases become:

(a) The fluid level in the arm attached to the tank is higher (vacuum):

$$P_{\text{abs}} = P_{\text{atm}} - P_{\text{vac}} = 12.7 - 1.26 = 11.44 \text{ psia}$$

(b) The fluid level in the arm attached to the tank is lower:

$$P_{\text{abs}} = P_{\text{gage}} + P_{\text{atm}} = 12.7 + 1.26 = 13.96 \text{ psia}$$

Discussion Note that we can determine whether the pressure in a tank is above or below atmospheric pressure by simply observing the side of the manometer arm with the higher fluid level.

1-42 The pressure in a pressurized water tank is measured by a multi-fluid manometer. The gage pressure of air in the tank is to be determined.

Assumptions The air pressure in the tank is uniform (i.e., its variation with elevation is negligible due to its low density), and thus we can determine the pressure at the air-water interface.

Properties The densities of mercury, water, and oil are given to be 13,600, 1000, and 850 kg/m³, respectively.

Analysis Starting with the pressure at point 1 at the air-water interface, and moving along the tube by adding (as we go down) or subtracting (as we go up) the ρgh terms until we reach point 2, and setting the result equal to P_{atm} since the tube is open to the atmosphere gives

$$P_1 + \rho_{\text{water}} g h_1 + \rho_{\text{oil}} g h_2 - \rho_{\text{mercurv}} g h_3 = P_{atm}$$

Solving for P_1

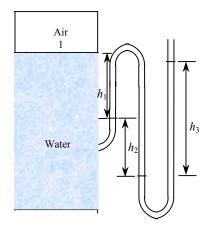
$$P_1 = P_{\text{atm}} - \rho_{\text{water}} g h_1 - \rho_{\text{oil}} g h_2 + \rho_{\text{mercurv}} g h_3$$

or,

$$P_1 - P_{\text{atm}} = g(\rho_{\text{mercury}} h_3 - \rho_{\text{water}} h_1 - \rho_{\text{oil}} h_2)$$

Noting that $P_{1,\text{gage}} = P_1 - P_{\text{atm}}$ and substituting,

$$P_{1,\text{gage}} = (9.81 \,\text{m/s}^2)[(13,600 \,\text{kg/m}^3)(0.46 \,\text{m}) - (1000 \,\text{kg/m}^3)(0.2 \,\text{m})$$
$$- (850 \,\text{kg/m}^3)(0.3 \,\text{m})] \left(\frac{1 \,\text{N}}{1 \,\text{kg} \cdot \text{m/s}^2}\right) \left(\frac{1 \,\text{kPa}}{1000 \,\text{N/m}^2}\right)$$



= 56.9 kPa

Discussion Note that jumping horizontally from one tube to the next and realizing that pressure remains the same in the same fluid simplifies the analysis greatly.

1-43 The barometric reading at a location is given in height of mercury column. The atmospheric pressure is to be determined.

Properties The density of mercury is given to be 13,600 kg/m³.

Analysis The atmospheric pressure is determined directly from

$$P_{\text{atm}} = \rho g h$$
= (13,600 kg/m³)(9.81 m/s²)(0.750 m) $\left(\frac{1 \text{ N}}{1 \text{ kg} \cdot \text{m/s}^2}\right) \left(\frac{1 \text{ kPa}}{1000 \text{ N/m}^2}\right)$
= **100.1 kPa**

1-44 The gage pressure in a liquid at a certain depth is given. The gage pressure in the same liquid at a different depth is to be determined.

Assumptions The variation of the density of the liquid with depth is negligible.

Analysis The gage pressure at two different depths of a liquid can be expressed as

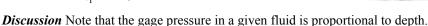
$$P_1 = \rho g h_1$$
 and $P_2 = \rho g h_2$

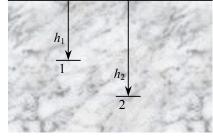
Taking their ratio,

$$\frac{P_2}{P_1} = \frac{\rho g h_2}{\rho g h_1} = \frac{h_2}{h_1}$$

Solving for P_2 and substituting gives

$$P_2 = \frac{h_2}{h_1} P_1 = \frac{9 \text{ m}}{3 \text{ m}} (28 \text{ kPa}) = 84 \text{ kPa}$$





1-45 The absolute pressure in water at a specified depth is given. The local atmospheric pressure and the absolute pressure at the same depth in a different liquid are to be determined.

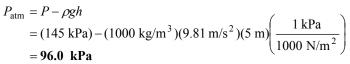
Assumptions The liquid and water are incompressible.

Properties The specific gravity of the fluid is given to be SG = 0.85. We take the density of water to be 1000 kg/m³. Then density of the liquid is obtained by multiplying its specific gravity by the density of water,

$$\rho = SG \times \rho_{H_2O} = (0.85)(1000 \text{ kg/m}^3) = 850 \text{ kg/m}^3$$

Analysis (a) Knowing the absolute pressure, the atmospheric pressure can be determined from

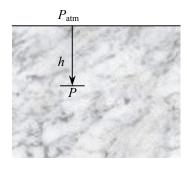
$$P_{\text{atm}} = P - \rho g h$$
= (145 kPa) - (1000 kg/m³)(9.81 m/s²)(5 m) $\left(\frac{1 \text{ kPa}}{1000 \text{ N/m}^2}\right)$



(b) The absolute pressure at a depth of 5 m in the other liquid is

$$P = P_{\text{atm}} + \rho g h$$

= (96.0 kPa) + (850 kg/m³)(9.81 m/s²)(5 m) $\left(\frac{1 \text{ kPa}}{1000 \text{ N/m}^2}\right)$
= **137.7 kPa**



Discussion Note that at a given depth, the pressure in the lighter fluid is lower, as expected.

1-46E It is to be shown that $1 \text{ kgf/cm}^2 = 14.223 \text{ psi}$.

Analysis Noting that 1 kgf = 9.80665 N, 1 N = 0.22481 lbf, and 1 in = 2.54 cm, we have

1 kgf = 9.80665 N =
$$(9.80665 \text{ N}) \left(\frac{0.22481 \text{ lbf}}{1 \text{ N}} \right) = 2.20463 \text{ lbf}$$

and

$$1 \text{ kgf/cm}^2 = 2.20463 \text{ lbf/cm}^2 = (2.20463 \text{ lbf/cm}^2) \left(\frac{2.54 \text{ cm}}{1 \text{ in}}\right)^2 = 14.223 \text{ lbf/in}^2 = \mathbf{14.223 \text{ psi}}$$

1-47E The weight and the foot imprint area of a person are given. The pressures this man exerts on the ground when he stands on one and on both feet are to be determined.

Assumptions The weight of the person is distributed uniformly on foot imprint area.

Analysis The weight of the man is given to be 200 lbf. Noting that pressure is force per unit area, the pressure this man exerts on the ground is

(a) On both feet:
$$P = \frac{W}{2A} = \frac{200 \text{ lbf}}{2 \times 36 \text{ in}^2} = 2.78 \text{ lbf/in}^2 = 2.78 \text{ psi}$$

(b) On one foot:
$$P = \frac{W}{A} = \frac{200 \text{ lbf}}{36 \text{ in}^2} = 5.56 \text{ lbf/in}^2 = 5.56 \text{ psi}$$

Discussion Note that the pressure exerted on the ground (and on the feet) is reduced by half when the person stands on both feet.



1-48 The mass of a woman is given. The minimum imprint area per shoe needed to enable her to walk on the snow without sinking is to be determined.

Assumptions 1 The weight of the person is distributed uniformly on the imprint area of the shoes. 2 One foot carries the entire weight of a person during walking, and the shoe is sized for walking conditions (rather than standing). 3 The weight of the shoes is negligible.

Analysis The mass of the woman is given to be 70 kg. For a pressure of 0.5 kPa on the snow, the imprint area of one shoe must be

$$A = \frac{W}{P} = \frac{mg}{P} = \frac{(70 \text{ kg})(9.81 \text{ m/s}^2)}{0.5 \text{ kPa}} \left(\frac{1 \text{ N}}{1 \text{ kg} \cdot \text{m/s}^2} \right) \left(\frac{1 \text{ kPa}}{1000 \text{ N/m}^2} \right) = 1.37 \text{ m}^2$$

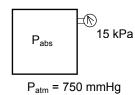
Discussion This is a very large area for a shoe, and such shoes would be impractical to use. Therefore, some sinking of the snow should be allowed to have shoes of reasonable size.

1-49 The vacuum pressure reading of a tank is given. The absolute pressure in the tank is to be determined.

Properties The density of mercury is given to be $\rho = 13,590 \text{ kg/m}^3$.

Analysis The atmospheric (or barometric) pressure can be expressed as

$$P_{\text{atm}} = \rho g h$$
= (13,590 kg/m³)(9.807 m/s²)(0.750 m) $\left(\frac{1 \text{ N}}{1 \text{ kg} \cdot \text{m/s}^2}\right) \left(\frac{1 \text{ kPa}}{1000 \text{ N/m}^2}\right)$



Then the absolute pressure in the tank becomes

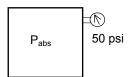
$$P_{
m abs} = P_{
m atm} - P_{
m vac} = 100.0 - 15 = {\bf 85.0 \ kPa}$$

1-50E A pressure gage connected to a tank reads 50 psi. The absolute pressure in the tank is to be determined.

Properties The density of mercury is given to be $\rho = 848.4 \text{ lbm/ft}^3$.

Analysis The atmospheric (or barometric) pressure can be expressed as

$$P_{\text{atm}} = \rho g h$$
= (848.4 lbm/ft³)(32.2 ft/s²)(29.1/12 ft) $\left(\frac{1 \text{ lbf}}{32.2 \text{ lbm} \cdot \text{ft/s}^2}\right) \left(\frac{1 \text{ ft}^2}{144 \text{ in}^2}\right)$



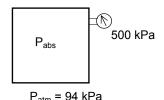
Then the absolute pressure in the tank is

$$P_{\rm abs} = P_{\rm gage} + P_{\rm atm} = 50 + 14.29 =$$
64.3 psia

1-51 A pressure gage connected to a tank reads 500 kPa. The absolute pressure in the tank is to be determined.

Analysis The absolute pressure in the tank is determined from

$$P_{\rm abs} = P_{\rm gage} + P_{\rm atm} = 500 + 94 =$$
594 kPa

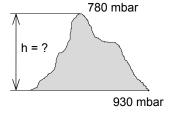


1-52 A mountain hiker records the barometric reading before and after a hiking trip. The vertical distance climbed is to be determined.

Assumptions The variation of air density and the gravitational acceleration with altitude is negligible.

Properties The density of air is given to be $\rho = 1.20 \text{ kg/m}^3$.

Analysis Taking an air column between the top and the bottom of the mountain and writing a force balance per unit base area, we obtain



$$W_{\text{air}} / A = P_{\text{bottom}} - P_{\text{top}}$$

 $(\rho g h)_{\text{air}} = P_{\text{bottom}} - P_{\text{top}}$

$$(1.20 \text{ kg/m}^3)(9.81 \text{ m/s}^2)(h) \left(\frac{1 \text{ N}}{1 \text{ kg} \cdot \text{m/s}^2}\right) \left(\frac{1 \text{ bar}}{100,000 \text{ N/m}^2}\right) = (0.930 - 0.780) \text{ bar}$$

It yields

$$h = 1274 \text{ m}$$

which is also the distance climbed.

1-53 A barometer is used to measure the height of a building by recording reading at the bottom and at the top of the building. The height of the building is to be determined.

Assumptions The variation of air density with altitude is negligible.

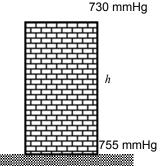
Properties The density of air is given to be $\rho = 1.18 \text{ kg/m}^3$. The density of mercury is $13,600 \text{ kg/m}^3$.

Analysis Atmospheric pressures at the top and at the bottom of the building are

$$P_{\text{top}} = (\rho g h)_{\text{top}}$$

$$= (13,600 \text{ kg/m}^3)(9.807 \text{ m/s}^2)(0.730 \text{ m}) \left(\frac{1 \text{ N}}{1 \text{ kg} \cdot \text{m/s}^2}\right) \left(\frac{1 \text{ kPa}}{1000 \text{ N/m}^2}\right)$$

$$= 97.36 \text{ kPa}$$



$$P_{\text{bottom}} = (\rho g h)_{\text{bottom}}$$
= (13,600 kg/m³)(9.807 m/s²)(0.755 m) $\left(\frac{1 \text{N}}{1 \text{kg} \cdot \text{m/s}^2}\right) \left(\frac{1 \text{ kPa}}{1000 \text{ N/m}^2}\right)$

Taking an air column between the top and the bottom of the building and writing a force balance per unit base area, we obtain

$$W_{\text{air}} / A = P_{\text{bottom}} - P_{\text{top}}$$

$$(\rho g h)_{\text{air}} = P_{\text{bottom}} - P_{\text{top}}$$

$$(1.18 \text{ kg/m}^3)(9.807 \text{ m/s}^2)(h) \left(\frac{1 \text{ N}}{1 \text{ kg} \cdot \text{m/s}^2}\right) \left(\frac{1 \text{ kPa}}{1000 \text{ N/m}^2}\right) = (100.70 - 97.36) \text{ kPa}$$

It yields

$$h = 288.6 \text{ m}$$

which is also the height of the building.

1-54 EES Problem 1-53 is reconsidered. The entire EES solution is to be printed out, including the numerical results with proper units.

Analysis The problem is solved using EES, and the solution is given below.

```
P_bottom=755"[mmHg]"
P_top=730"[mmHg]"
g=9.807 "[m/s^2]" "local acceleration of gravity at sea level"
rho=1.18"[kg/m^3]"
DELTAP_abs=(P_bottom-P_top)*CONVERT('mmHg','kPa')"[kPa]" "Delta P reading from the barometers, converted from mmHg to kPa."
DELTAP_h =rho*g*h/1000 "[kPa]" "Equ. 1-16. Delta P due to the air fluid column height, h, between the top and bottom of the building."
"Instead of dividing by 1000 Pa/kPa we could have multiplied rho*g*h by the EES function, CONVERT('Pa','kPa')"
DELTAP_abs=DELTAP_h
```

SOLUTION Variables in Main DELTAP_abs=3.333 [kPa] DELTAP_h=3.333 [kPa] g=9.807 [m/s^2] h=288 [m] P_bottom=755 [mmHg] P_top=730 [mmHg] rho=1.18 [kg/m^3]

1-55 A diver is moving at a specified depth from the water surface. The pressure exerted on the surface of the diver by water is to be determined.

Assumptions The variation of the density of water with depth is negligible.

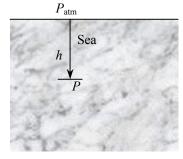
Properties The specific gravity of seawater is given to be SG = 1.03. We take the density of water to be 1000 kg/m^3 .

Analysis The density of the seawater is obtained by multiplying its specific gravity by the density of water which is taken to be 1000 kg/m³:

$$\rho = \text{SG} \times \rho_{H_2O} = (1.03)(1000 \text{ kg/m}^3) = 1030 \text{ kg/m}^3$$

The pressure exerted on a diver at 30 m below the free surface of the sea is the absolute pressure at that location:

$$P = P_{\text{atm}} + \rho g h$$
= (101 kPa) + (1030 kg/m³)(9.807 m/s²)(30 m) $\left(\frac{1 \text{ kPa}}{1000 \text{ N/m}^2}\right)$
= **404.0 kPa**



1-56E A submarine is cruising at a specified depth from the water surface. The pressure exerted on the surface of the submarine by water is to be determined.

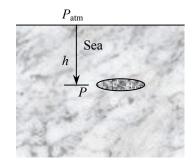
Assumptions The variation of the density of water with depth is negligible.

Properties The specific gravity of seawater is given to be SG = 1.03. The density of water at 32°F is 62.4 lbm/ft³ (Table A-3E).

Analysis The density of the seawater is obtained by multiplying its specific gravity by the density of water,

$$\rho = \text{SG} \times \rho_{\text{H},\text{O}} = (1.03)(62.4 \text{ lbm/ft}^3) = 64.27 \text{ lbm/ft}^3$$

The pressure exerted on the surface of the submarine cruising 300 ft below the free surface of the sea is the absolute pressure at that location:



$$P = P_{\text{atm}} + \rho g h$$
= (14.7 psia) + (64.27 lbm/ft³)(32.2 ft/s²)(175 ft) $\left(\frac{1 \text{ lbf}}{32.2 \text{ lbm} \cdot \text{ft/s}^2}\right) \left(\frac{1 \text{ ft}^2}{144 \text{ in}^2}\right)$
= **92.8 psia**

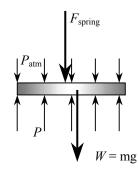
1-57 A gas contained in a vertical piston-cylinder device is pressurized by a spring and by the weight of the piston. The pressure of the gas is to be determined.

Analysis Drawing the free body diagram of the piston and balancing the vertical forces yield

$$PA = P_{\text{atm}} A + W + F_{\text{spring}}$$

Thus,

$$P = P_{\text{atm}} + \frac{mg + F_{\text{spring}}}{A}$$
= (95 kPa) + $\frac{(4 \text{ kg})(9.81 \text{ m/s}^2) + 60 \text{ N}}{35 \times 10^{-4} \text{ m}^2} \left(\frac{1 \text{ kPa}}{1000 \text{ N/m}^2} \right)$
= **123.4 kPa**

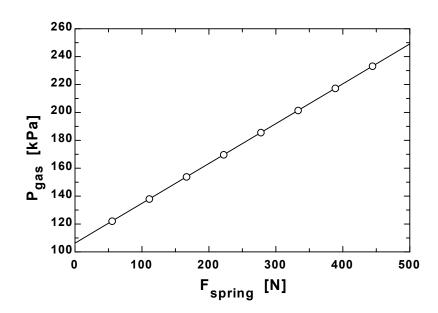


1-58 EES Problem 1-57 is reconsidered. The effect of the spring force in the range of 0 to 500 N on the pressure inside the cylinder is to be investigated. The pressure against the spring force is to be plotted, and results are to be discussed.

Analysis The problem is solved using EES, and the solution is given below.

```
g=9.807"[m/s^2]"
P_atm= 95"[kPa]"
m_piston=4"[kg]"
{F_spring=60"[N]"}
A=35*CONVERT('cm^2','m^2')"[m^2]"
W_piston=m_piston*g"[N]"
F_atm=P_atm*A*CONVERT('kPa','N/m^2')"[N]"
"From the free body diagram of the piston, the balancing vertical forces yield:"
F_gas= F_atm+F_spring+W_piston"[N]"
P_gas=F_gas/A*CONVERT('N/m^2','kPa')"[kPa]"
```

F _{spring} [N]	P _{gas} [kPa]
0	106.2
55.56	122.1
111.1	138
166.7	153.8
222.2	169.7
277.8	185.6
333.3	201.4
388.9	217.3
444.4	233.2
500	249.1



1-59 [Also solved by EES on enclosed CD] Both a gage and a manometer are attached to a gas to measure its pressure. For a specified reading of gage pressure, the difference between the fluid levels of the two arms of the manometer is to be determined for mercury and water.

Properties The densities of water and mercury are given to be $\rho_{water} = 1000 \text{ kg/m}^3$ and be $\rho_{Hg} = 13,600 \text{ kg/m}^3$.

Analysis The gage pressure is related to the vertical distance h between the two fluid levels by

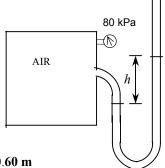
$$P_{\text{gage}} = \rho g h \longrightarrow h = \frac{P_{\text{gage}}}{\rho g}$$

(a) For mercury,

$$h = \frac{P_{\text{gage}}}{\rho_{Hg}g} = \frac{80 \text{ kPa}}{(13,600 \text{ kg/m}^3)(9.81 \text{ m/s}^2)} \left(\frac{1 \text{ kN/m}^2}{1 \text{ kPa}}\right) \left(\frac{1000 \text{ kg/m} \cdot \text{s}^2}{1 \text{ kN}}\right) = \mathbf{0.60 m}$$

(b) For water,

$$h = \frac{P_{\text{gage}}}{\rho_{\text{H}_2\text{O}}g} = \frac{80 \text{ kPa}}{(1000 \text{ kg/m}^3)(9.81 \text{ m/s}^2)} \left(\frac{1 \text{ kN/m}^2}{1 \text{ kPa}}\right) \left(\frac{1000 \text{ kg/m} \cdot \text{s}^2}{1 \text{ kN}}\right) = 8.16 \text{ m}$$



1-60 EES Problem 1-59 is reconsidered. The effect of the manometer fluid density in the range of 800 to 13,000 kg/m³ on the differential fluid height of the manometer is to be investigated. Differential fluid height against the density is to be plotted, and the results are to be discussed.

Analysis The problem is solved using EES, and the solution is given below.

Function fluid density(Fluid\$) If fluid\$='Mercury' then fluid density=13600 else fluid density=1000 end

Input from the diagram window. If the diagram window is hidden, then all of the input must come from the equations window. Also note that brackets can also denote comments - but these comments do not appear in the formatted equations window.}

{Fluid\$='Mercury'

P atm = 101.325

"kpa"

n þ

m

DELTAP=80 Window."

"kPa Note how DELTAP is displayed on the Formatted Equations

g=9.807 "m/s2, local acceleration of gravity at sea level" rho=Fluid density(Fluid\$) "Get the fluid density, either Hg or H2O, from the function" "To plot fluid height against density place {} around the above equation. Then set up the parametric table and solve."

DELTAP = RHO*g*h/1000

"Instead of dividing by 1000 Pa/kPa we could have multiplied by the EES function, CONVERT('Pa','kPa')"

h mm=h*convert('m','mm')

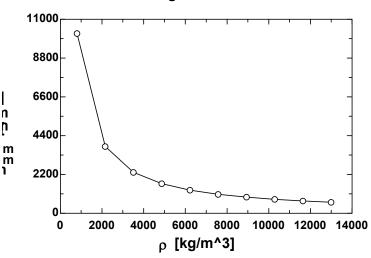
"The fluid height in mm is found using the built-in CONVERT

function."

P_abs= P_atm + DELTAP

Manometer Fluid Height vs Manometer Fluid Density

h _{mm} [mm]	ρ [kg/m³]
10197	800
3784	2156
2323	3511
1676	4867
1311	6222
1076	7578
913.1	8933
792.8	10289
700.5	11644
627.5	13000

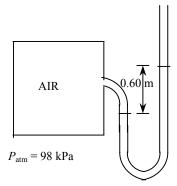


1-61 The air pressure in a tank is measured by an oil manometer. For a given oil-level difference between the two columns, the absolute pressure in the tank is to be determined.

Properties The density of oil is given to be $\rho = 850 \text{ kg/m}^3$.

Analysis The absolute pressure in the tank is determined from

$$P = P_{\text{atm}} + \rho gh$$
= (98 kPa) + (850 kg/m³)(9.81m/s²)(0.60 m) $\left(\frac{1\text{kPa}}{1000 \text{ N/m}^2}\right)$



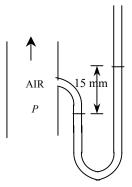
1-62 The air pressure in a duct is measured by a mercury manometer. For a given mercury-level difference between the two columns, the absolute pressure in the duct is to be determined.

Properties The density of mercury is given to be $\rho = 13,600 \text{ kg/m}^3$.

Analysis (a) The pressure in the duct is above atmospheric pressure since the fluid column on the duct side is at a lower level.

(b) The absolute pressure in the duct is determined from

$$P = P_{\text{atm}} + \rho g h$$
= (100 kPa) + (13,600 kg/m³)(9.81 m/s²)(0.015 m) $\left(\frac{1 \text{ N}}{1 \text{ kg} \cdot \text{m/s}^2}\right) \left(\frac{1 \text{ kPa}}{1000 \text{ N/m}^2}\right)$
= **102 kPa**



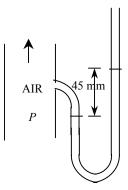
1-63 The air pressure in a duct is measured by a mercury manometer. For a given mercury-level difference between the two columns, the absolute pressure in the duct is to be determined.

Properties The density of mercury is given to be $\rho = 13,600 \text{ kg/m}^3$.

Analysis (a) The pressure in the duct is above atmospheric pressure since the fluid column on the duct side is at a lower level.

(b) The absolute pressure in the duct is determined from

$$P = P_{\text{atm}} + \rho g h$$
= (100 kPa) + (13,600 kg/m³)(9.81 m/s²)(0.045 m) $\left(\frac{1 \text{ N}}{1 \text{ kg} \cdot \text{m/s}^2}\right) \left(\frac{1 \text{ kPa}}{1000 \text{ N/m}^2}\right)$



1-64 The systolic and diastolic pressures of a healthy person are given in mmHg. These pressures are to be expressed in kPa, psi, and meter water column.

Assumptions Both mercury and water are incompressible substances.

Properties We take the densities of water and mercury to be 1000 kg/m³ and 13,600 kg/m³, respectively.

Analysis Using the relation $P = \rho g h$ for gage pressure, the high and low pressures are expressed as

$$P_{\text{high}} = \rho g h_{\text{high}} = (13,600 \text{ kg/m}^3)(9.81 \text{ m/s}^2)(0.12 \text{ m}) \left(\frac{1 \text{ N}}{1 \text{kg} \cdot \text{m/s}^2}\right) \left(\frac{1 \text{kPa}}{1000 \text{ N/m}^2}\right) = \mathbf{16.0 \text{ kPa}}$$

$$P_{\text{low}} = \rho g h_{\text{low}} = (13,600 \text{ kg/m}^3)(9.81 \text{ m/s}^2)(0.08 \text{ m}) \left(\frac{1 \text{ N}}{1 \text{kg} \cdot \text{m/s}^2}\right) \left(\frac{1 \text{kPa}}{1000 \text{ N/m}^2}\right) = \mathbf{10.7 \text{ kPa}}$$

Noting that 1 psi = 6.895 kPa,

$$P_{\text{high}} = (16.0 \,\text{Pa}) \left(\frac{1 \,\text{psi}}{6.895 \,\text{kPa}} \right) = 2.32 \,\text{psi}$$
 and $P_{\text{low}} = (10.7 \,\text{Pa}) \left(\frac{1 \,\text{psi}}{6.895 \,\text{kPa}} \right) = 1.55 \,\text{psi}$

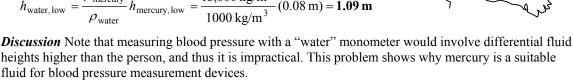
For a given pressure, the relation $P=\rho gh$ can be expressed for mercury and water as $P=\rho_{\rm water}gh_{\rm water}$ and $P=\rho_{\rm mercury}gh_{\rm mercury}$. Setting these two relations equal to each other and solving for water height gives

$$P = \rho_{\text{water}} g h_{\text{water}} = \rho_{\text{mercury}} g h_{\text{mercury}}$$
 \rightarrow $h_{\text{water}} = \frac{\rho_{\text{mercury}}}{\rho_{\text{water}}} h_{\text{mercury}}$

Therefore,

$$h_{\text{water, high}} = \frac{\rho_{\text{mercury}}}{\rho_{\text{water}}} h_{\text{mercury, high}} = \frac{13,600 \text{ kg/m}^3}{1000 \text{ kg/m}^3} (0.12 \text{ m}) = \mathbf{1.63 m}$$

$$h_{\text{water, low}} = \frac{\rho_{\text{mercury}}}{\rho_{\text{water}}} h_{\text{mercury, low}} = \frac{13,600 \text{ kg/m}^3}{1000 \text{ kg/m}^3} (0.08 \text{ m}) = \mathbf{1.09 m}$$



1-65 A vertical tube open to the atmosphere is connected to the vein in the arm of a person. The height that the blood will rise in the tube is to be determined.

Assumptions 1 The density of blood is constant. 2 The gage pressure of blood is 120 mmHg.

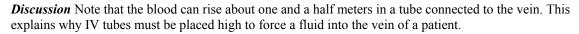
Properties The density of blood is given to be $\rho = 1050 \text{ kg/m}^3$.

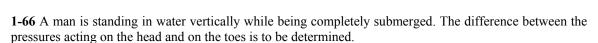
Analysis For a given gage pressure, the relation $P = \rho g h$ can be expressed for mercury and blood as $P = \rho_{\rm blood} g h_{\rm blood}$ and $P = \rho_{\rm mercury} g h_{\rm mercury}$. Setting these two relations equal to each other we get

$$P = \rho_{\text{blood}} g h_{\text{blood}} = \rho_{\text{mercury}} g h_{\text{mercury}}$$

Solving for blood height and substituting gives

$$h_{\text{blood}} = \frac{\rho_{\text{mercury}}}{\rho_{\text{blood}}} h_{\text{mercury}} = \frac{13,600 \text{ kg/m}^3}{1050 \text{ kg/m}^3} (0.12 \text{ m}) = 1.55 \text{ m}$$





Assumptions Water is an incompressible substance, and thus the density does not change with depth.

Properties We take the density of water to be $\rho = 1000 \text{ kg/m}^3$.

Analysis The pressures at the head and toes of the person can be expressed as

$$P_{\text{head}} = P_{\text{atm}} + \rho g h_{\text{head}}$$
 and $P_{\text{toe}} = P_{\text{atm}} + \rho g h_{\text{toe}}$

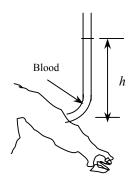
where h is the vertical distance of the location in water from the free surface. The pressure difference between the toes and the head is determined by subtracting the first relation above from the second,

$$P_{\text{toe}} - P_{\text{head}} = \rho g h_{\text{toe}} - \rho g h_{\text{head}} = \rho g (h_{\text{toe}} - h_{\text{head}})$$

Substituting,

$$P_{\text{toe}} - P_{\text{head}} = (1000 \text{ kg/m}^3)(9.81 \text{ m/s}^2)(1.80 \text{ m} - 0) \left(\frac{1 \text{ N}}{1 \text{kg} \cdot \text{m/s}^2}\right) \left(\frac{1 \text{kPa}}{1000 \text{ N/m}^2}\right) = 17.7 \text{ kPa}$$

Discussion This problem can also be solved by noting that the atmospheric pressure (1 atm = 101.325 kPa) is equivalent to 10.3-m of water height, and finding the pressure that corresponds to a water height of 1.8 m.

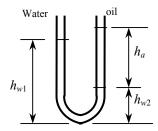


1-67 Water is poured into the U-tube from one arm and oil from the other arm. The water column height in one arm and the ratio of the heights of the two fluids in the other arm are given. The height of each fluid in that arm is to be determined.

Assumptions Both water and oil are incompressible substances.

Properties The density of oil is given to be $\rho = 790 \text{ kg/m}^3$. We take the density of water to be $\rho = 1000 \text{ kg/m}^3$.

Analysis The height of water column in the left arm of the monometer is given to be $h_{\rm w1}=0.70$ m. We let the height of water and oil in the right arm to be $h_{\rm w2}$ and $h_{\rm a}$, respectively. Then, $h_{\rm a}=4h_{\rm w2}$. Noting that both arms are open to the atmosphere, the pressure at the bottom of the U-tube can be expressed as



$$P_{\text{bottom}} = P_{\text{atm}} + \rho_{\text{w}} g h_{\text{w}1}$$
 and $P_{\text{bottom}} = P_{\text{atm}} + \rho_{\text{w}} g h_{\text{w}2} + \rho_{\text{a}} g h_{\text{a}}$

Setting them equal to each other and simplifying,

$$\rho_{\mathbf{w}}gh_{\mathbf{w}1} = \rho_{\mathbf{w}}gh_{\mathbf{w}2} + \rho_{\mathbf{a}}gh_{\mathbf{a}} \qquad \rightarrow \qquad \rho_{\mathbf{w}}h_{\mathbf{w}1} = \rho_{\mathbf{w}}h_{\mathbf{w}2} + \rho_{\mathbf{a}}h_{\mathbf{a}} \qquad \rightarrow \qquad h_{\mathbf{w}1} = h_{\mathbf{w}2} + (\rho_{\mathbf{a}}/\rho_{\mathbf{w}})h_{\mathbf{a}}$$

Noting that $h_a = 4h_{w2}$, the water and oil column heights in the second arm are determined to be

$$0.7 \text{ m} = h_{w2} + (790/1000) 4h_{w2} \rightarrow h_{w2} = 0.168 m$$

 $0.7 \text{ m} = 0.168 \text{ m} + (790/1000)h_a \rightarrow h_a = 0.673 m$

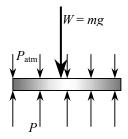
Discussion Note that the fluid height in the arm that contains oil is higher. This is expected since oil is lighter than water.

1-68 The hydraulic lift in a car repair shop is to lift cars. The fluid gage pressure that must be maintained in the reservoir is to be determined.

Assumptions The weight of the piston of the lift is negligible.

Analysis Pressure is force per unit area, and thus the gage pressure required is simply the ratio of the weight of the car to the area of the lift,

$$P_{\text{gage}} = \frac{W}{A} = \frac{mg}{\pi D^2 / 4}$$
$$= \frac{(2000 \text{ kg})(9.81 \text{ m/s}^2)}{\pi (0.30 \text{ m})^2 / 4} \left(\frac{1 \text{ kN}}{1000 \text{ kg} \cdot \text{m/s}^2}\right) = 278 \text{ kN/m}^2 = 278 \text{ kPa}$$



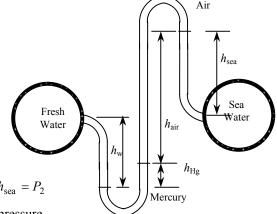
Discussion Note that the pressure level in the reservoir can be reduced by using a piston with a larger area.

1-69 Fresh and seawater flowing in parallel horizontal pipelines are connected to each other by a double U-tube manometer. The pressure difference between the two pipelines is to be determined.

Assumptions 1 All the liquids are incompressible. 2 The effect of air column on pressure is negligible.

Properties The densities of seawater and mercury are given to be $\rho_{\text{sea}} = 1035 \text{ kg/m}^3$ and $\rho_{\text{Hg}} = 13,600 \text{ kg/m}^3$. We take the density of water to be $\rho_{\text{w}} = 1000 \text{ kg/m}^3$.

Analysis Starting with the pressure in the fresh water pipe (point 1) and moving along the tube by adding (as we go down) or subtracting (as we go up) the ρgh terms until we reach the sea water pipe (point 2), and setting the result equal to P_2 gives



$$P_1 + \rho_{\rm w} g h_w - \rho_{\rm Hg} g h_{\rm Hg} - \rho_{\rm air} g h_{\rm air} + \rho_{\rm sea} g h_{\rm sea} = P_2$$

Rearranging and neglecting the effect of air column on pressure,

$$P_1 - P_2 = -\rho_{\rm w} g h_{\rm w} + \rho_{\rm Hg} g h_{\rm Hg} - \rho_{\rm sea} g h_{\rm sea} = g(\rho_{\rm Hg} h_{\rm Hg} - \rho_{\rm w} h_{\rm w} - \rho_{\rm sea} h_{\rm sea})$$

Substituting,

$$P_1 - P_2 = (9.81 \,\mathrm{m/s^2})[(13600 \,\mathrm{kg/m^3})(0.1 \,\mathrm{m})$$

$$- (1000 \,\mathrm{kg/m^3})(0.6 \,\mathrm{m}) - (1035 \,\mathrm{kg/m^3})(0.4 \,\mathrm{m})] \left(\frac{1 \,\mathrm{kN}}{1000 \,\mathrm{kg \cdot m/s^2}}\right)$$

$$= 3.39 \,\mathrm{kN/m^2} = 3.39 \,\mathrm{kPa}$$

Therefore, the pressure in the fresh water pipe is 3.39 kPa higher than the pressure in the sea water pipe.

Discussion A 0.70-m high air column with a density of 1.2 kg/m³ corresponds to a pressure difference of 0.008 kPa. Therefore, its effect on the pressure difference between the two pipes is negligible.

1-70 Fresh and seawater flowing in parallel horizontal pipelines are connected to each other by a double U-tube manometer. The pressure difference between the two pipelines is to be determined.

Assumptions All the liquids are incompressible.

Properties The densities of seawater and mercury are given to be $\rho_{\text{sea}} = 1035 \text{ kg/m}^3$ and $\rho_{\text{Hg}} = 13,600 \text{ kg/m}^3$. We take the density of water to be $\rho_{\text{w}} = 1000 \text{ kg/m}^3$. The specific gravity of oil is given to be 0.72, and thus its density is 720 kg/m^3 .

Analysis Starting with the pressure in the fresh water pipe (point 1) and moving along the tube by adding (as we go down) or subtracting (as we go up) the ρgh terms until we reach the sea water pipe (point 2), and setting the result equal to P_2 gives

$$P_1 + \rho_{\rm w}gh_{\rm w} - \rho_{\rm Hg}gh_{\rm Hg} - \rho_{\rm oil}gh_{\rm oil} + \rho_{\rm sea}gh_{\rm sea} = P_2$$

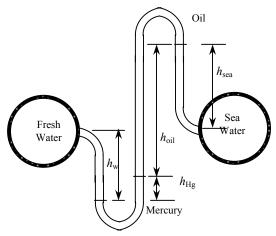
Rearranging,

$$P_1 - P_2 = -\rho_w g h_w + \rho_{Hg} g h_{Hg} + \rho_{oil} g h_{oil} - \rho_{sea} g h_{sea}$$
$$= g (\rho_{Hg} h_{Hg} + \rho_{oil} h_{oil} - \rho_w h_w - \rho_{sea} h_{sea})$$

Substituting,

$$P_1 - P_2 = (9.81 \,\mathrm{m/s^2})[(13600 \,\mathrm{kg/m^3})(0.1 \,\mathrm{m}) + (720 \,\mathrm{kg/m^3})(0.7 \,\mathrm{m}) - (1000 \,\mathrm{kg/m^3})(0.6 \,\mathrm{m})$$
$$- (1035 \,\mathrm{kg/m^3})(0.4 \,\mathrm{m})] \left(\frac{1 \,\mathrm{kN}}{1000 \,\mathrm{kg \cdot m/s^2}}\right)$$
$$= 8.34 \,\mathrm{kN/m^2} = \mathbf{8.34 \,\mathrm{kPa}}$$

Therefore, the pressure in the fresh water pipe is 8.34 kPa higher than the pressure in the sea water pipe.



1-71E The pressure in a natural gas pipeline is measured by a double U-tube manometer with one of the arms open to the atmosphere. The absolute pressure in the pipeline is to be determined.

Assumptions 1 All the liquids are incompressible. 2 The effect of air column on pressure is negligible. 3 The pressure throughout the natural gas (including the tube) is uniform since its density is low.

Properties We take the density of water to be $\rho_{\rm w}$ = 62.4 lbm/ft³. The specific gravity of mercury is given to be 13.6, and thus its density is $\rho_{\rm Hg}$ = 13.6×62.4 = 848.6 lbm/ft³.

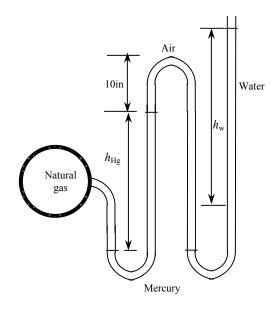
Analysis Starting with the pressure at point 1 in the natural gas pipeline, and moving along the tube by adding (as we go down) or subtracting (as we go up) the ρgh terms until we reach the free surface of oil where the oil tube is exposed to the atmosphere, and setting the result equal to $P_{\rm atm}$ gives

$$P_1 - \rho_{\rm Hg} g h_{\rm Hg} - \rho_{\rm water} g h_{\rm water} = P_{atm}$$

Solving for P_1

$$P_1 = P_{\text{atm}} + \rho_{\text{Hg}} g h_{\text{Hg}} + \rho_{\text{water}} g h_1$$

Substituting,



$$P = 14.2 \text{ psia} + (32.2 \text{ ft/s}^2) [(848.6 \text{ lbm/ft}^3)(6/12 \text{ ft}) + (62.4 \text{ lbm/ft}^3)(27/12 \text{ ft})] \left(\frac{1 \text{ lbf}}{32.2 \text{ lbm} \cdot \text{ft/s}^2}\right) \left(\frac{1 \text{ ft}^2}{144 \text{ in}^2}\right)$$

$$= 18.1 \text{psia}$$

Discussion Note that jumping horizontally from one tube to the next and realizing that pressure remains the same in the same fluid simplifies the analysis greatly. Also, it can be shown that the 15-in high air column with a density of 0.075 lbm/ft³ corresponds to a pressure difference of 0.00065 psi. Therefore, its effect on the pressure difference between the two pipes is negligible.

1-72E The pressure in a natural gas pipeline is measured by a double U-tube manometer with one of the arms open to the atmosphere. The absolute pressure in the pipeline is to be determined.

Assumptions 1 All the liquids are incompressible. 2 The pressure throughout the natural gas (including the tube) is uniform since its density is low.

Properties We take the density of water to be $\rho_{\rm w} = 62.4$ lbm/ft³. The specific gravity of mercury is given to be 13.6, and thus its density is $\rho_{\rm Hg} = 13.6 \times 62.4 = 848.6$ lbm/ft³. The specific gravity of oil is given to be 0.69, and thus its density is $\rho_{\rm oil} = 0.69 \times 62.4 = 43.1$ lbm/ft³.

Analysis Starting with the pressure at point 1 in the natural gas pipeline, and moving along the tube by adding (as we go down) or subtracting (as we go up) the ρgh terms until we reach the free surface of oil where the oil tube is exposed to the atmosphere, and setting the result equal to $P_{\rm atm}$ gives

$$P_1 - \rho_{\rm Hg} g h_{\rm Hg} + \rho_{\rm oil} g h_{\rm oil} - \rho_{\rm water} g h_{\rm water} = P_{atm}$$

Solving for P_1

$$P_1 = P_{\text{atm}} + \rho_{\text{Hg}} g h_{\text{Hg}} + \rho_{\text{water}} g h_1 - \rho_{\text{oil}} g h_{\text{oil}}$$

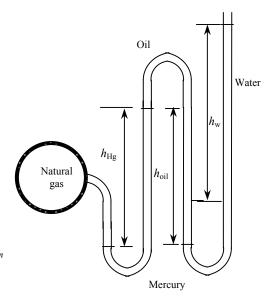
Substituting.

$$P_1 = 14.2 \text{ psia} + (32.2 \text{ ft/s}^2)[(848.6 \text{ lbm/ft}^3)(6/12 \text{ ft}) + (62.4 \text{ lbm/ft}^3)(27/12 \text{ ft})]$$

$$-(43.1 \text{ lbm/ft}^3)(15/12 \text{ ft})] \left(\frac{1 \text{ lbf}}{32.2 \text{ lbm} \cdot \text{ft/s}^2}\right) \left(\frac{1 \text{ ft}^2}{144 \text{ in}^2}\right)$$

$$= 17.7 \text{psia}$$

Discussion Note that jumping horizontally from one tube to the next and realizing that pressure remains the same in the same fluid simplifies the analysis greatly.



1-73 The gage pressure of air in a pressurized water tank is measured simultaneously by both a pressure gage and a manometer. The differential height h of the mercury column is to be determined.

Assumptions The air pressure in the tank is uniform (i.e., its variation with elevation is negligible due to its low density), and thus the pressure at the air-water interface is the same as the indicated gage pressure.

Properties We take the density of water to be $\rho_w = 1000 \text{ kg/m}^3$. The specific gravities of oil and mercury are given to be 0.72 and 13.6, respectively.

Analysis Starting with the pressure of air in the tank (point 1), and moving along the tube by adding (as we go down) or subtracting (as we go up) the ρgh terms until we reach the free surface of oil where the oil tube is exposed to the atmosphere, and setting the result equal to P_{atm} gives

$$P_1 + \rho_{\rm w} g h_w - \rho_{\rm Hg} g h_{\rm Hg} - \rho_{\rm oil} g h_{\rm oil} = P_{atm}$$

Rearranging,

$$P_1 - P_{\text{atm}} = \rho_{\text{oil}} g h_{\text{oil}} + \rho_{\text{Hg}} g h_{\text{Hg}} - \rho_{\text{w}} g h_{\text{w}}$$

or,

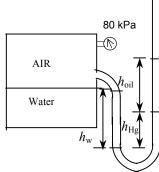
$$\frac{P_{1,\text{gage}}}{\rho_{\text{w}}g} = \text{SG}_{\text{oil}}h_{\text{oil}} + \text{SG}_{\text{Hg}}h_{\text{Hg}} - h_{w}$$

Substituting,

$$\left(\frac{80 \text{ kPa}}{(1000 \text{ kg/m}^3)(9.81 \text{ m/s}^2)}\right) \left(\frac{1000 \text{ kg} \cdot \text{m/s}^2}{1 \text{ kPa} \cdot \text{m}^2}\right) = 0.72 \times (0.75 \text{ m}) + 13.6 \times h_{\text{Hg}} - 0.3 \text{ m}$$

Solving for h_{Hg} gives $h_{\text{Hg}} = 0.582$ m. Therefore, the differential height of the mercury column must be 58.2 cm.

Discussion Double instrumentation like this allows one to verify the measurement of one of the instruments by the measurement of another instrument.



1-74 The gage pressure of air in a pressurized water tank is measured simultaneously by both a pressure gage and a manometer. The differential height h of the mercury column is to be determined.

Assumptions The air pressure in the tank is uniform (i.e., its variation with elevation is negligible due to its low density), and thus the pressure at the air-water interface is the same as the indicated gage pressure.

Properties We take the density of water to be $\rho_{\rm w} = 1000 \text{ kg/m}^3$. The specific gravities of oil and mercury are given to be 0.72 and 13.6, respectively.

Analysis Starting with the pressure of air in the tank (point 1), and moving along the tube by adding (as we go down) or subtracting (as we go up) the ρgh terms until we reach the free surface of oil where the oil tube is exposed to the atmosphere, and setting the result equal to P_{atm} gives

$$P_1 + \rho_{\rm w} g h_w - \rho_{\rm Hg} g h_{\rm Hg} - \rho_{\rm oil} g h_{\rm oil} = P_{atm}$$

Rearranging,

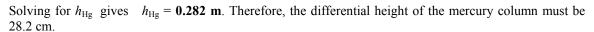
$$P_1 - P_{\text{atm}} = \rho_{\text{oil}} g h_{\text{oil}} + \rho_{\text{Hg}} g h_{\text{Hg}} - \rho_{\text{w}} g h_{\text{w}}$$

or,

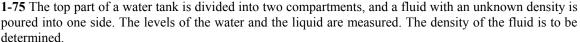
$$\frac{P_{1,\text{gage}}}{\rho_{\text{w}}g} = \text{SG}_{\text{oil}}h_{\text{oil}} + \text{SG}_{\text{Hg}}h_{\text{Hg}} - h_{\text{w}}$$

Substituting,

$$\left[\frac{40 \text{ kPa}}{(1000 \text{ kg/m}^3)(9.81 \text{ m/s}^2)}\right] \left(\frac{1000 \text{ kg} \cdot \text{m/s}^2}{1 \text{ kPa} \cdot \text{m}^2}\right) = 0.72 \times (0.75 \text{ m}) + 13.6 \times h_{\text{Hg}} - 0.3 \text{ m}$$



Discussion Double instrumentation like this allows one to verify the measurement of one of the instruments by the measurement of another instrument.



Assumptions 1 Both water and the added liquid are incompressible substances. **2** The added liquid does not mix with water.

Properties We take the density of water to be $\rho = 1000 \text{ kg/m}^3$.

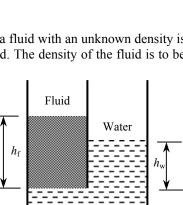
Analysis Both fluids are open to the atmosphere. Noting that the pressure of both water and the added fluid is the same at the contact surface, the pressure at this surface can be expressed as

$$P_{\rm contact} = P_{\rm atm} + \rho_{\rm f} \, g h_{\rm f} = P_{\rm atm} + \rho_{\rm w} \, g h_{\rm w}$$

Simplifying and solving for ρ_f gives

$$\rho_f g h_f = \rho_w g h_w \rightarrow \rho_f = \frac{h_w}{h_f} \rho_w = \frac{45 \text{ cm}}{80 \text{ cm}} (1000 \text{ kg/m}^3) = 562.5 \text{ kg/m}^3$$

Discussion Note that the added fluid is lighter than water as expected (a heavier fluid would sink in water).



AIR

Water

1-76 A double-fluid manometer attached to an air pipe is considered. The specific gravity of one fluid is known, and the specific gravity of the other fluid is to be determined.

Assumptions 1 Densities of liquids are constant. 2 The air pressure in the tank is uniform (i.e., its variation with elevation is negligible due to its low density), and thus the pressure at the air-water interface is the same as the indicated gage pressure.

Properties The specific gravity of one fluid is given to be 13.55. We take the standard density of water to be 1000 kg/m^3 .

Analysis Starting with the pressure of air in the tank, and moving along the tube by adding (as we go down) or subtracting (as we go up) the ρgh terms until we reach the free surface where the oil tube is exposed to the atmosphere, and setting the result equal to P_{atm} give

Fluid 1

$$SG_1$$
 SG_2
 SG_2

$$P_{\rm air} + \rho_1 g h_1 - \rho_2 g h_2 = P_{\rm atm} \qquad \rightarrow \qquad P_{\rm air} - P_{\rm atm} = SG_2 \rho_{\rm w} g h_2 - SG_1 \rho_{\rm w} g h_1$$

Rearranging and solving for SG₂.

$$SG_2 = SG_1 \frac{h_1}{h_2} + \frac{P_{air} - P_{atm}}{\rho_w gh_2} = 13.55 \frac{0.22 \text{ m}}{0.40 \text{ m}} + \left(\frac{76 - 100 \text{ kPa}}{(1000 \text{ kg/m}^3)(9.81 \text{ m/s}^2)(0.40 \text{ m})} \right) \left(\frac{1000 \text{ kg} \cdot \text{m/s}^2}{1 \text{ kPa} \cdot \text{m}^2}\right) = \mathbf{5.0}$$

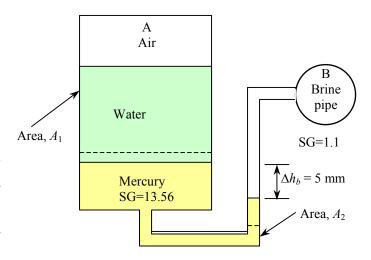
Discussion Note that the right fluid column is higher than the left, and this would imply above atmospheric pressure in the pipe for a single-fluid manometer.

1-77 The fluid levels in a multi-fluid U-tube manometer change as a result of a pressure drop in the trapped air space. For a given pressure drop and brine level change, the area ratio is to be determined.

Assumptions 1 All the liquids are incompressible. 2 Pressure in the brine pipe remains constant. 3 The variation of pressure in the trapped air space is negligible.

Properties The specific gravities are given to be 13.56 for mercury and 1.1 for brine. We take the standard density of water to be $\rho_w = 1000 \text{ kg/m}^3$.

Analysis It is clear from the problem statement and the figure that the brine pressure is much higher than the air pressure, and when the air pressure drops by 0.7 kPa, the pressure difference between the brine and the air space increases also by the same amount.



Starting with the air pressure (point A) and moving along the tube by adding (as we go down) or subtracting (as we go up) the ρgh terms until we reach the brine pipe (point B), and setting the result equal to P_B before and after the pressure change of air give

Before:
$$P_{A1} + \rho_{\text{w}} g h_{\text{w}} + \rho_{\text{Hg}} g h_{\text{Hg},1} - \rho_{\text{br}} g h_{\text{br},1} = P_B$$

After:
$$P_{A2} + \rho_{w} g h_{w} + \rho_{Hg} g h_{Hg,2} - \rho_{br} g h_{br,2} = P_{B}$$

Subtracting,

$$P_{A2} - P_{A1} + \rho_{Hg} g \Delta h_{Hg} - \rho_{br} g \Delta h_{br} = 0 \quad \to \quad \frac{P_{A1} - P_{A2}}{\rho_{w} g} = SG_{Hg} \Delta h_{Hg} - SG_{br} \Delta h_{br} = 0$$
 (1)

where $\Delta h_{\rm Hg}$ and $\Delta h_{\rm br}$ are the changes in the differential mercury and brine column heights, respectively, due to the drop in air pressure. Both of these are positive quantities since as the mercury-brine interface drops, the differential fluid heights for both mercury and brine increase. Noting also that the volume of mercury is constant, we have $A_1 \Delta h_{\rm Hg,left} = A_2 \Delta h_{\rm Hg,right}$ and

$$\begin{split} P_{A2} - P_{A1} &= -0.7 \text{ kPa} = -700 \text{ N/m}^2 = -700 \text{ kg/m} \cdot \text{s}^2 \\ \Delta h_{\text{br}} &= 0.005 \text{ m} \\ \Delta h_{\text{Hg}} &= \Delta h_{\text{Hg,right}} + \Delta h_{\text{Hg,left}} = \Delta h_{\text{br}} + \Delta h_{\text{br}} A_2 / A_1 = \Delta h_{\text{br}} (1 + A_2 / A_1) \end{split}$$

Substituting,

$$\frac{700 \text{ kg/m} \cdot \text{s}^2}{(1000 \text{ kg/m}^3)(9.81 \text{ m/s}^2)} = [13.56 \times 0.005(1 + A_2/A_1) - (1.1 \times 0.005)] \text{ m}$$

It gives

$$A_2/A_1 = \mathbf{0.134}$$

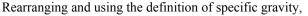
1-78 A multi-fluid container is connected to a U-tube. For the given specific gravities and fluid column heights, the gage pressure at A and the height of a mercury column that would create the same pressure at A are to be determined.

Assumptions 1 All the liquids are incompressible. 2 The multi-fluid container is open to the atmosphere.

Properties The specific gravities are given to be 1.26 for glycerin and 0.90 for oil. We take the standard density of water to be $\rho_w = 1000 \text{ kg/m}^3$, and the specific gravity of mercury to be 13.6.

Analysis Starting with the atmospheric pressure on the top surface of the container and moving along the tube by adding (as we go down) or subtracting (as we go up) the ρgh terms until we reach point A, and setting the result equal to P_A give

$$P_{\text{atm}} + \rho_{\text{oil}} g h_{\text{oil}} + \rho_{\text{w}} g h_{\text{w}} - \rho_{\text{gly}} g h_{\text{gly}} = P_{\text{A}}$$



$$P_{\rm A} - P_{\rm atm} = SG_{\rm oil} \rho_w g h_{\rm oil} + SG_w \rho_w g h_w - SG_{\rm gly} \rho_w g h_{\rm gly}$$

or

$$P_{A,\text{gage}} = g\rho_w(SG_{\text{oil}}h_{\text{oil}} + SG_wh_w - SG_{\text{gly}}h_{\text{gly}})$$

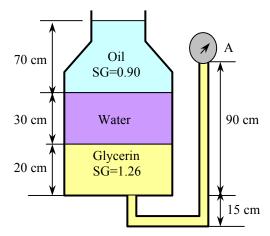
Substituting,

$$P_{\text{A,gage}} = (9.81 \,\text{m/s}^2)(1000 \,\text{kg/m}^3)[0.90(0.70 \,\text{m}) + 1(0.3 \,\text{m}) - 1.26(0.70 \,\text{m})] \left(\frac{1 \,\text{kN}}{1000 \,\text{kg} \cdot \text{m/s}^2}\right)$$
$$= 0.471 \,\text{kN/m}^2 = \textbf{0.471 \,\text{kPa}}$$

The equivalent mercury column height is

$$h_{\rm Hg} = \frac{P_{\rm A,gage}}{\rho_{\rm Hg}g} = \frac{0.471 \, \rm kN/m^2}{(13.6)(1000 \, \rm kg/m^3)(9.81 \, m/s^2)} \left(\frac{1000 \, \rm kg \cdot m/s^2}{1 \, \rm kN}\right) = 0.00353 \, \rm m = 0.353 \, cm$$

Discussion Note that the high density of mercury makes it a very suitable fluid for measuring high pressures in manometers.



Solving Engineering Problems and EES

1-79C Despite the convenience and capability the engineering software packages offer, they are still just tools, and they will not replace the traditional engineering courses. They will simply cause a shift in emphasis in the course material from mathematics to physics. They are of great value in engineering practice, however, as engineers today rely on software packages for solving large and complex problems in a short time, and perform optimization studies efficiently.

1-80 EES Determine a positive real root of the following equation using EES:

$$2x^3 - 10x^{0.5} - 3x = -3$$

Solution by EES Software (Copy the following line and paste on a blank EES screen to verify solution):

$$2*x^3-10*x^0.5-3*x = -3$$

Answer: x = 2.063 (using an initial guess of x=2)

1-81 EES Solve the following system of 2 equations with 2 unknowns using EES:

$$x^3 - y^2 = 7.75$$

 $3xy + y = 3.5$

Solution by EES Software (Copy the following lines and paste on a blank EES screen to verify solution):

$$3*x*y+y=3.5$$

Answer x=2 y=0.5

1-82 EES Solve the following system of 3 equations with 3 unknowns using EES:

$$2x - y + z = 5$$

 $3x^2 + 2y = z + 2$

$$3x^{2} + 2y = z +$$

$$xy + 2z = 8$$

Solution by EES Software (Copy the following lines and paste on a blank EES screen to verify solution):

$$2*x-v+z=5$$

$$3*x^2+2*y=z+2$$

$$x*v+2*z=8$$

Answer x=1.141, y=0.8159, z=3.535

1-83 EES Solve the following system of 3 equations with 3 unknowns using EES:

$$x^{2}y - z = 1$$

 $x - 3y^{0.5} + xz = -2$
 $x + y - z = 2$

Solution by EES Software (Copy the following lines and paste on a blank EES screen to verify solution):

$$x^2*v-z=1$$

$$x-3*y^0.5+x*z=-2$$

$$x+y-z=2$$

Answer x=1, y=1, z=0

1-84E EES Specific heat of water is to be expressed at various units using unit conversion capability of EES.

Analysis The problem is solved using EES, and the solution is given below.

EQUATION WINDOW

"GIVEN"

 $C_p=4.18 [kJ/kg-C]$

"ANALYSIS"

C_p_1=C_p*Convert(kJ/kg-C, kJ/kg-K)

C_p_2=C_p*Convert(kJ/kg-C, Btu/lbm-F)

C_p_3=C_p*Convert(kJ/kg-C, Btu/lbm-R)

C_p_4=C_p*Convert(kJ/kg-C, kCal/kg-C)

FORMATTED EQUATIONS WINDOW

GIVEN

$$C_p = 4.18 [kJ/kg-C]$$

ANALYSIS

$$C_{p,1} = C_p \cdot \left| 1 \cdot \frac{kJ/kg - K}{kJ/kg - C} \right|$$

$$C_{p,2} = C_p \cdot \left| 0.238846 \cdot \frac{Btu/lbm - F}{kJ/kg - C} \right|$$

$$C_{p,3} = C_p \cdot \left[0.238846 \cdot \frac{Btu/lbm-R}{kJ/kg-C} \right]$$

$$C_{p,4} = C_p \cdot \left[0.238846 \cdot \frac{\text{kCal/kg-C}}{\text{kJ/kg-C}} \right]$$

SOLUTION WINDOW

C_p=4.18 [kJ/kg-C]

C_p_1=4.18 [kJ/kg-K]

C_p_2=0.9984 [Btu/lbm-F]

C_p_3=0.9984 [Btu/lbm-R]

C_p_4=0.9984 [kCal/kg-C]