

## **Examination Heat Transfer**

code: 4B680

date: 2 February 2007

time: 14.00 - 17.00 hours

### **Note:**

There are 4 questions in total. The first one consists of independent sub-questions. If possible and necessary, guide numbers are given for the answers.

Good luck

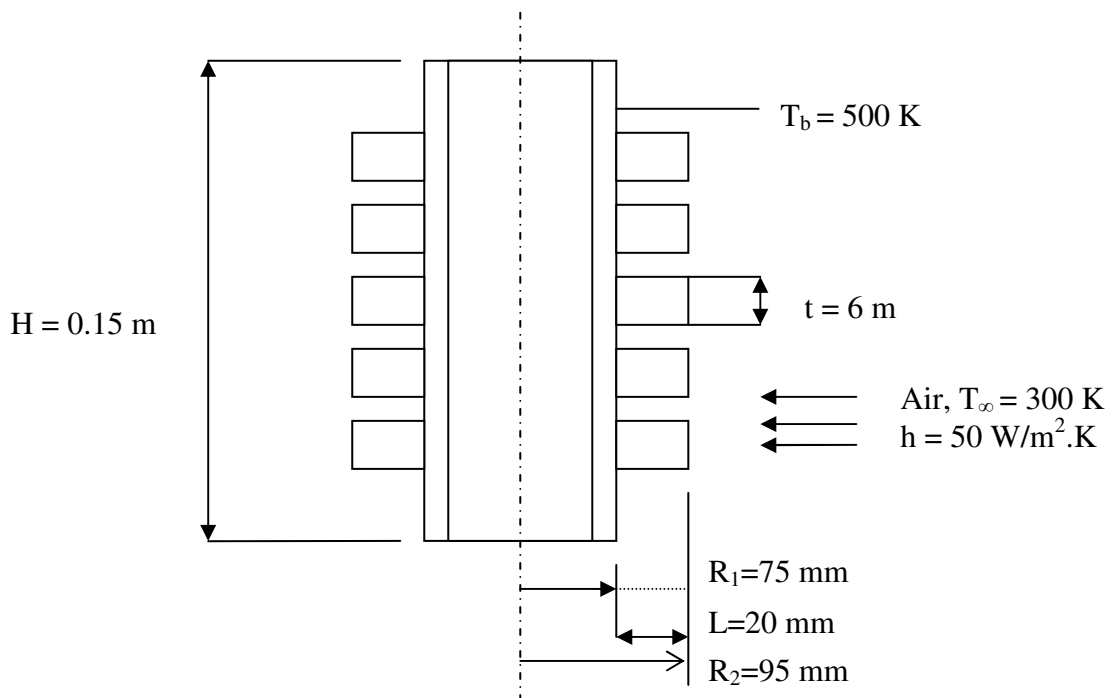
**Question 1** (all sub-questions can be solved independently)

- a) A 10 cm thick slab of aluminum at a uniform temperature of  $200^{\circ}\text{C}$  is submerged in a bath of oil at a temperature of  $70^{\circ}\text{C}$ . The heat transfer from the slab to the oil can be described by a convection coefficient which is assumed to be infinitely large. One is interested in the temperature distribution in the slab as a function of time. Give an estimation of the time interval over which the temperature distribution in the slab can be calculated using the semi-infinite solid approach. Errors large than  $5^{\circ}\text{C}$  are not allowed. Aluminum has the following properties:  $\rho = 2707 \text{ kg/m}^3$ ;  $c_p = 896 \text{ J/kg.K}$ ;  $k = 204 \text{ W/m.K}$ .
- b) Water at  $20^{\circ}\text{C}$  and a mass flow rate of  $0.1 \text{ kg/s}$  enters a pipe with an inner diameter of 2 cm and a length of 2 m. A constant heat flux is imposed on the tube wall of  $5000 \text{ W/m}$ . Calculate the exit temperature of the water and the wall. The water properties can be evaluated at a temperature of about  $20^{\circ}\text{C}$ . The flow is supposed to be hydrodynamically and thermally fully developed.
- c) Water at a mass flow rate of  $68 \text{ kg/min}$  is heated from  $35$  to  $75^{\circ}\text{C}$  by oil having a specific heat of  $1.9 \text{ kJ/kg}^{\circ}\text{C}$ . The fluids are used in a shell-and-tube heat exchanger with the water making one shell pass and the oil making two tube passes. The oil enters the exchanger at  $110^{\circ}\text{C}$  and leaves at  $75^{\circ}\text{C}$ . The overall heat transfer coefficient is  $320 \text{ W/m}^2\text{.K}$ . Calculate the heat exchanger area.

**Question 2** (all sub-questions can be solved independently)

The engine of a motorcycle consists of a metal cylinder with a heat conduction coefficient equal to  $k = 186 \text{ W/m.K}$ . The cylinder has a height of  $H = 0.15 \text{ m}$  and an outside diameter of  $D = 150 \text{ mm}$ . Under typical operating conditions the outer surface of the cylinder is at a temperature of  $500 \text{ K}$  and exposed to ambient air at  $300 \text{ K}$  and a convection coefficient of  $50 \text{ W/m}^2.\text{K}$ . Circumferential fins with a rectangular cross section are applied to increase the heat transfer rate to the surroundings. Consider five such fins, which are equally spaced and have a thickness of  $t = 6 \text{ mm}$  and a length of  $L = 20 \text{ mm}$ . Because the cylinder diameter is relatively large compared to the length of the fins, the fins may be supposed to be straight with an equivalent width equal to the perimeter of the cylinder.

- Calculate the efficiency of the rectangular fins. ( $\eta_e = 0.8$ )
- Calculate the convection heat transfer rate using fins. ( $q_{fins} = 500 \text{ W}$ )
- What is the increase in heat transfer rate by using fins?
- Is a value of  $50 \text{ W/m}^2.\text{K}$  for the convection heat transfer coefficient realistic if assumed that the cylinder is freely exposed to the surroundings at a cruising speed of  $100 \text{ km/h}$ .



**Question 3** (all sub-questions can be solved independently)

To increase the contribution of green energy an electricity company considers the construction of a solar panel field in a dessert. A disadvantage of solar cells is that their efficiency is inversely proportional to their temperature. A part of the total incident solar energy is converted to electricity, a part is reflected and a part is absorbed as heat by the solar cells. The latter quantity amounts  $q''_{\text{zon}} = 500 \text{ W/m}^2$ .

The solar panels have dimensions of  $1.0\text{m} \times 0.5\text{m} \times 0.01\text{m}$  (Length  $\times$  Width  $\times$  Thickness). It can be assumed that the solar cells are made of pure silicon (high heat conduction coefficient) and that the rear side of the panels is perfectly insulated. The properties of air can be determined at a temperature of 350 K.

- a) On a windless, sunny day ( $v_{\text{air}} = 0 \text{ m/s}$ ) the air temperature equals  $T_{\text{air}} = 32^\circ\text{C}$ . Assume that heat transfer is only taking place by natural convection to the environment and that the solar panels are positioned perfectly horizontal.

What is the mean surface temperature in steady state?

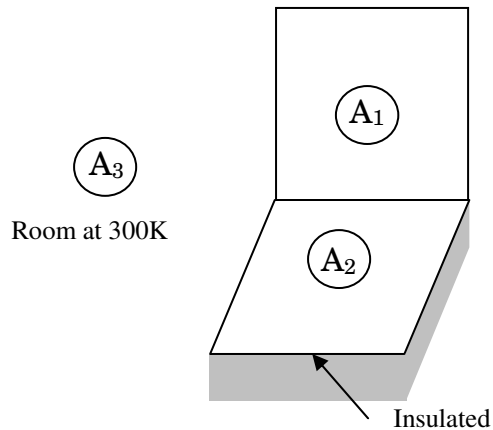
- b) At a certain moment wind starts blowing at a speed of  $v_{\text{air}} = 8 \text{ m/s}$  in the width direction of the solar panels ( $B = 0.5 \text{ m}$ ). From now on natural convection can be disregarded.

How thick are the hydrodynamic ( $\delta$ ) and thermal ( $\delta_t$ ) boundary layers at the end of the panel?

- c) What is the maximum surface temperature for the forced convection case? Assume that there is no conduction heat transfer in the panel due to temperature differences.
- d) Does it matter for the mean heat transfer coefficient  $\bar{h}_L$  if the solar panels are positioned in length ( $L = 1.0 \text{ m}$ ) or width direction ( $B = 0.5 \text{ m}$ ) with respect to the wind direction? Substantiate your answer.

**Question 4** (the sub-questions a), b) and d) can be solved independently)

Two flat plates are placed perpendicularly with one common edge, see figure. Surface 1 is at a temperature of  $T_1 = 1000$  K and has an emissivity of  $\epsilon_1 = 0.6$ . Surface 2 is insulated at its bottom and is in thermal equilibrium with surface  $A_1$  and with a large surrounding room at temperature  $T_3 = 300$  K. Both surfaces have dimensions  $50 \times 50$  cm.



- Calculate the radiation view factors  $F_{12}$ ,  $F_{13}$ ,  $F_{21}$  and  $F_{23}$ .  
(If you don't succeed then estimate the values and use those further on)
- Consider the enclosure consisting of the surfaces  $A_1$ ,  $A_2$  and  $A_3$  and sketch the electrical analogy for this enclosure indicating all resistances non-equal to zero. Try to simplify the system as much as possible.
- Determine the heat lost by surface  $A_1$ . ( $q_1 = 10$  kW)
- Determine the temperature of surface  $A_2$ .