

Q1)

i. Conversion of $A + ((B - C * D) / E) + F - G / H$ to postfix.

Next Token	Effect on Stack	Effect on Postfix
A		A
+	+	A
(+(A
(+((A
B	+((A B
-	+((-	A B
C	+((-	A B C
*	+((- *	A B C
D	+((- *	A B C D
)	+(A B C D * -
/	+(/	A B C D * -
E	+(/	A B C D * - E
)	+	A B C D * - E /
+	+	A B C D * - E / +
F	+	A B C D * - E / + F
-	-	A B C D * - E / + F +
G	-	A B C D * - E / + F + G
/	- /	A B C D * - E / + F + G
H	- /	A B C D * - E / + F + G H
End of Input	-	A B C D * - E / + F + G H /
End of Input and Stack		A B C D * - E / + F + G H / -

Conversion of $A + ((B - C * D) / E) + F - G / H$ to prefix.

To do this we need to convert this statement to reverse so we will get;

$H / G - F + (E / (D * C - B)) + A$

Next Token	Effect on Stack	Effect on Prefix
H		H
/	/	H
G	/	H G
-	-	H G /
F	-	H G / F
+	+	H G / F -

(+(H G / F -
E	+(H G / F - E
/	+(/	H G / F - E
(+(/(H G / F - E
D	+(/(H G / F - E D
*	+(/(*	H G / F - E D
C	+(/(*	H G / F - E D C
-	+(/(-	H G / F - E D C *
B	+(/(-	H G / F - E D C * B
)	+(/	H G / F - E D C * B -
)	+	H G / F - E D C * B - /
+	+	H G / F - E D C * B - / +
A	+	H G / F - E D C * B - / + A
End of Input and Stack		H G / F - E D C * B - / + A +
Reverse Prefix		+ A + / - B * C D E - F / G H

Evaluating postfix expression **A B C D * - E / + F + G H / -**

Expression	Action	Stack
A B C D * - E / + F + G H / -	Push A,B,C,D	A, B, C, D
* - E / + F + G H / -	Pop C, D evaluate C*D push C*D	A, B, (C*D)
- E / + F + G H / -	Pop C*D, B evaluate B - C*D push B - C*D	A, (B - C*D)
E / + F + G H / -	Push E	A, (B - C*D), E
/ + F + G H / -	Pop (B - C*D), E evaluate (B - C*D)/E push (B - C*D) /E	A, (B - C*D)/E
+ F + G H / -	Pop A, (B - C*D)/E evaluate A + (B - C*D)/E push A + (B - C*D) /E	A + (B - C*D) /E
F + G H / -	Push F	A + (B - C*D) /E, F
+ G H / -	Pop (B - C*D)/E + A, F evaluate (B - C*D)/E + A + F push A + (B - C*D) /E + F	A + (B - C*D) /E + F

G H / -	Push G H	$A + (B - C * D) / E + F, G, H$
/ -	Pop G,H evaluate G/H Push G/H	$A + (B - C * D) / E + F, G/H$
-	Pop $A + (B - C * D) / E + F$ and G/H evaluate $A + (B - C * D) / E + F - G/H$ push $A + (B - C * D) / E + F - G/H$	$A + (B - C * D) / E + F - (G/H)$

Evaluating postfix expression **A B C D * - E / + F + G H / -** with numbers

A = 7, B =14 , C = 4, D=1, E =5, F =3 , G=8 , H=2

Result of infix: $7 + ((14 - 4 * 1) / 5) + 3 - 8 / 2 = 7 + 2 + 3 - 4 = 8$

Expression	Action	Stack
7 14 4 1 * - 5 / + 3 + 8 2 / -	Push 7,14,4,1	7, 14, 4, 1
* - 5 / + 3 + 8 2 / -	Pop 4, 1 Evaluate 4*1 Push 4	7, 14, 4
- 5 / + 3 + 8 2 / -	Pop 14, 4 Evaluate 14-4 Push 10	7, 10
5 / + 3 + 8 2 / -	Push 5	7, 10, 5
/ + 3 + 8 2 / -	Pop 10, 5 Evaluate 10/5 Push 2	7, 2
+ 3 + 8 2 / -	Pop 7, 2 Evaluate 7+2 Push 9	9
3 + 8 2 / -	Push 3	9, 3
+ 8 2 / -	Pop 9, 3 Evaluate 9+3 Push 12	12
8 2 / -	Push 8, 2	12, 8, 2

/ -	Pop 8,2 Evaluate 8/2 Push 4	12, 4
-	Pop 12, 4 Evaluate 12-4 Push 8	8

ii. Conversion of $!(A \&\& !((B < C) || (C > D))) || (C < E)$ to postfix.

Next Token	Effect on Stack	Effect on Postfix
!	!	
(!(
A	!(A
&&	!(&&	A
!	!(&&!	A
(!(&&!(A
(!(&&!((A
B	!(&&!((A B
<	!(&&!(<	A B
C	!(&&!(<	A B C
)	!(&&!(A B C <
	!(&&!(A B C <
(!(&&!((A B C <
C	!(&&!((A B C < C
>	!(&&!((>	A B C < C
D	!(&&!((>	A B C < C D
)	!(&&!(A B C < C D >
)	!(&&!	A B C < C D >
)	!	A B C < C D > ! &&
		A B C < C D > ! && !
((A B C < C D > ! && !
C	(A B C < C D > ! && ! C
<	(<	A B C < C D > ! && ! C
E	(<	A B C < C D > ! && ! C E
)		A B C < C D > ! && ! C E <
End of Input		A B C < C D > ! && ! C E <
End of Input and Stack		A B C < C D > ! && ! C E <

Conversion of $!(A \&\& !((B < C) || (C > D))) || (C < E)$ to prefix.

To do this we need to convert this statement to reverse so we will get;

$(E < C) || (((D > C) || (C < B))! \&\& A)!$

Next Token	Effect on Stack	Effect on Postfix
((
E	(E
<	(<	E
C	(<	E C
)		E C <
		E C <
((E C <
((E C <
((E C <
D	(E C < D
>	(E C < D
C	(E C < D C
)		E C < D C >
		E C < D C >
((E C < D C >
C	(E C < D C > C
<	(E C < D C > C
B	(E C < D C > C B
)		E C < D C > C B <
)		E C < D C > C B <
!	!	E C < D C > C B <
&&	&&	E C < D C > C B < !
A	&&	E C < D C > C B < ! A
)		E C < D C > C B < ! A &&
!	!	E C < D C > C B < ! A &&
End of Input		E C < D C > C B < ! A && !
End of Input and Stack		E C < D C > C B < ! A && !
Reverse of the statement		! && A ! < B C > C D < C E

Evaluating postfix expression **A B C < C D > || ! && ! C E < ||**

Expression	Action	Stack
A B C < C D > ! && ! C E <	Push A,B,C	A B C
< C D > ! && ! C E <	Pop B, C evaluate B < C push B < C	A B < C
C D > ! && ! C E <	Push C, D	A B < C C D
> ! && ! C E < 	Pop C, D evaluate C > D push C > D	A B < C C > D
! && ! C E <	Pop B < C, C > D evaluate B < C C > D push B < C C > D	A B < C C > D
! && ! C E <	Pop B < C C > D evaluate !(B < C C > D) push !(B < C C > D)	A !(B < C C > D)
&& ! C E <	Pop A, !(B < C C > D) evaluate A && !(B < C C > D) push A && !(B < C C > D)	A && !(B < C C > D)
! C E <	Pop A && !(B < C C > D) evaluate !(A && !(B < C C > D)) push !(A && !(B < C C > D))	!(A && !(B < C C > D))
C E <	Push C, E	!(A && !(B < C C > D)) C E
<	Pop C E evaluate C < E push C < E	!(A && !(B < C C > D)) C < E
	Pop !(A && !(B < C C > D)), C < E evaluate !(A && !(B < C C > D)) C < E push !(A && !(B < C C > D)) C < E	!(A && !(B < C C > D)) C < E

Evaluating postfix expression **A B C < C D > || ! && ! C E < ||** with numbers

A = 7, B =2 , C = 3, D=4, E =5

Result of infix: $!(7 \&\& !((2 < 3) || (3 > 4))) || (3 < 5)$

$= !(7 \&\& 0) || 0 = !0 || 0 = 1 || 0 = 1$

Expression	Action	Stack
7 2 3 < 3 4 > ! && ! 3 5 <	Push 7,2,3	7 2 3
< 3 4 > ! && ! 3 5 <	Pop 2, 3 Evaluate 2 < 3 Push 0	7 0
3 4 > ! && ! 3 5 <	Push 3, 4	7 0 3 4
> ! && ! 3 5 < 	Pop 3, 4 Evaluate 3 > 4 Push 0	7 0 0
! && ! 3 5 <	Pop 0, 0 Evaluate 0 0 Push 0	7 0
! && ! 3 5 <	Pop 0 Evaluate !0 Push 1	7 1
&& ! 3 5 <	Pop 7, 1 Evaluate 7 && 1 Push 7	7
! 3 5 <	Pop 7 Evaluate !7 Push !7	!7
3 5 <	Push 3, 5	!7 3 5
<	Pop 3 5 Evaluate 3 < 5 Push 1	!7 1
	Pop !7, 1 Evaluate !7 1 Push 1	1