BIOS 902: Bayesian Statistics Byron J. Gajewski KU Department of Biostatistics Due 9/18/2018

## Homework #2

1. Gelman et al.: Exercise 2.11

2.

An experiment was performed to estimate the effect of beta-blockers on mortality of cardiac patients. A group of patients were randomly assigned to treatment and control groups: out of 674 patients receiving the control, 39 died, and out of 680 receiving the treatment, 22 died. Assume that the outcomes are independent and binomially distributed, with probabilities of death of  $p_0$  and  $p_1$  under the control and treatment, respectively. Set up a noninformative or weakly informative prior distribution on  $(p_0, p_1)$ .

- a) Summarize the posterior distribution for the odds ratio,  $(p_1/(1-p_1))/(p_0/(1-p_0))$ .
- b) Discuss the sensitivity of your inference to your choice of prior density.

3. Consider a case where the same factory has two production lines for manufacturing car wind-shields. Independent samples from the two production lines were tested for hardness. The hardness measurements for the two samples y<sub>1</sub> and y<sub>2</sub> are given in the files windshieldy1.txt and windshieldy2.txt.

We assume that the samples have unknown standard deviations  $\sigma_1$  and  $\sigma_2$ . Use uninformative or weakly informative priors and answer the following questions:

a) What can you say about  $\mu_d = \mu_1 - \mu_2$ ?. Summarize your results using Bayesian point and interval estimates.

windshieldy2

b) Are the means the same?

windshieldy1

Williabiliolay 1		
13.357	15.98	
14.928	14.206	
14.896	16.011	
15.297	17.25	
14.82	15.993	
12.067	15.722	
14.824	17.143	
13.865	15.23	
17.447	15.125	
	16.609	
	14.735	
	15.881	
	15.789	

4. Gelman et al.: Exercise 3.10